

**Title:** Magnetic Field Evolution and Superconductivity of Pulsars

**Speakers:** Ashley Bransgrove

**Collection/Series:** Magnetic Fields Around Compact Objects Workshop

**Subject:** Strong Gravity

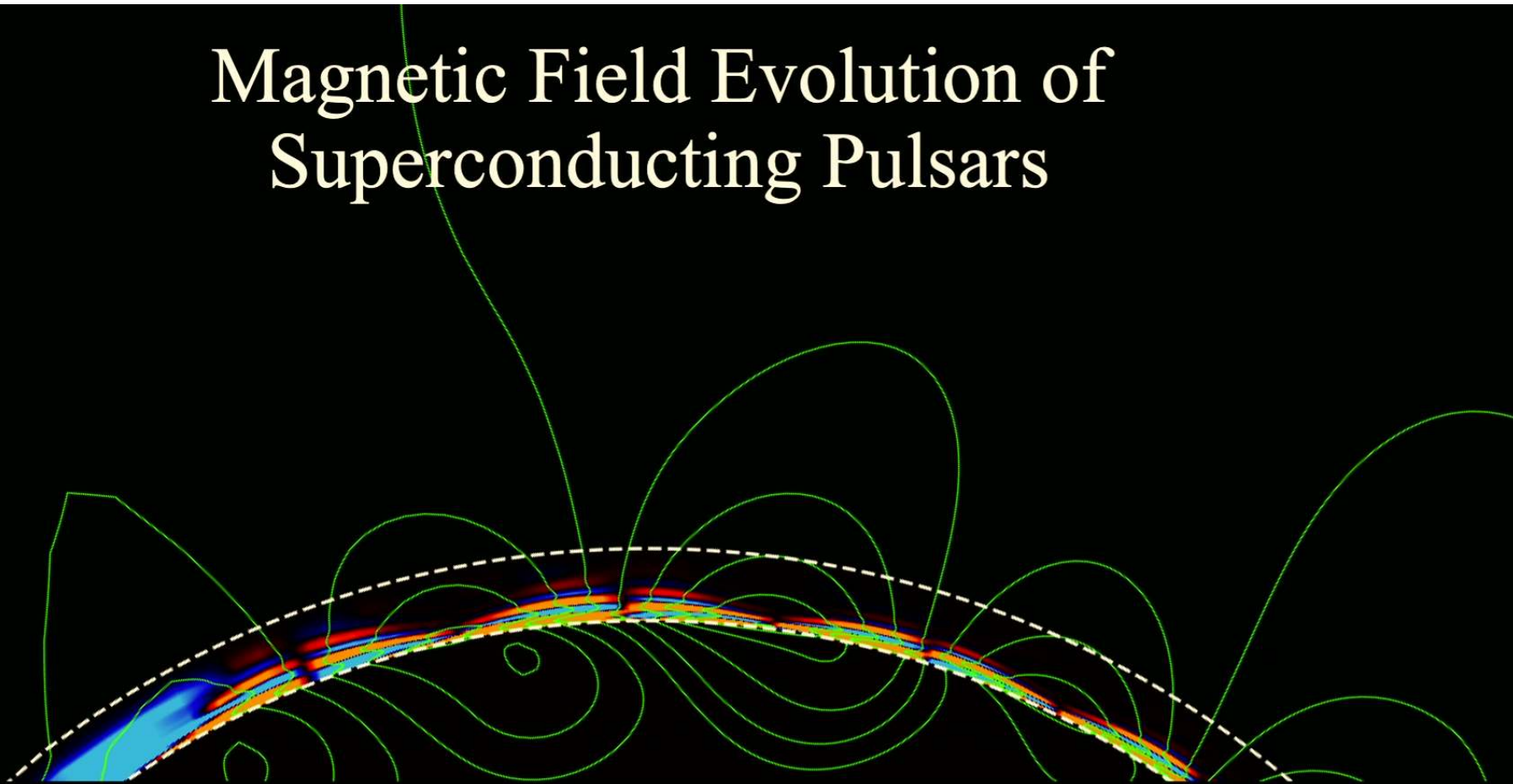
**Date:** March 28, 2025 - 10:15 AM

**URL:** <https://pirsa.org/25030148>

**Abstract:**

Radio pulsars display a range of puzzling long-term variability in their magnetospheric emission and spin-down. In this talk I will discuss the mechanisms for internal magnetic field evolution of pulsars, how it differs from the MHD of classical conducting fluids, and how the neutron star interior couples to the magnetosphere and its radiation.

