

Title: Lecture - Quantum Foundations, PHYS 639

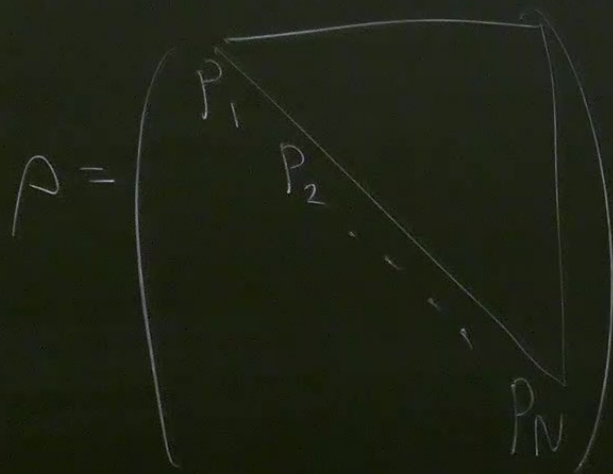
Speakers: Lucien Hardy

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Subject: Quantum Foundations

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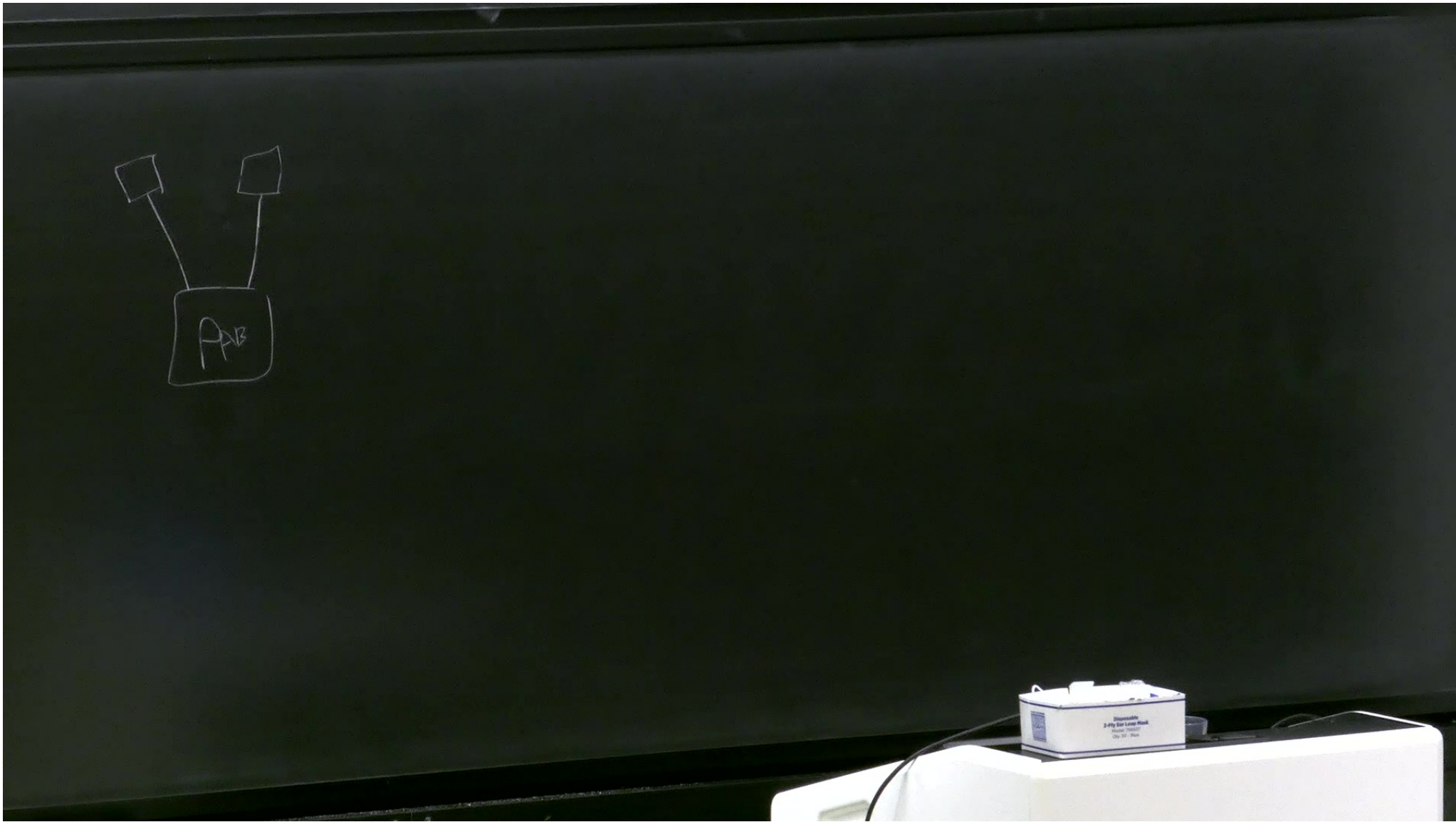


$$K = N + 2 \frac{1}{2} N(N-1) = N^2$$

$$\mathcal{H}_{AB} = \mathcal{H}_A \otimes \mathcal{H}_B$$

$$N_{AB} = N_A N_B$$

$$K_{AB} = K_A K_B$$



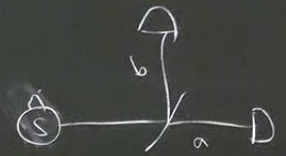
$$|s\rangle |A_0\rangle |B_0\rangle |me\rangle \rightarrow (\sqrt{T} |a\rangle + i\sqrt{R} |b\rangle) |A_0\rangle |B_0\rangle |me\rangle$$

$$\rightarrow \sqrt{T} |A\rangle |B_0\rangle \left| \frac{I}{A} \right\rangle + i\sqrt{R} |A_0\rangle |B\rangle \left| \frac{I}{B} \right\rangle$$

$$\xrightarrow{\frac{I}{A}} \sqrt{T} |A\rangle |B_0\rangle \left| \frac{I}{A} \right\rangle$$

What is the basis (in H) wrt which I have separations } Decoherece Theory

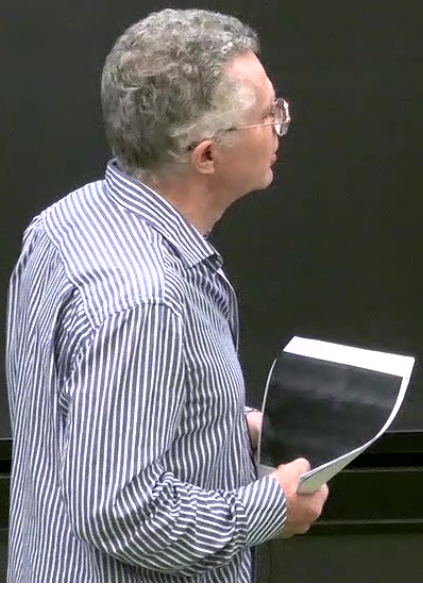
$$\frac{1}{\sqrt{2}} \left(\begin{array}{c} I \\ \text{see} \\ A \end{array} \right) + \begin{array}{c} I \\ \text{see} \\ B \end{array} \right)$$



$$|s\rangle |A_0\rangle |B_0\rangle |me\rangle \rightarrow (\sqrt{T} |a\rangle + i\sqrt{R} |b\rangle) |A_0\rangle |B_0\rangle |me\rangle |E_0\rangle$$

$$\rightarrow \sqrt{T} |A\rangle |B_0\rangle \begin{array}{c} I \\ \text{see} \\ A \end{array} |E_A\rangle + i\sqrt{R} |A_0\rangle |B\rangle \begin{array}{c} I \\ \text{see} \\ B \end{array} |E_B\rangle$$

$$\begin{array}{c} \text{see} \\ \rightarrow \\ A \end{array} \sqrt{T} |A\rangle |B_0\rangle \begin{array}{c} I \\ \text{see} \\ A \end{array}$$



$$\xrightarrow{\text{sep}} \frac{1}{\sqrt{2}} \left(|A\rangle |B_0\rangle + \frac{1}{\sqrt{2}} |A\rangle \right)$$

1) No actual collapse. The reality problem

2) Actual collapse.

} modify Schröd eqn.
GRW

Zell (are there quantum jumps?)

Easy problem

What is the basis (in H) wrt which I have sensations

$$\frac{1}{\sqrt{2}} \left(\frac{1}{\sqrt{2}} |A\rangle + \frac{1}{\sqrt{2}} |B\rangle \right)$$

} Decoherence Theory

1) No actual collapse. The measurement problem

2) Actual collapse.

} modify Schröd eqn.
GRW

Bell (are there quantum jumps?)

Easy problem

What is the basis (in H) wrt which I have sensations?

$$\frac{1}{\sqrt{2}} \left(\left| \begin{smallmatrix} I \\ A \end{smallmatrix} \right\rangle + \left| \begin{smallmatrix} I \\ B \end{smallmatrix} \right\rangle \right)$$

} Decoherence
Theory

$$\frac{1}{\sqrt{2}} \left(\left| \frac{I}{\sqrt{2}} \right\rangle_A + \left| \frac{I}{\sqrt{2}} \right\rangle_B \right)$$

} Theory

Hard problem What actually picks out (the sensation of) a definite outcome?

