

Title: Reliable quantum computational advantages from quantum simulation

Speakers: Juani Bermejo Vega

Collection: Foundations of Quantum Computational Advantage

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Abstract: Demonstrating quantum advantages in near term quantum devices is a notoriously difficult task. Ongoing efforts try to overcome different limitations of quantum devices without fault-tolerance, such as their limited system size or obstacles towards verification of the outcome of the computation. Proposals that exhibit more reliable quantum advantages for classically hard-to-simulate verifiable problems lack, at the same time, practical applicability. In this talk we will review different approaches to demonstrate quantum advantages inspired from many-body quantum physics. The first of them use entangled quantum resources such as cluster states, which are useful to demonstrate verifiable quantum advantages based on sampling problems (Theory proposal Phys. Rev. X 8, 021010, 2018 and recent experimental demonstration arXiv preprint arXiv:2307.14424). The second probe measurement of many-body quantities such as dynamical structure factors in quantum simulation setups (Proceedings of the National Academy of Sciences 117 (42), 26123-26134).

# Reliable quantum computational advantages from quantum simulation

Jara Juana Bermejo-Vega  
University de Granada / iC1 Institute

Foundations of Quantum Computational Advantage  
April 30, 2023

Foto: Erik Lucero/Google

# I am La Juani

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# Quantum Computing, Information & Thermodynamics