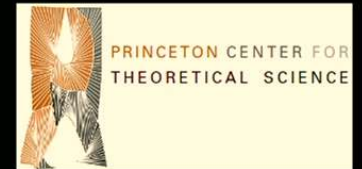
# Magnetic Field Evolution of Superconducting Pulsars

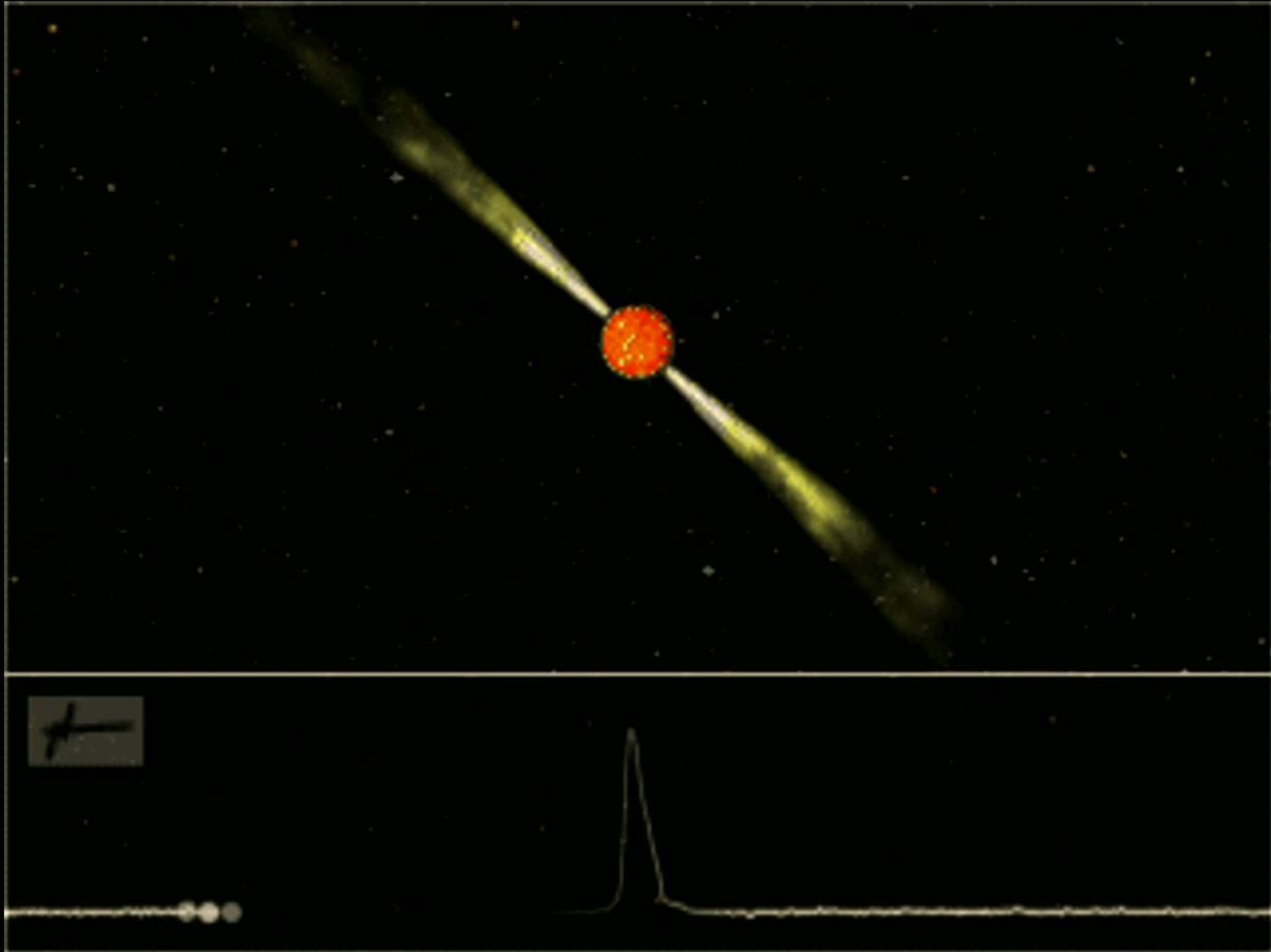


Ashley Bransgrove

Princeton University, PCTS

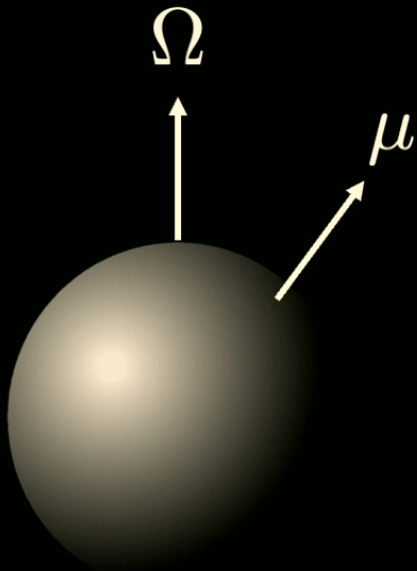
Thanks to Yuri Levin and Andrei Beloborodov





Joeri van Leeuwen, [www.ligo.org/science/](http://www.ligo.org/science/)

