

**Title:** Millihertz Gravitational Waves: Challenges and opportunities in the LISA Era

**Speakers:** Lorenzo Speri

**Collection/Series:** Strong Gravity

**Subject:** Strong Gravity

**Date:** January 30, 2025 - 1:00 PM

**URL:** <https://pirsa.org/25010074>

**Abstract:**

In January 2024, the Laser Interferometer Space Antenna (LISA) mission was officially adopted by the European Space Agency, marking a new era in gravitational wave astronomy. LISA will be the first space-based gravitational wave detector, designed to explore the cosmos in the millihertz frequency range. This talk will present the mission's key scientific objectives and how the scientific community is preparing for the exploitation of LISA data. I will discuss the anticipated source types and the fundamental questions they could help answer. Then, we will focus on Extreme Mass Ratio Inspirals (EMRIs), a class of sources where small compact objects orbit the massive black holes at the centers of galaxies. These systems hold immense scientific potential for the LISA mission, as they encode a detailed map of the spacetime around the massive black hole. I will discuss how future detections of EMRIs can be used to constrain parameters related to accretion disks and modifications of General Relativity. Finally, I will highlight the path forward in preparing for LISA's launch and how to get involved in contributing to the mission scientific success.

# Millihertz Gravitational Waves: Challenges and opportunities in the LISA Era

Perimeter Institute, Strong Gravity Seminar

Lorenzo Speri

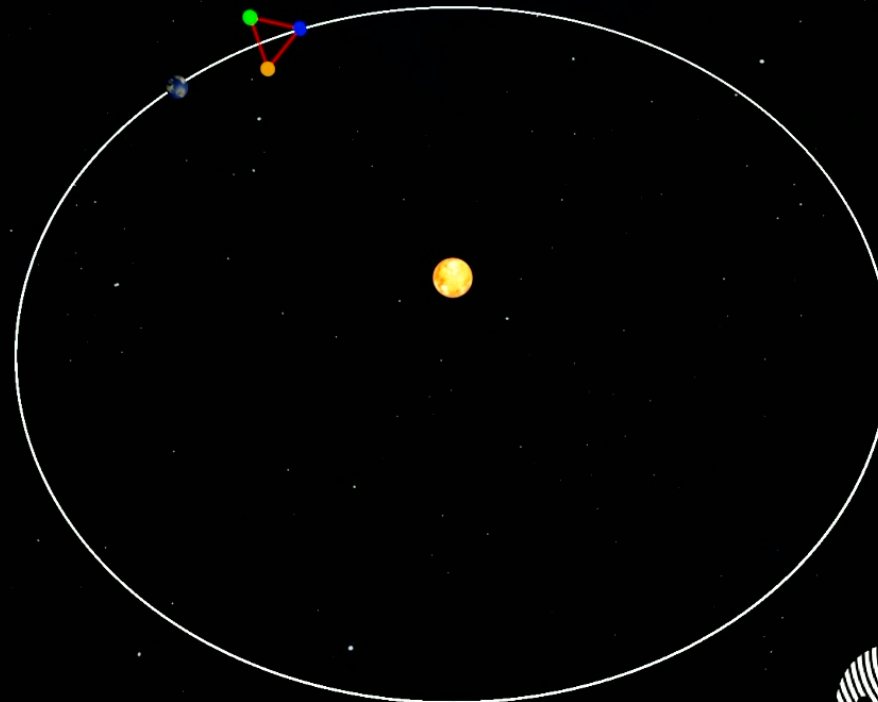


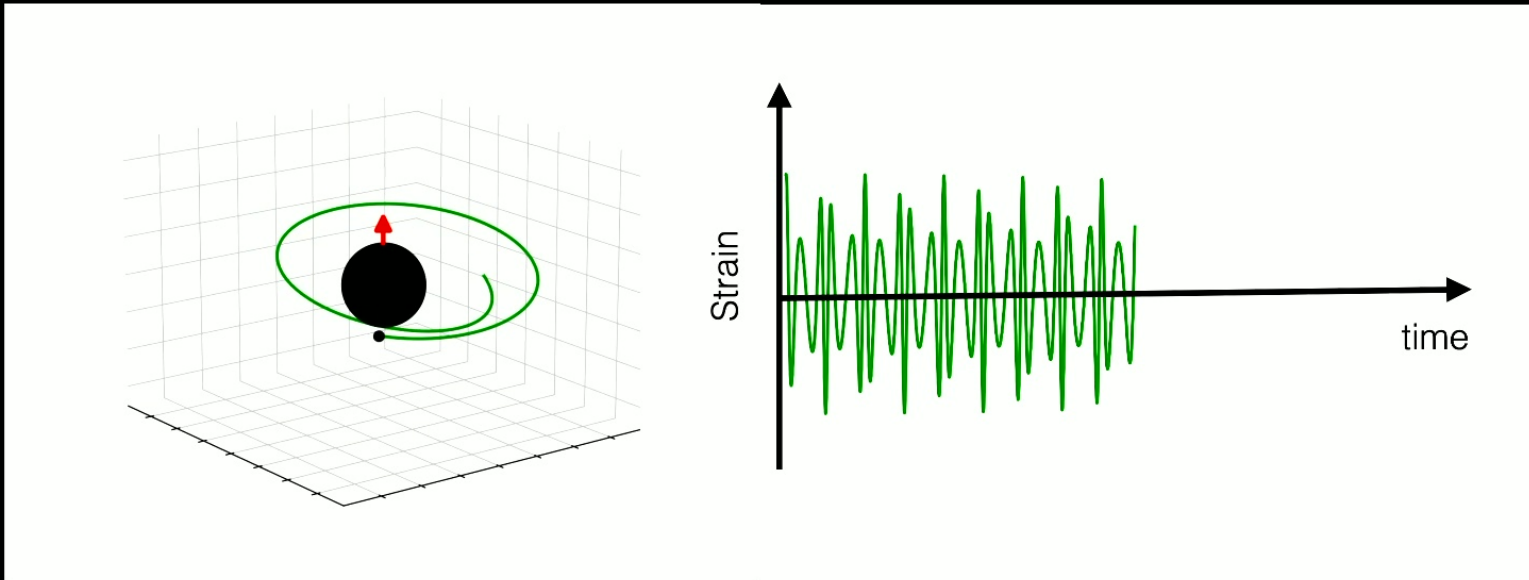
Image credit: Strub

# Talk Outline

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1. Gravitational Wave Data Analysis
2. The Laser Interferometer Space Antenna
3. Prospects and challenges of the LISA mission
4. Extreme Mass Ratio Inspirals
5. Conclusions

# Gravitational Waves



Frequency evolution  $\longleftrightarrow$  Binary orbital dynamics

# How do we find GW signals?

Data = Signal ( parameters ) + Noise

$$\text{Signal} (a, f, \dot{f}) = a \cos \left[ 2\pi t (f + \dot{f}t) \right]$$

$$\text{log-likelihood} \propto - \frac{|\text{Data} - \text{Signal}|^2}{2 \sigma_n^2}$$

