

Title: Lecture - Beautiful Papers

Speakers: Pedro Vieira

Collection/Series: Beautiful Papers - October 7, 2024 - January 31, 2025

Subject: Other

Date: November 15, 2024 - 9:15 AM

URL: <https://pirsa.org/24110034>

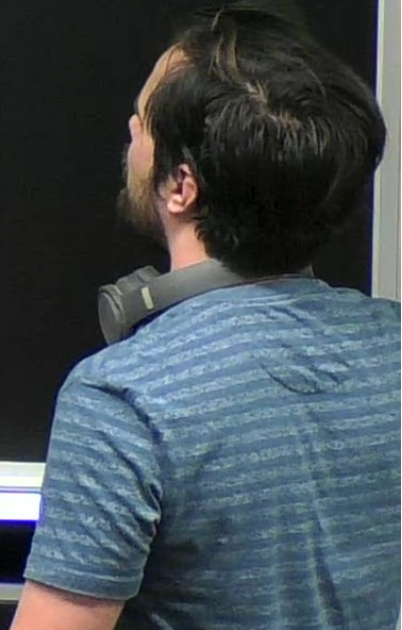
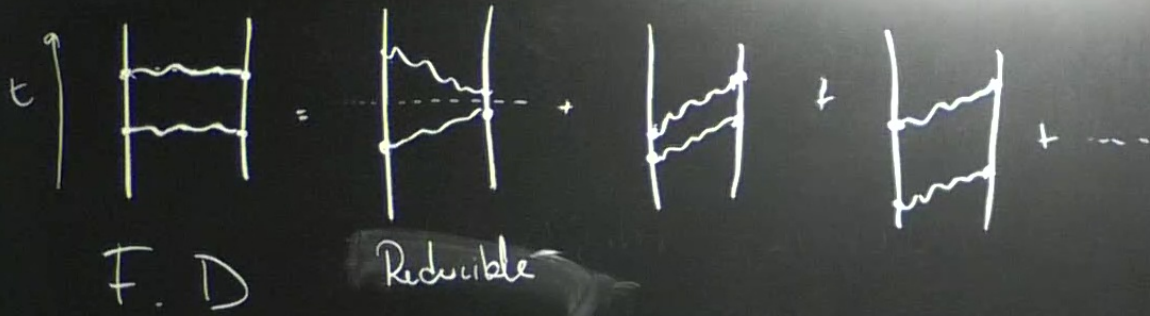
Nuclear From Ch. Lagr.

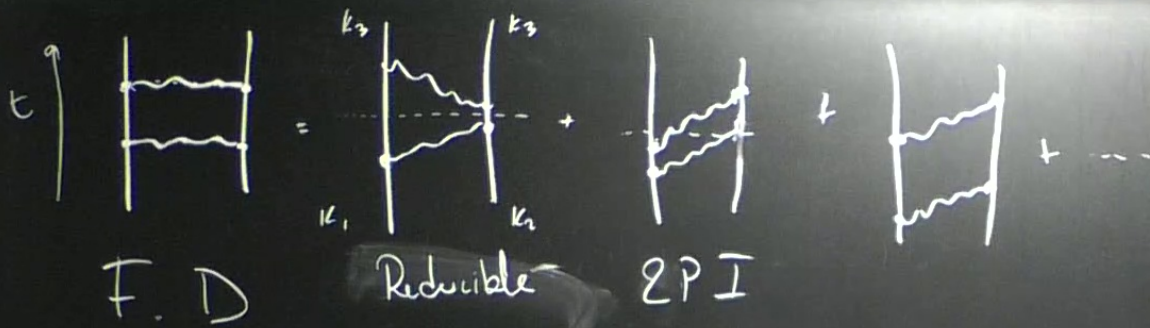
- Can you bound states and binding Energ

$$(H_0 + V)\psi = i\hbar \partial_t \psi$$

- Use chiral Lag. to constrain V .

$$\begin{aligned} \mathcal{L} = & D_\mu \bar{\pi} \cdot D^\mu \vec{\pi} + \bar{D} + D^6 + \dots & ; N = \begin{bmatrix} p \\ n \end{bmatrix} \\ & + \bar{N} (\not{\partial} + m + g \not{D} \vec{\pi} \cdot \vec{\tau} \gamma_5) N + \dots & \delta N = (\epsilon \times \frac{\vec{\pi}}{F}) \cdot \vec{\tau} N \\ & & \delta D N = (\epsilon \times \frac{\vec{\pi}}{F}) \cdot \vec{\tau} D_\mu N \end{aligned}$$





$$\textcircled{2PI} = f(k_1 \dots k_4) = \langle k_4 k_3 | V^{(2)} | k_1 k_2 \rangle$$

