

Title: Gong Show

Speakers:

Collection: Foundations of Quantum Computational Advantage

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Abstract: IN PERSON - Lorenzo Catani, Matthew Fox, Hlér Kristjánsson, Gabrielle Tournaire

VIRTUAL - Jonte Hance, Sidiney Montanhano, Shiroman Prakash, Amr Sabry

**Gong Show Presentations  
Tuesday, April 30th, 2024**



Workshop

**In person:**

Lorenzo Catani  
Matthew Fox  
Hlér Kristjánsson  
Gabrielle Tournaire

**Virtual:**

Jonte Hance  
Sidiney Montanhano  
Shiroman Prakash  
Amr Sabry





# Alternative robust ways of witnessing nonclassicality in the simplest scenario

FoQaCia conference, Waterloo - 30/04/2024

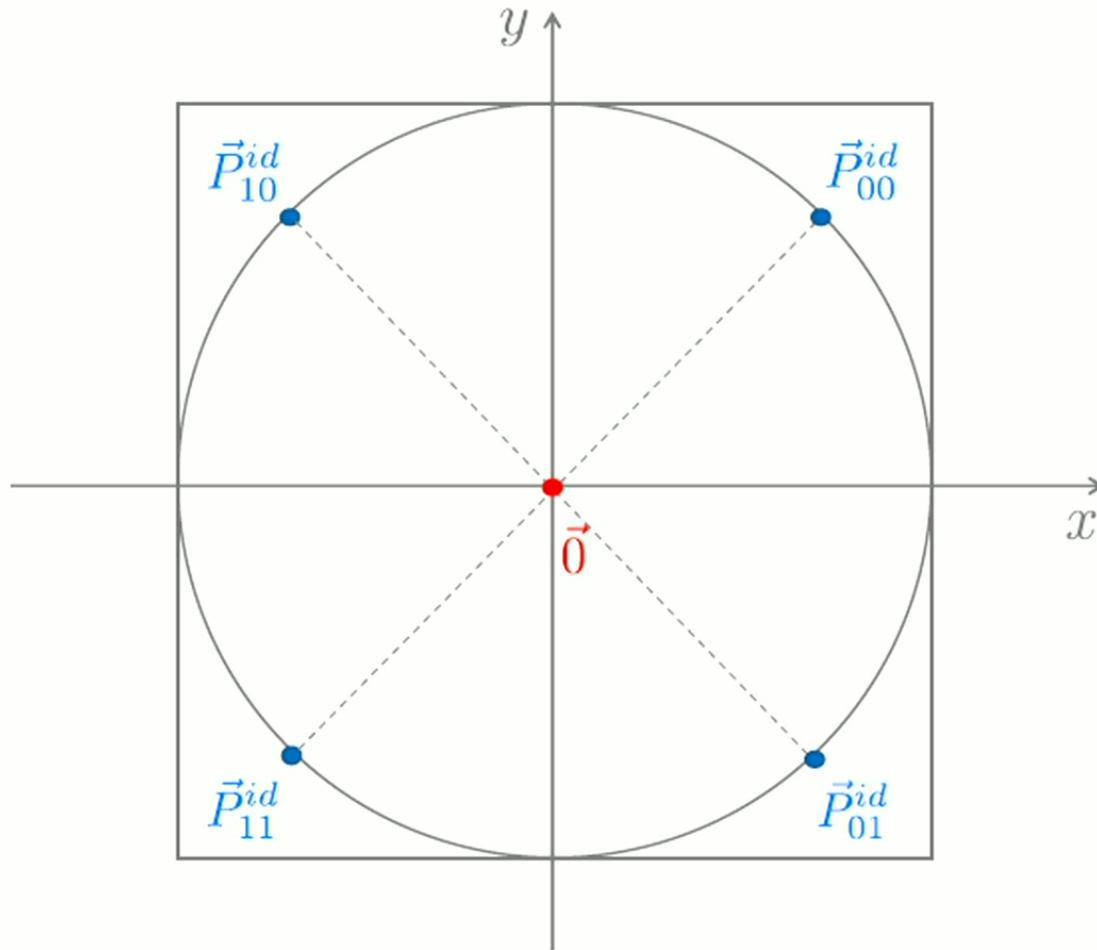
Lorenzo Catani

Joint work with Massy Khoshbin and Matt Leifer

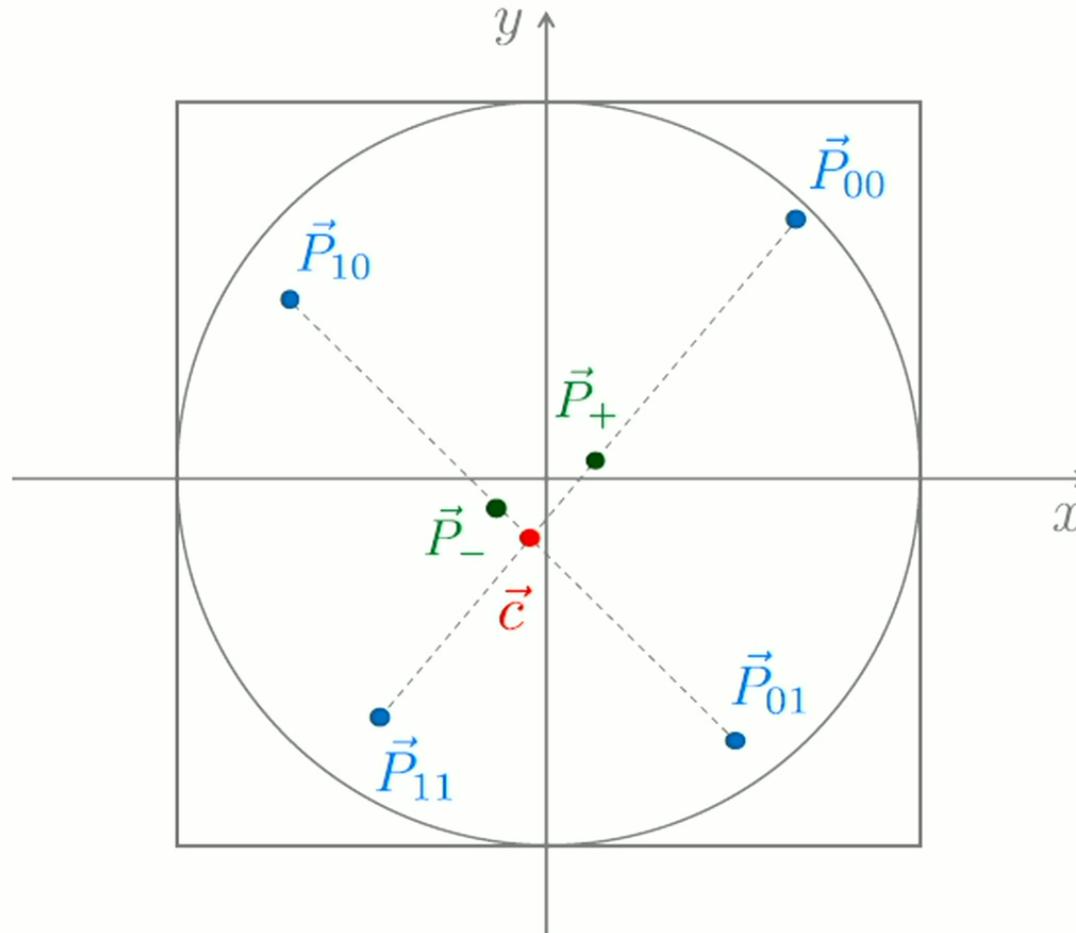
[PRA 109, 032212 \(2024\)](#)



