

**Title:** Cosmic-string gravitational wave backgrounds: detectability, signal reconstruction, and model comparison at LISA

**Speakers:** Dani Figueroa

**Collection/Series:** Strong Gravity

**Subject:** Strong Gravity

**Date:** April 10, 2025 - 1:00 PM

**URL:** <https://pirsa.org/25040106>

**Abstract:**

Cosmic string networks are expected to generate a large gravitational wave background (GWB). We present a survey of GWB signal templates depending on the underlying hypothesis of the cosmic-string network. Following, we introduce a machine learning method based on SBI techniques, to determine the detectability of these signals by LISA, including signal spectral reconstruction and model comparison procedures.

# The gravity of the cosmic-string case



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Valencia, Spain



( w/ A. Dimitriou, P. Simakachorn, B. Zaldivar )

Perimeter Institute, Waterloo, Canada, Strong Gravity Seminar, April 10th 2025



EXCELENCIA  
SEVERO  
OCHOA

UNIVERSITAT  
DE VALÈNCIA

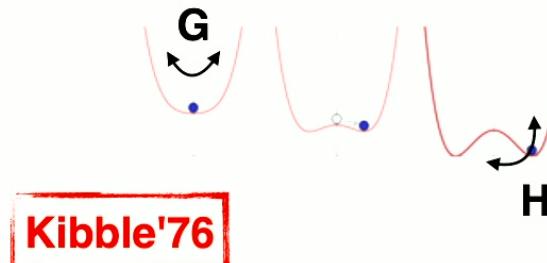
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GENERALITAT  
VALENCIANA

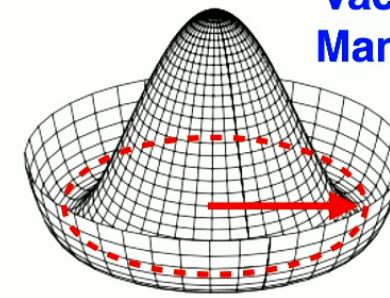
# Cosmic Defects

Spontaneous Symm. Break.



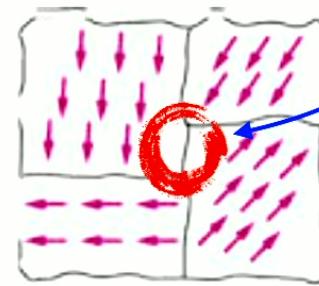
Kibble'76

Higgs fld  
Vacuum  
Manifold



$$M = G/H$$

Spatial Dist.



Topological  
Properties

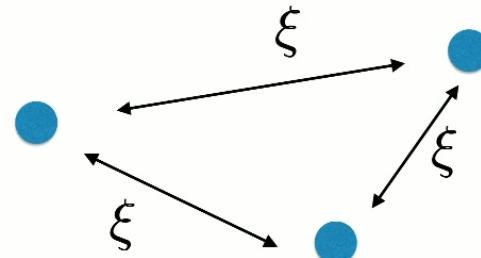
(Homotopy  
Groups  $\Pi_n(M) \neq I$ )

$\Pi_1(M) \neq I \Rightarrow$  Strings

# Cosmic Defects

DEFECTS: Aftermath of PhT  $\rightarrow \left\{ \begin{array}{l} \left\{ \begin{array}{l} \text{Domain Walls} \\ \text{Cosmic Strings} \\ \text{Cosmic Monopoles} \end{array} \right\} \\ \text{Non - Topological} \end{array} \right\}$

CAUSALITY & MICROPHYSICS  $\Rightarrow$  Corr. Length:  $\xi(t) = \lambda(t) H^{-1}(t)$

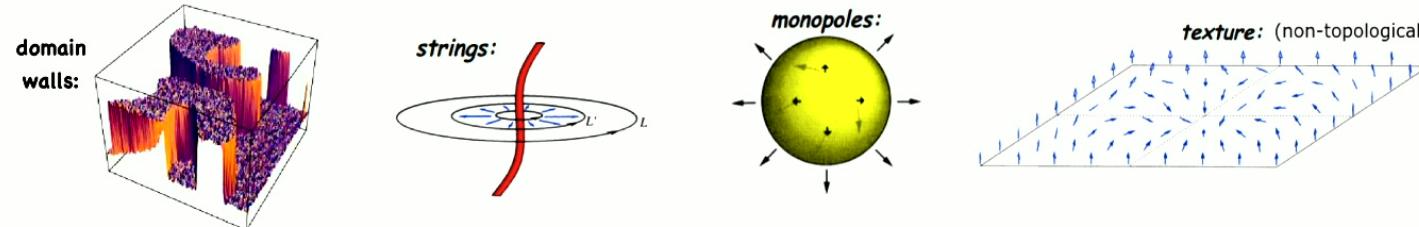


**Defect  
Networks**

# Cosmic Defects

DEFECTS: Aftermath of PhT  $\rightarrow$  

- Domain Walls
- Cosmic Strings
- Cosmic Monopoles
- Non - Topological



MICRO-PHYSICS  $\longrightarrow$  COSMIC DEFECTS  
 $(M = G/H)$

# Cosmic Defects

DEFECTS: Aftermath of PhT  $\rightarrow \left\{ \begin{array}{l} \text{Domain Walls} \\ \text{Cosmic Strings} \\ \text{Cosmic Monopoles} \\ \text{Non - Topological} \end{array} \right.$

CAUSALITY & MICROPHYSICS  $\Rightarrow$  Corr. Length:  $\xi(t) = \lambda(t) H^{-1}(t)$

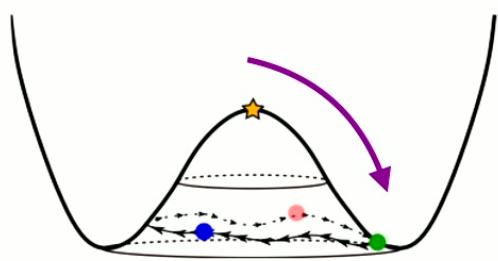
(Kibble' 76)

SCALING<sup>\*</sup>:  $\lambda(t) = \text{const.} \rightarrow \lambda \sim 1$

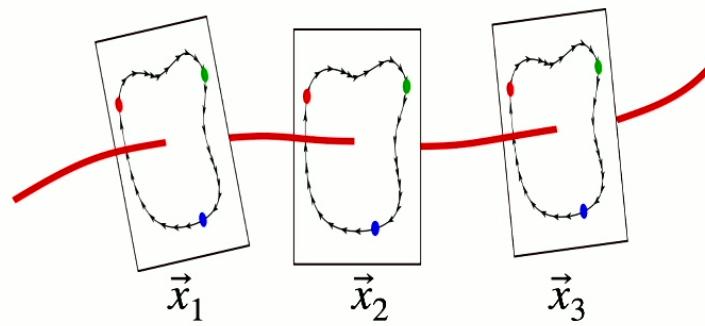
\* Could be not exact in some cases

# Cosmic Strings

One-dimensional topological defects ( $\Pi_1(M) \neq I$ )



Symm. Breaking Fld ('Higgs')

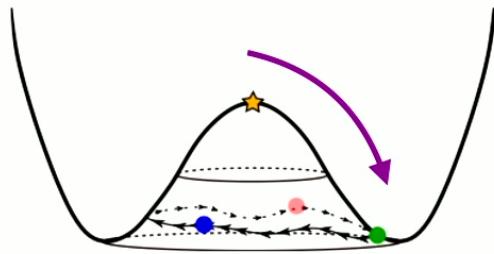


Different Vacua (at different locations)

e.g. ~~U(1)~~

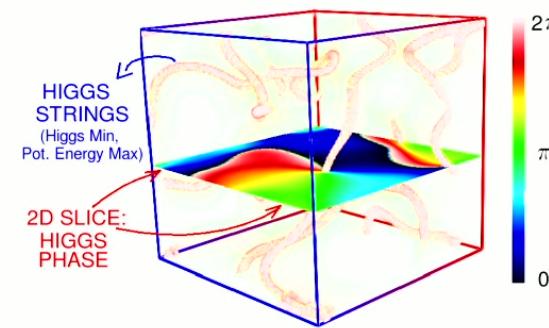
# Cosmic Strings

One-dimensional topological defects ( $\Pi_1(M) \neq I$ )



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e.g. ~~U(1)~~

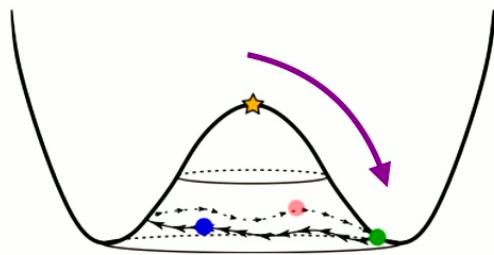


Different Vacua (at different locations)

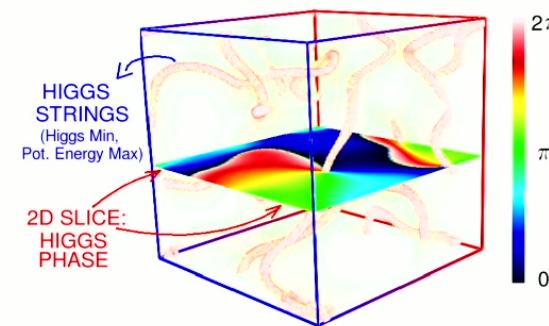
DGF, PhD Thesis 2010

# Cosmic Strings

One-dimensional topological defects ( $\Pi_1(M) \neq I$ )



Symm. Breaking Fld ('Higgs')



Different Vacua (at different locations)

Global ( $\phi$ )

- \* Long range int.
- \*  $m_1 = 0, m_2 \neq 0$
- \* e.g. Axion DM

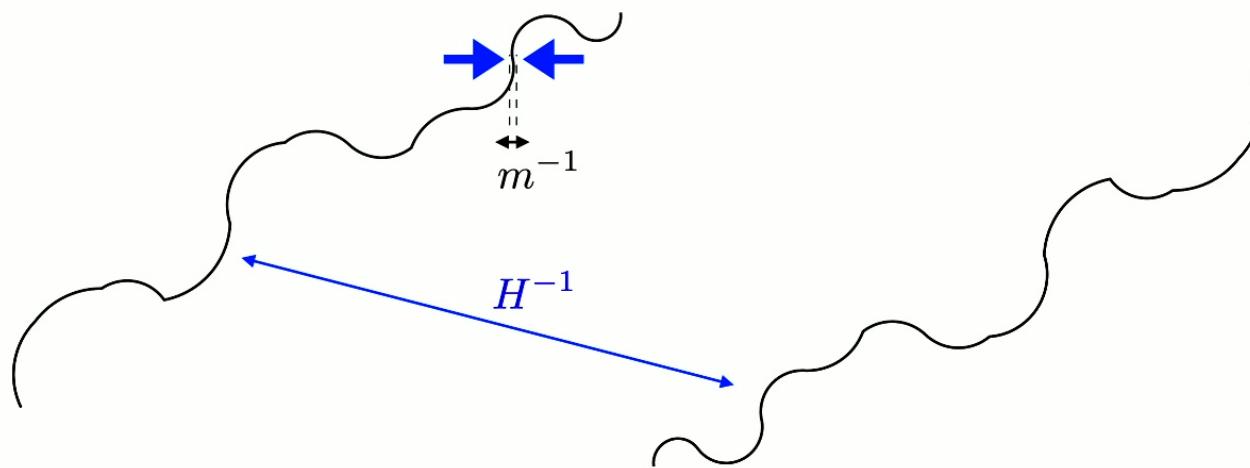
or

Local ( $\phi, A_\mu$ )

- \* Short range int.
- \*  $m_1 \neq 0, m_2 \neq 0$
- \* e.g. GUT models

# Cosmic String Networks

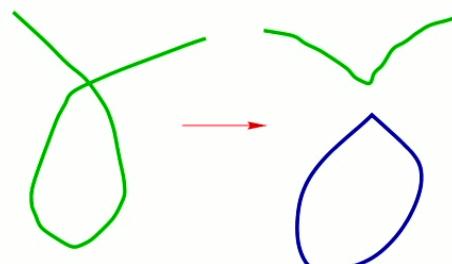
'Infinitely' thin:  $H^{-1} \gg m^{-1}$



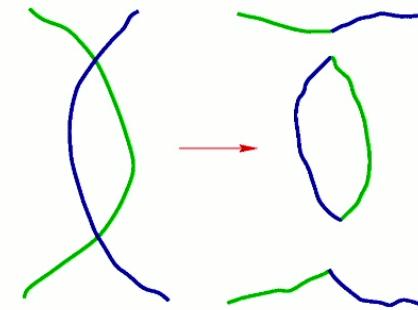
Nambu-Goto

# Cosmic String Networks

## Intercommutation



Loops !

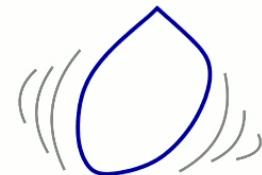


Loops !

# Cosmic String Networks

$$G\mu \equiv (\eta/M_p)^2$$

**Loops are formed !** Vibrate under their **tension** !

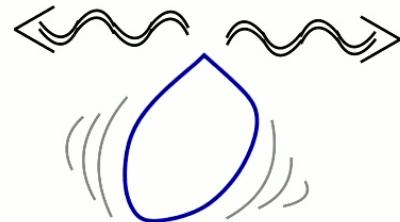


**Periodic  
Oscillations**

# Cosmic String Networks

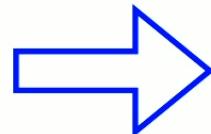
$$G\mu \equiv (\eta/M_p)^2$$

**Loops are formed !** Vibrate under their **tension** !



**Gravitational  
Waves (GW)  
are emitted !**

$$L = l(t_e)$$



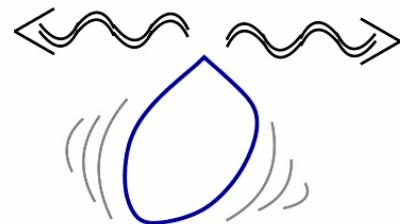
$$f_j = \frac{2}{L} \cdot j ; \quad j = 1, 2, 3, \dots$$

(Harmonic freq's)

# Cosmic String Networks

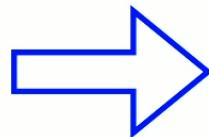
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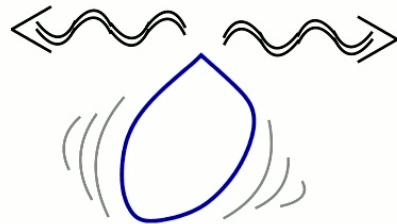
$$f = \left[ \frac{2j}{l(t_e)} \right] \cdot \left[ \frac{a(t_e)}{a_0} \right]$$

(Freq. Today)

# Cosmic String Networks

$$G\mu \equiv (\eta/M_p)^2$$

**Loops are formed !** Vibrate under their **tension** !



**Gravitational  
Waves (GW)  
are emitted !**

**Superposition from many loop signals**



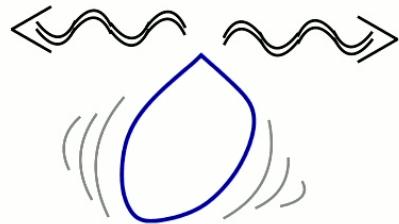
=  
**Gravitational Wave Background**



# Cosmic String Networks

$$G\mu \equiv (\eta/M_p)^2$$

**Loops are formed !** Vibrate under their **tension** !



**Gravitational  
Waves (GW)  
are emitted !**

**Word of Caution !**

Field-theory strings can also decay via particle production

**Following ... we assume GW emission dominates<sup>\*</sup> !**

(\* We will review this at the end of the talk)

# Grav. Wave Background

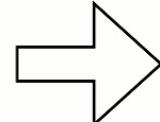
$$\frac{d\rho_{\text{GW}}^{(0)}}{df} \equiv \int_{t_*}^{t_0} dt \left( \frac{a(t)}{a(t_0)} \right)^3 \int_0^{a/H} dl n(l, t) P_{\text{GW}}(f, l)$$

↓  
expansion history      ↓  
length      ↓  
Loop number density      ↓  
( Nambu-Goto calculation )  
GW power emission  
 $\propto 1/(fl)^q$

GW power emission (NG)

$$\left( \frac{dE}{dt} \right)_{\text{tot}} = \Gamma G \mu^2 = G \mu^2 \sum_j P_j$$

↑  
Just a number      Sum over harmonics



$$P_j \equiv \Gamma \frac{j^{-q}}{\zeta(q)}$$

# Grav. Wave Background

$$\frac{d\rho_{\text{GW}}^{(0)}}{df} \equiv \int_{t_*}^{t_0} dt \left( \frac{a(t)}{a(t_0)} \right)^3 \int_0^{a/H} dl n(l, t) P_{\text{GW}}(f, l)$$

