

**Title:** Lecture - Beautiful Papers

**Speakers:** Pedro Vieira

**Collection/Series:** Beautiful Papers - October 7, 2024 - January 31, 2025

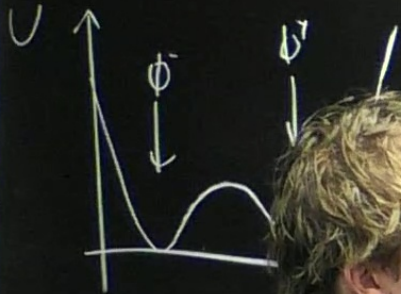
**Subject:** Other

**Date:** November 25, 2024 - 9:15 AM

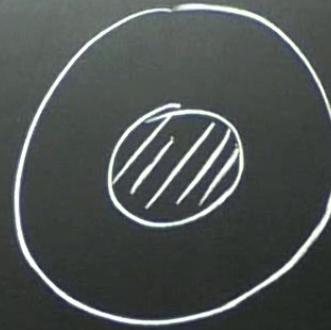
**URL:** <https://pirsa.org/24110036>

# Black holes as bubble nucleation sites [14101.0017]

Gregory, Mass, Withers



$$= \frac{3}{4} = 8\pi G \rho$$



Assumptions:  $\Gamma \sim e^{-\frac{\beta}{\hbar}}$ ,  $\beta = S_F(\psi) - S_F(\psi^+)$

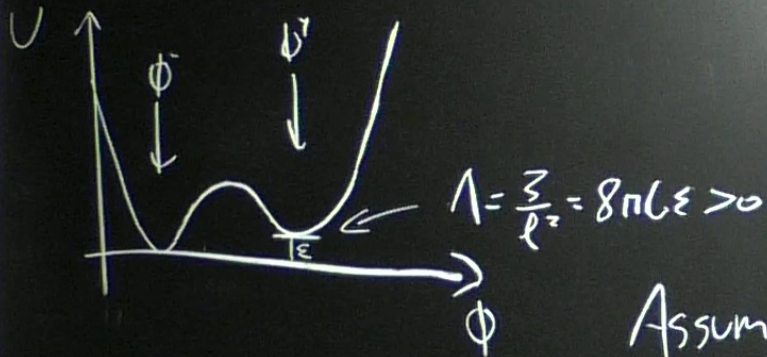
$$ds^2 = -f(r)dt^2 + \frac{1}{f(r)}dr^2 + r^2 d\Omega^2$$

Black

reaction

[14101.0012]

Gregory, Mass, Withers



Assumptions:  $\Gamma \sim e^{-\frac{\beta}{\hbar}}$ ,  $\beta = S_E(\psi) - S_E(\psi^+)$

$$ds^2 = -f(r) dt^2 + \frac{1}{f(r)} dr^2 + r^2 d\Omega^2$$

$$f_- = 1 - \frac{2M}{r}, \quad f_+(r) = 1 - \frac{2M^+}{r} + \frac{r^2}{l^2}$$

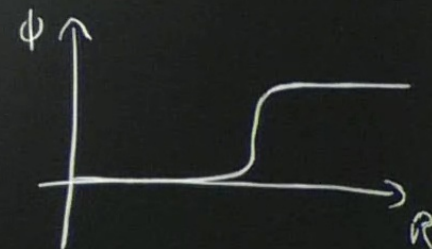
Israel junction conditions:

$$h_{ab}^+ - h_{ab}^- = 0$$

$$K_{ab}^+ - K_{ab}^- = -8\pi G \left( T_{ab}^{\text{wall}} - \frac{1}{2} h_{ab} T^{\text{wall}} \right)$$