# Pulsar Spin-down



$$\dot{\Omega} = -k\Omega^n$$

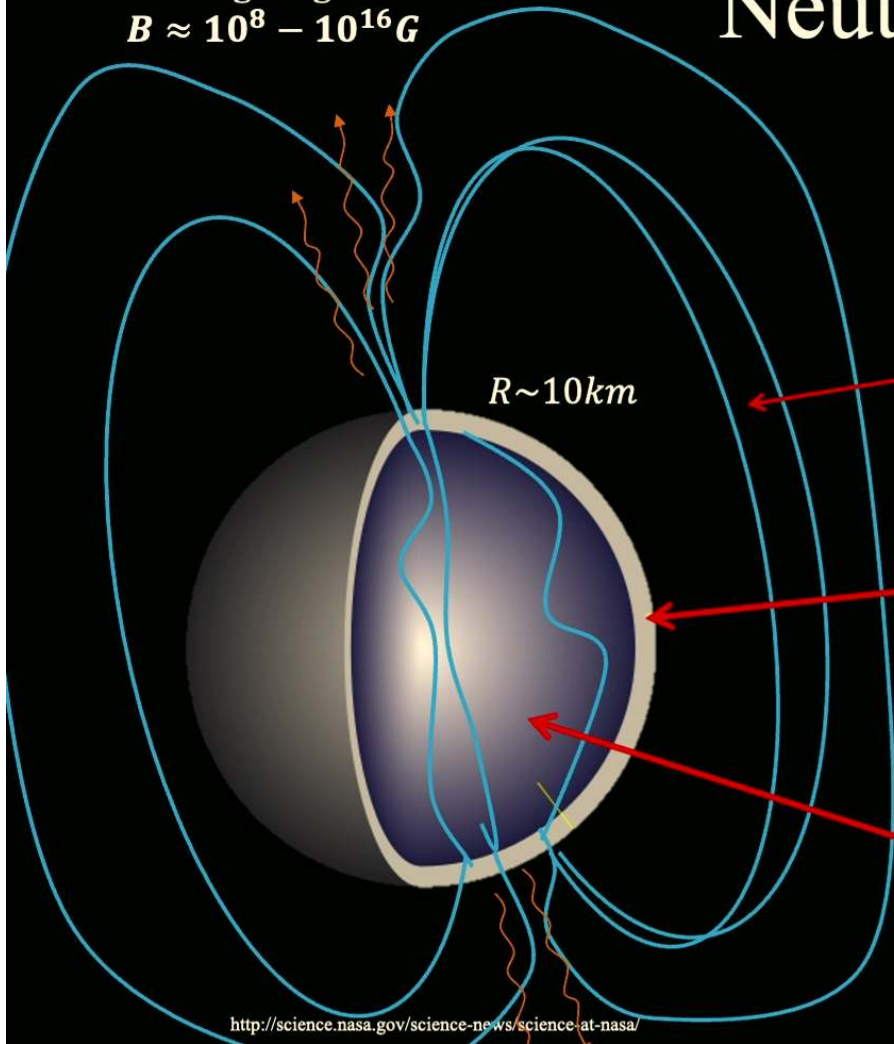
$$k = \frac{\mu^2 \Omega^4}{Ic^3}, \quad n = 3$$

Vacuum rotator: Pacini 68, Ostriker & Gunn 69  
Force-free rotator: Goldreich & Julian 69, Spitkovsky 06  
+ many more

Ultra-strong magnetic fields  
 $B \approx 10^8 - 10^{16} \text{ G}$

# Neutron Stars: Physics Playground

*~ solar mass of baryons supported against gravitational collapse by strong nuclear forces, threaded by the strongest magnetic fields in the universe*  
 $B \approx 10^8 - 10^{16} \text{ G}$



