

**Title:** Cosmological Foundations revisited with Pantheon+

**Speakers:** Antonia Seifert

**Collection/Series:** Cosmology and Gravitation

**Subject:** Cosmology

**Date:** January 28, 2025 - 11:00 AM

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**Abstract:**

The standard model of cosmology is built upon the assumptions of homogeneity and isotropy. Invoking backreaction of inhomogeneities leads to an alternative model, the timescape cosmology. It is homogeneous and isotropic on a statistical level but departs from average Friedmann-Lemaître-Robertson-Walker evolution and replaces dark energy by kinetic gravitational energy and its gradients.

In this talk, I will give an overview of the timescape cosmology and present a statistical analysis of the Pantheon+ Type Ia Supernovae spectroscopic comparing the timescape and spatially flat  $\Lambda$ CDM cosmological models. This analysis is based on the Tripp equation for supernova standardisation alone, thereby avoiding any potential correlation in the stretch and colour distributions and finds very strong evidence ( $\ln B > 5$ ) in favour of timescape over  $\Lambda$ CDM when considering the entire Pantheon+ sample.

# Cosmological Foundations revisited with Pantheon+

Antonia Seifert

Cosmology Group Seminar  
January 28, 2025



UNIVERSITÄT  
HEIDELBERG  
ZUKUNFT  
SEIT 1386



work with Zachary Lane, Marco Galoppo,  
Ryan Ridden-Harper and David Wiltshire

arXiv:2311.01438  
MNRAS, 536, 1752

arXiv:2412.15143  
MNRAS: Letters, 537, L55

MNRAS 000, 1–26 (2024)

Preprint 8 November 2024

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### Cosmological foundations revisited in Pantheon+

Zachary G. Lane<sup>1</sup>, Antonia Seifert<sup>1,2</sup>, Ryan Ridden-Harper<sup>1</sup>, and David L. Wiltshire<sup>1</sup>\*

<sup>1</sup>*School of Physical and Chemical Sciences — Te Kura Matū, University of Canterbury, Private Bag 4800, Christchurch 8140, New Zealand*

<sup>2</sup>*Institut für Theoretische Physik, Universität Heidelberg, Philosophenweg 12, D-69120 Heidelberg, Germany*

MNRAS 000, 1–6 (2024)

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### Supernovae evidence for foundational change to cosmological models

Antonia Seifert<sup>1,2</sup>, Zachary G. Lane<sup>1</sup>\*, Marco Galoppo<sup>1</sup>

Ryan Ridden-Harper<sup>1</sup>, and David L. Wiltshire<sup>1</sup>

<sup>1</sup>*School of Physical and Chemical Sciences — Te Kura Matū, University of Canterbury, Private Bag 4800, Christchurch 8140, New Zealand*

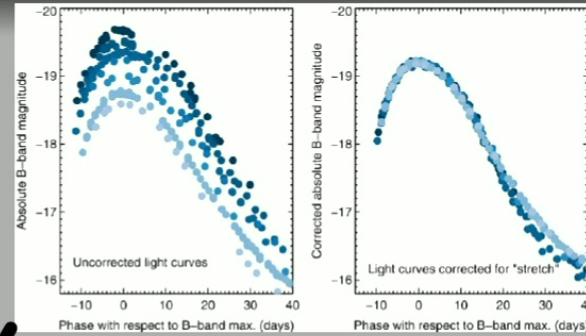
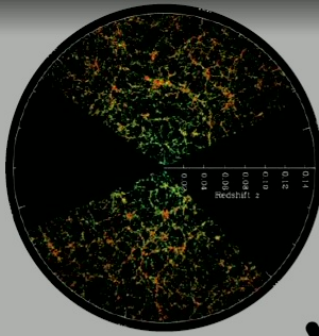
<sup>2</sup>*Institut für Theoretische Physik, Universität Heidelberg, Philosophenweg 12, D-69120 Heidelberg, Germany*



published on December 19, 2024

INPUT

Cosmological models:  
 $\Lambda$ CDM vs Timescape



Supernova  
standardisation

MNRAS 000, 1–6 (2024) Preprint 8 November 2024

Compi  $\mathcal{L}(M_B, x_1, c)$

**Cosmological foundations revisited in Pantheon+**

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Compi  $\mathcal{L}(M_B) |_{\text{fitted } x_1, c}$

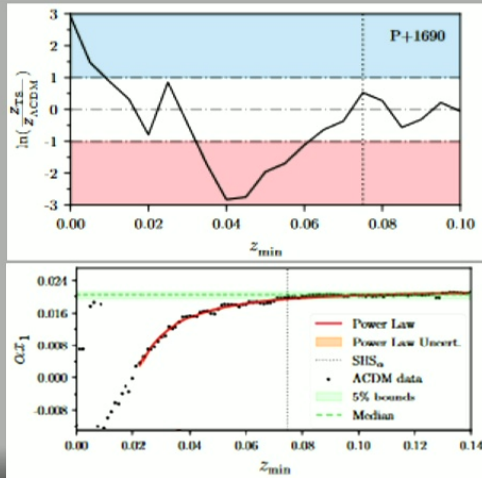
**Supernovae evidence for foundational change to cosmology**

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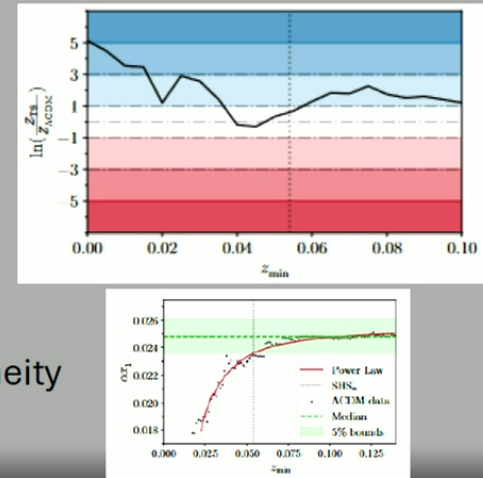
<sup>1</sup>School of Physical and Chemical Sciences — Te Kura Matu, University of Canterbury, Private Bag 4800, Christchurch 8140, New Zealand  
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RESULTS

Bayesian analysis



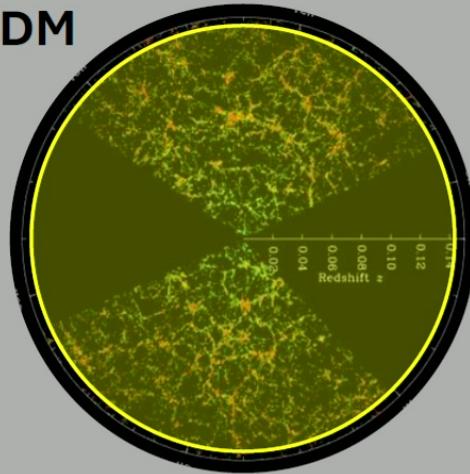
Scale of Statistical Homogeneity



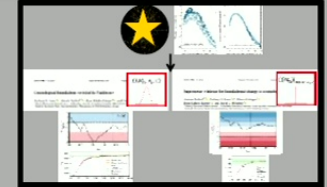
Credits: SDSS  
and Maguire (2017)

# Cosmological models

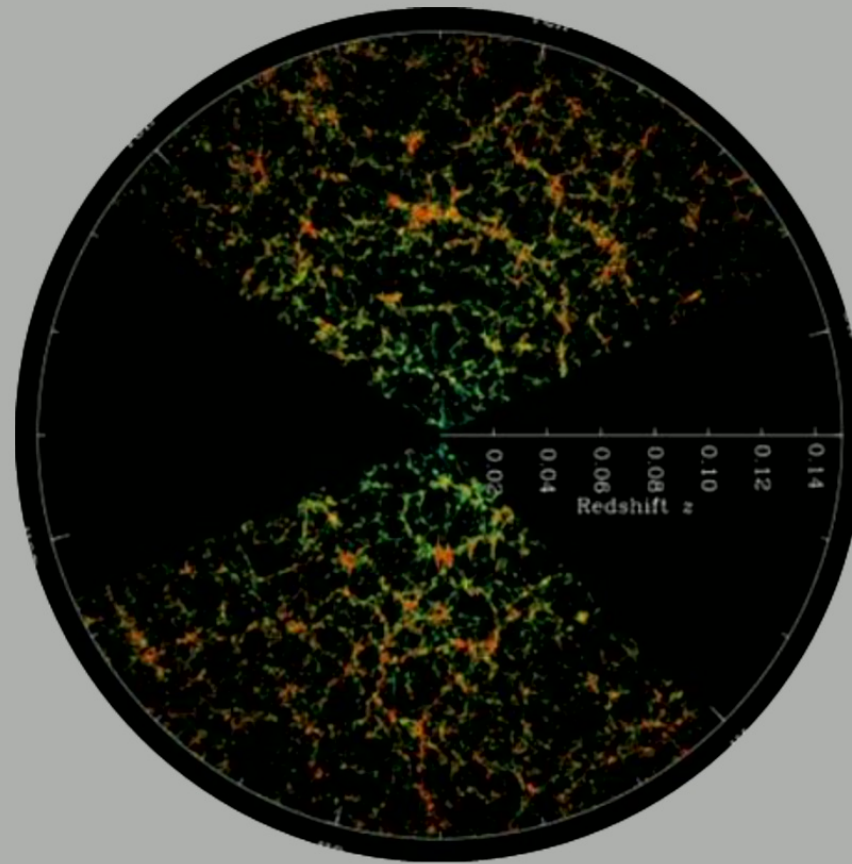
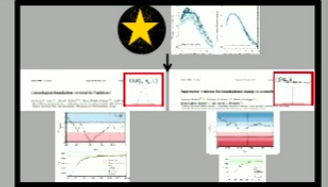
## Spatially flat $\Lambda$ CDM



- same metric everywhere
- flat
- homogeneous & isotropic



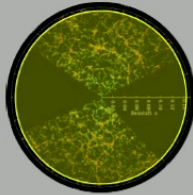
# Cosmological models



Credit: SDSS

# Cosmological models

## Spatially flat $\Lambda$ CDM



- spatially flat metric:

$$ds^2 = -dt^2 + a(t)(dr^2 + r^2 d\Omega)$$

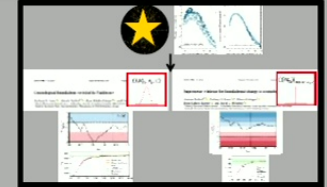
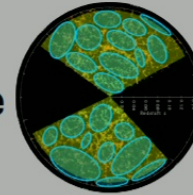
- Friedmann equations:

$$\frac{\dot{a}^2}{a^2} = \frac{8\pi G\rho}{3} - \frac{k}{a^2} + \frac{\Lambda}{3}$$

$$\frac{\ddot{a}}{a} = -\frac{4\pi G(1+3w)\rho}{3} + \frac{\Lambda}{3}$$

- model parameter  $\Omega_M = \frac{8\pi G\rho}{3H^2} = 1 - \Omega_\Lambda$  for  $k = 0$