No Signal Please check your connection

- Use chiral Lag. to constrain V .

$$D_\mu \pi = \frac{\partial_\mu \pi}{1 + \pi^2} = \partial_\mu \pi + \dots$$

$$\mathcal{L} = D_\mu \vec{\pi} \cdot D^\mu \vec{\pi} + D^4 + D^6 + \dots$$

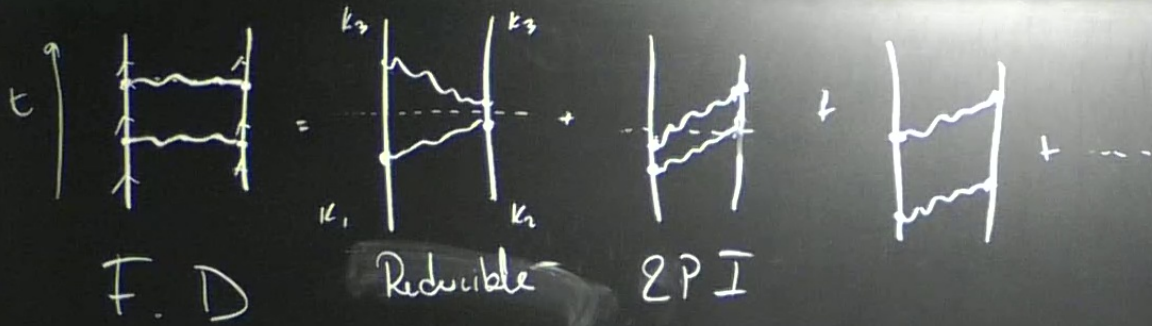
$$; N = \begin{bmatrix} P \\ n \end{bmatrix}$$

$$+ \bar{N} (\not{\partial} + m + g \not{D} \vec{\pi} \cdot \vec{\tau} \gamma_5) N + \dots$$

$$\delta N = (\epsilon \times \frac{\vec{\pi}}{1 + \pi^2}) \cdot \vec{\tau} N$$

$$\delta D N = (\epsilon \times \frac{\vec{\pi}}{1 + \pi^2}) \cdot \vec{\tau} D_\mu N$$





$$\textcircled{2PI} = f(k_1 \dots k_4) = \langle k_4 k_3 | V^{(2)} | k_1 k_2 \rangle$$

$$V^{(2)}(x, y) = \delta(x-y) + g^2 Y(x, y)$$



No Signal. Please check your connection

Polchinski: 92'
EFT's Cliff

Phono. L 's

I conductor e, m, M

$$\frac{e^2}{\hbar^2} m = 27 \frac{eV}{\epsilon_0}, T_{\text{room}} \sim 10 eV$$

$$E \ll \epsilon_0 \int d^3p \left[\psi_P^\dagger \dot{\psi}_P + (\epsilon_P - \epsilon_F) \psi_P^\dagger \psi_P \right]$$

Nuclear T

Polchinski: §2'
EFT's Cliff

Phono... L 's

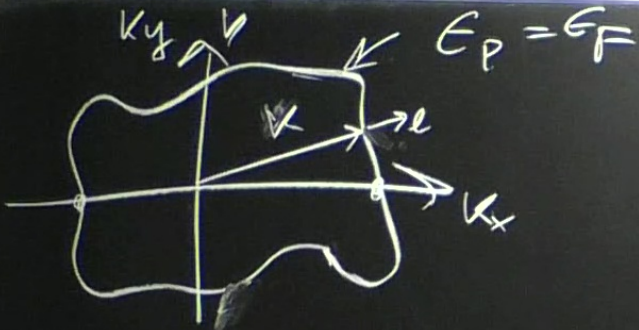
I conductor e, m, M

$$\frac{e^2}{\hbar^2} m$$

$$= 27 \frac{eV}{\epsilon_0}, T_{\text{room}} \sim 10^{-2} eV$$

$$E \ll \epsilon_0 \int d^3p \left[\psi_P^\dagger \psi_P + (\epsilon_P - \epsilon_F) \psi_P^\dagger \psi_P \right]$$