Magnetosphere:  $e^\pm$  pair plasma

Solid crust, highly conducting

Liquid core – nuclear soup,  
superconducting protons,  
superfluid neutrons

<http://science.nasa.gov/science-news/science-at-nasa/>

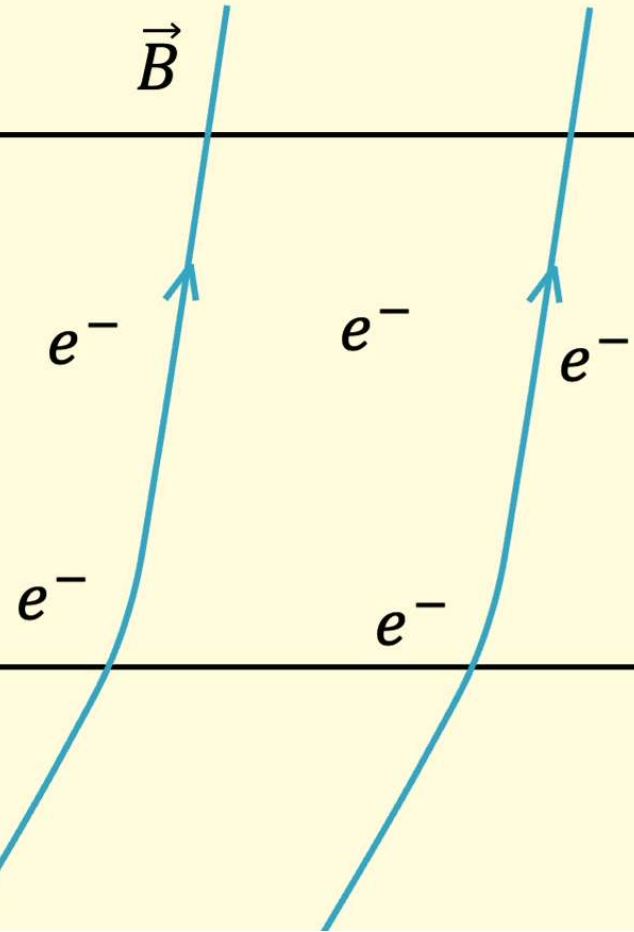
# Internal Magnetic Evolution of Pulsars

Magnetosphere

$\vec{B}$

Hall Magneto-Elastic Dynamics

Solid crust



$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v}_e \times \mathbf{B}) - \nabla \times (\eta \nabla \times \mathbf{B})$$

$$\mathbf{v}_e = - \underbrace{\frac{c}{4\pi n_e e} \nabla \times \mathbf{B}}_{\text{Hall}} + \underbrace{\dot{\xi}}_{\text{Elasticity}}$$

Hall

Elasticity

Liquid core

# Internal Magnetic Evolution of Pulsars

Magnetosphere

$\vec{B}$

Hall Magneto-Elastic Dynamics

Solid crust

$e^-$

$e^-$

$e^-$

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v}_e \times \mathbf{B}) - \nabla \times (\eta \nabla \times \mathbf{B})$$

$$\mathbf{v}_e = - \underbrace{\frac{c}{4\pi n_e e} \nabla \times \mathbf{B}}_{\text{Hall}} + \underbrace{\dot{\boldsymbol{\xi}}}_{\text{Elasticity}}$$

$$0 = (\nabla \mu \cdot \nabla) \boldsymbol{\xi} - (\boldsymbol{\xi} \cdot \nabla) \nabla \mu + \mu \nabla^2 \boldsymbol{\xi} + \frac{\mathbf{j} \times \mathbf{B}}{c}$$

Magneto-elastic equilibrium

$e^-$

$e^-$

Liquid core

# Internal Magnetic Evolution of Pulsars

Magnetosphere

$\vec{B}$

Hall Magneto-Elastic Dynamics

Solid crust

$e^-$

$e^-$

$e^-$

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v}_e \times \mathbf{B}) - \nabla \times (\eta \nabla \times \mathbf{B})$$

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Hall

Elasticity

Liquid core

$e^-$

$e^-$

Maxwell stress

$$\frac{B_z B_x}{4\pi}$$

# Internal Magnetic Evolution of Pulsars

Magnetosphere

$\vec{B}$

Hall Magneto-Elastic Dynamics

Solid crust

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v}_e \times \mathbf{B}) - \nabla \times (\eta \nabla \times \mathbf{B})$$

$$\mathbf{v}_e = - \underbrace{\frac{c}{4\pi n_e e} \nabla \times \mathbf{B}}_{\text{Hall}} + \underbrace{\dot{\xi}}_{\text{Elasticity}}$$