## Simplest Scenario – Ideal Case



## Simplest Scenario – Realistic Case



## Summary of Results

Approach	Notion of nonclassicality	Reference to <i>a priori</i> ideal preparations	Noise threshold of violation
Pusey's	Preparation contextuality	No	$\delta \leq 0.06$
Marvian's	Preparation contextuality	No	$\delta \leq 0.1$
Our work	Violation of BOD	Yes	$\delta \leq 0.007$

M. F. Pusey, Phys. Rev. A 98, 022112 (2018).

I. Marvian, arXiv:2003.05984v1 (2020).

A. Chaturvedi and D. Saha, Quantum 4, 345(2020).

Is Entanglement Necessary for

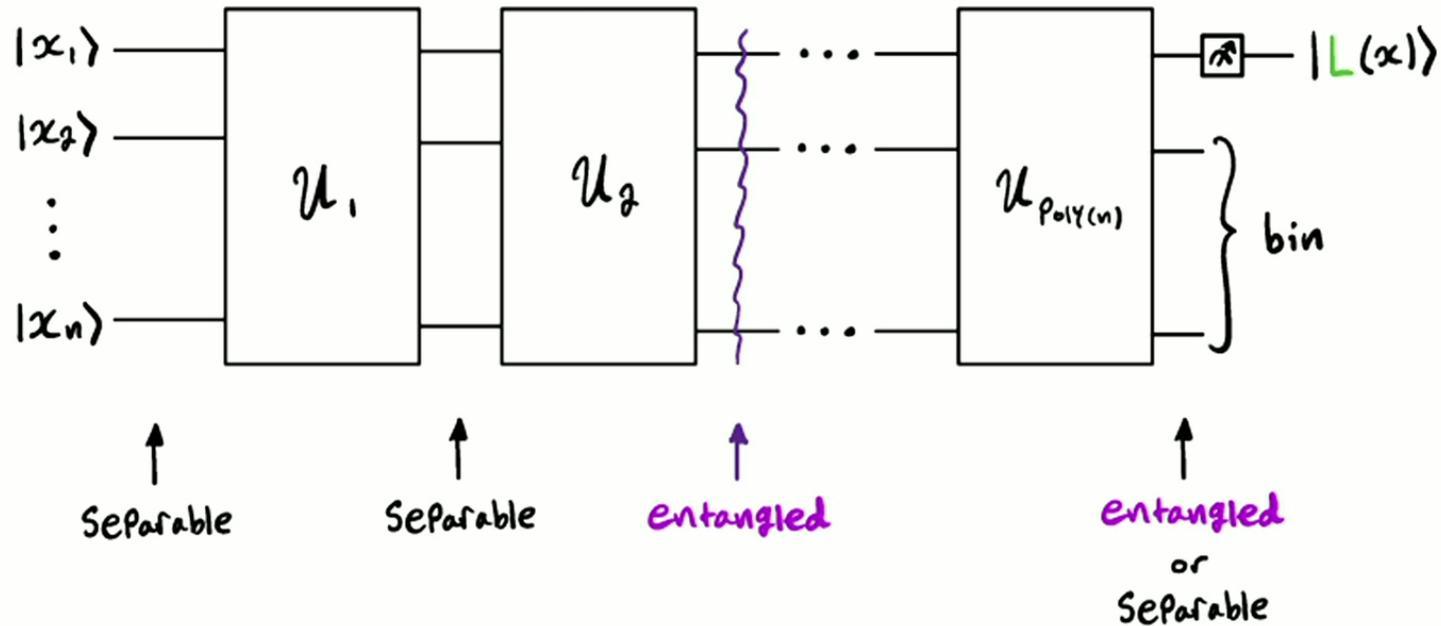
$BPP \neq BQP?$



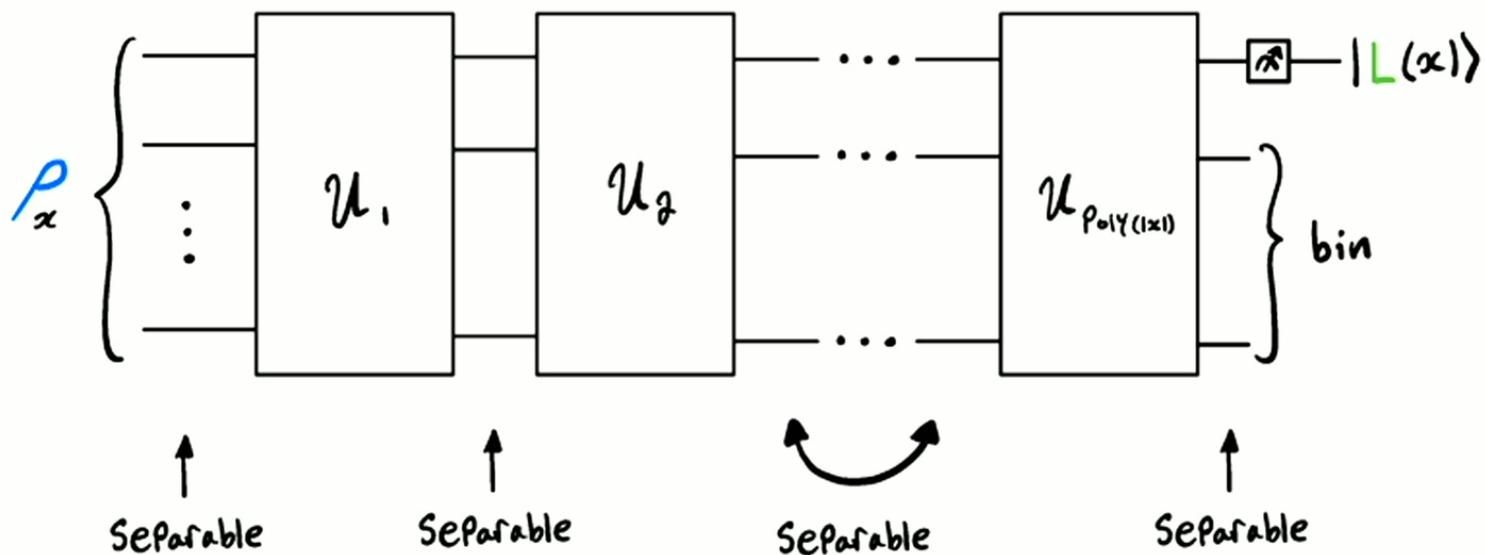
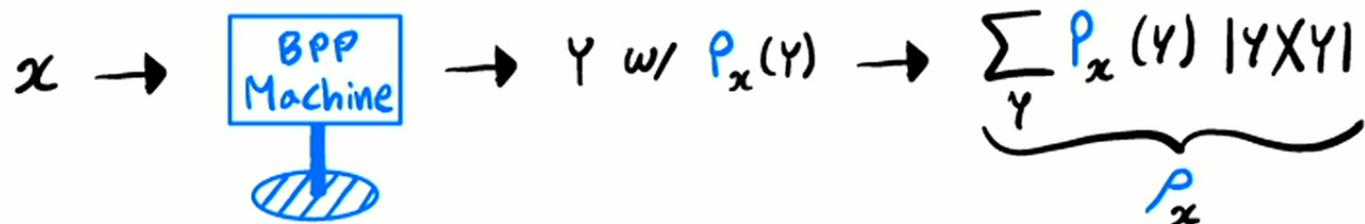
Matthew Fox

University of Colorado Boulder

Q: Does every (uniform, poly-size) circuit for  $L \in BQP \setminus BPP$  necessarily entangle its input?



Q: Decide  $L \in \text{BQP} \setminus \text{BPP}$  like this?



Def:  $L \in \text{BQP}_{\text{sep}}$  iff  $L \in \text{BQP}$  and "entanglement is not necessary to decide  $L$ ".

### Basic Properties:

- $\text{BPP} \subseteq \text{BQP}_{\text{sep}} \subseteq \text{BQP}$