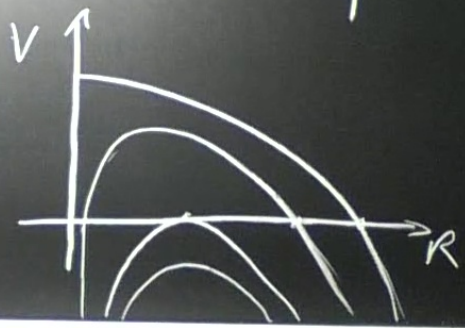
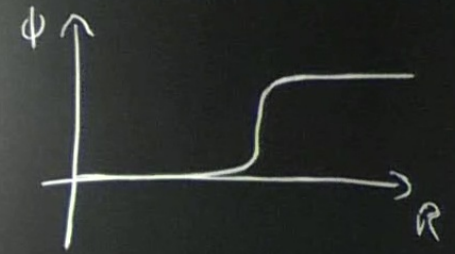
$$T_{ab}^{\text{wall}} = -\sigma h^{ab}$$

$$\Rightarrow \text{EOM: } \ddot{R} + V_{\sigma, \ell, M^+, M^-} = 0, \dot{t} = \dots$$



$$T_{ab}^{wall} = -\sigma h$$

$$\Rightarrow \text{EOM: } \ddot{R} + V_{\sigma, \ell, M, M} = 0, \dot{t} = v$$

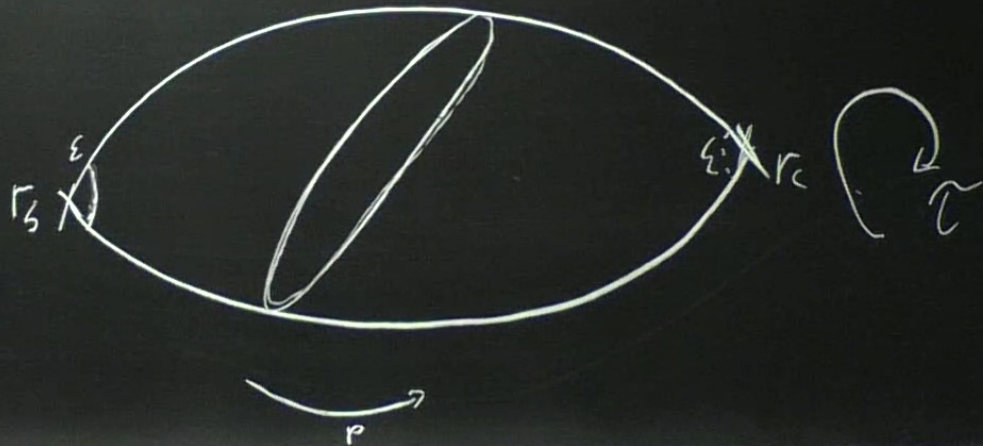


$$t \rightarrow -i\tau$$

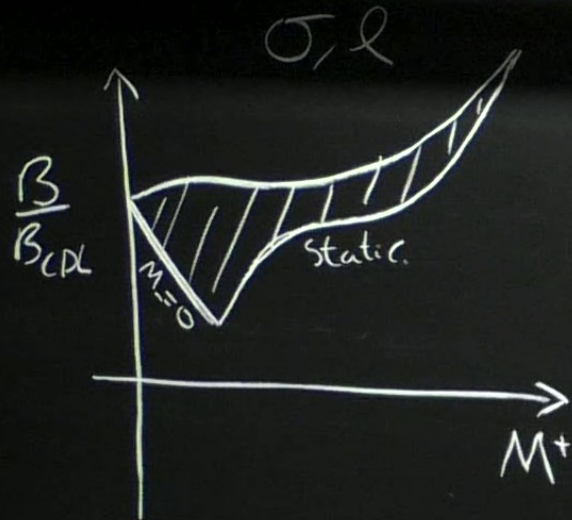
Near horizon BH:

$$ds^2 = f'(r_s)(r-r_s)d\tau^2 + \frac{1}{f'(r_s)(r-r_s)} dr^2 + r^2 d\Omega^2 \rightarrow d\rho^2 + \rho^2 \left( \frac{1}{f'(r_s)} d\tau \right)^2 + r^2 d\Omega^2$$

$$\int_E^M = \int_E^{M-B} + \int_E^B$$



$$f_- = 1 - \frac{2M_-}{r}, \quad f_+(r) = 1 - \frac{2M_+}{r} + \frac{r^2}{l^2}$$