Hall Elasticity



Liquid core

Jones 75, Easson & Pethick 77,  
Akgun & Wasserman 2008

**TYPE II SUPERCONDUCTOR**

Maxwell stress

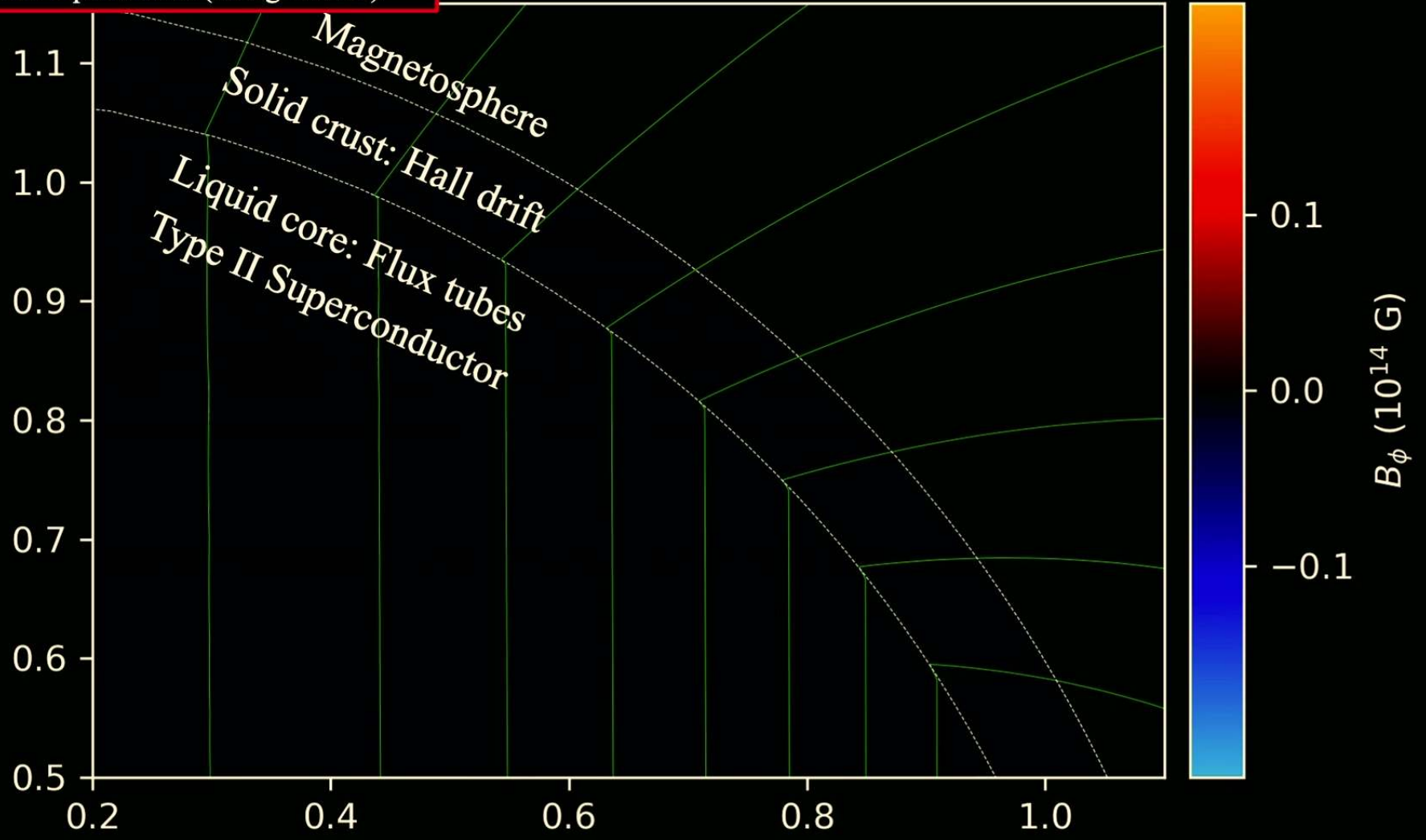
$$\frac{B_z B_x}{4\pi}$$

$$\frac{B_z H_x}{4\pi} \text{ 1000x larger}$$

Simple model: Flux tubes remain in tension equilibrium (straight lines)

Bransgrove, Levin, Beloborodov  
([arXiv:2408.10888](https://arxiv.org/abs/2408.10888))

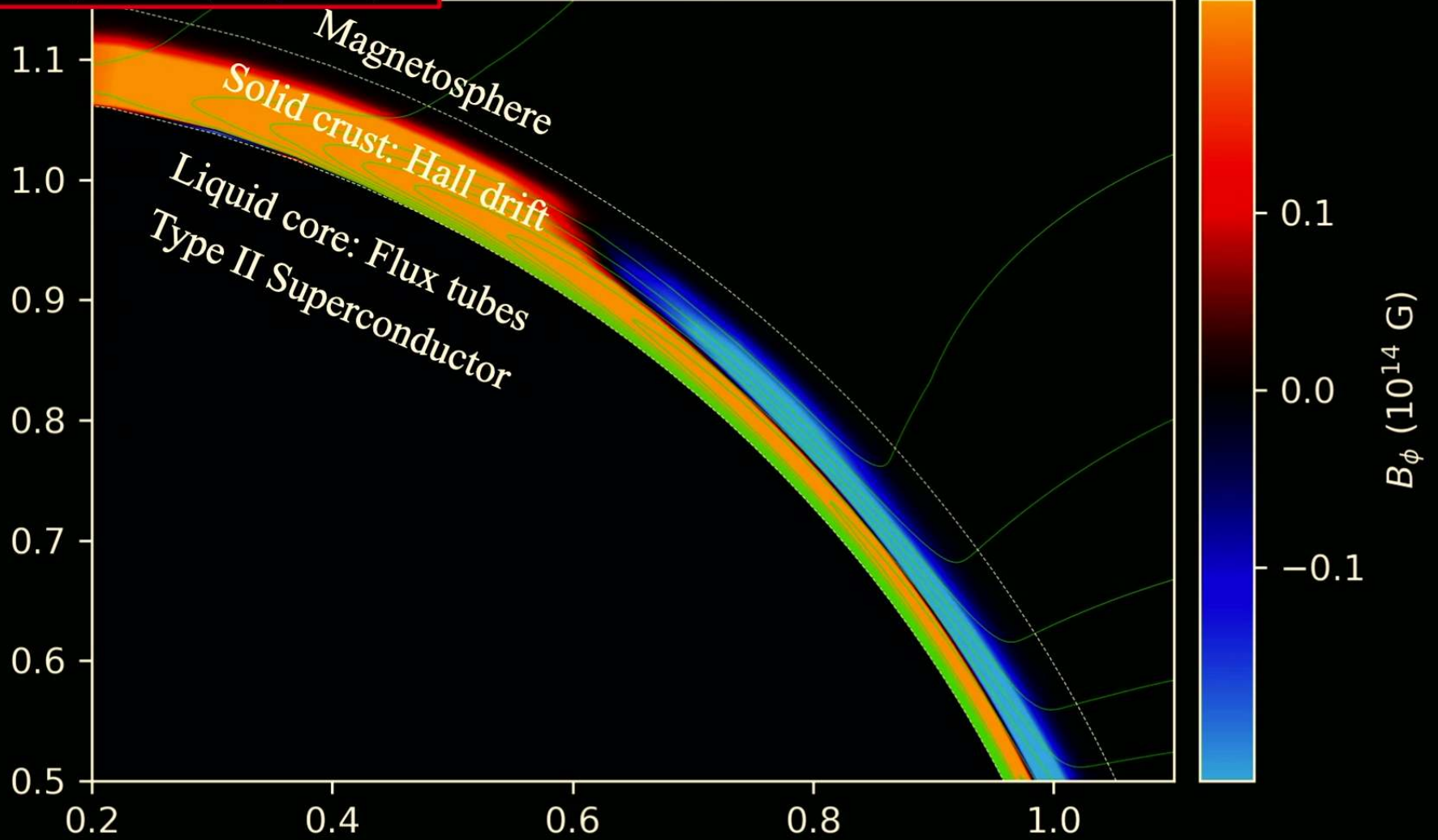
$t = 0$  yr



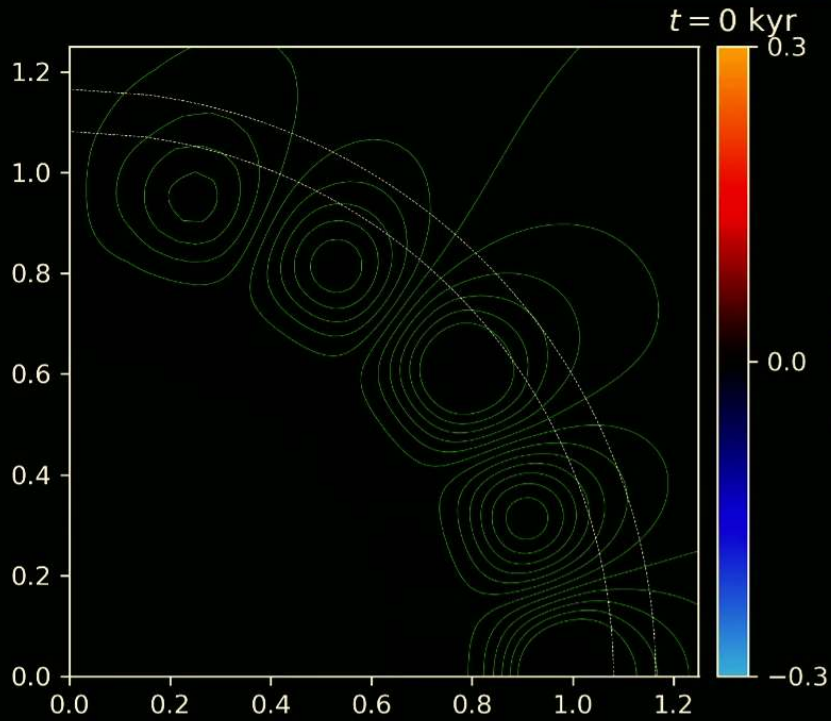
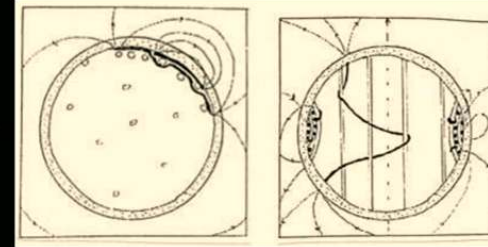
