

Title: Vision Talk

Speakers:

Collection: Celestial Holography Summer School 2024

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Celestial Holography

Past, Present and Future

Andy Strominger
Perimeter/Simons Celestial Summer School
July 2024

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Talk Outline

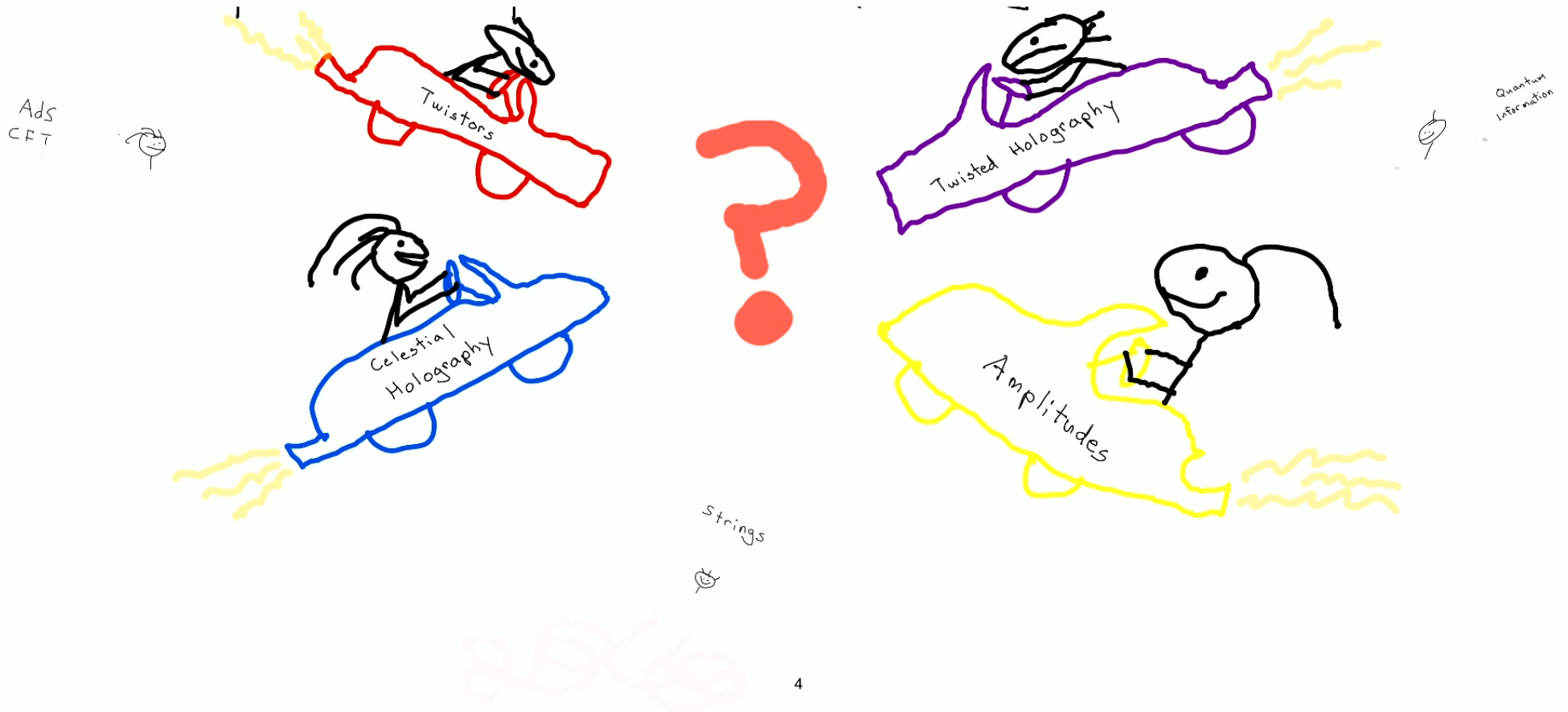
Talk Outline

- Motivations, assumptions and philosophy
- Highlights of some basic **past** results
- **Present** conundrums

My motivation, assumptions and philosophy

- We have learned a fantastic amount, much of it driven by string theory over the last 40 years, about quantum mechanics, gravity and QFT. The time is ripe to apply these insights to learn something about quantum gravity in the **real world**.
- Assume the **holographic principle** holds in flat space as well as BHs and AdS \Leftrightarrow QG S-matrix = QFT on 'spacetime boundary'.
- Take **lessons** from, but do not assume, **string theory** or **AdS/CFT**.
- Not seeking TOE, or even fundamental new laws of physics. (Although would be happy to find them!) Largely **bottom-up**.
- Guided by (i) self-consistency (ii) symmetries (iii) top-down toy models = **very powerful guides**.