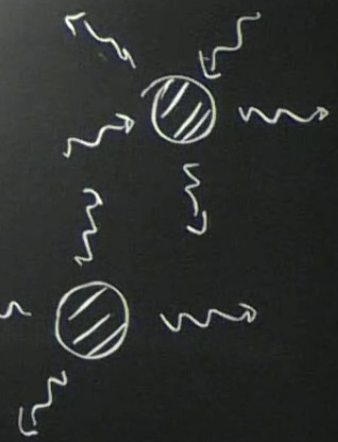


2105.0933

Euclidean bounce = thermal equilibrium  
[HH state]

vs

realistic BH [Unruh state]



junction conditions.

$$h^+ = h^- = 0$$

$$k_+^+ - k_-^- = -8\pi G (T_{wall} - \frac{1}{2} h_{wall} T_{wall})$$

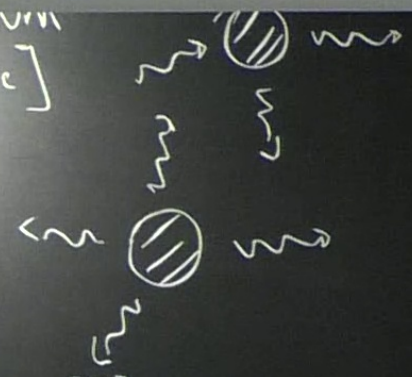


Euclidean

equilibrium  
state]

vs

realistic BH [Unruh state]



$$P_{\text{decay}} = \sum_F \underbrace{|\langle f | i \rangle|}^2 \int \mathcal{D}\varphi_f \mathcal{D}\varphi_i \mathcal{D}\phi e^{iI[\phi]} \langle f | \varphi_f, t_f \rangle \langle \varphi_i, t_i | i \rangle$$

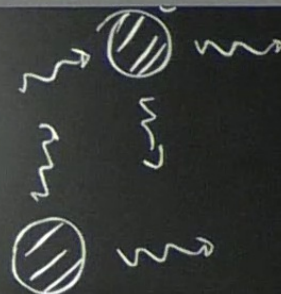
Euclidean

equilibrium

[H state]

vs

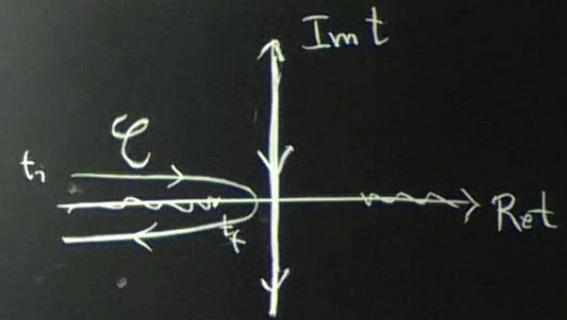
realistic BH [Unruh state]



$$P_{\text{decay}} = \sum_F \underbrace{|\langle f | i \rangle|^2}_{\substack{t_f \quad t_i}} \int \mathcal{D}\varphi_i \mathcal{D}\varphi_f \mathcal{D}\phi \underbrace{e^{-iI[\phi]}}_{\substack{\phi|_{t_f} = \phi'|_{t_f} = \varphi_f \\ \langle f | \varphi_f, t_f \rangle \\ \langle \varphi_i, t_i | i \rangle}} \mathcal{D}\varphi'_i \mathcal{D}\varphi'_f \mathcal{D}\phi'$$

$$P_{\text{decay}} = \int D\varphi'_2 D\varphi_1 D\varphi_2 e^{i\int [\mathcal{L}(\varphi)]}$$

$$\phi_2|_{t_f} \sim \text{true solution} \underbrace{\langle \varphi, t_2 | \varphi', t_2 \rangle}_{\rho_2}$$



Semiclassical appr.

$$\phi_b$$

$$t \rightarrow -i\tau$$

$$P_{\text{decay}} = \int \mathcal{D}\varphi'_i \mathcal{D}\varphi_f \mathcal{D}\varphi_i$$

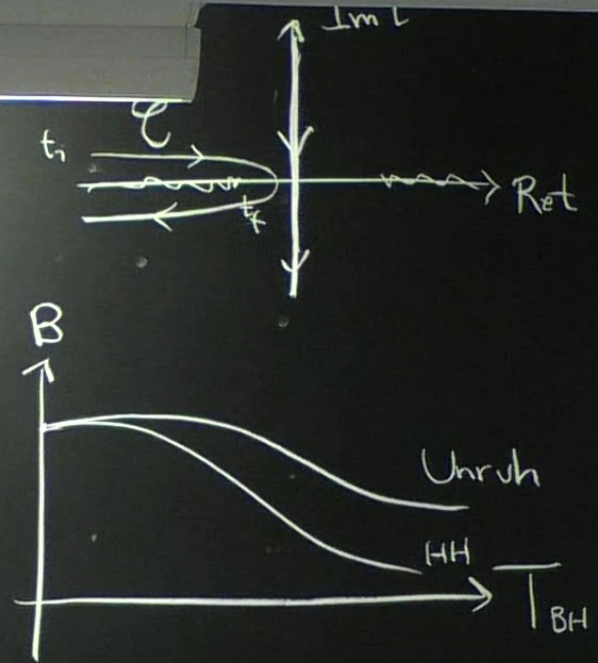
$$\phi_{\varphi|t_f} \sim \text{true vacuum} \langle \varphi, t_2 | \varphi', t_2 \rangle$$

$\underbrace{\hspace{10em}}_{\rho_2}$

Semiclassical appr.

$$\phi_b$$

$$\Gamma \sim e^{-B}$$



$$P_{\text{decay}} = \int D\varphi'_1 D\varphi_1 D\varphi_2$$

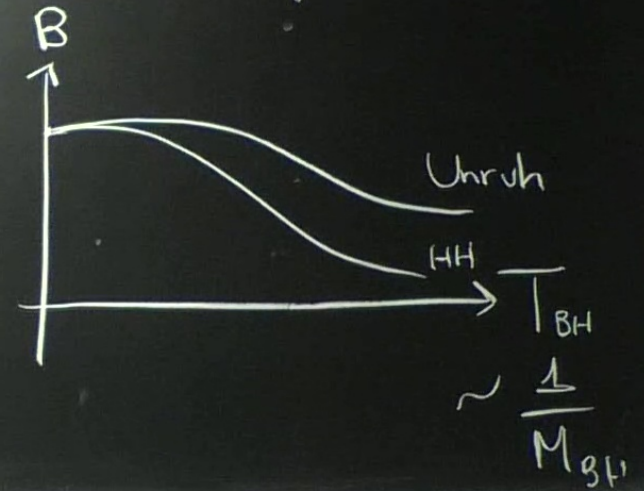
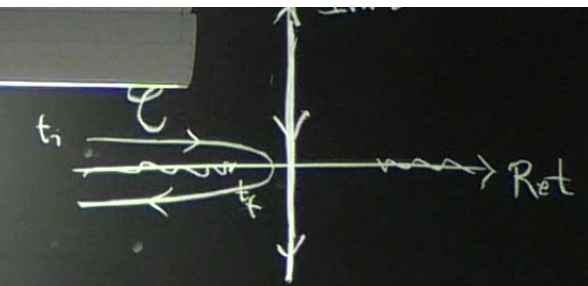
$$\phi_2|_{t_f} \sim \text{true sum} \langle \varphi, t_2 | \varphi', t_2 \rangle$$

$\rho_2$

Semiclassical appr.

