

**Title:** Berry-curvature physics of magnons and magnon-polarons

**Speakers:** Se Kwon Kim

**Collection/Series:** Quantum Matter

**Subject:** Condensed Matter

**Date:** April 15, 2025 - 3:30 PM

**URL:** <https://pirsa.org/25040111>

# Berry-curvature physics of magnons and magnon-polarons

Se Kwon Kim  
Department of Physics, KAIST

Perimeter Institute, April 2025

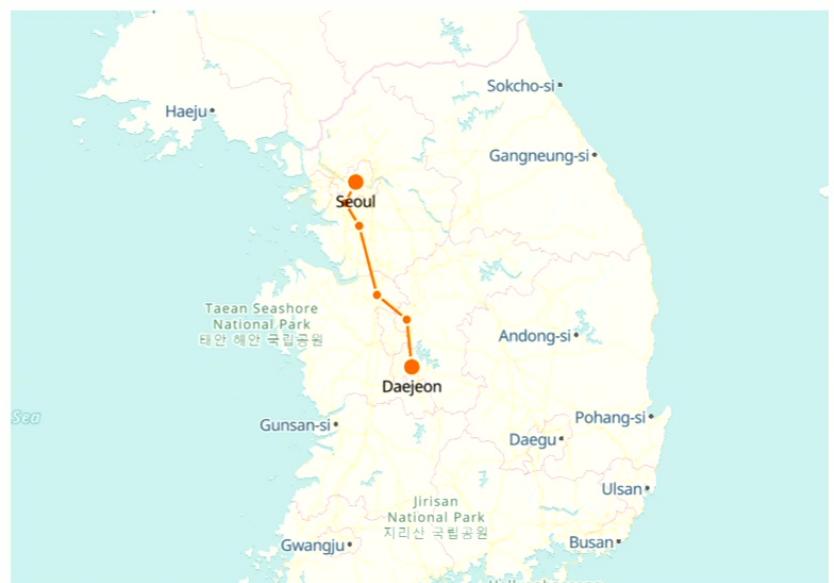


## KAIST the Future of Korea

KAIST is committed to resolving the challenges humanity faces by educating creative talents, staying ahead of new research topics, and producing entrepreneurs that will impact the global community.

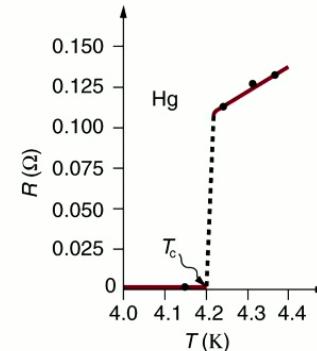
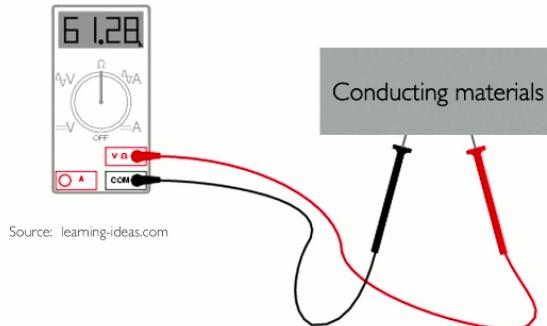
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# Charge transport measurement

Charge transport measurement has been a central probe of **conducting** materials.

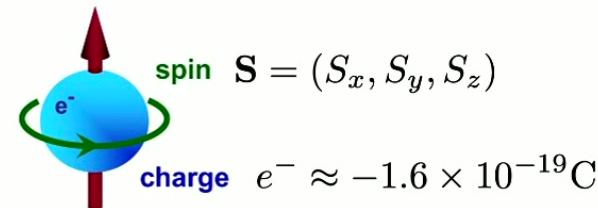


superconducting phase transition

However, it cannot be used for insulating materials, which are abundant in nature.

# Spintronics = Spin + electronics

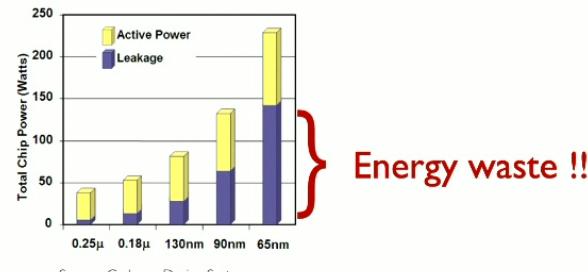
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**Spintronics vision:** computing based on **spin** in addition to charge of electrons



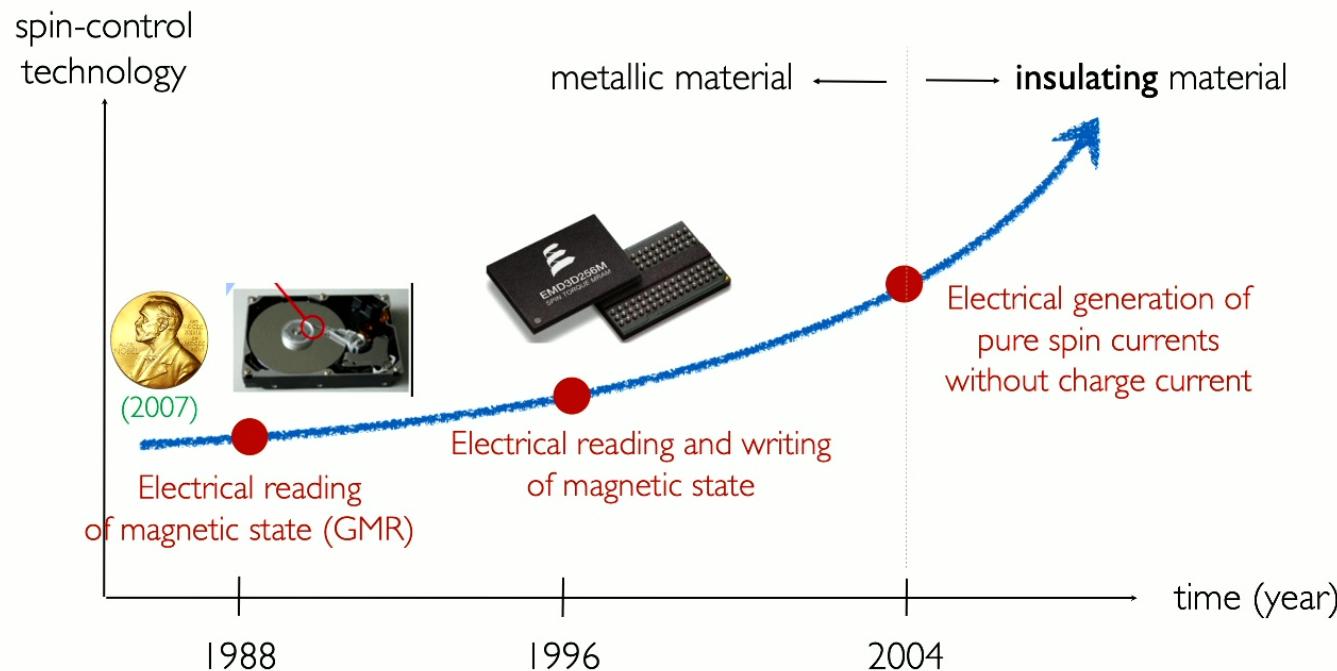
Credit: Gene Siegel, Shiang Teng



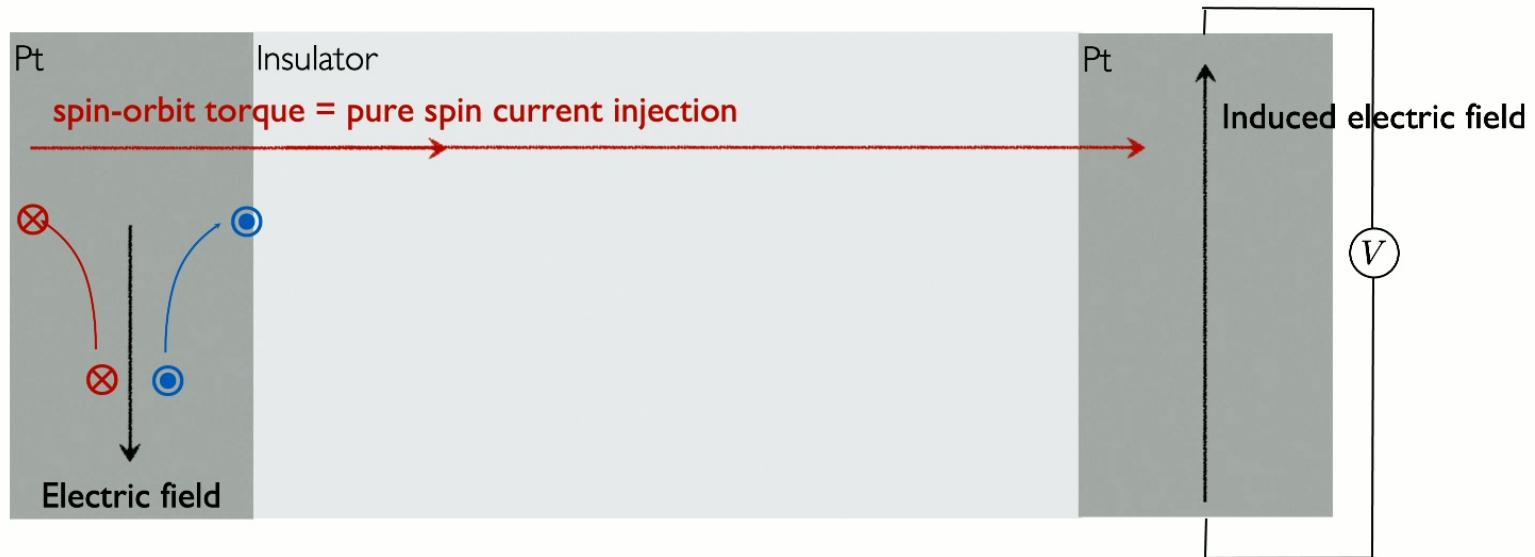
Challenge: **significant energy loss in conventional electronics**

# Spintronics = Spin + electronics

Our ability to control **spin** has been improved tremendously,  
driven by practical motivations to advance **spintronics**.



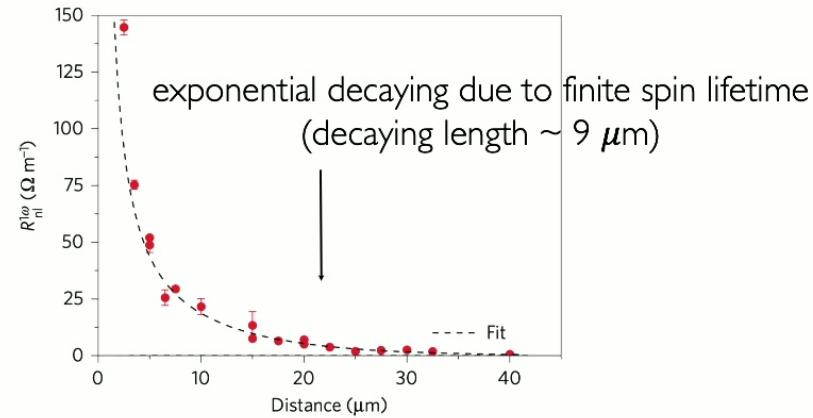
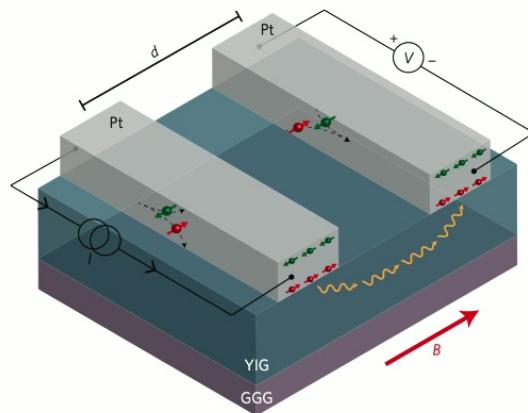
# Technology for pure spin-current manipulation



Generation: spin Hall effects

Detection: inverse spin Hall effects

# Spin transport in insulating ferromagnets



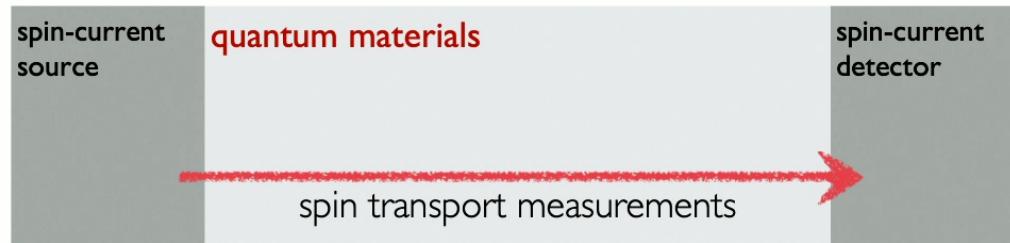
Exponential spin-current decaying in a magnetic insulator, yttrium-iron-garnet

Cornelissen, van Wees, et al, *Nat. Phys.* (2015)

**One of the clearest signatures of exponential decaying of diffusive spin currents !!**

# Spin transport through quantum materials

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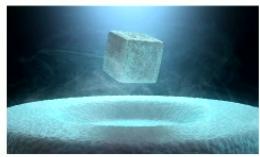
Novel spin transport in quantum materials ??