Nuclear T

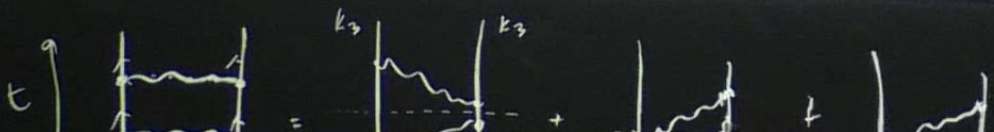


$$\begin{aligned}
 E &\rightarrow s E & (t &\rightarrow s^{-1} t) \\
 \ell &\rightarrow s \ell & \vec{p} &= \vec{k} + \vec{\ell} \\
 \psi &\rightarrow s^{-1/2} \psi
 \end{aligned}$$

$$V_{int} = \sum_{\substack{k_1, k_2 \\ k_3, k_4}} \int_{P_1 P_2 P_3 P_4} \psi_{P_1}^\dagger \psi_{P_3} \psi_{P_2}^\dagger \psi_{P_4} \delta(p_1 + p_2 - p_3 - p_4)$$

$$V_{int} \rightarrow s V_{int} \text{ , special kinematics: } V_{int} \rightarrow s^0 V_{int}$$

No Signal. Please check your connection



$$\langle GB | \psi^0 | 0 \rangle \neq 0$$

$$\xi^m : \nabla_\mu \xi_\nu$$

$$g^{\mu\nu} = T^{\mu}_{\nu} \xi^{\nu}$$

spacetime \rightarrow Lattice
symmetries \rightarrow symmetries

3 pions

$$SU(2) \times SU(2) \rightarrow SU(2)$$

phonons

$$\int \mathcal{H} d^3q \left[\underbrace{\dot{D}^2 + \frac{g_{\mu\nu}}{\hbar M} \Delta g}_{\text{phonons}} \right] \langle GB | T^0 | 0 \rangle \neq 0$$

$$\langle GB | \psi^0 | 0 \rangle \neq 0$$

$$\xi^M : \nabla_\mu \xi_\nu$$

$$\xi^{\mu\nu} = T^{\mu\nu} \xi^{\nu}$$

$$\int \mathcal{H} d^3g \left[\underbrace{\dot{D}^2 + \frac{g_{\mu\nu}}{\hbar M} \Delta g}_{\text{}} \right] \langle GB | T^0_i | 0 \rangle \neq 0$$