Jara Juana  
Bermejo Vega



Daniel  
Manzano



Rhea  
Alexander



Álvaro  
Tejero



Dolores  
Esteve-Díaz



Antonio Jesús  
Rivera Pérez



Carlos  
Cano



Michalis  
Skotiniotis



Giulio  
Camillo



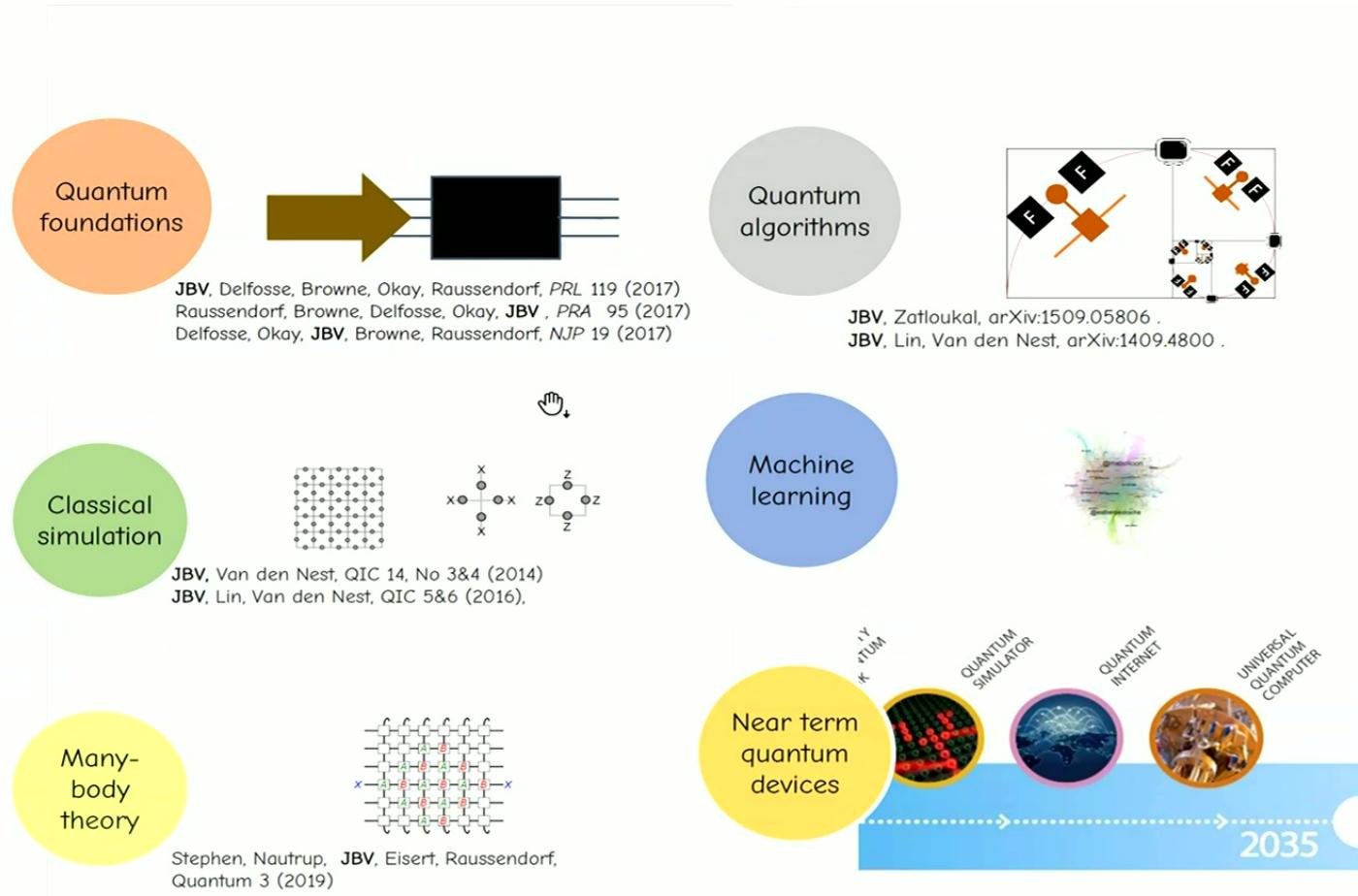
Ana  
Martínez-Sabiote

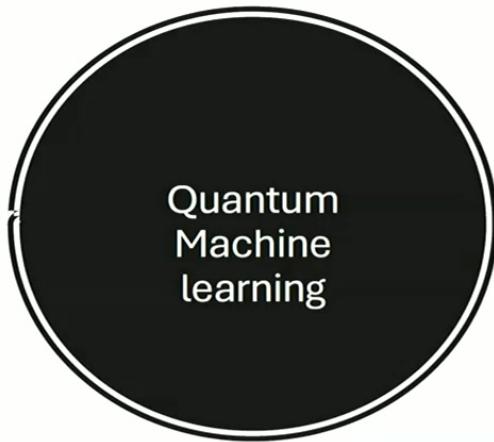


Noelia  
Sánchez Gómez



# Quantum and Classical Computing in Granada





# Entanglement detection with classical deep neural networks

Julio Ureña, Antonio M. Sojo, Jara J. Bermejo-Vega, and Daniel Manzano

Electromagnetism and Matter Physics Department and Institute Carlos I of Theoretical and Computational Physics, University of Granada, E-18071, España.



Entanglement is one of the most important features of quantum mechanics, and its detection and classification is a hard problem. In this paper we present a novel approach to this problem by training a multi layer perceptron to detect entanglement in two and three qubits systems. Our network achieves high efficiencies around 100% in the two qubits case and above 90% for the three qubits one. We also show that it is possible to train the network to classify the states between the different entanglement families with a success ratio up to 77%.

# Granada Quantum Machine Learning Group



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Prof. Carlos Cano



Prof. Antonio Lasanta



Prof. Joaquín J. Torres



Prof. Carlos Pérez-Espigares



Dr. Jara J. Bermejo-Vega



Prof. Ricardo Gutiérrez



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WORKSHOP & NETWORK  
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a diverse community of quantum information scientists,  
technologists, engineers, mathematicians

WE ORGANIZE  
inclusive quantum information conferences

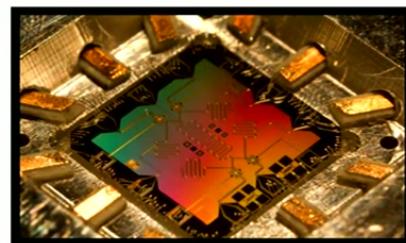
WE CARE ABOUT  
working conditions, equity, diversity, privilege, bias, health,  
safety, responsible research, harassment- and  
discrimination-free environments

WE ARE A SAFE SPACE FOR  
underrepresented groups in quantum STEM: womxn, POC,  
LGBTQ, chronically ill academics ++