New spin physics from Berry curvatures ??

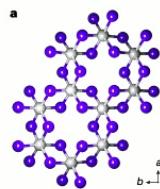
# Quantum materials

Quantum materials are material systems  
where quantum effects remain manifest over a wider range of energy and length scales.

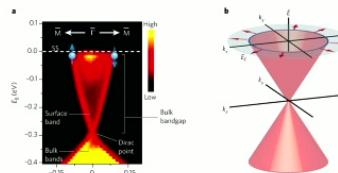
Keimer and Moore, *Nat. Phys.* (2017)



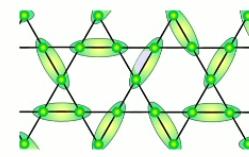
Superconductors



2D materials/magnets

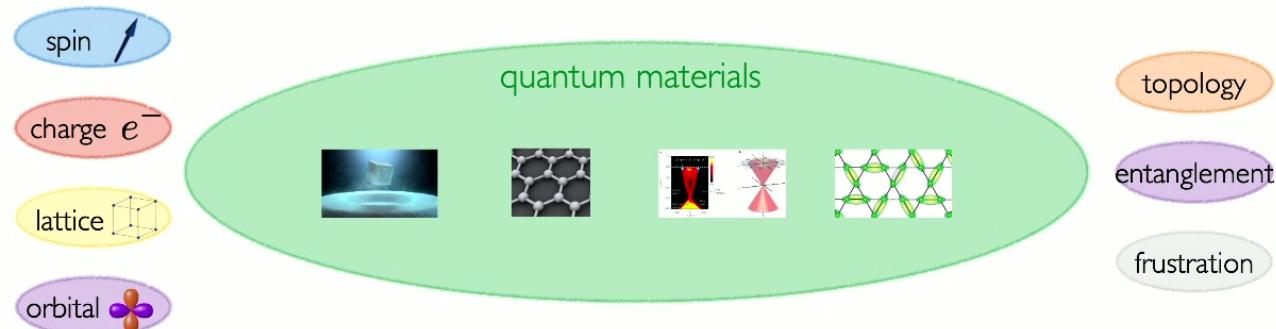
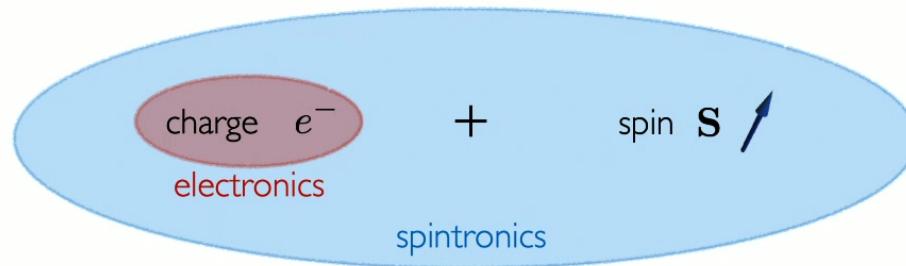


Topological insulators



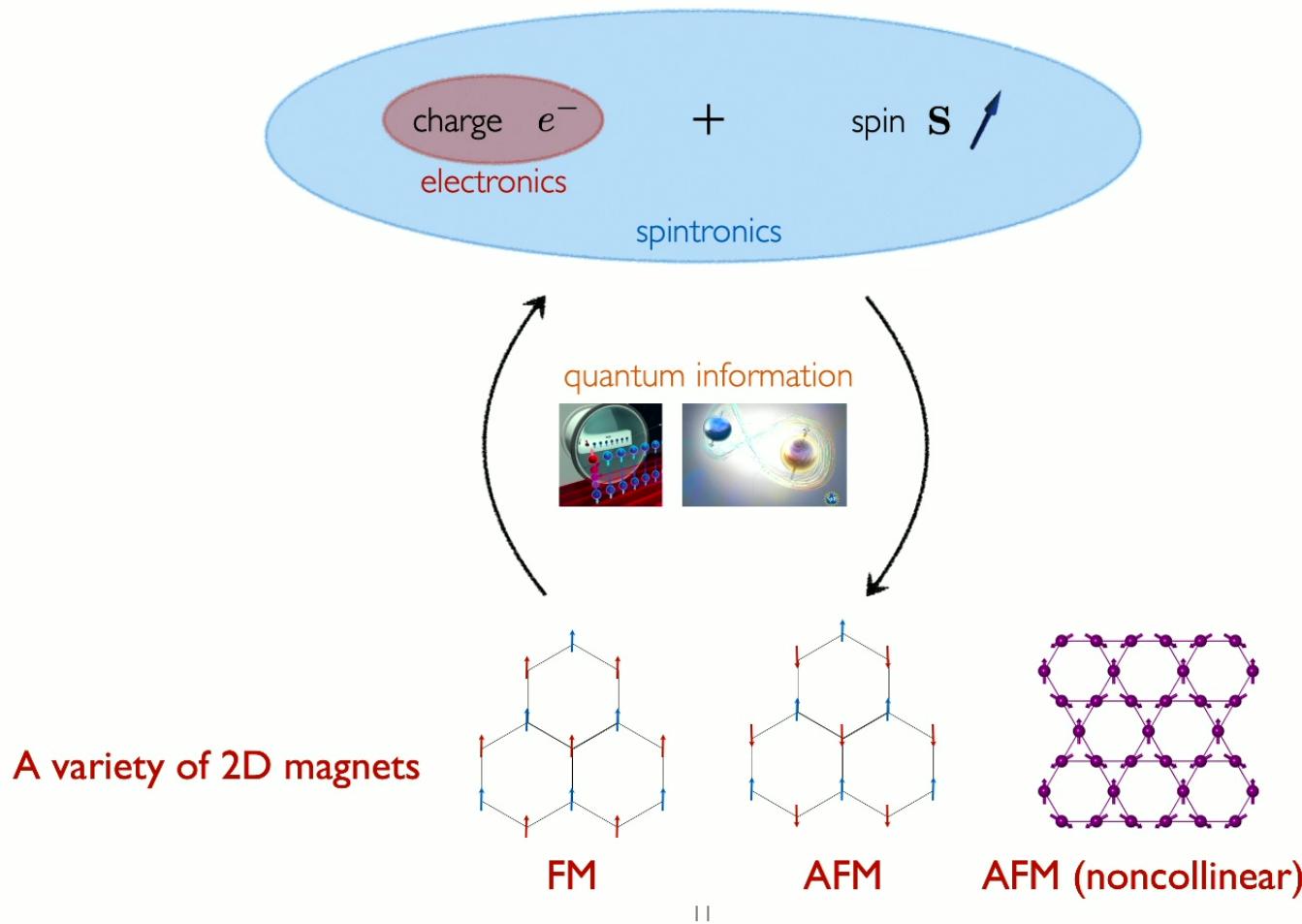
Quantum spin liquids

# Quantum spintronics



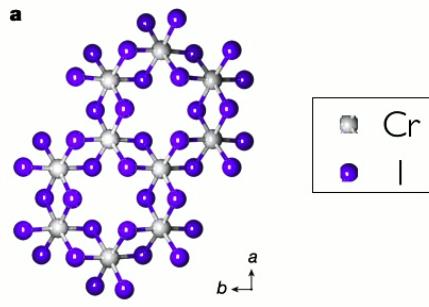
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# Quantum spintronics



# Discovery of monolayer ferromagnetism, CrI<sub>3</sub>

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LETTER

doi:10.1038/nature22391

## Layer-dependent ferromagnetism in a van der Waals crystal down to the monolayer limit

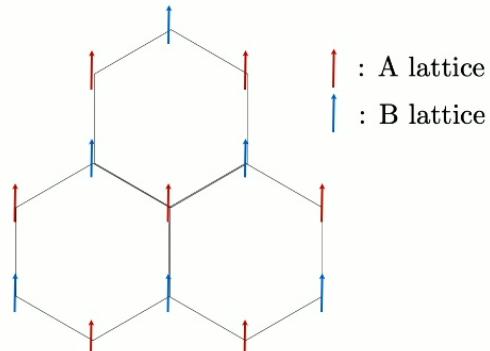
Bevin Huang<sup>1\*</sup>, Genevieve Clark<sup>2,\*</sup>, Efrén Navarro-Moratalla<sup>3,\*</sup>, Dahlia R. Klein<sup>1</sup>, Ran Cheng<sup>4</sup>, Kyle L. Seyler<sup>1</sup>, Ding Zhong<sup>1</sup>, Emma Schmidgall<sup>1</sup>, Michael A. McGuire<sup>5</sup>, David H. Cobden<sup>1</sup>, Wang Yao<sup>6</sup>, Di Xiao<sup>6</sup>, Pablo Jarillo-Herrero<sup>3</sup> & Xiaodong Xu<sup>1,2</sup>

Huang, Xu, et al., *Nature* (2017)

The first material realization of *monolayer 2D ferromagnets !!*

## 2D honeycomb ferromagnet

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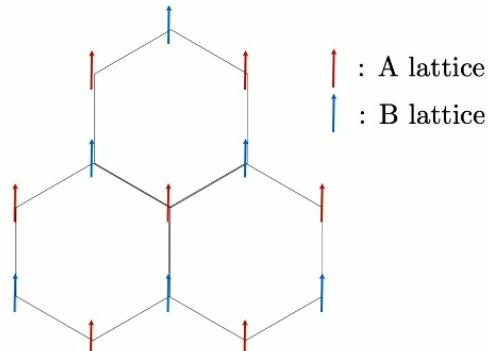
SKK, Ochoa, Zarzuela, and Tserkovnyak, *PRL* 117, 227201 (2016)

$$H = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + D \sum_{\langle\langle i,j \rangle\rangle} \nu_{ij} \hat{\mathbf{z}} \cdot \mathbf{S}_i \times \mathbf{S}_j - B \sum_i S_i^z$$

ferromagnetic exchange      spin-orbit coupling  
[Dzyaloshinskii-Moriya (DM) interaction]

## 2D honeycomb ferromagnet

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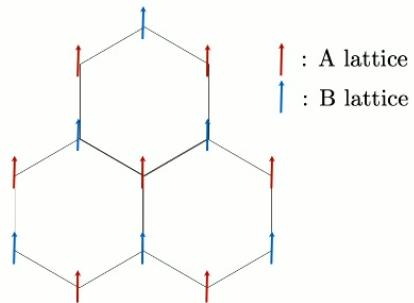
SKK, Ochoa, Zarzuela, and Tserkovnyak, *PRL* 117, 227201 (2016)

$$H = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + D \sum_{\langle\langle i,j \rangle\rangle} \nu_{ij} \hat{\mathbf{z}} \cdot \mathbf{S}_i \times \mathbf{S}_j - B \sum_i S_i^z$$

ferromagnetic exchange      spin-orbit coupling      Zeeman coupling  
[Dzyaloshinskii-Moriya (DM) interaction]

# Magnon Hamiltonian

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$$H = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + D \sum_{\langle\langle i,j \rangle\rangle} \nu_{ij} \hat{\mathbf{z}} \cdot \mathbf{S}_i \times \mathbf{S}_j - B \sum_i S_i^z$$

Holstein-Primakoff transformation

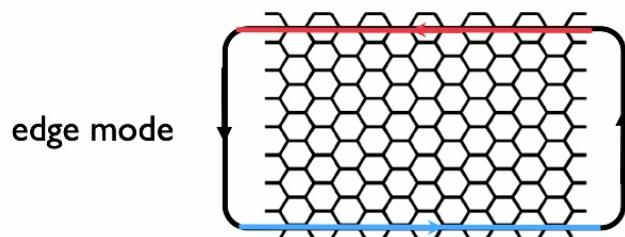
$$H_m = (3JS + B) \sum_i d_i^\dagger d_i \quad \xleftarrow{\text{on-site term}}$$

$$- JS \sum_{\langle i,j \rangle} (d_i^\dagger d_j + \text{H.c.}) \quad \xleftarrow{\text{hopping term}} \quad (\text{exchange energy})$$

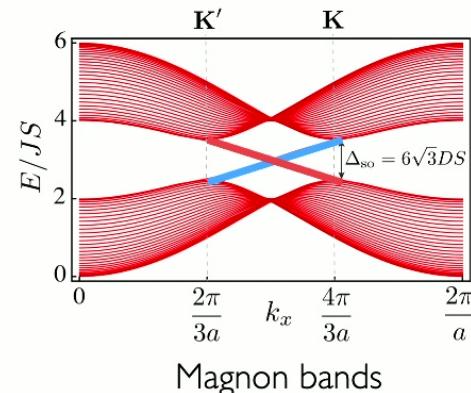
$$- DS \sum_{\langle\langle i,j \rangle\rangle} (i\nu_{ij} d_i^\dagger d_j + \text{H.c.}) \quad \xleftarrow{\text{hopping term}} \quad (\text{spin-orbit coupling})$$

Haldane's mass term for electrons in a honeycomb lattice [Haldane, PRL (1988)]

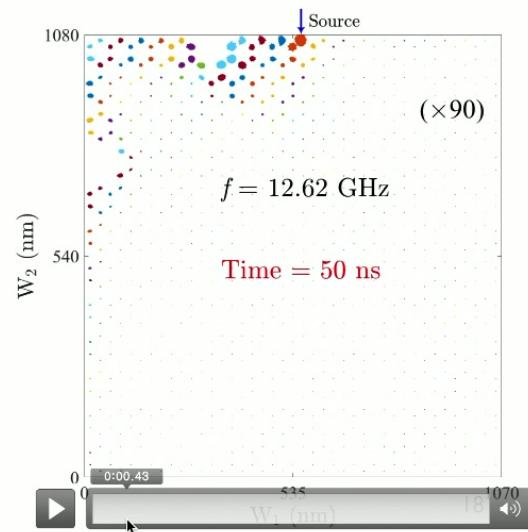
# Magnon bands with edge modes



Finite sample



Magnon bands

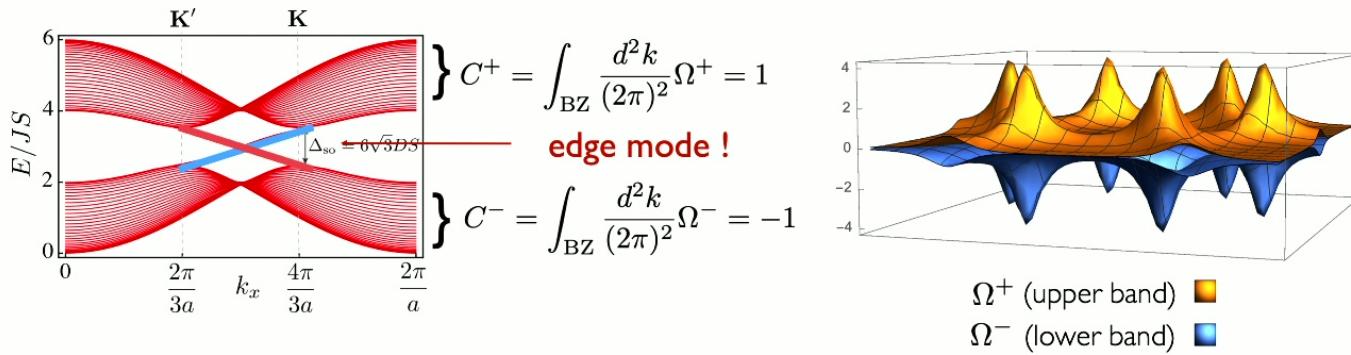


Numerical simulation:

1. Localized along the edge
2. Fixed chirality
3. Backward scattering free

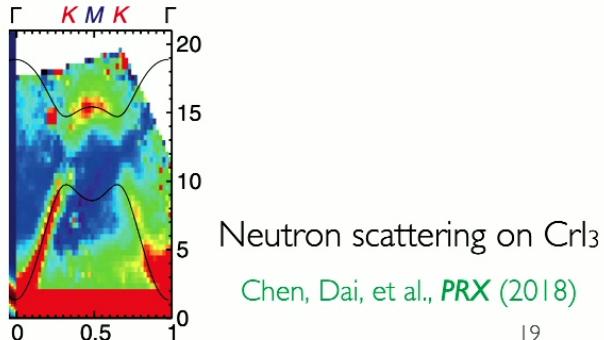
Li, Yan, et al., PRB (2018)

# Magnonic topological insulator



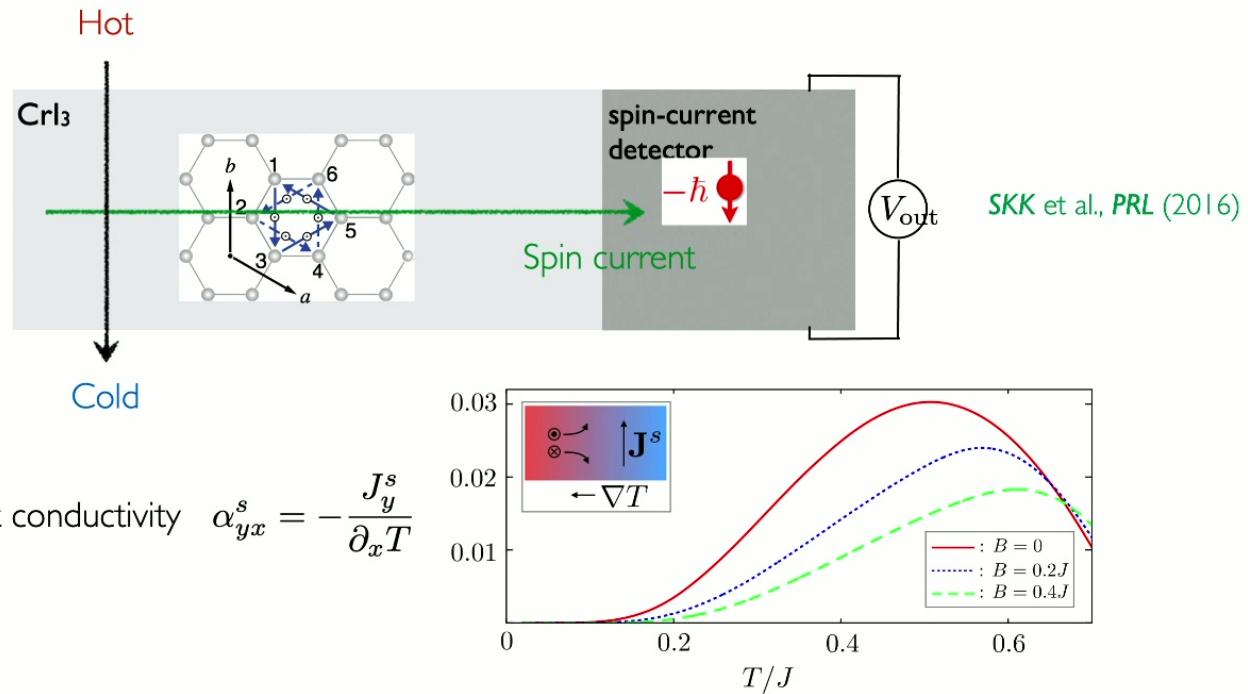
Berry curvature:  $\Omega_n(\mathbf{q}) = \nabla_{\mathbf{q}} \times \langle u_n(\mathbf{q}) | i \nabla_{\mathbf{q}} | u_n(\mathbf{q}) \rangle$ . SKK et al., PRL (2016); Owerre JPCM (2016)

**Magnonic topological insulator !!** : analogous to Haldane's topological (Chern) insulator

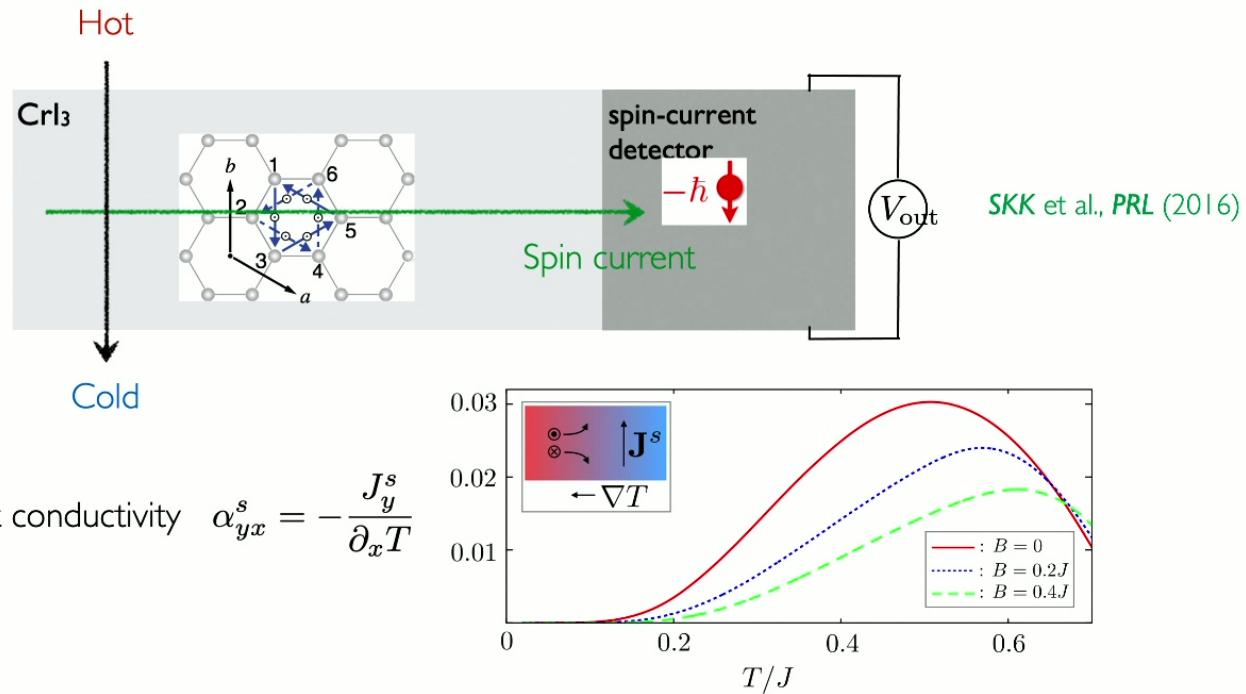


Haldane, PRL (1988) (2016)

# Spin transport of magnonic topological insulators



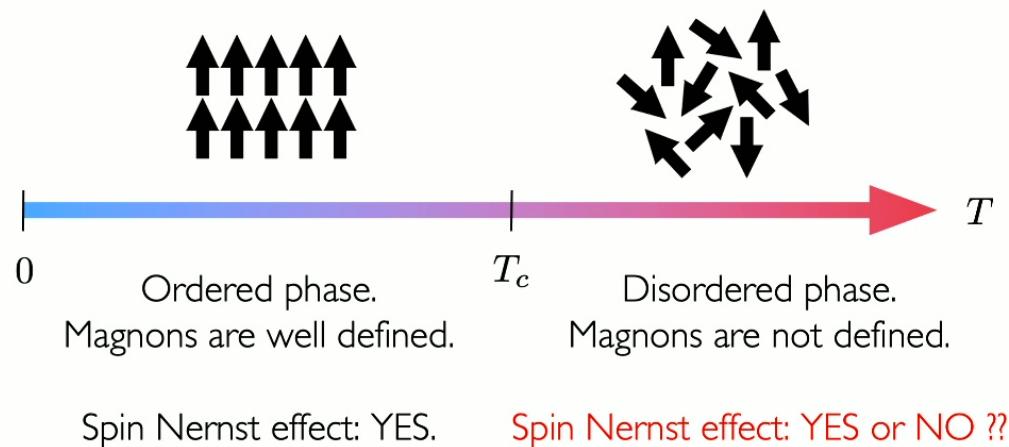
# Spin transport of magnonic topological insulators



The magnon picture for the spin Nernst effect is valid only for low temperatures, i.e., ordered phases.