$$\int \mathcal{P} \mathcal{P} \mathcal{P} \mathcal{P} \quad 4+4D$$

spacetime \rightarrow Lattice
symmetry symmetry

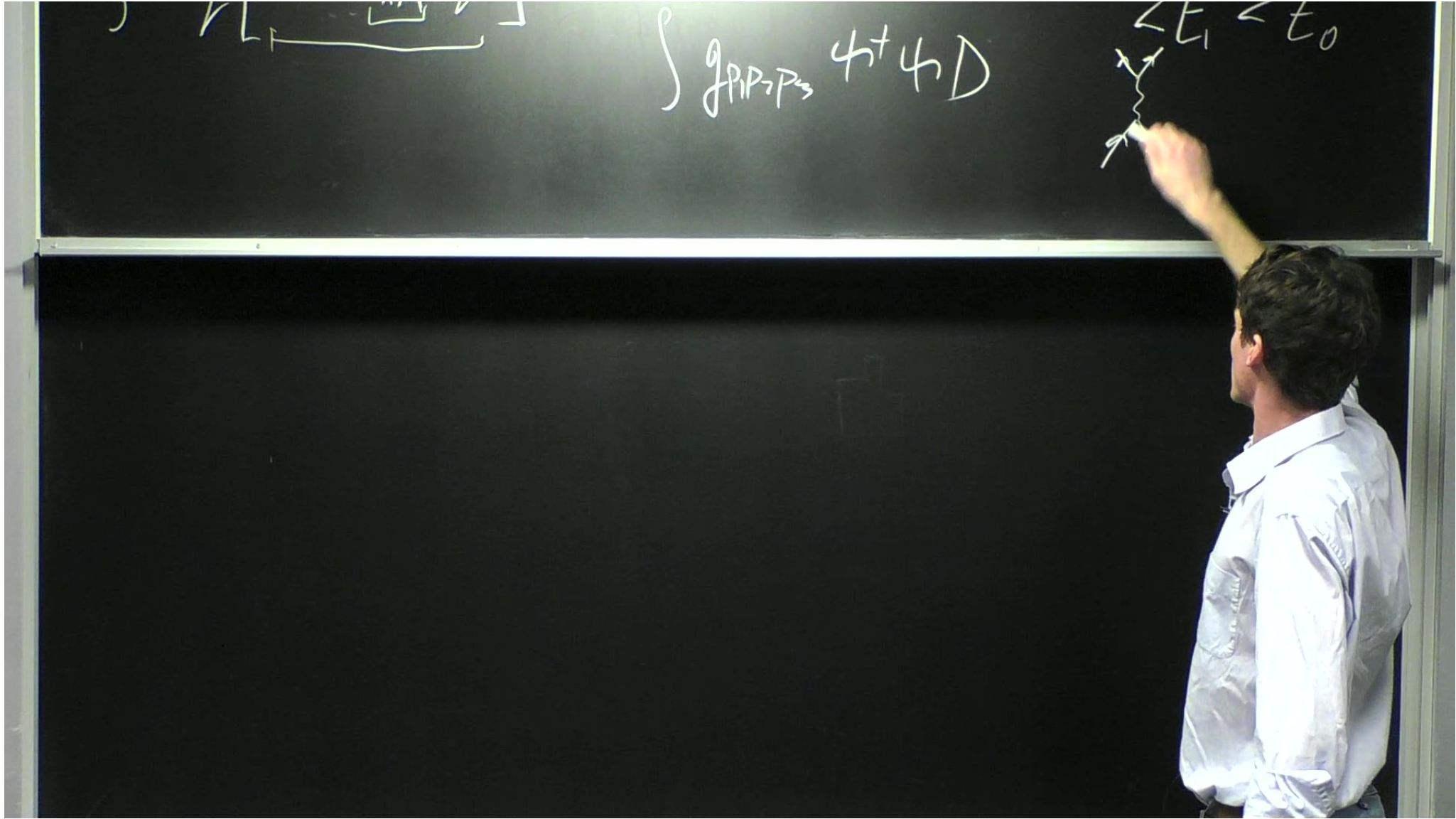
3 pions

$SU(2) \times SU(2)$

3 phonons

$\langle E_i$





EFT's Cliff

I conductor e, m, M

$$\frac{e^2}{\hbar^2} m = 27 \frac{eV}{\tau_0}, \quad T_{\text{room}} \sim 10^{-2} eV$$

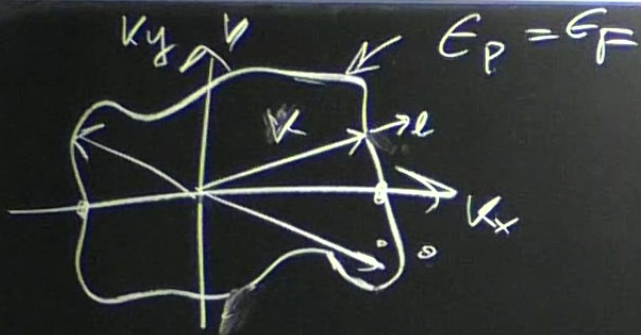
$$E \ll \tau_0 \left[\int A \mathbf{k} d\mathbf{k} \right] \left\{ \psi_P^\dagger \psi_P + (\underbrace{\epsilon_P - \epsilon_F}_{\neq l}) \psi_P^\dagger \psi_P \right\} + V_{\text{int}}$$

$$w = v_F l$$

$$\epsilon_P = \epsilon_k + \underbrace{\partial_p \epsilon_p}_l$$

o o o
o o o
o o o
o o o

Nuclear From Ch. Lagr.
- Can you bound states

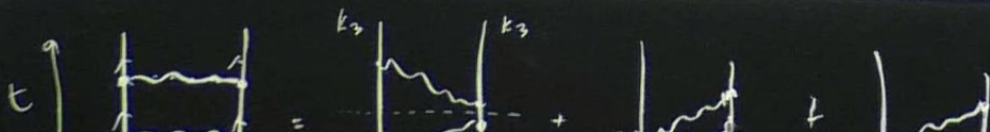


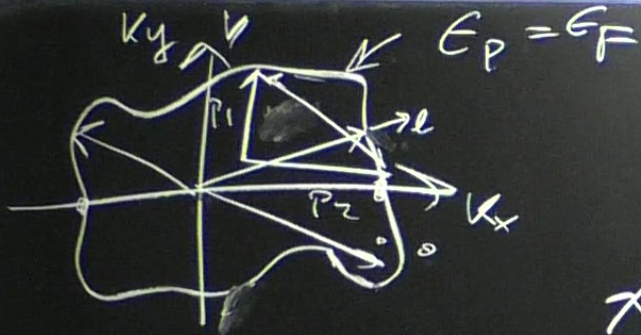
$$\begin{aligned}
 E &\rightarrow s E & (t &\rightarrow s^{-1} t \\
 l &\rightarrow s l & \vec{p} &= \vec{k} + \vec{l} \\
 \psi &\rightarrow s^{-1/2} \psi
 \end{aligned}$$

$$V_{int} = \int \prod_{i=1}^4 V_{P_i} \psi_{P_1}^\dagger \psi_{P_2} \psi_{P_3}^\dagger \psi_{P_4} \delta(\underbrace{P_1 + P_2 - P_3 - P_4}_{k_1 + k_2 + k_3 + k_4})$$

