

Title: Entanglement and DMRG in the Generalised Landau Paradigm

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Collection/Series: Mathematical Physics

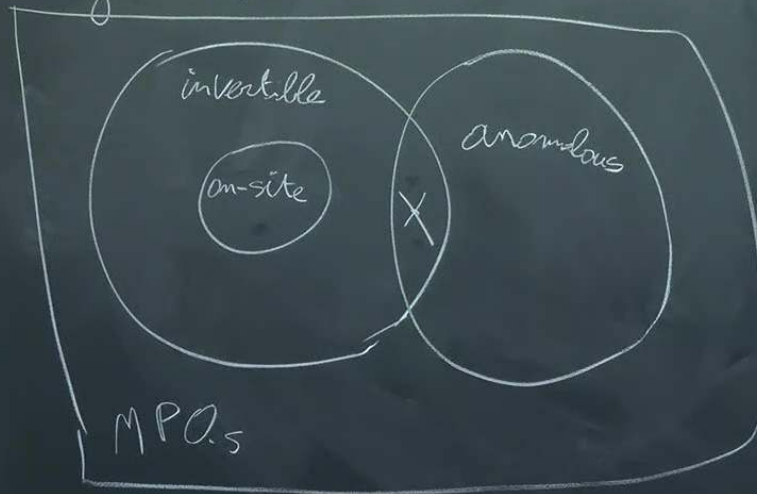
Subject: Mathematical physics

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URL: <https://pirsa.org/26020054>

MPO-symmetries

global symm. in 1+1D lattice models

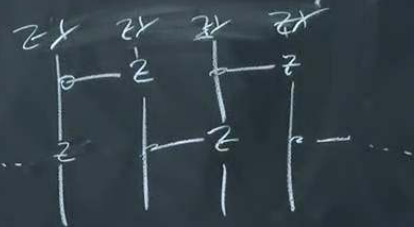


ce modelle

$$H = \sum_{i=1}^N X_i - z_{i-1} X_i z_{i+1}$$

$$U_{CZY} = \prod_{i=1}^N CZ_{i,i+1} \prod_{i=1}^N z_i X_i$$

$$CZ_{i,i+1} = \begin{pmatrix} 1 & & & \\ & 1 & & \\ & & 1 & \\ & & & 1 \end{pmatrix} = \begin{array}{c} \text{---} \\ | \\ \text{---} \\ | \\ \text{---} \\ | \\ \text{---} \\ | \\ \text{---} \end{array}$$

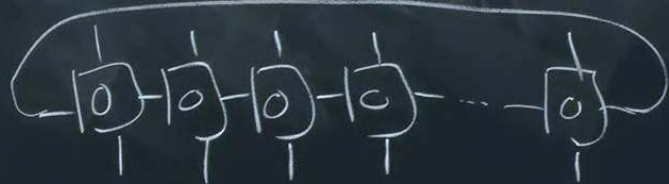


$$[U_{CZY}, H] = 0, U_{CZY}^2 = \mathbb{1}$$

U_{CZY} is an MPO

$$= \sum_{\{i\} \{j\}} \text{Tr}(O^{i_j} O^{j_k} \dots O^{i_{jN}}) |i_1 \dots i_N \rangle \langle j_1 \dots j_N|$$

$$O^{01} = \begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix}, O^{10} = \begin{pmatrix} 0 & 0 \\ 1 & -1 \end{pmatrix}$$



$$\left(\begin{array}{c} \circ \\ \circ \\ \dots \\ \circ \\ \square \end{array} \right) = O(B), [O(B), H] = 0$$

$$O(B_1)O(B_2) = \tilde{O}(B_3)$$

$$\tilde{O}^{200} = \begin{pmatrix} 0 & -1 & 1 \\ 0 & 1 & -1 \\ 0 & 0 & 0 \end{pmatrix}, \tilde{O}^{11} = \begin{pmatrix} 0 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 0 \end{pmatrix}$$

