

Title: Electromagnetic precursors to compact mergers (and other EM-GR phenomena)

Speakers: Maxim Lyutikov

Series: Strong Gravity

Date: May 30, 2024 - 4:00 PM

URL: <https://pirsa.org/24050096>

Abstract: I will review various mechanisms and detection strategies of precursor emission to black holes and neutron stars mergers. I will also discuss other peculiar physical processes at the intersection of electromagnetism, classical General Relativity, and the physics of continuous media.

--

Zoom link

# Electromagnetic precursors to compact mergers (and other EM-GR phenomena)

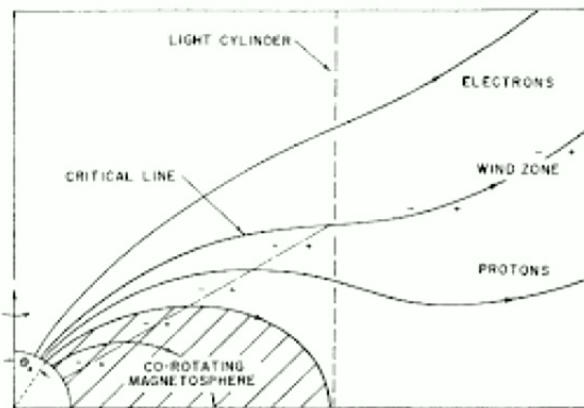
**Maxim Lyutikov (Purdue University)**

# Outline

- I. Relativistic unipolar inductor
  1. rotation and linear motion
  2. gaps/E-regions
- II. NS-NS mergers
  1. draping
  2. double -magnetized (gaps)
  3. flares
- III. BH-NS merger
  1. E-regions
- IV. NS to BH collapse
  1. prompt flash
  2. magnetic hair
- V. Observational strategies
- VI. Fun topics:
  - I. Cherenkov emission by Schwarzschild BH
  - II. Axion production by Schwarzschild BH

# The paradigm: relativistic Faraday's wheel/ unipolar inductor

- *Pulsar Electrodynamics*  
Goldreich & Julian, 1969



Rotating magnetized sphere generates EMF

- *Io, a jovian unipolar inductor*  
Goldreich & Lynden-Bell, 1969

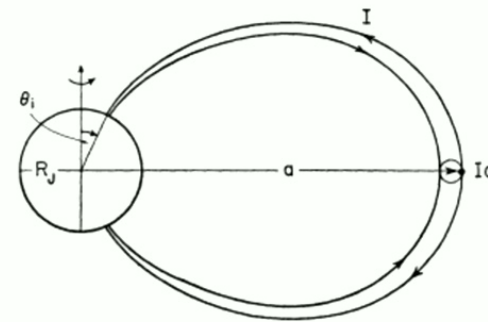


FIG. 2.—Current circuit in the meridian plane (not to scale)

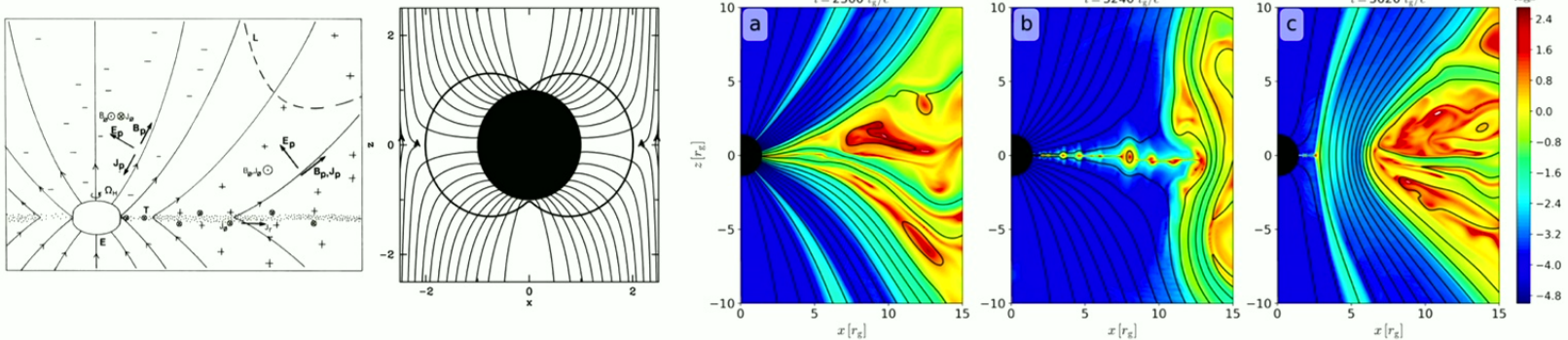
Linearly moving conductor generates EMF

- In both cases parallel E-field is generated
- pulsars:  $E_{\parallel}$  is quickly killed due to vacuum breakdown
- Plasma is accelerated: pulsar emission and Jovian aurora



# Extension to GR. 1 BZ-effect

- Rotation: Blandford-Znajek
  - new effects at GR + EM + plasma
  - Rotating space ``drags'' B-field similar to metal plate
  - details are still debated (should a field line cross horizon, or ergosphere is enough)



Chashkina + , 2021

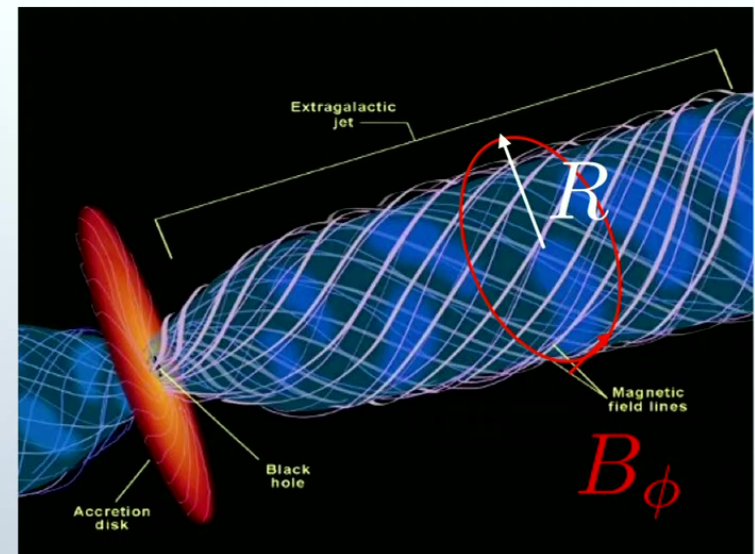
# Power of relativistic unipolar inductor

- Expected power:  $L_U \sim \frac{c}{4\pi}(\Delta\Phi)^2$
- **EM-dominated** relativistic sources, matter inertia not important
- $4\pi/c = 377$  Ohm
- Potential E-field times size:  $\Delta\Phi \sim E \times L, E \sim \beta B$ 
  - linear:  $\beta$ , size  $D$ , B-field:  $(\Delta\Phi) \sim \beta LB$
  - Rotating NS:  $\Delta\Phi \sim B_{NS} R_{NS}^3 (\Omega_{NS}/c)^2$  (Goldreich-Julian) (which is  $\Delta\Phi \sim B_{LC} \times R_{LC}$  and  $\beta \sim 1$ )
  - open magnetic flux

$$L_{EM} \sim (\Phi_B \Omega)^2 / c$$

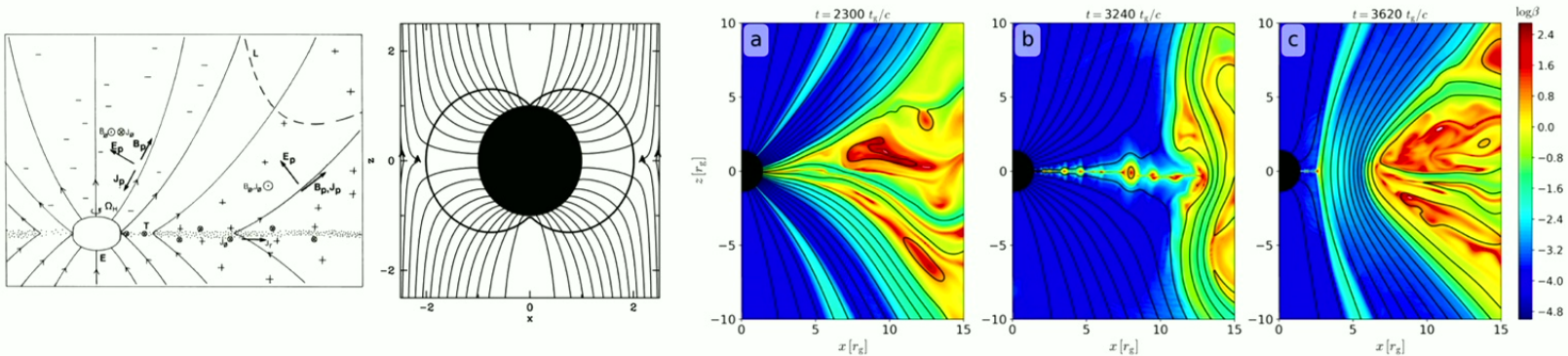
$$\Phi_B \sim BR^2$$

Eg, AGN jet  $L \sim B_\phi^2 R^2 c \sim \Phi_E^2 c$



# Extension to GR. 1 BZ-effect

- Rotation: Blandford-Znajek
  - new effects at GR + EM + plasma
  - Rotating space ``drags'' B-field similar to metal plate
  - details are still debated (should a field line cross horizon, or ergosphere is enough)



Chashkina + , 2021

Later: extension to GR. 2 - linearly moving BH

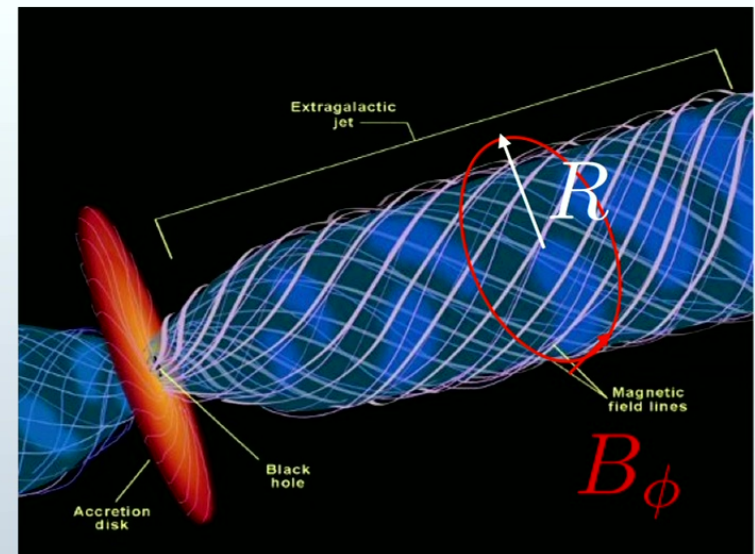
# Power of relativistic unipolar inductor

- Expected power:  $L_U \sim \frac{c}{4\pi} (\Delta\Phi)^2$
- **EM-dominated** relativistic sources, matter inertia not important
- $4\pi/c = 377$  Ohm
- Potential E-field times size:  $\Delta\Phi \sim E \times L, E \sim \beta B$ 
  - linear:  $\beta$ , size  $D$ , B-field:  $(\Delta\Phi) \sim \beta LB$
  - Rotating NS:  $\Delta\Phi \sim B_{NS} R_{NS}^3 (\Omega_{NS}/c)^2$  (Goldreich-Julian) (which is  $\Delta\Phi \sim B_{LC} \times R_{LC}$  and  $\beta \sim 1$ )
  - open magnetic flux

$$L_{EM} \sim (\Phi_B \Omega)^2 / c$$

$$\Phi_B \sim BR^2$$

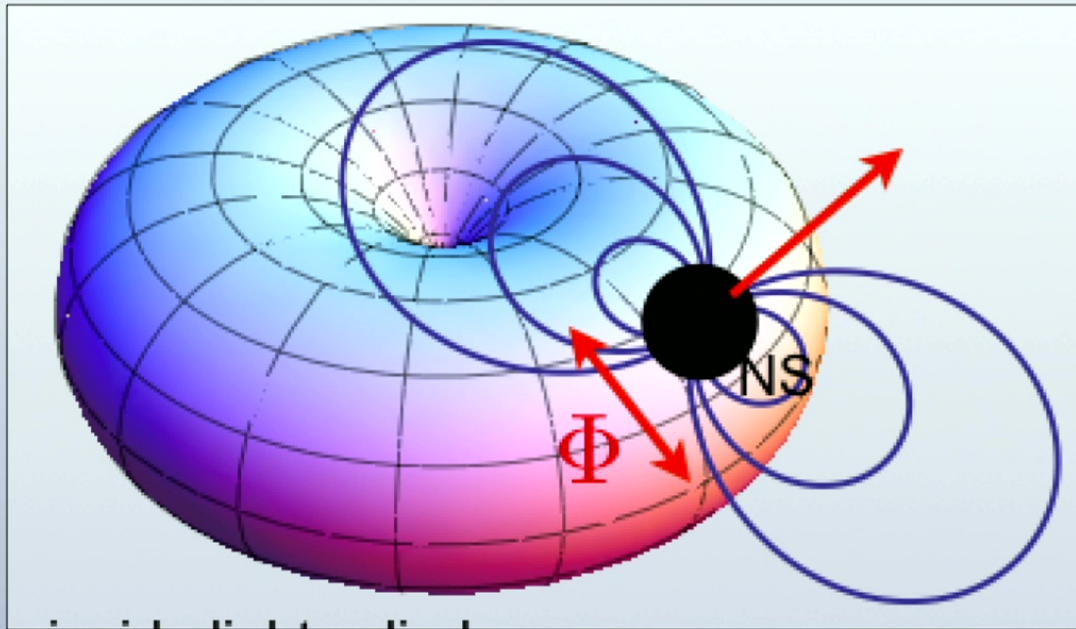
Eg, AGN jet  $L \sim B_\phi^2 R^2 c \sim \Phi_E^2 c$





## II NS-NS mergers

Question 1: before merger a NS moves through companion's B-field: what we expect?

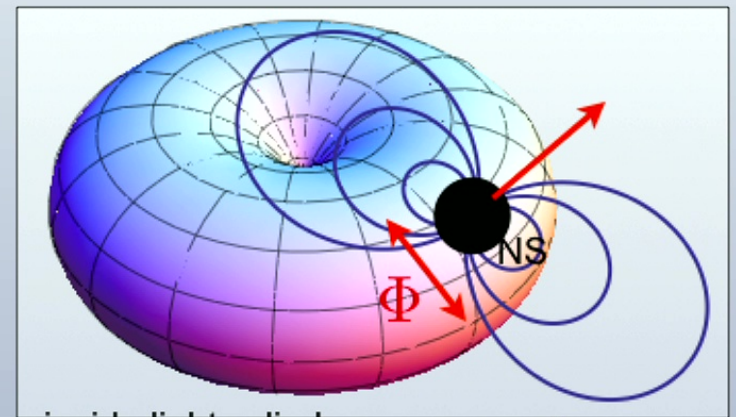
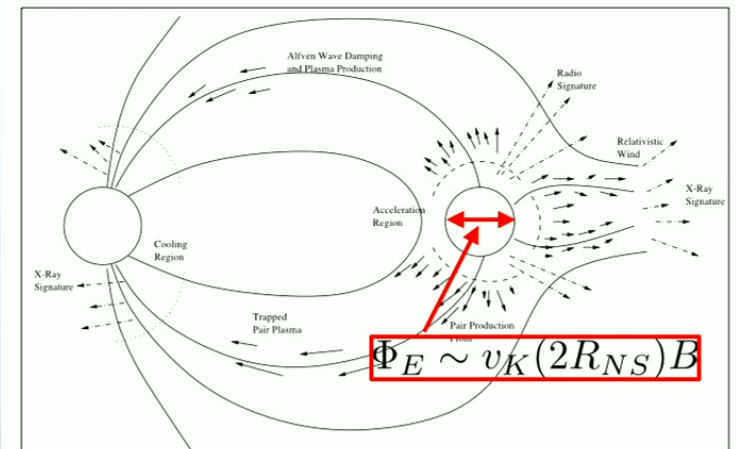


# Precursor emission to LIGO NS-NS events

- Hansen & Lyutikov 2001: NS in the B-field of companion

$$L \sim \frac{GM}{c} B_{NS}^2 \frac{R_{NS}^8}{a^7} \approx 10^{46} B_{12}^2 a_6^{-7} \text{ erg s}^{-1}$$

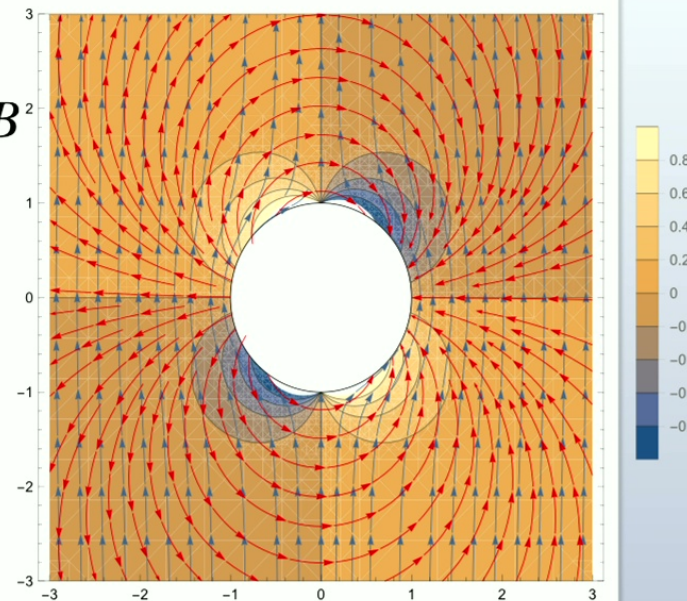
- Not very bright... Unless coherent! - **Radio**
- $F_\nu \sim 10^3 \text{ Jy}$  from 1 Gpc
- That was the best model for the Lorimer Burst, not anymore, FRBs are not mergers.
- Short GRBs from NS-NS merger need B-field amplification to  $\sim 10^{14} \text{ G}$



# NS moving through B-field: Creation of dissipative regions

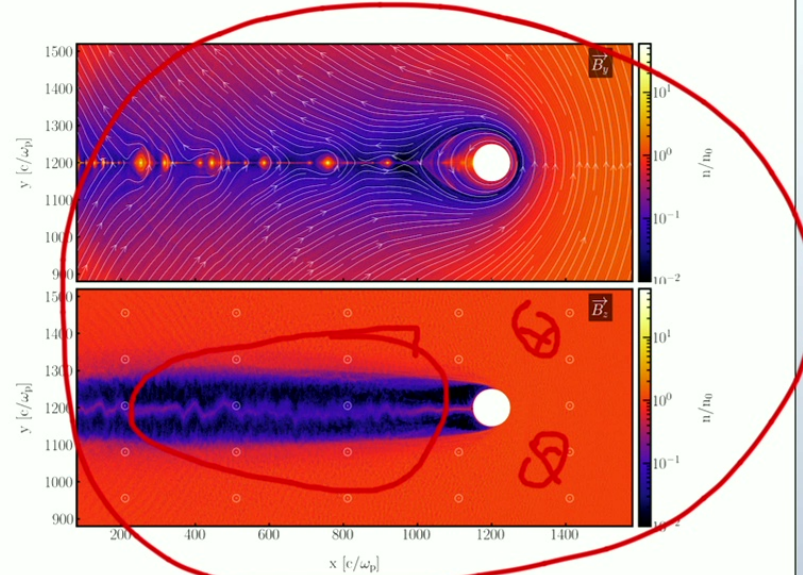
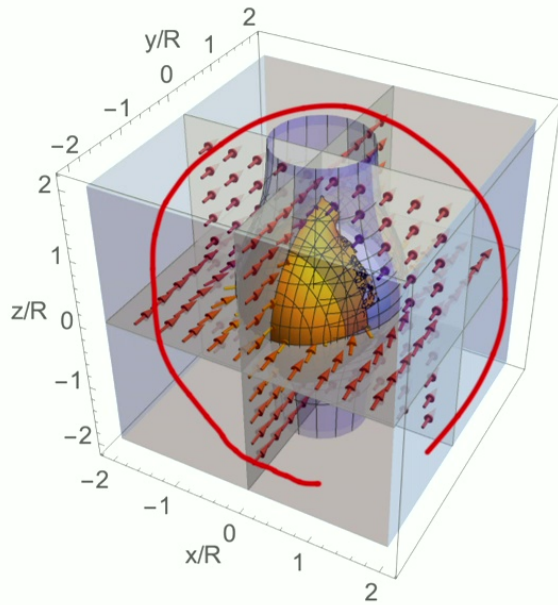
Lyutikov 2018

- Try vacuum, if  $\mathbf{E} \cdot \mathbf{B} \neq 0$  -> most likely a problem
- Electrodynamics ~ pulsars
  - Motional E-field
  - regions with  $\mathbf{E} \cdot \mathbf{B} \neq 0$  and  $E > B$
  - orbital modulation



# Even with plasma: Draping of merging NS

- EM interaction of merging neutron stars is necessarily dissipative due to formation of draping layer,  $E_{\parallel}$  and/or  $E > B$