- $\text{BPP} = \text{BQP}_{\text{sep}} \rightarrow$  "entanglement necessary"
- $\text{BQP}_{\text{sep}} = \text{BQP} \rightarrow$  "entanglement NOT necessary"

### Some Complexity Questions:

- $\text{BPP} \stackrel{?}{=} \text{BQP}_{\text{sep}}$
- $\text{PostBQP}_{\text{sep}}$  and PH collapse?
- Deferred measurements in  $\text{BQP}_{\text{sep}}$
- Non-entangling oracles

Thank You!



Slides



# Universal algorithm for transforming Hamiltonian eigenvalues

arXiv:2312.08848

Tatsuki Odake<sup>1</sup>, Hlér Kristjánsson<sup>2,3,1</sup>, Philip Taranto<sup>1</sup> and Mio Murao<sup>1</sup>

1. The University of Tokyo
2. Perimeter Institute for Theoretical Physics
3. Institute for Quantum Computing, University of Waterloo

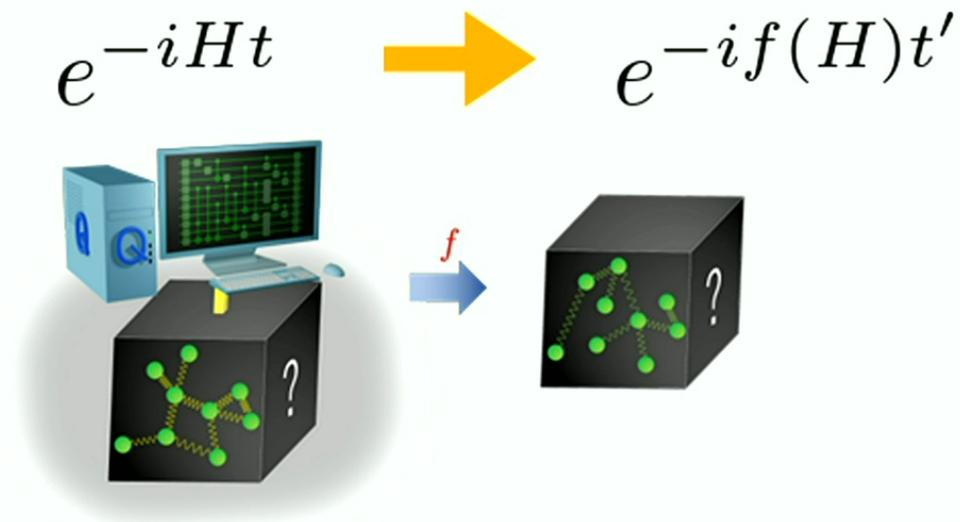


# Simulating quantum systems

- So far: given classical description of Hamiltonian, simulate its dynamics<sup>[1]</sup>

$$H = \sum_j h_j H_j \quad \longrightarrow \quad U = e^{-iHt}$$

- Here: given **black-box** access to Hamiltonian dynamics, simulate a **functional transformation** of the Hamiltonian dynamics



<sup>[1]</sup> e.g. Berry et al., *PRL*, 2015; Low & Chuang, *PRL*, 2017; Campbell, *PRL*, 2019