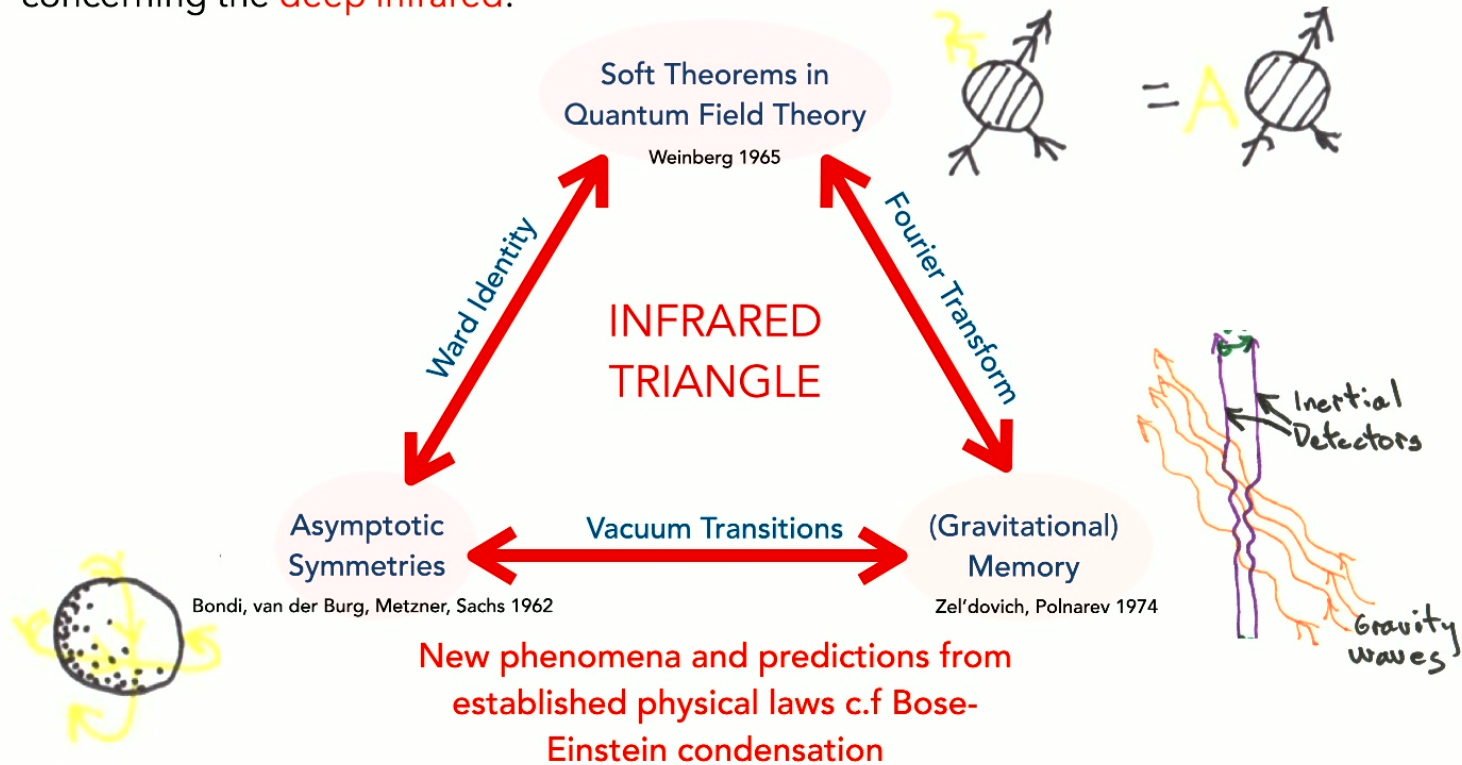
This is my perspective: as you have heard the field is a fertile amalgamation of colliding approaches, armed with other sets of motivations, assumptions and philosophies:



Highlights of past results

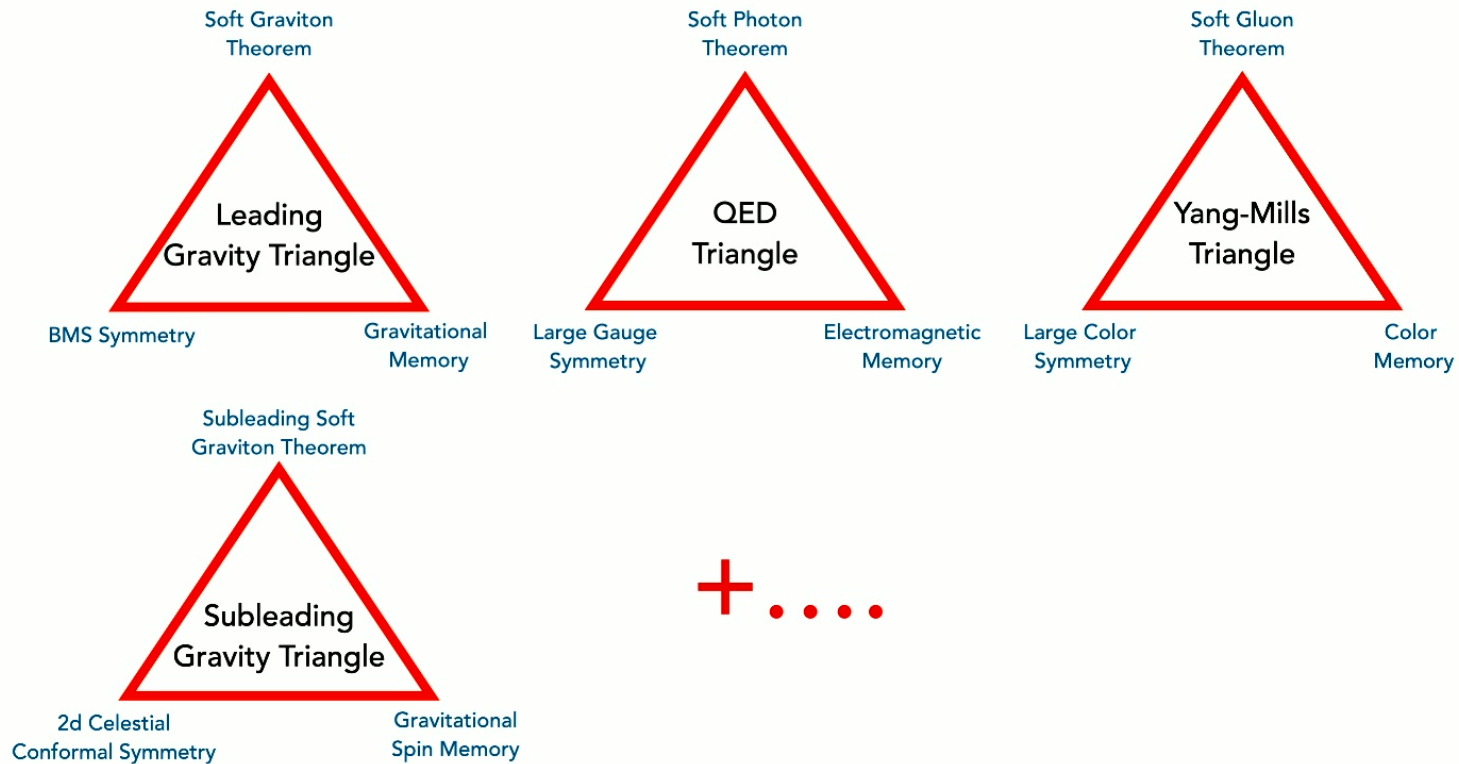
New insights on the Infrared

Progress on ? has been enabled by the recent discovery of an exact mathematical equivalence between three seemingly disparate half-century-old discoveries concerning the **deep infrared**:



More infrared relations

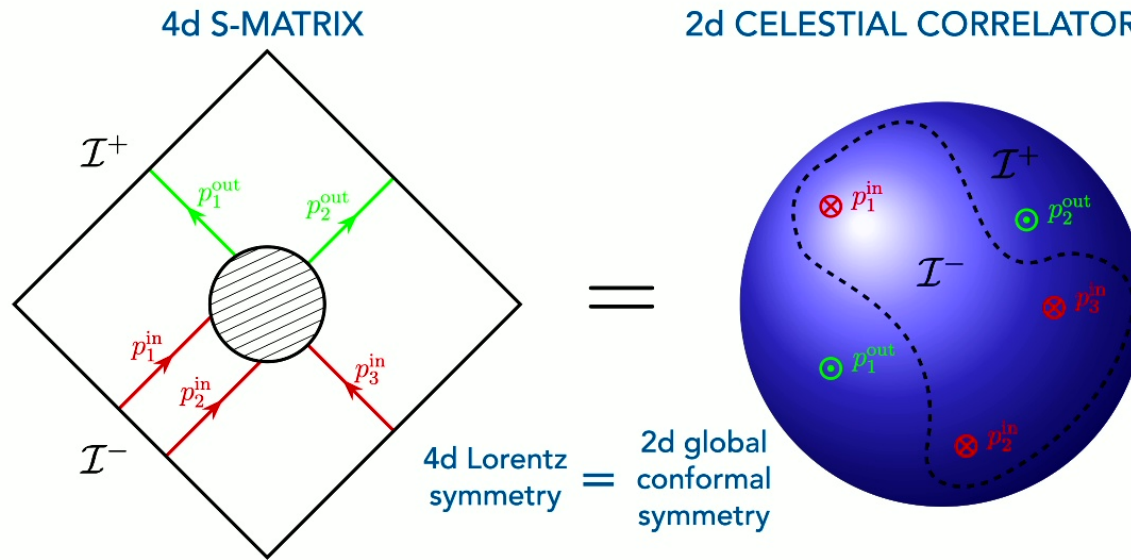
reverberate throughout gravity, QED and Yang-Mills Theory:



Akhoury, Ball, Banerjee, Cachazo, Campiglia, Casali, Cheung, Choi, He, Himwich, Kapec, Laddha, Lysov, Mittman, Mitra, Nande, Nichols, Pasterski, Pate, Porfyriadis, Raclariu, AS, Teukolsky, Venugopalan, Zhiboedov, ...

Celestial holography

This improved understanding of symmetries in flat space is just what the doctor ordered for applying the holographic principle to flat space: the first step in the construction of a dual pair is identifying the symmetries that both sides must obey. The subleading soft graviton theorem \rightarrow local 2d conformal symmetry of the celestial sphere (+spin memory). We may therefore rewrite:



So far the LHS largely defines the RHS. The goal is to give an intrinsic definition to the RHS.

4d QUANTUM GRAVITY = 2d CELESTIAL CFT

Conformal Primary Basis

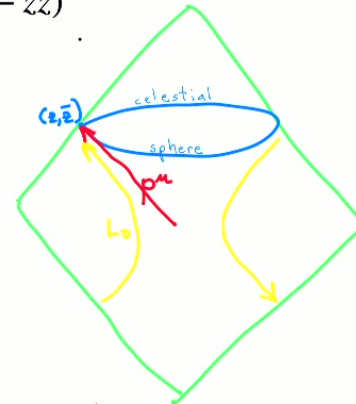
2D conformal covariance of 4D scattering amplitudes are manifest in a conformal basis of modes:

$$\Phi_{\Delta}(z, \bar{z}) = \int_0^{\infty} d\omega \omega^{\Delta-1} e^{i\omega(\hat{p} \cdot X + i\epsilon)} = \frac{\Gamma(\Delta)}{(i\hat{p} \cdot X - \epsilon)^{\Delta}}$$

conformal primary wavefunction
Mellin transform
plane wave
boost weight
point on celestial sphere
 $\hat{p}^{\mu}(z, \bar{z}) = (1 + z\bar{z}, z + \bar{z}, i(z - \bar{z}), 1 - z\bar{z})$

$$L_1 \Phi_{\Delta} = 0$$

$$L_0 \Phi_{\Delta} = \frac{\Delta}{2} \Phi_{\Delta}$$



$$A^{\text{celestial}}(\Delta_1, z_1, \bar{z}_1, \dots, \Delta_n, z_n, \bar{z}_n) = \int d\omega_1 \omega_1^{\Delta_1-1} \dots d\omega_n \omega_n^{\Delta_n-1} A^{\text{momentum}}(p_1, \dots, p_n)$$

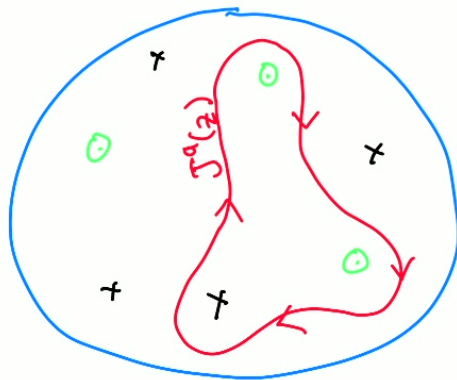
There have been extensive studies of these `celestial amplitudes' and their properties.

(Conformally) soft theorems imply 2D current algebras

The $\Delta = 1$ conformal primary in nonabelian gauge theory

$$J^a(z) = \int_{\mathcal{F}} du F_{uz}^a$$

is holomorphic on the celestial sphere. It generates a Kac-Moody algebra:



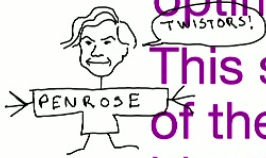
Ditto for gravity.

Sure looks like string theory!

$\mathcal{L}W_{1+\infty}^\wedge$ soft symmetries

Primary operators at $\Delta = 1, 0, -1, \dots$ are all governed by a tower of soft theorems. For minimally-coupled tree-level gravity they generate the well-known loop algebra of 2D area-preserving diffeomorphisms $\mathcal{L}W_{1+\infty}^\wedge$. The conformal basis organizes the tower of soft theorems in gauge theory and gravity into a **chiral soft algebra**. This result is relevant for flat space holography whether or not a celestial CFT is the optimal formulation.

Guevara, Himwich, Pate, AS, Donnay, Freidel, Herfray, Raclariu, Pranzetti



This same symmetry was used 50 years ago in Penrose's construction of the non-linear graviton and plays a central role in twistor theory. The identification is established by explicit comparison of the graviton wave functions. This forges a powerful connection and brings the analytic methods of twistor theory along with those of 2D CFT to bear on the problem of 4D gravity!

Adamo, Mason, Sharma, Casali, AS, Costello, Paquette, Skinner, Bu, Bittleston, Hueveline,...

These symmetries exist in the 'holomorphic expansion' around $z \rightarrow 0$, \bar{z} fixed. This is tantamount to analytic continuation to (2,2) signature Klein space, which has many interesting subtleties.

Exciting recent generalization of chiral soft algebra to AdS/dS, Hueveline poster, Skinner lecture(?)
Taylor, Zhu, Bittleston, Bogna, Hueveline, Knežević, Mason, Skinner

More!

- Top-down twisted holography (Gaiotto lectures(?))
- Carrollian holography (Ruzziconi lectures)
- Twistorial developments (Mason, Skinner lectures?)
- Gravitational memory experiments
- IR divergences (Honneseottir lectures)
- Asymptotic structure (Mitra lectures)