$V_{int} \rightarrow V_{int}$, special kinematics: $V_{int} \rightarrow s V_{int}$

No Signal. Please check your connection





$$E \rightarrow s E \quad (t \rightarrow s^{-1} t)$$

$$l \rightarrow s l \quad \vec{P} = \vec{K} + \vec{L}$$

$$\psi \rightarrow s^{-1/2} \psi$$

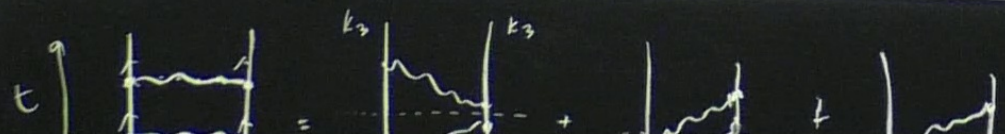


$$V_{int} = \int d^4x \sum_{P_1 P_2 P_3 P_4} \psi_{P_1}^+ \psi_{P_2} \psi_{P_3}^+ \psi_{P_4} \delta(\underbrace{P_1 + P_2 - P_3 - P_4}_{k_1 + k_2 + k_3 + k_4})$$

k_1, k_2, k_3, k_4
 l_1, l_2, l_3, l_4

$V_{int} \rightarrow V_{int}$, special kinematics: $V_{int} \rightarrow s V_{int}$

No Signal. Please check your connection



The (classical) EFT

Guiding principles:

- ① $\{g_{\mu\nu}, \psi\}$ are the correct degrees of freedom to describe low-energy physics
- ② diffeo. invariance
- ③ curvatures are small

The (classical) EFT

Guiding principles:

① $\{g_{\mu\nu}, \psi\}$ are the correct degrees of freedom
to describe low-energy physics

② diffeo. invariance

③ curvatures are small

$g, \partial g, \partial\partial g, \sqrt{g} \partial^2 \psi, \dots$

$$D_\mu A^\nu = \partial_\mu A^\nu + \Gamma_{\mu\lambda}^\nu A^\lambda$$

\Downarrow derivative expansion!

The (classical) EFT

$$S = \int d^4x \sqrt{g} \left(\overset{\partial^0}{\Lambda} + \overset{\partial^2}{\frac{2}{\kappa^2} R} + c_1 \overset{\partial^4}{R^2} + c_2 R_{\mu\nu} R^{\mu\nu} + \dots \right)$$

$\underset{\approx 0}{\Lambda}$
 $\underset{= 32\pi G \sim 1/M_P^2}{\frac{2}{\kappa^2}}$
 $\overset{O(1)}{\uparrow} c_1$
 $\overset{O(1)}{\uparrow} c_2$

and $\mathcal{L}_{\text{matter}}!$

\downarrow
 ∂^6
 \downarrow



Sketchy notation:

$$\mathcal{L} = \frac{2}{\kappa^2} R + c R^2 + \mathcal{L}_{\text{matter}} .$$

$$\mathcal{L} = \frac{2}{\kappa^2} R + c R^2 + \mathcal{L}_{\text{matter}}$$

Newtonian potential, take 1

$$g_{\mu\nu} = \eta_{\mu\nu} + \kappa h_{\mu\nu} \quad + \quad G_\alpha(h) = 0 \quad \text{gauge fixing}$$

↓

EOM

$$\square h_{\mu\nu} + \kappa^2 c \square \square h_{\mu\nu} = 8\pi G T_{\mu\nu}$$

↙ q^2 ↙ q^4

Green's function: $\int d^4 q \frac{e^{iq \cdot x}}{q^2 + \kappa^2 c q^4} = \int d^4 q e^{iq \cdot x} \left[\frac{1}{q^2} - \frac{1}{q^2 + (1/\kappa^2 c)} \right]$

$$\mathcal{L} = \frac{2}{\hbar^2} R + c R^2 + \mathcal{L}_{\text{matter}}$$

Newtonian potential, take 1

But no need to worry!

$$\int d^4 q e^{iq \cdot x} \frac{1}{q^2} \xrightarrow{\text{FOURIER}} - \frac{G m_1 m_2}{r}$$

$$\int d^4 q e^{iq \cdot x} \left[- \frac{1}{q^2 + (1/\hbar^2 c)} \right] \longrightarrow \frac{G m_1 m_2}{r} e^{-\frac{r}{\hbar c}}$$

$$\mathcal{L} = \frac{2}{\kappa^2} R + c R^2 + \mathcal{L}_{\text{matter}}$$

Newtonian potential, take 1

But no need to worry!