## How about above the Curie temperature ?

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\* the figure is taken from [https://en.wikipedia.org/wiki/Curie\\_temperature](https://en.wikipedia.org/wiki/Curie_temperature).

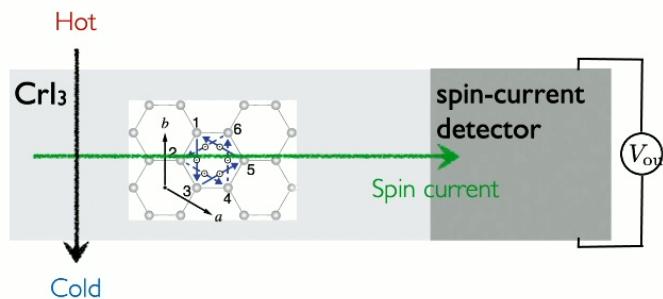
# Spin Nernst effect in a disordered phase?

A spin current is even under time reversal.

$$J_i^\alpha = v_i s^\alpha \xrightarrow{\text{time reversal}} J_i^\alpha = (-v_i)(-s^\alpha) = v_i s^\alpha$$

velocity      spin

This indicates that the spin current does not need breaking of time-reversal symmetry, and therefore, the spin Nernst effect may exist even when there is no magnetic ordering.



Does the spin Nernst effect exist even above the Curie temperature?

# Schwinger spinons

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$$S^+ = c_{\uparrow}^\dagger c_{\downarrow}$$
$$S^- = c_{\downarrow}^\dagger c_{\uparrow}$$
$$S^z = (c_{\uparrow}^\dagger c_{\uparrow} - c_{\downarrow}^\dagger c_{\downarrow})/2$$

spin-up spinon                      spin-up spinon

with the local number constraint

$$\sum_s c_{i,s}^\dagger c_{i,s} = 2S$$

Arovas and Auerbach, *PRB* (1988)  
Auerbach and Arovas, *PRL* (1988)

The **Schwinger spinon representation does not need information about a ground state.**

# Spinon Hamiltonian

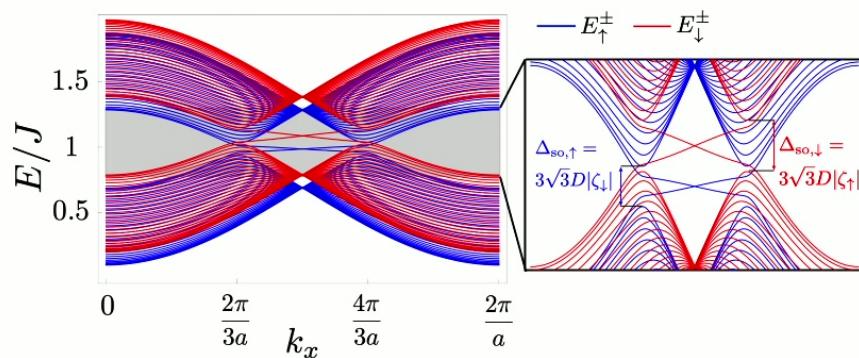
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$$H = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + D \sum_{\langle\langle i,j \rangle\rangle} \nu_{ij} \hat{\mathbf{z}} \cdot \mathbf{S}_i \times \mathbf{S}_j - B \sum_i S_i^z$$

↓  
Schwinger representation & mean-field approach

$$\begin{aligned} H_s = & -\eta J \sum_{\langle i,j \rangle, s} \left[ c_{i,s}^\dagger c_{j,s} + \text{h.c.} \right] \\ & + \frac{D}{2} \sum_{\langle\langle i,j \rangle\rangle, s} \left[ i\nu_{ij} s \zeta_{-s} c_{i,s}^\dagger c_{j,s} + \text{h.c.} \right] \\ & + \frac{D}{2} \sum_{\langle\langle i,j \rangle\rangle, s} \left[ s \xi_{-s} c_{i,s}^\dagger c_{j,s} + \text{h.c.} \right] \\ & + \sum_{i,s} \left( \lambda - s \frac{B}{2} \right) c_{i,s}^\dagger c_{i,s} . \end{aligned}$$

# Topological spinon bands

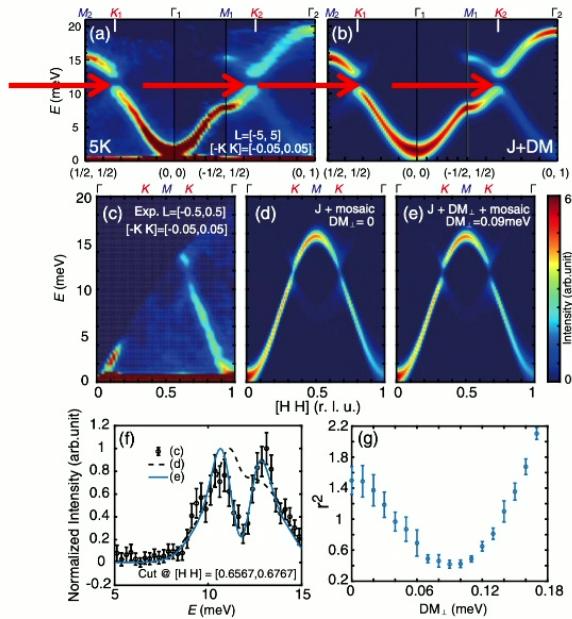


Both spin-up and spin-down spinons have the topological bands !!!

The spin Nernst effect should exist even above the Curie temperature !!!,  
albeit decreasing with increasing temperature.

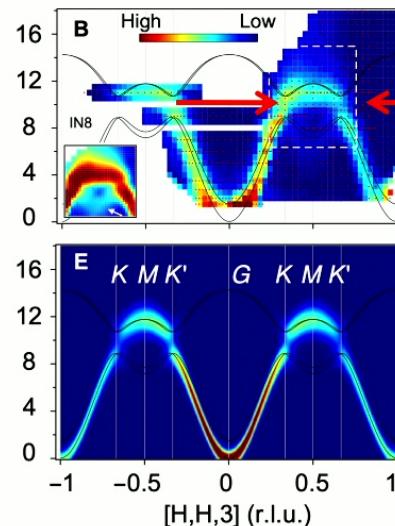
SKK, Ochoa, Zarzuela, and Tserkovnyak, PRL 117, 227201 (2016)

# Experimental status of searching for topological magnons



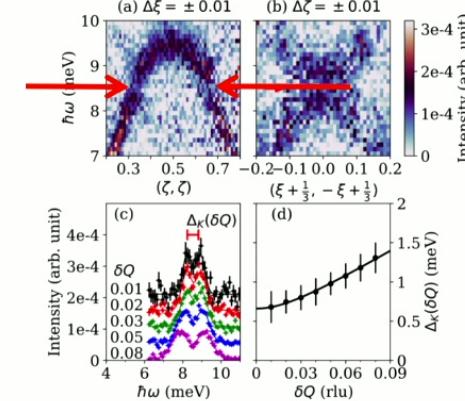
Neutron scattering on CrI<sub>3</sub>

Chen, Dai, et al., *PRX* (2021)



Neutron scattering on CrSiTe<sub>3</sub>

Zhu, Bruckel et al., *Sci. Adv.* (2022)

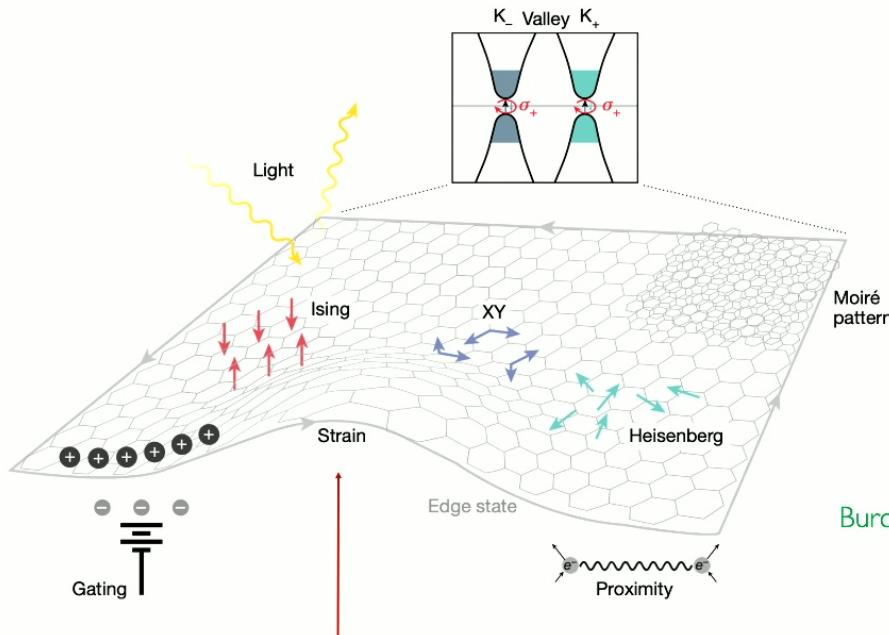


Neutron scattering on CoTiO<sub>3</sub>

Yuan, Kim et al., *PRB* (2024)

**Neutron scattering experiments demonstrate finite gaps at K points,  
but there is no experimental proof showing that the gaps are topological.**

# Phonons are important in 2D materials.

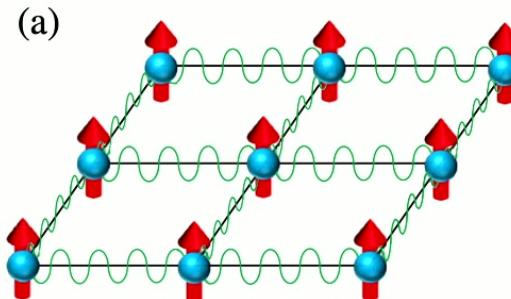


Burch, Mandrus, and Park., *Nature* (2018)

2D materials including 2D magnets are easy to bend, which indicates the importance of lattice vibrations, i.e., phonons, in their properties.

