

**Title:** Fault Tolerance via Mixed-State Phases

**Speakers:** Amirreza Negari

**Collection/Series:** Training Programs (TEOSP)

**Subject:** Other

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**Abstract:**

In this talk, I will explain the concept of fault tolerance, which ensures reliable quantum computation. Building on recent advancements in mixed-state phases of matter, I introduce a new diagnostic called the spacetime Markov length. The divergence of this length scale signals the intrinsic breakdown of fault tolerance.

- 1) Error Correction & Fault tolerance
- 2) Phases of Matter as Equivalents classes
- 3) 1+2
- 4) Introducing diagnostic for fault tolerance

$$0 \rightarrow \underbrace{00 \dots 0}_N$$

$$1 \rightarrow \underbrace{111 \dots 1}_N$$

$$P < \frac{1}{2}$$

$$P(X \geq 0.49) = P(X \geq 0.5 + 0.01) \rightarrow 0.01$$

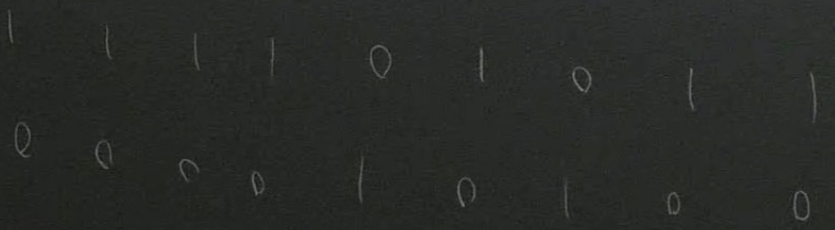
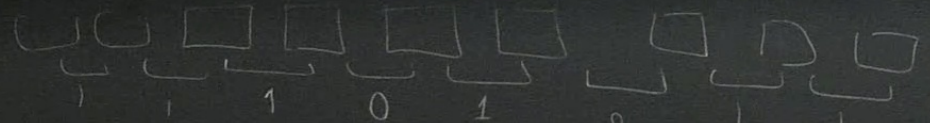
$$0 \ 0 \ 0 \ 1 \ 1 \ 0 \ 0 \rightarrow 0$$

$$0 \rightarrow \underbrace{00 \dots 0}_N$$

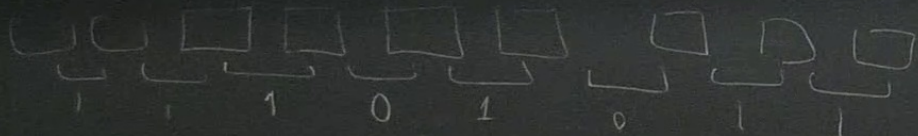
$$1 \rightarrow \underbrace{11 \dots 1}_N$$

$$P < \frac{1}{2}$$

...  $0111 \dots 1111 \rightarrow 0 \dots 1$



parity string  $\rightarrow$  0 1 1



Parity checks

1	1	1	1	0	0	0	1	1
0	0	0	0	1	1	1	0	0

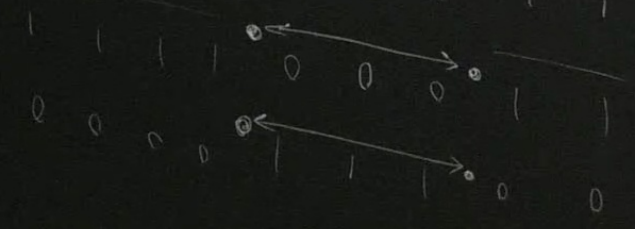
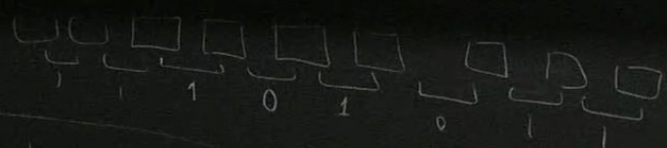
0 →  $\underbrace{0000}_N$

1 →  $\underbrace{1111}_N$

$P < \frac{1}{2}$

More parity bits → 0 or 1

Some channels

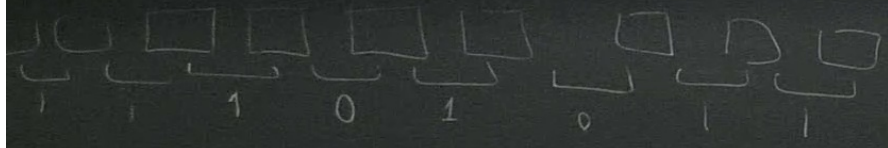


Parity checks

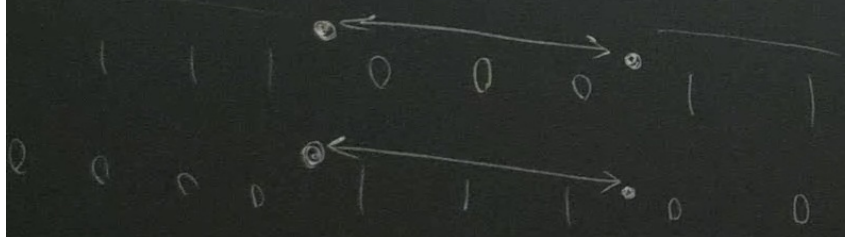
$P_1$   
 $P_2$   $< N$

... → 0 ...

sem. classical



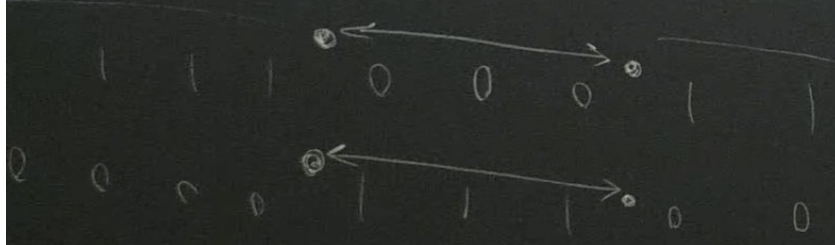
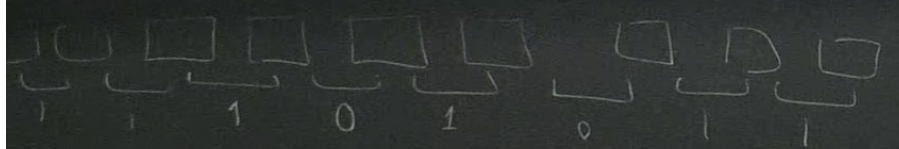
Parity checks



$$\frac{P_1}{P_2} \sim e^{-\alpha N}$$

parity check  $\rightarrow$  0

Some constraint  $\{S_i, S_j\} = 0$



Parity checks =  $\hat{S}_i$

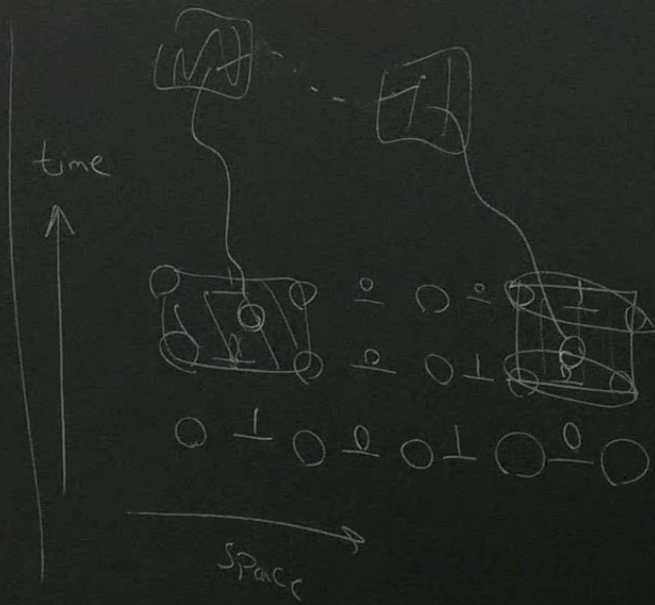
$$\frac{P_1}{P_2} \sim e^{-\alpha N}$$

$S_i$



$$S_i |\psi\rangle = \pm |\psi\rangle$$

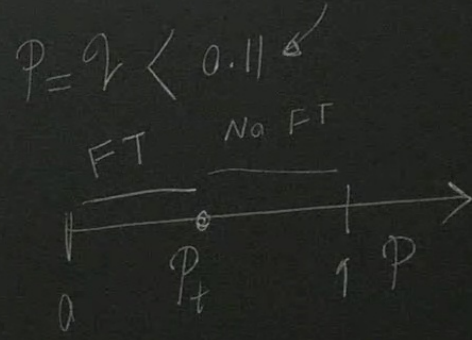
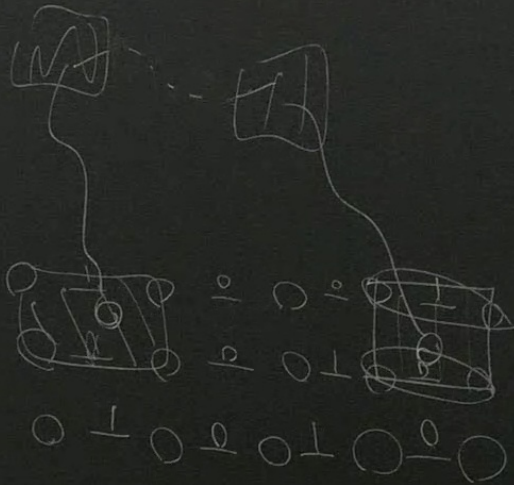
$$S_i = -1$$



$$S_i |\psi\rangle = 1 |\psi\rangle$$

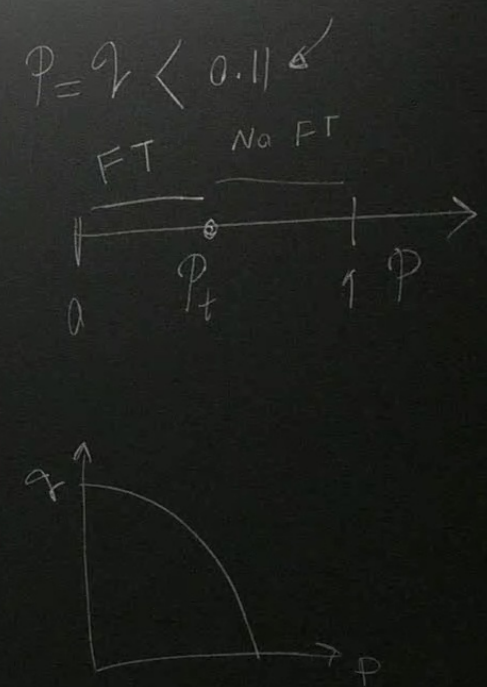
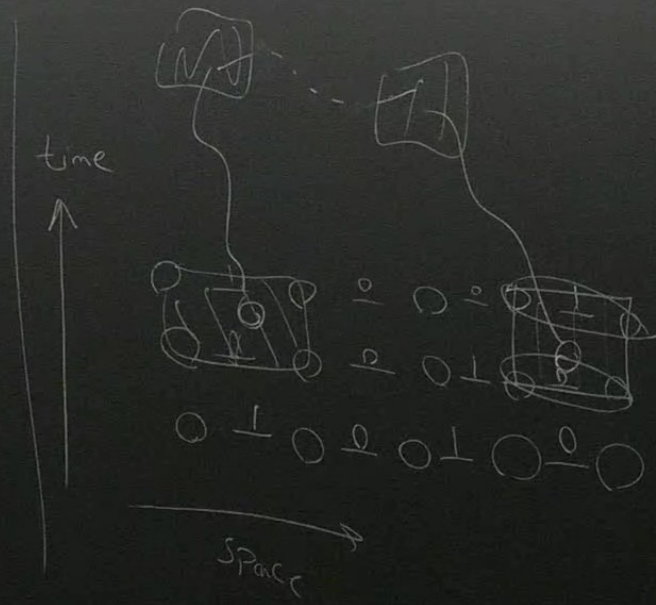
$$S_i = -1$$

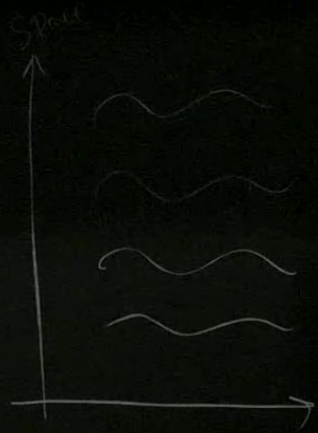
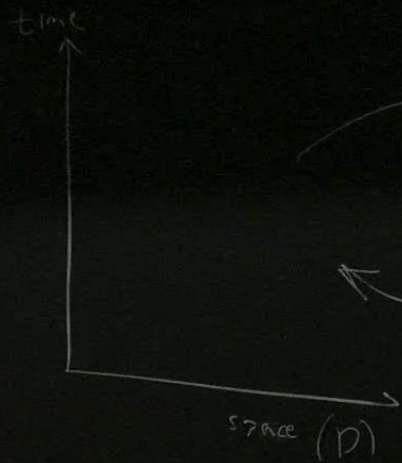
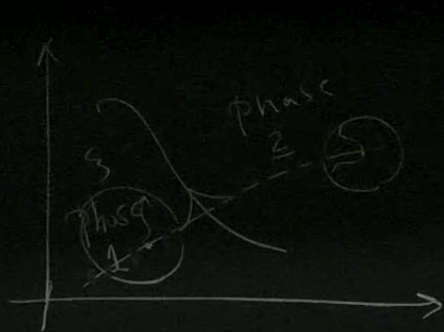
time