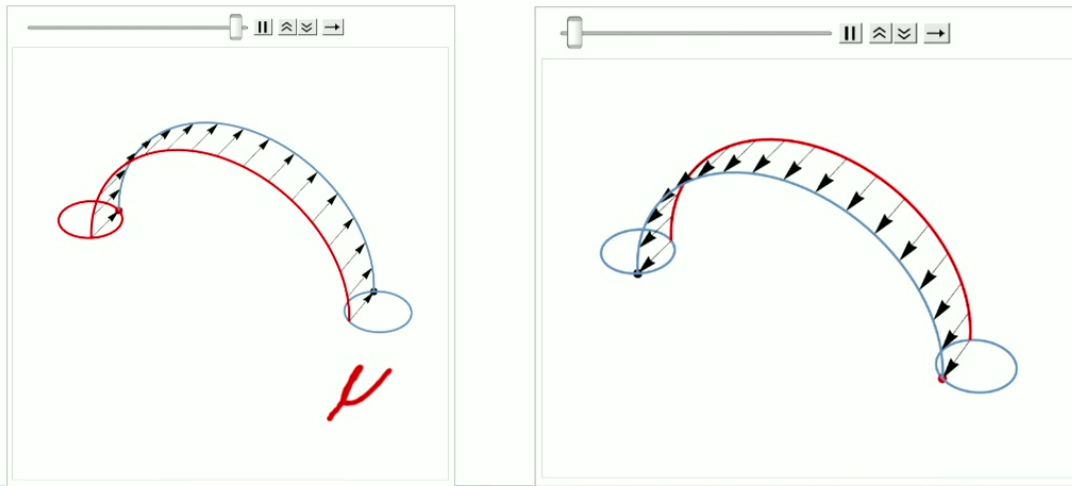


Sironi+, in prep.

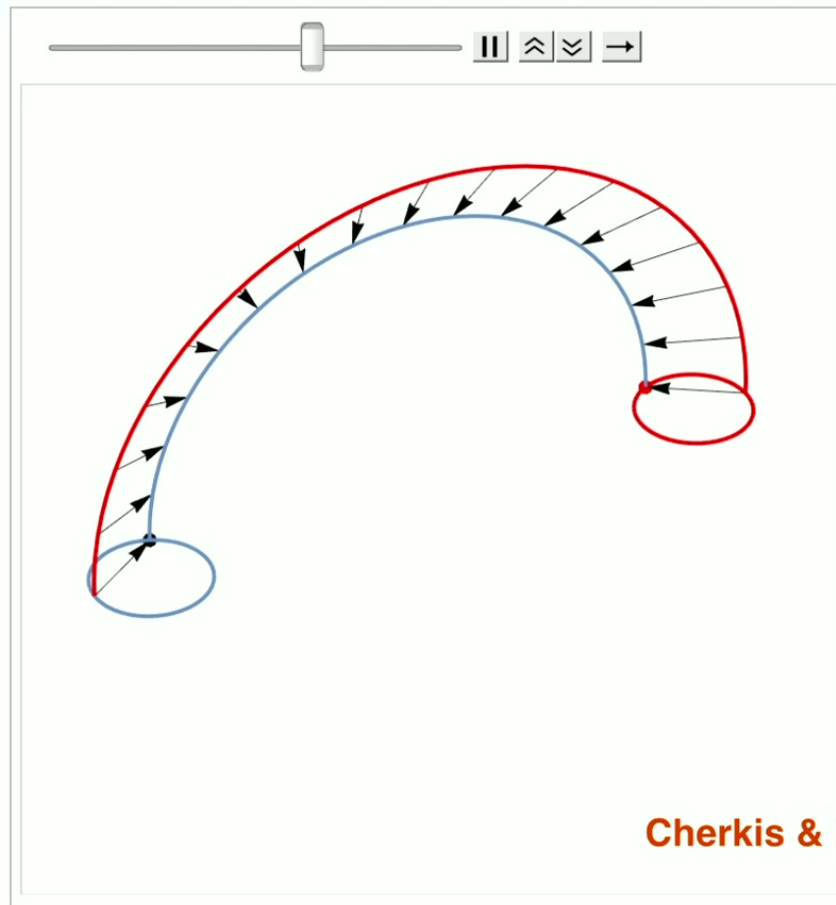


# Flares!

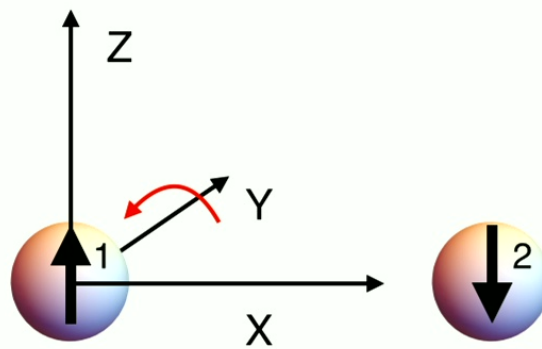
- Store energy **slowly** in connected magnetospheres – release explosively
- **Combination of spins and orbital motion can “unwind”**
- Special configurations of interacting NSs
  - Fully locked
  - $\omega_1 = -\omega_2$



Basic-Z:  $\omega_1 + \omega_2 = 2\Omega$



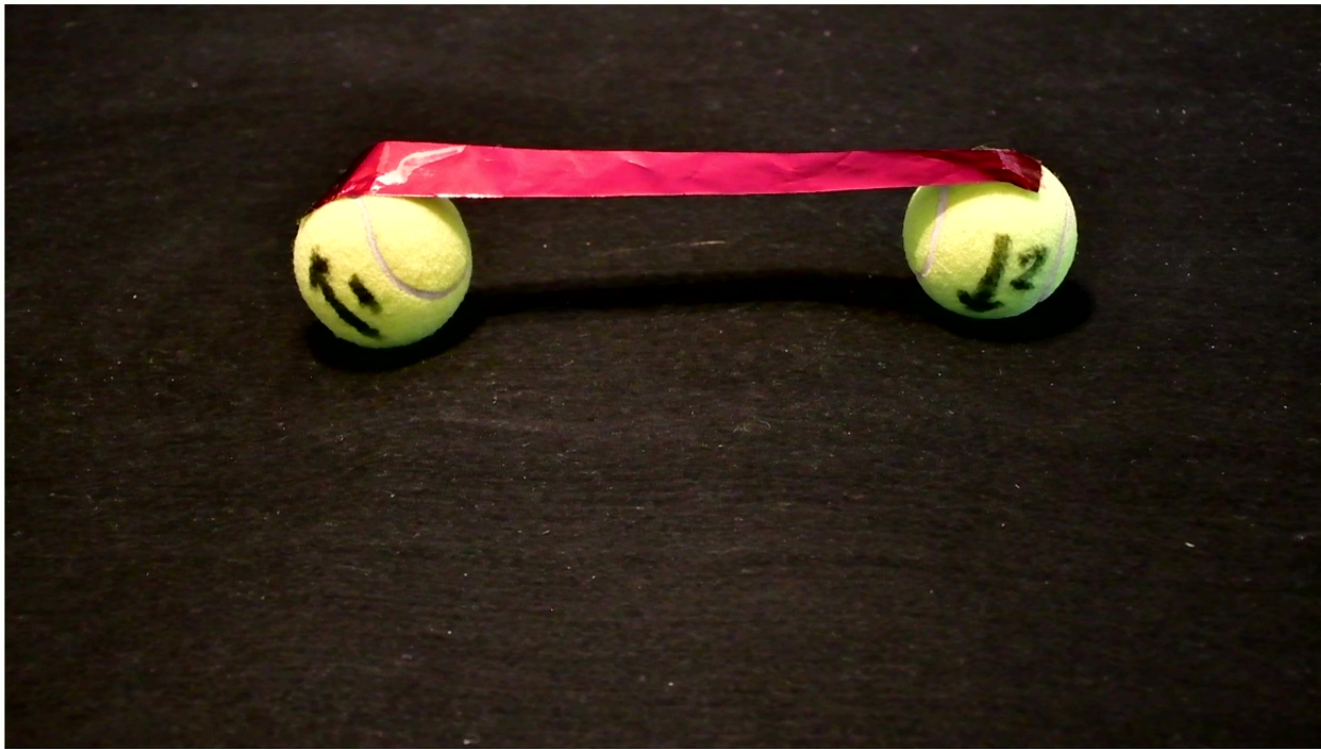
# Y-spin



**Cherkis & Lyutikov ApJ, 2021**

14

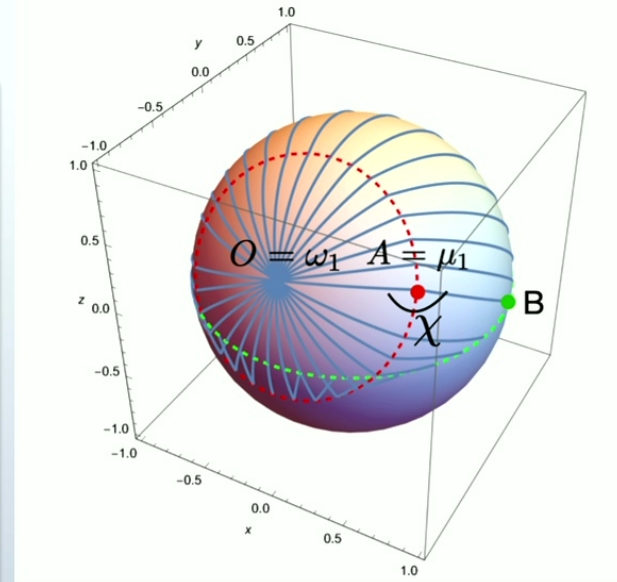
# Y-spin



15

# Topology of magnetically coupled stars

- Direction of B-field from #1 to #2: a path on 2-sphere
- Curl B is not important: each hair in a braid can be twisted: we are for **braiding**
- Need to track 3 points on the 2-sphere of B-direction to define braiding.




O - omega of 1  
A - mu of 1  
B: radius 1-2

- 8
- 9
- 10
- 11
- 12
- 13
- 14**
- 15
- 16
- 17
- 18
- 19
- 20

# Y-spin

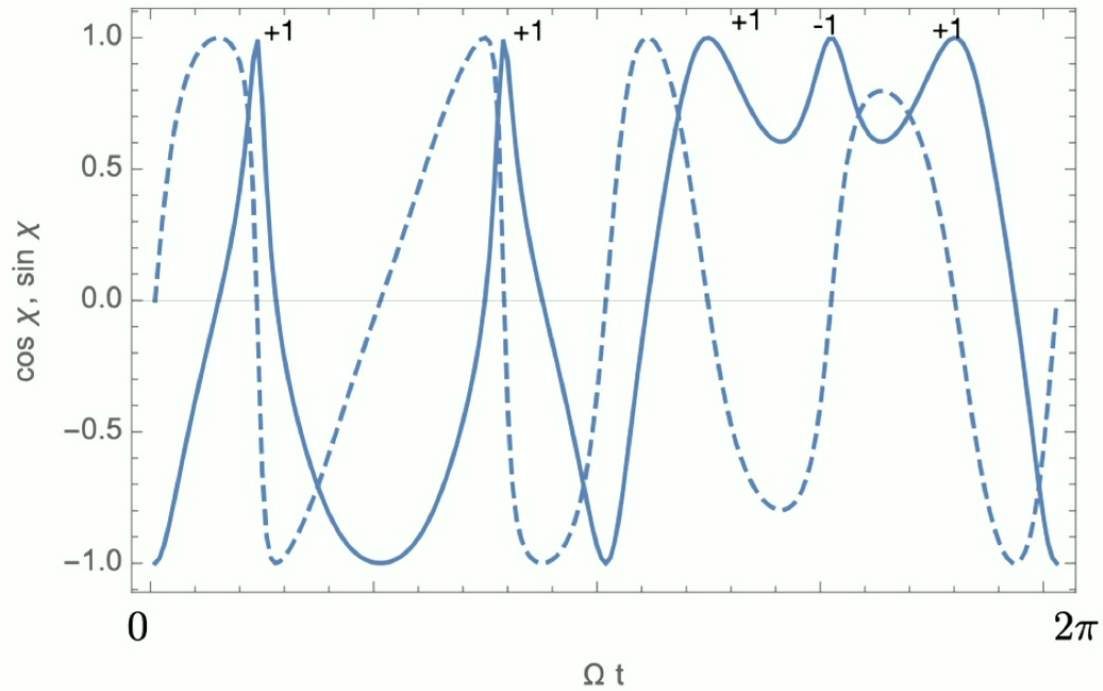
• Double-tap to edit



Cherkis & Lyutikov ApJ, 2021

14

# Counting twists



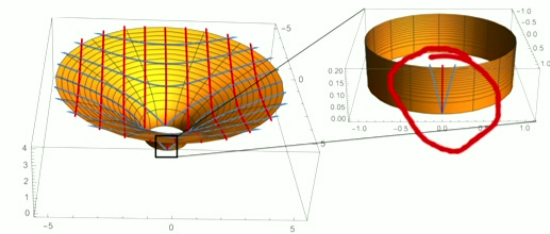
### III. BH-NS merger (and supermassive BH-BH)



# Extension to GR. 2: Linear unipolar inductor: Schwarzschild BH moving across B-field generates EM wind

Lyutikov 2011  
Palenzuela +2010

- Linear motion: A Schwarzschild BH moving across B-field generates  $E \cdot B \neq 0$  and EM wind

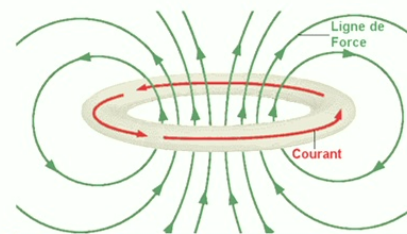
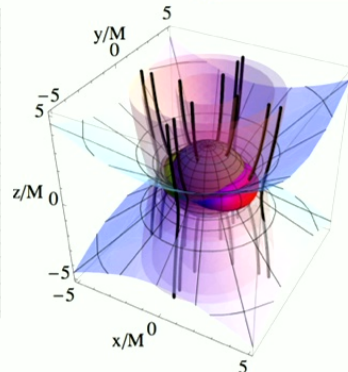
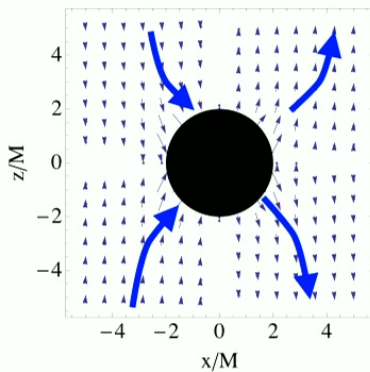
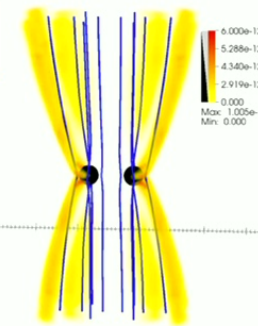


$$\mathbf{E} \cdot \mathbf{B} = -\cos \phi \sin 2\theta \beta_0 B_0^2 \frac{M}{r}$$

$$\rho_0 = \frac{B_0(v_0/R_G)}{2\pi c}$$

$$L_{EM} \approx M^2 \beta_0^2 B_0^2$$

$$L_{EM,u} = \frac{(GM)^3 B_0^2}{c^5 R}$$

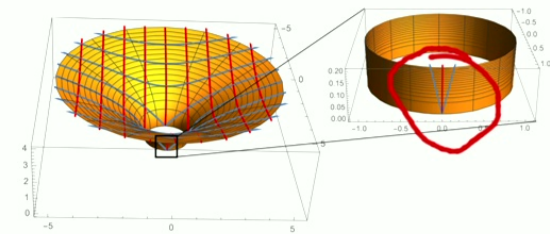


- BH-BH merger ( $B_0$  from disk)