# Magnon-phonon hybridized mode = magnon-polaron

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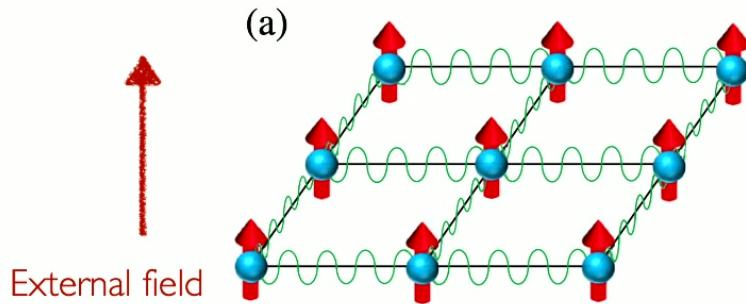
Go, SKK, and Lee., *PRL* (2020)

The number of magnon bands is one, thus topologically trivial.

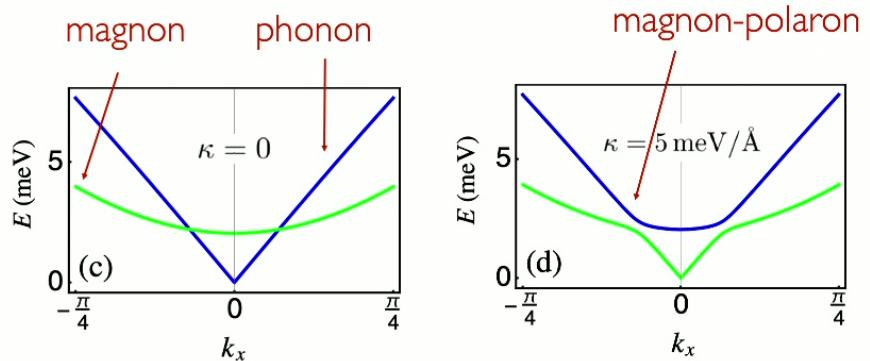
Phonons are also topologically trivial.

Can magnon-polarons be topological ??

# Topological magnon-polarons



Go, SKK, and Lee., *PRL* (2020)

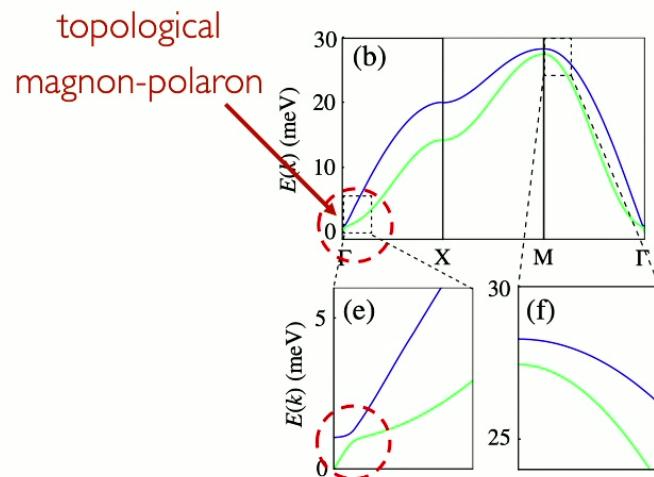


Magnetic sector:  $H_{\text{mag}} = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j - \frac{K_z}{2} \sum_i S_{i,z}^2 - \mathcal{B} \sum_i S_{i,z},$

Lattice sector:  $H_{\text{ph}} = \sum_i \frac{\mathbf{p}_i^2}{2M} + \frac{1}{2} \sum_{i,j,\alpha,\beta} u_i^\alpha \Phi_{i,j}^{\alpha,\beta} u_j^\beta,$

Magnetoelastic coupling:  $H_{\text{mp}} = \kappa \sum_i \sum_{\mathbf{e}} (\mathbf{S}_i \cdot \mathbf{e})(u_i^z - u_{i+\mathbf{e}}^z),$  (first discussed by Kittel in 1958)  
 continuum  $\downarrow$   
 $H_{\text{mp}} \propto (\mathbf{S} \cdot \nabla u^z - u_z \nabla \cdot \mathbf{S})$   
 C. Kittel, *Phys. Rev.* 110, 836 (1958).

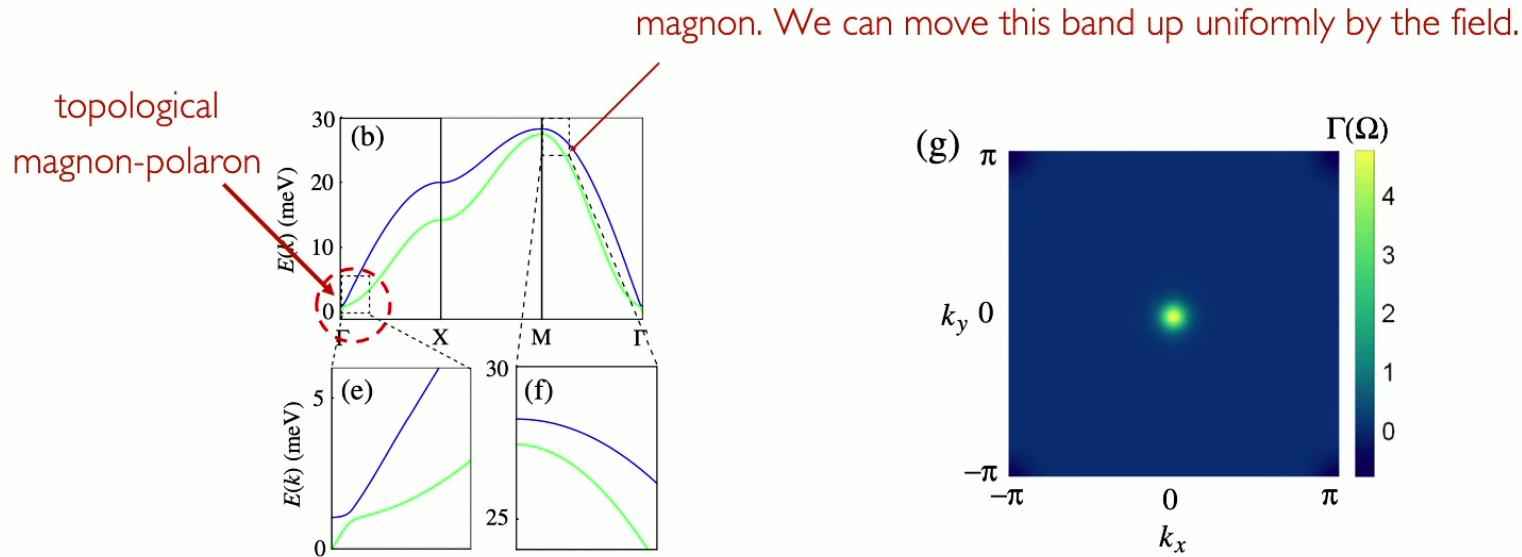
# Berry curvature of magnon-polarons



Go, SKK, and Lee., *PRL* (2020)

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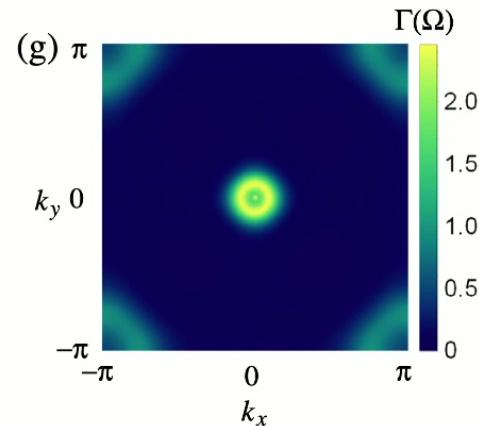
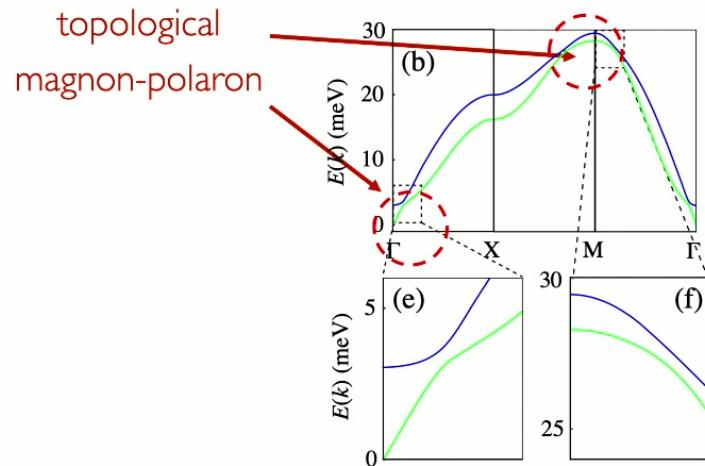
# Berry curvature of magnon-polarons



Finite Berry curvature near  $\Gamma$  point.  
The Chem number (of the upper band) is one.

Go, SKK, and Lee., *PRL* (2020)

# Berry curvature of magnon-polarons



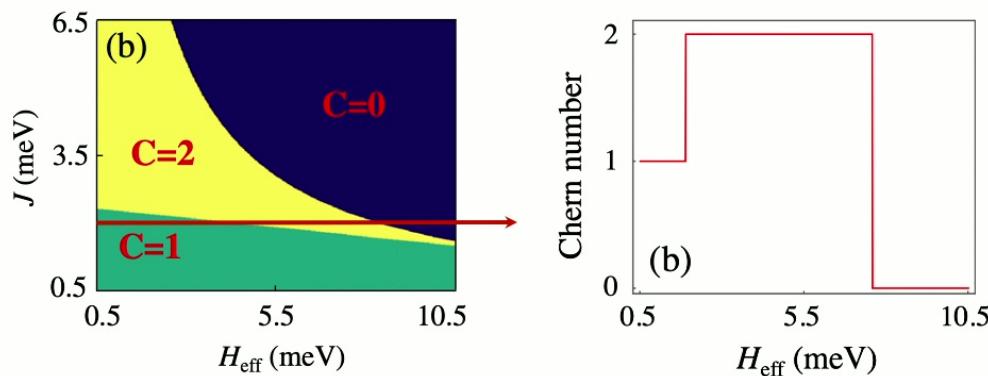
Finite Berry curvature near  $\Gamma$  & **M** points.  
The Chern number (of the upper band) is two.

Go, SKK, and Lee., *PRL* (2020)

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# Topological magnon-polarons

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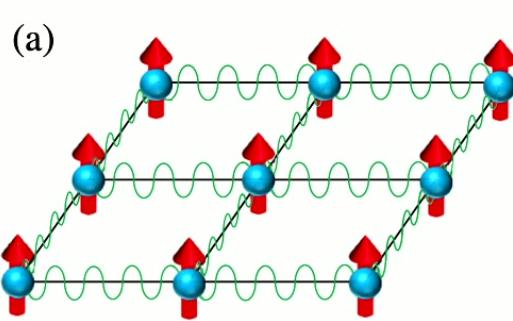


The Chern number can be controlled by varying an external field !!

Go, SKK, and Lee, *PRL* (2020)

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# Unsolved: spin transfer between magnon and phonon?



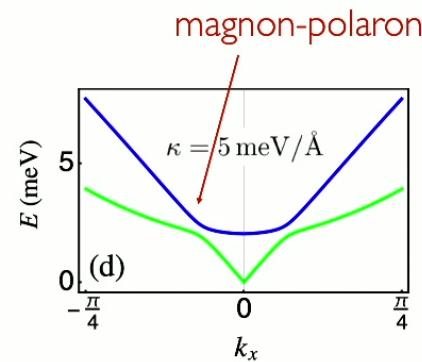
Go, SKK, and Lee, PRL (2020)

Magnetic sector:

$$H_{\text{mag}} = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j - \frac{K_z}{2} \sum_i S_{i,z}^2 - \mathcal{B} \sum_i S_{i,z},$$

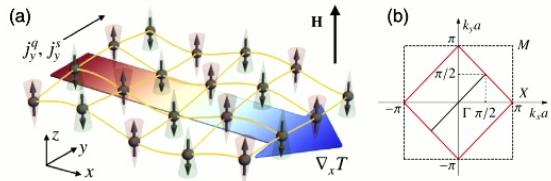
Lattice sector:

$$H_{\text{ph}} = \sum_i \frac{\mathbf{p}_i^2}{2M} + \frac{1}{2} \sum_{i,j,\alpha,\beta} u_i^\alpha \Phi_{i,j}^{\alpha,\beta} u_j^\beta,$$

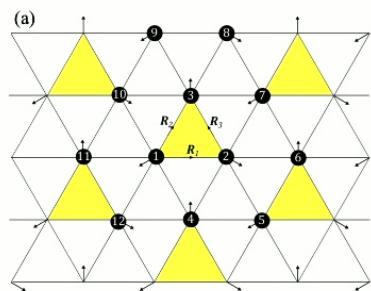


Magnetoelastic coupling:  $H_{\text{mp}} = \kappa \sum_i \sum_{\mathbf{e}} (\mathbf{S}_i \cdot \mathbf{e})(u_i^z - u_{i+\mathbf{e}}^z),$  (first discussed by Kittel in 1958)  
C. Kittel, Phys. Rev. 110, 836 (1958).