$$\int d^4 q e^{iq \cdot x} \frac{1}{q^2} \xrightarrow{\text{FOURIER}} - \frac{G_{m_1, m_2}}{r}$$

$$\frac{1}{q^2 + \kappa^2 c q^4} = \frac{1}{q^2} - \kappa^2 c + \dots$$

$$\int d^4 q e^{iq \cdot x} \left[- \frac{1}{q^2 + (1/\kappa^2 c)} \right] \longrightarrow \frac{G_{m_1, m_2}}{r} e^{-\frac{r}{\kappa \sqrt{c}}} \sim c \kappa^4 \delta^3(r)$$

Ghosts are heavily suppressed, only playing a role at the scale of new physics.

$$\mathcal{L} = \frac{2}{\hbar^2} R + c R^2 + \mathcal{L}_{\text{matter}}$$

Newtonian potential, take 1

Remark: in modern treatments, replace

$$\mathcal{L} = \frac{2}{\hbar^2} R + \underset{\substack{\uparrow \\ O(1)}}{c} R^2 \quad \text{with} \quad \mathcal{L} = \frac{2}{\hbar^2} \left(R + \underset{\substack{\uparrow \\ O\left(\frac{1}{M_s^2}\right)}}{c} R^2 \right).$$

Allows for possibility that new physics appears below M_{planck} .

Analogy:

	Naive SONP	Actual SONP
Gravity	M_{planck}	" M_{string} "
Weak interactions	100 GeV	$M_{Z\text{-boson}} \sim 70 \text{ GeV}$

<http://www.hartmanhep.net/topics2015/gravity-lectures.pdf>

Newtonian potential, take 2 : "quantum" EFT @ tree level

$$g_{\mu\nu} = \bar{g}_{\mu\nu} + \kappa h_{\mu\nu}$$

\bar{g} solves EE

$$\sqrt{g} \mathcal{L}_{\text{grav.}} = \sqrt{g} \frac{2}{\kappa^2} R = \sqrt{\bar{g}} \left(\frac{2}{\kappa^2} \bar{R} + \bar{D} h \bar{D} h + \bar{R} h^2 \right)$$

$$Z \neq \int \mathcal{D}h_{\mu\nu} e^{iS} \rightsquigarrow Z = \int \mathcal{D}h_{\mu\nu} \underbrace{\delta(G_\alpha(h))}_{\text{More } \bar{D} h \bar{D} h} \underbrace{\det \left| \frac{\delta G_\alpha}{\delta E_B} \right|}_{\eta^* [\bar{D}^2 \bar{g} - \bar{R}] \eta} e^{iS}.$$

Newtonian potential, take 2 : "quantum" EFT @ tree level

A nice quadratic theory!

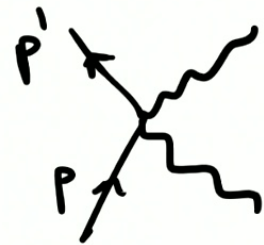
$$\mathcal{L} = -\frac{1}{2} h_{\alpha\beta} D^{\alpha\beta, \gamma\delta} h_{\gamma\delta} + \text{ghost} + (\bar{g}, \bar{R}) + \mathcal{L}_{\text{matter}}$$

$$g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi$$

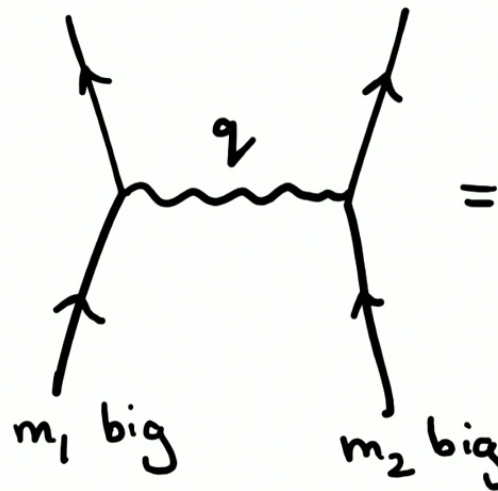
$$q \text{ wavy line} = \frac{i}{q^2 + i\epsilon} (\eta\eta)$$



$$P \text{ and } P' \text{ meeting at a vertex with a wavy line} = -\frac{i\kappa}{2} (pp' - \bar{g}_{\mu\nu} (p \cdot p' - m^2))$$



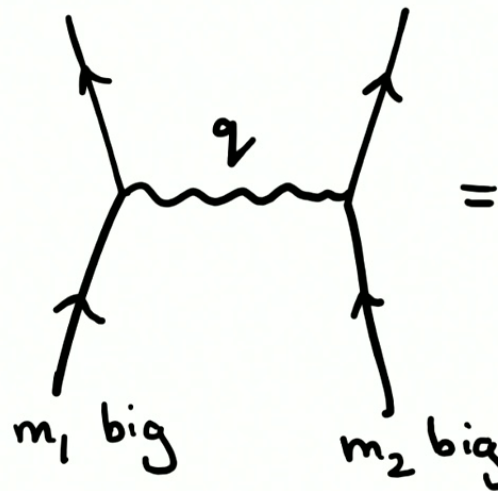
Newtonian potential, take 2 : "quantum" EFT @ tree level