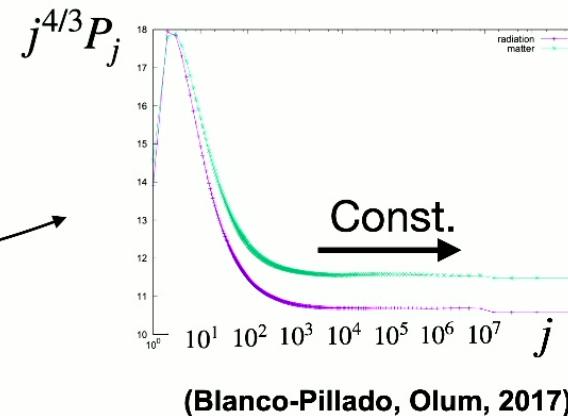
↓  
**expansion history**  
 ↓  
**length**  
 ↓  
**Loop number density**  
 ↓  
**( Nambu-Goto calculation )**  
 ↓  
**GW power emission**  
 $\propto 1/(fl)^q$

GW power emission (NG)

$$P_j \equiv \Gamma \frac{j^{-q}}{\zeta(q)}$$

$$q = \frac{4}{3} \quad (\text{cusps})$$

Reality...  
(From NG sim's)

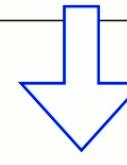


# Grav. Wave Background

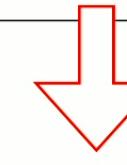
$$\Omega_{\text{GW}}(f) = \frac{1}{3H_0^2 m_{\text{Pl}}^2} \sum_{j=1}^{\infty} \underbrace{\frac{2j}{f} (G\mu^2 P_j)}_{\text{GW emission from single loops}} \int_{a_2}^{a_1} da \underbrace{\frac{1}{H(a)} \left(\frac{a}{a_0}\right)^4}_{\text{cosmic history}} \underbrace{n\left[\frac{2j}{f} \cdot \frac{a}{a_0}, t(a)\right]}_{\text{loop number density}}$$



**Conventional**



NG analytics



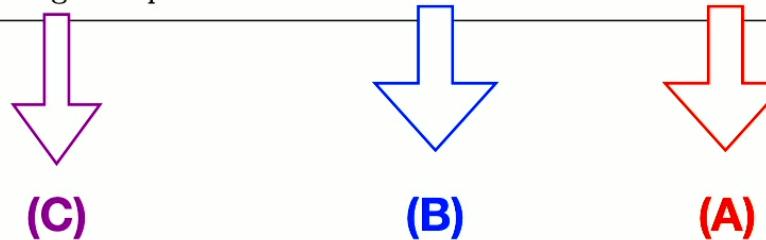
$\Lambda$ CDM

NG analytics

Beyond  
Conventional

# Grav. Wave Background

$$\Omega_{\text{GW}}(f) = \frac{1}{3H_0^2 m_{\text{Pl}}^2} \sum_{j=1}^{\infty} \underbrace{\frac{2j}{f} (G\mu^2 P_j)}_{\text{GW emission from single loops}} \int_{a_2}^{a_1} da \underbrace{\frac{1}{H(a)} \left(\frac{a}{a_0}\right)^4}_{\text{cosmic history}} \underbrace{n\left[\frac{2j}{f} \cdot \frac{a}{a_0}, t(a)\right]}_{\text{loop number density}}$$



Conventional

NG analytics

$\Lambda$ CDM

NG analytics

NG sims

$\Lambda$ CDM

NG sims

**Beyond  
Conventional**

....

e.g. Kination

....

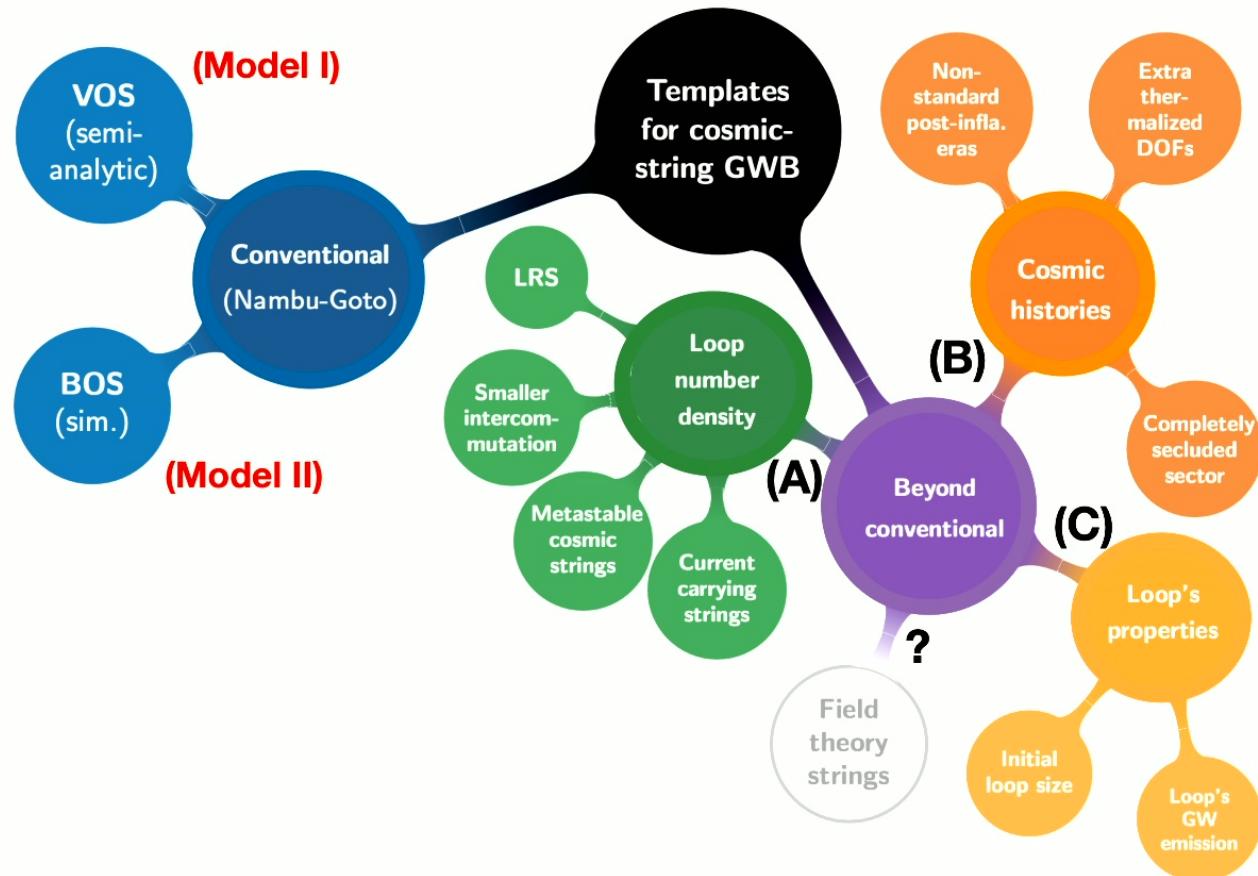
$q \neq 4/3$

....

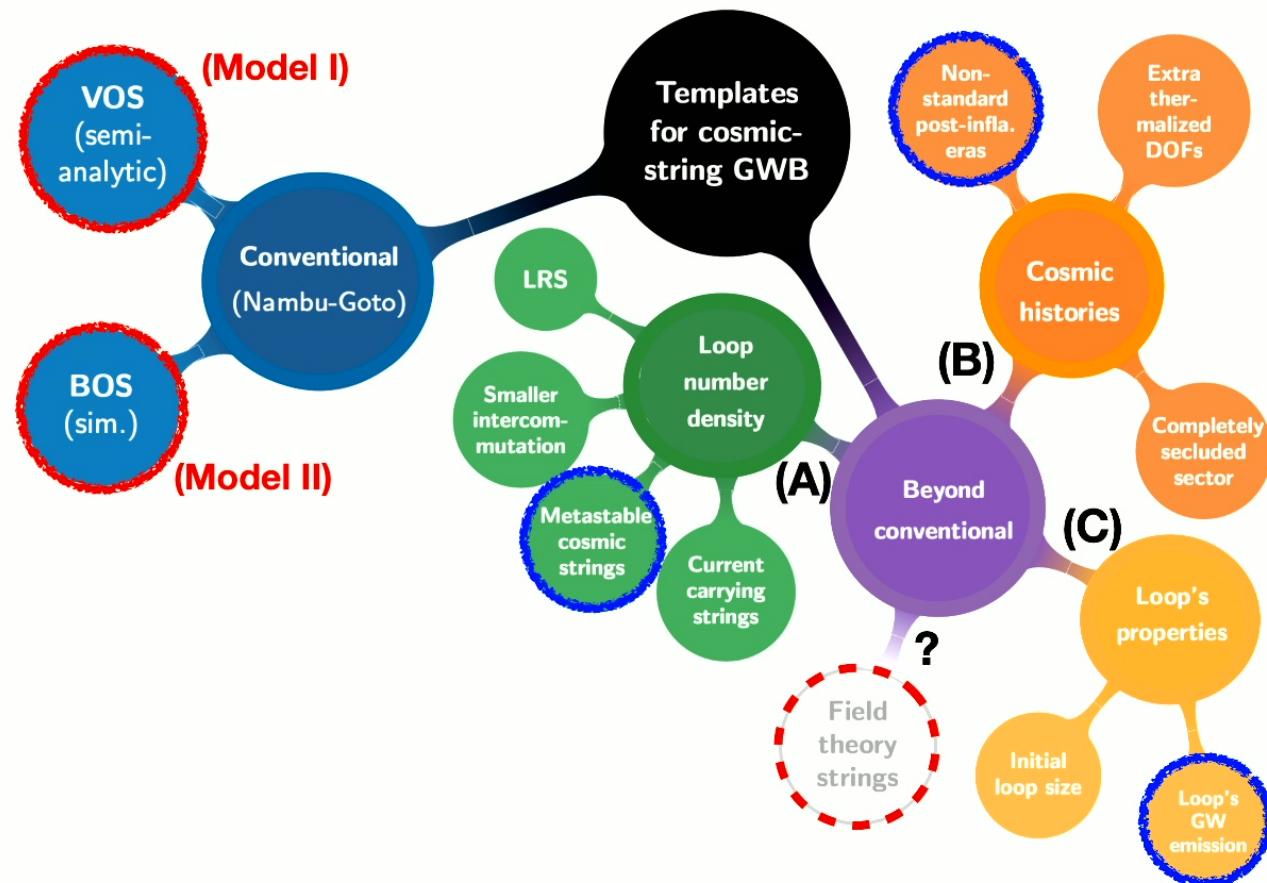
e.g. Metastable strings

....

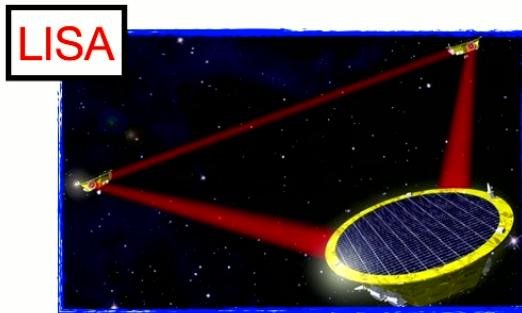
# Grav. Wave Background(s)



# Grav. Wave Background(s)



# GW Background Signals: Detectability



3 interferometric channels

$$X, Y, Z \longleftrightarrow A, E, T$$

$$\begin{pmatrix} XX & XY & XZ \\ YX & YY & YZ \\ ZX & ZY & ZZ \end{pmatrix} \quad \begin{pmatrix} AA & 0 & 0 \\ 0 & EE & 0 \\ 0 & 0 & TT \end{pmatrix}$$

$$N_{AA}(f; A_P, A_{acc}) = N_{EE}(f; A_P, A_{acc})$$

$$= 8 \sin^2 x_f [4(1 + \cos x_f + \cos^2 x_f) P_{acc}(f; A_{acc}) + (2 + \cos x_f) P_{IMS}(f; A_P)]$$

$$N_{TT}(f; A_P, A_{acc}) = 16 \sin^2 x_f [2(1 - \cos x_f)^2 P_{acc}(f; A_{acc}) + (1 - \cos x_f) P_{IMS}(f; A_P)].$$

$$\left. \begin{array}{l} P_{IMS} = 1.6 \times 10^{-43} A_P^2 \left[ 1 + (2 \text{ mHz}/f)^4 \right] x_f^2 \text{ Hz}^{-1}, \text{ (Interferometry Metrology System, e.g. shot noise)} \\ P_{acc} = 7.7374 \times 10^{-46} A_{acc}^2 \left[ 1 + (0.4 \text{ mHz}/f)^2 \right] \left[ 1 + (f/8 \text{ mHz})^4 \right] x_f^{-2} \text{ Hz}^{-1}. \text{ (Mass acceleration)} \end{array} \right\}$$

$\downarrow$

$$A_{acc} = 3 \pm 0.6$$

$$A_P = 15 \pm 3$$

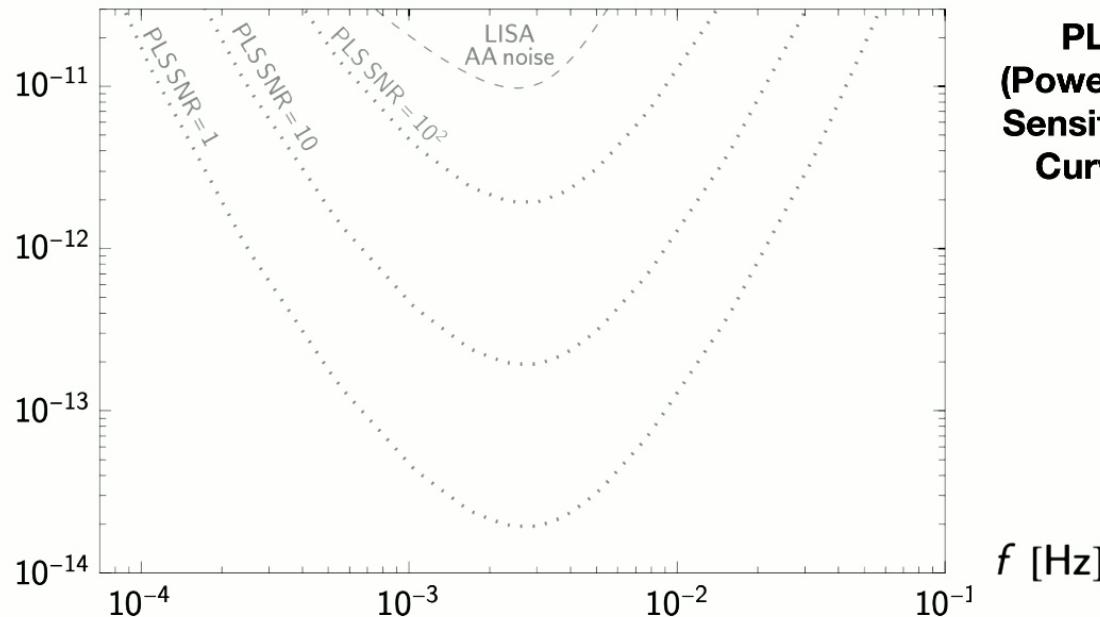
LISA Data Challenge Manual. Tech. Rep.  
 LISA-LCST-SGS-MAN-002. APC Paris, July 2020.  
 LISA Pathfinder (2016) [PhysRevLett.116.231101](#)

# GW Background Signals: Detectability

$$\text{SNR} = \sqrt{T_{\text{obs}} \int_{f_{\text{min}}}^{f_{\text{max}}} df \left[ \frac{\Omega_{\text{GW}}(f)}{\Omega_{\text{noise}}(f)} \right]^2}$$

Signal-to-Noise Ratio  
**(Naive Method ?)**

$h^2 \Omega_{\text{GW}}$

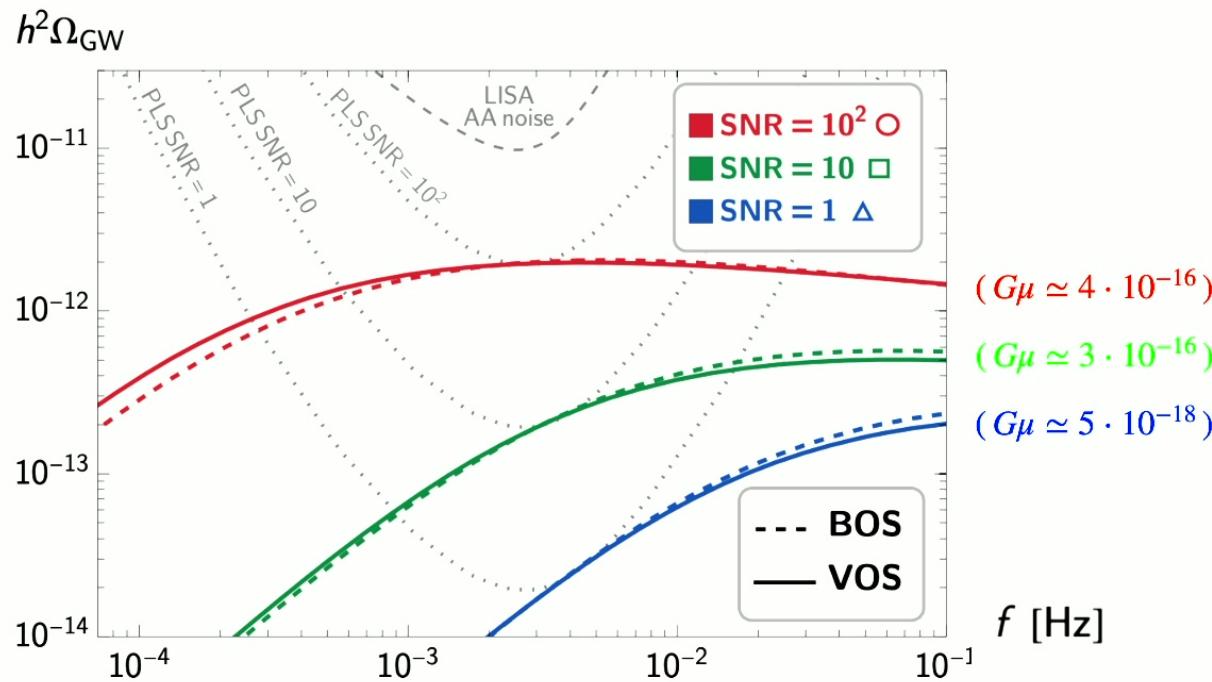


**PLS**  
**(PowerLaw**  
**Sensitivity)**  
Curves

# GW Background Signals: Detectability

$$\text{SNR} = \sqrt{T_{\text{obs}} \int_{f_{\min}}^{f_{\max}} df \left[ \frac{\Omega_{\text{GW}}(f)}{\Omega_{\text{noise}}(f)} \right]^2}$$