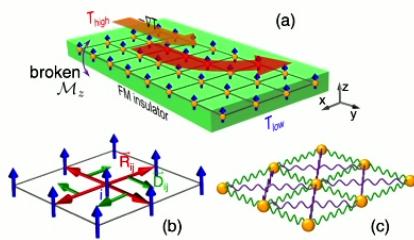
# A variety of topological magnon-polarons



SU(3) topology of magnon-polaron in 2D antiferromagnets  
Zhang, SKK, et al., *PRL* (2020)

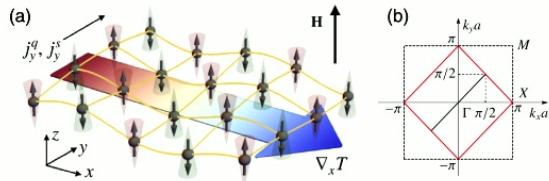


2D triangular antiferromagnet  
Park and Yang, *PRB* (2019)



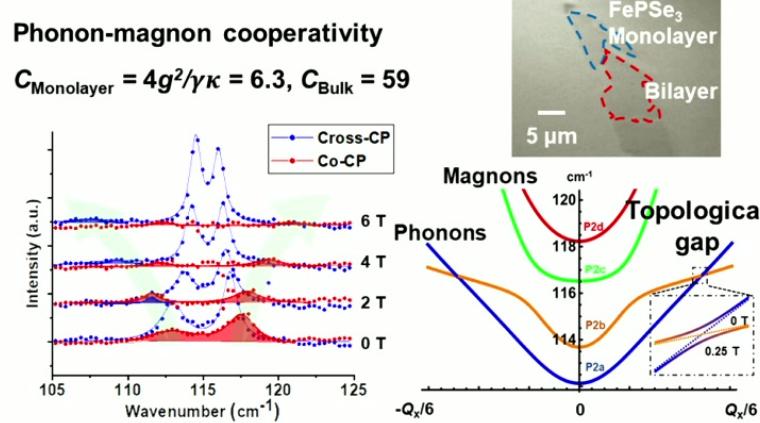
Inversion-symmetry-broken 2D ferromagnet  
(With Dzyaloshinskii-Moriya interaction)  
Zhang, Xiao, et al., *PRL* (2019)

# A variety of topological magnon-polarons



SU(3) topology of magnon-polaron in 2D antiferromagnets

Zhang, SKK, et al., *PRL* (2020)

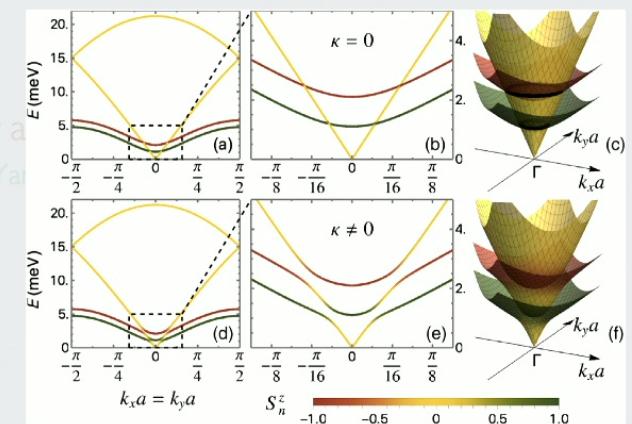


Experimental confirmation of a  
topological magnon-phonon coupling  
in a 2D magnet FePSe<sub>3</sub> !!

Inversion-symmetry-broken 2D ferromagnet

(With Dzyaloshinskii-Moriya interaction)  
Luo, Zhu et al., *Nano Lett.* (2023)

Zhang, Xiao, et al., *PRL* (2019)



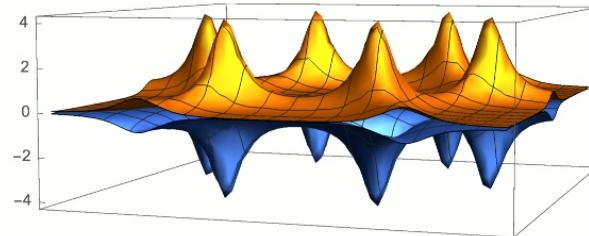
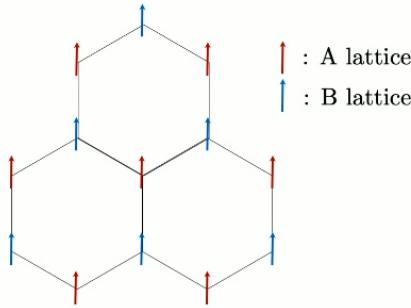
Wait!

All the known Hall effects of magnons require spin-orbit coupling.

Is spin-orbit coupling essential for Hall effects?

The known magnon Hall effects require spin-orbit coupling.

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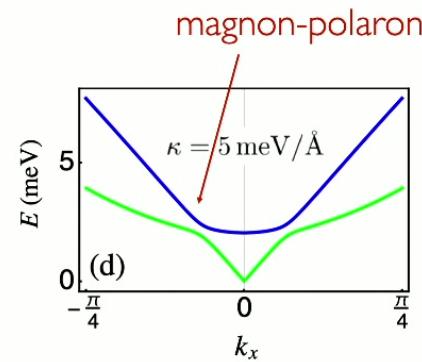
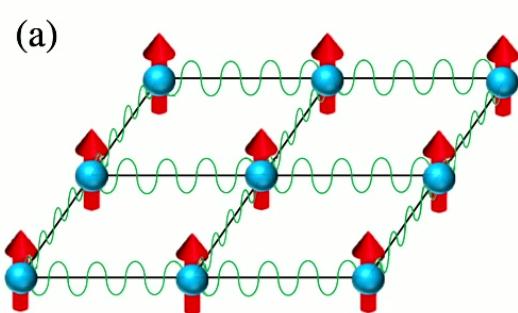


$$H = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + D \sum_{\langle\langle i,j \rangle\rangle} \nu_{ij} \hat{\mathbf{z}} \cdot \mathbf{S}_i \times \mathbf{S}_j - B \sum_i S_i^z$$

spin-orbit coupling (DMI)

In the example of a honeycomb ferromagnet,  
DMI gives rise to the Berry curvature and thus the spin Nernst effect.

The known magnon Hall effects require spin-orbit coupling.



Magnetic sector:

$$H_{\text{mag}} = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j - \frac{K_z}{2} \sum_i S_{i,z}^2 - \mathcal{B} \sum_i S_{i,z},$$

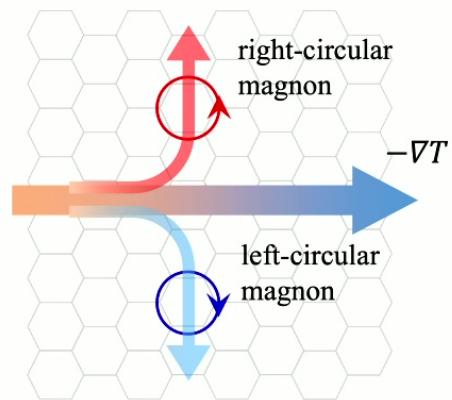
Lattice sector:

$$H_{\text{ph}} = \sum_i \frac{\mathbf{p}_i^2}{2M} + \frac{1}{2} \sum_{i,j,\alpha,\beta} u_i^\alpha \Phi_{i,j}^{\alpha,\beta} u_j^\beta,$$

Magnetoelastic coupling:  $H_{\text{mp}} = \kappa \sum_i \sum_{\mathbf{e}} (\mathbf{S}_i \cdot \mathbf{e})(u_i^z - u_{i+\mathbf{e}}^z),$   
spin-orbit coupling (magnon-phonon coupling)

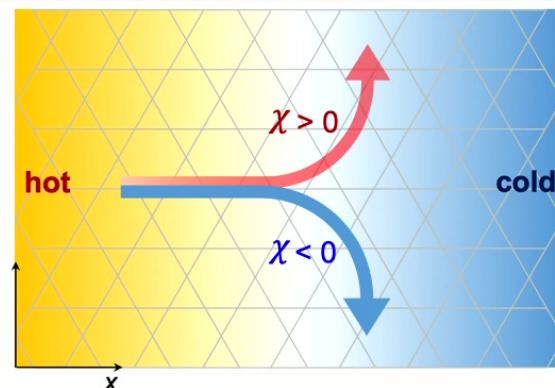
**The magnon-phonon coupling (effective spin-orbit coupling) gives rise to the Berry curvature and thus the thermal Hall effect.**

Is it possible for magnets to exhibit a Hall effect without SOC?



Magnon orbital Hall effect

Go, SKK, et al., Nano Lett. (2024)



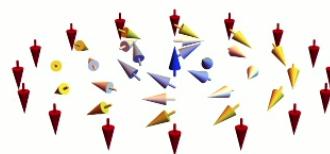
Scalar spin chirality Hall effect

Go, Prasad Goli, Esaki, Tserkovnyak, and SKK, arXiv:2411.03679

## Scalar spin chirality: an elementary unit of skyrmions

Skyrmion's topological charge:

Skyrmion:



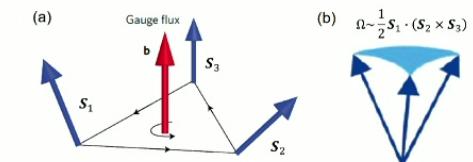
$$Q = \frac{1}{4\pi} \int dx dy \mathbf{n}_0 \cdot (\partial_x \mathbf{n}_0 \times \partial_y \mathbf{n}_0)$$
$$= \pm 1 \text{ for a full skyrmion}$$

lattice version

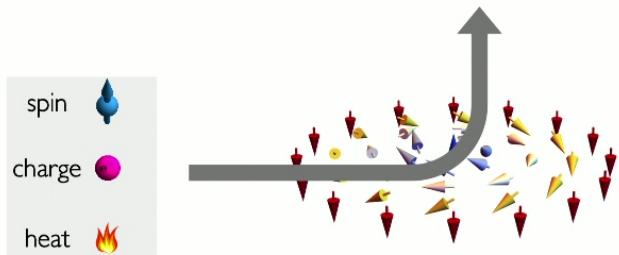


$$Q = \frac{1}{4\pi} \sum_{\Delta} \underline{\mathbf{S}_i \cdot (\mathbf{S}_j \times \mathbf{S}_k)} \approx \pm 1$$

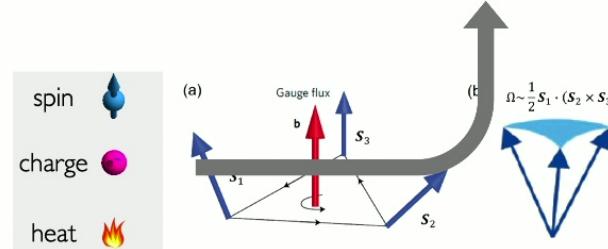
Scalar spin chirality:



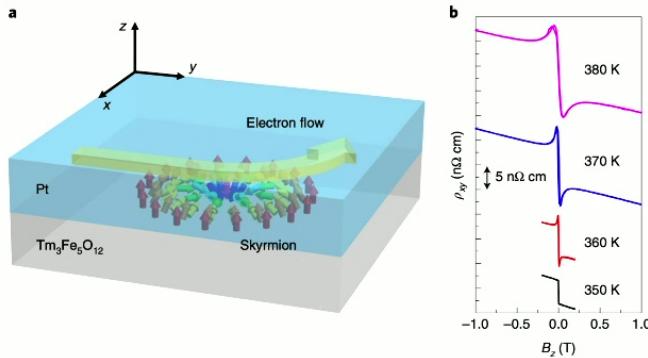
## Hall effect due to spin textures



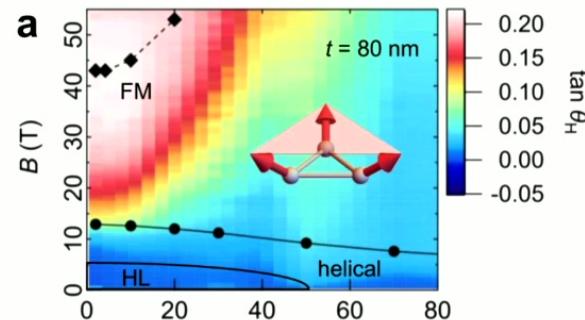
Topological Hall effect due to static skyrmions



Topological Hall effect due to the static scalar spin chirality



Topological Hall resistivity of Pt | TmIG  
Shao, SKK, et al. Nat. Electron. (2019)



Topological Hall angle of MnGe thin films  
Fujishiro, Tokura et al., Nat. Commun. (2021)

# Scalar spin chirality: known source of the various Hall effects

Science Advances

HOME > SCIENCE ADVANCES > VOL. 4, NO. 2 > SPIN CHIRALITY INDUCED SKW SCATTERING AND ANOMALOUS HALL EFFECT IN CHIRAL MAGNETS

RESEARCH ARTICLE PHYSICS

Spin chirality induced skew scattering and anomalous Hall effect in chiral magnets

Hiroaki Ishizuka  and Naoya Nagasawa  Authors info & Affiliations

SCIENCE ADVANCES • 9 Feb 2018 • Vol. 4, Issue 2 • <https://doi.org/10.1126/sciadv.020792>

nature materials

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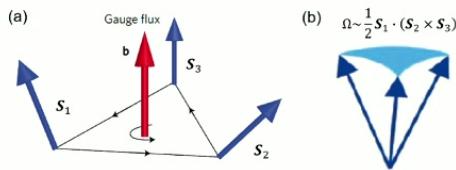
nature > nature materials > letters > article

Letter Published: 12 August 2019

Spin chirality fluctuation in two-dimensional ferromagnets with perpendicular magnetic anisotropy

Wenbo Wang, Matthew W. Daniels, Zhaoliang Liao, Yifan Zhao, Jun Wang, Gertjan Koster, Guus Rijnders, Cui-Zu Chang, Di Xiao & Weida Wu 

Nature Materials 18, 1054–1059 (2019) | [Cite this article](#)



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Article | Open access Published: 12 January 2021

Giant anomalous Hall effect from spin-chirality scattering in a chiral magnet

Yukako Fujishiro , Naoya Kanazawa , Ryosuke Kurihara, Hiroaki Ishizuka, Tomohiro Hori, Fehmi Sami Yasin, Xizhen Yu, Atsushi Tsukazaki, Masakazu Ichikawa, Masashi Kawasaki, Naoto Nagaosa, Masashi Tokunaga & Yoshinori Tokura 

Nature Communications 12, Article number: 317 (2021) | [Cite this article](#)

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Article | Open access Published: 24 March 2023

Field-linear anomalous Hall effect and Berry curvature induced by spin chirality in the kagome antiferromagnet Mn<sub>3</sub>Sn

Xiaokang Li , Jahyun Koo, Zengwei Zhu , Kamran Behnia & Binghai Yan 

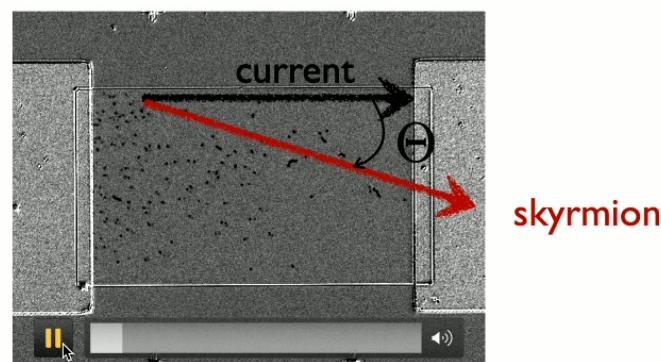
Nature Communications 14, Article number: 1642 (2023) | [Cite this article](#)

The scalar spin chirality generates an effective magnetic field for electrons, whereby inducing various Hall effects.

In all the previous studies, the scalar spin chirality is assumed to be static.

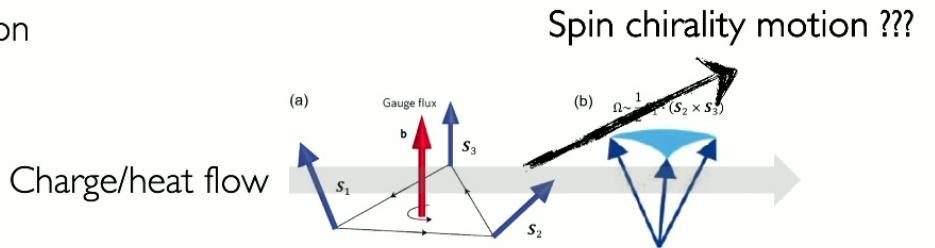
## Hall effect of mobile spin textures

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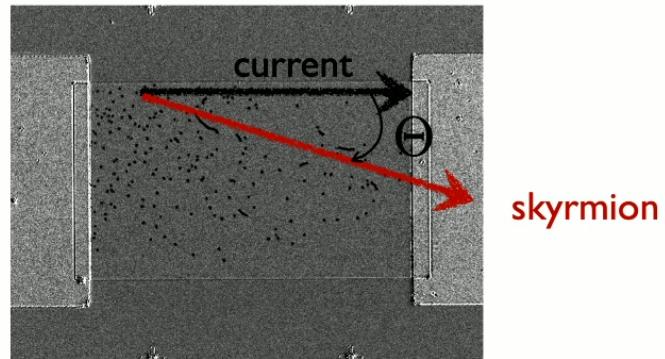


Skymion Hall effect in Ta | CoFeB | MgO  
Yu, SKK, et al. Nano Lett. (2016)

# Hall effect of mobile spin textures



Open question: If we allow the spin chirality to move, would there be the scalar spin chirality Hall effect ???

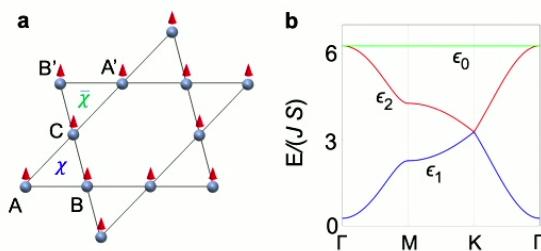


Skyrmion Hall effect in Ta | CoFeB | MgO  
Yu, SKK, et al. Nano Lett. (2016)

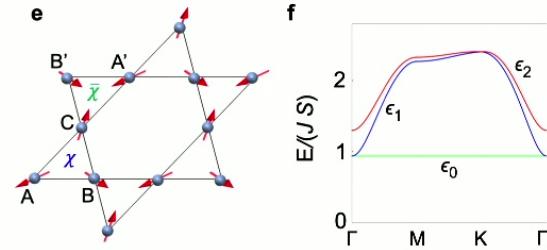
# Scalar-spin-chirality Nernst effect in FM/AFM Kagome lattices

$$H = -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j - K \sum_i (\mathbf{S}_i \cdot \mathbf{e}_i)^2, \quad \text{No spin-orbit coupling !!}$$

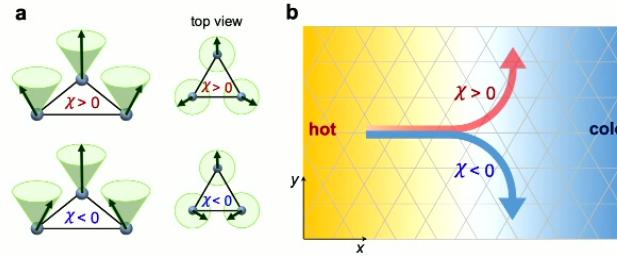
Ferromagnet (FM)



Antiferromagnet (AFM)



Both systems exhibit finite Nernst effect of the scalar spin chirality !!

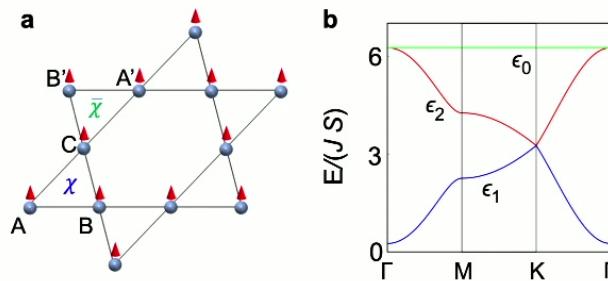


Go, Prasad Goli, Esaki, Tserkovnyak, and SKK, arXiv:2411.03679

# Scalar-spin-chirality Nernst effect in FM Kagome lattices

How can we describe the transport of the scalar spin chirality ? In terms of magnons !

$$\begin{aligned}
 H &= -J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j - K \sum_i (S_{i,z})^2 + \sum_{\langle i,j \rangle} \mathbf{D}_{ij} \cdot (\mathbf{S}_i \times \mathbf{S}_j) - g\mu_B B \sum_i S_{i,z}, \\
 H &= \sum_{\mathbf{k}} \Psi_{\mathbf{k}}^\dagger h_{\mathbf{k}} \Psi_{\mathbf{k}}, \quad \Psi_{\mathbf{k}} = (a_{\mathbf{k}}, b_{\mathbf{k}}, c_{\mathbf{k}})^T, \\
 h_{\mathbf{k}} &= \bar{\epsilon} - 2S\sqrt{J^2 + D^2} \begin{pmatrix} 0 & \cos(\mathbf{k} \cdot \mathbf{a}_1)e^{i\phi} & \cos(\mathbf{k} \cdot \mathbf{a}_2)e^{-i\phi} \\ \cos(\mathbf{k} \cdot \mathbf{a}_1)e^{-i\phi} & 0 & \cos(\mathbf{k} \cdot \mathbf{a}_3)e^{i\phi} \\ \cos(\mathbf{k} \cdot \mathbf{a}_2)e^{i\phi} & \cos(\mathbf{k} \cdot \mathbf{a}_3)e^{-i\phi} & 0 \end{pmatrix}, \\
 \epsilon_{\mathbf{k}}^1 &= \bar{\epsilon} - JS(\sqrt{1 + 4f_{\mathbf{k}}} + 1), \quad \epsilon_{\mathbf{k}}^2 = \bar{\epsilon} + JS(\sqrt{1 + 4f_{\mathbf{k}}} - 1), \quad \epsilon_{\mathbf{k}}^0 = \bar{\epsilon} + 2JS,
 \end{aligned}$$



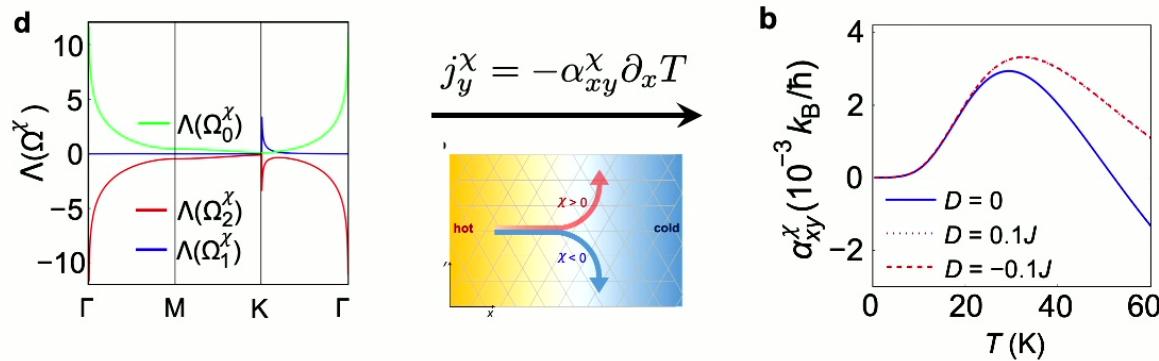
# Scalar-spin-chirality Nernst effect in FM Kagome lattices

How can we describe the transport of the scalar spin chirality ? In terms of magnons !