A Feynman diagram showing two external lines representing massive particles. The left line is labeled m_1 big and the right line is labeled m_2 big. Both lines have arrows pointing upwards. They are connected by a wavy internal line representing a graviton, with a label g above it. To the right of the diagram is an equals sign followed by a hash symbol and a fraction: $\frac{G m_1 m_2}{q^2}$. Below the q^2 in the denominator is a small downward-pointing arrow. An arrow labeled "FOURIER" points to the right, leading to a minus sign followed by a fraction: $-\frac{G m_1 m_2}{r}$.

$$= \# \frac{G m_1 m_2}{q^2} \xrightarrow{\text{FOURIER}} - \frac{G m_1 m_2}{r}$$

Newtonian potential, take 2 : "quantum" EFT @ tree level

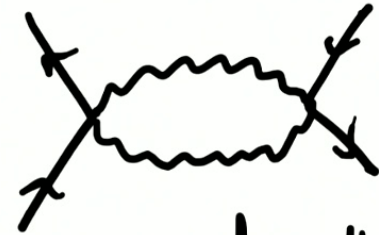


A Feynman diagram showing two external lines representing massive particles. The left line is labeled m_1 big and the right line is labeled m_2 big. Both lines have arrows pointing upwards. They are connected by a wavy internal line representing a graviton, labeled with q and a downward arrow. To the right of the diagram is an equals sign followed by a hash symbol and the expression $\frac{G m_1 m_2}{q^2}$, where q^2 has a downward arrow. An arrow labeled "FOURIER" points to the right, leading to the expression $-\frac{G m_1 m_2}{r}$.



For all our hard work?!

Loops: a taste of non-reno.



$$d = 4 - \epsilon$$

$\frac{2}{k^2} R$

$$\mathcal{L} = -\frac{1}{2} h_{\mu\nu} \mathcal{D}^{\alpha\beta, \gamma\delta} h_{\gamma\delta} + \text{ghost} + (\bar{g}, \bar{R}) + \mathcal{L}_{\text{matter}}$$

$$Z[\bar{g}] = \int \mathcal{D}h e^{i \int d^4x \mathcal{L}}$$

needs

$$\mathcal{L}_{\text{ct}}^{\text{1-loop}} = \frac{1}{8\pi^2 \epsilon} \left(c_1 \bar{R}^2 + c_2 \bar{R}_{\mu\nu} \bar{R}^{\mu\nu} \right).$$

New !!

$$c_1^{(r)} = c_1 + \frac{\#}{\epsilon}$$

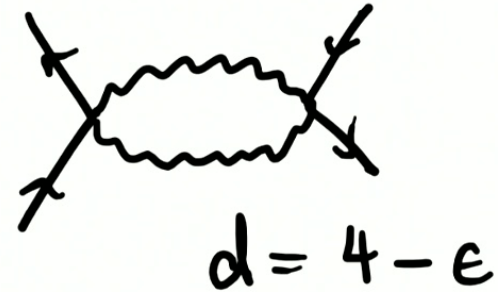
$$c_2^{(r)} = c_2 + \frac{\#}{\epsilon}$$

$$1 \text{ loop} \rightarrow R^2 + (R_{\mu\nu})^2$$

$$2 \text{ loops} \rightarrow (R_{\mu\nu\rho\sigma})^3$$

$$3 \text{ loops} \rightarrow R_{\mu\nu}^4 \dots$$

Loops: a taste of non-reno.



$\frac{2}{k^2} R$

$$\mathcal{L} = -\frac{1}{2} h_{\alpha\beta} \mathcal{D}^{\alpha\beta, \gamma\delta} h_{\gamma\delta} + \text{ghost} + (\bar{g}, \bar{R}) + \mathcal{L}_{\text{matter}}$$

$Z[\bar{g}] = \int \mathcal{D}h e^{i \int d^4x \mathcal{L}}$ needs

$$\mathcal{L}_{\text{ct}}^{\text{1-loop}} = \frac{1}{8\pi^2 \epsilon} \left(c_1 \bar{R}^2 + c_2 \bar{R}_{\mu\nu} \bar{R}^{\mu\nu} \right).$$

New !!

