

Title: Lecture - Quantum Foundations, PHYS 639

Speakers: Lucien Hardy

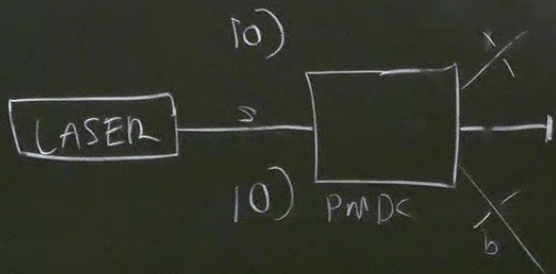
Collection/Series: Quantum Foundations (Elective), PHYS 639, January 6 - February 5, 2025

Subject: Quantum Foundations

Date: January 16, 2025 - 11:30 AM

URL: <https://pirsa.org/25010042>

PMDC



$$\vec{k}_a + \vec{k}_b = \vec{k}_s$$

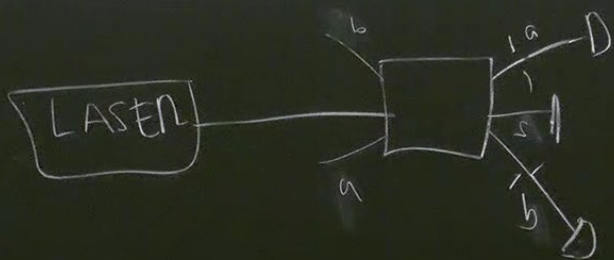
$$\hat{S}|\alpha\rangle = \alpha|\alpha\rangle$$

$$\hat{H}_I = k \hat{a}^\dagger \hat{b}^\dagger \hat{S} + k \hat{a} \hat{b} \hat{S}^\dagger$$

$$e^{-i\hat{H}_I t/\hbar} = \mathbb{1} - \frac{ikt}{\hbar} \hat{a}^\dagger \hat{b}^\dagger \hat{S}$$



LAS



$$|0\rangle = \bigotimes_m |0\rangle_m$$

either 0 clicks

or 1 click in each detector

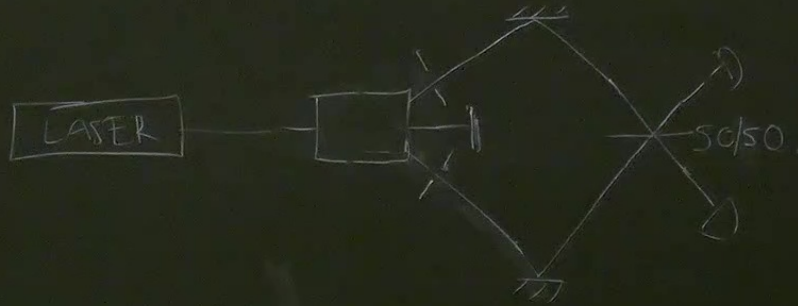
$$|\alpha\rangle_s |0\rangle_c |0\rangle_a \rightarrow e^{i\hat{H}_I dt/\hbar} |\alpha\rangle_s |0\rangle_c |0\rangle_a$$

$$= \left(\mathbb{1} - \frac{i\hat{H}_I dt}{\hbar} \right) |\alpha\rangle_s |0\rangle_c |0\rangle_a$$

$$= |\alpha\rangle_s |0\rangle_c |0\rangle_a - \frac{i\kappa dt}{\hbar} \alpha |\alpha\rangle_s |1\rangle_c |1\rangle_a$$

$$S|\alpha\rangle = \alpha|\alpha\rangle$$

Hong Ou Mandel Dip



$$\omega_a = \omega_b$$

$$|\alpha\rangle_1 |0\rangle_a |0\rangle_b \rightarrow c\alpha |0\rangle_a |0\rangle_b$$

$$|\alpha\rangle_1 |0\rangle_a |0\rangle_b \rightarrow c\alpha |0\rangle_a |0\rangle_b$$

either 0 clicks

or 1 click in each detector

$$|\alpha\rangle_q |0\rangle_a |0\rangle_b = c\alpha |\alpha\rangle_a |1\rangle_a |1\rangle_b$$

$$|\alpha\rangle_q |0\rangle_a |0\rangle_b = c\alpha \hat{a}^\dagger \hat{b}^\dagger |\alpha\rangle_q |0\rangle_a |0\rangle_b$$

$$|\alpha\rangle_q |0\rangle_a |0\rangle_b = \frac{c\alpha}{2} (\hat{c}^\dagger + id^\dagger)(i\hat{c}^\dagger + \hat{d}^\dagger) |\alpha\rangle_q |0\rangle_a |0\rangle_b$$
$$i\hat{c}\hat{c}^\dagger + id\hat{d}^\dagger + (\hat{c}^\dagger\hat{d}^\dagger - \hat{d}^\dagger\hat{c}^\dagger) = [\hat{c}^\dagger, \hat{d}^\dagger] = 0$$

either 0 clicks
or 1 click in each detector

$$|0\rangle_a |0\rangle_b - c\alpha |\alpha\rangle_a |1\rangle_b$$

$$|0\rangle_a |0\rangle_b - c\alpha \hat{a}^\dagger \hat{b}^\dagger |\alpha\rangle_a |0\rangle_b$$

$$|0\rangle_a |0\rangle_b - \frac{c\alpha}{2} (\hat{c}^\dagger + i\hat{d}^\dagger)(i\hat{c}^\dagger + \hat{d}^\dagger) |\alpha\rangle_a |0\rangle_b$$

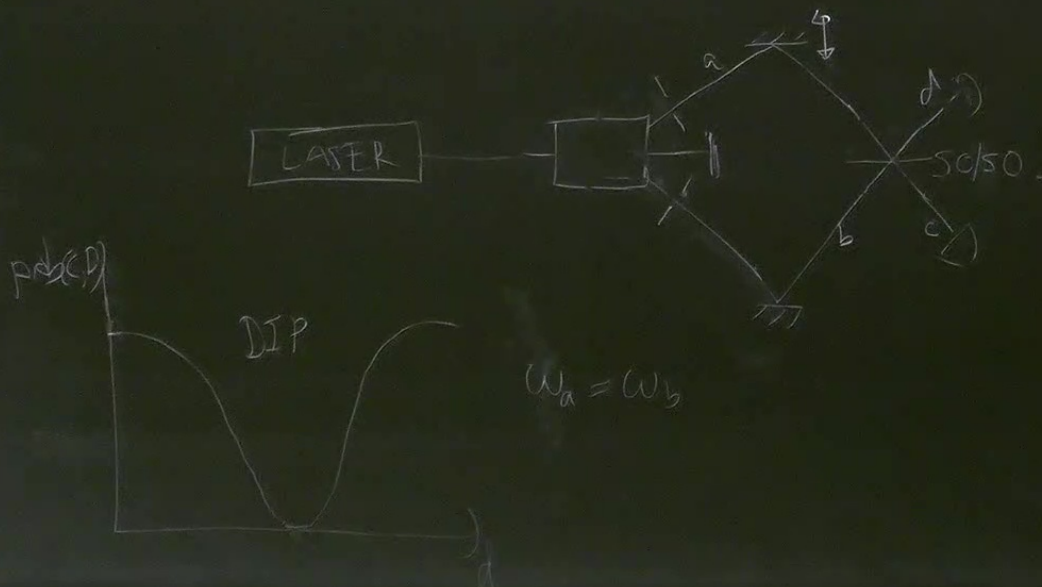
$$i\hat{c}\hat{c}^\dagger + i\hat{d}\hat{d}^\dagger + (\hat{c}^\dagger\hat{d}^\dagger - \hat{d}^\dagger\hat{c}^\dagger) = [\hat{c}^\dagger, \hat{d}^\dagger] = 0$$

$$\rightarrow \alpha, |0\rangle_a |0\rangle_b$$

$$- \frac{c\alpha}{2} (\sqrt{2}|2\rangle_c |0\rangle_d + \sqrt{2}|0\rangle_c |2\rangle_d)$$

$$S(\alpha) = \alpha / |\alpha|$$

Hong On Mandle Dip



$$|\alpha\rangle_1 |0\rangle_a |0\rangle_b - \alpha / |\alpha|$$

$$|\alpha\rangle_1 |0\rangle_a |0\rangle_b -$$

$$|\alpha\rangle_1 |0\rangle_a |0\rangle_b -$$