FAPP

The no cloning theorem.
 M clones states in \mathcal{H}_{a_1}

$$|\psi\rangle_{a_1} |M\rangle_{b_3} \xrightarrow{U} |\psi\rangle_{a_1} |\psi\rangle_{a_2} |M_\psi\rangle_{c_f} \quad \forall |\psi\rangle_{a_1} \in \mathcal{H}_{a_1}$$

The no cloning theorem.

M clones states in \mathcal{H}_{a_1}

$$|\psi\rangle_{a_1} |M\rangle_{b_3} \xrightarrow{U} |\psi\rangle_{a_1} |\psi\rangle_{a_2} |M_{\psi}\rangle_{c_4} \quad \forall |\psi\rangle_{a_1} \in \mathcal{H}_{a_1}$$

$$|\varphi\rangle_{a_2} |M\rangle_{b_3} \xrightarrow{U} |\varphi\rangle_{a_1} |\varphi\rangle_{a_2} |M_{\varphi}\rangle_{c_4}$$

Decoherence
Theory

sensations of a definite outcome?

$|u\rangle$

$|v\rangle$

$$\langle v | \underbrace{U^\dagger U}_{I} | u \rangle = \langle v | u \rangle$$

$$\langle \phi | \psi \rangle \langle m | m \rangle = \langle \phi | \psi \rangle^2 \langle m_\phi | m_\psi \rangle$$

Case 1 $\langle \phi | \psi \rangle = 0$

Case 2 $\langle \phi | \psi \rangle \neq 0$

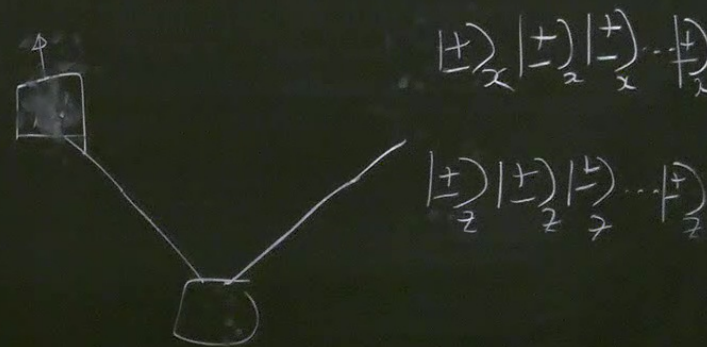
$$1 = \langle \phi | \psi \rangle \langle m_\phi | m_\psi \rangle$$

$$|\langle \phi | \psi \rangle| = \frac{1}{|\langle m_\phi | m_\psi \rangle|} \geq 1 \Rightarrow \langle \phi | \psi \rangle = 1$$

$$|\psi\rangle = |0\rangle$$

$$|\phi\rangle = \alpha|0\rangle + \beta|1\rangle$$

have situations } Decoherence
 Theory



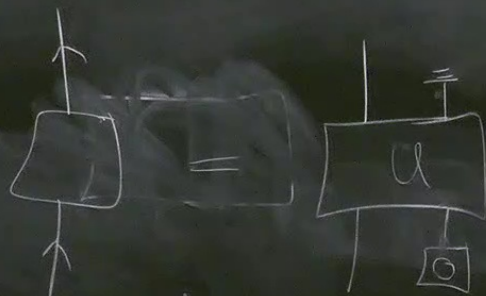
$$\begin{pmatrix} \frac{1}{\sqrt{2}} & 0 \\ 0 & \frac{1}{\sqrt{2}} \end{pmatrix}$$

$$\left(|+\rangle_x |-\rangle_x - |-\rangle_x |+\rangle_x \right)$$

have situations } Decoherence Theory

Stinespring

$$\frac{1}{2} \left[\begin{pmatrix} + & \chi & + \\ z & z & \end{pmatrix} + \begin{pmatrix} - & \chi & - \\ z & z & \end{pmatrix} \right]$$



completely positive maps.



$$\left| \frac{+}{2} \right\rangle \left| \frac{+}{2} \right\rangle \left| \frac{+}{2} \right\rangle \dots \left| \frac{+}{2} \right\rangle$$

$$\left| \frac{+}{2} \right\rangle \left| \frac{+}{2} \right\rangle \left| \frac{+}{2} \right\rangle \dots \left| \frac{+}{2} \right\rangle$$

$$\begin{pmatrix} \frac{1}{2} & 0 \\ 0 & \frac{1}{2} \end{pmatrix}$$

$$\left(\left| \frac{+}{2} \right\rangle \left| \frac{-}{2} \right\rangle - \left| \frac{-}{2} \right\rangle \left| \frac{+}{2} \right\rangle \right)$$