## Timescape



- wall metric:

$$ds^2 = -d\tau_w^2 + a_w(\tau_w)(d\eta_w^2 + \eta_w^2 d\Omega)$$

- void metric:

$$ds^2 = -d\tau_v^2 + a_v(\tau_v)(d\eta_v^2 + \sinh^2(\eta_v) d\Omega)$$

- volume average weighted with void fraction  $f_v$  (Buchert 2000, Wiltshire 2007)

$$\bar{a}^3 = \frac{V(t)}{V(t_0)} = f_{vi} a_v^3 + (1 - f_{vi}) a_w^3$$

- Friedmann-like evolution equations:

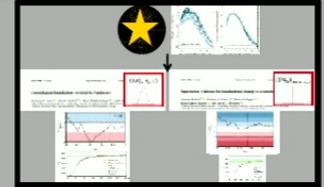
$$\frac{\dot{\bar{a}}^2}{\bar{a}^2} = \frac{8\pi G\langle\rho\rangle}{3} - \frac{\langle\mathcal{R}\rangle}{6} - \frac{Q}{6}$$

$$\frac{\ddot{\bar{a}}}{\bar{a}} = -\frac{4\pi G\langle\rho\rangle}{3} + \frac{Q}{3}$$

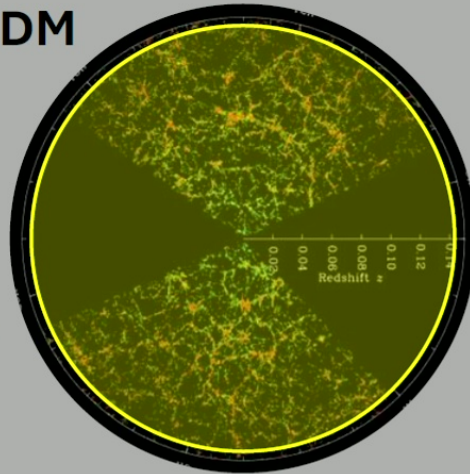
- $\langle\mathcal{R}\rangle$  and backreaction  $Q = \frac{2\dot{f}_v^2}{3f_v(1-f_v)}$  functions of  $f_v$

Credit: D. Wiltshire

# Cosmological models



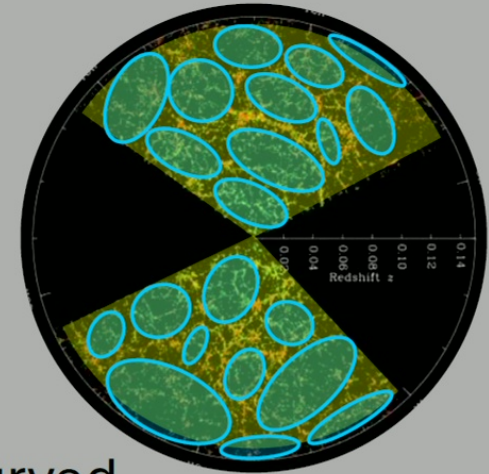
## Spatially flat $\Lambda$ CDM



- same metric everywhere
- flat
- homogeneous & isotropic
- model parameter:  $\Omega_M$

metric(s)  $ds^2 \rightarrow$  luminosity distance  $d_L$

## Timescape



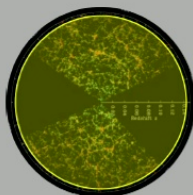
- wall metric: flat
- void metric: negatively curved
- not homogeneous
- model parameter:  $f_v$

Credit: SDSS



# Cosmological models

## Spatially flat $\Lambda$ CDM



- Luminosity distance  $d_L$ :

$$\frac{d_L}{(1+z)^2} = d_A = \frac{a_0 \chi(r)}{1+z}$$

- Spatially flat:  $\chi(r) = r$

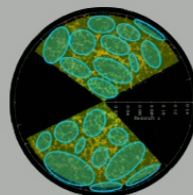
- From geometry:

$$ds^2 = -dt^2 + a(t)(dr^2 + \chi^2(r) d\Omega)$$

$$a dr = dt$$

$$\chi(r) = r = \int_t^{t_0} \frac{dt}{a} = \int_t^{t_0} \frac{da}{a H(a)}$$

## Timescape



- Luminosity distance  $d_L$ :

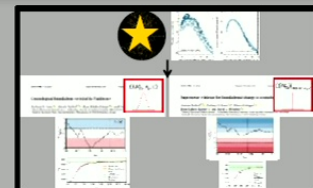
$$\frac{d_L}{(1+z)^2} = d_A = \frac{a_0 r_w}{1+z}$$

- Volume-averaged geometry:

$$\text{conformal time } \bar{a} d\bar{\eta} = dt = \bar{\gamma} d\tau_w = \bar{\gamma} \bar{a} \left( \frac{1-f_v}{f_{wi}} \right)^{\frac{1}{3}} d\eta_w$$

- Observer in wall:  $ds^2 = -d\tau_w^2 + a_w(\tau_w)(d\eta_w^2 + \eta_w^2 d\Omega)$

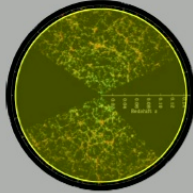
$$ds^2 = -\frac{dt^2}{\bar{\gamma}} + \frac{\bar{a}}{\bar{\gamma}} \left( d\bar{\eta}^2 + \left( \frac{\bar{\gamma}(1-f_v)^{\frac{1}{3}}}{f_{wi}^{\frac{1}{3}} \eta_w} \right)^2 d\Omega \right)$$



Credit: D. Wiltshire

# Cosmological models

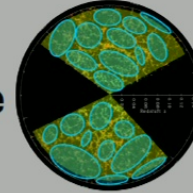
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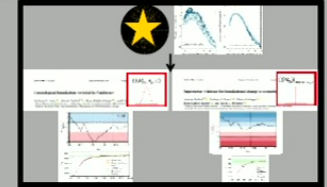
## Timescape



- Luminosity distance  $d_L$ :

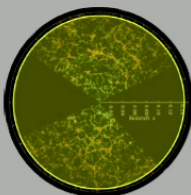
$$\frac{d_L}{(1+z)^2} = d_A = \frac{a_0 r_w}{1+z}$$

$$\mu = 25 + \log_{10} \left( \frac{d_L}{\text{Mpc}} \right)$$



# Cosmological models

## Spatially flat $\Lambda$ CDM



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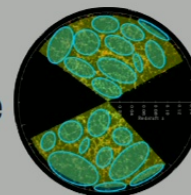
$$ds^2 = -dt^2 + a(t)(dr^2 + \chi^2(r) d\Omega)$$

$$a dr = dt$$

$$\chi(r) = r = \int_t^{t_0} \frac{dt}{a} = \int_t^{t_0} \frac{da}{a H(a)}$$



## Timescape



- Luminosity distance  $d_L$ :

$$\frac{d_L}{(1+z)^2} = d_A = \frac{a_0 r_w}{1+z}$$

- Volume-averaged geometry:

$$\text{conformal time } \bar{a} d\bar{\eta} = dt = \bar{\gamma} d\tau_w = \bar{\gamma} \bar{a} \left( \frac{1-f_v}{f_{wi}} \right)^{\frac{1}{3}} d\eta_w$$

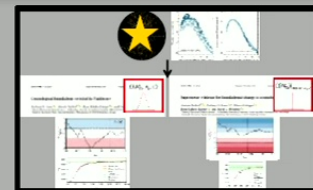
- Observer in wall:  $ds^2 = -d\tau_w^2 + a_w(\tau_w)(d\eta_w^2 + \eta_w^2 d\Omega)$

$$ds^2 = -\frac{dt^2}{\bar{\gamma}} + \frac{\bar{a}}{\bar{\gamma}} \left( d\bar{\eta}^2 + \left( \frac{\bar{\gamma}(1-f_v)^{\frac{1}{3}}}{f_{wi}^{\frac{1}{3}}} \eta_w \right)^2 d\Omega \right)$$

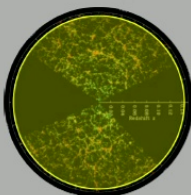
$$r_w = \frac{\bar{\gamma}(1-f_v)^{\frac{1}{3}}}{f_{wi}^{\frac{1}{3}}} \int d\eta_w = \bar{\gamma}(1-f_v)^{\frac{1}{3}} \int_t^{t_0} \frac{dt}{\bar{\gamma}(1-f_v)^{\frac{1}{3}} \bar{a}}$$

Credit: D. Wiltshire

# Cosmological models



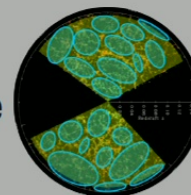
## Spatially flat $\Lambda$ CDM



- Luminosity distance  $d_L$ :

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## Timescape



- Luminosity distance  $d_L$ :

$$\frac{d_L}{(1+z)^2} = d_A = \frac{a_0 r_w}{1+z}$$

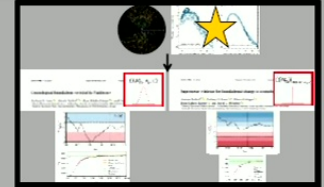
$$\mu = 25 + \log_{10} \left( \frac{d_L}{\text{Mpc}} \right)$$

$$\mu_{\text{TS}} = \mu_0(z) + \frac{5}{\ln 10} \left\{ \left[ \frac{24 f_{v0}^4 - 23 f_{v0}^3 + 99 f_{v0}^2 + 8}{2 (4 f_{v0}^2 + f_{v0} + 4)^2} \right] z - \left[ \frac{1984 f_{v0}^8 - 4352 f_{v0}^7 + 16515 f_{v0}^6 + 14770 f_{v0}^5 + 7819 f_{v0}^4 - 11328 f_{v0}^3 + 32080 f_{v0}^2 - 128 f_{v0} + 960}{24 (4 f_{v0}^2 + f_{v0} + 4)^4} \right] z^2 + \dots \right\}$$

$$\mu_{\Lambda\text{CDM}} = \mu_0(z) + \frac{5}{\ln 10} \left\{ (1 - \frac{3}{4} \Omega_{M0}) z - \left[ \frac{1}{2} + \frac{1}{2} \Omega_{M0} - \frac{27}{32} \Omega_{M0}^2 \right] z^2 + \left[ \frac{1}{3} - \frac{1}{8} \Omega_{M0} + \frac{21}{16} \Omega_{M0}^2 - \frac{45}{32} \Omega_{M0}^3 \right] z^3 + \dots \right\}$$