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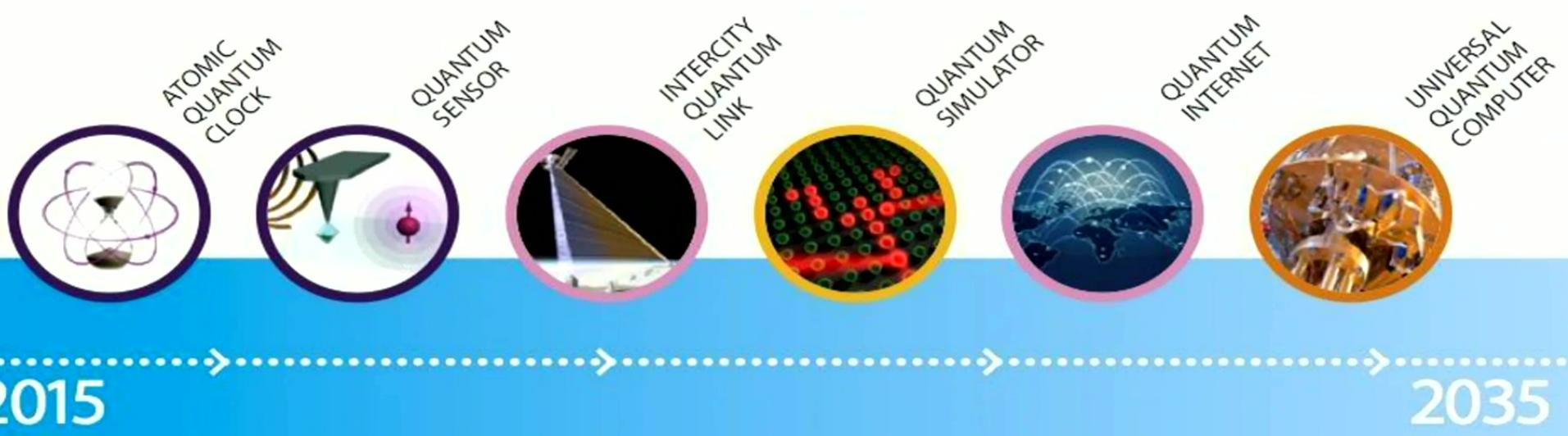
## Noisy Intermediate Scale Quantum computers (NISQ)

- 😊 Quantum computers offer advantages in computation
- 😊 50-1000 qubits devices are under construction



- 😢 Quantum applications are **hard to find** and **implement**

Quantum simulations can offer **practical** quantum advantages



# Quantum Simulation

Dynamical quantum simulators (e.g., using  $10^4\text{-}10^5$  cold atoms in optical lattices) cannot be efficiently classically simulated with state-of-the-art tensor-network algorithms (a la DMRG). *But are these good enough?*

Trotzky et. al., Nature Phys. 8 (2012), Choi et al., Science 352 (2016)



$$\hat{H} = \sum_j \left[ -J (\hat{a}_j^\dagger \hat{a}_{j+1} + \text{h.c.}) + \frac{U}{2} \hat{n}_j (\hat{n}_j - 1) + \frac{K}{2} \hat{n}_j j^2 \right]$$

# Quantum Sampling problems offer complexity-theoretic advantages

## Boson sampling

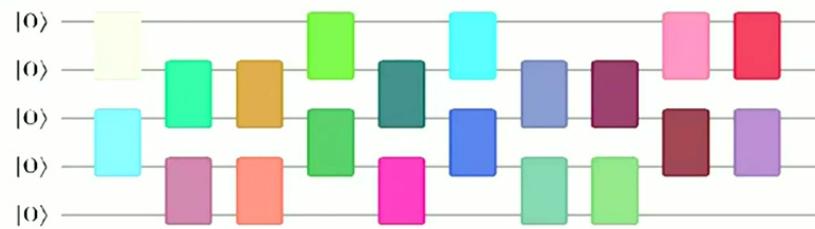
Generates random numbers using a random photonic circuit, hard to simulate based on complexity theoretic evidence.



Aaronson, Arkhipov, Th. Comp. 9 (2013)

## