

**Title:** Lecture - QFT II, PHYS 603

**Speakers:** Francois David

**Collection/Series:** Quantum Field Theory II (Core), PHYS 603, November 12 - December 11, 2024

**Subject:** Condensed Matter, Particle Physics, Quantum Fields and Strings

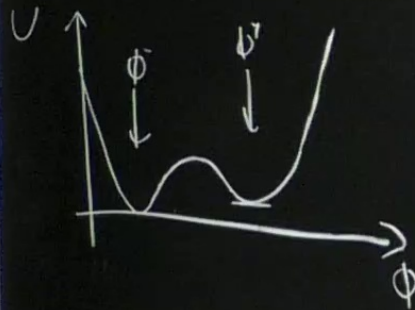
**Date:** November 26, 2024 - 9:00 AM

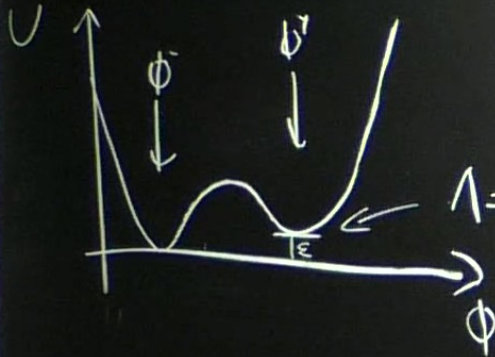
**URL:** <https://pirsa.org/24110015>

# Black holes as bubble nucleation sites

[14101.0017]

Gregory, Mass, Withers





$$\lambda = \frac{z}{\epsilon^2} = 8\pi\epsilon > 0$$

Assumptions:  $\Gamma \sim e^{-\frac{\beta}{\hbar}}$ ,  $\beta = S_F(\psi) - S_E(\psi^+)$

$$ds^2 = -f(r)dt^2 + \frac{1}{f(r)}dr^2 + r^2 d\Omega^2$$

$$f_- = 1 - \frac{2M_-}{r}, \quad f_+(r) = 1 - \frac{2M_+}{r} + \frac{r^2}{\lambda^2}$$



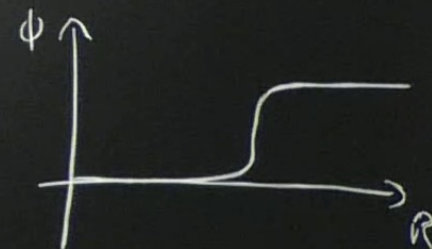
Israel junction conditions:

$$h_{ab}^+ - h_{ab}^- = 0$$

$$K_{ab}^+ - K_{ab}^- = -8\pi G \left( T_{ab}^{\text{wall}} - \frac{1}{2} h_{ab} T^{\text{wall}} \right)$$

$$T_{ab}^{\text{wall}} = -\sigma h^{ab}$$

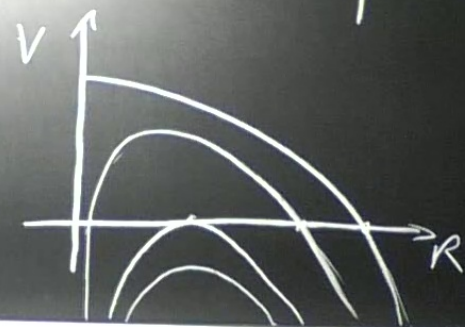
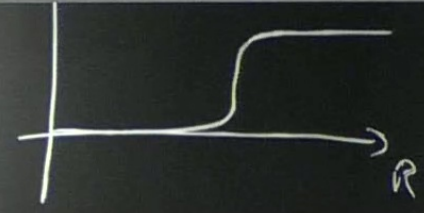
$$\Rightarrow \text{EOM: } \ddot{R} + V_{\sigma, \ell, M^+, M^-} = 0, \dot{t} = \dots$$





T<sub>well</sub>  
T<sub>ab</sub>

$$\Rightarrow \text{EOM: } \ddot{R} + V_{\sigma, R, M, M} = 0, \quad t = \dots V \uparrow$$

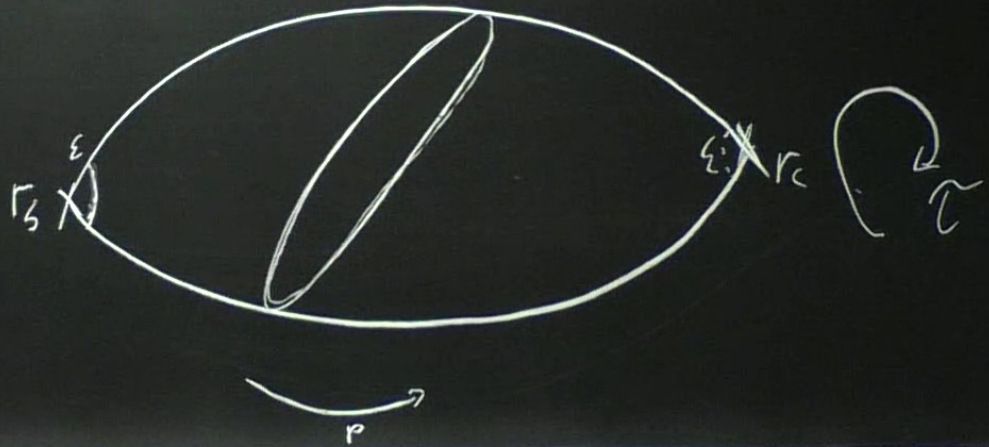


$$t \rightarrow -i\tau$$

Near horizon BH:

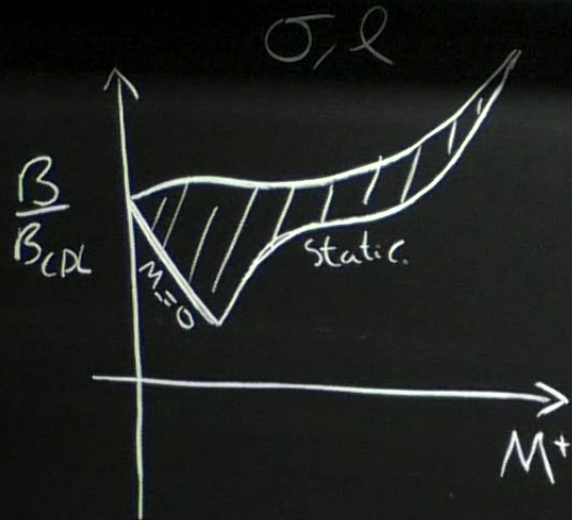
$$ds^2 = f'(r_s)(r-r_s)d\tau^2 + \frac{1}{f'(r_s)(r-r_s)} dr^2 + r^2 d\Omega^2 \rightarrow d\rho^2 + \rho^2 \left( \frac{\sqrt{f'(r_s)}}{2} d\tau \right)^2 + r^2 d\Omega^2$$

$$\int_E^M = \int_E^{M-B} + \int_E^B$$





$$f_- = 1 - \frac{2M_-}{r}, \quad f_+(r) = 1 - \frac{2M_+}{r} + \frac{r^2}{l^2}$$



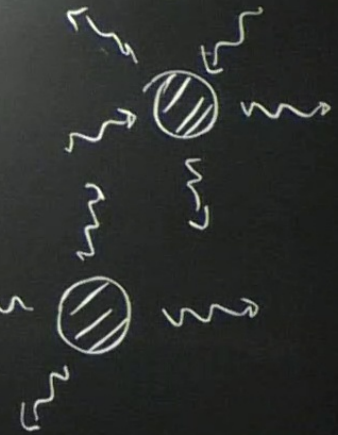


2105.0933

Euclidean bounce = thermal equilibrium  
[HH state]

vs

realistic BH [Unruh state]



Israel junction conditions:

$$h^+ = h^- = 0$$

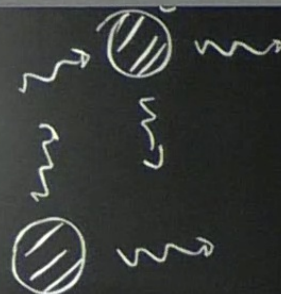
$$K_i^+ - K_i^- = -8\pi G (T_{wall} - \frac{1}{2} h_i T)$$

Euclidean

equilibrium  
[H state]

vs

realistic BH [Unruh state]

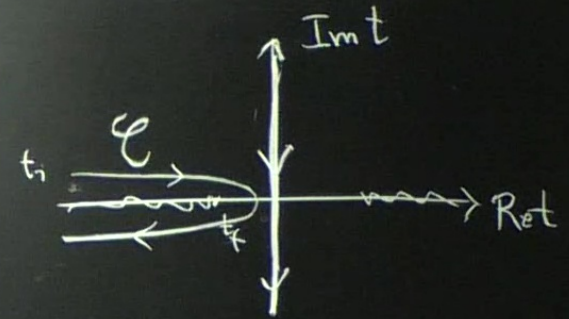


$$\phi|_{t_f} = \phi'|_{t_i} = \varphi_F$$

$$P_{\text{decay}} = \sum_F \underbrace{|\langle f | i \rangle|^2}_{\int \mathcal{D}\varphi_i \mathcal{D}\varphi_f \mathcal{D}\phi} e^{iI[\phi]} \langle f | \varphi_f, t_f \rangle \langle \varphi_i, t_i | i \rangle$$



$$P_{\text{decay}} = \int D\varphi'_2 D\varphi_1 D\varphi_2 e^{iI[\varphi_2]} \underbrace{\langle \varphi, t_2 | \varphi', t_2 \rangle}_{\rho_2} \phi_2 |_{t_2} \sim \text{true solution}$$



Semiclassical appr.

$$\phi_b$$

$$t \rightarrow -i\tau$$



$$P_{decay} = \int \mathcal{D}\varphi'_i \mathcal{D}\varphi_f \mathcal{D}\varphi_i$$

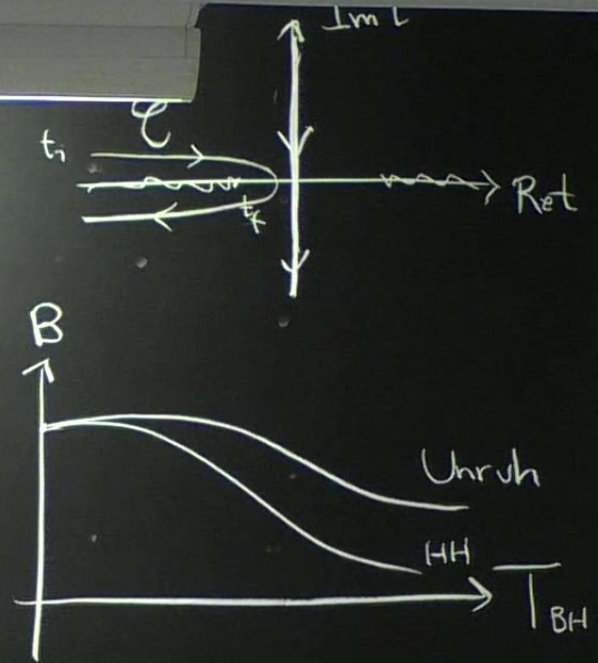
$$\phi_{\varphi|t_f} \sim \text{true solution} \langle \varphi, t_2 | \varphi', t_2 \rangle$$

$\rho_2$

Semiclassical appr.

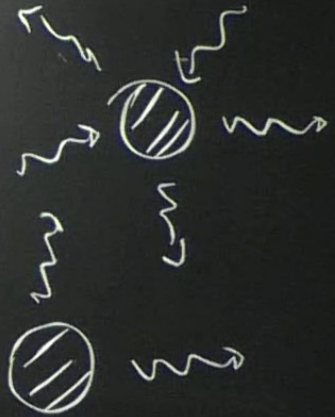
$$\phi_b$$

$$\Gamma \sim e^{-B}$$



2105.0933

Euclidean bounce = thermal equilibrium  
[HH state]



vs

realistic BH [Unruh state]



$$\phi|_{t_f} = \phi|_{t_i} = \varphi_F$$

$$P_{\text{decay}} = \sum_F \underbrace{|\langle f | i \rangle|^2}_{\int \mathcal{D}\varphi_i \mathcal{D}\varphi_f \mathcal{D}\phi} e^{-2I[\phi]} \langle f | \varphi_{t_f}, t_f \rangle \langle \varphi_{t_i}, t_i | i \rangle$$