# Extension to GR. 2: Linear unipolar inductor: Schwarzschild BH moving across B-field generates EM wind

Lyutikov 2011  
Palenzuela +2010

- Linear motion: A Schwarzschild BH moving across B-field generates E.B I=0 and EM wind

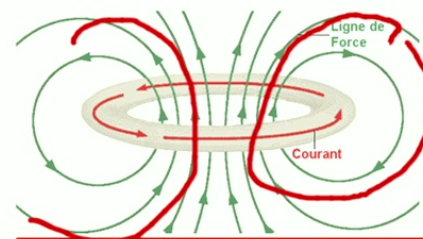
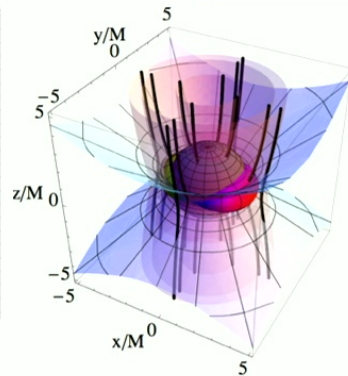
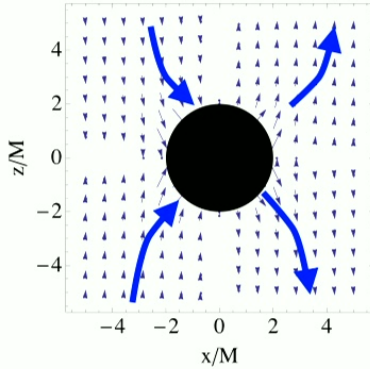
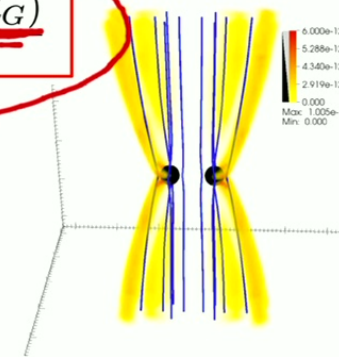


$$\mathbf{E} \cdot \mathbf{B} = -\cos \phi \sin 2\theta \beta_0 B_0^2 \frac{M}{r}$$

$$\rho_0 = \frac{B_0(v_0/R_G)}{2\pi c}$$

$$L_{EM} \approx M^2 \beta_0^2 B_0^2$$

$$L_{EM,u} = \frac{(GM)^3 B_0^2}{c^5 R}$$



- BH-BH merger ( $B_0$  from disk)

# Early stage of NS collapse: pulsar-like EM signal during prompt collapse - not much

- Power increases but collapse time is very short

$$L_{NS} \sim B_{NS}^2 R_{NS}^2 c \left( \frac{R_{NS} \Omega}{c} \right)^4$$

$$L \sim L_{NS} \left( \frac{R}{R_{NS}} \right)^{-4}$$

$$t_{col} \sim \sqrt{R_{NS}^3 / (GM_{NS})} \sim 0.1 \text{ msec} \quad (\text{rotational support will prolong})$$

- After NS collapse, the BH rotates with smaller frequency!

$$\Omega_H \approx \frac{\chi}{5} \frac{c^4 R_{NS}^2}{(GM_{NS})^2} \Omega_{NS} = 2.9 \times 10^3 \text{ rads}^{-1} \chi_{-1} P_{NS,-3}^{-1}$$

- $\alpha = 0.04$  for a ms - NS slows down!

# Magnetic hair of BHs

Lyutikov 2011  
Lyutikov+2012  
Bransgrove+ 2021

- Loop-hole in “NO-HAIR” theorem: frozen-in B-fields
- Hair are conserved (in ideal plasma)

$$N_B = e\Phi_\infty / (\pi c \hbar) = B_{NS} e R_{NS}^3 \Omega_{NS} / (c^2 \hbar) = 10^{41} \frac{B_{NS}}{10^{12} \text{G}} \frac{P_{NS}}{1 \text{msec}}$$

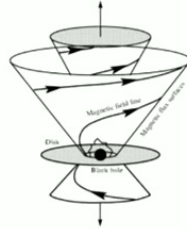
- No prompt EM pulse due to “released” B-field

- Analytics: time-dependent B-field in Schwarzschild geom.

$$B_\phi = -\frac{R_s^2 \Omega \sin \theta}{\alpha r} B_s, \quad B_r = \left(\frac{R_s}{r}\right)^2 B_s,$$

$$E_\theta = B_\phi, \quad j_r = -2 \left(\frac{R_s}{r}\right)^2 \frac{\cos \theta \Omega B_s}{\alpha}$$

$$\Omega \equiv \Omega (r - t + r(1 - \alpha^2) \ln(r\alpha^2)) \quad \alpha = \sqrt{1 - 2M/r}$$

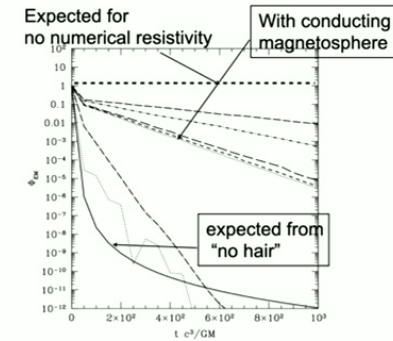
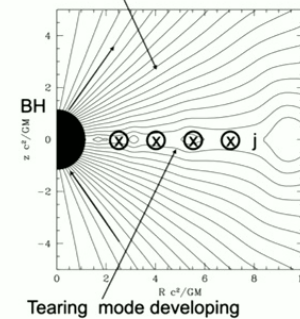


- Nonlinear, time-dependent solution in GR (small  $\alpha$ )

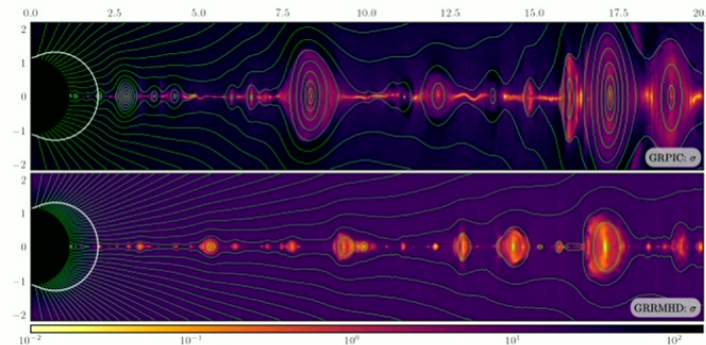
- arbitrary  $\Omega(t, \theta)$  in Schwarzschild metric
  - Alfvén mode propagating along (!) B-field
- BH slows down during collapse (! - anti-skater)
- Released spin-down power is small  $\sim L_{sd} R_{NS} / c$

- Magnetic hair (Slowly balding black holes, Lyutikov and McKinney 2011)