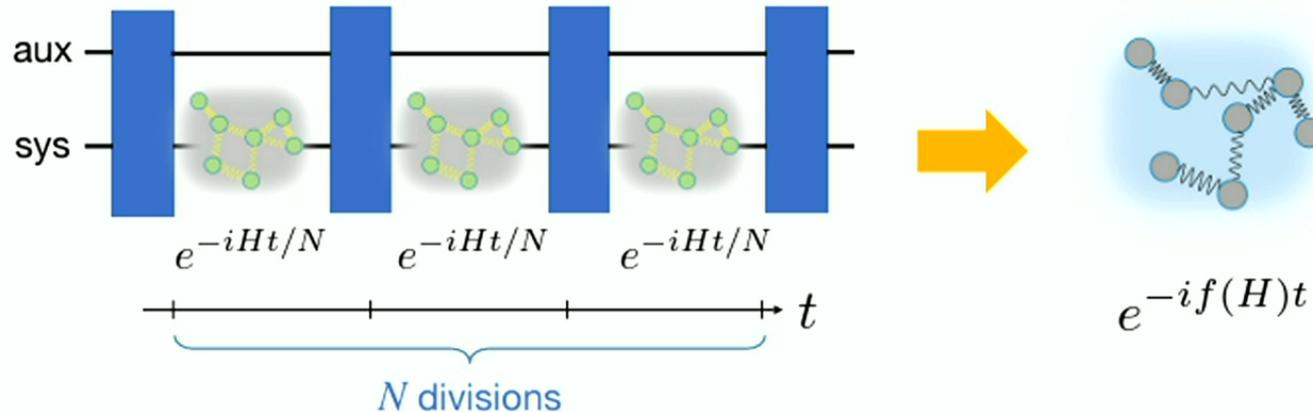
# Higher-order transformations of Hamiltonian dynamics

Functional transformations of Hamiltonian dynamics can be achieved using **higher-order quantum computation** <sup>[1]</sup>

- Universal transformation of the **eigenvalues of any Hamiltonian (energy levels)** by any sufficiently differentiable function  $f(H)$ :

- Deterministic and  $\epsilon$ -approximate with time complexity

$$\underbrace{O\left(\frac{t^6}{\epsilon^6}\right)}_{\text{preprocessing}} + \underbrace{O\left(\frac{t^2 n}{\epsilon}\right)}_{\text{main process}}$$

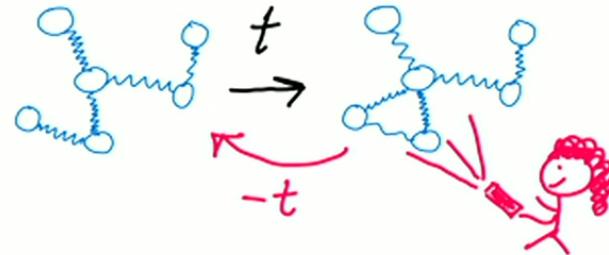


<sup>[1]</sup>Chiribella, D'Ariano, Perinotti, *PRL*, 2008

# Functional programming approach

1. Simulate the **negative-time evolution** <sup>[1]</sup>:

$$e^{-iHt} \longrightarrow e^{+iHt'}$$



Can be done without any additional auxiliary qubits!

2. Simulate the **controlled dynamics** <sup>[2]</sup>

$$e^{\pm iHt} \longrightarrow |0\rangle \langle 0| \otimes I + |1\rangle \langle 1| \otimes e^{\pm iHt}$$

3. Simulate the **Fourier series** of the function  $f$

$$|0\rangle \langle 0| \otimes I + |1\rangle \langle 1| \otimes e^{\pm iHt} \longrightarrow e^{-if(H)t'}$$

4. **Compile** the randomisation in each step globally to improve time complexity

<sup>[1]</sup> Otake, Kristjánsson, Soeda, Murao, *PRR*, 2022. <sup>[2]</sup> Dong, Nakayama, Soeda, Murao, *arXiv*, 2019  
see also: **QSVT**, e.g. Low & Chuang, *Quantum*, 2019



# Topological Measurement-Based Quantum Computation

Gabrielle Tournaire (PhD)  
Sven Bachmann and Robert Raussendorf



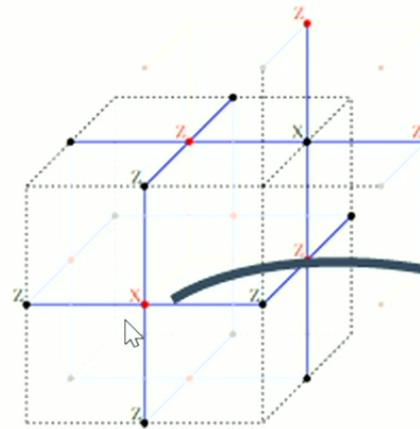
Stewart Blusson  
Quantum Matter Institute

UNIVERSITY OF BRITISH COLUMBIA

# MEASUREMENT BASED QUANTUM COMPUTATION

- 3D cluster state lattice:
  - Black qubits on primal edges and dual faces
  - Red qubits on primal faces and dual edges
  - Stabilizers on primal and dual surfaces
- Measurement in the bulk = Toric code on the surface:
  - Cluster face = Toric code plaquette
  - X measurements: Toric code stabilizers
  - Z measurements: "holes" encoding logical qubits
- Processing information from one Toric code to another:
  - Different measurement patterns in the bulk.
  - Pauli and CNot gates topologically
  - Universality by magic state injection

3D cluster state unit cell:

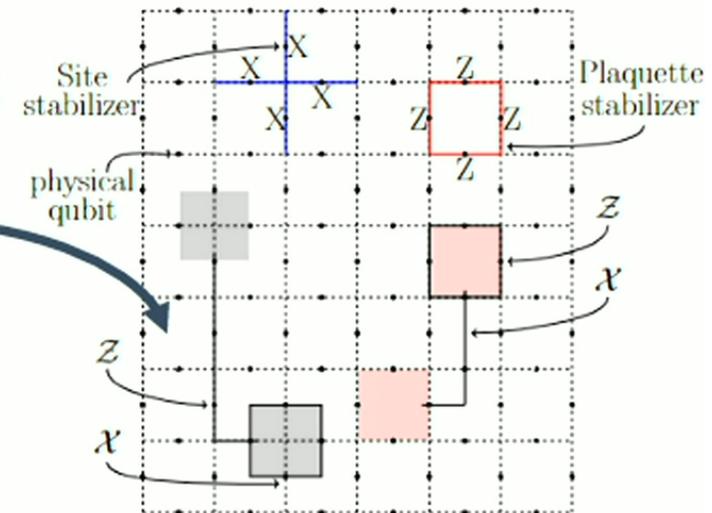


3D cluster state stabilizers:

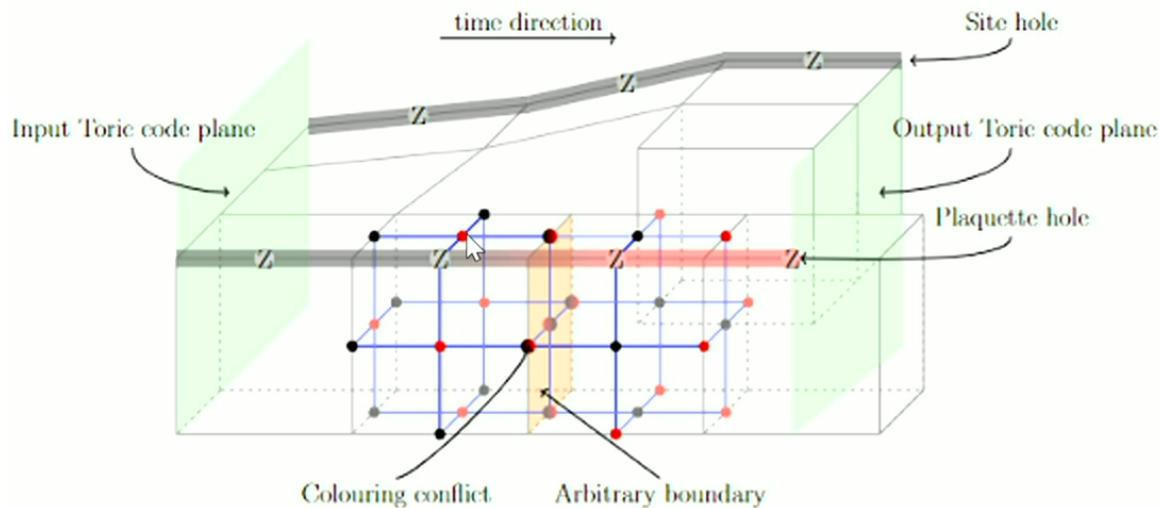
$$K(c_2) = X(c_2)Z(\partial c_2)$$

$$K(\bar{c}_2) = X(\bar{c}_2)Z(\partial \bar{c}_2)$$

Logical qubits in the Toric code:



# TWIST DEFECT: THE HADAMARD GATE

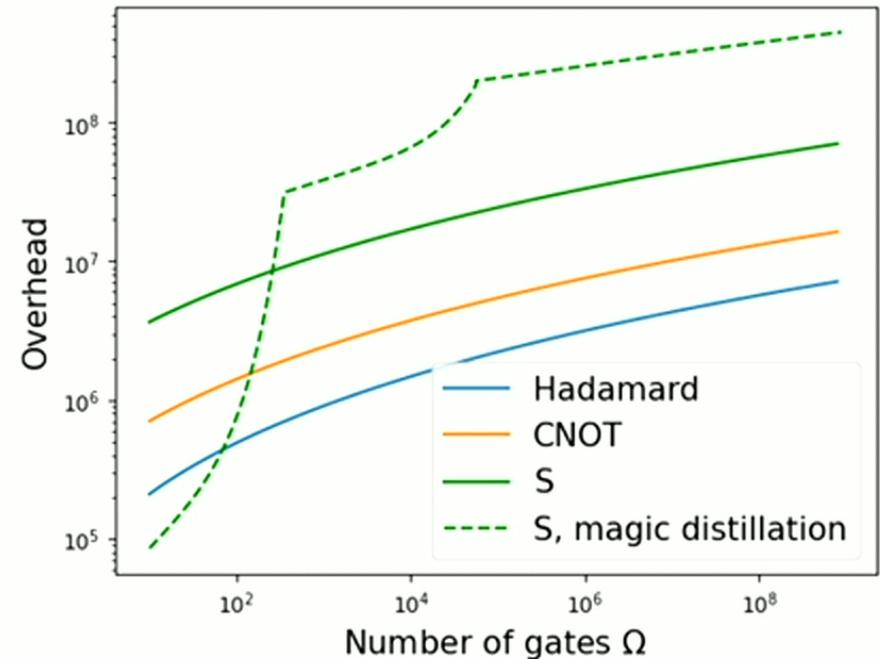


Twist defect: Sites holes  $\leftrightarrow$  Plaquette holes

- Dislocation defect
- Bi-coloring conflict
- Arbitrary boundary where the hole line changes type:
  - Site  $\leftrightarrow$  Plaquette
  - $\mathcal{X}_{\text{primal}} \longleftrightarrow \mathcal{Z}_{\text{dual}}$
  - $\mathcal{Z}_{\text{primal}} \longleftrightarrow \mathcal{X}_{\text{dual}}$
- $\rightarrow$  Hadamard gate
- Topological Clifford group
  - Paulis, CNot, Hadamard, S

# OPERATIONAL OVERHEAD AND CLIFFORD GATES

- Operational cost of a gate
- Number of necessary operations vs number of gates in the circuit
- Low overhead for Hadamard and CNot
- S gate:
  - Hadamard defect yields one order of magnitude improvement
  - Kinks = another round of distillation



# Measurement Back Action causes the difference between Classical and Quantum Counterfactual Effects

**Jonte R Hance**<sup>1,2</sup>, Tomonori Matsushita<sup>3</sup>, Holger F Hofmann<sup>3</sup>

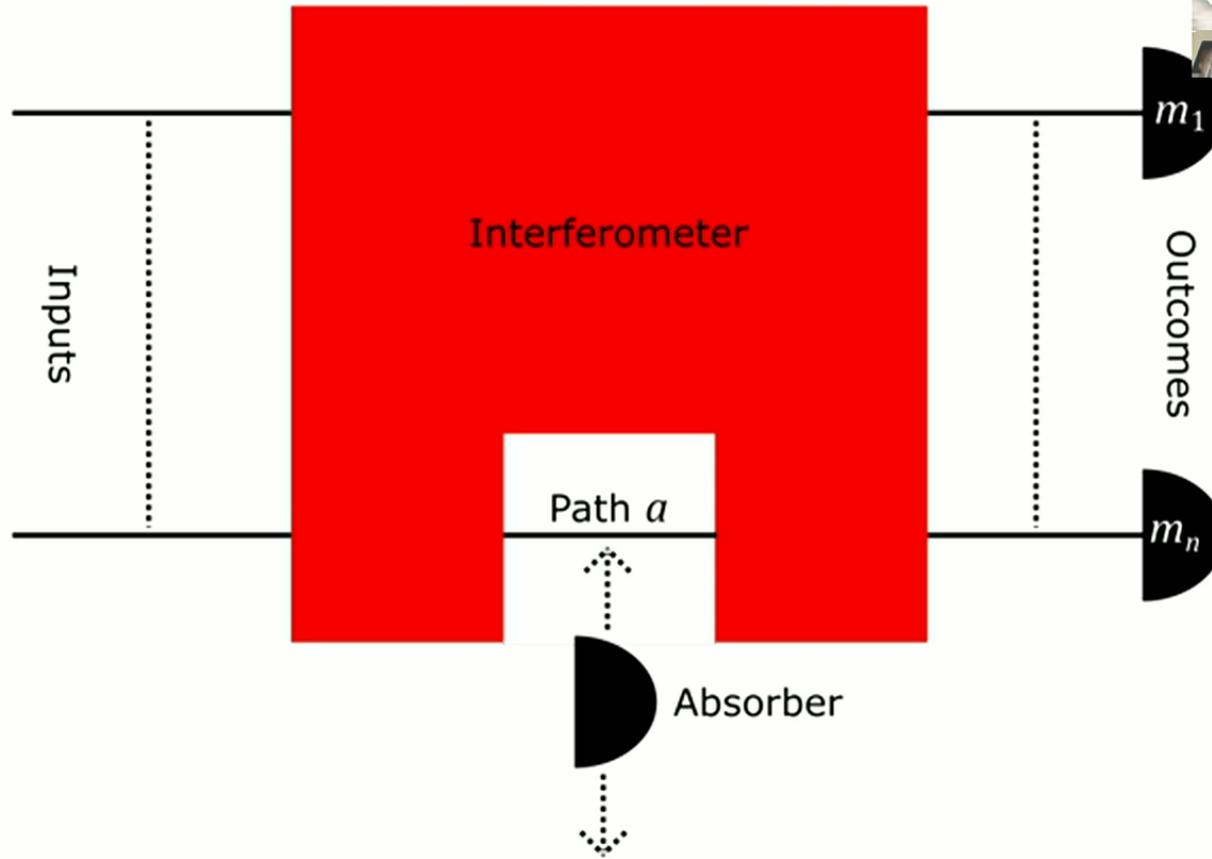
<sup>1</sup> School of Computing, Newcastle University, 1 Science Square, Newcastle upon Tyne, NE4 5TG, UK

<sup>2</sup> Quantum Engineering Technology Laboratories, Department of Electrical and Electronic Engineering, University of Bristol, Woodland Road, Bristol, BS8 1US, UK

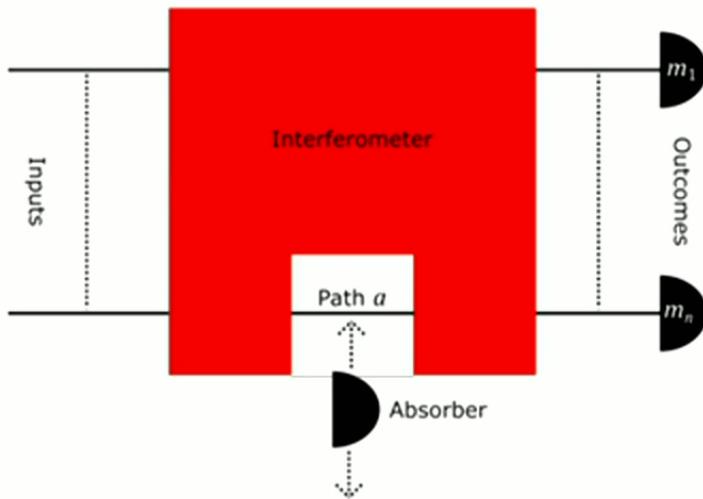
<sup>3</sup> Graduate School of Advanced Science and Engineering, Hiroshima University, Kagamiyama 1-3-1, Higashi Hiroshima 739-8530, Japan



# Generalised Multi-Path Single-Particle Interferometer



# Statistical Distance and Counterfactual Gain



Statistical Distance:  $\Delta_a \equiv \frac{1}{2}P(a) + \frac{1}{2} \sum_m |h_{am}|^2$

Classically, is always  $P(a)$

Counterfactual Gain – difference between a scenario

and classical Stat Distance:  $\Delta_a - P(a) = \sum_{P(m|X_a) > P(m)} (P(m|X_a) - P(m))$   
 $= \sum_{P(m|X_a) > P(m)} (|\langle m|a \rangle|^2 P(a) - 2\varrho(a, m))$

where  $\varrho(a, m) = \text{Re}[\langle m|a \rangle \langle a|\hat{\rho}|m \rangle]$

In EV-type Scenarios,  $\varrho(a, m) = 0$

so  $\Delta_a - P(a) = \sum_{P(m|X_a) > P(m)} (|\langle m|a \rangle|^2 P(a))$

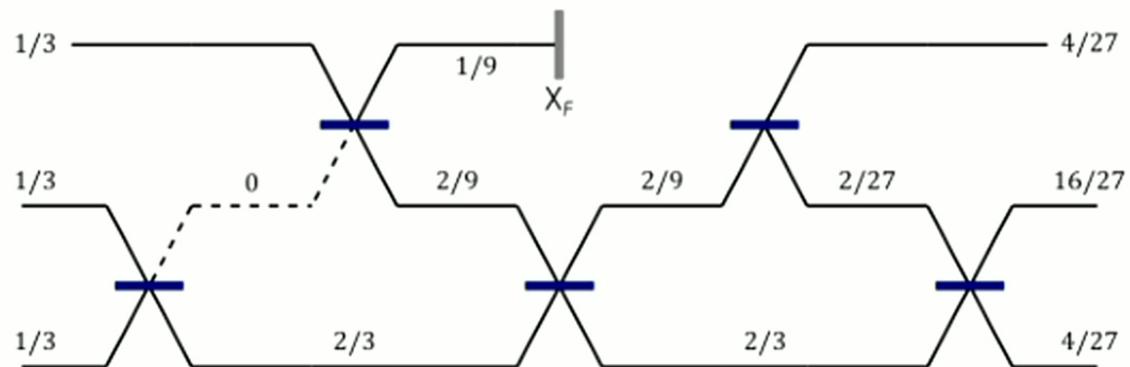
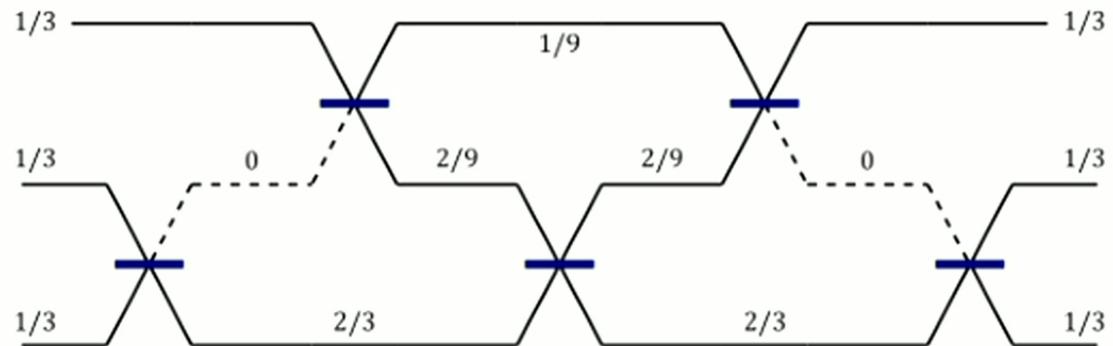
But, if  $\varrho(a, m) < 0$

then the Counterfactual Gain is higher than in the EV Scenario – which hasn't been explored before!