$$c_1^{(r)} = c_1 + \frac{\#}{\epsilon}$$

$$c_2^{(r)} = c_2 + \frac{\#}{\epsilon}$$

1 loop $\rightarrow R^2 + (R_{\mu\nu})^2$

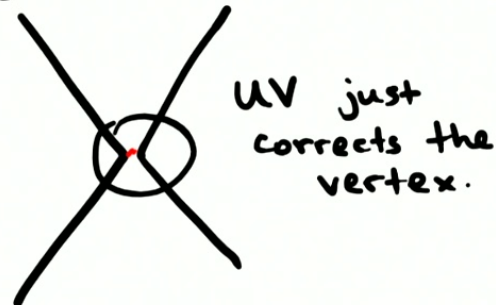
2 loops $\rightarrow (R_{\mu\nu\rho\sigma})^3$

3 loops $\rightarrow R_{\mu\nu}^4 \dots$

The key point: one can renormalize the theory at any given order.

Predictions in EFT

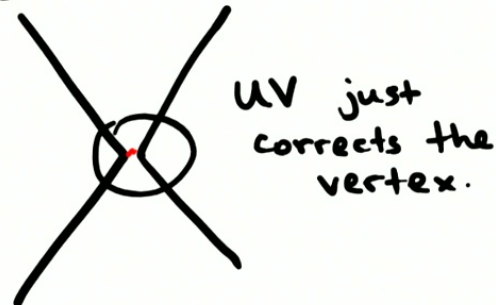
Key assumption: local terms in \mathcal{L} account for the most general high-energy effects.



So if a loop gives a nonlocal divergence, we are seeing a genuinely low-energy effect.

Predictions in EFT

Key assumption: local terms in \mathcal{L} account for the most general high-energy effects.



So if a loop gives a nonlocal divergence, we are seeing a genuinely low-energy effect.

Nonlocal = nonanalytic in \vec{k} space.

Newtonian potential, take 3 : 1-loop

NONLINEAR
CLASSICAL

QUANTUM
LOOP

???

Final result:

$$V(q) = \frac{Gm_1 m_2}{q} \left(1 + \underbrace{a G q^2 \sqrt{\frac{m^2}{-q^2}} + b G q^2 \ln(-q^2)}_{\text{NON-ANALYTIC}} + c G q^2 \right)$$

$$V(r) = - \frac{Gm_1 m_2}{r} \left(1 + \underbrace{a \frac{Gm}{rc^2} + b \frac{G\hbar}{r^2 c^3}}_{\text{True low-energy prediction: } a, b \text{ indep. of } C_1^{(r)}, C_2^{(r)}, \text{ etc.}} + \underbrace{c G^2 \delta^3(r)}_{\text{Suppressed UV effect.}} \right)$$

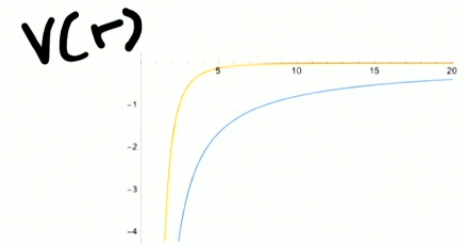
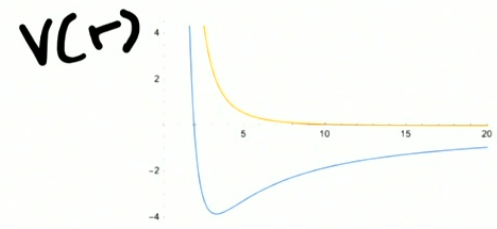
How big?

$$b \frac{G \hbar}{r^2 c^3} = b \left(\frac{l_{\text{Planck}}}{r} \right)^2.$$

"unlikely to generate an active phenomenology"

What's b ?

A series of papers b/w '93-'02
are consistently confused.
Even about the sign!



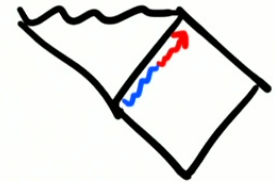
Exceptions to the game: theories w UV/IR mixing

- String theory
- Noncommutative (quantum) geometry
- Holography
- Arguably, any theory of QG:
 - o UV collisions/fluctuations can create BH!
 - o Gravitational redshift means UV at horizon = IR far away!



Exceptions to the game: theories w UV/IR mixing

- String theory
- Noncommutative (quantum) geometry
- Holography
- Arguably, any theory of QG:
 - o UV collisions/fluctuations can create BH!
 - o Gravitational redshift means UV at horizon = IR far away!



Then, why care? My favorite 2 reasons:

- Does Lambda run? (Cosmology)
- Does G run, such that generalized BH entropy is well-defined? (Susskind-Uglum conjecture)