- Fields are NOT anchored in heavy crust



Tearing mode developing





# Magnetic hair of BHs

Lyutikov 2011  
~~Lyutikov+2012~~  
 Bransgrove+ 2021

- Loop-hole in “NO-HAIR” theorem: frozen-in B-fields
- Hair are conserved (in ideal plasma)

$$N_B = e\Phi_\infty / (\pi c \hbar) = B_{NS} e R_{NS}^3 \Omega_{NS} / (c^2 \hbar) \approx 10^{41} \frac{B_{NS}}{10^{12} \text{G}} \frac{P_{NS}}{1 \text{msec}}$$

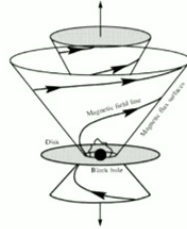
- No prompt EM pulse due to “released” B-field

- Analytics: time-dependent B-field in Schwarzschild geom.

$$B_\phi = -\frac{R_s^2 \Omega \sin \theta}{\alpha r} B_s, \quad B_r = \left(\frac{R_s}{r}\right)^2 B_s,$$

$$E_\theta = B_\phi, \quad j_r = -2 \left(\frac{R_s}{r}\right)^2 \frac{\cos \theta \Omega B_s}{\alpha}$$

$$\Omega \equiv \Omega (r - t + r(1 - \alpha^2) \ln(r\alpha^2)) \quad \alpha = \sqrt{1 - 2M/r}$$

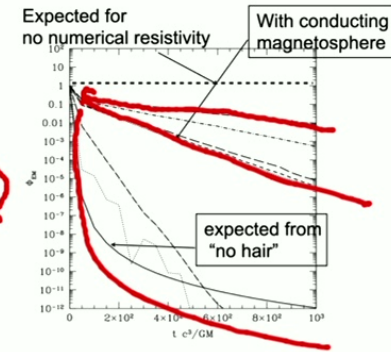
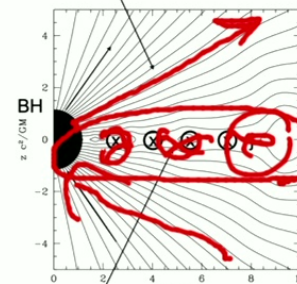


- Nonlinear, time-dependent solution in GR (small  $\alpha$ )

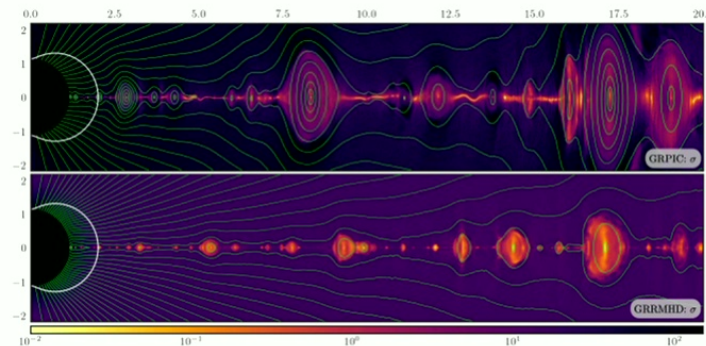
- arbitrary  $\Omega(t, \theta)$  in Schwarzschild metric
  - Alfvén mode propagating along (!) B-field
- BH slows down during collapse (! - anti-skater)
- Released spin-down power is small  $\sim L_{sd} R_{NS} / c$

- Magnetic hair (Slowly balding black holes, Lyutikov and McKinney 2011)

- Fields are NOT anchored in heavy crust



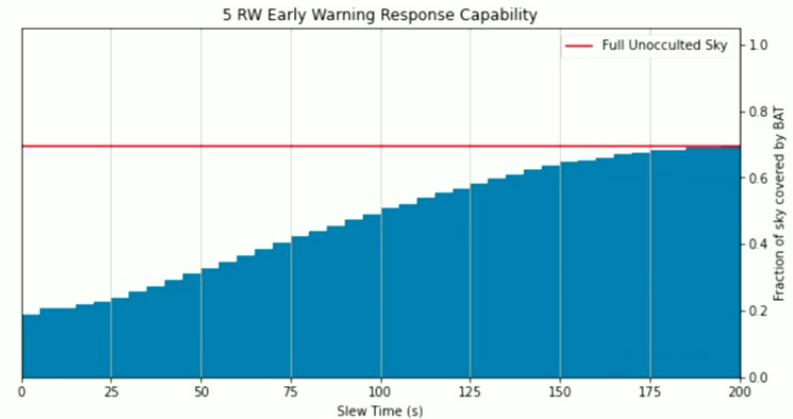
Tearing mode developing



## Best chance to detect LIGO precursors: low frequency radio

- Expected EM power of precursor emission is mild,  $\leq 10^{43}(-t/msec)^{-7/4}$  erg/s
- flares: pre-merger flashes at spin+ and orbital beats:  $n(\omega_1 + \omega_2) = m\Omega$ ,  $10^{45}$  erg/s
- beaming in high energy needed
- LIGO early warning: up to a minute,
- ~10 sec before merger, 100 deg<sup>2</sup>
- **Optical**
  - flashes of  $m \sim 15$
  - LSST image will be only in one plate
  - Readout While Exposing mode

- **Radio:**
  - Jansky-level flashes  $F_{\nu,peak} = 0.5 Jy \eta_{R,-3} \nu_9^{-1} d_{200}^{-2}$
  - delayed by  $\sim \Delta t = 14 \text{ sec } \nu_9^{-2} d_{200}$
  - LOFAR & MWA: "see" whole sky, but need to



SWIFTGUANO: Fraction of sky BAT can cover as a function of latency

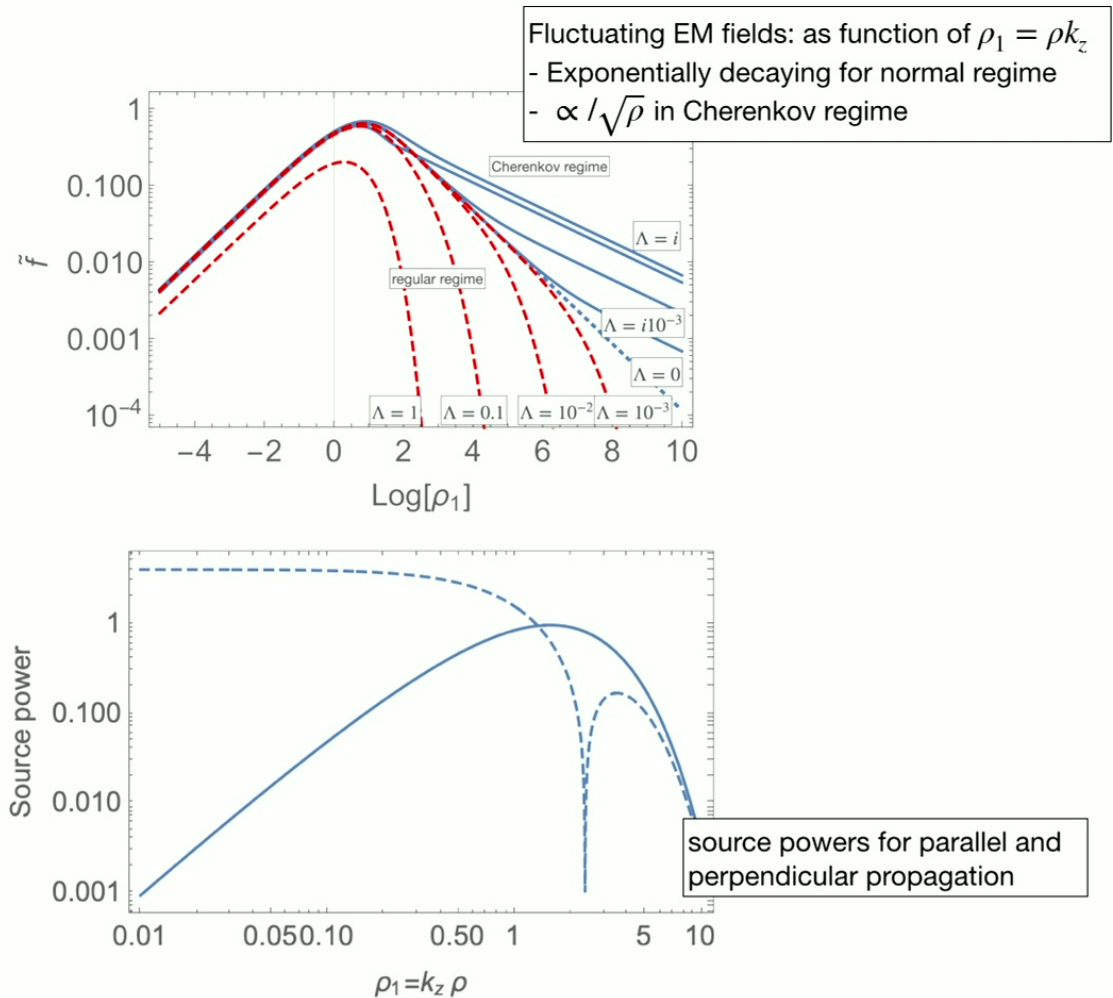
# VI Fun topics

# Cherenkov emission by Schwarzschild BH

## Cherenkov emission by Schwarzschild BH

- $L_{Ch} \propto (\epsilon - 1) \times B_0 \times (GM) \times \beta$
- No source!
- Distributed effective source
- BH induces superluminal EM perturbations
- Distributed effective source  $\rho \sim 1/k_z$
- Spectrum  $L_{CH} \propto \frac{dk_z}{k_z}$
- Even BH moving along the B-field emits (except

EM emission by purely charge-neutral “particle”.

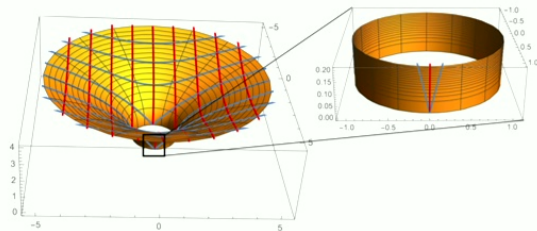




# Axion production by Schwarzschild BH

- BH in crossed E & B  $\rightarrow \mathbf{E} \cdot \mathbf{B} \neq 0$

Lyutikov 2108.06364



Oscillating  $\mathbf{E} \cdot \mathbf{B} \rightarrow$  The triangle anomaly

- Axion-photon coupling  $\mathcal{L}_{a\gamma} = g_{a\gamma} a \mathbf{E} \cdot \mathbf{B}$

- Coupling is non-local

$$\mathbf{E} \cdot \mathbf{B} = - \frac{M \sin(2\theta) \cos(\phi)}{r} B_0 E_0$$

- time-dependent

- plasma may not have time to screen

- topological current

$$J_\nu = A^\mu (*F_{\mu\nu})$$

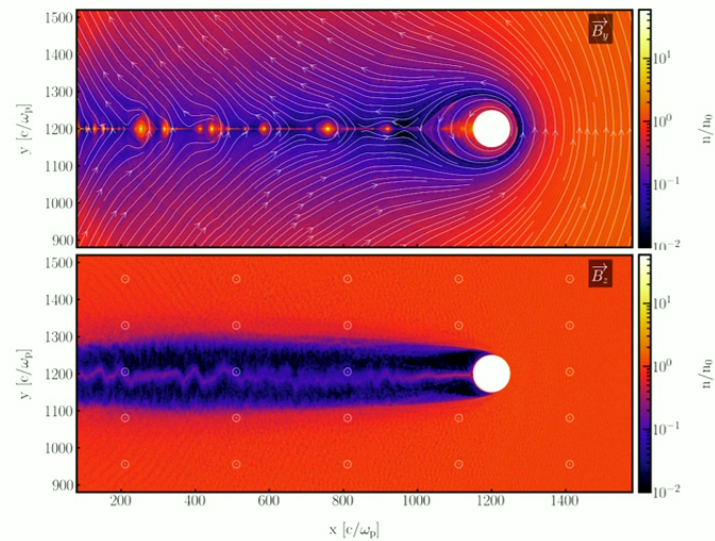
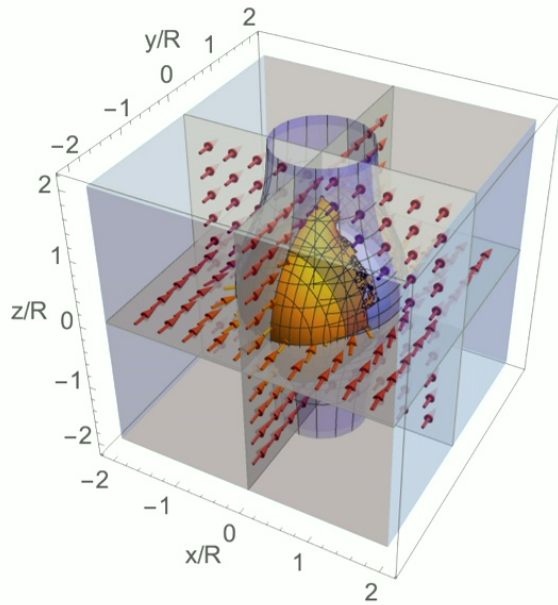
$$J_0 = \mathbf{A} \cdot \mathbf{B} = 0$$

$$J_i = \mathbf{E} \times \mathbf{A} + \frac{A_0}{\alpha} \mathbf{B}$$

$$J_{\mu;\mu} = -\frac{7}{4} \sin 2\theta \cos \phi B_0 E_0 \frac{M}{r} = \frac{7}{4} \mathbf{E} \cdot \mathbf{B}$$

# Even with plasma: Draping of merging NS

- EM interaction of merging neutron stars is necessarily dissipative due to formation of draping layer,  $E_{\parallel}$  and/or  $E > B$

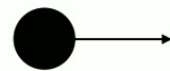
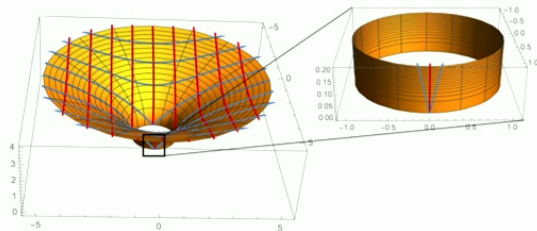


Sironi+, in prep.

# Axion production by Schwarzschild BH

- BH in crossed E & B  $\rightarrow \mathbf{E} \cdot \mathbf{B} \neq 0$

Lyutikov 2108.06364



Alfven wave



Oscillating  $\mathbf{E} \cdot \mathbf{B}$   $\rightarrow$  The triangle anomaly

