Title: Exploring Quantum Many-Body Scars: Anomalies to Thermalization in Quantum Systems

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Abstract:

Quantum many-body scars (QMBS) have emerged as a captivating anomaly within the landscape of quantum physics, challenging the conventional expectations of the eigenstate thermalization hypothesis (ETH). According to ETH, an isolated quantum system is expected to evolve toward thermal equilibrium, with local observables equilibrating to values predicted by statistical mechanics, independent of the initial state of the system. However, QMBS present a remarkable exception by exhibiting resistance to thermalization, thus maintaining quantum information for unexpectedly long durations.

This colloquium will delve into the intriguing realm of QMBS, highlighting their pivotal role in advancing our understanding of quantum thermalization and their potential applications in quantum dynamics and technology. The discussion will cover recent theoretical and experimental progress in identifying systems that display these scars, focusing on their properties and the mechanisms by which they arise.

A specific area of interest is the construction of QMBS states emerging from Einstein-Podolsky-Rosen (EPR) states in bilayer systems, where each layer is maximally entangled. We will explore applications of this framework in quantum dimer models, examining various features of the bilayer model that contribute to the emergence of these states. Furthermore, if time allows, the talk will extend to systems of itinerant bosons, demonstrating how an infinite tower of many-body scar states can manifest in bilayer Bose-Hubbard models with charge conservation. We will discuss the implications of these findings in the context of recent experimental advancements, considering how these theoretical constructs relate to physically realizable systems in laboratory settings.

Exploring Quantum Many-Body Scars: Anomalies to Thermalization in Quantum Systems

ALES PROM THE QUANTUM CAPP

Wildeboer et al., PRB 106, 205142 (2022)

... more has been done ...

... more to come ...

Julia Wildeboer

Condensed Matter Physics and Material Science Division

Description

Desc

Overarching Theme



Remembering the last days of summer ... (from last summer)!



Remembering the last days of summer ... (from last summer)!



What is a scar?

► Ernst Chladni: acoustics experiment



vibrating plate and sand



pattern formation

picture taken from https://www.carlopasceri.it/blog/ ernst-chladni-e-la-magia-visibile-della-musica

What is a scar?

Quantum Chaos: Bunimovich Stadium

- chaotic system: ball will cover every possible trajectory inside the stadium
- if ball is started at a certain angle, it will instead retrace the same path forever
- same situation for if ball is replaced by quantum particle



What is a scar?

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What is a quantum many-body scar?



• each configuration is a vertex

- vertices i and j are connected by $\langle \Psi_i | \mathcal{H} | \Psi_j
angle$

- 10 atoms oscillating between ground state (black) and excited state (white). Atoms can be simultaneously in the superposition of all possible 47 configurations.
- ► Top plot shows different probabilities of individual configurations over time.

What is a quantum many-body scar?



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ullet vertices i and j are connected by $\langle \Psi_i | \mathcal{H} | \Psi_j
angle$



► Top plot shows different probabilities of individual configurations over time.

Quantum Dynamics/Ergodicity

 \implies many-body physics beyond the ground states

- advances in experiments: isolated quantum systems
- ▶ fundamental questions: When and how is quantum information lost/retained?

\Rightarrow ergocity

• isolated system: quantum quench

$$|\Psi\rangle \longrightarrow U(t) \longrightarrow |???\rangle$$

Motivation: Progress in Experiments





fermionic atoms in optical lattice: dynamics depend on (non)-interacting atoms [Bloch group (MPQ, Munich)]

- · systems are isolated from environment
- non-equilibrium physics
- quantum dynamics: prepare precise initial states and observe the ensuing dynamics in real time

(ultracold) Rydberg atoms



alkali-metal atoms (lithium, sodium, potassium, rubidium, cesium, and francium) [Harvard group]

 experimental realization of topological matter

Ergodicity in Quantum Dynamics

• isolated system: quantum quench

$$|\Psi\rangle \longrightarrow U(t) \longrightarrow |???\rangle$$

- ergodic dynamics: system relaxes to locally thermal state regardless of initial condition
- mechanism: system acts as its own bath
- many-body time evolution washes away quantum correlations
- quantum information stored in local objects is rapidly lost as these get entangled with the rest of the systems.
- many-body system is essentially devoid of any remaining structure



time



spin system: spins will get entangled with other spins as time progresses

Eigenstate Thermalization Hypothesis (ETH)

Deutsch 1991, Srednicki 1994

- interested in generic high energy eigenstates $|E\rangle$ (finite energy density above ground state)
- ETH: eigenstates of <u>thermalizing</u> systems appear thermal to all local measurements

$$\rho_A = \operatorname{tr}_B |E\rangle\langle E| \longrightarrow \frac{1}{Z_A} e^{-\beta H_A}$$

$$S_A = \operatorname{tr}[\rho_A \ln \rho_A] = s(E)L_A^d \propto S_{ther} \sim \operatorname{Vol}(A)$$

 $\langle \mathcal{O}_A \rangle_E = Tr(\rho_A \mathcal{O}_A) \approx \langle \mathcal{O}_A \rangle_{E'}$

• ground state(s) are special: $S_A \sim$

$$\sim L_{_{A}}^{d-1}~$$
 area law



В

- Eigenstate Thermalization Hypothesis (ETH) Deutsch 1991, Srednicki 1994
- entanglement behavior of generic highly excited many-body states



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 Dynamics in MBL systems: all states retain memory of initial state (nonergodicity) strong ergodicity breaking

- Eigenstate Thermalization Hypothesis (ETH) Deutsch 1991, Srednicki 1994
- entanglement behavior of generic highly excited many-body states



Quantum many-body Scars \iff Quantum Information

- motivation in applications/advances in quantum information
 - Quantum Memory: persistent long-lived oscillations relevant for quantum information storage, interest for applications in quantum memory and quantum error correction
 - Entanglement Properties: unique entanglement structures can be leveraged to study entanglement dynamics and correlations, critical for quantum information processing, understanding how entanglement evolves (entanglement dynamics) provides insights into non-equilibrium dynamics valuable for developing quantum algorithms/protocols
 - Quantum Computing and Algorithms: efficient state preparation in quantum computing, robustness against decoherence
 - Information Scrambling: study of QMBS can contribute to understanding how information is scrambled in quantum systems, relevant for quantum communication and information security
 - Exp. Realization in Cold Atoms: providing platforms for exploring quantum information concepts in controlled environments, serve as testbeds for developing quantum information technologies

Experimental Realization

- **b** scars in a quantum generic system
 - 51 (Rydberg) Rb atoms placed in a row: every other atom in either a high-energy excited state or a low-energy ground state
 - atoms reach equilibrium, then quickly revert to the original "antiferromagnet" state

Rydberg experiment:



ORDERED SEQUENCE OF ATOMS

Experimental Realization

Many-body physics with Rydberg atoms



Bernien et al., Nature 551, 579 (2017)

- individual ⁸⁷Rb atoms are trapped using optical tweezers (vertical red beams) and arranged into defect-free arrays
- coherent interactions V_{ij} between the atoms (arrows) are enabled by exciting them (horizontal blue and red beams) to a Rydberg state, with strength Ω
- strong van-der-Waals interaction between excited (spin-up) particles
- tune atomic spacing so that $|g\rangle |r\rangle |r\rangle |g\rangle = 1$

Model for Rydberg Experiment

Many-body physics with Rydberg atoms

⇒ effective model for 1d chain of Rydberg atoms: spin-1/2 model

$$\mathcal{H} = \sum_{i=1}^{L} P_i X_{i+1} P_{i+2}$$

 X_i, Y_i, Z_i are Pauli operators

local basis states at site i: $|ullet
angle=|\uparrow
angle$ $|\circ
angle=|\downarrow
angle$

•
$$X_i = |\circ\rangle\langle \bullet| + |\bullet\rangle\langle \circ|$$
 creates or removes an excitation at site i

$$P_i = |\circ\rangle\langle \circ| = (1 - Z_i)/2$$
$$Z_i = |\bullet\rangle\langle \bullet| - |\circ\rangle\langle \circ|$$

projectors ensure that the nearby atoms are not simultaneously in the excited state

$$P_1 X_2 P_3 | \circ \circ \circ \rangle = | \circ \bullet \circ \rangle$$
$$P_1 X_2 P_3 | \bullet \circ \circ \rangle = 0$$
$$P_1 X_2 P_3 | \circ \circ \bullet \rangle = 0$$
$$P_1 X_2 P_3 | \bullet \circ \bullet \rangle = 0$$

This model:

C.J. Turner et al., Nature 14, 745-749 (2018)

- $\implies \text{able to describe unexpected revivals in certain states} \\ |\mathbb{Z}_2\rangle = | \bullet \circ \bullet \circ \bullet \circ \ldots \rangle$
- ⇒ identifies special states responsible: quantum many-body scar states

Model for Rydberg Experiment

Many-body physics with Rydberg atoms

• start with antiferromagnetic initial state and evolve it for some time t: $|\mathbb{Z}_2\rangle = |\bullet \circ \bullet \circ \bullet \circ \cdots \rangle$



MBL

• strong coherent revivals after quench from Neel state $|\mathbb{Z}_2\rangle = |\bullet \circ \bullet \circ \bullet \circ \circ \ldots\rangle$

• no revivals for generic initial product states, they thermalize quickly example: $|\mathbb{Z}_0\rangle = |\circ \circ \circ \circ \circ \circ \cdots \rangle$

C.J. Turner et al., Nature 14, 745–749 (2018)

⇒ Highly unexpected! Model does not seem to satisfy ETH!!!

 \Rightarrow strong dependence on initial state: ETF

Quantum Many-Body Scar States

Are there models (classes or families) that contain scar states that do not thermalize?

Characteristics of systems with scars?