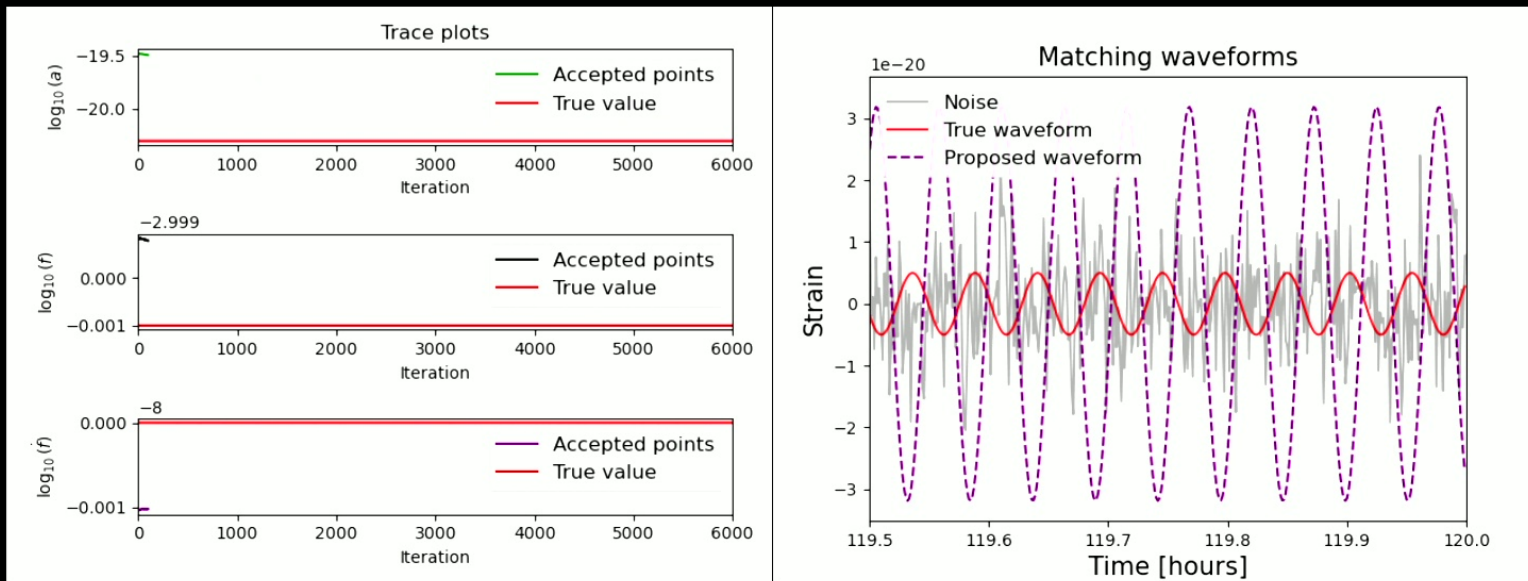


Image credit: O. Burke

# How do we estimate GW parameters?

Likelihood x Prior / Evidence = Posterior Distribution

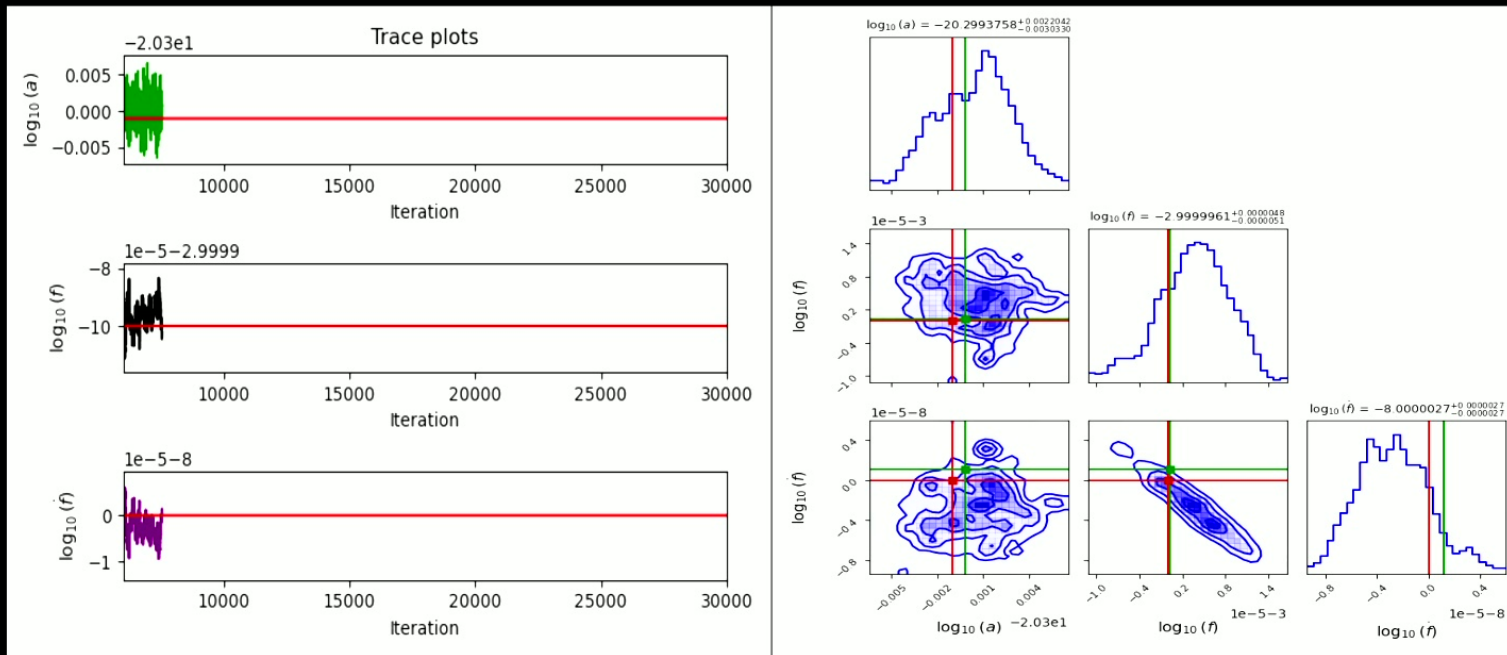


Image credit: O. Burke

# How do we estimate GW parameters?

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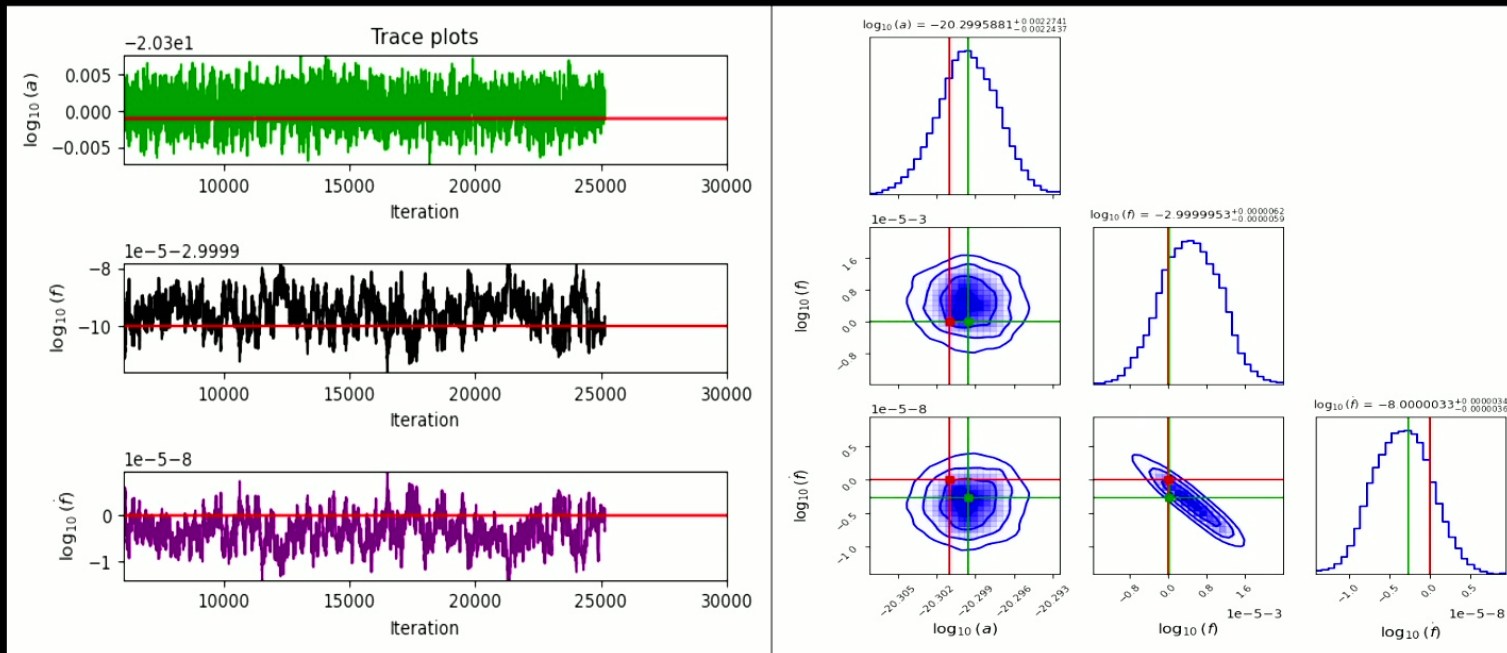
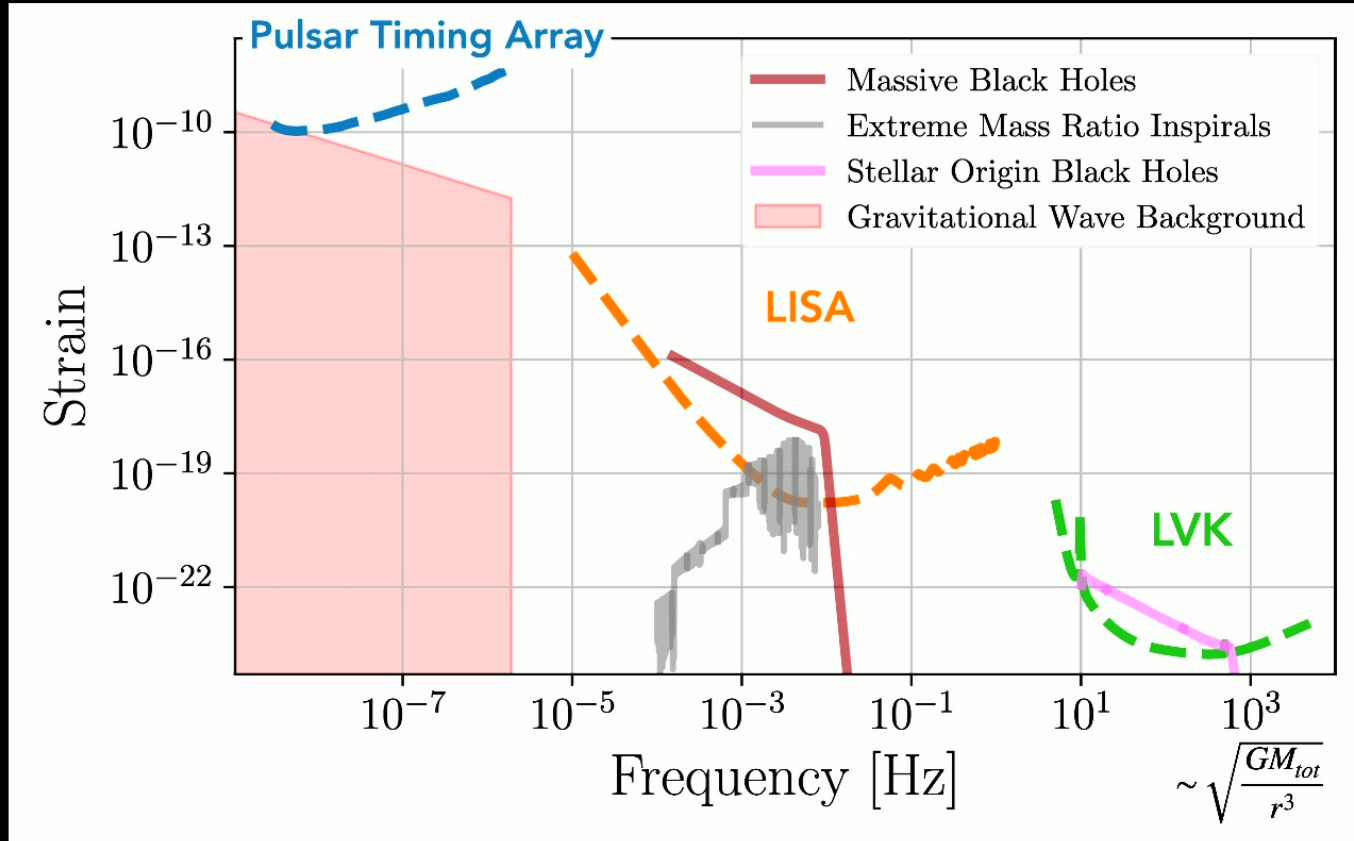


Image credit: O. Burke

# Gravitational Wave Spectrum

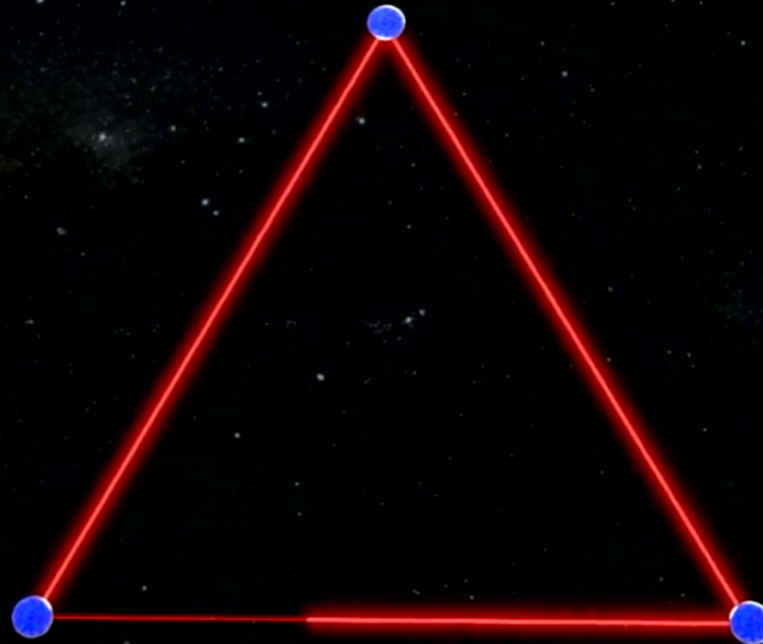
GW Strain  $h$  induces a change in the detector arms  $\frac{\Delta L}{L} \sim h_{GW}$