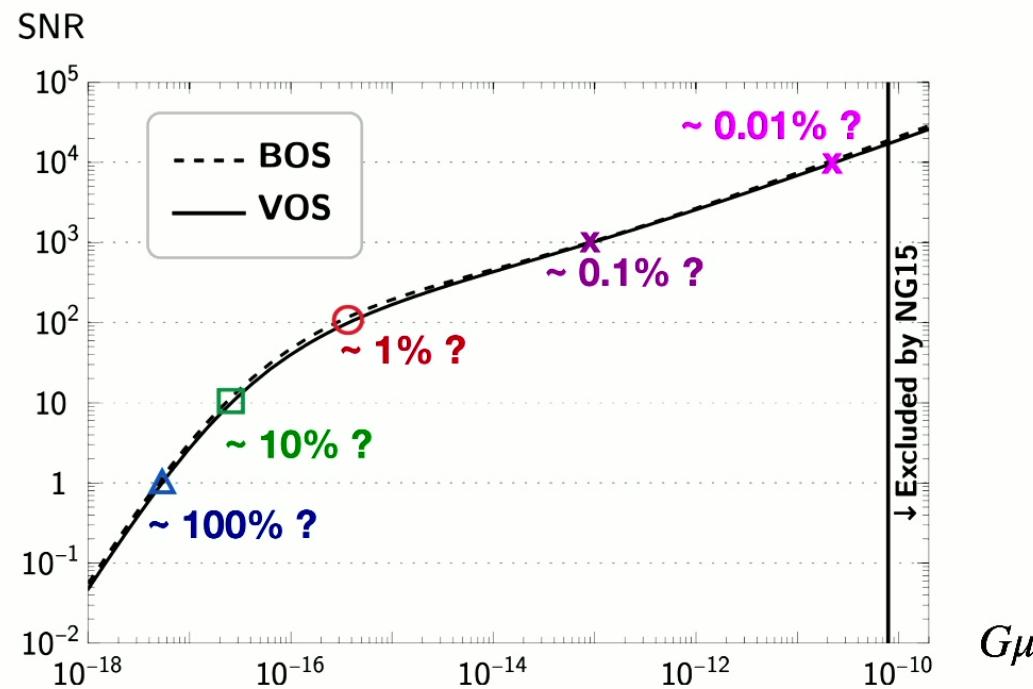
Signal-to-Noise Ratio  
**(Naive Method ?)**



# GW Background Signals: Detectability

$$\text{SNR} = \sqrt{T_{\text{obs}} \int_{f_{\min}}^{f_{\max}} df \left[ \frac{\Omega_{\text{GW}}(f)}{\Omega_{\text{noise}}(f)} \right]^2}$$

Signal-to-Noise Ratio  
(Naive Method ?)



# **GW Background Signals: Detectability**

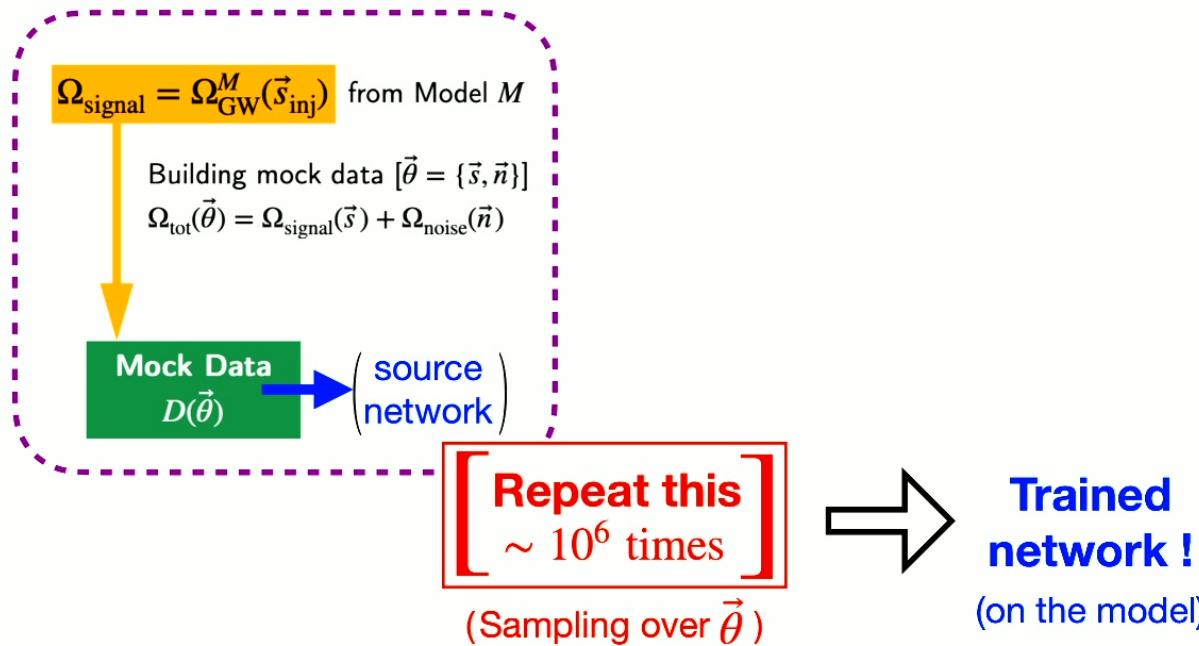
**We want precision  
cosmology/HEP !**

- Signal error reconstruction**
- Proper Parameter Estimation**

# GW Background Signals: Detectability

## Simulation-Based Inference (SBI)

( Machine Learning method )

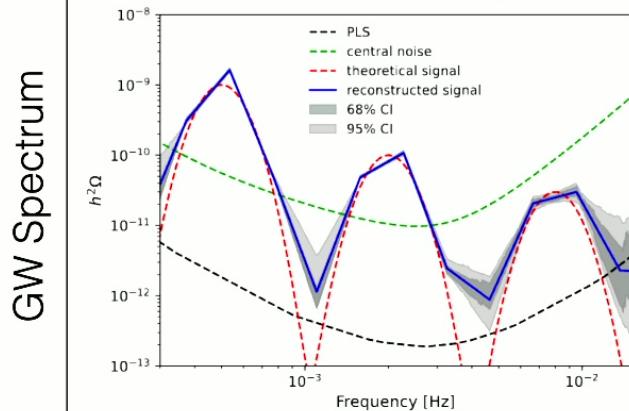


# GW Background Signals: Detectability

## Simulation-Based Inference (SBI)

Blind signal  
Reconstruction

### Arbitrary Spectrum



### Code GWBackFinder

(Dimitriou et al [2309.08430](#))

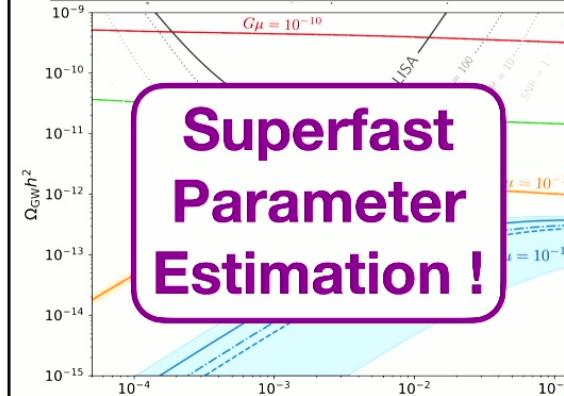
# GW Background Signals: Detectability

## Simulation-Based Inference (SBI)

Blind signal  
Reconstruction  
Arbitrary Spectrum

Template signal  
reconstruction

### Template ( $\vec{\alpha}$ ) Spectrum

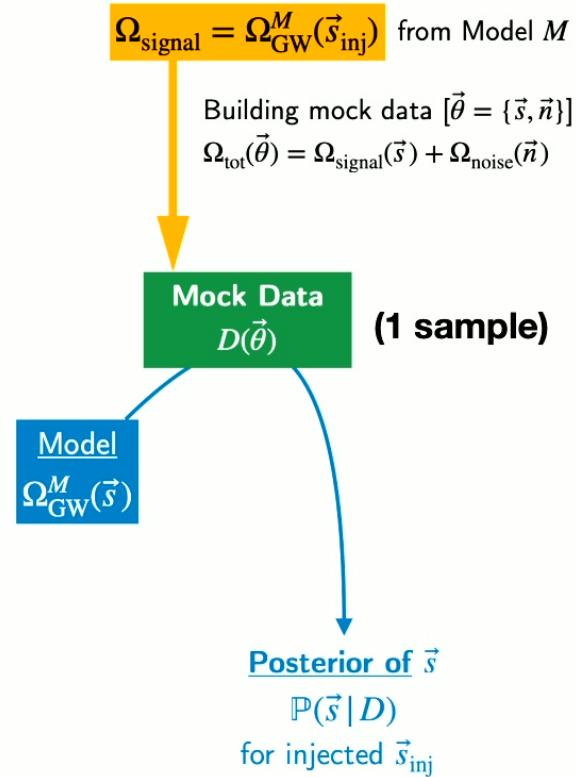


Applications to Cosmic Strings,  
Phase Transitions, Inflation, ...

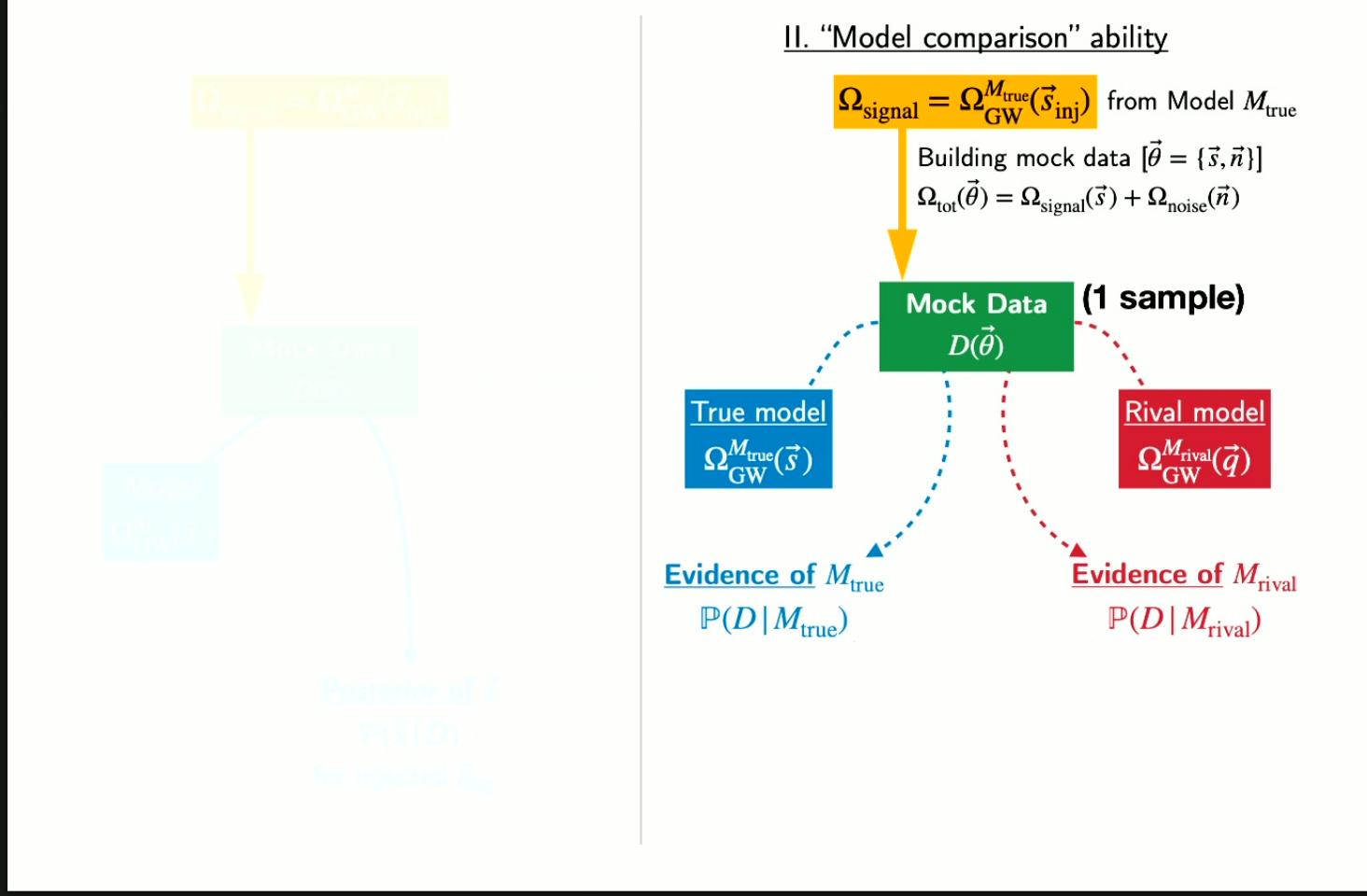
Dimitriou et al, Work in progress

# GW Background Signals: Detectability

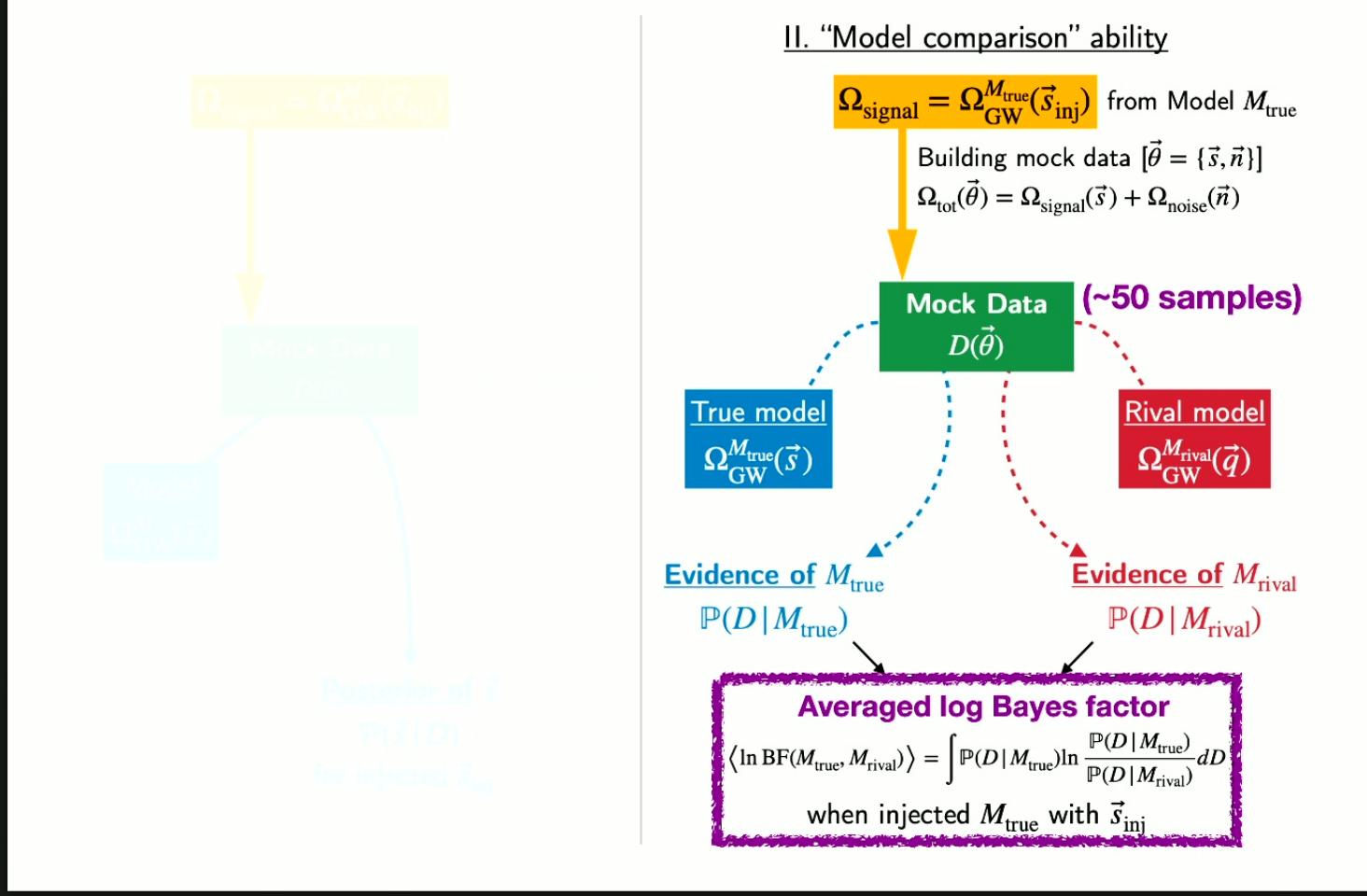
## I. "Signal reconstruction" ability



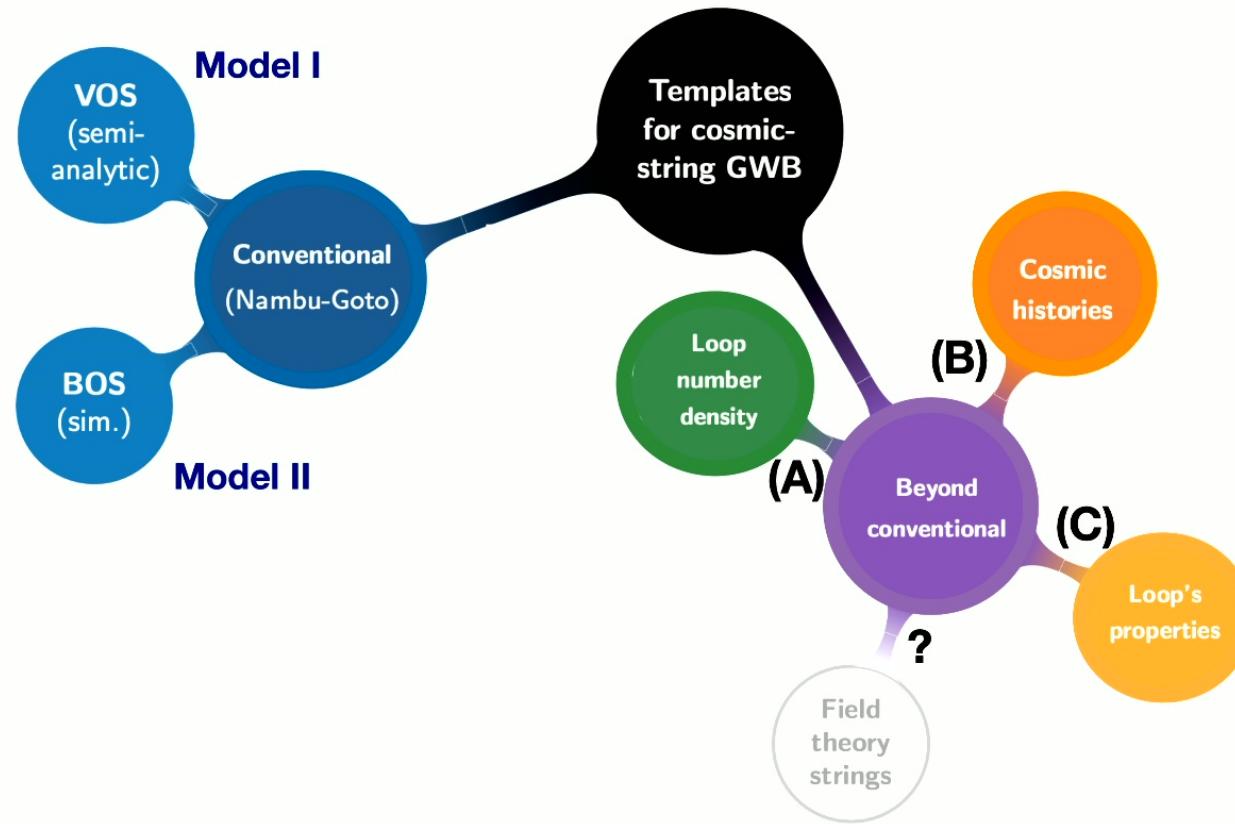
# GW Background Signals: Detectability



# GW Background Signals: Detectability



# GW Background Signals: Detectability



# Conventional Signals: VOS & BOS

(analytical) (simulation)

One-parameter templates:  $G\mu$

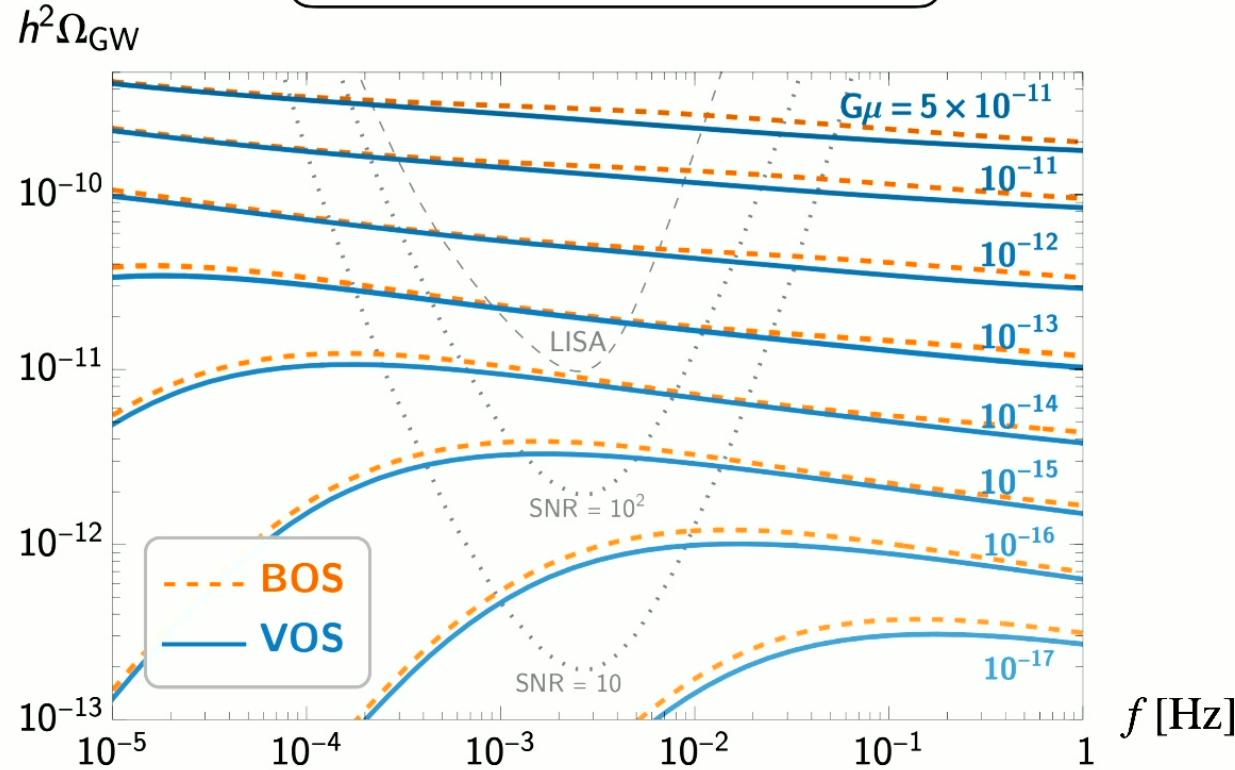
(String tension  $G\mu$ : log-uniform  $[10^{-18}, 10^{-9}]$ )

$$\Omega_{\text{GW}}(f) = \frac{1}{3H_0^2 m_{\text{Pl}}^2} \sum_{j=1}^{\infty} \underbrace{\frac{2j}{f} (G\mu^2 P_j)}_{\text{GW emission from single loops}} \int_{a_2}^{a_1} da \underbrace{\frac{1}{H(a)} \left(\frac{a}{a_0}\right)^4}_{\text{cosmic history}} \underbrace{\mathbf{n} \left[ \frac{2j}{f} \cdot \frac{a}{a_0}, t(a) \right]}_{\text{loop number density}}$$

# Conventional Signals: VOS & BOS

(analytical) (simulation)

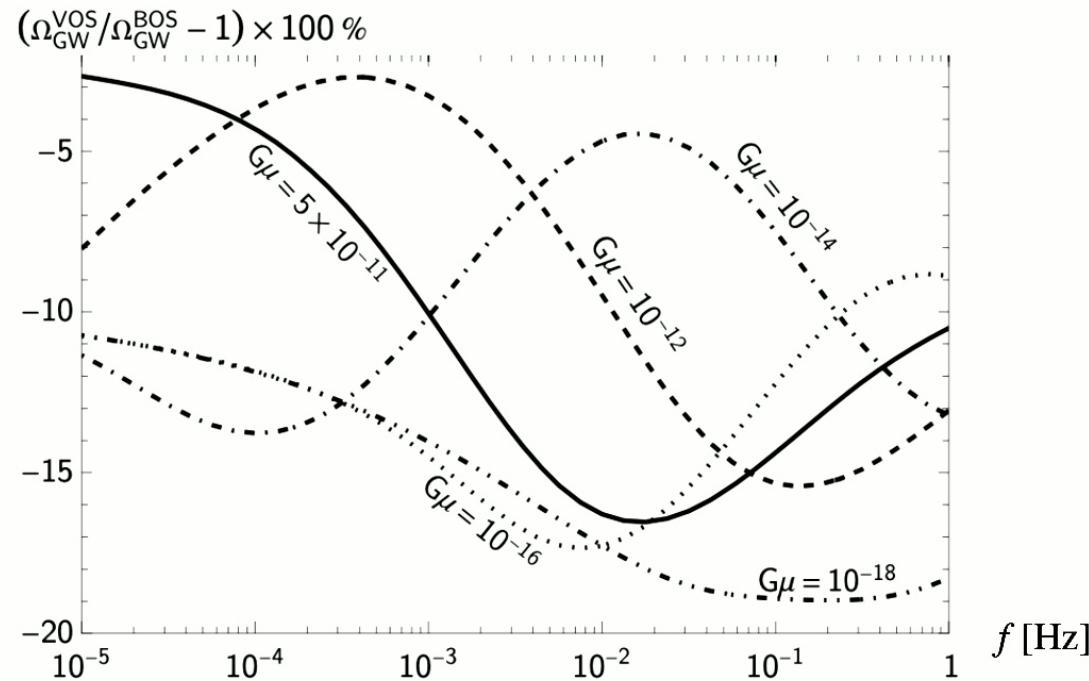
One-parameter templates:  $G\mu$



# Conventional Signals: VOS & BOS

(analytical) (simulation)

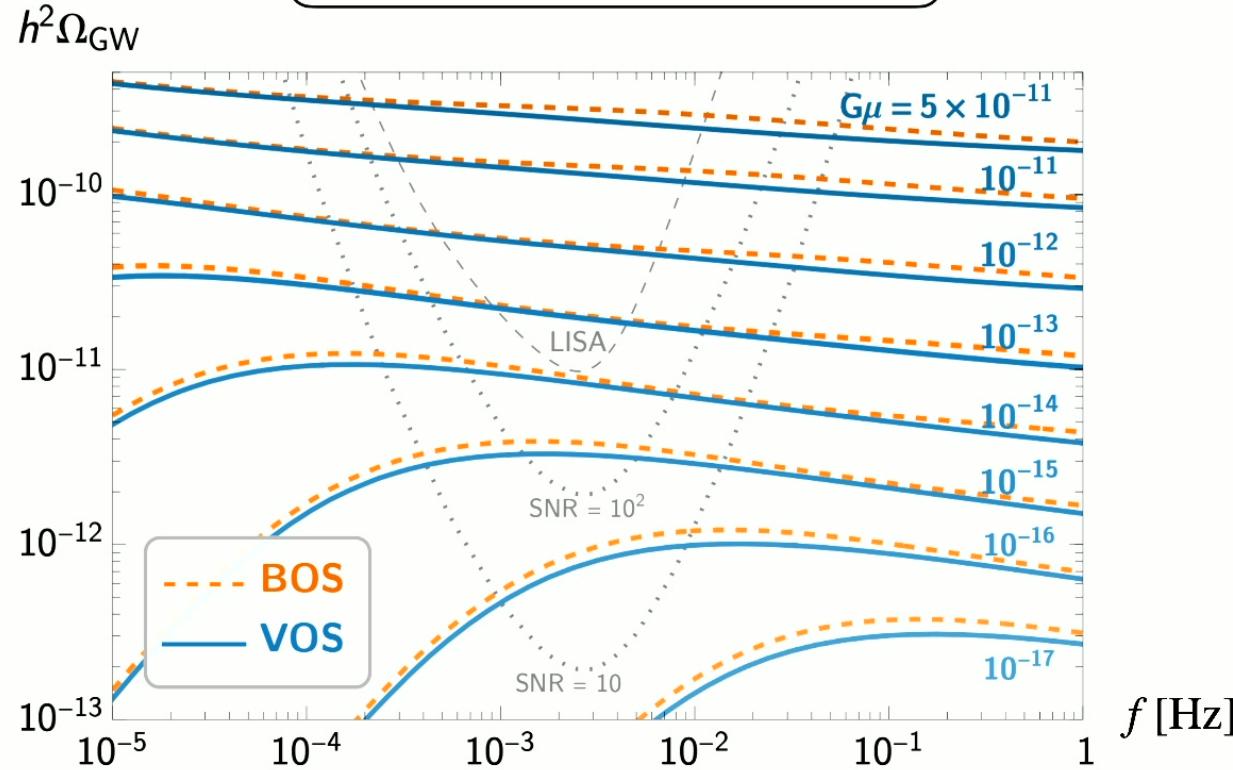
One-parameter templates:  $G\mu$



# Conventional Signals: VOS & BOS

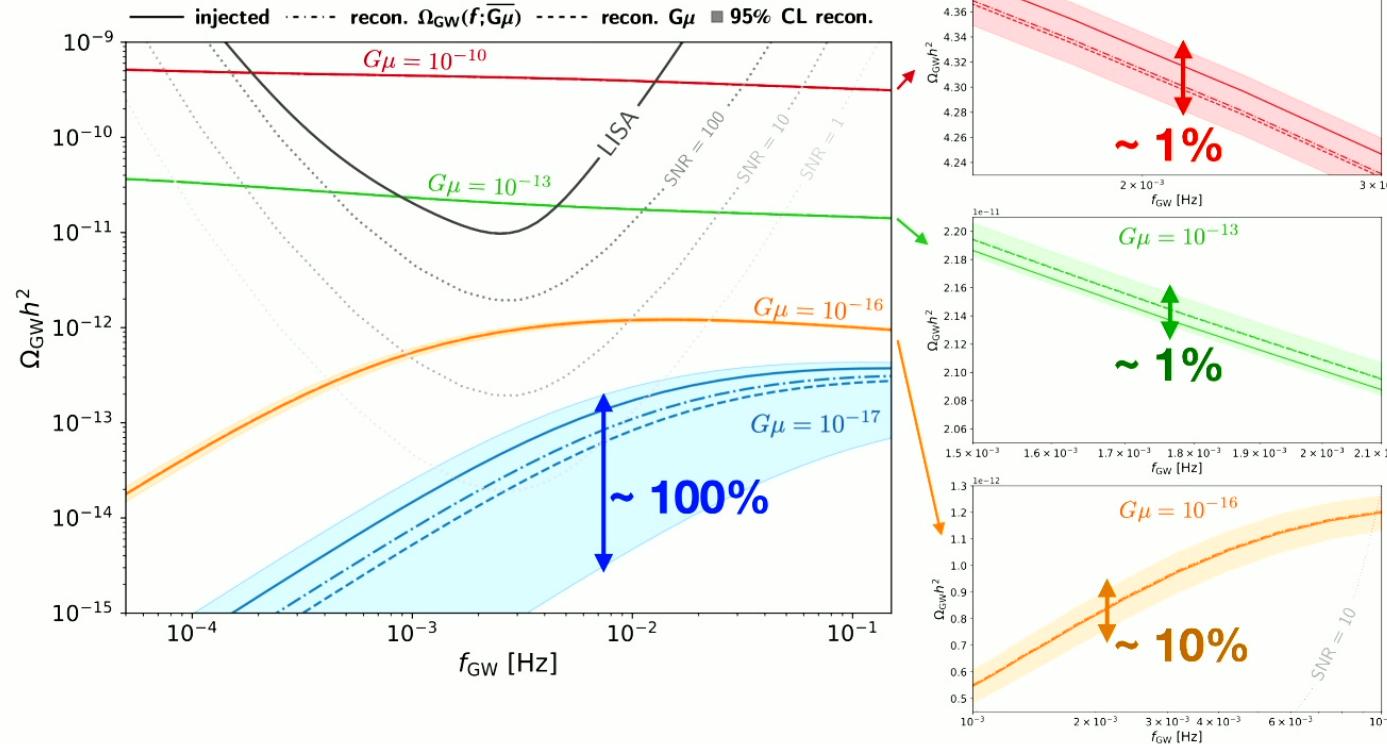
(analytical) (simulation)