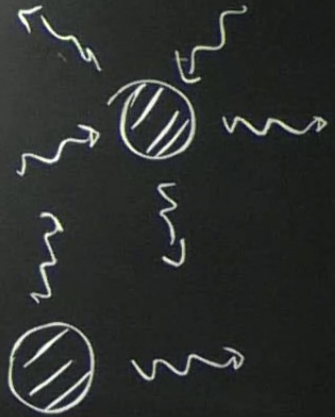
$$\phi_b$$

$$\Gamma \sim e^{-B}$$



2105.0933

Euclidean bounce = thermal equilibrium  
[HH state]



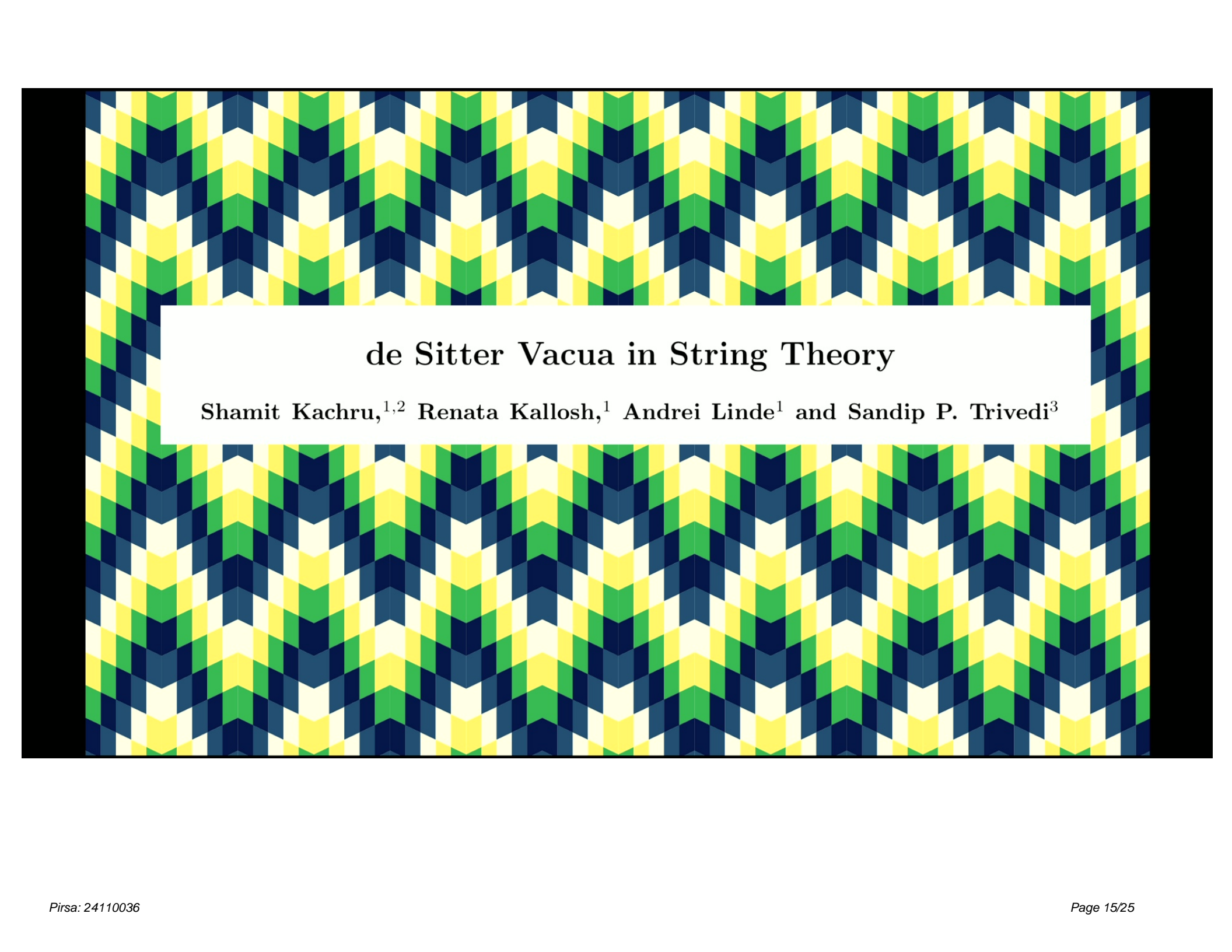
vs

realistic BH [Unruh state]