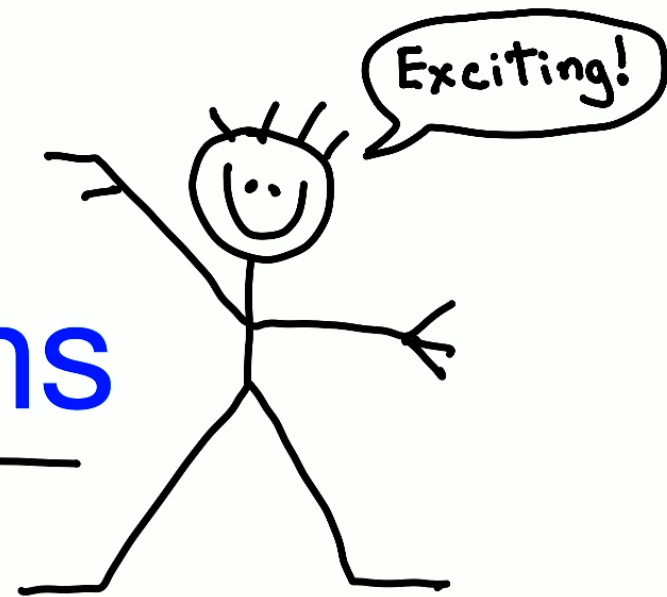
Present conundrums

some basic things we don't understand now under active investigation

- What is the physical spectrum of operator dimensions $\Delta? 1 + i\lambda?$
Integers?
- How do we understand/resolve the distributional nature of some low point celestial amplitudes implied by 4D translation invariance? (Puhm lecture)
- What kind of corrections can the chiral soft algebras have?

The Future

Open Questions



The general subjects of quantum gravity in flat space or dS along with the associated mathematics and experiments are wide open and developing in multiple directions. In advance of the annual meeting last April I collected 70+ very interesting questions (with hints in some cases) and posted them on the Simons Collaboration website. This is a good place to get ideas for research projects! I am now going to discuss a few of the collected questions.

14: Can one predict an observable which is a direct consequence of the subleading structure of soft theorems/memories/symmetries and design a protocol to observe it in the coming years?

HINT: The leading order displacement memory effect is on the way to be observed.

– **Geoffrey Compere**

54: What is the most promising method for detecting a memory effect?

HINT: Consider all fundamental forces: gravitational, electromagnetic, strong, and perhaps even weak.

– **David Nichols**

7: Find observable memory effects corresponding to $w_{1+\infty}$ symmetries of celestial holography.

8: Find memory observables corresponding to black hole horizon symmetries (of course one can think about displacement of test masses, but no experimenter would buy that!).

HINT: Contact author for hints and possible collaboration!

– **Ali Seraj**

Experiment

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- In principle observable memory effects exist for gravity, QED and QCD.
- They measure the transition between degenerate vacua induced by outgoing radiation, or equivalently edge modes at the boundary of spacetime. There is an infinite tower of such effects.
- The leading gravitational memory is predicted to be measured with 5 years of running at advanced LIGO.
- Newly predicted subleading ‘spin memory’ might be measured at LIGO or LISA, and QCD color memory at the electron-ion colliders.
- Finding the clean and practical methods for observing memory is a theoretically and experimentally interesting problem.

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Constraining the 4-graviton tree amplitude

- Few constraints in the Wilsonian paradigm.
- UV/IR connections give new perspectives.
- UV softness required by high energy black hole production 'baked in' to celestial amplitudes.
- 'Relevant physical principles' include soft symmetries.
- 2D crossing of 4D amplitude $\Rightarrow \sum_s poles = \sum_t poles$ as in string theory!

45: Is the tree-level Einstein S matrix the only consistent asymptotically flat n graviton S matrix (i.e. only poles and no cuts) that does not include pole exchange contributions from particles of arbitrarily high spin? Do the tree level n graviton Einstein, Type II and Heterotic S matrices constitute an exhaustive listing of such S matrices once we drop the constraint on the spins of exchange poles?

HINT:

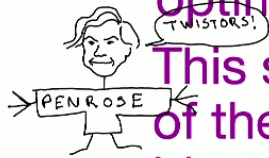
- "Consistent" means respecting all relevant general physical principles.
- A has been established for 4-graviton scattering assuming a constraint on growth of tree level S matrices with energy (CRG conjecture). Exercise: Prove CRG and extend to n-point scattering.
- Either a proof or counterexample would be interesting. Note that
 - a) Tree-level Type II/ Heterotic graviton S matrices on S^4 (times CY) are universal (independent of the CY).
 - b) May be useful to systematically study warped compactifications that have the dilaton as a modulus.

– Shiraz Minwalla

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