One-parameter templates:  $G\mu$



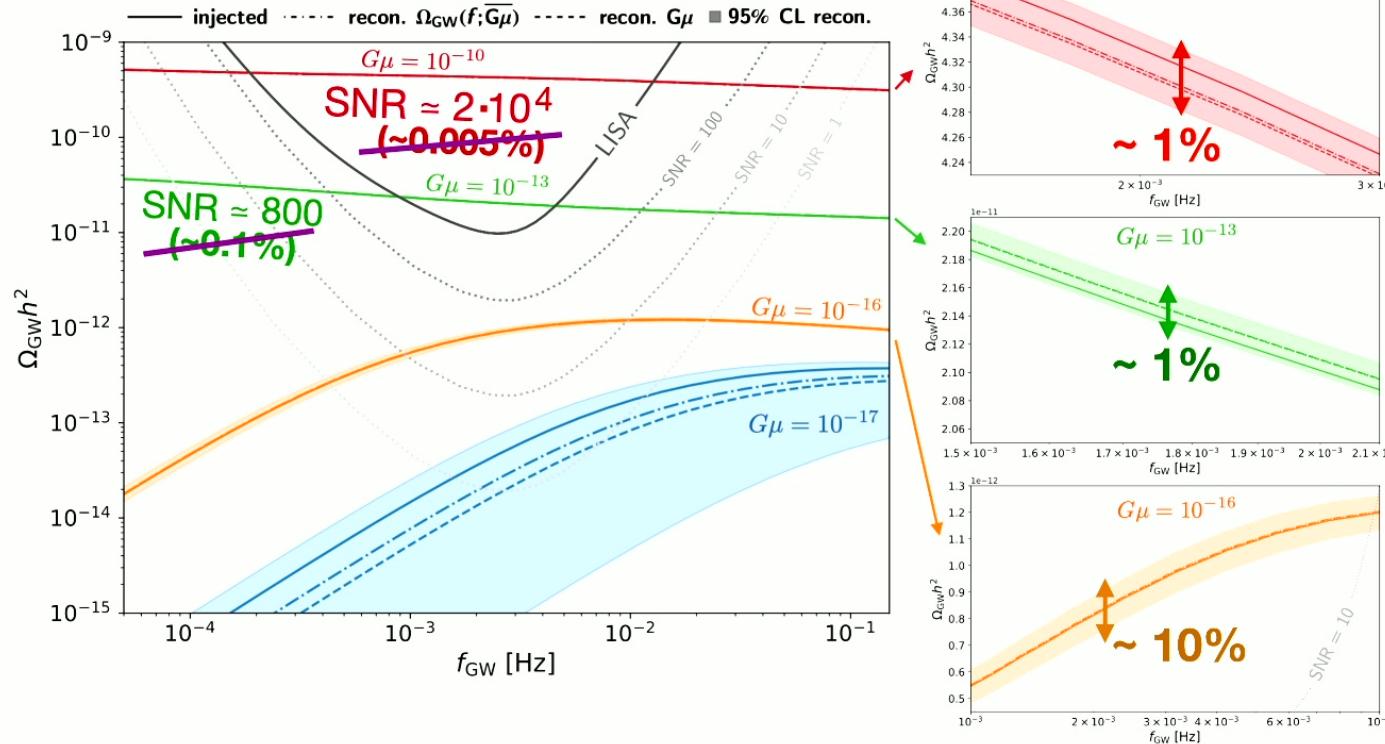
# Conventional Signal Reconstruction

(BOS: 1-parameter template  $\rightarrow G\mu$ )

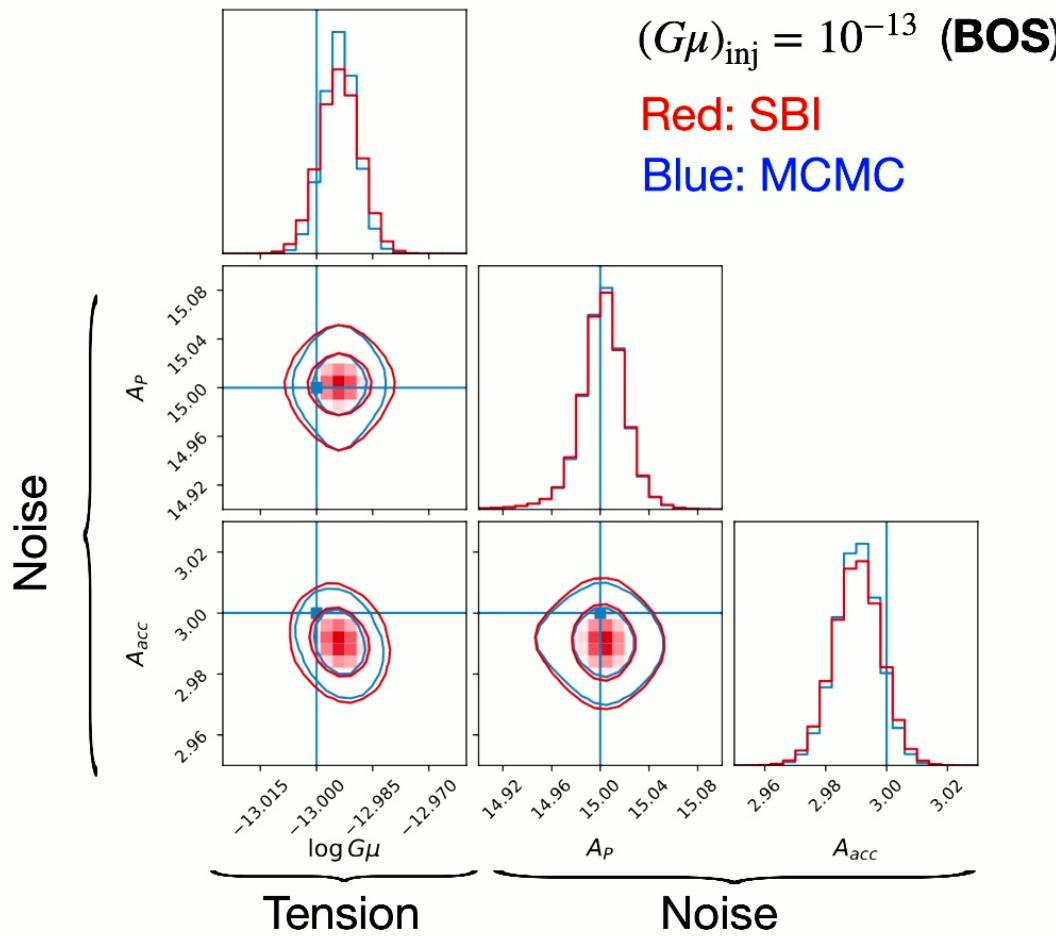


# Conventional Signal Reconstruction

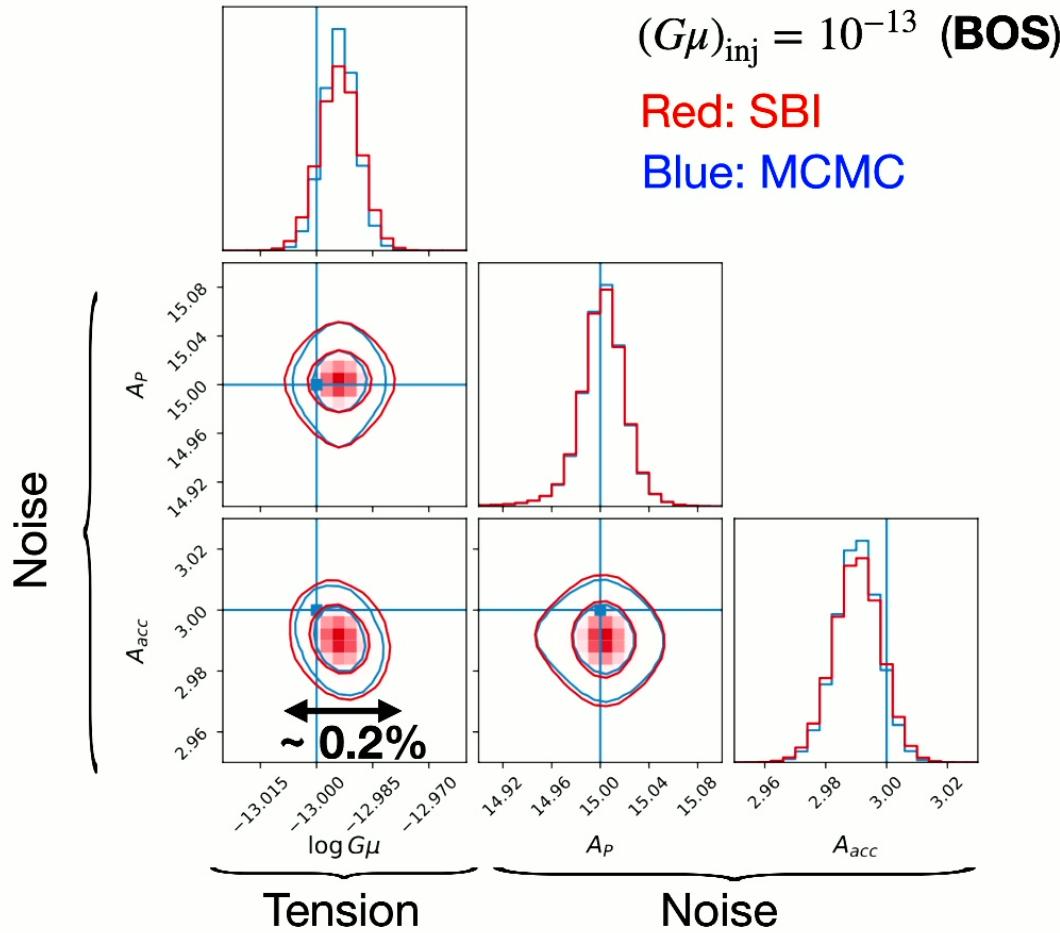
(BOS: 1-parameter template  $\rightarrow G\mu$ )



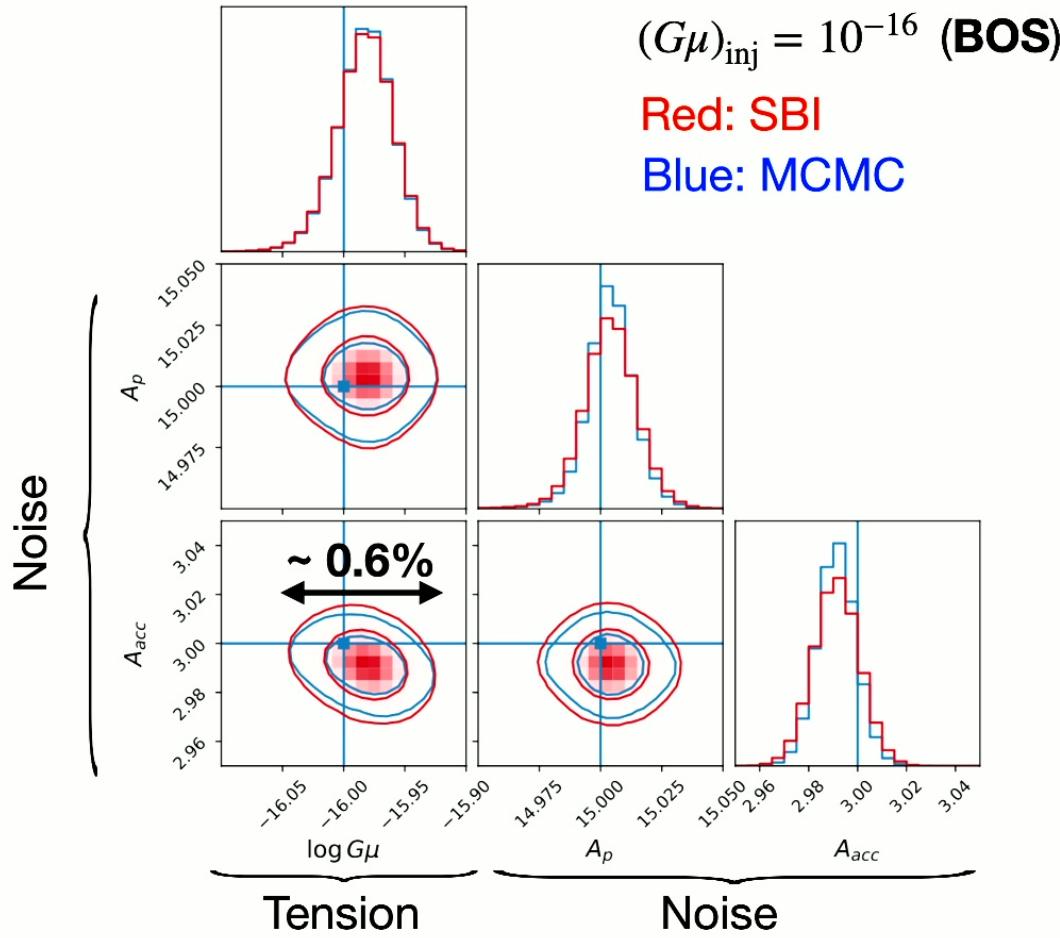
# Conventional Signal Reconstruction



# Conventional Signal Reconstruction

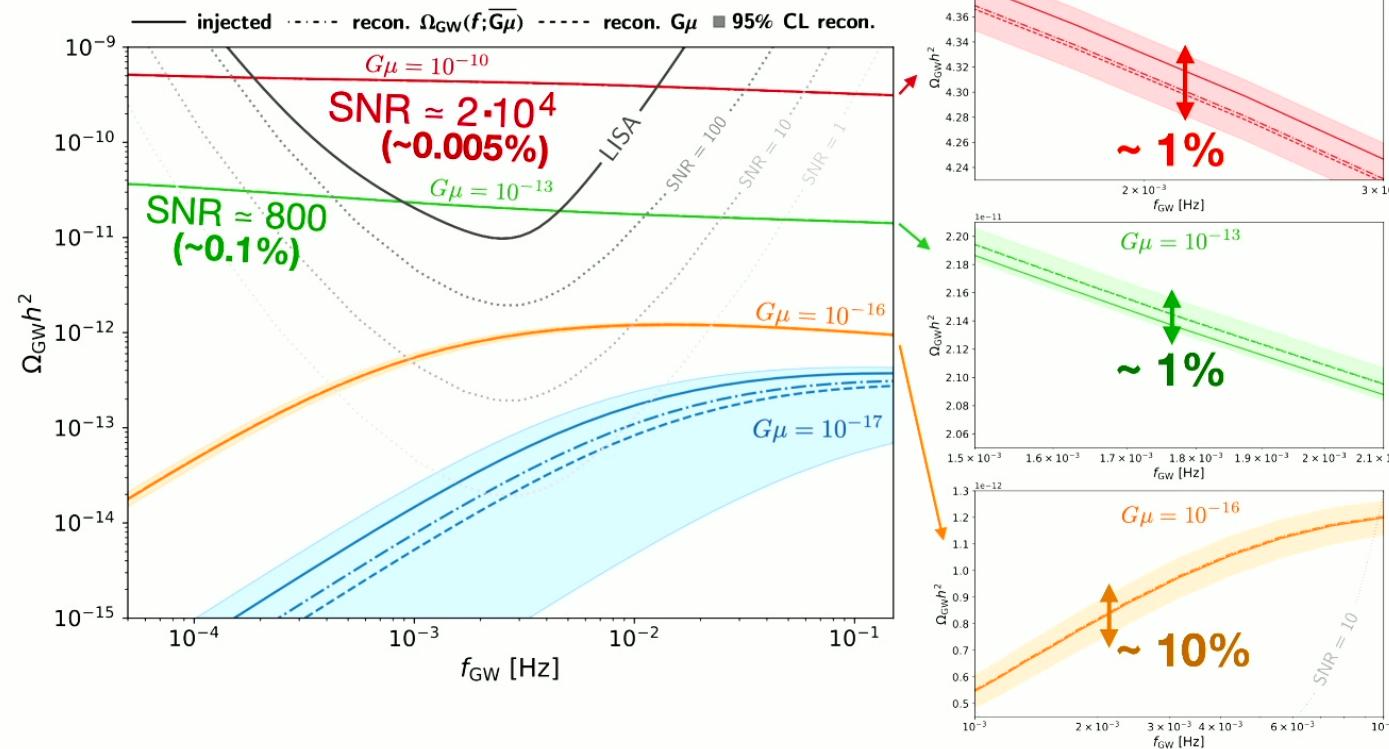


# Conventional Signal Reconstruction

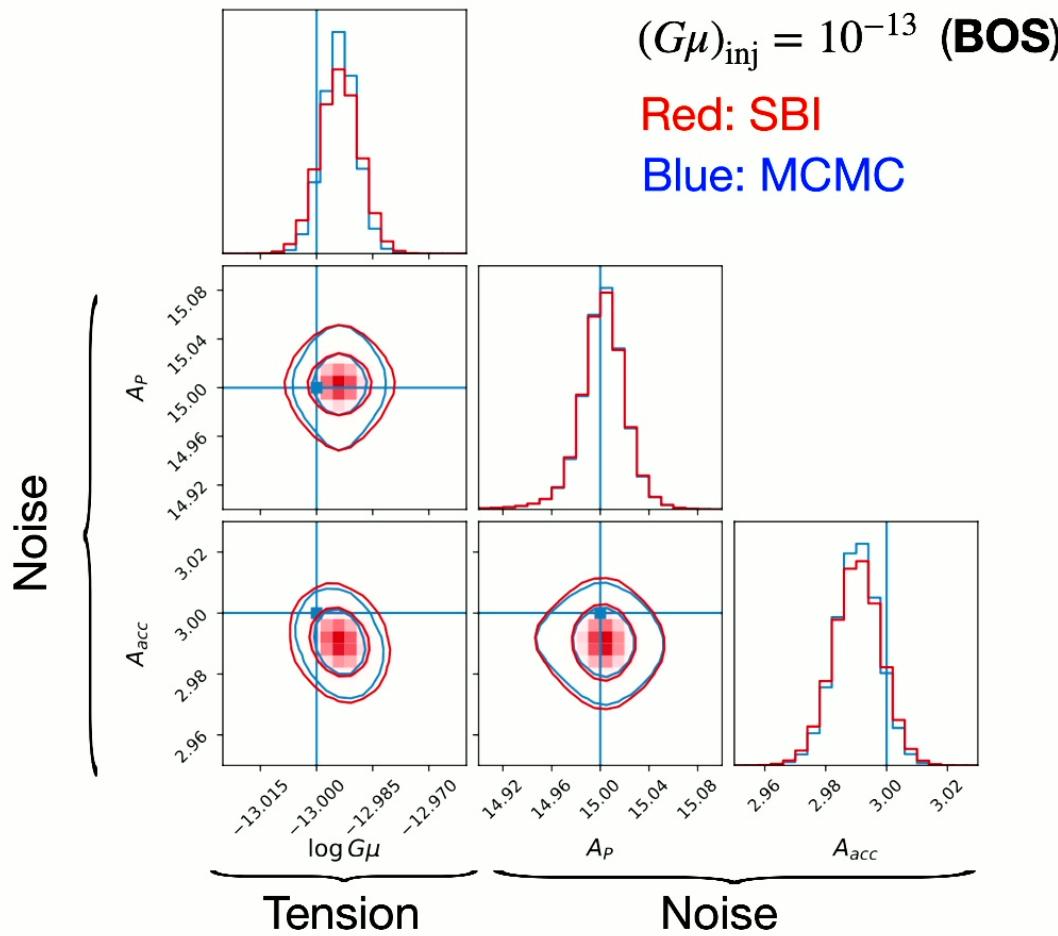


# Conventional Signal Reconstruction

(BOS: 1-parameter template  $\rightarrow G\mu$ )

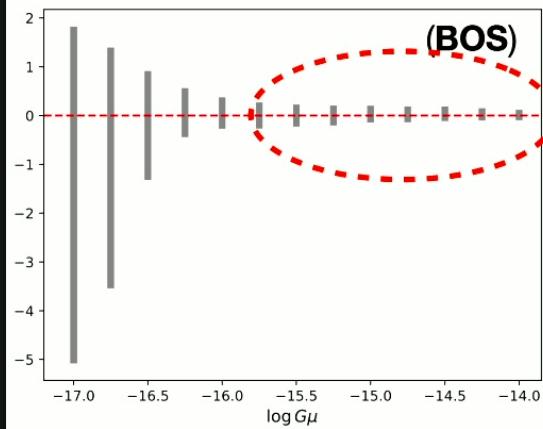


# Conventional Signal Reconstruction



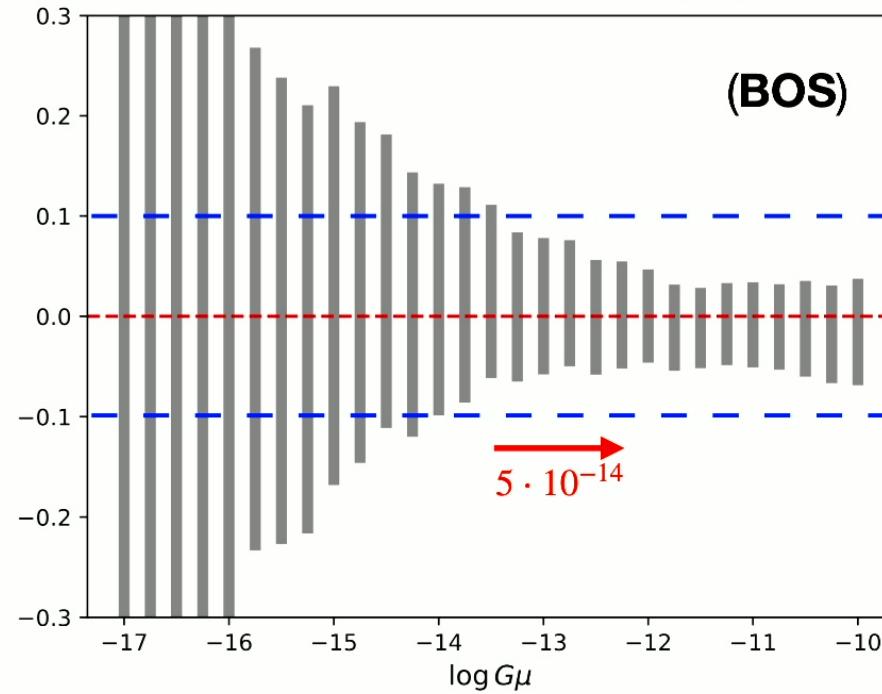
# Conventional Signal Reconstruction

% Relative Error:  $\Delta(\log G\mu)$

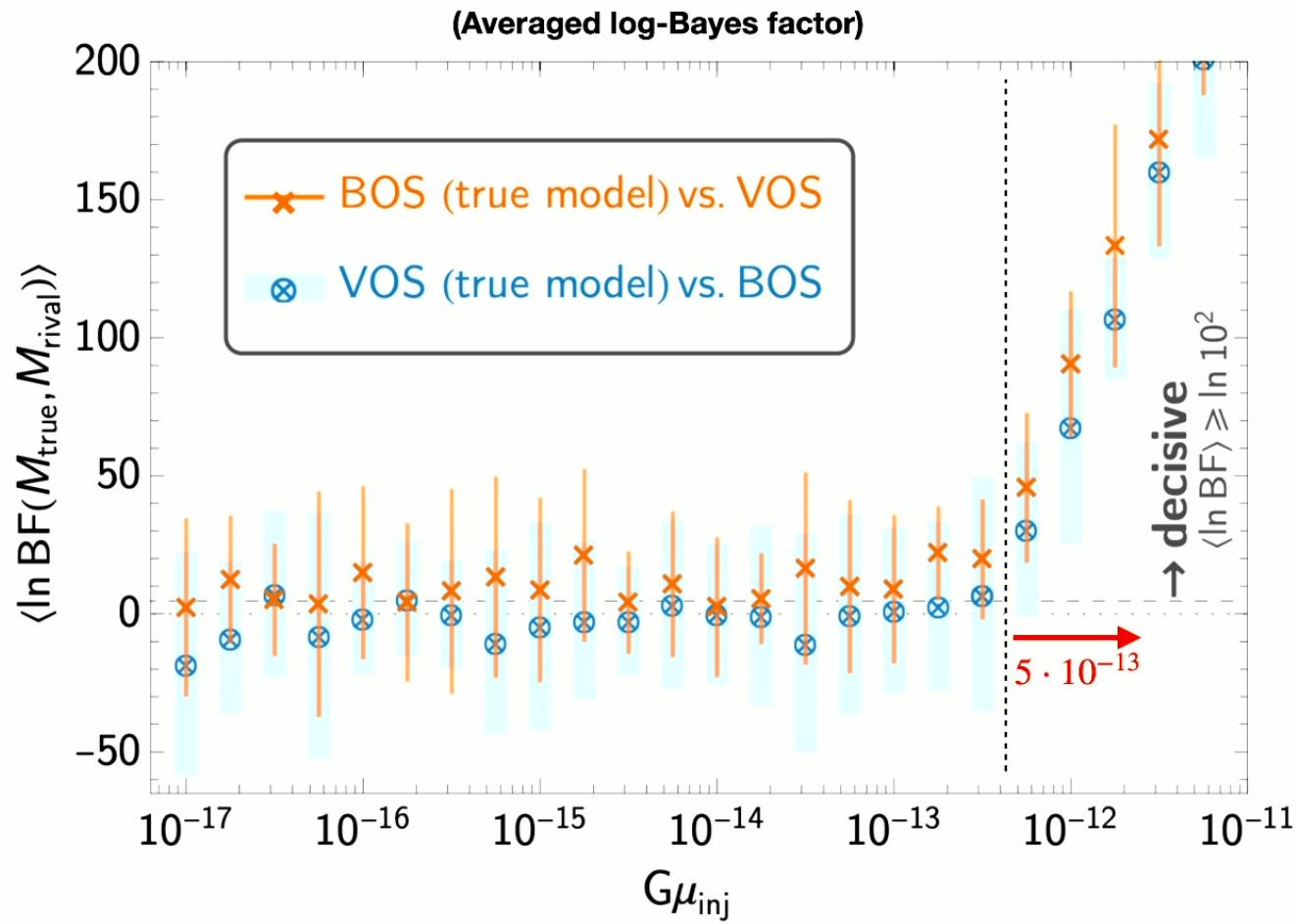


ZOOM-IN

% Relative Error:  $\Delta(\log G\mu)$

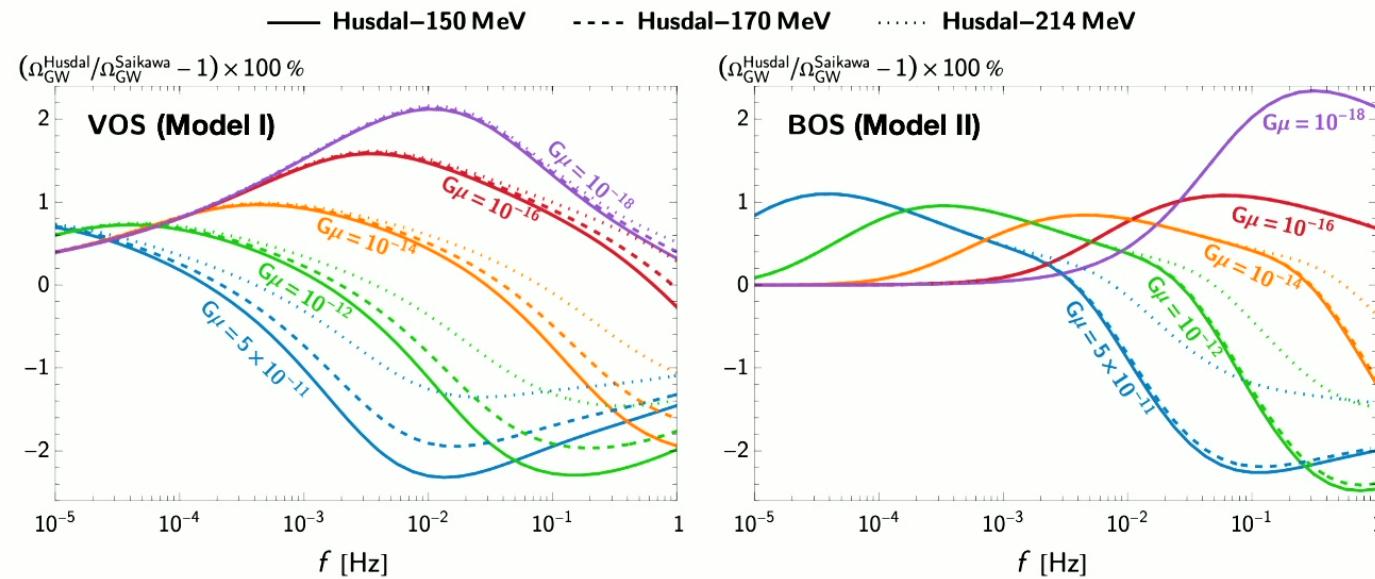


# Model Comparison: BOS vs VOS



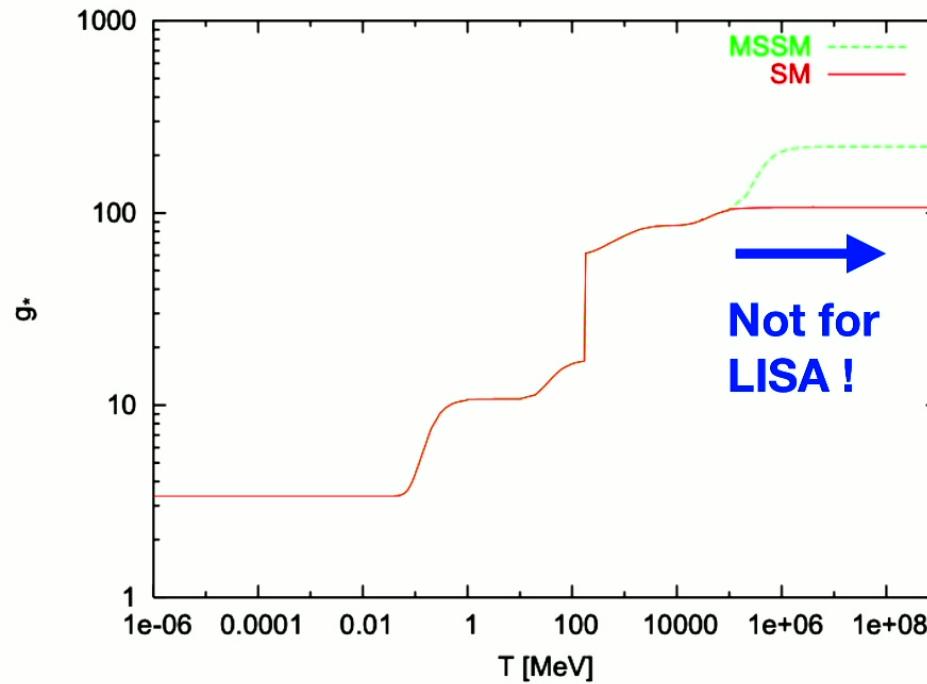
# Model Comparison: *dof* evolution

$$\Omega_{\text{GW}}(f) = \frac{1}{3H_0^2 m_{\text{Pl}}^2} \sum_{j=1}^{\infty} \underbrace{\frac{2j}{f} (G\mu^2 P_j)}_{\text{GW emission from single loops}} \int_{a_2}^{a_1} da \underbrace{\frac{1}{H(a)} \left(\frac{a}{a_0}\right)^4}_{\text{cosmic history}} \underbrace{n\left[\frac{2j}{f} \cdot \frac{a}{a_0}, t(a)\right]}_{\text{loop number density}}$$



# Model Comparison: *dof* evolution

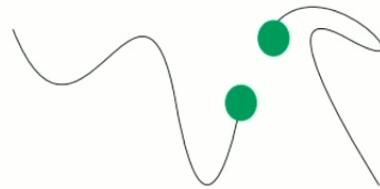
But opens  to BSM !



# Beyond Conventional Signals: Detectability

## (A) MetaStable Cosmic Strings

(Domcke et al  
2020-2023)



Grand Unified Theories: Symm. Breaking @ multiple steps  
(monopoles & strings)

Monopole-antimonopole pair nucleates → cuts loops → segments

Nucleation rate

$$\Gamma_d = \frac{\mu}{2\pi} e^{-\pi\kappa}, \text{ with } \kappa \equiv \left( \frac{m_M}{\eta} \right)^2.$$

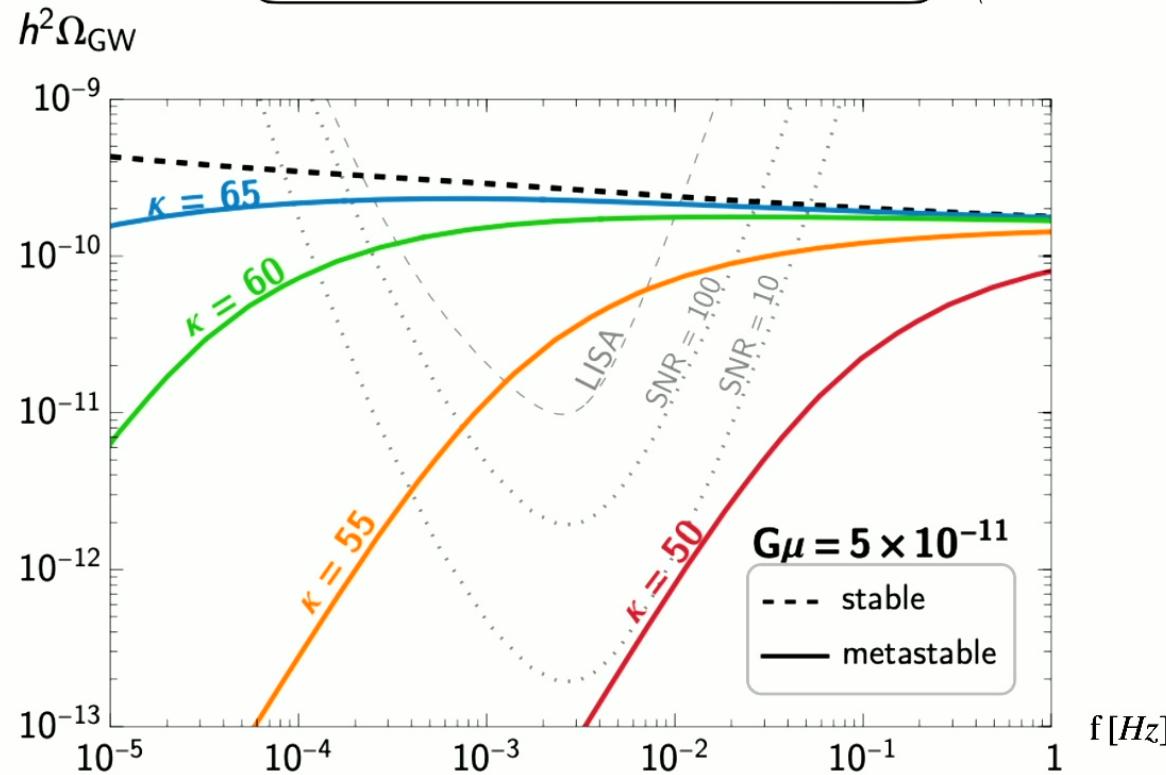
monopole formation scale

String formation scale

# Beyond Conventional Signals: Detectability

## (A) MetaStable Cosmic Strings

Two-parameter template:  $G\mu, \kappa$   $\begin{pmatrix} G\mu: \text{Log-uniform } [10^{-18}, 10^{-9}] \\ \kappa: \text{Uniform } [40, 80] \end{pmatrix}$

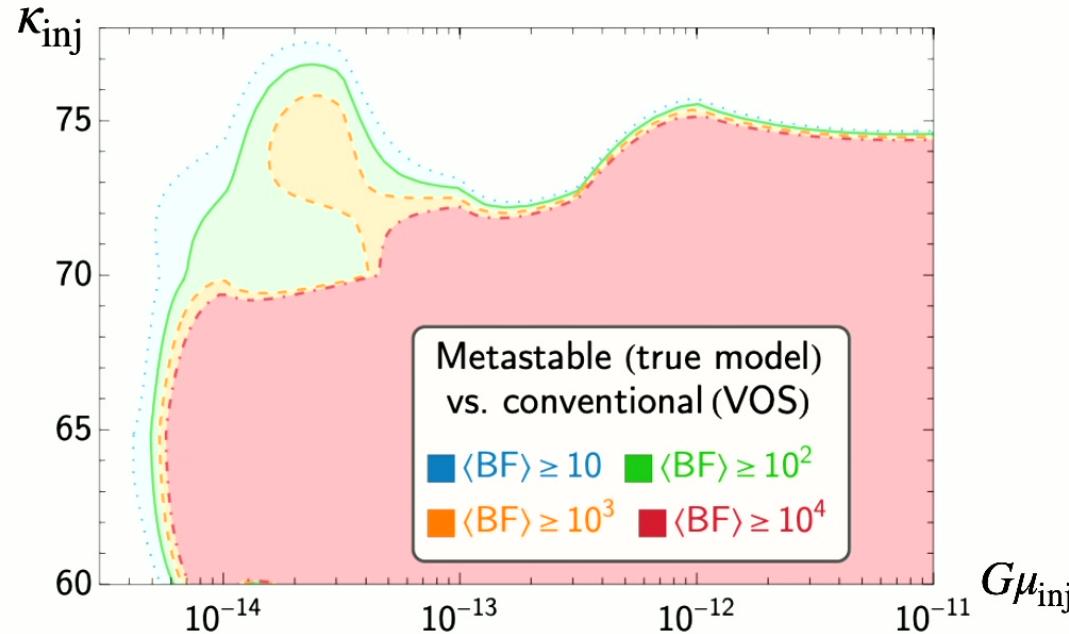


# Beyond Conventional Signals: Detectability

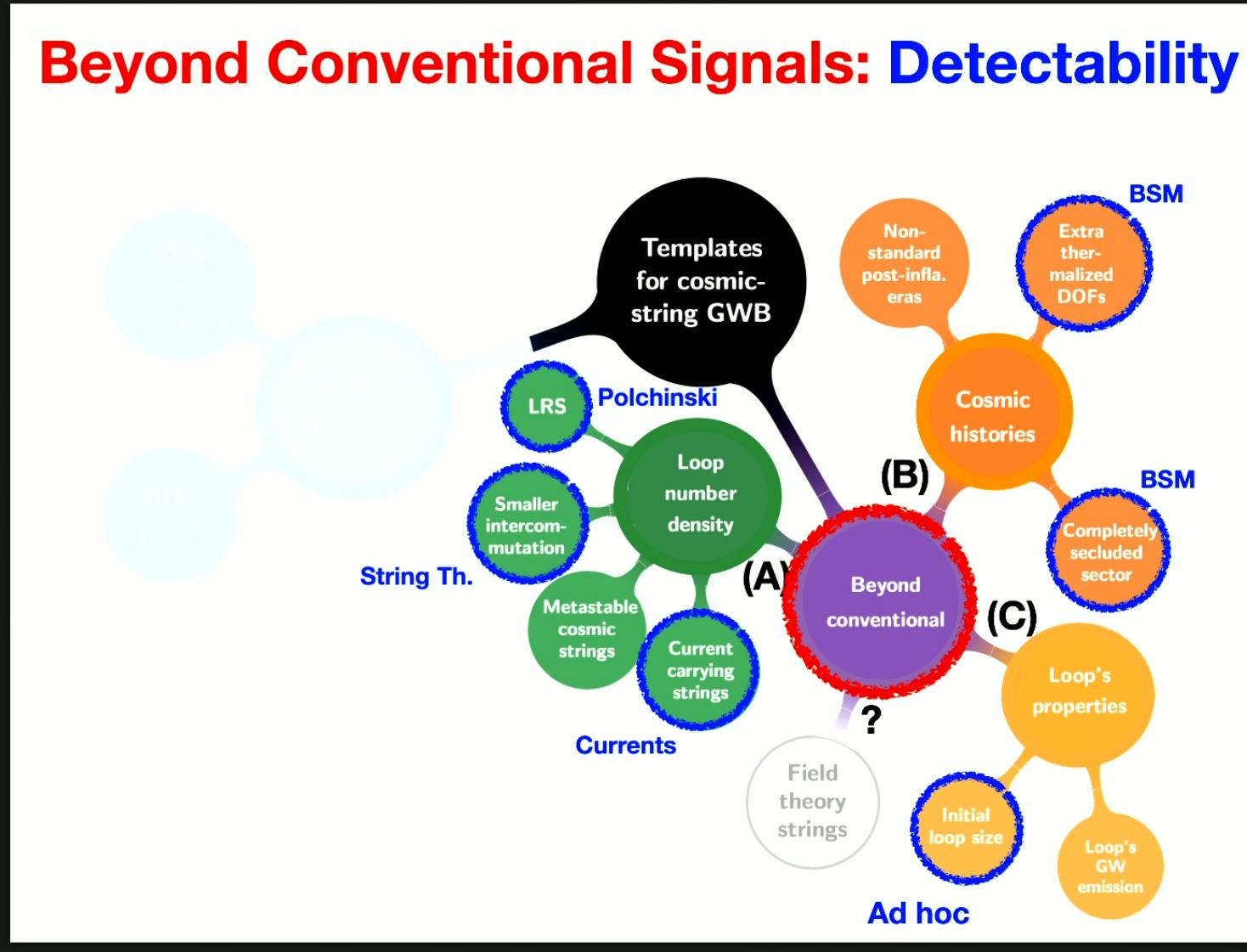
## (A) MetaStable Cosmic Strings

Two-parameter template:  $G\mu, \kappa$   $\begin{cases} G\mu: \text{Log-uniform } [10^{-18}, 10^{-9}] \\ \kappa: \text{Uniform } [40, 80] \end{cases}$

### Model comparison: conventional vs meta-stable



# Beyond Conventional Signals: Detectability

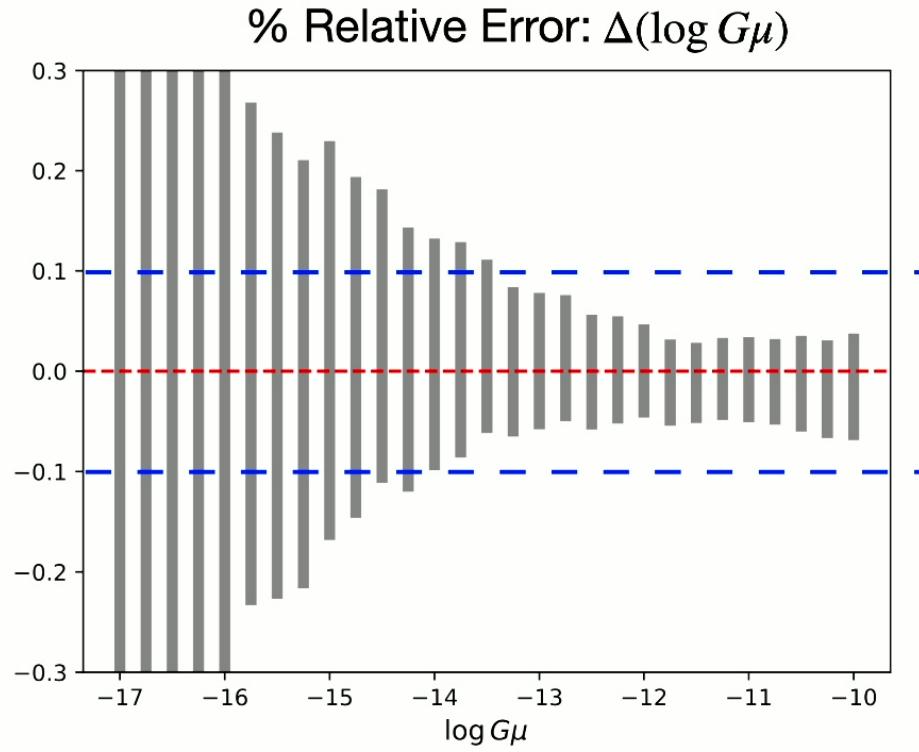


# GW Background Signals: Detectability (over foregrounds)

Which  
foregrounds ?

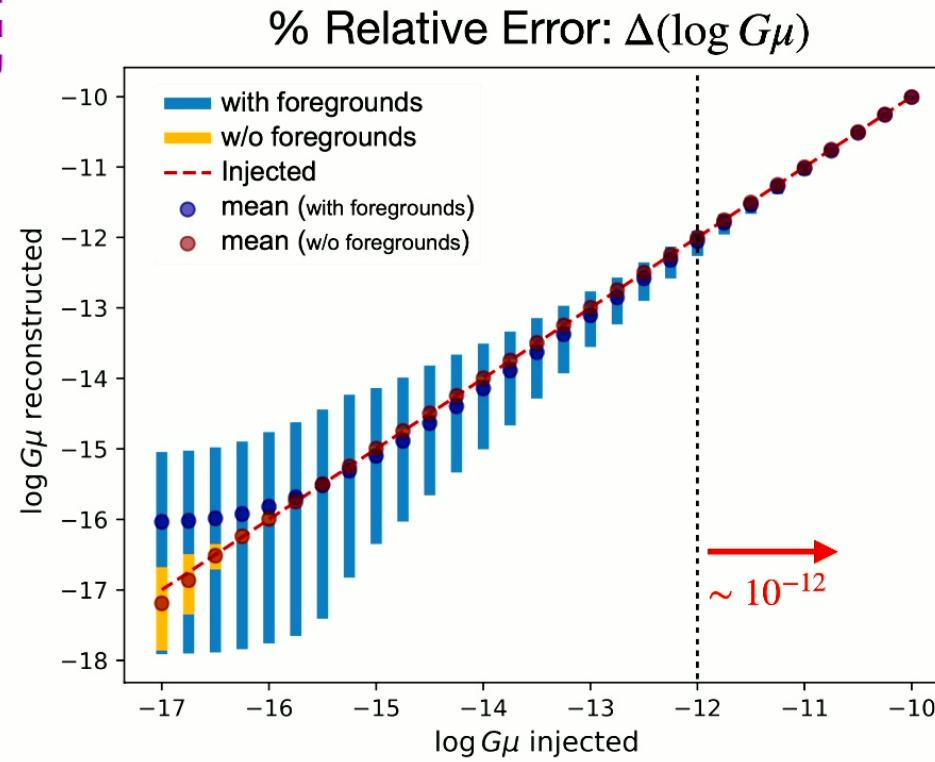
# GW Background Signals: Detectability (over foregrounds)

If you remember:  
**No foregrounds**

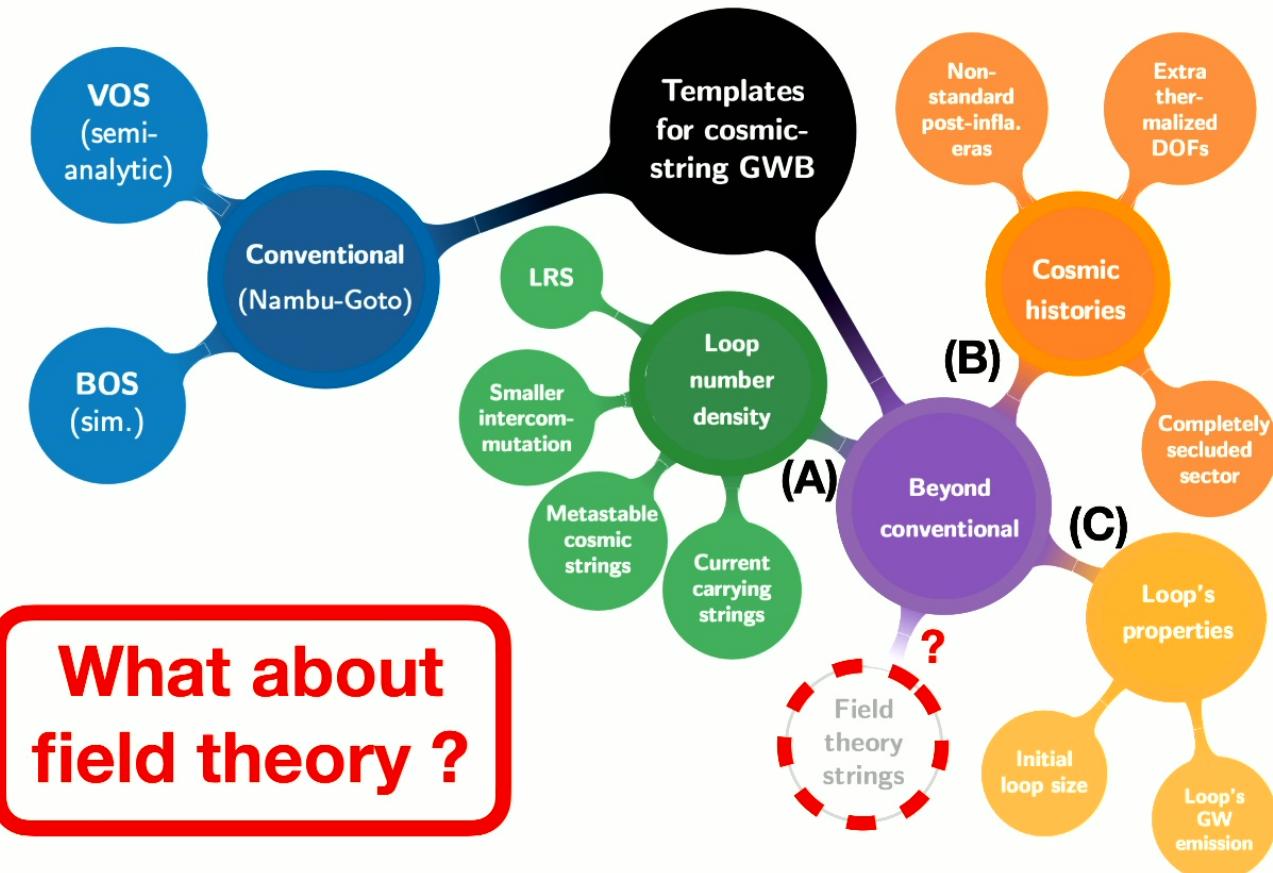


# GW Background Signals: Detectability (over foregrounds)

With/without  
foregrounds

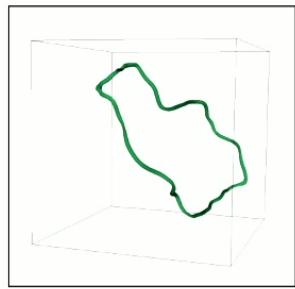


# GW Background Signals: Detectability

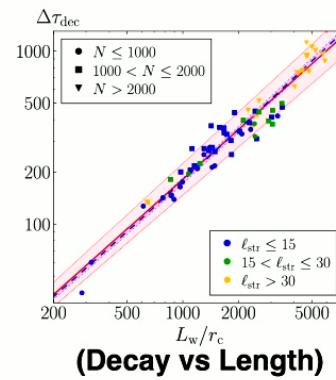


# String Loop Dynamics + GW emission

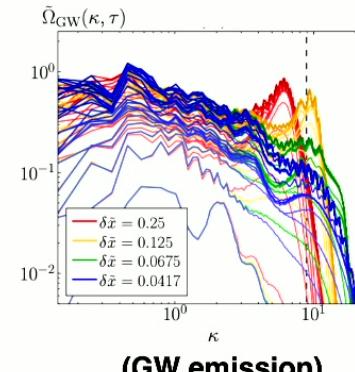
## GWs & Particles Emitted



(Loops isolated)



(Decay vs Length)



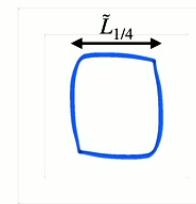
(GW emission)

Baeza-Ballesteros et al, 2024

**(Local Strings)**

[  $L/w \simeq 200 - 6000$  ]

If loops Artificial (w/ Kinks)



# String Loop Dynamics + GW emission

## GWs & Particles Emitted

This will open PTA bounds to GUT scales !