Credit: D. Wiltshire

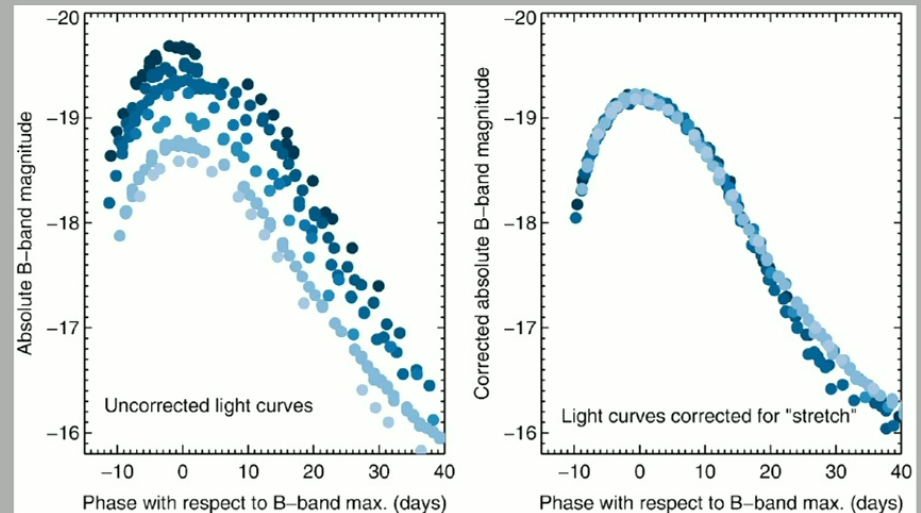
# Supernova standardisation



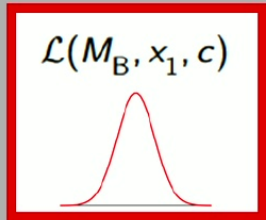
- Tripp equation:

$$\mu = m_B^* - M_B + \alpha x_1 - \beta c$$

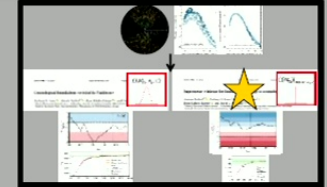
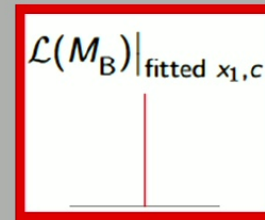
- Distance modulus
- SALT2 fit variables
- Cosmology constants
- Absolute magnitude (B filter)



Credit: Maguire (2017)



# Likelihood

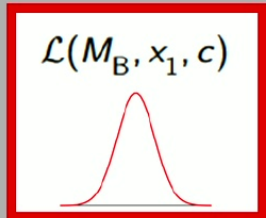


- Assumption:  
the fit values of all supernovae follow the same Gaussian
- 3N-dimensional Gaussian distribution for fitted values

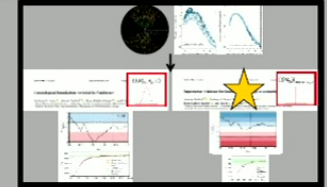
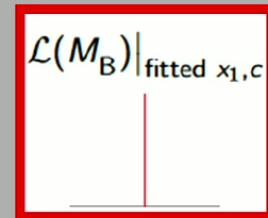
$$X - \hat{X} = \begin{pmatrix} M_B - \alpha x_1 + \beta c \\ x_1 \\ c \end{pmatrix} - \begin{pmatrix} \mu - \hat{m}_B^* \\ \hat{x}_1 \\ \hat{c} \end{pmatrix}$$

- No assumptions on the gaussianity of the SALT2 parameters
- Take the fit values as true values in the Tripp equation

$$X - \hat{X} = (M_B - \alpha \hat{x}_1 + \beta \hat{c}) - (\mu - \hat{m}_B^*)$$



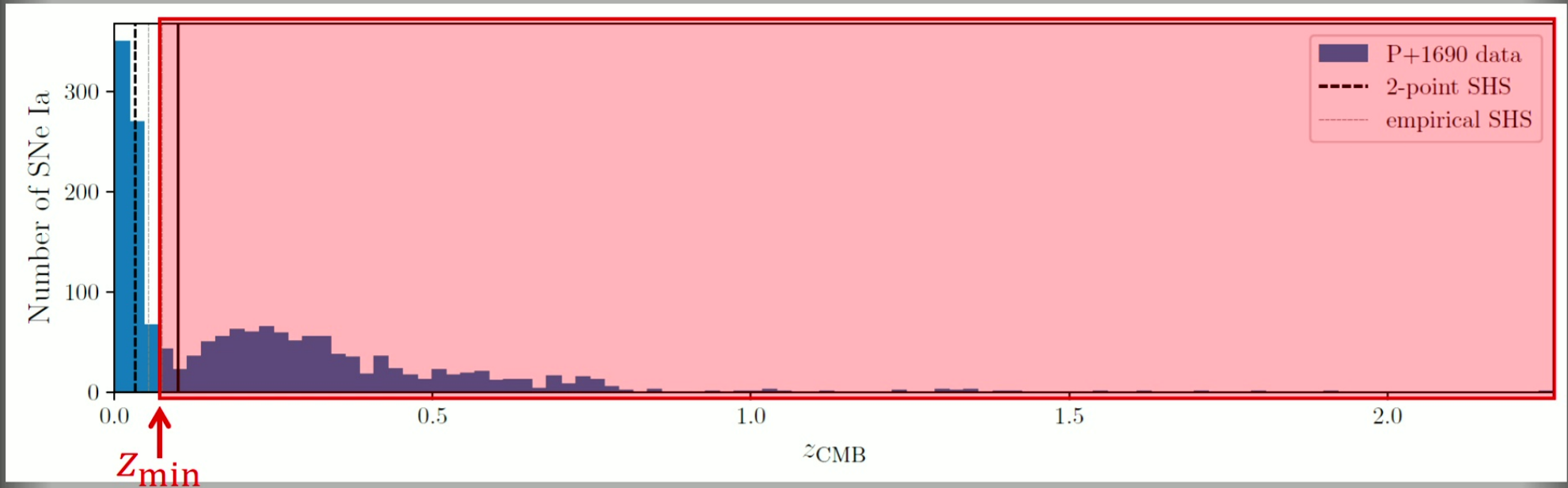
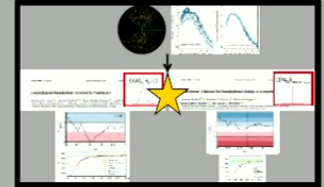
# Likelihood



$$X - \hat{X} = \begin{pmatrix} M_B - \alpha x_1 + \beta c \\ x_1 \\ c \end{pmatrix} - \begin{pmatrix} \mu - \hat{m}_B^* \\ \hat{x}_1 \\ \hat{c} \end{pmatrix} \quad \Bigg| \quad X - \hat{X} = (M_B - \alpha \hat{x}_1 + \beta \hat{c}) - (\mu - \hat{m}_B^*)$$

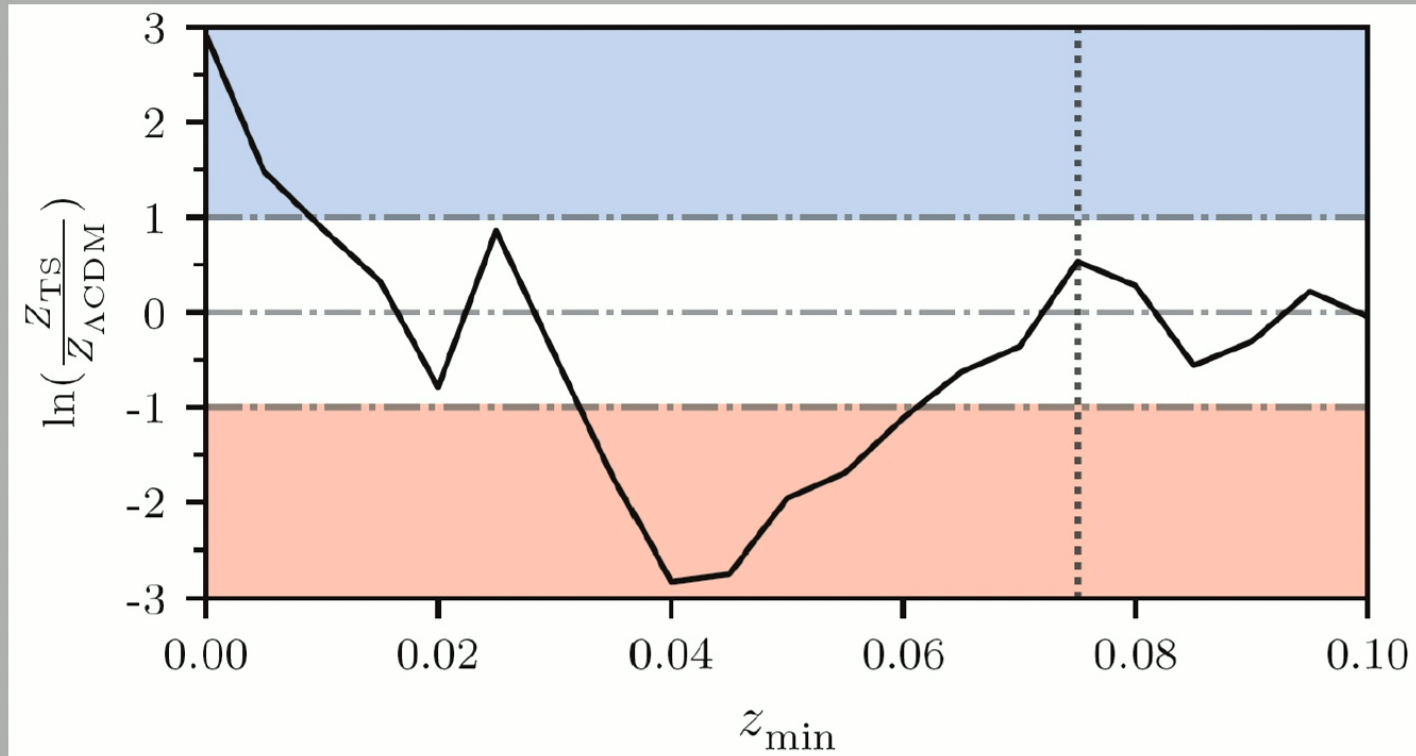
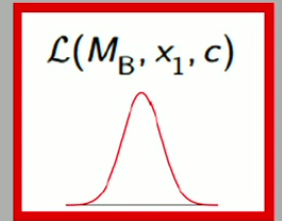
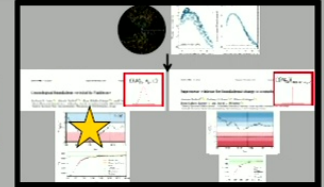
- Likelihood  $\mathcal{L} \propto \exp\left(-\frac{(X-\hat{X})^T \Sigma^{-1} (X-\hat{X})}{2}\right)$
- Covariance  $\Sigma$ :
  - Gaussian variance  $\sigma_{M_B}^2, \sigma_{x_1}^2, \sigma_c^2$
  - Statistical covariance (SALT2 fit)
  - Systematics:
    - Bias corrections
    - Gravitational lensing
    - Redshift measurement uncertainty
    - Peculiar velocities

# Bayesian Analysis

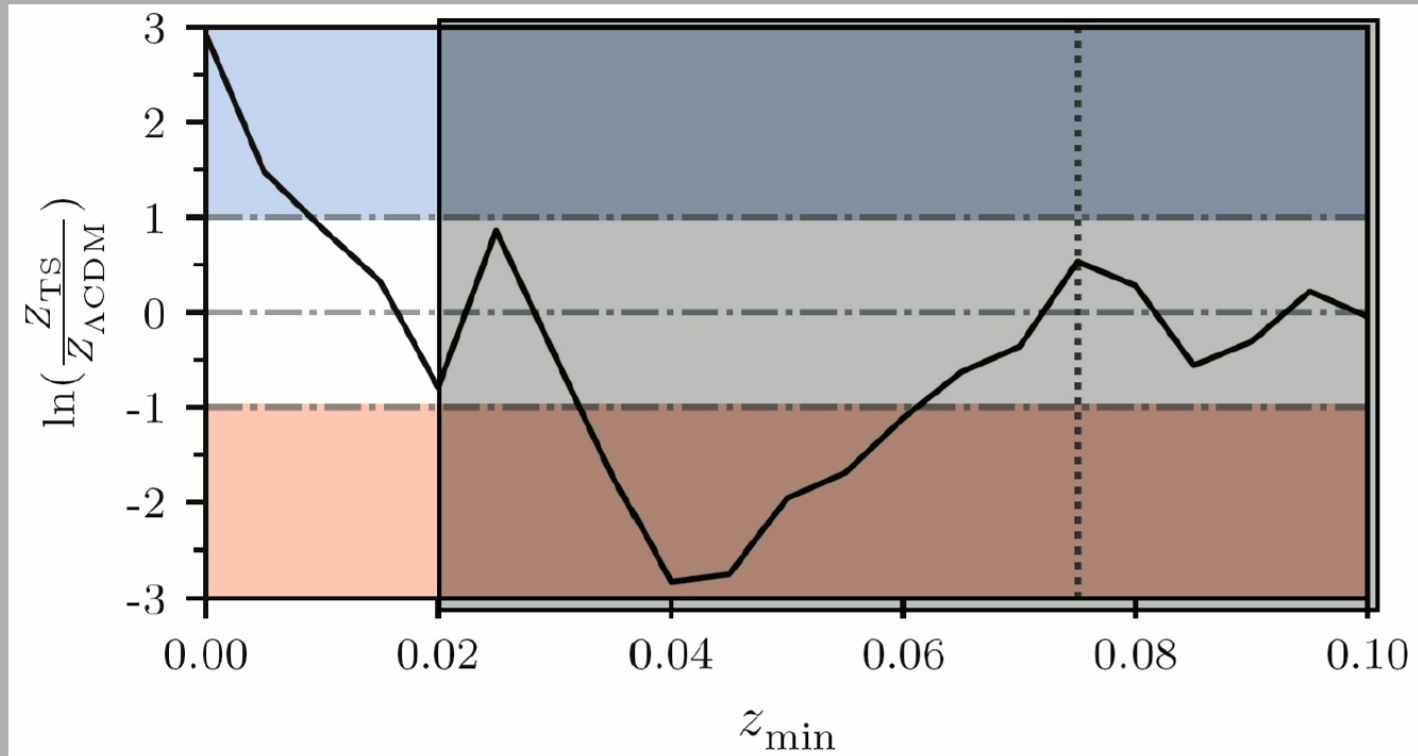
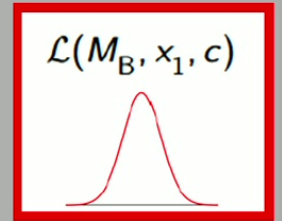
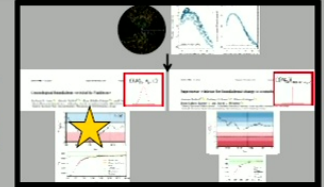




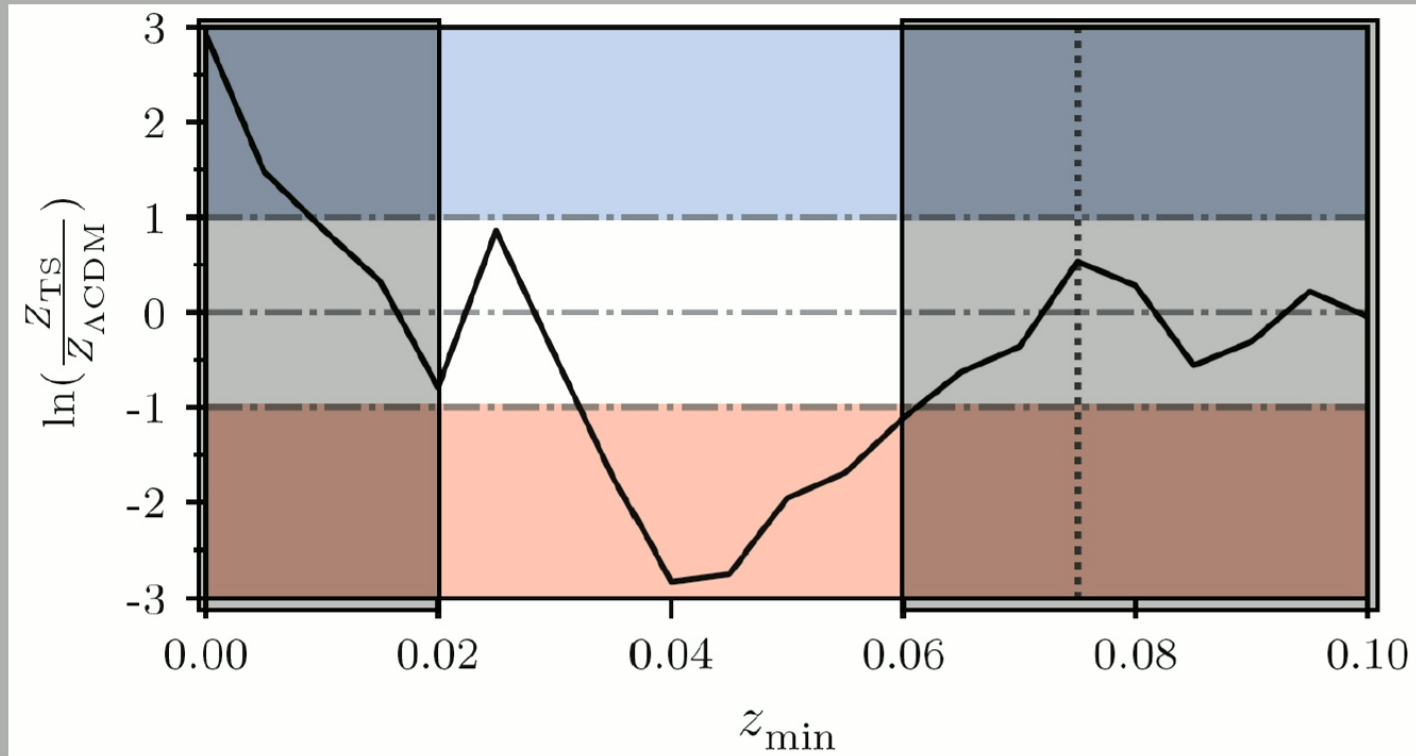
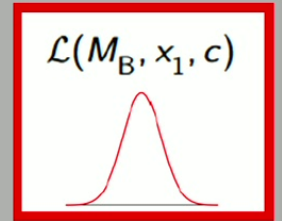
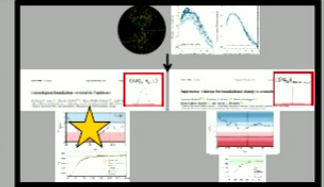
# Bayesian Analysis: Gaussian Likelihood



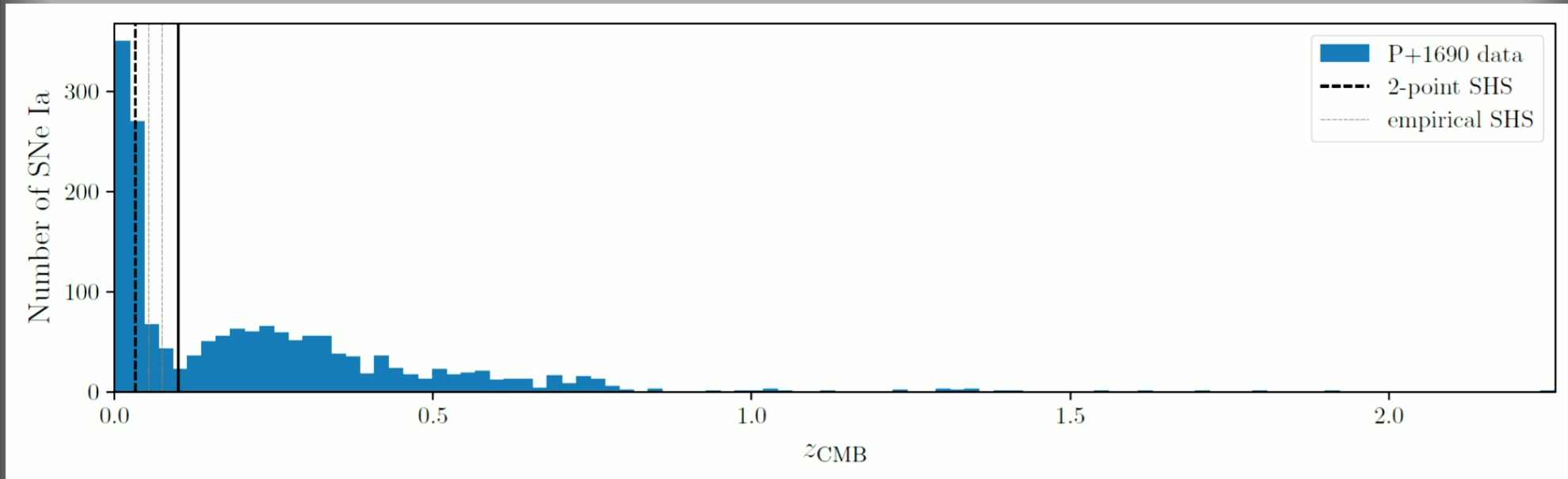
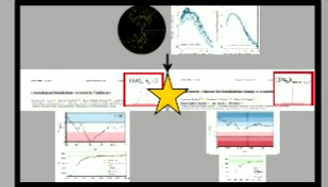
# Bayesian Analysis: Gaussian Likelihood