$$B_3 = \begin{pmatrix} 0 & 0 \\ a & b & 0 \\ c & d & 0 \end{pmatrix}$$

$$O_a(B_1)O_b(B_2) = O_{aob}(B_3)$$

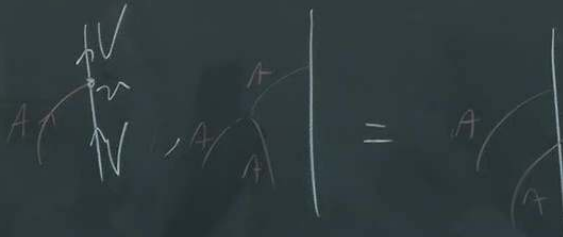
2) bialgebra

- $A, \mu: A \times A \rightarrow A$



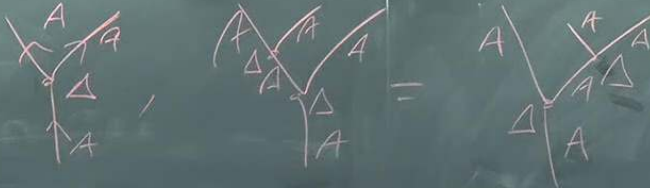
- modules over A:

$V \in \text{Mod}(A), \nu: A \times V \rightarrow V$



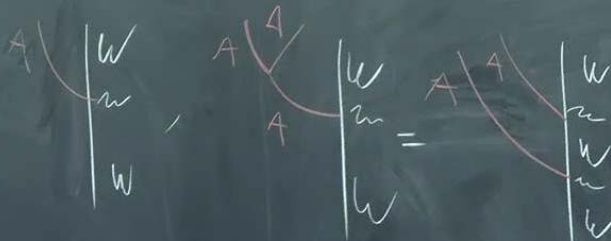
Coalgebra

$$\Delta: A \rightarrow A \times A$$



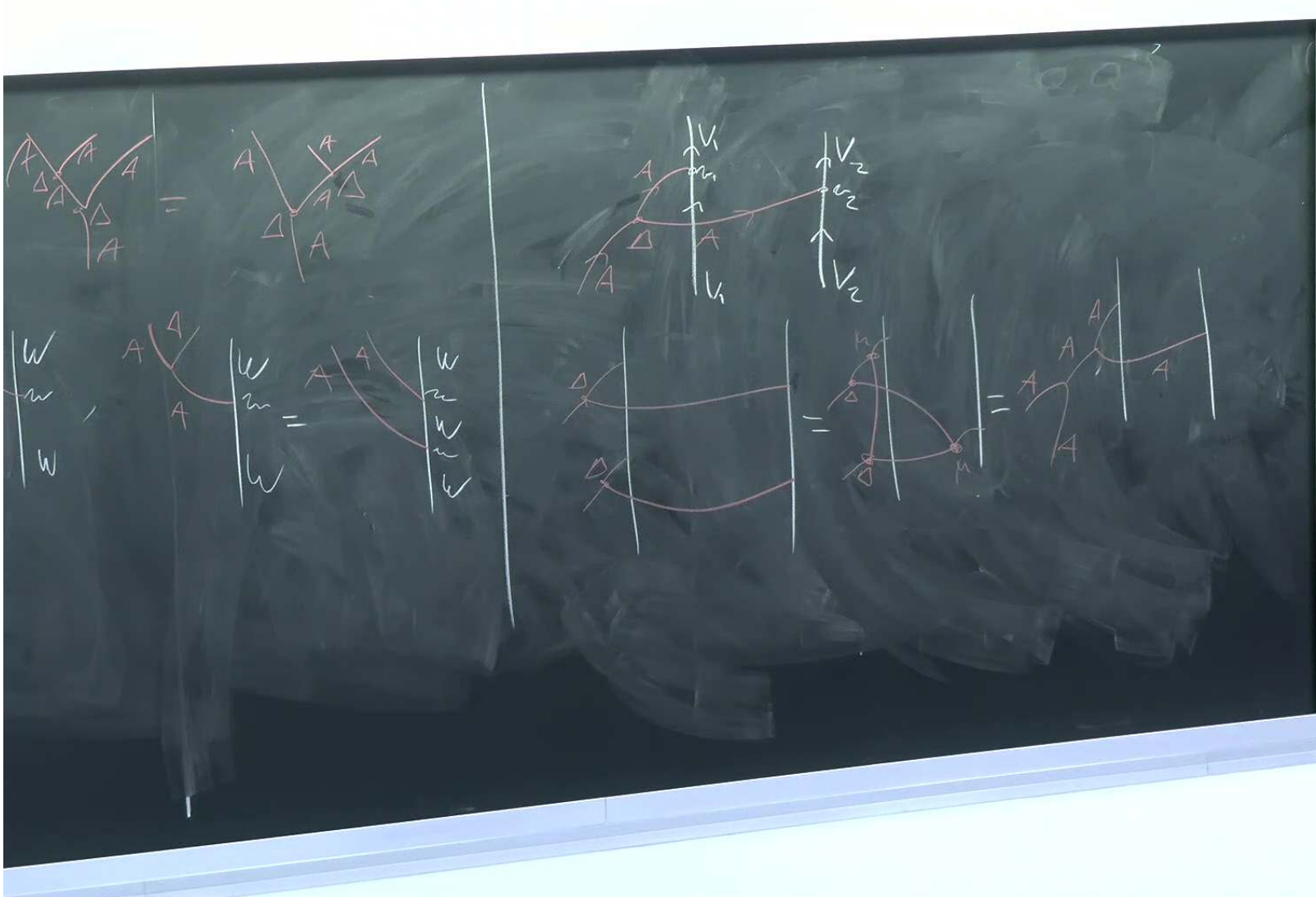
Comodule

$$W \in \text{Comod}(A), w: W \rightarrow A \times W$$