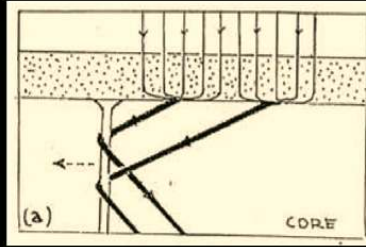
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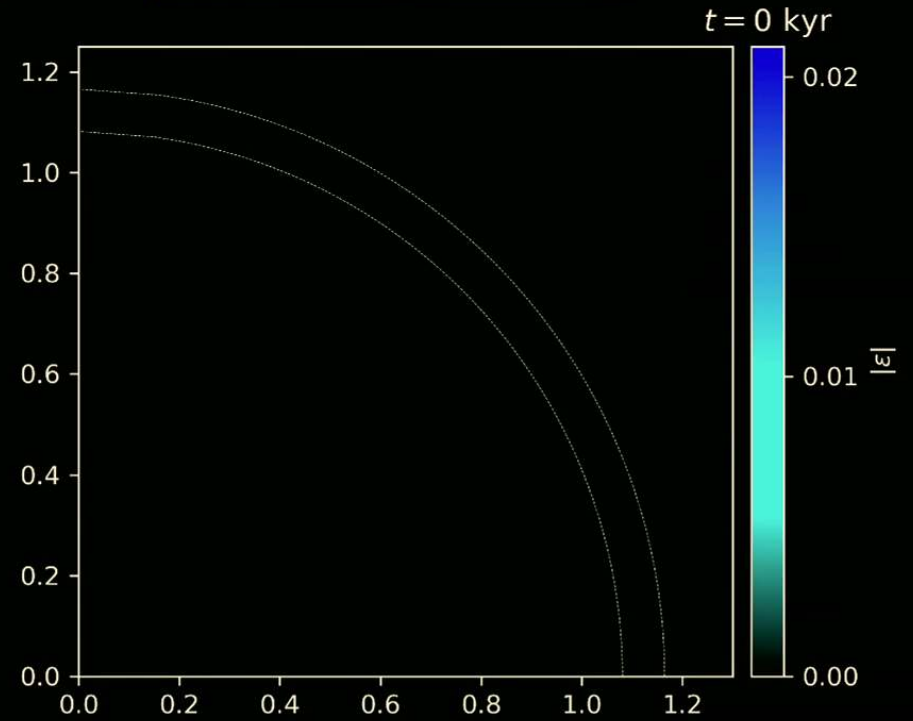
$t = 155000$  yr



Ruderman-like model  
for vortex - flux tube  
interactions



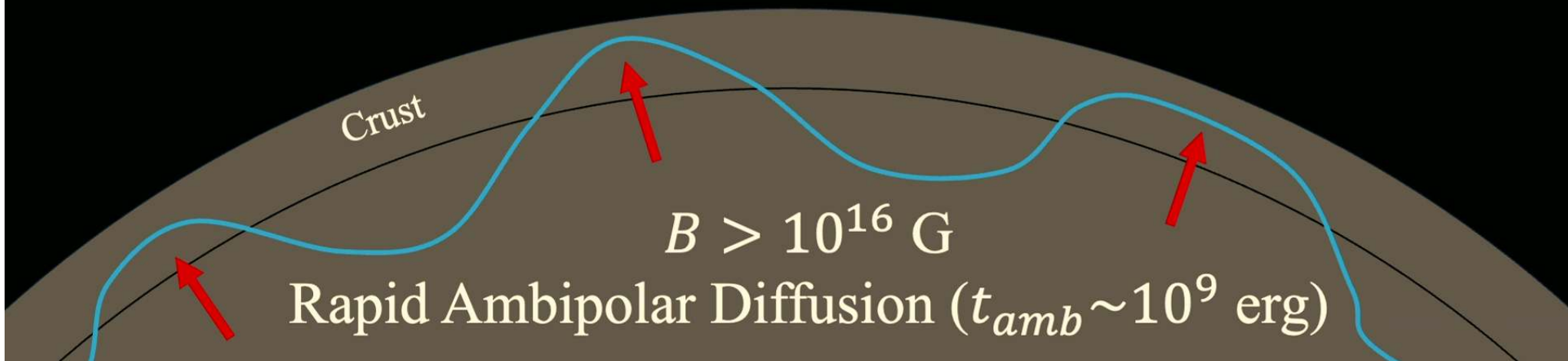
Magnetic Field



Elastic Strain

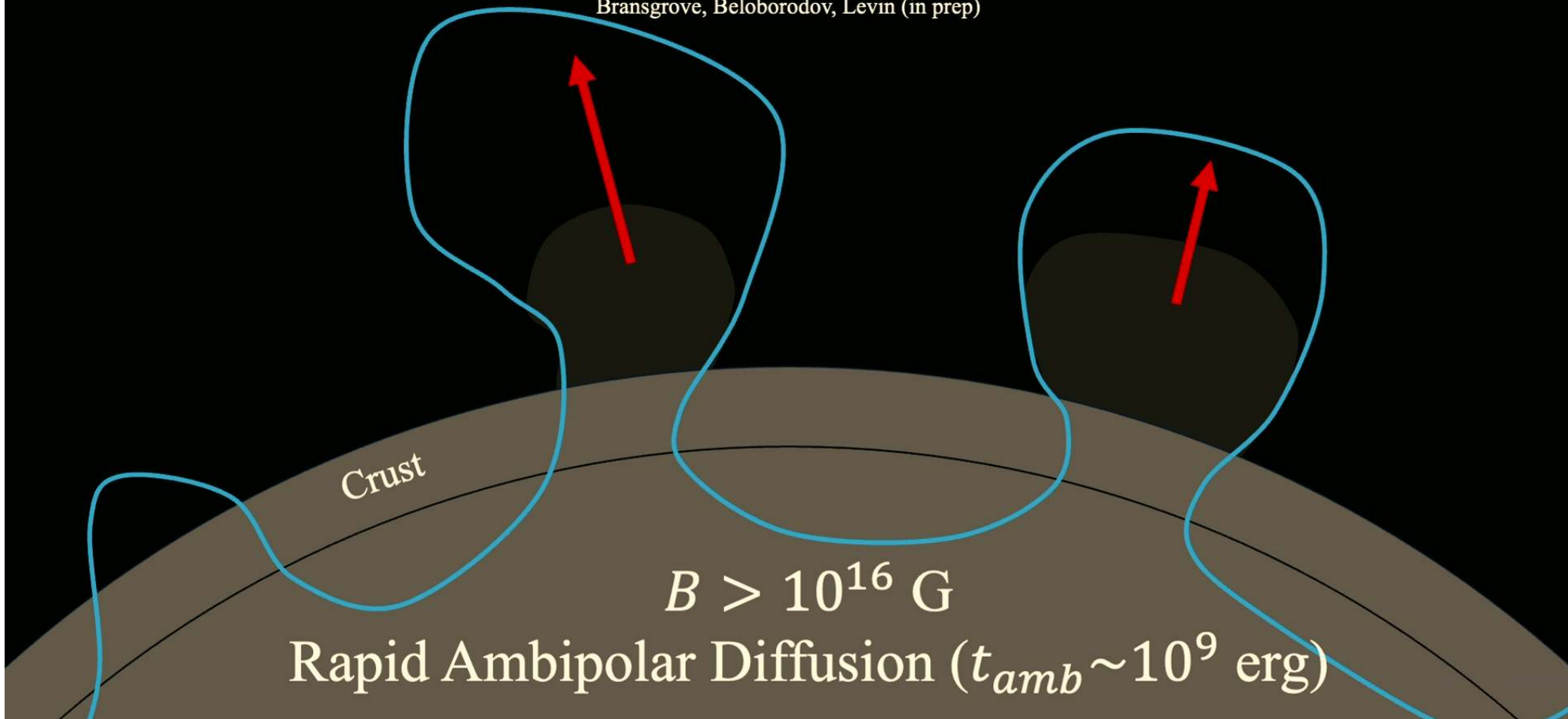
# Preview: Hyperactive Magnetars

Bransgrove, Beloborodov, Levin (in prep)



# Preview: Hyperactive Magnetars

Bransgrove, Beloborodov, Levin (in prep)



# Summary

- Superconductivity may be the dominant driver of magnetic field evolution in the first  $\sim$ Myr of a pulsar's life.
- Pulsar variability may be related to evolution of their magnetic fields.
- Hyperactive magnetars powered by ambipolar diffusion.

# Extreme Physics of Neutron Star Interiors

May 14-16, 2025

407 Jadwin Hall, Princeton University

Pulsars

Magnetars

Fast Radio Bursts

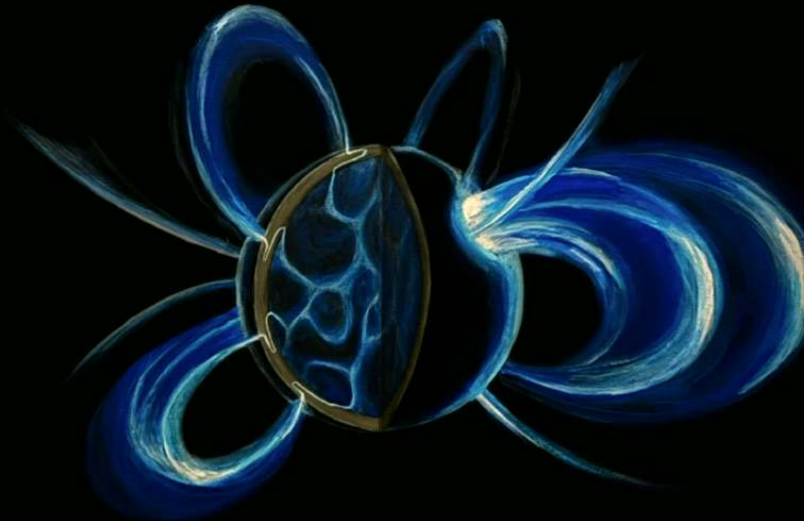
Plasma Physics

Dense Matter

Nuclear Physics

Magnetic Fields

Quantum Fluids



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[pcts.princeton.edu/events](https://pcts.princeton.edu/events)

Organizers: Ashley Bransgrove, Anirudh Prabhu,  
Peter Rau, Anatoly Spitkovsky, Andrei Beloborodov