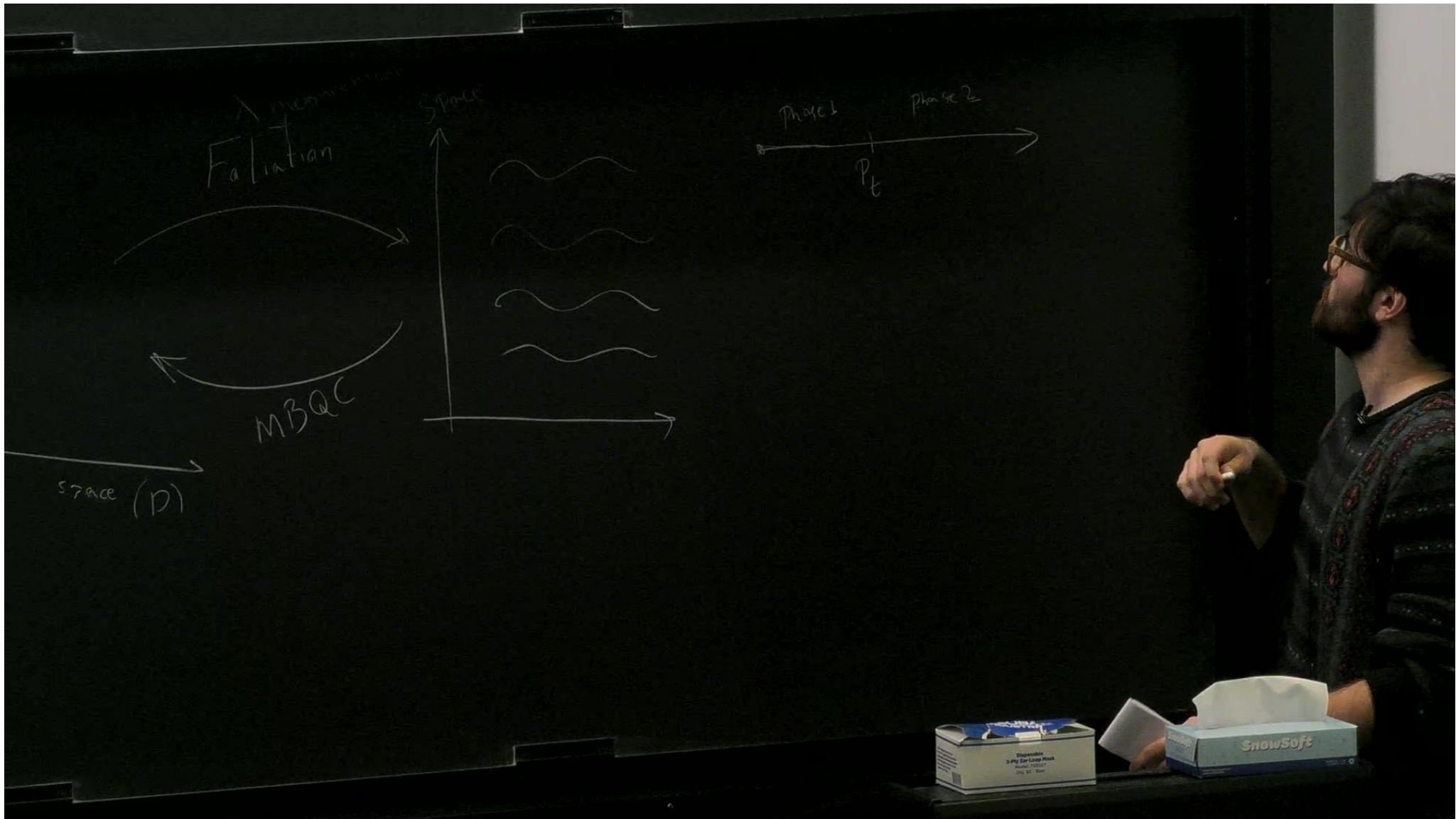


$$S_i |\psi\rangle = \pm |\psi\rangle$$

$$S_i = -1$$





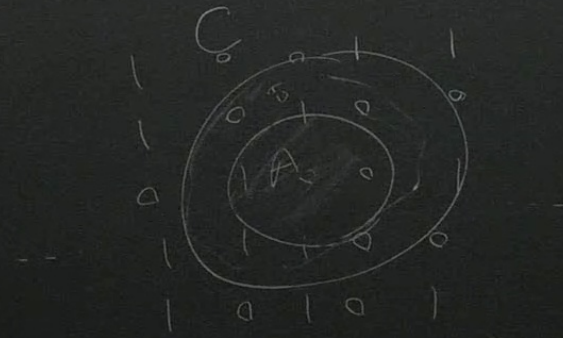


1) Error Correction & Fault tolerance

2) Phases of Matter as Equivalents classes

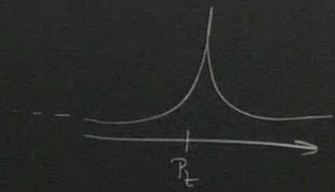
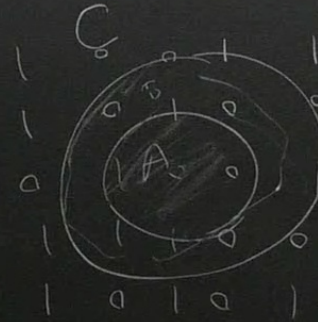
3) 1+2

4) Introducing diagnostic for fault tolerance



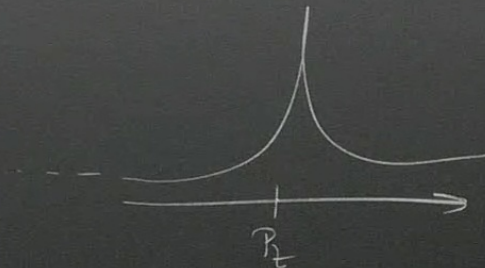
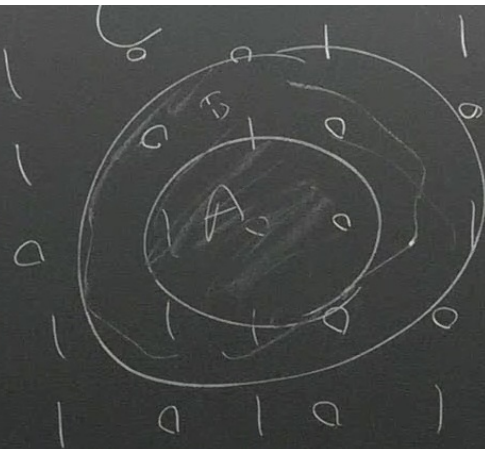
$$C = (A \cup B)' = I(A:c|B) \approx e^{-\frac{r_B}{\lambda}}$$
$$(P_{AC} - P_A P_C) | B$$

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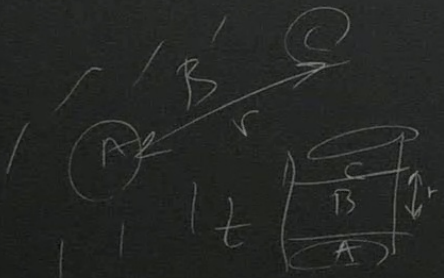


$$\begin{aligned}
 C &= (A \cup B)' && (P_{AC} - P_{AP_C})|_B \\
 &= I(A:c|B) \approx e^{-\frac{r_B}{k_p}} \\
 &= S_{(AB)} + S_{(BC)} - S_{(P)} - S_{(ABC)}
 \end{aligned}$$

Equivalent classes



tolerance



$$C = (A \cup B)' = I(A:c|B) \approx e^{-\frac{r_B}{r_A}}$$

$$= S_{(AB)} + S_{(BC)} - S_{(B)} - S_{(ABC)}$$

$$(P_{AC} - P_A P_C) |_B$$