Bialgebra $\Delta(ab) = \Delta(a)\Delta(b)$





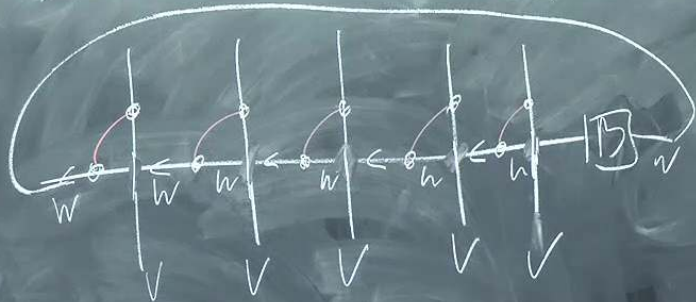
$$\begin{matrix} \circ & \circ & \dots & \circ & \square \\ | & | & & | & | \\ \circ & \circ & & \circ & \square \end{matrix}$$

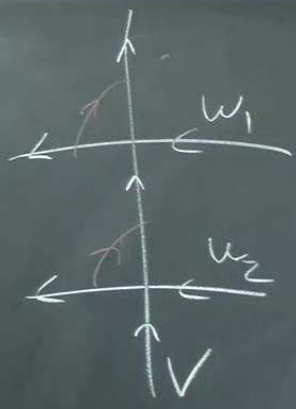
$$O(B_1)O(B_2) = \tilde{O}(B)$$

$$O = \begin{pmatrix} 0 & -1 & 1 \\ 0 & 1 & -1 \\ 0 & 0 & 0 \end{pmatrix}, \tilde{O} = \begin{pmatrix} 0 & & \\ 0 & & \\ 0 & & 0 \end{pmatrix}$$

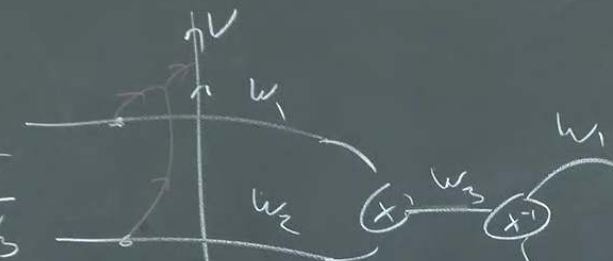
$$B_i = \begin{pmatrix} 0 & 0 \\ a & b \\ c & d \end{pmatrix}$$