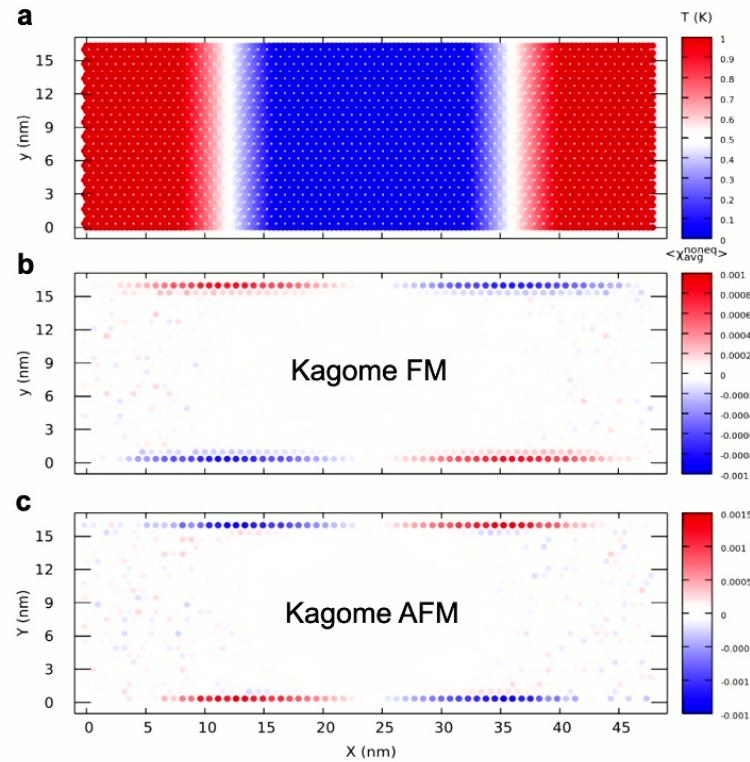
$$\chi_i = \hat{\mathbf{S}}_{\mathbf{r}_i}^A \cdot (\hat{\mathbf{S}}_{\mathbf{r}_i}^B \times \hat{\mathbf{S}}_{\mathbf{r}_i}^C) = -\frac{i}{S} \left( a_{\mathbf{r}_i}^\dagger b_{\mathbf{r}_i+\mathbf{a}_1} + b_{\mathbf{r}_i+\mathbf{a}_1}^\dagger c_{\mathbf{r}_i+\mathbf{a}_1+\mathbf{a}_2} + c_{\mathbf{r}_i+\mathbf{a}_1+\mathbf{a}_2}^\dagger a_{\mathbf{r}_i} \right) + \text{h.c.} = \Psi(\mathbf{r}_i)^\dagger \hat{\chi}_{\mathbf{r}} \Psi(\mathbf{r}_i),$$

$$\hat{\chi}_{\mathbf{k}} = -\frac{i}{S} \begin{pmatrix} 0 & e^{i\mathbf{k}\cdot\mathbf{a}_1} & -e^{-i\mathbf{k}\cdot\mathbf{a}_3} \\ -e^{-i\mathbf{k}\cdot\mathbf{a}_1} & 0 & e^{i\mathbf{k}\cdot\mathbf{a}_2} \\ e^{i\mathbf{k}\cdot\mathbf{a}_3} & -e^{-i\mathbf{k}\cdot\mathbf{a}_2} & 0 \end{pmatrix}$$

$$\Omega_{n,\mathbf{k}}^{\chi(\bar{\chi})} = - \sum_{m \neq n} \frac{2\hbar^2 \text{Im} \langle n | j_{y,\mathbf{k}}^{\chi(\bar{\chi})} | m \rangle \langle m | v_x | n \rangle}{(\epsilon_{n,\mathbf{k}} - \epsilon_{m,\mathbf{k}})^2}. \quad j_{y,\mathbf{k}}^{\chi} = \frac{1}{2}(v_y \hat{\chi}_{\mathbf{k}} + \hat{\chi}_{\mathbf{k}} v_y), j_{y,\mathbf{k}}^{\bar{\chi}} = \frac{1}{2}(v_y \hat{\bar{\chi}}_{\mathbf{k}} + \hat{\bar{\chi}}_{\mathbf{k}} v_y)$$

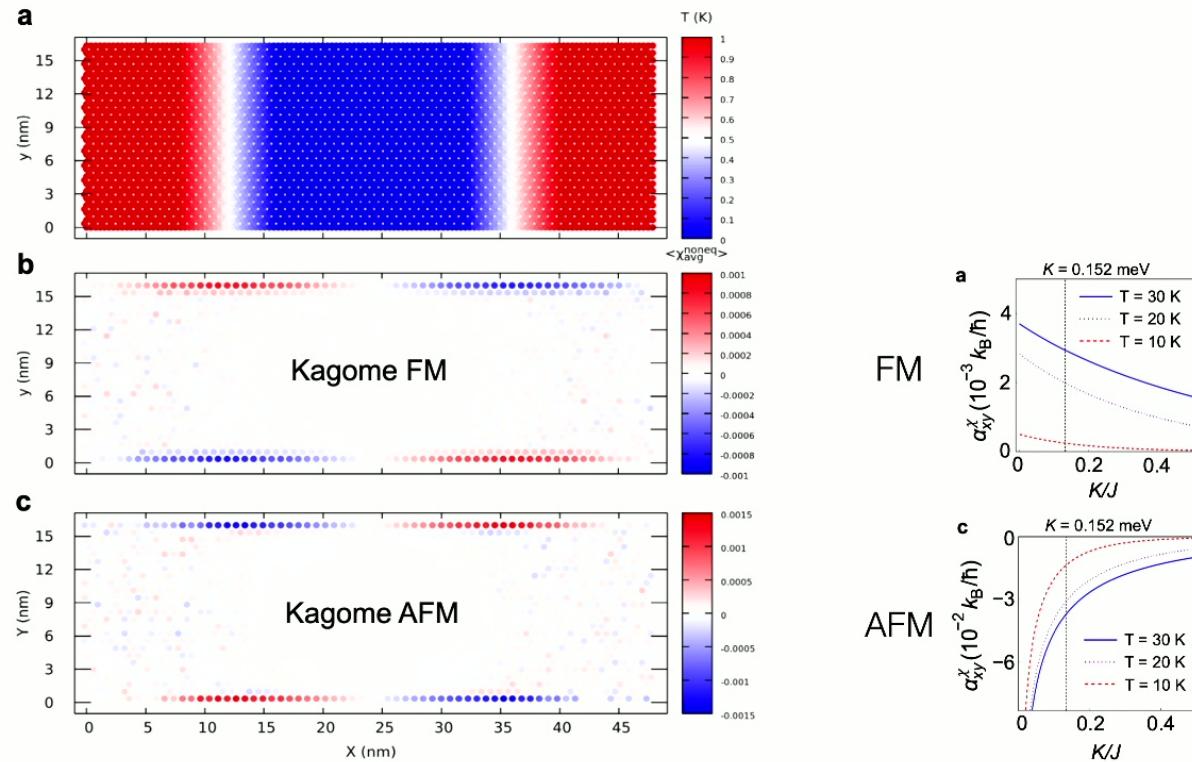


# Scalar-spin-chirality Nernst effect in FM/AFM Kagome lattices



Go, Prasad Goli, Esaki, Tserkovnyak, and SKK, arXiv:2411.03679

# Scalar-spin-chirality Nernst effect in FM/AFM Kagome lattices



FM and AFM systems exhibit the opposite signs of the scalar-spin-chirality Nernst conductivities.

Go, Prasad Goli, Esaki, Tserkovnyak, and SKK, arXiv:2411.03679

# Detection of the scalar spin chirality

## COMMUNICATIONS PHYSICS

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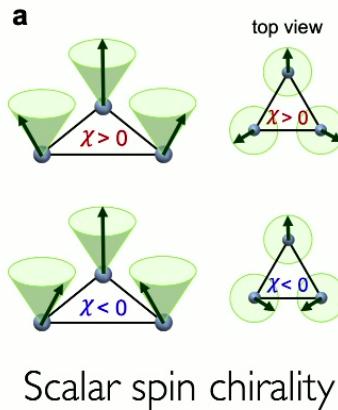
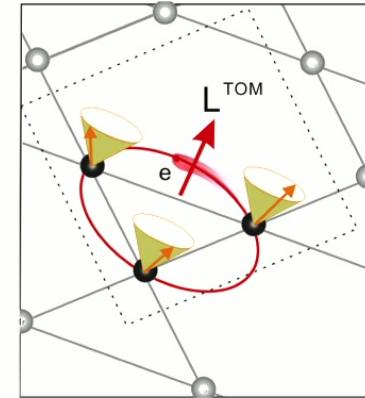
<https://doi.org/10.1038/s42005-020-00490-3>

OPEN

Check for updates

### Imprinting and driving electronic orbital magnetism using magnons

Li-chuan Zhang<sup>1,2</sup>, Dongwook Go<sup>1,3</sup>, Jan-Philipp Hanke<sup>1</sup>, Patrick M. Buhl<sup>3</sup>, Sergii Grytsiuk<sup>1</sup>, Stefan Blügel<sup>1</sup>, Fabian R. Lux<sup>1,2</sup> & Yury Mokrousov<sup>1,3✉</sup>



$$\longrightarrow L_z > 0$$

$$\longrightarrow L_z < 0$$

topological orbital magnetization,  
which can be detected by MOKE.

## Take-home message

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So far, only magnons or solitons such as skyrmions have been considered as a transportable quantity in magnetic insulators.

Go, Prasad Goli, Esaki, Tserkovnyak, and SKK, arXiv:2411.03679

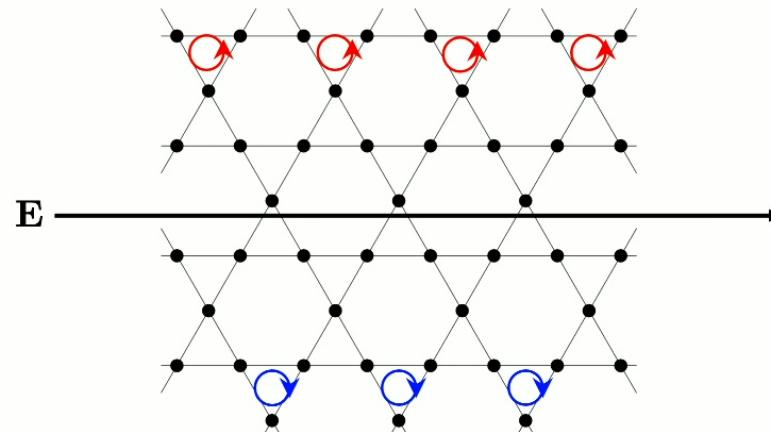
## Future investigations

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## Future investigations

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- The  $S=1/2$  limit of topological magnon physics.
- The  $S=1/2$  limit of topological magnon-polaron physics.
- The possibility of the scalar-spin-chirality Hall effect in  $S=1/2$  Kagome systems (*quantum spin liquids?*).
- The possibility of analogous Hall effects of *a charge loop current* in itinerant systems without spin-orbit coupling.



55

Thank you !!