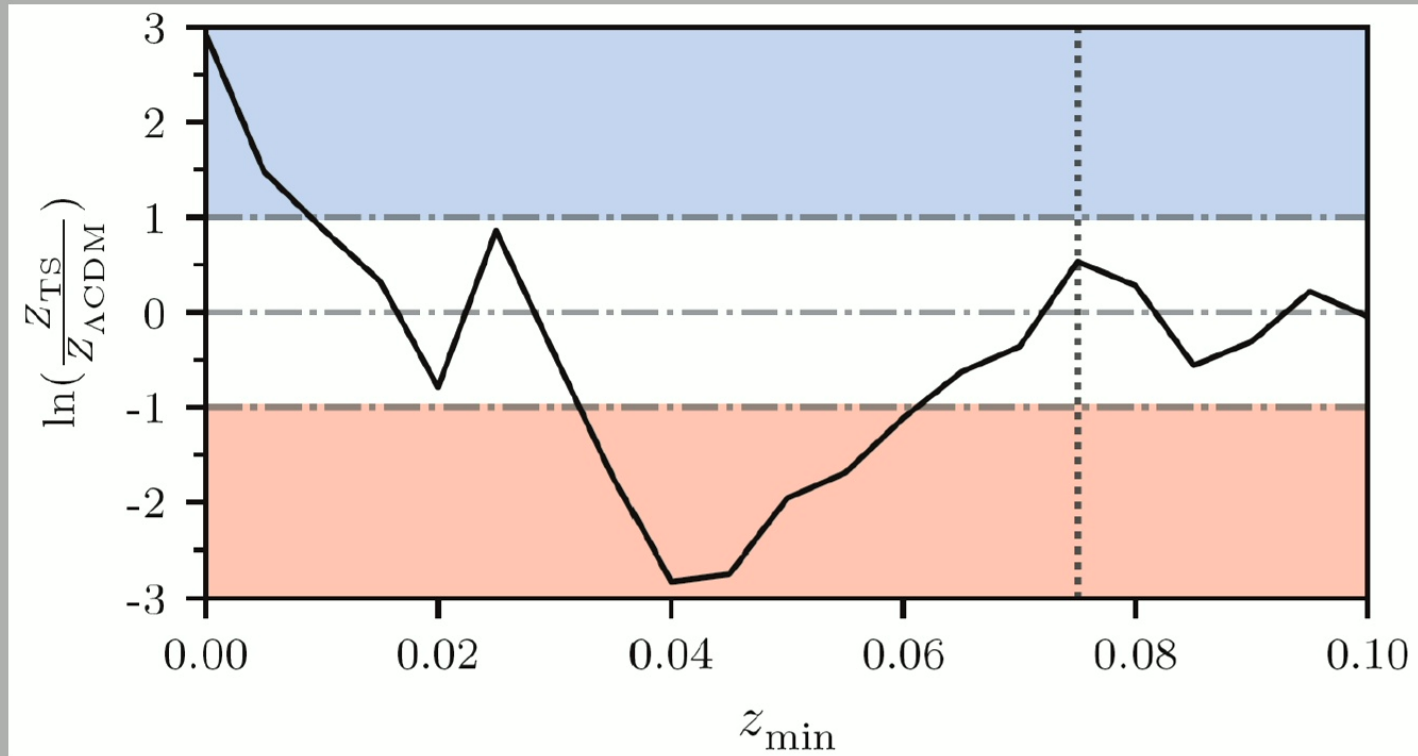
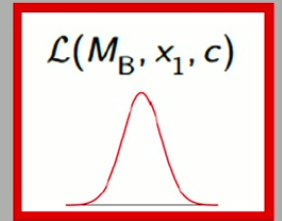
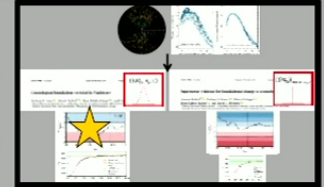
# Bayesian Analysis: Gaussian Likelihood



# Bayesian Analysis

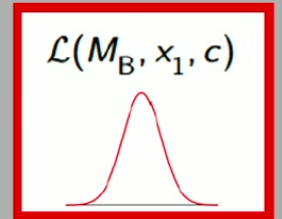
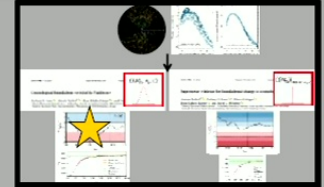


# Bayesian Analysis: Gaussian Likelihood

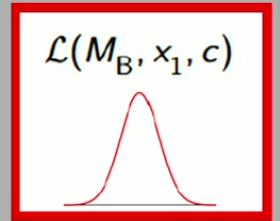
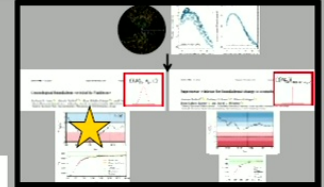
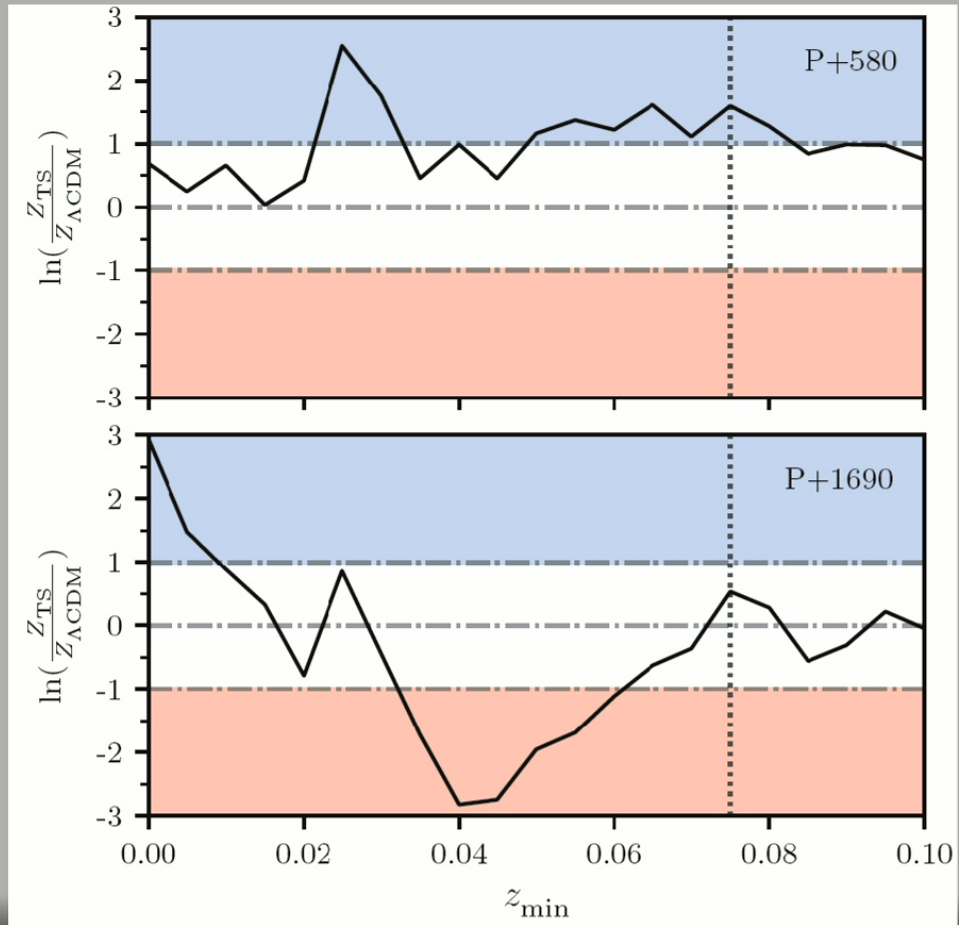


# Comparison to Previous Work

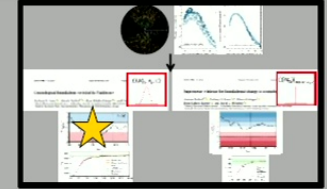
- Dam et al. 2017: JLA catalogue, Gaussian likelihood
- less clear evidence ( $-1 < \ln B \leq 1$ )
- Consider common subsample JLA/Pantheon+ for comparison