$A, V \in \text{Mod}(A), W \in \text{Comod}(A), B \in \text{End}(W)$

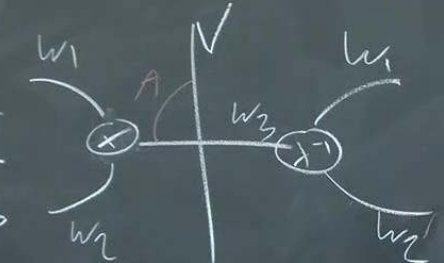




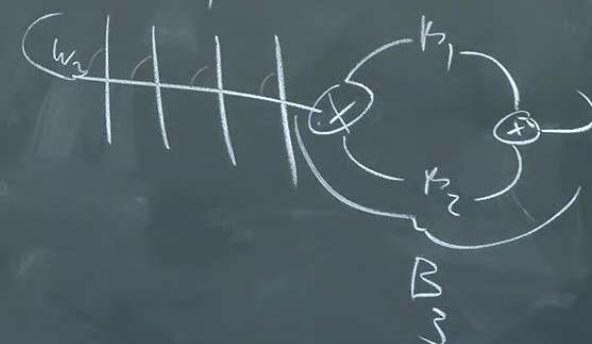
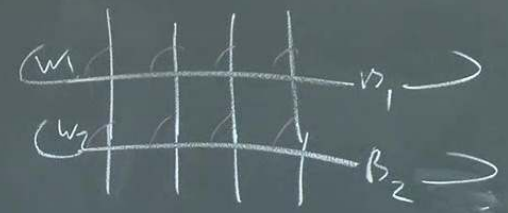
$$= \sum_{w_3}$$



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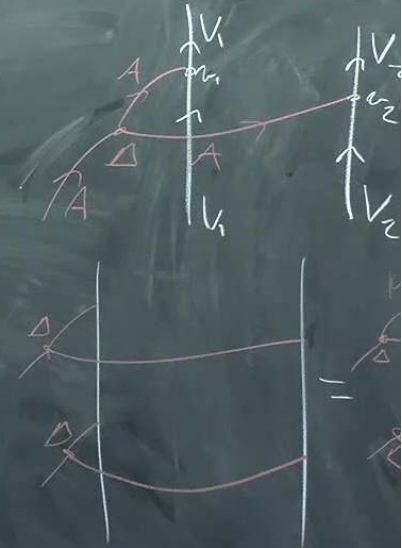
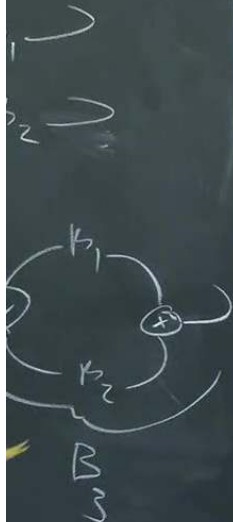
$$= \sum_{w_3} \sum_{w_2} \sum_{w_1}$$



CZY: $-A$ is \mathcal{B} -dim.

- $\text{mod}(A)$ is ss, pre-monomial cont
- $\text{comod}(A)$ is non-ss, monomial cont

Vec_2^w is semi-simpl. of $\text{comod}(A)$
 $w \in H^3(\mathbb{Z}_2, \mathbb{K}_1)$



-dim.

(\mathfrak{g} ss, pre-nilpotent cart

(\mathfrak{g} non ss, nilpotent cart

simpl. of \mathfrak{g} mod (A)

$$U(\mathfrak{sl}(2))$$

$$[E, F] = \dots$$

$$\Delta(x) = x \otimes 1 + 1 \otimes x$$

$$U_q(\mathfrak{sl}(2))$$

A,