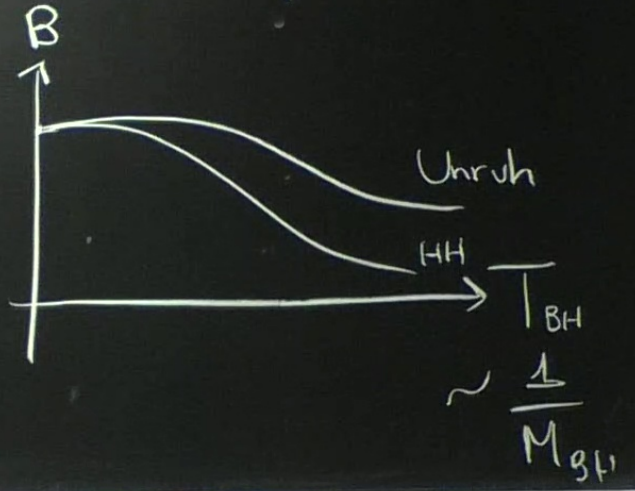
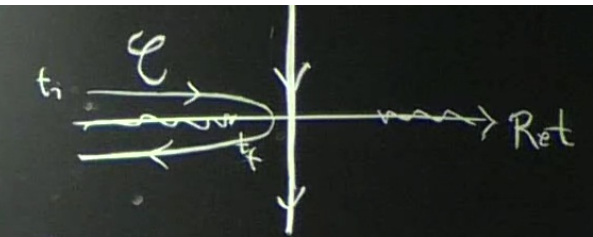
$$P_{decay} = \int D\varphi_1 D\varphi_2 D\varphi_3 e^{-S}$$

$$\phi_{cl}|_{t_1} \sim \text{true vacuum} \langle \varphi, t_2 | \underbrace{\rho_2}_{\rho_2} | \varphi', t_2 \rangle$$

Semiclassical appr.