General mechanism

1. Unconventional Symmetries or Conservation Laws:

- Hidden Symmetries: QMBS states often arise from hidden symmetries/conserved quantities not immediately apparent in the Hamiltonian. These symmetries can protect certain eigenstates from thermalizing and contribute to the scars' formation.
- Strongly Broken Symmetries: Some systems with QMBS have Hamiltonians that break certain symmetries, leading to a small subset of states that exhibit non-ergodic behavior.

2. Group-Theoretic Constructions:

Group-Theoretic Methods: QMBS states can be constructed using group-theoretic methods, where special algebraic structures or symmetry groups lead to a discrete set of scar states. These constructions often reveal how such states can be embedded within the Hilbert space of a many-body system.

3. Entanglement Structure:

Special Entanglement Patterns: QMBS states often exhibit unique entanglement properties, such as specific patterns of entanglement that prevent them from mixing with other states. These entanglement patterns can lead to slow dynamics and long-lived oscillations in observables.

4. Perturbative Analysis

Perturbative Methods: In some cases, QMBS can be understood as perturbations or excitations around exactly solvable points or models. These perturbative approaches help in identifying the conditions under which scar states persist.

5. Construction from Specific Models, Exact Solutions, Numerical and Experimental Observations

General Construction: Bilayer System



• $\mathcal{H} = \mathcal{H}_1 + \mathcal{H}_2$ $\begin{array}{c} \mathcal{H}_2 = -\mathcal{H}_1 \\ \text{mirror symmetry } \mathcal{M}: i \to \tilde{i} \end{array}$

 $\{ |\Psi_{nn}
angle = |\psi_n
angle \otimes |\psi_n
angle : orall \ n = 1, \dots d^N \}$

General Construction: Bilayer System



- $\mathcal{H} = \mathcal{H}_1 + \mathcal{H}_2 + \mathcal{H}_{12}$ $\mathcal{H}_2 = -\mathcal{H}_1$ mirror symmetry $\mathcal{M} : i \to \tilde{i}$
- We demand in addition: $\; {\cal H}_{12} |\Psi_{nn}
 angle = E_{12} |\Psi_{nn}
 angle$

Wildeboer et al., PRB 106, 205142 (2022) Langlett et al., PRB 105, L060301 (2021)

 $\{|\Psi_{nn}
angle=|\psi_n
angle\otimes|\psi_n
angle:orall\;n=1,\dots d^N\}$ are quantum many-body scar states !

⇒ Einstein-Podolsky-Rosen (EPR) scar states are born!

EPR Scar States

 \Rightarrow examples:

- quantum dimer model as bilayer system on square lattice, ...
- Bose-Hubbard model as bilayer system
- bilayer triangular lattice Heisenberg model with SU(2) symmetry

... and more see Wildeboer et al., PRB 106, 205142 (2022) and future work

Dimers on the square lattice



• Bose-Hubbard model $\mathcal{H} = \sum_{\langle i,j
angle} -t_{ij} \left(b_i^{\dagger} b_j + h.c.
ight) + U \sum_i n_i \left(n_i - 1
ight)$

bosonic occupation operators $n_i=0,1,2,3,\dots$

$$[\mathcal{H}, n_i] = 0$$

$$\implies \mathcal{H}_{1} = \sum_{\langle i,j \rangle} -t_{ij} \left(b_{i}^{\dagger} b_{j} + h.c. \right) + U \sum_{i} n_{i} \left(n_{i} - 1 \right)$$
$$\mathcal{H}_{2} = -\mathcal{H}_{1}$$

$$\mathcal{H}_{12} = \lambda \sum_i \left(n_i - n_{\widetilde{i}}
ight)^2$$



square lattice bilayer

• Einstein-Podolsky-Rosen (EPR) scar states $|\text{EPR}\rangle = \sum_{M=0}^{M_{\text{max}}} c_M |\text{EPR}\rangle_M$

sector M bosons

$$|\text{EPR}\rangle_M = \mathcal{P}_M \left[\bigotimes_{i \le N} \left(\frac{1}{\sqrt{\alpha_{BH}}} \sum_{n=0}^M |n, n\rangle \right)_{i, \tilde{i}} \right]$$

"bosonic configurations identical in both layers"







Summary

Quantum many-body scar states

new class of non-integrable many-body systems with atypical (non-thermal) eigenstates throughout the spectrum that display periodic quantum revivals observed in quench experiments

- background on quantum many-body scars
 - ► billiard Bunimovich stadium, Rydberg experiment at Harvard
 - PXP model and its experimental realization
- 2D bilayer systems of various degrees of freedom:

spins, bosons, fermions, quantum dimers, ...

- future
 - mechanism for scar existence?
 - ► How far are the applications for quantum many-body scars (quantum information)?
 - quantum many-body scars in an actual compound <--> theory & experiment collaboration in the CMPMSD at BNL



2D bilayer system

Wildeboer et al., PRB 106 (2022) Langlett et al., PRB 105, L060301 (2022) Wildeboer et al., PRB 104, 121103 (2021) Srivatsa et al., PRB 102, 235106 (2020)

Thank you for your attention!

... more to come ...