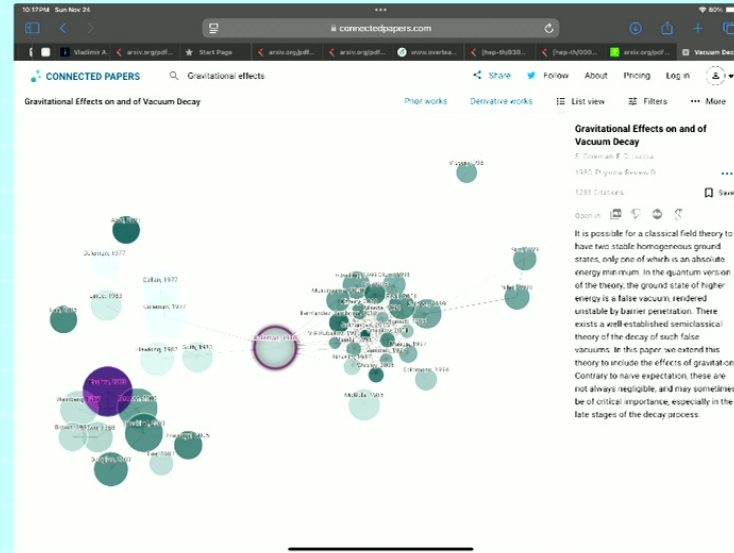
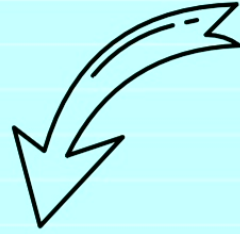
$$\phi|_{t_f} = \phi|_{t_i} = \phi_F$$

$$P_{\text{decay}} = \sum_F \underbrace{|\langle f | i \rangle|^2}_{\int \mathcal{D}\varphi_i \mathcal{D}\varphi_f \mathcal{D}\phi} e^{-2I[\phi]} \langle f | \varphi_{t_f}, t_f \rangle \langle \varphi_{t_i}, t_i | i \rangle$$



# de Sitter Vacua in String Theory

Shamit Kachru,<sup>1,2</sup> Renata Kallosh,<sup>1</sup> Andrei Linde<sup>1</sup> and Sandip P. Trivedi<sup>3</sup>



### De Sitter vacua in string theory

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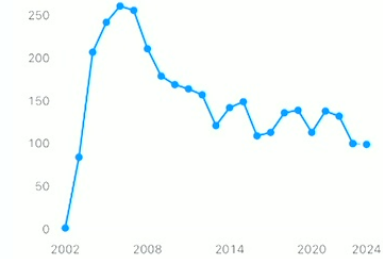
Report number: SLAC-PUB-9630, SU-ITP-03-01, TIFR-TH-03-03

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### Citations per year



1/9



# Plan for the talk:

I) Some reasons why it is hard to find de Sitter vacuum in string theory

II) Overview of the KKLT construction

III) Stability of the solution,  
relation to

GRAVITATIONAL EFFECTS ON AND OF VACUUM DECAY\*  
Sidney Coleman<sup>†</sup>  
Stanford Linear Accelerator Center  
Stanford University, Stanford, California 94305  
and  
Frank De Luccia  
Institute for Advanced Study  
Princeton, New Jersey 88548

IV) People still talk about it! Controversies  
and relation to The Swampland Program

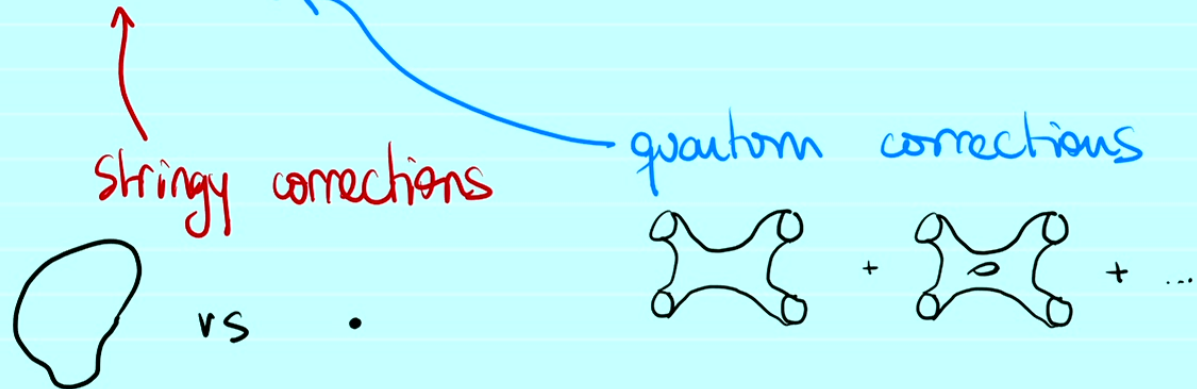
2/9

# I) Some reasons why it is hard to find de Sitter vacuum in string theory

- No-go theorem by [Maldacena, Nuñez ; '00]

In the second part of this paper, which can be read independently of the first, we show that there are no non-singular Randall-Sundrum or de-Sitter compactifications for large class of gravity theories.

- without sources
- without  $\alpha'$  or  $g_s$  corrections

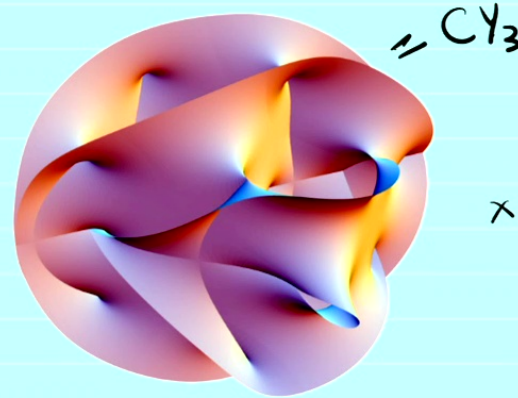


3/9

(I) Some reasons why it is hard to find de Sitter vacuum in string theory compactifications

- Moduli stabilization

10d spacetime =



$\times M_4$  ←  
where we live

moduli  $\equiv$  massless fields characterizing  $CY_3$

- shape
- size
- ...

4/9

- Scale separation

## ② Overview of the KKLT construction

Two steps:

① Stabilize all moduli in a supersymmetric way

1.1 Fix all moduli except for volume with fluxes

1.2 Fix the volume with quantum corrections

AdS vacua with exponentially large warping

② Break supersymmetry and get a de Sitter vacuum  $\rightarrow$  introducing  $\overline{D3}$

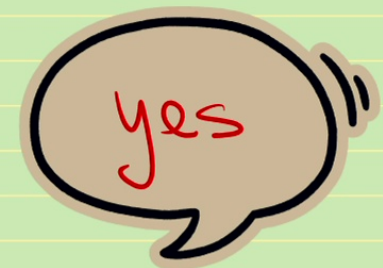
5/9

### III) Stability of the solution

The de Sitter vacua is metastable so following Coleman, De Luccia they argue

1) Do our dS vacua survive for a large number of Planck times? For instance, if we fine tune to get a small cosmological constant, is the dS vacuum sufficiently stable to survive during the  $10^{10}$  years of the cosmological evolution? If the answer is positive, one can use the dS minimum for the phenomenological description of the current stage of acceleration (late-time inflation) of the universe.

2) Is the typical decay time of the dS vacuum longer or shorter than the recurrence time  $t_r \sim e^{S_0}$ , where  $S_0 = \frac{24\pi^2}{V_0}$  is the dS entropy [43]? If the decay time is longer than  $t_r \sim e^{S_0}$ , one may need to address the issues about the consistency of the stringy description of dS space raised in [2, 5, 8].