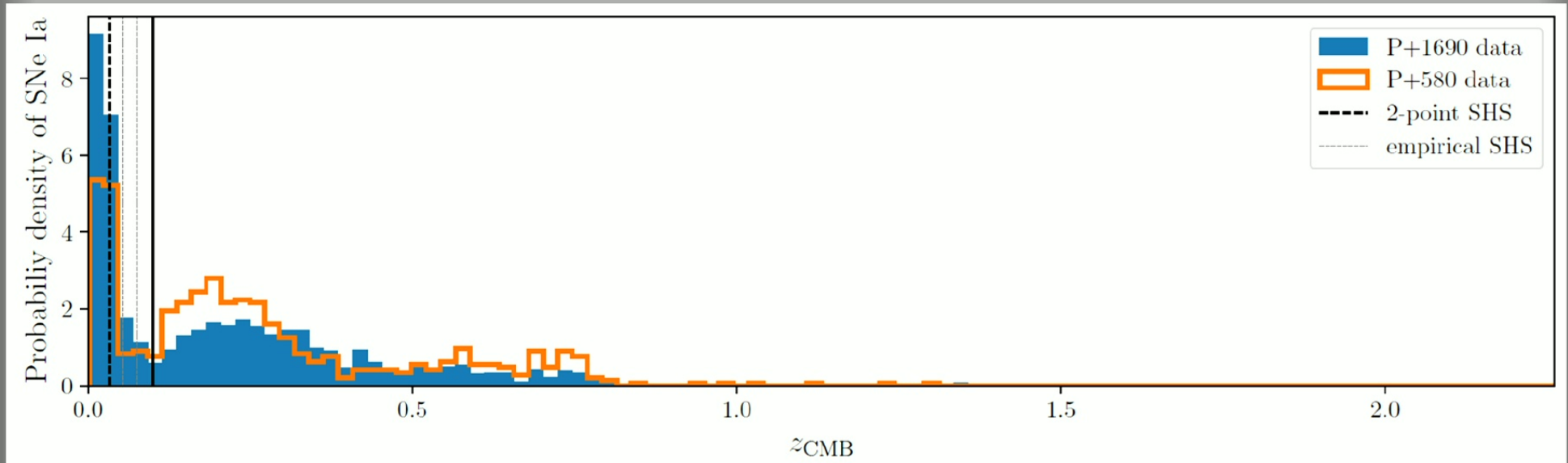
# Comparison to Previous Work



# Sample Dependence

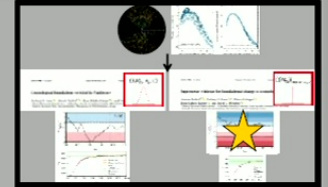
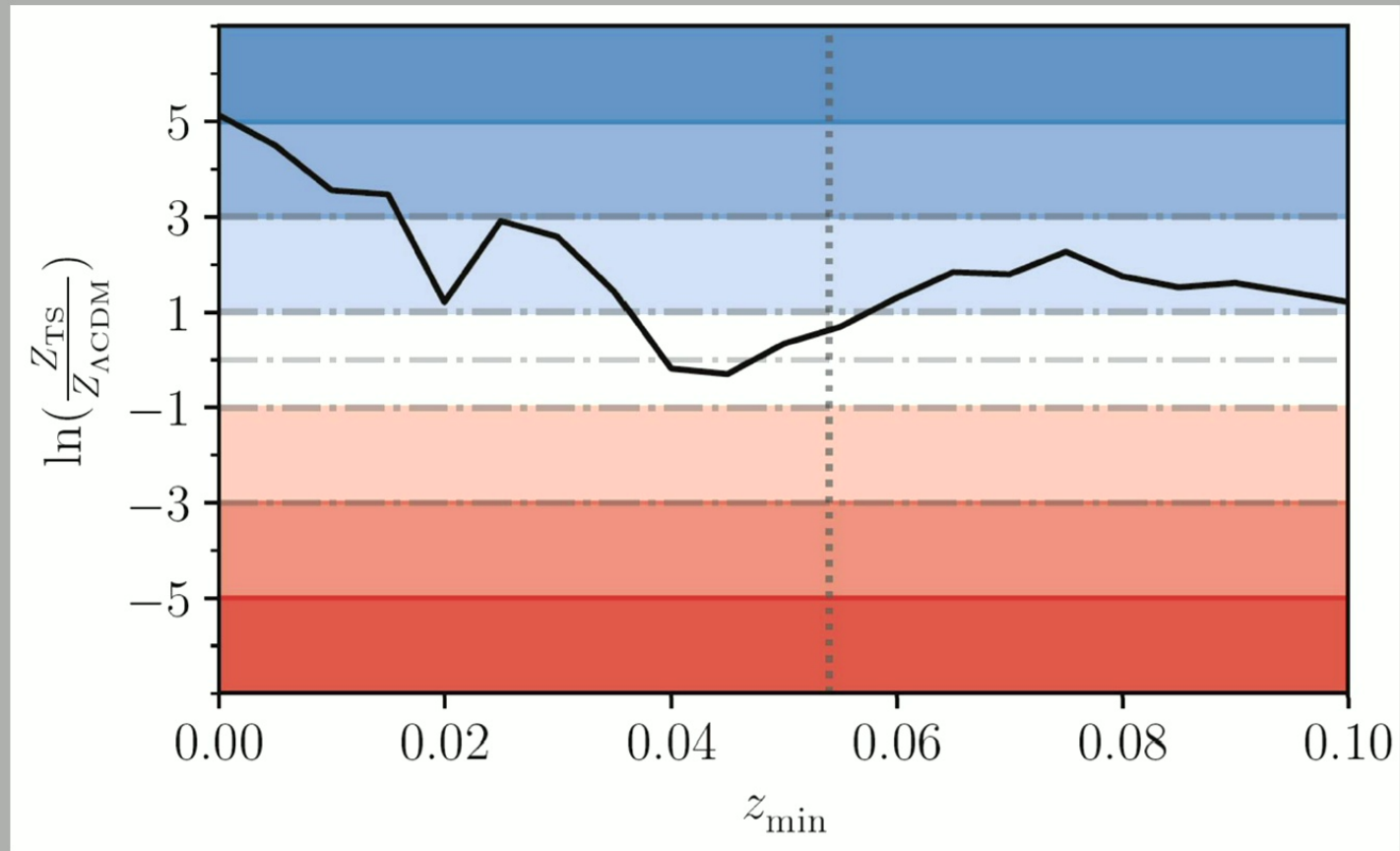


$$\mathcal{L}(M_B, x_1, c)$$



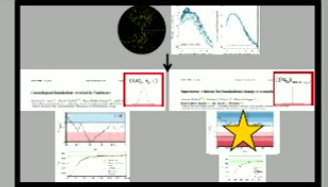
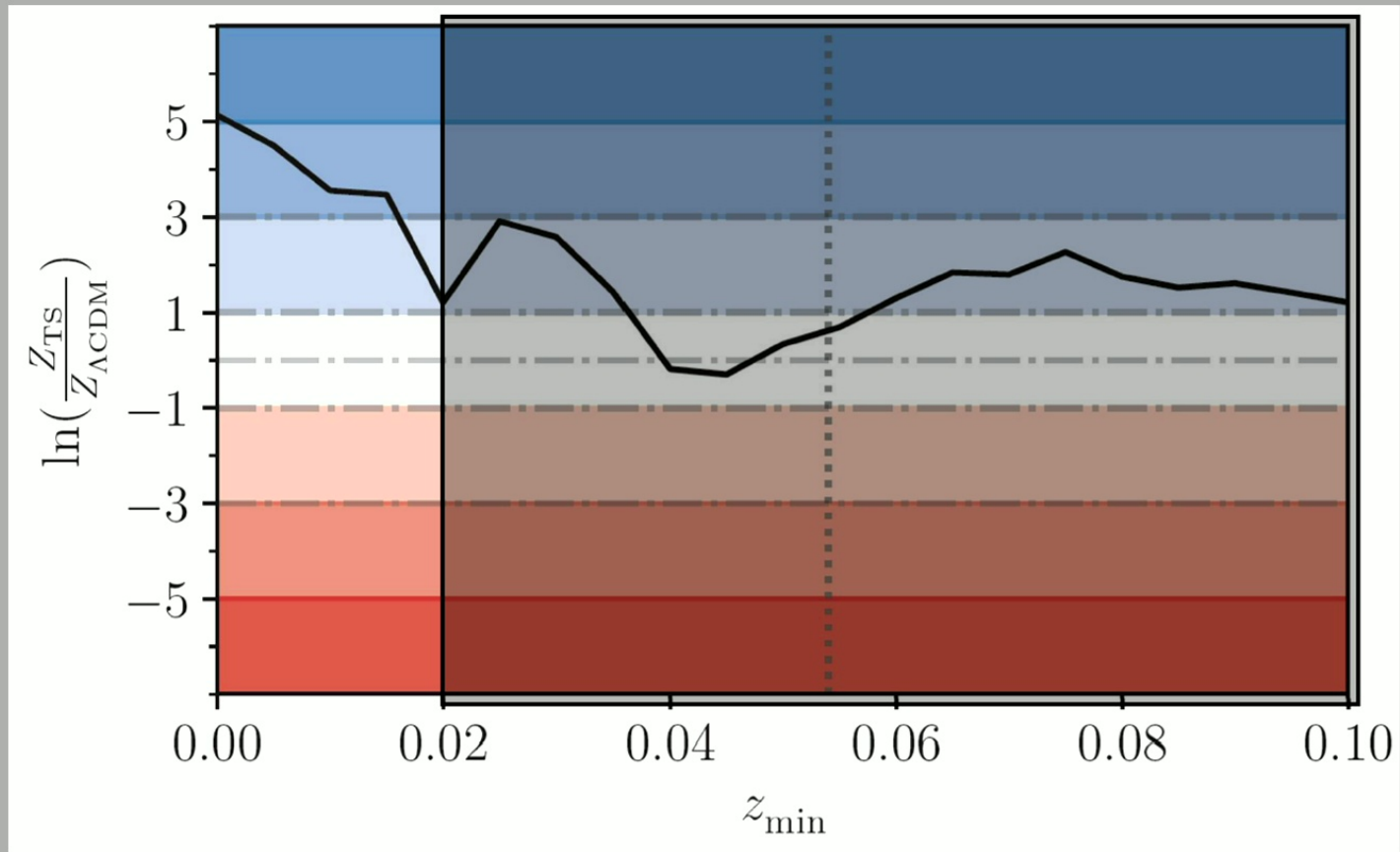


# Bayesian Analysis: Fit Likelihood



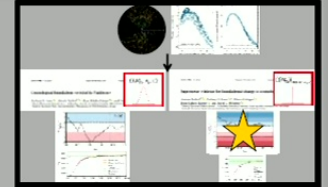
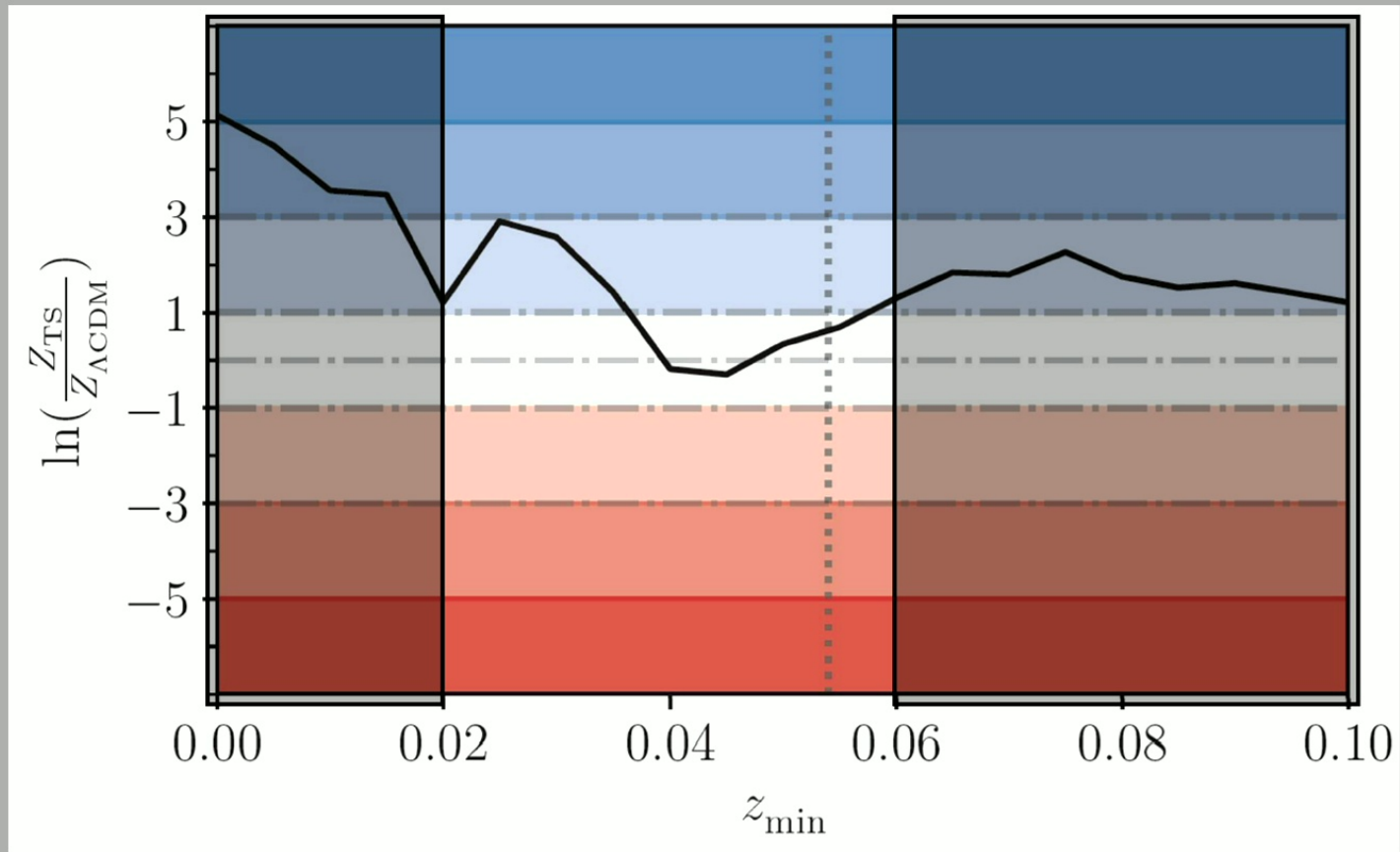
$$\mathcal{L}(M_B) |_{\text{fitted } x_{1,c}}$$