$$\phi_b$$

$$\Gamma \sim e^{-B}$$

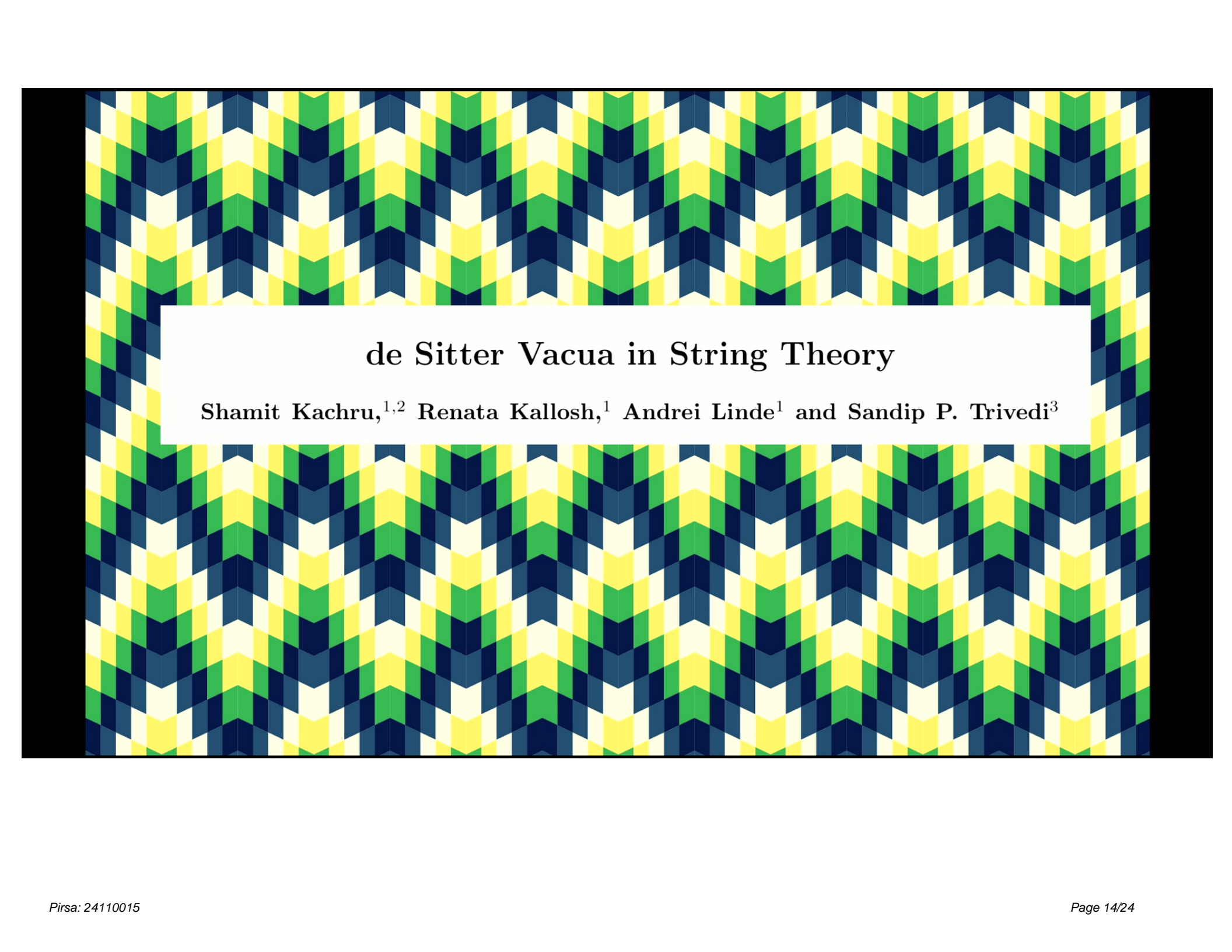


$i\tau$

horizon BH:

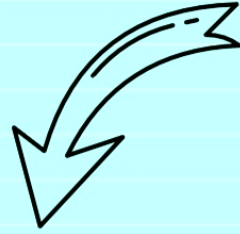
$$ds^2 = -dt^2 + dr^2 + \rho^2 d\Omega^2$$





# de Sitter Vacua in String Theory

Shamit Kachru,<sup>1,2</sup> Renata Kallosh,<sup>1</sup> Andrei Linde<sup>1</sup> and Sandip P. Trivedi<sup>3</sup>



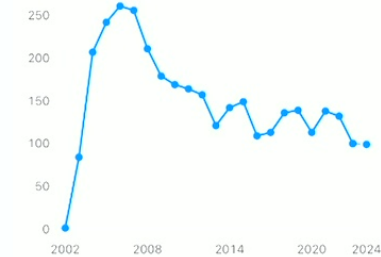
### De Sitter vacua in string theory

Shamit Kachru (Stanford U., Phys. Dept. and SLAC), Renata Kallosh (Stanford U., Phys. Dept.), Andrei D. Linde (Stanford U., Phys. Dept.), Sandip P. Trivedi (Tata Inst.)  
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Citations per year



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# Plan for the talk:

- I) Some reasons why it is hard to find de Sitter vacuum in string theory
- II) Overview of the KKLT construction
- III) Stability of the solution, relation to
- IV) People still talk about it! Controversies and relation to The Swampland Program

GRAVITATIONAL EFFECTS ON AND OF VACUUM DECAY\*  
Sidney Coleman<sup>†</sup>  
Stanford Linear Accelerator Center  
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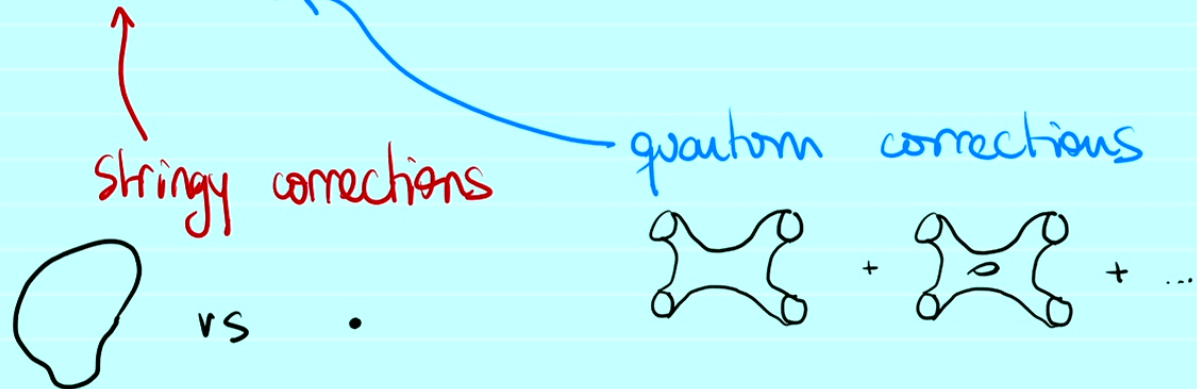


I) Some reasons why it is hard to find de Sitter vacuum in string theory

- No-go theorem by [Maldacena, Nuñez ; '00]

In the second part of this paper, which can be read independently of the first, we show that there are no non-singular Randall-Sundrum or de-Sitter compactifications for large class of gravity theories.

- without sources
- without  $\alpha'$  or  $g_s$  corrections

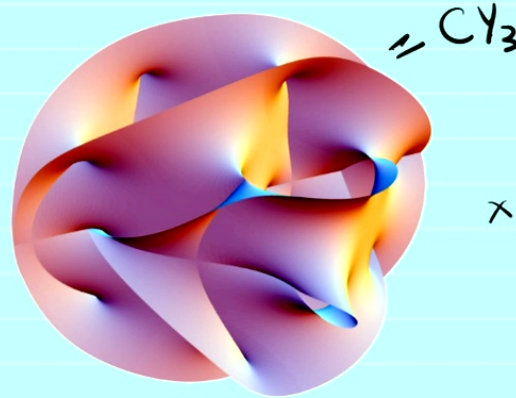


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(I) Some reasons why it is hard to find de Sitter vacuum in string theory compactifications

- Moduli stabilization

10d spacetime =



$\times M_{4d}$  ←  
where we live

moduli  $\equiv$  massless fields characterizing  $CY_3$

- shape

- size

...

- Scale separation

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## ② Overview of the KKLT construction

Two steps:

① Stabilize all moduli in a supersymmetric way

1.1 Fix all moduli except for volume with fluxes

1.2 Fix the volume with quantum corrections

AdS vacuum with exponentially large warping

② Break supersymmetry and get a de Sitter vacuum  $\rightarrow$  introducing  $\overline{D3}$

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### III) Stability of the solution

The de Sitter vacua is metastable so following Coleman, De Luccia they argue

1) Do our dS vacua survive for a large number of Planck times? For instance, if we fine tune to get a small cosmological constant, is the dS vacuum sufficiently stable to survive during the  $10^{10}$  years of the cosmological evolution? If the answer is positive, one can use the dS minimum for the phenomenological description of the current stage of acceleration (late-time inflation) of the universe.

2) Is the typical decay time of the dS vacuum longer or shorter than the recurrence time  $t_r \sim e^{S_0}$ , where  $S_0 = \frac{24\pi^2}{V_0}$  is the dS entropy [43]? If the decay time is longer than  $t_r \sim e^{S_0}$ , one may need to address the issues about the consistency of the stringy description of dS space raised in [2, 5, 8].



to these questions

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① Thin wall approximation

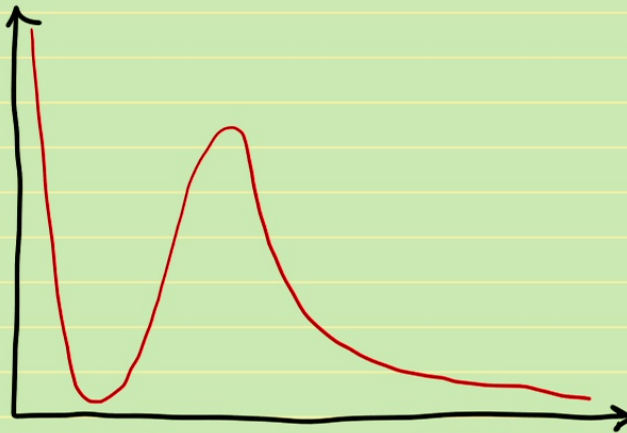
$$P \approx \exp(-S(\varphi_0)) = \exp\left(-\frac{24\pi^2}{V_0}\right) \sim \exp(-10^{122}) .$$

$$t_{\text{decay}}^{\text{CDL}} \sim t_r \exp\left(-\frac{64\pi^2}{T^2}\right)$$

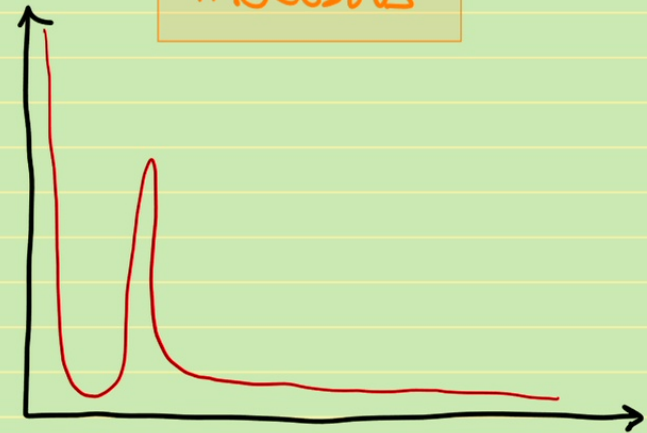
② No wall approximation

$$t_{\text{decay}}^{\text{HM}} = e^{-S_1+S_0} = t_r \exp\left(-\frac{24\pi^2}{V_1}\right) \ll t_r .$$

DIFFERENT  
PHYSICAL  
PROCESSES



vs



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## IV

## Criticisms to KKLT

- Does the  $\overline{D3}$  mechanism really work?  
singularities, backreaction, stability ...
- Moduli stabilisation  
separation of scales  $\begin{matrix} \uparrow \\ m_{\text{c}} \\ m_{\text{p}} \end{matrix}$   $\leftarrow$  can you justify the hierarchy?
- Are the  $\alpha'$  and  $g_s$  corrections really controlled?  
 $\oplus$  non easy no instability concerns  
Dine-Seiberg problem
- Explicit construction with consistent uplift to 10d string theory?

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IV

## The de Sitter conjecture and the Swampland program

### Conjecture 9: de Sitter Conjecture

A scalar potential of an EFT weakly coupled to Einstein gravity must satisfy

$$M_P \frac{|\nabla V|}{V} \geq c, \quad (9.1)$$

with  $c$  some  $\mathcal{O}(1)$  constant. This was further refined by stating that the previous bound only needs to be imposed if the following condition on the second derivative of the potential is violated,

$$\min(\nabla_i \nabla_j V) \leq \frac{-c' V}{M_P^2}, \quad (9.2)$$

with  $c'$  another  $\mathcal{O}(1)$  constant. This way, only dS minima (and not critical points in general) are ruled out.

No proof for this conjecture but people believe no de Sitter solution has been well formulated yet.

ongoing research program

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## ② Overview of the KKLT construction

① Stabilize all moduli in a supersymmetric way

1.1 Fix all moduli except for volume with fluxes

- Axio-dilaton  $\tau = G_0 + i e^{-\phi}$
  - Complex structure  $S^1 \times S^1 \xrightarrow{\tau} X_{CY4}$
- $\downarrow$   
 $M_{CY3}$   
 $\cong$

But the volume  $\rho$  (Kähler modulus) does not appear in the potential  $\rightarrow$  FLAT DIRECTION

Find exponentially large warping in the compactification

$$ds_{10}^2 = e^{2A(y)} \eta_{\mu\nu} dx^\mu dx^\nu + e^{-2A(y)} \tilde{g}_{mn} dy^m dy^n$$

$$e^{A_{\min}} \sim e^{-\frac{20K}{3g_s M}}$$