(Local Strings)

GW

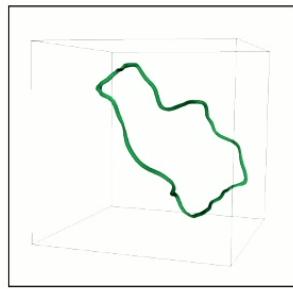
GWs from element production

<< 1

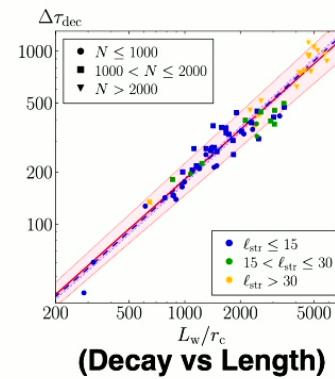
Essentially GW suppressed: no constraints on GUT scales

# String Loop Dynamics + GW emission

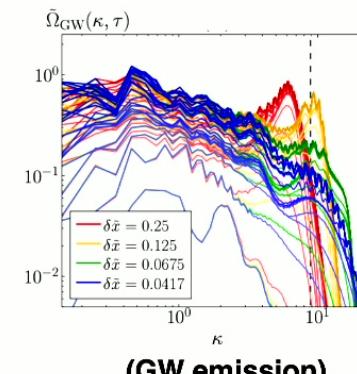
## GWs & Particles Emitted



(Loops isolated)



(Decay vs Length)



(GW emission)

Baeza-Ballesteros et al, 2024

**(Local Strings)**

[  $L/w \simeq 200 - 6000$  ]

If loops Artificial (w/ Kinks)

Critical  
Length  $L_c$

(Vachaspati  
et al 2019)

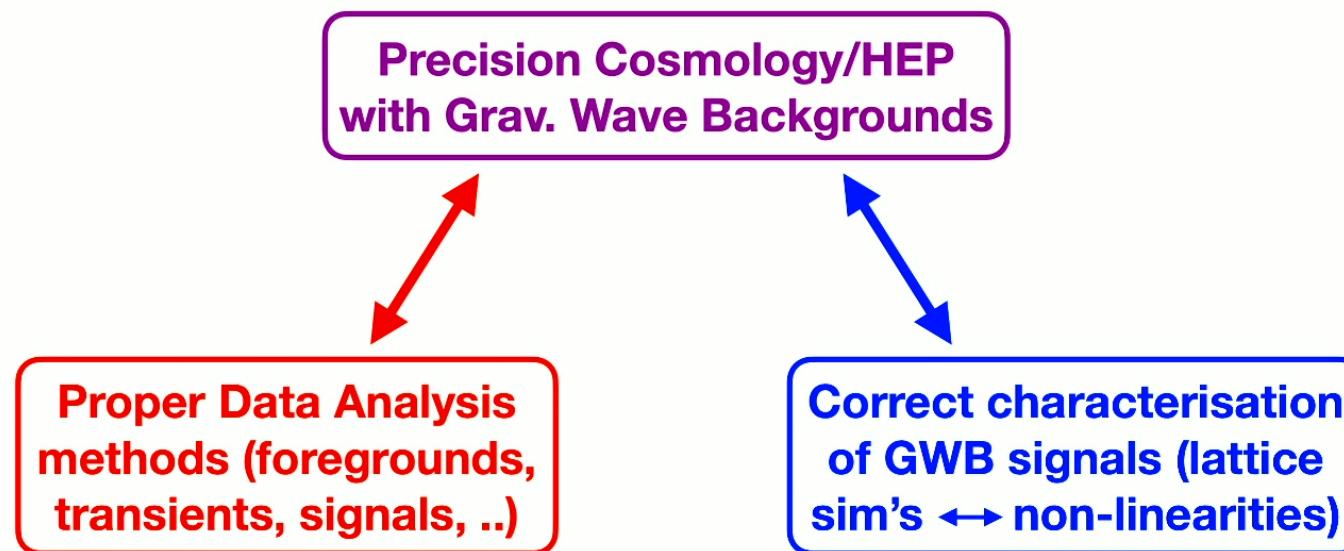
If  $L \gg L_c : \frac{P_{\text{GW}}}{P_\phi} \gg 1$

(In agreement with NG)

# A message before we conclude ...

Precision Cosmology/HEP  
with Grav. Wave Backgrounds

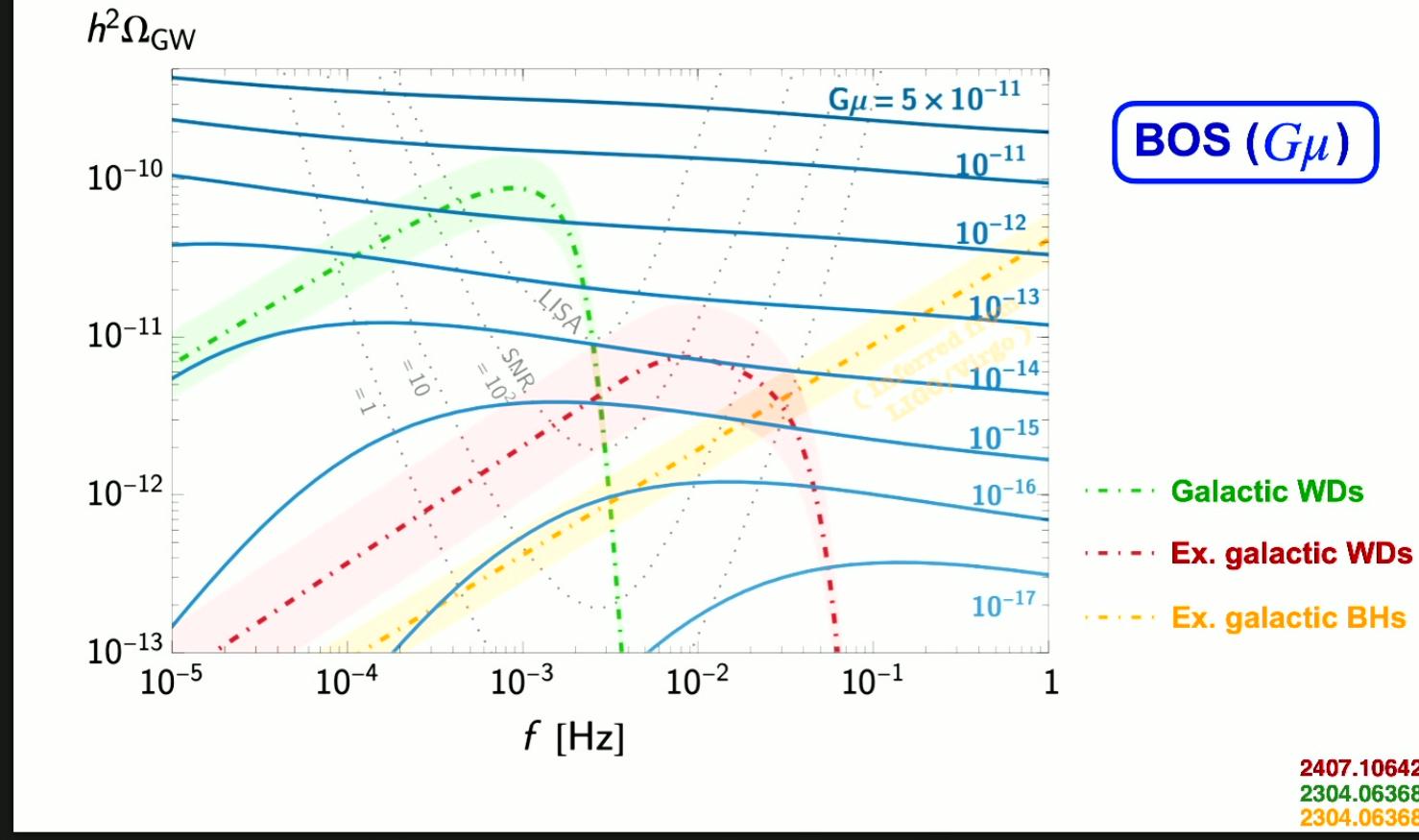
# A message before we conclude ...



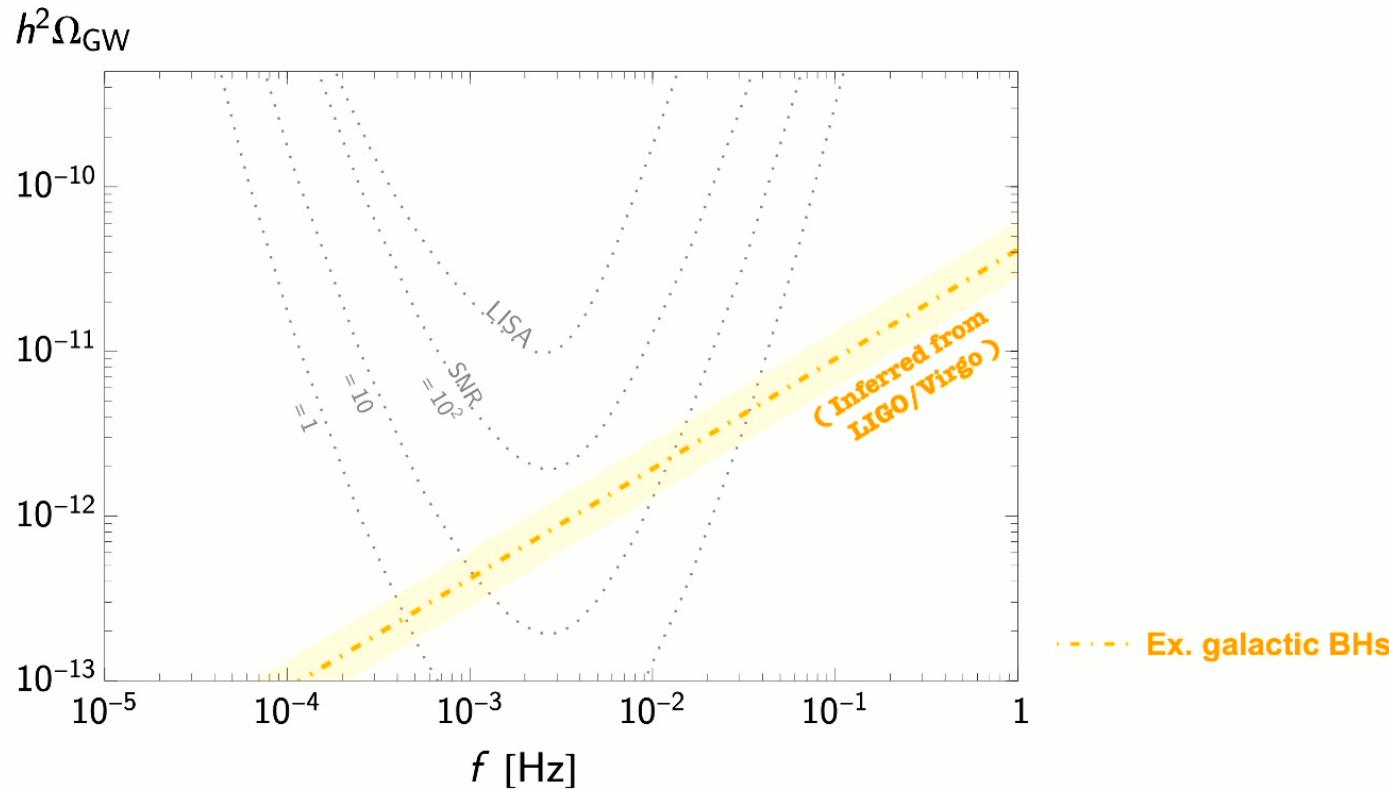
**Thanks for your attention**

**Merci pour votre attention**

# GW Background Signals: Detectability (over foregrounds)

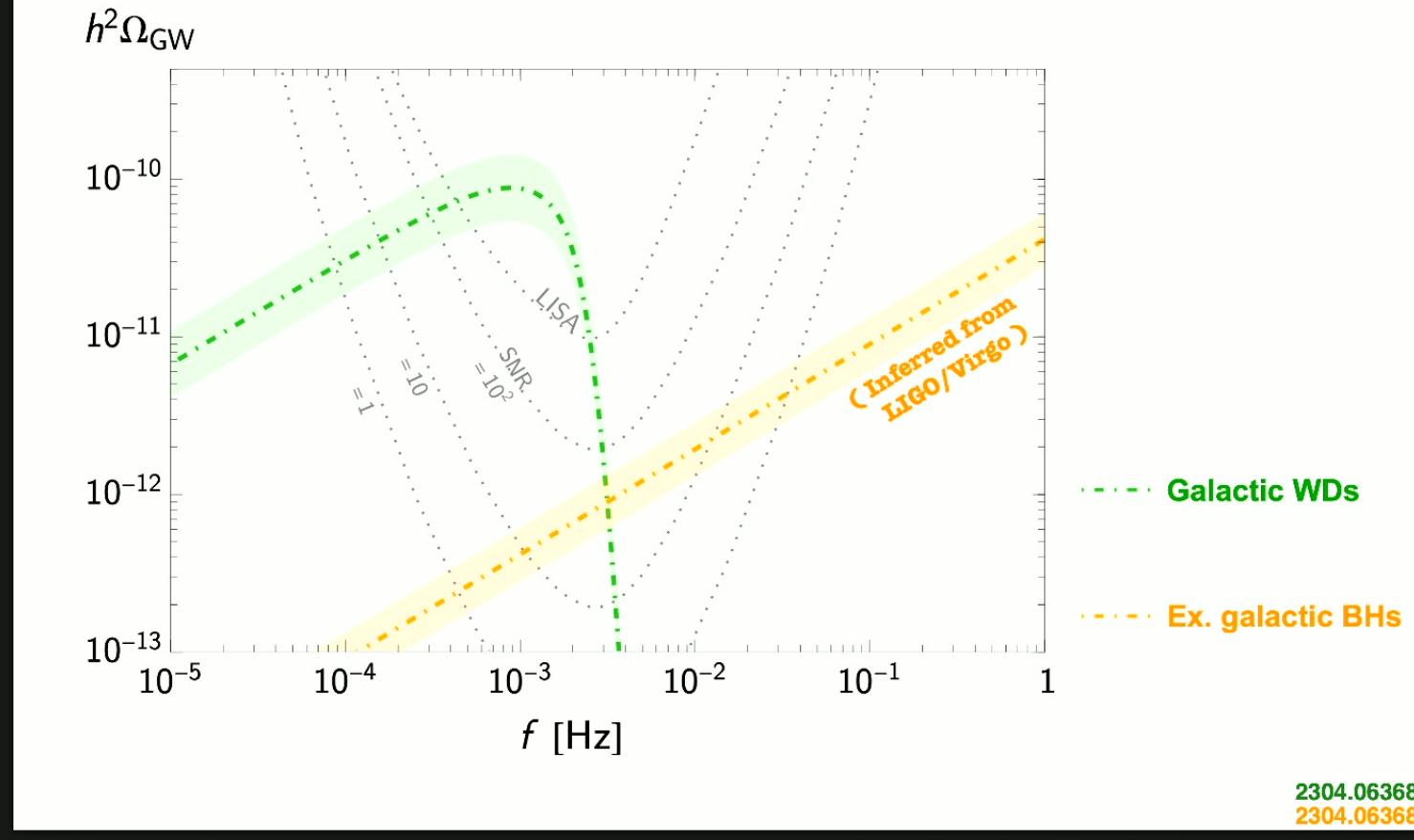


# GW Background Signals: Detectability (over foregrounds)



2304.06368

# GW Background Signals: Detectability (over foregrounds)



# GW Background Signals: Detectability (over foregrounds)