# Bayesian Analysis: Fit Likelihood



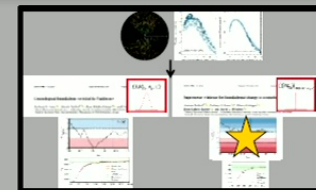
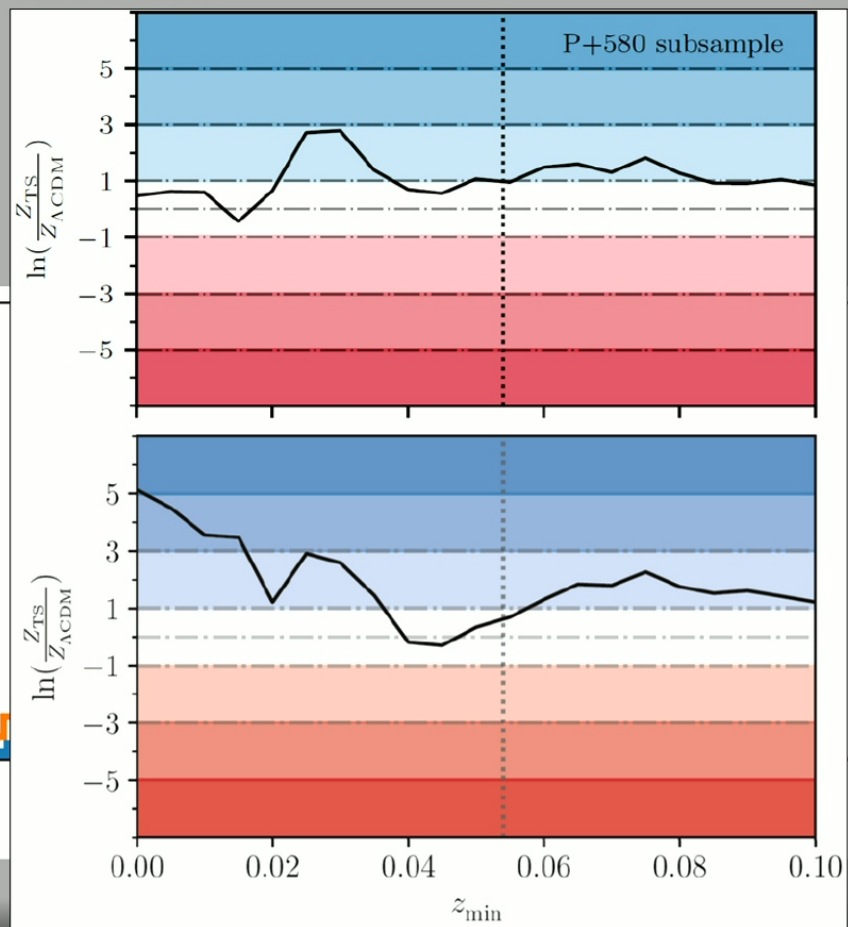
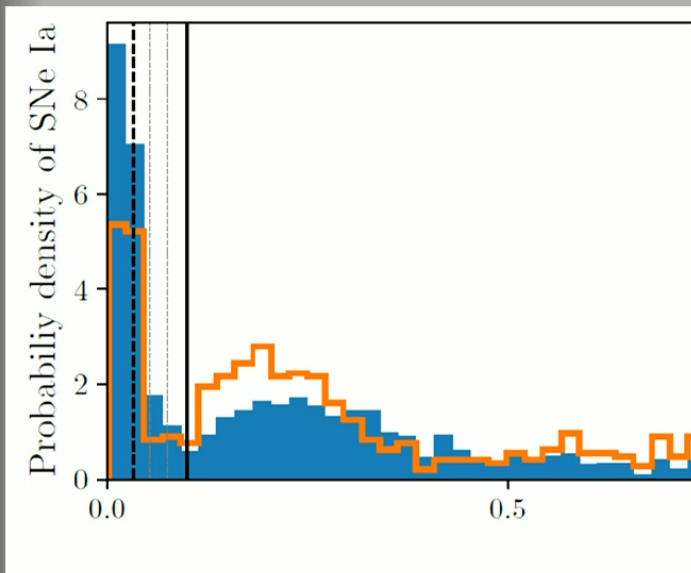
$$\mathcal{L}(M_B) |_{\text{fitted } x_{1,c}}$$

# Bayesian Analysis: Fit Likelihood



$$\mathcal{L}(M_B) |_{\text{fitted } x_{1,c}}$$

# Sample Dependence

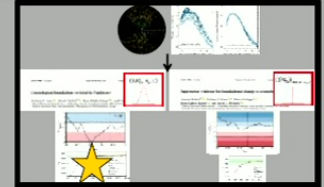


$$\mathcal{L}(M_B) |_{\text{fitted } x_{1,c}}$$

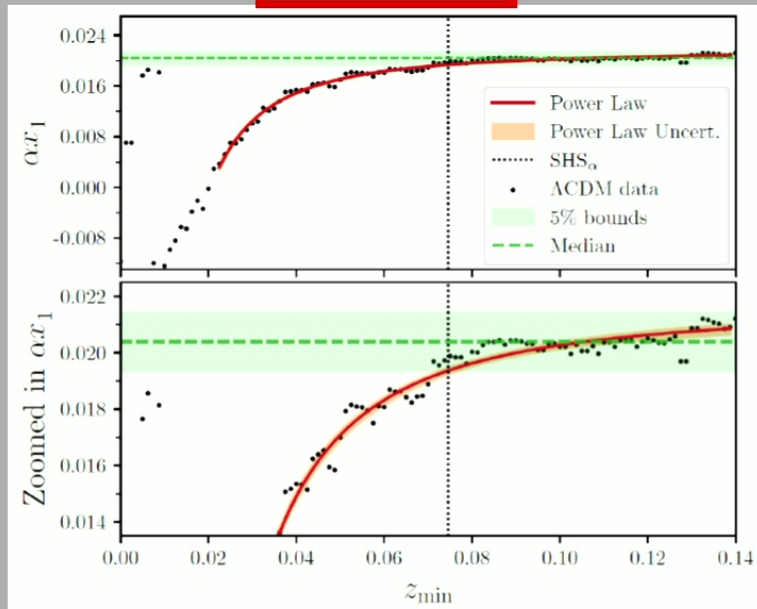
- P+1690 data
- P+580 data
- 2-point SHS
- empirical SHS