# The Laser Interferometer Space Antenna

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# The Laser Interferometer Space Antenna



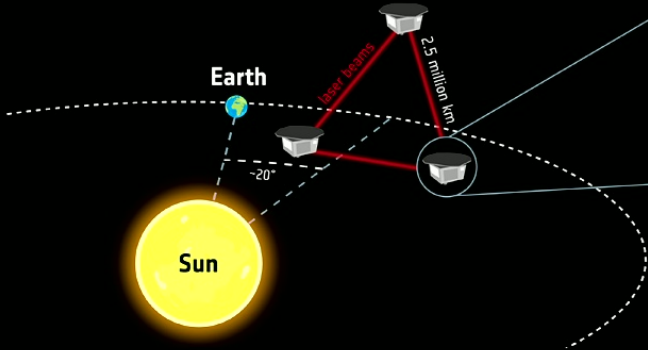
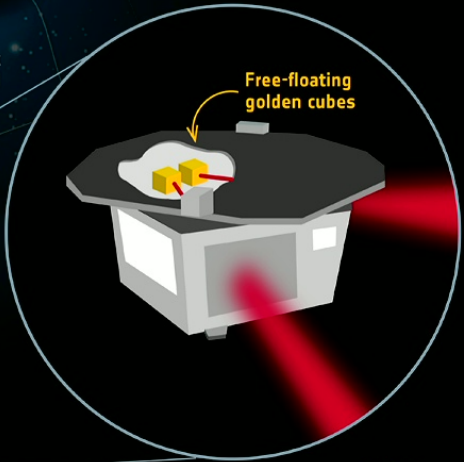
## LISA - LASER INTERFEROMETER SPACE ANTENNA

Gravitational waves are ripples in spacetime that alter the distances between objects. LISA will detect them by measuring subtle changes in the distances between **free-floating cubes** nestled within its three spacecraft.

3 identical spacecraft exchange **laser beams**. Gravitational waves change the distance between the **free-floating cubes** in the different spacecraft. This tiny change will be measured by the laser beams.

\* Changes in distances travelled by the laser beams are not to scale and extremely exaggerated

Powerful events such as **colliding black holes** shake the fabric of spacetime and cause gravitational waves



# The Laser Interferometer Space Antenna

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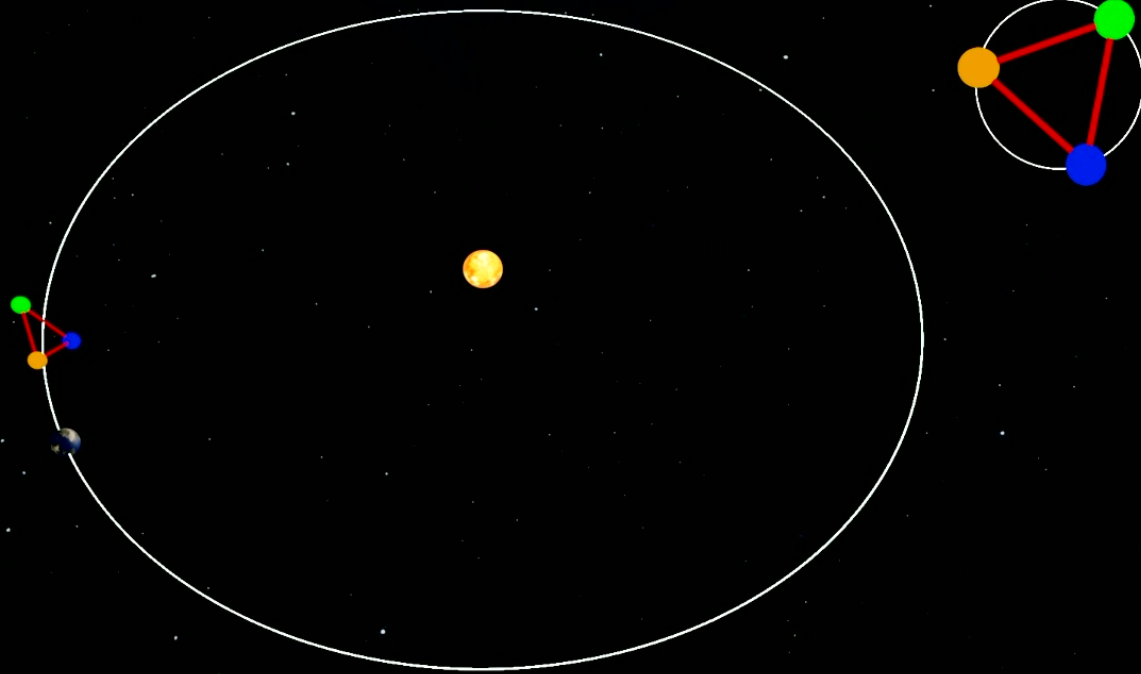
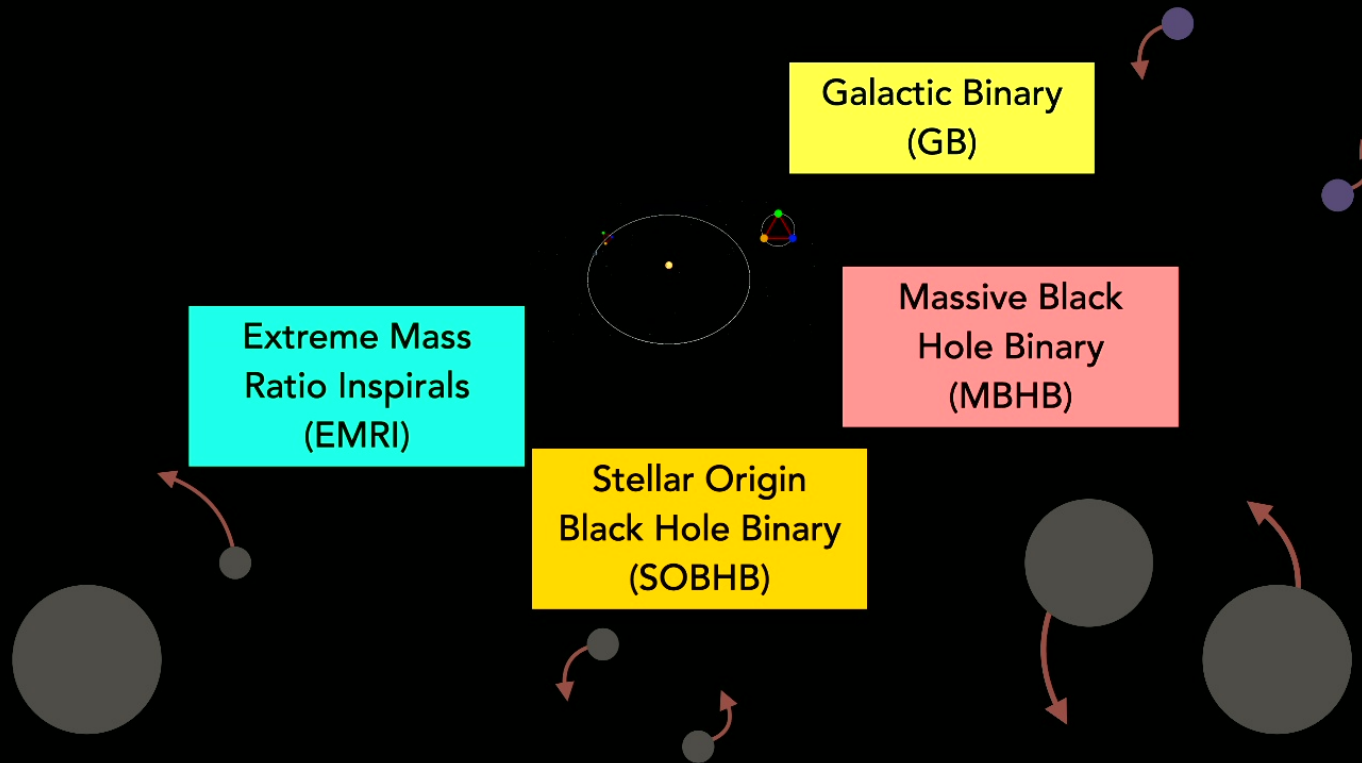
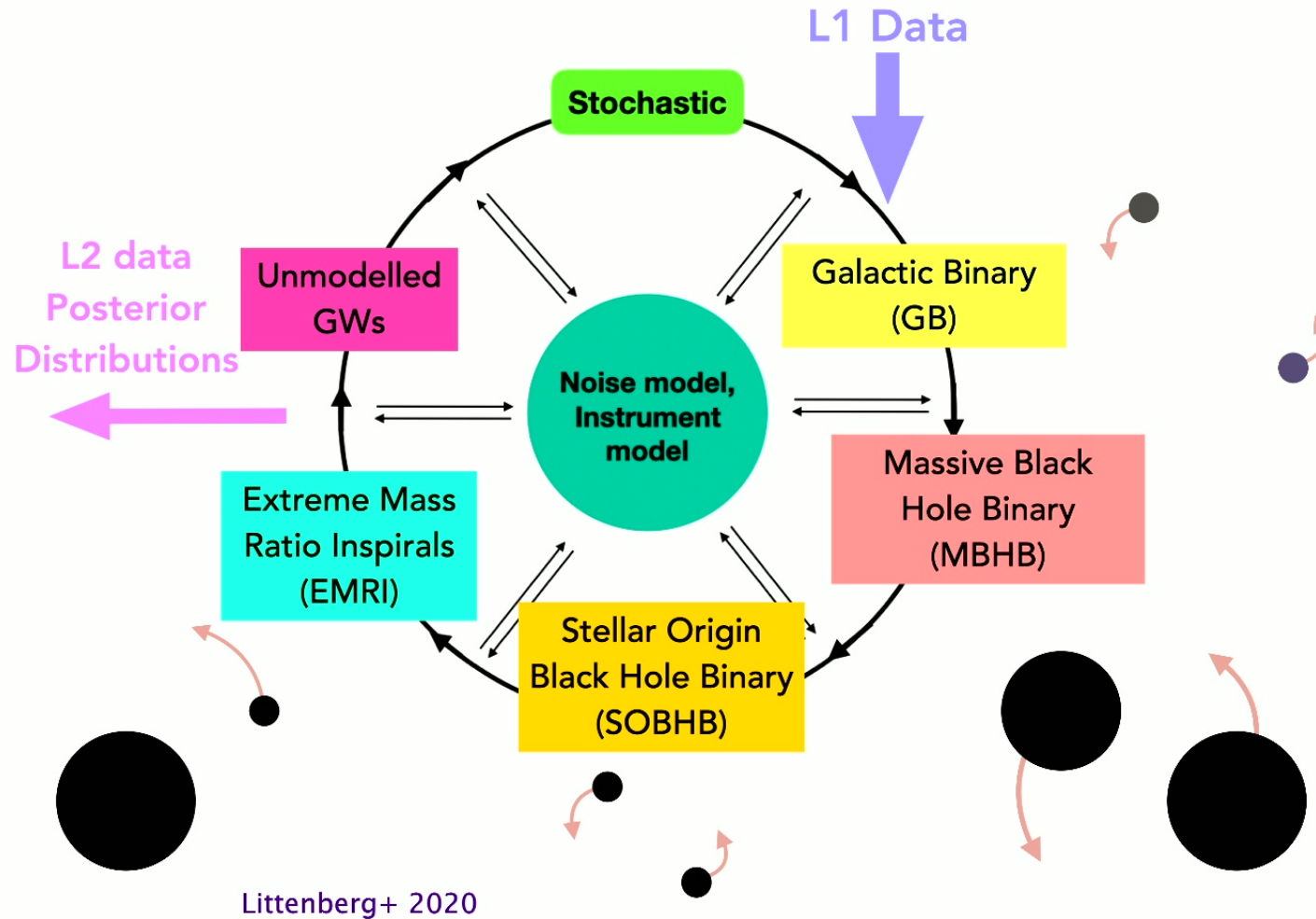