# Applied to Hofmann's Three-Path Interferometer

$$|N_F\rangle = \frac{1}{\sqrt{3}} (|1\rangle + |2\rangle + |3\rangle)$$



# WIGNER AND FRIENDS, A MAP IS NOT THE TERRITORY! CONTEXTUALITY IN MULTI-AGENT PARADOXES

[ARXIV.ORG/ABS/2305.07792](https://arxiv.org/abs/2305.07792)



SIDINEY B. MONTANHANO



MFQ



FOQACIA CONFERENCE

MAY 2024





## Multi-agent scenarios

- Set of agents  $I$ .
- Multi-modal logic (System S4 and topological semantics).
- Knowledge operators  $(K_i, E_U, D_U)$ .
- Trust relation:  $i$  trusts  $j$

$$(j \rightsquigarrow i) \leftrightarrow (K_i K_j \phi \rightarrow K_i \phi) \forall \phi$$

- Example: Wigner's friend scenario, Frauchiger-Renner scenario...

## Sheaf approach to contextuality

- Set  $X$  of measurements.
- Cover of contexts on  $X$ .
- Measurement scenario: sheaf of events  $\mathcal{E} : \langle X, \mathcal{M} \rangle^{op} \rightarrow \mathbf{Set} :: U \mapsto \mathcal{O}^U$ .
- Empirical model: presheaf  $\mathcal{D} : \mathbf{Set} \rightarrow \mathbf{Set} :: \mathcal{O}^U \mapsto \{\mu^{\mathcal{O}^U}\}$ .
- No-disturbance condition:  $\mu^{\mathcal{O}^j} |_{kj} = \mu^{\mathcal{O}^k} |_{kj}$ .
- Noncontextual if there is a global distribution  $\mu^{\mathcal{O}^X}$  which marginalizes to  $\mu^{\mathcal{O}^U}$ .

# RESULTS

## Fundamental truth from trust

The following statements are valid:

- Axiom Truth turns trust relations vacuous.
- The trust relation  $\overset{D}{\rightsquigarrow}$ , along with the condition that  $(\phi \rightarrow D_1\phi) \forall \phi$ , induces a fundamental truth.

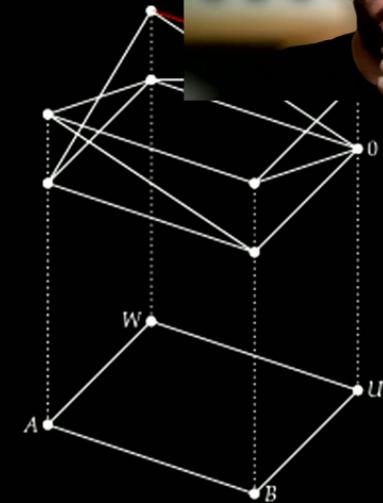
## Measurement scenario as a multi-agent scenario

Measurement scenario	Multi-agent scenario
$X$	$I$
$\mathcal{U}$	$C \subset I$ with $\overset{E}{\rightsquigarrow}$ an equivalence relation
$\mathcal{E}(X)$	$\mathcal{B}_{E_I}$
$\mathcal{E}(\mathcal{U})_{\mathcal{U} \in \mathcal{U}}$	$\mathcal{B}_{D_1}$

## Multi-agent paradox is contextuality

Frauchiger-Renner scenario is mapped as an empirical model presenting logic contextuality.

## Frauchiger-Renner



	00	01	10	11
$A \wedge B$	1/3	0	1/3	1/3
$A \wedge W$	1/6	1/6	2/3	0
$U \wedge W$	3/4	1/12	1/12	1/12
$U \wedge B$	2/3	1/6	0	1/6

## TAKE-HOME MESSAGE



- Alfred Korzybski's statement, "a map is not the territory" and ontological assumptions made in physical theories.
- Modal logic is adequate in quantum and other non-classical settings (at the cost of lambda-dependence).
- Paradoxes and contextuality are the same phenomenon (up to limitations of the Sheaf approach).

Thank you!

Sidiney B. Montanhano. **Wigner and friends, a map is not the territory! Contextuality in multi-agent paradoxes.** arXiv:2305.07792 [quant-ph].



# New Qutrit Tri-orthogonal Codes

Shiroman Prakash, Tanay Saha

Dayalbagh Educational Institute  
Department of Physics and Computer Science

April 22, 2024

# What is the optimum dimensionality of a qudit for fault-tolerance?



- No reason to assume qubits have best overheads/thresholds
- Hints that higher dimensions offer advantages: Classical Reed-Solomon codes/Connections to contextuality for odd prime dimensional qudits
- Experimental realizations of qutrits, Eg: (Goss et al., 2022), (Luo et al., 2023), (Subramanian & Lupascu, 2023)
- **Magic state distillation:** Number of noisy magic states required to produce a pure magic state scales with target noise rate  $\epsilon$  as:

$$\mathcal{O}(\log^\gamma(1/\epsilon)).$$

- The **yield parameter**  $\gamma$  can be compared across different dimensions
- Better yields for larger dimensions: (Krishna & Tillich, 2019), (Campbell et al., 2012). However, these constructions require large dimension  $\sim 17$  for improvements over qubits.
  - **Can we obtain better yield parameters using qutrits rather than qubits?**

# Tri-orthogonal Codes

Tri-orthogonal codes are CSS codes designed to have a transversal non-Clifford gate (diagonal gate from 3<sup>rd</sup> level of the Clifford Hierarchy) for low-overhead magic state distillation.



- Constructed from classical tri-orthogonal spaces: Linear subspace  $C \subseteq \mathbb{F}^N$  s.t.  $\forall x, y, z \in C, \sum_i x_i y_i z_i = 0$  and  $\sum_i x_i y_i = 0$  (in  $\mathbb{F}$ )

Our construction:

- New family of ternary tri-orthogonal  $[9m, 3m]_3$  spaces spanned by the rows of:

$$H = \begin{pmatrix} 0 & 1 & 2 & 0 & 1 & 2 & 0 & 1 & 2 & \dots \\ 2 & 2 & 2 & 1 & 1 & 1 & 0 & 0 & 0 & \dots \\ 2 & 2 & 2 & 0 & 0 & 0 & 1 & 1 & 1 & \dots \\ \vdots & \vdots \end{pmatrix} \quad (1)$$

- Used to construct  $[[9m - k, k, 2]]_3$  quantum tri-orthogonal code ( $k \leq 3m - 2$ )

# Improving Magic State Distillation

- Our family of tri-orthogonal codes give yield parameter  $\gamma = \log_d(n/k) = \log_2 \left( 2 + \frac{6}{3^{m-2}} \right) \rightarrow 1$  as  $m \rightarrow \infty$

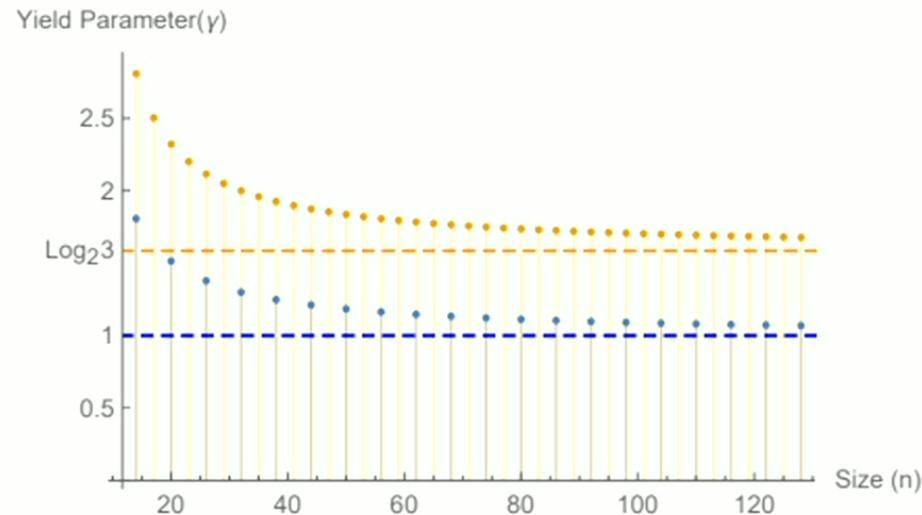


Figure: Blue-Our code; Orange-Best known qubit code (Bravyi & Haah, 2012)

- Analogous qubit construction by Bravyi & Haah has  $\gamma > 1.58$
- Possible to attain  $\gamma < 1$  for qubits, but we require  $2^{58}$  qubits (Hastings & Haah, 2017)



# The Hadamard Mystery

## {Toffoli, Hadamard} Computationally Universal for Quantum Computing



- Toffoli just represents (reversible) classical computing
- Hadamard realizes a variety of functionalities:
  - Change of basis
  - Square root of negation
  - Quantum Fourier Transform
  - Others?
- Any potential computational advantage must leverage the expressive power of Hadamard
- Two Characterizations of Hadamard-like Functionality follow
- Each provide a new perspective on Computationally Universal Quantum Computing



# The Hadamard Mystery

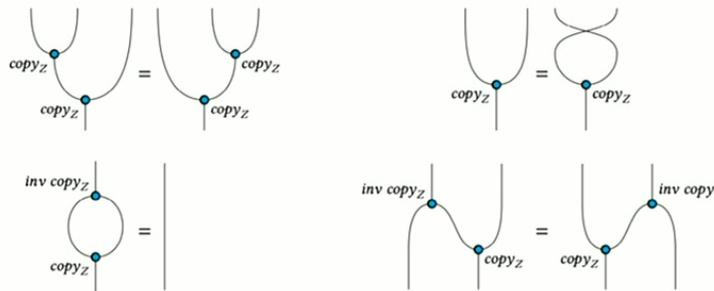
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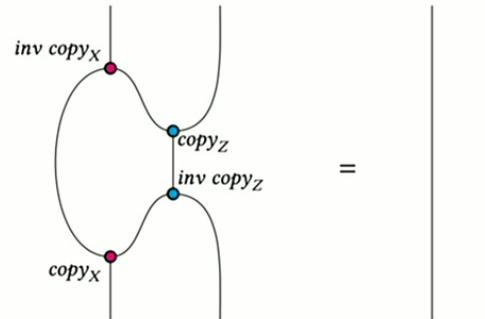


# Hadamard from Two Classical Languages glued by Complementarity [arXiv:2302.01885](https://arxiv.org/abs/2302.01885)



**Finding the Right Basis =>  
Speedup ?**

*FALSE<sub>Z</sub>, TRUE<sub>Z</sub>,  
NOT<sub>Z</sub>, CNOT<sub>Z</sub>, TOFFOLI<sub>Z</sub>,  
COPY<sub>Z</sub>, INV COPY<sub>Z</sub>,  
...*



*FALSE<sub>X</sub>, TRUE<sub>X</sub>,  
NOT<sub>X</sub>, CNOT<sub>X</sub>, TOFFOLI<sub>X</sub>,  
COPY<sub>X</sub>, INV COPY<sub>X</sub>,  
...*

# Hadamard from Classical Language with Steps, 1/4 Steps, and 1/8 Steps [arXiv:2310.14](https://arxiv.org/abs/2310.14)



Conventional classical execution



Running at Multiple Speeds =>  
Speedup ?

Allow  $\frac{1}{2}$  steps with arbitrary interleaving => Quantum



Formally

**Definition of the Quantum Model.** The model consists of a rig groupoid  $(C, \otimes, \oplus, O, I)$  equipped with maps  $\omega: I \rightarrow I$  and  $V: I \oplus I \rightarrow I \oplus I$  satisfying the equations:

$$(E1) \omega^8 = \text{id} \quad (E2) V^2 = \sigma_{\oplus} \quad (E3) V \circ S \circ V = \omega^2 \bullet S \circ V \circ S$$

where  $\circ$  is sequential composition,  $\bullet$  is scalar multiplication (cf. Def. 4),  $\sigma_{\oplus}$  is the symmetry on  $I \oplus I$ , exponents are iterated sequential compositions, and  $S: I \oplus I \rightarrow I \oplus I$  is defined as  $S = \text{id} \oplus \omega^2$ .