2.0

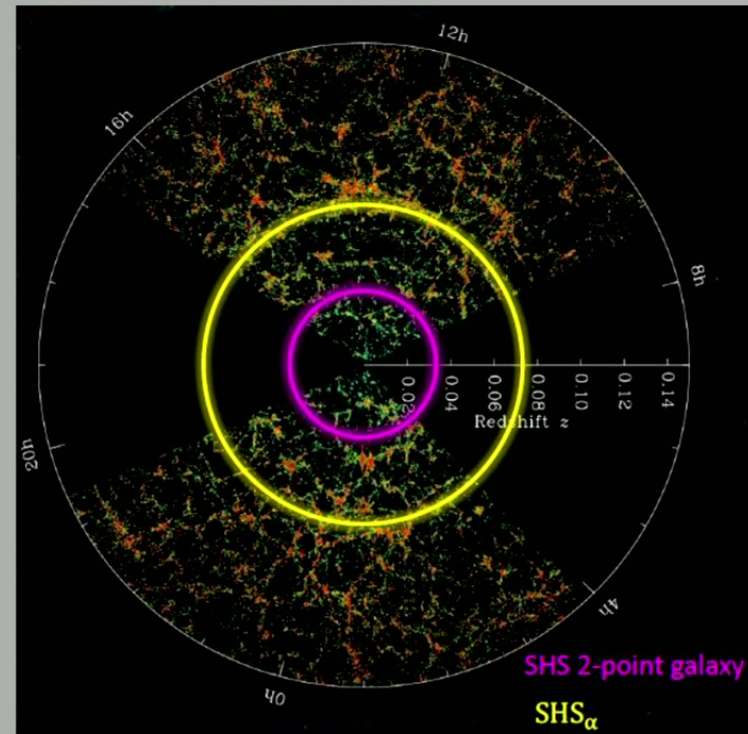
# Statistical Homogeneity



$$\mathcal{L}(M_B, x_1, c)$$

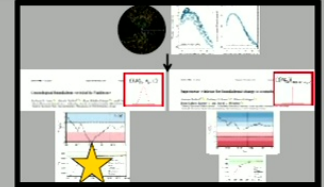


$$SHS_{\alpha} = 0.075^{+0.007}_{-0.009}$$

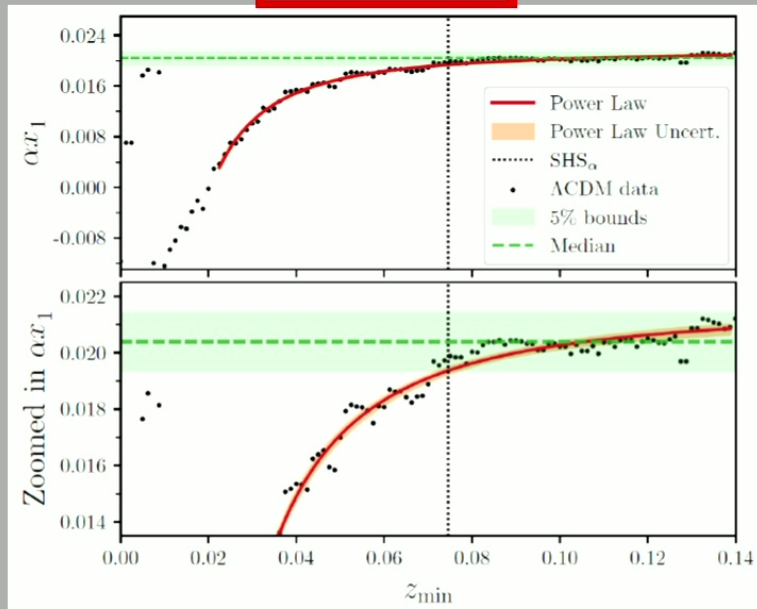


Credit: SDSS and Z. Lane

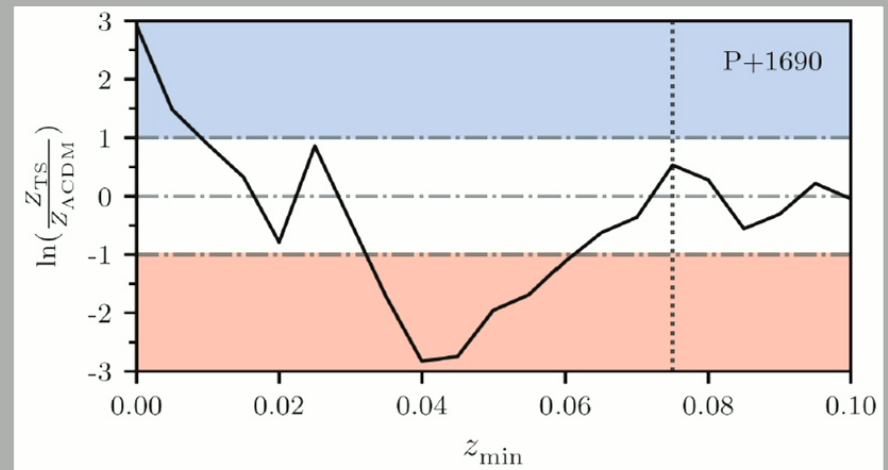
# Statistical Homogeneity



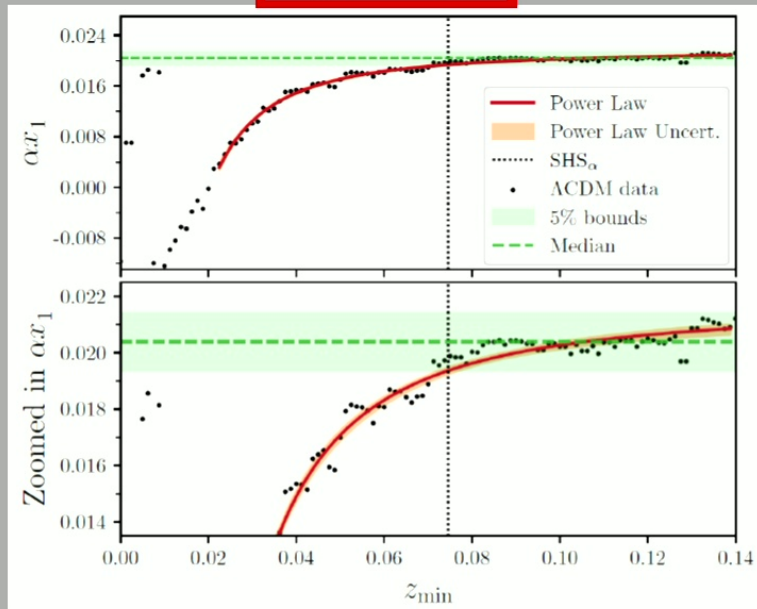
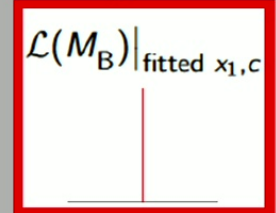
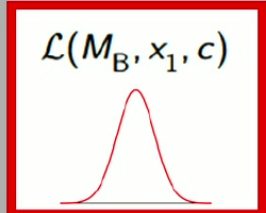
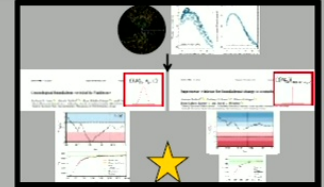
$$\mathcal{L}(M_B, x_1, c)$$



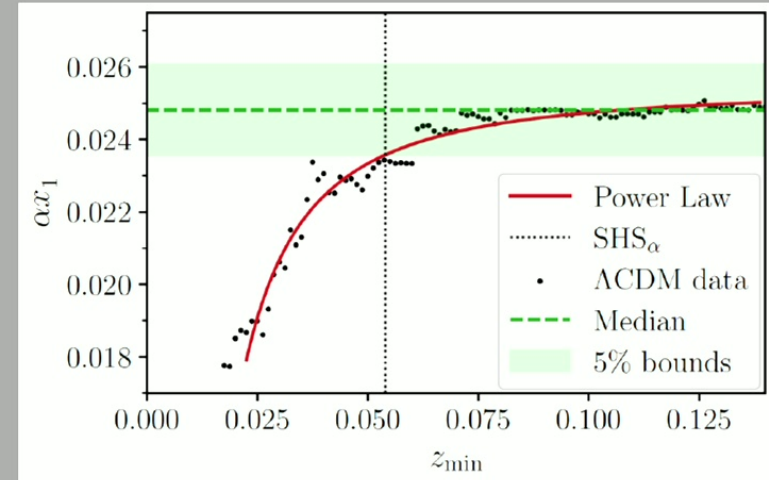
$$SHS_{\alpha} = 0.075^{+0.007}_{-0.009}$$



# Statistical Homogeneity

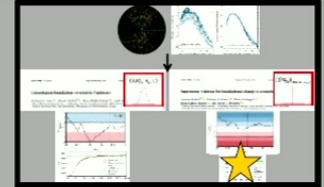


$$\text{SHS}_\alpha = 0.075^{+0.007}_{-0.009}$$

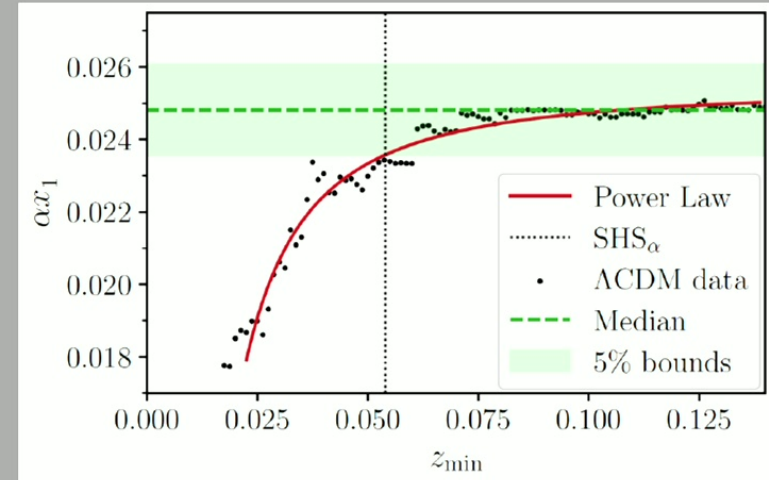
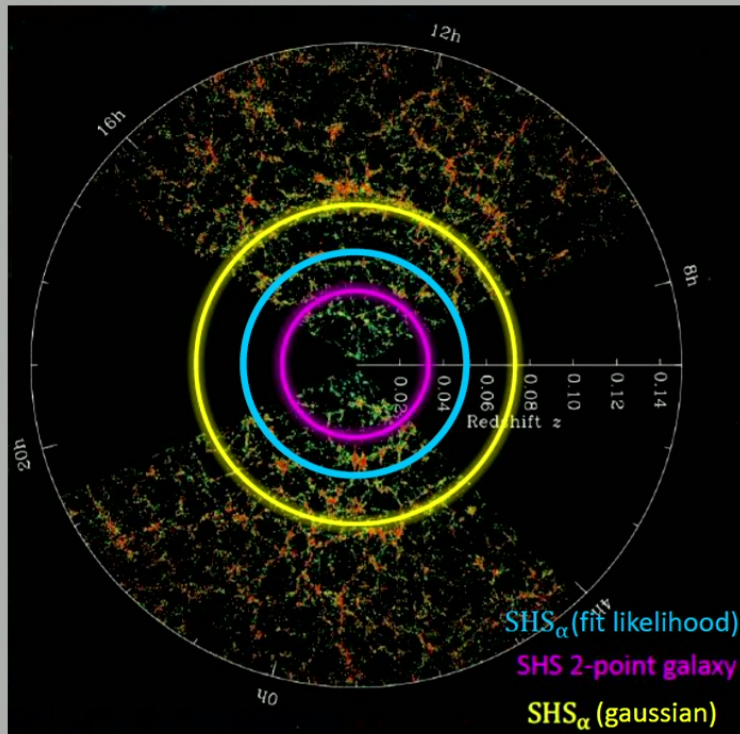


$$\text{SHS}_\alpha = 0.054^{+0.007}_{-0.012}$$

# Statistical Homogeneity



$$\mathcal{L}(M_B) |_{\text{fitted } x_{1,c}}$$

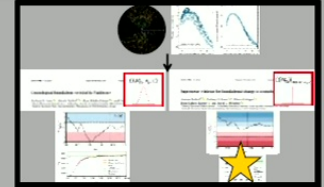


$$SHS_\alpha = 0.054^{+0.007}_{-0.012}$$

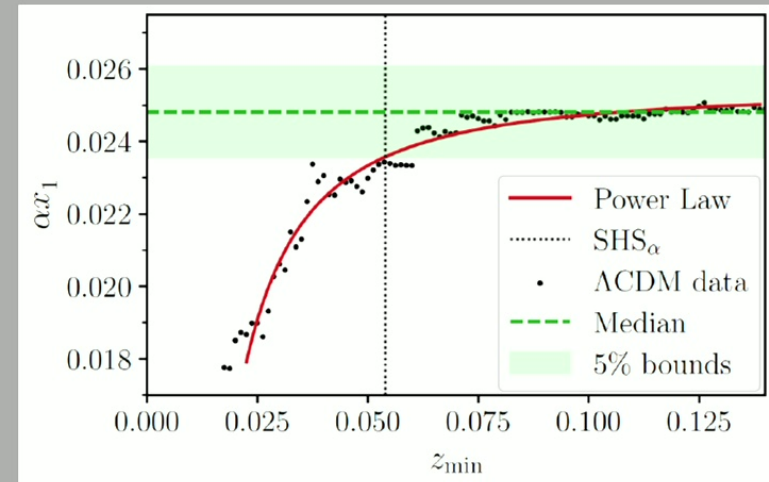
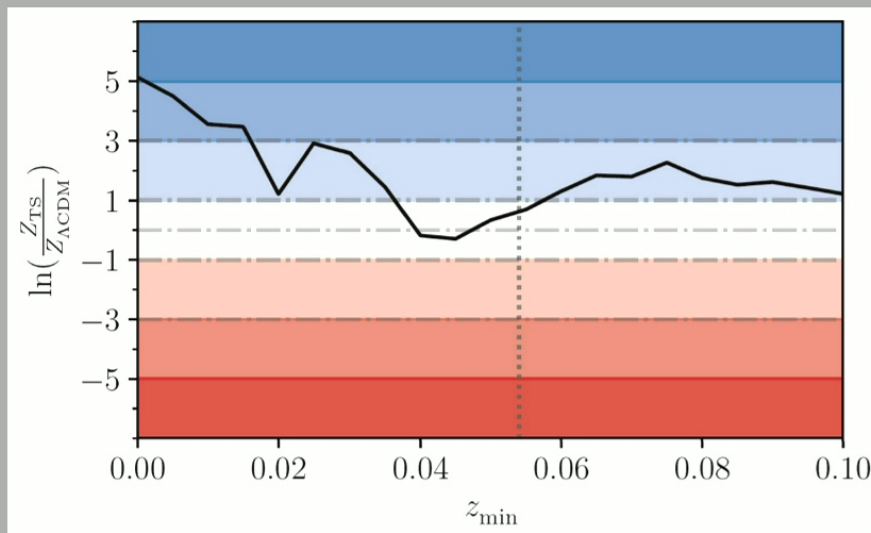
Credit: SDSS and Z. Lane



# Statistical Homogeneity

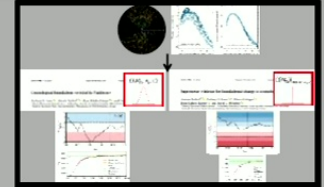


$$\mathcal{L}(M_B) |_{\text{fitted } x_{1,c}}$$



$$\text{SHS}_\alpha = 0.054^{+0.007}_{-0.012}$$

# Conclusions



- Assumptions on the distribution of  $x_1$  and  $c$  influences the Bayesian evidence
- Analysis based on fit likelihood favours timescape cosmology
- Particularly important in low-redshift regime
- Empirical SHS gives higher values than usually assumed
- Dependence on redshift-distribution of the sample: see Lane et al. (arXiv:2311.01438)
- Future work:
  - Likelihood with non-gaussian distribution
  - Reanalysis with more SNe from DES 5Y sample
  - Investigation of models to include more corrections



arXiv:2311.01438



arXiv:2412.15143