Image credit: Strub

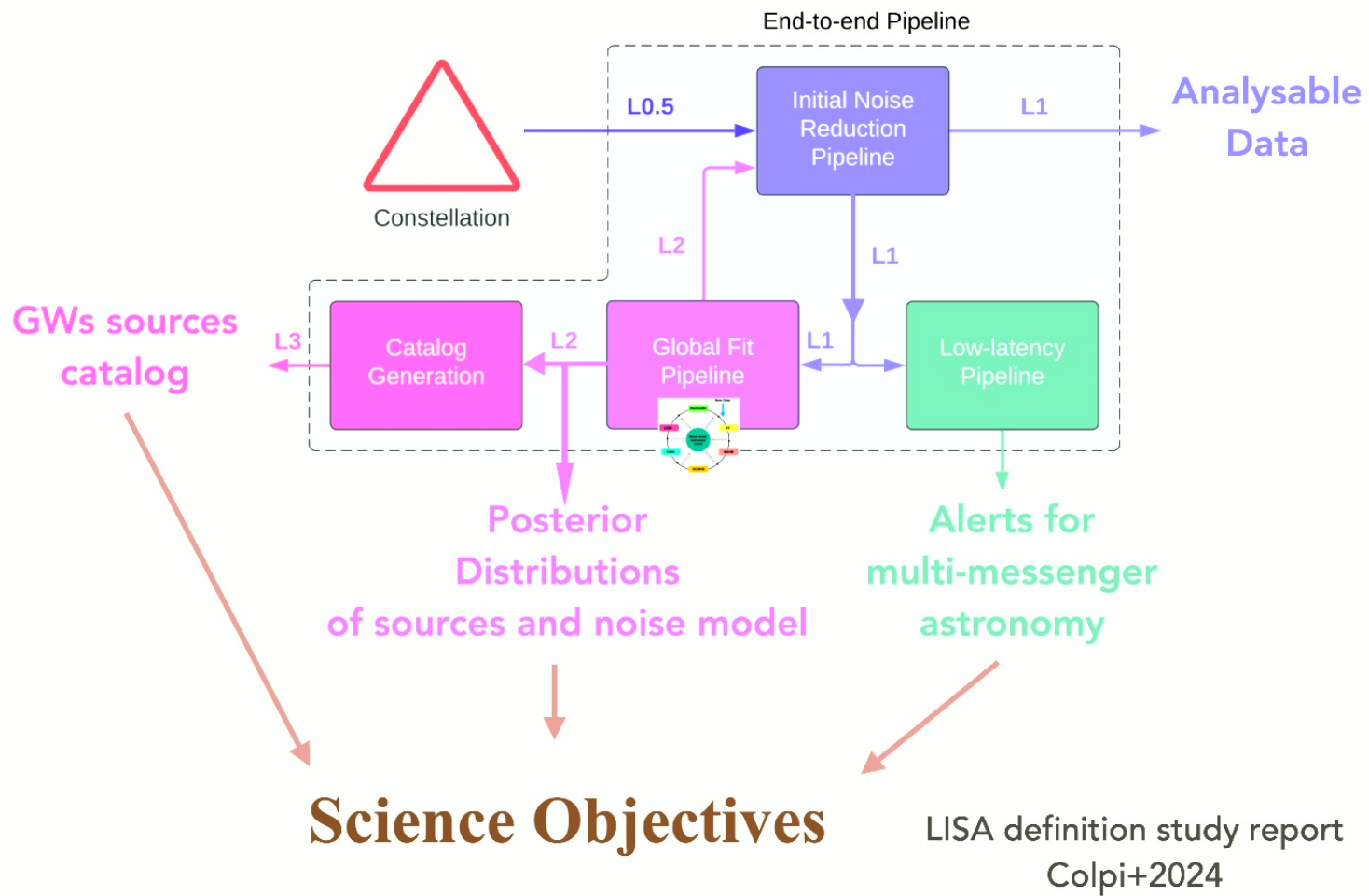
# The Laser Interferometer Space Antenna



# The LISA Global Fit



# LISA data analysis



# Prospects: Science Objectives

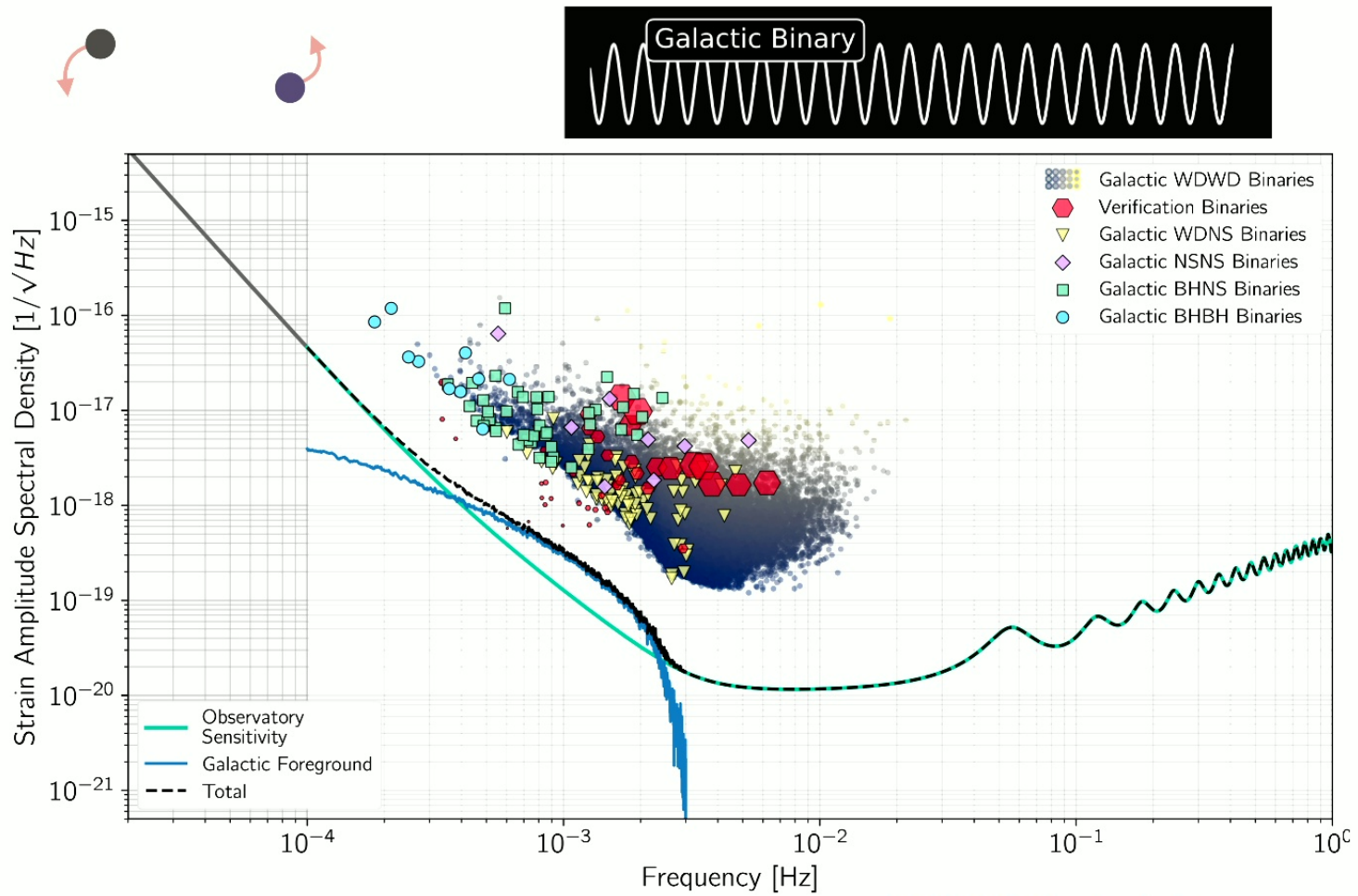
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1. Study the formation and evolution of **compact binary stars** and the structure of the Milky Way Galaxy
2. Trace the origins, growth and merger histories of **massive Black Holes** across cosmic epochs
3. Probe the properties and immediate environments of Black Holes in the local Universe using **extreme mass-ratio inspirals** and **intermediate mass-ratio inspirals**
4. Understand the astrophysics of **stellar-origin Black Holes**
5. Explore the **fundamental nature of gravity** and Black Holes
6. Probe the rate of **expansion of the Universe** with standard sirens
7. Understand **stochastic gravitational wave backgrounds** and their implications for the early Universe and TeV-scale particle physics
8. Search for gravitational wave bursts and **unforeseen sources**

LISA Definition Study Report



# Galactic Binaries



LISA Definition Study Report

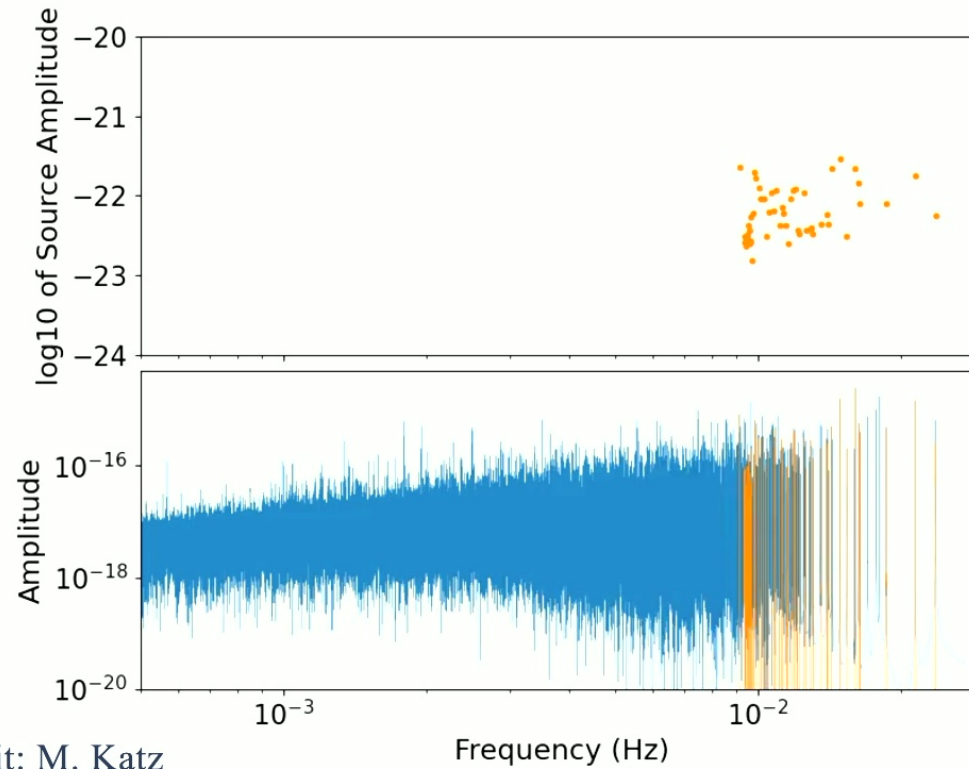


# Galactic Binaries

always in band quasi-monochromatic signals

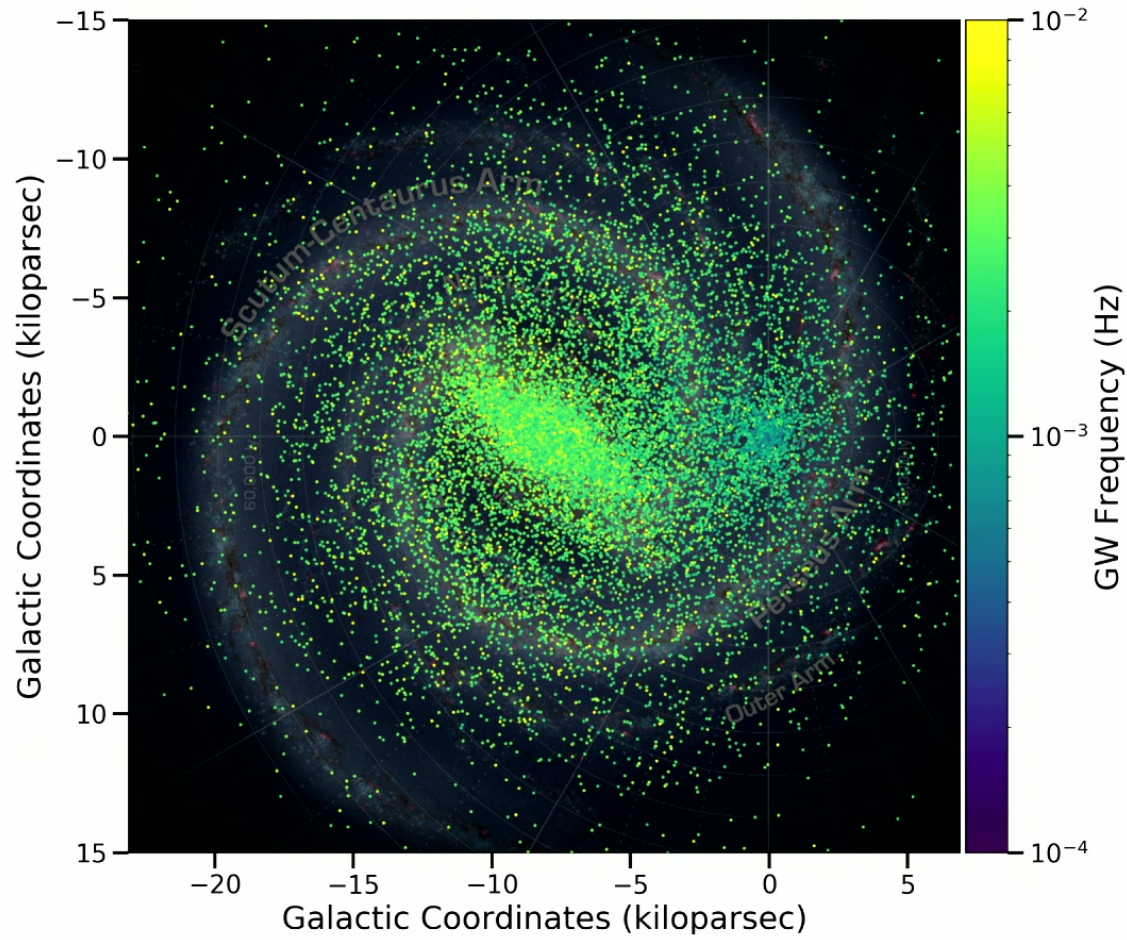
$10^6$  sources

$10^4$  resolvable

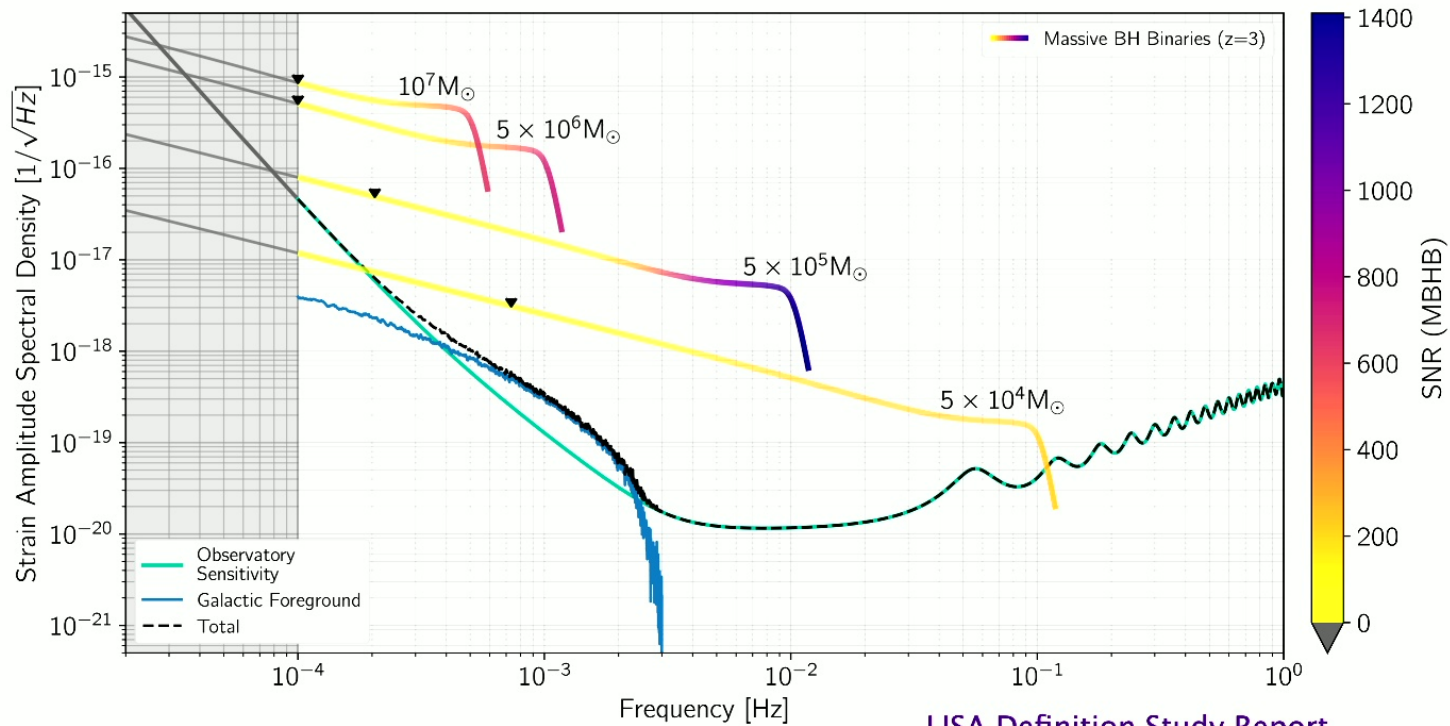
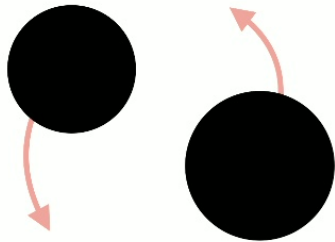


credit: M. Katz

# SO1: Galactic Binaries

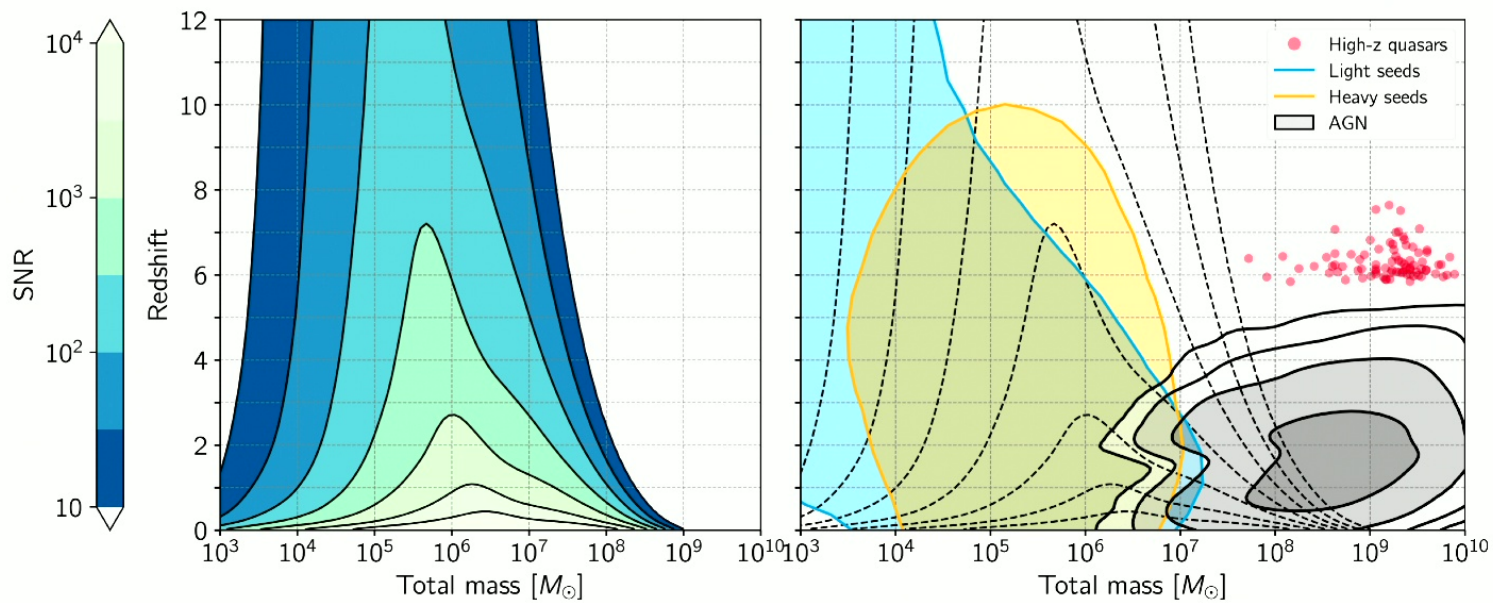
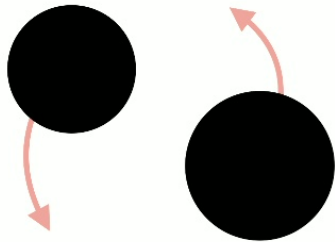


# Massive Black Hole Binaries



LISA Definition Study Report

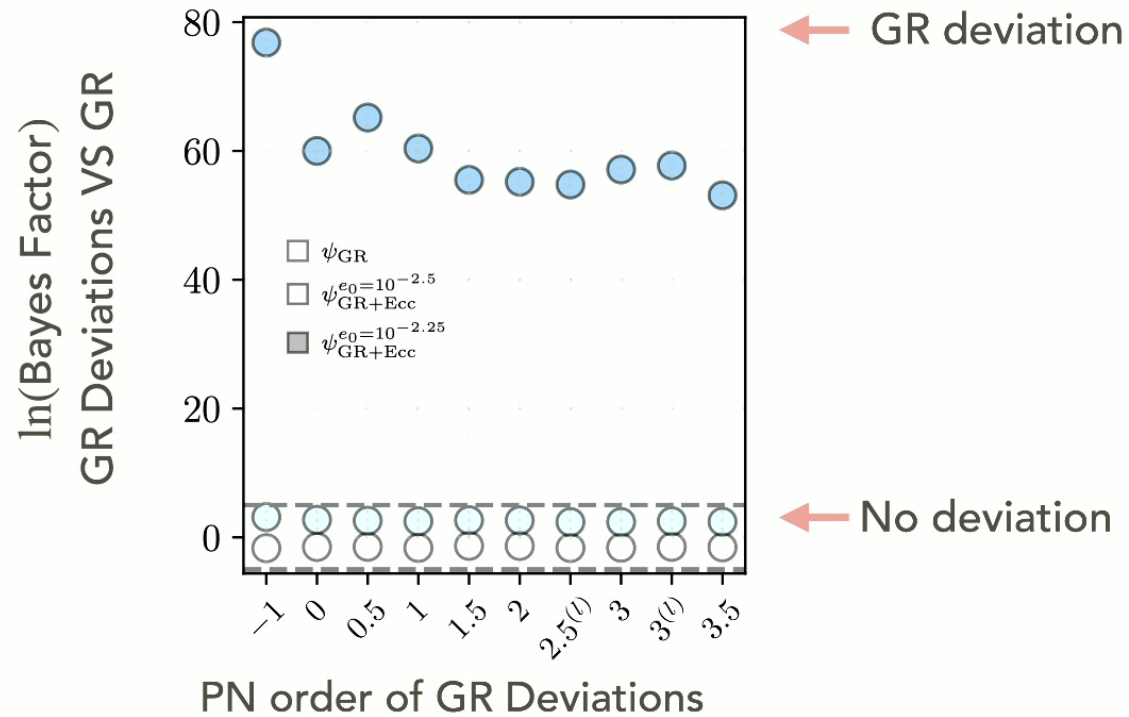
# SO2: Massive Black Hole Binaries



LISA Definition Study Report

# MBHBs Waveform systematics

What would happen if we ignore eccentricity?

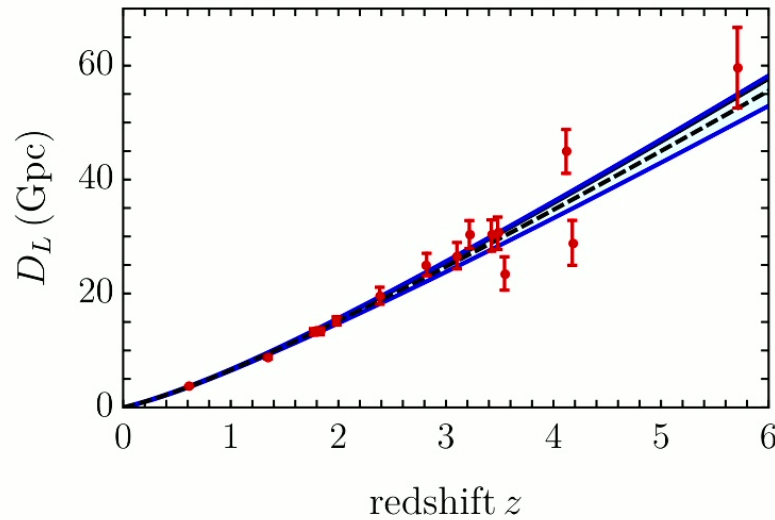


$$M_z = 10^5 M_\odot, q = 8, \chi_{1,2} = 0.9, t_c = 4 \text{ years}$$

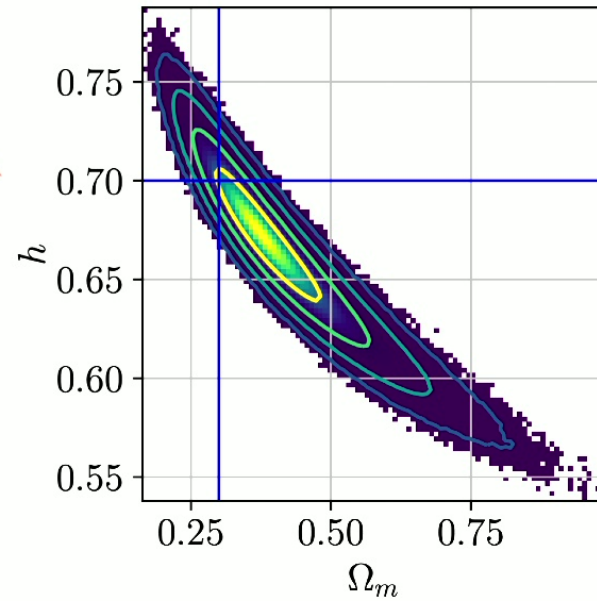
Garg, LS, et al. 2024 arXiv:2410.02910



# SO6: Probing the expansion of the universe



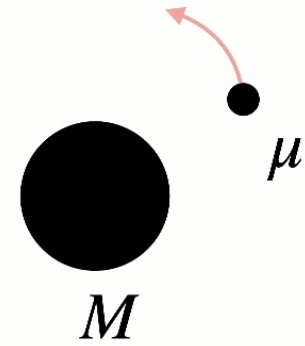
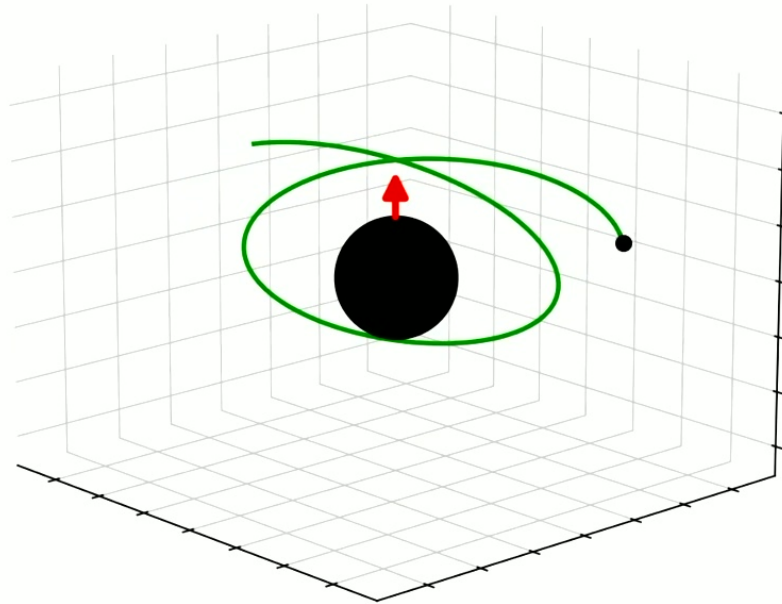
Massive Black Hole Binaries  
Standard Sirens



Mangiagli, LS, +2023  
Speri+ 2021

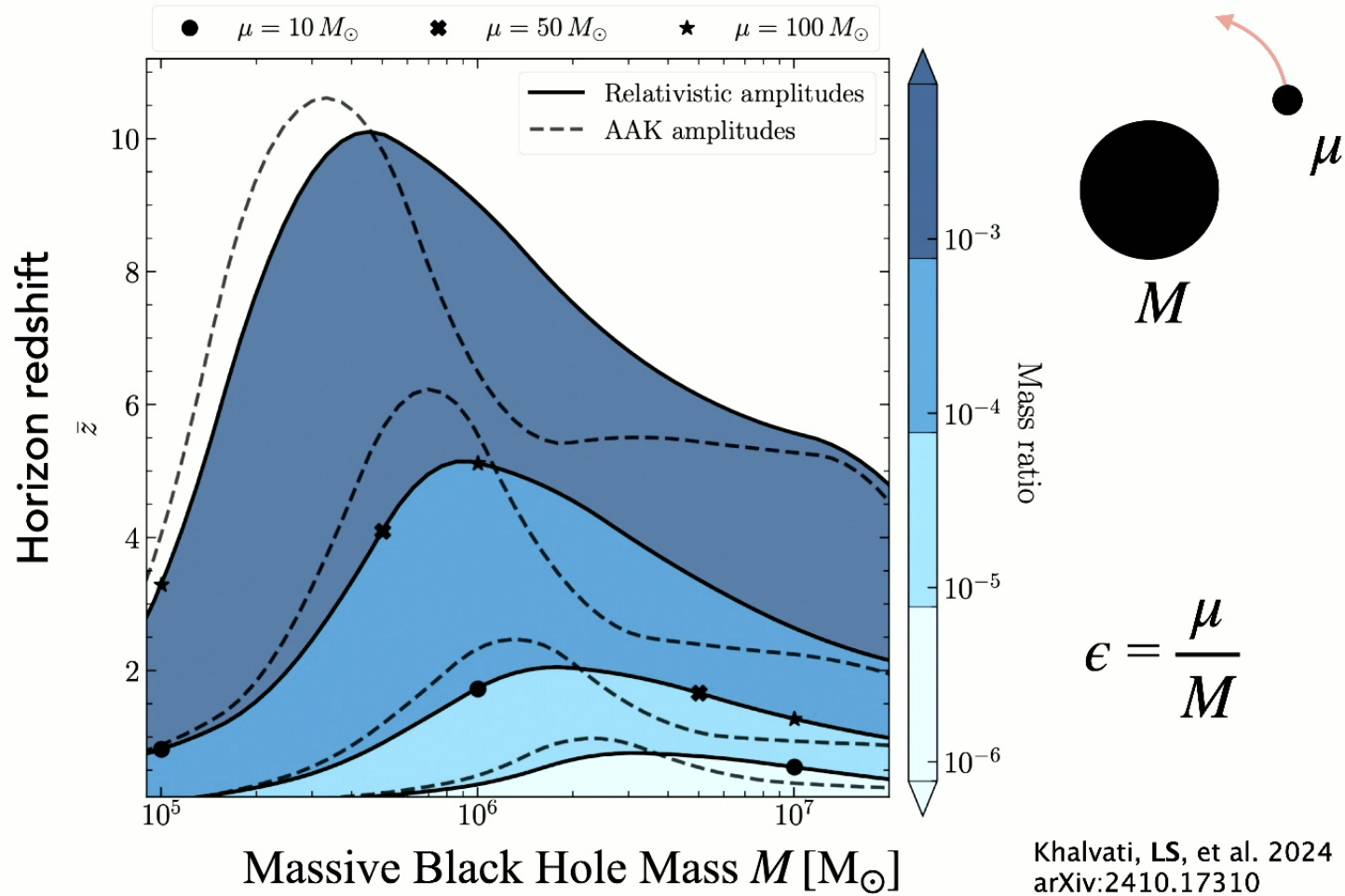
Cosmology with LISA  
arXiv:2204.05434

# Extreme Mass Ratio Inspirals (EMRIs)



$$\epsilon = \frac{\mu}{M}$$

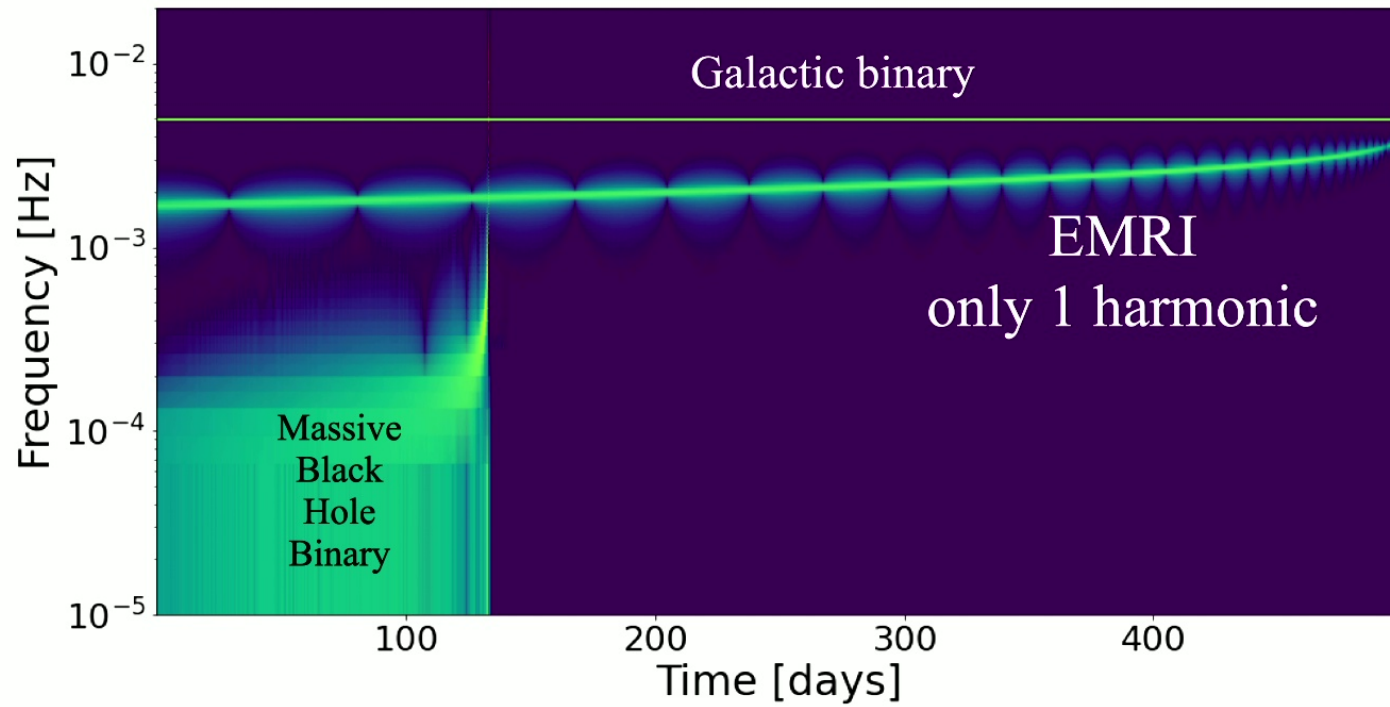
# SO3: Extreme Mass Ratio Inspirals (EMRIs)



26

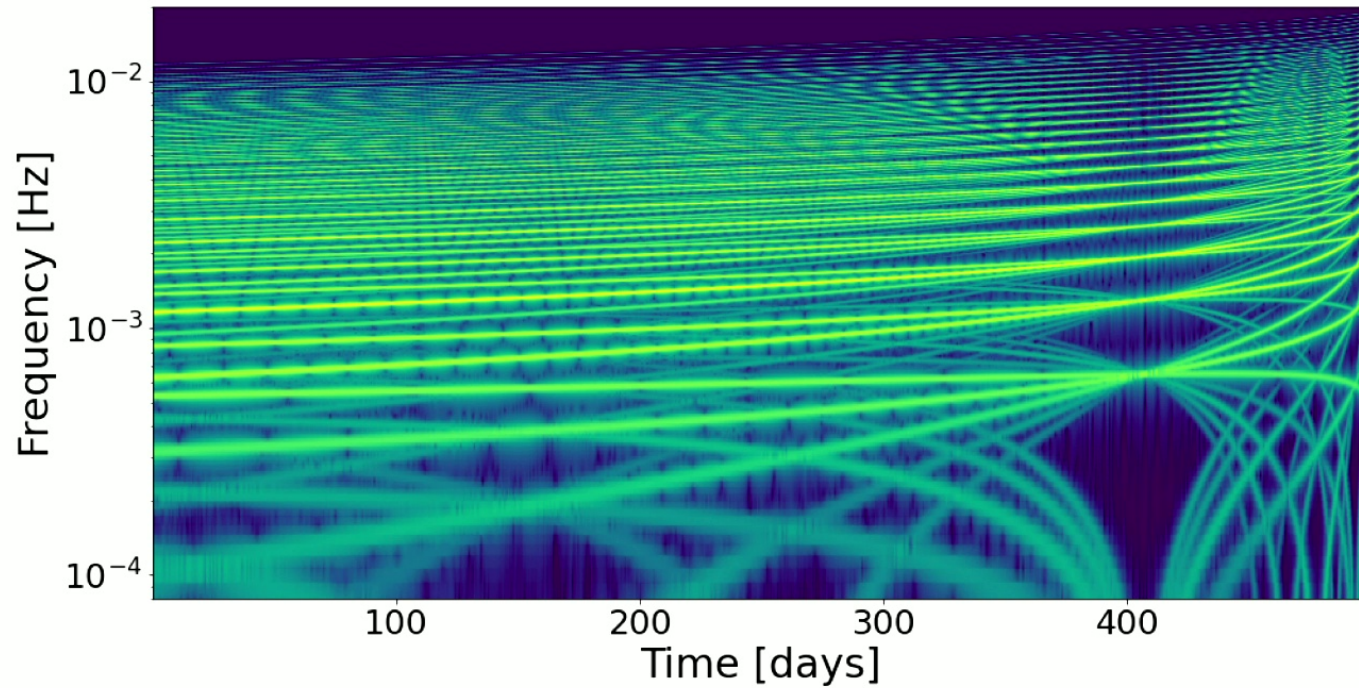


# LISA Sources



EMRI Evolution Time Scale  $T_{ev} \sim 1/\epsilon$

# EMRI Spectrogram



$$h = \sum_V A_V(t) \exp[-i\Phi_V(t)]$$

# Harmonics  $\sim$  orbit complexity

# Fast EMRI Waveforms

$$h = \sum_{lmnk} \left\{ S_{lmnk}(\theta, \phi) A_{lmnk}(p(t), e(t), x_I(t)) e^{-i\Phi_{mnk}(t)} \right\}$$

Trajectory

ODE integration

$$\frac{d}{dt}(p, e, x_I) = \epsilon f_p(a, p, e, x_I)$$

$$\frac{d}{dt}\Phi_{\varphi, \theta, r} = \Omega_{\varphi, \theta, r}(a, p, e, x_I)$$

Amplitudes

Modes Interpolation

$$A_{lmnk}(a, p, e, x_I)$$

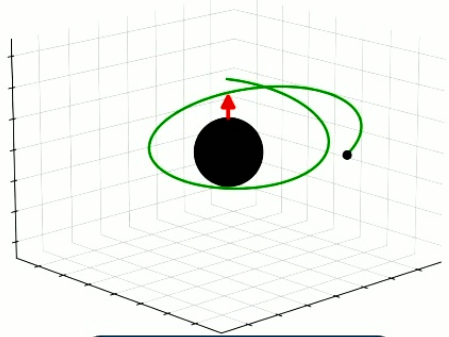
Chua+ 2020  
Katz+ 2021  
Speri+ 2023

29

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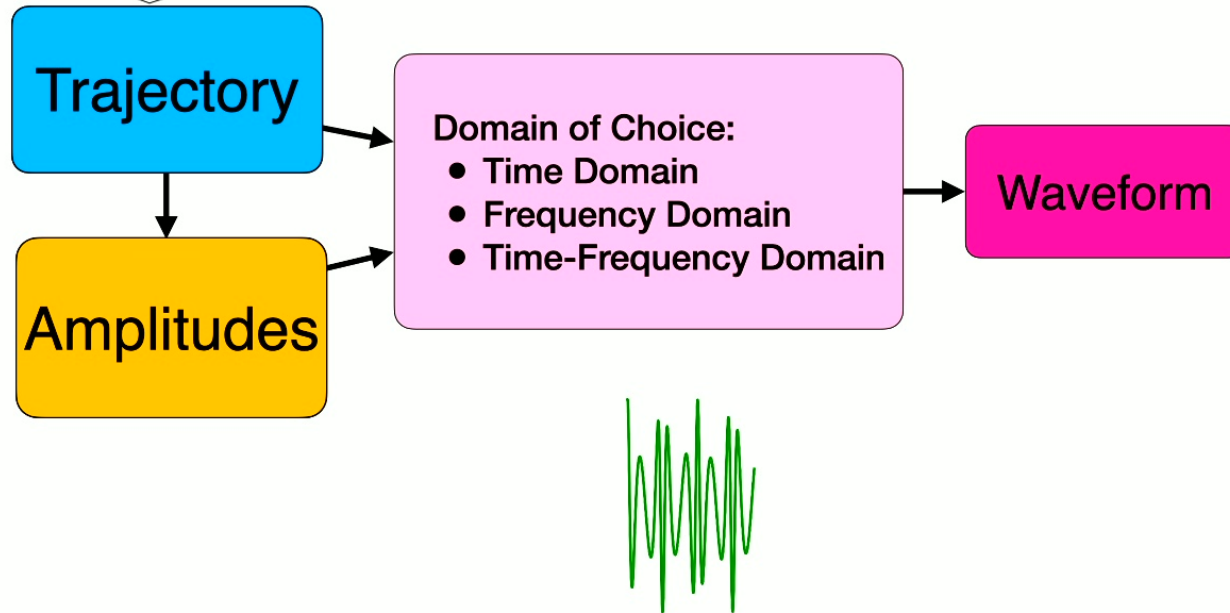
Trajectory