to these questions

6/9

① Thin wall approximation

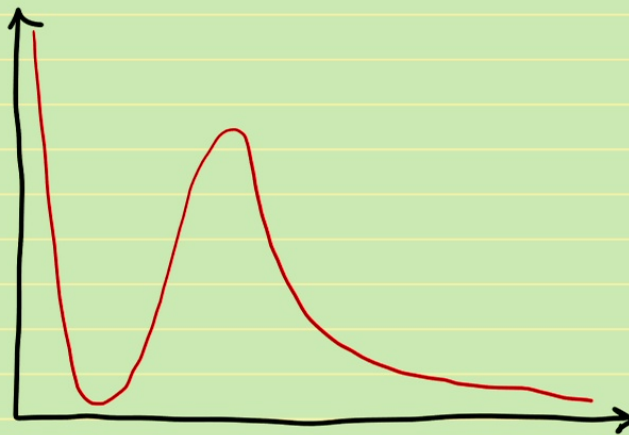
$$P \approx \exp(-S(\varphi_0)) = \exp\left(-\frac{24\pi^2}{V_0}\right) \sim \exp(-10^{122}) .$$

$$t_{\text{decay}}^{\text{CDL}} \sim t_r \exp\left(-\frac{64\pi^2}{T^2}\right)$$

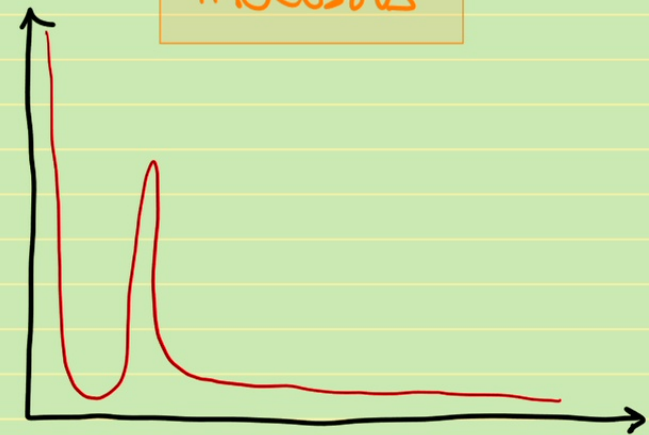
② No wall approximation

$$t_{\text{decay}}^{\text{HM}} = e^{-S_1+S_0} = t_r \exp\left(-\frac{24\pi^2}{V_1}\right) \ll t_r .$$

DIFFERENT  
PHYSICAL  
PROCESSES



vs



7/9

## IV

## Criticisms to KKLT

- Does the  $\overline{D3}$  mechanism really work?  
singularities, backreaction, stability ...
- Moduli stabilisation  
separation of scales  $\begin{matrix} \uparrow \\ m_{\text{c}} \\ m_{\text{p}} \end{matrix}$   $\leftarrow$  can you justify the hierarchy?
- Are the  $\alpha'$  and  $g_s$  corrections really controlled?  
 $\oplus$  non easy no instability concerns  
Dine-Seiberg problem
- Explicit construction with consistent uplift to 10d string theory?

8 / 9

IV

## The de Sitter conjecture and the Swampland program

### Conjecture 9: de Sitter Conjecture

A scalar potential of an EFT weakly coupled to Einstein gravity must satisfy

$$M_P \frac{|\nabla V|}{V} \geq c, \quad (9.1)$$

with  $c$  some  $\mathcal{O}(1)$  constant. This was further refined by stating that the previous bound only needs to be imposed if the following condition on the second derivative of the potential is violated,

$$\min(\nabla_i \nabla_j V) \leq \frac{-c' V}{M_P^2}, \quad (9.2)$$

with  $c'$  another  $\mathcal{O}(1)$  constant. This way, only dS minima (and not critical points in general) are ruled out.

No proof for this conjecture but people believe no de Sitter solution has been well formulated yet.

ongoing research program

9/9



## 1.2 Fix the volume with *quantum corrections*

They give examples of non-perturbative quantum corrections  $\sim e^{\rho}$

a) Euclidean D3 branes [Witten; '96]

b) Gluino condensation,  
non-abelian gauge theories living on  
geometric singularities on  $X_{Cr3}$

$$V_{\text{AdS}}^{\text{min}} = (-3e^{\kappa} W^2)_{\text{AdS}}$$

*all moduli stabilized  
while preserving susy*