# Fast EMRI Waveforms (FEW)



Chua+ 2020, Katz+ 2021, Speri+ 2023

[bhptoolkit.org/FastEMRIWaveforms](http://bhptoolkit.org/FastEMRIWaveforms)

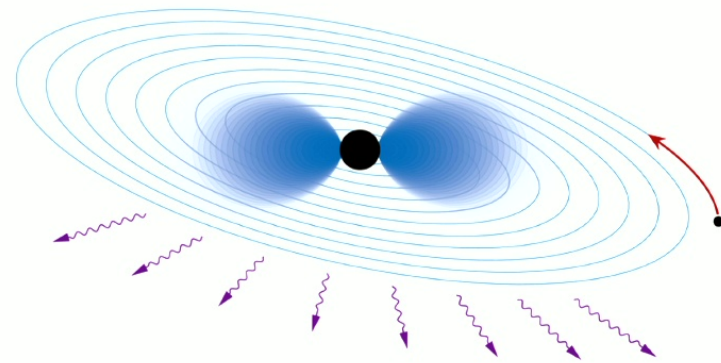
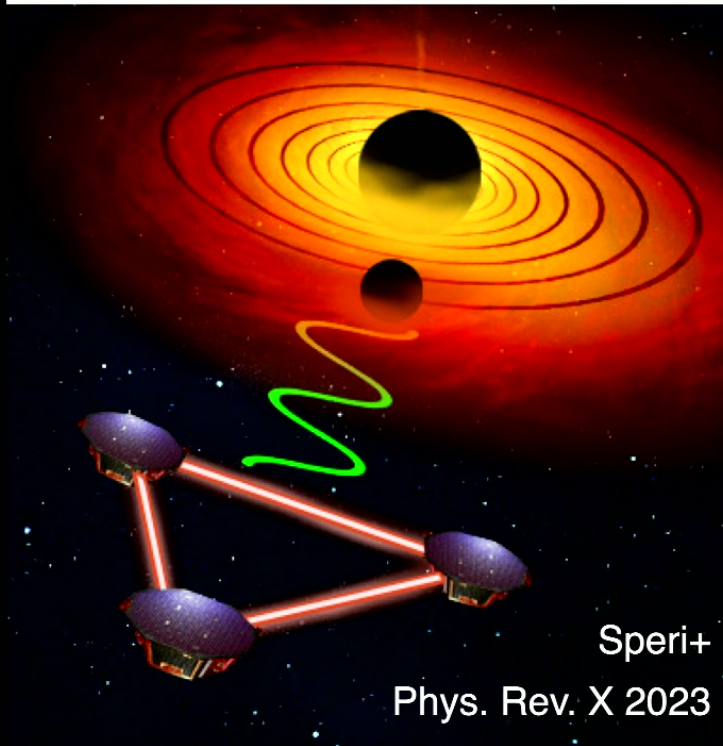


30

# SO3: Probing environments around MBHs

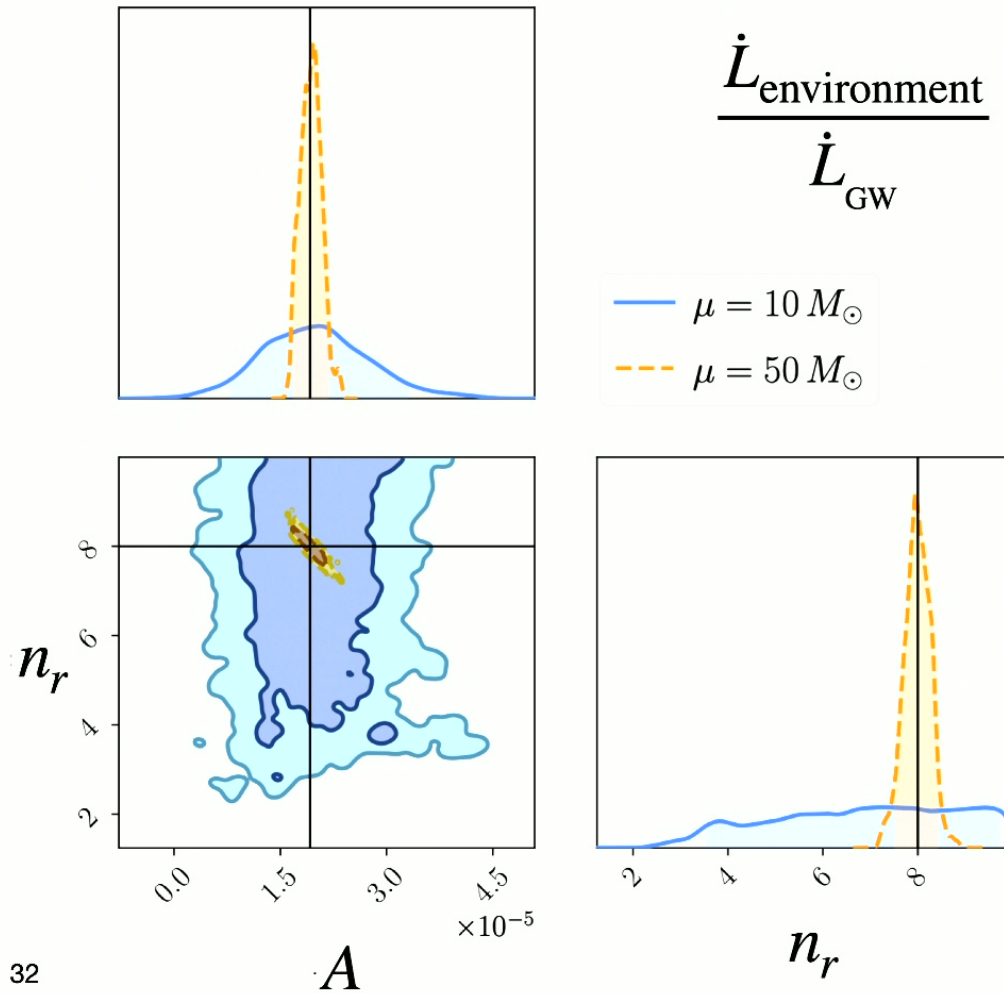
Trajectory

$$\dot{E}_{\text{total}} = \dot{E}_{\text{environment}} + \dot{E}_{\text{GW}}$$



Baumann et al. PRL 2022  
Cole et al. Nature Astron. 7  
(2023) 8, 943-950  
Khalvati, LS, et al. 2024  
arXiv:2410.17310

# EMRIs in Accretion disks



Speri+PRX 2023

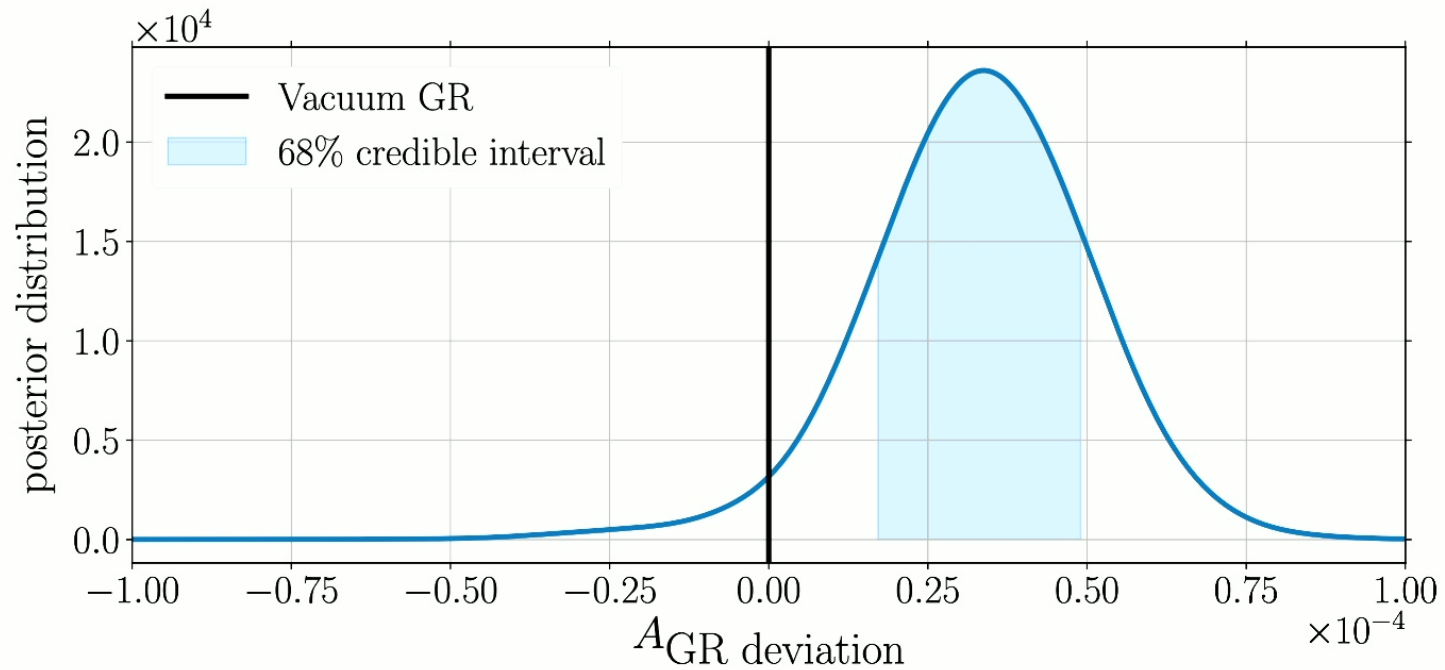
Khalvati, LS, et al. 2024  
arXiv:2410.17310

Copparoni+ in prep.



## If environmental effects are ignored

Unmodelled environmental effects could be mistaken for GR violations



Speri+

Phys. Rev. X 2023





# Conclusions

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## Waveforms

- Parameter space extension of models
- Accuracy and speed
- Beyond vacuum effects

## Data analysis

- Search of SOBHs and EMRIs
- Multiple sources and global fit
- Noise artifacts
- Population analysis

**We have the tools for addressing these questions!**

LISA Data Generation and Analysis Workshop

<https://indico.in2p3.fr/event/33255/>

LISA Analysis Tools Workshop (LATW)

<https://github.com/mikekatz04/LATW>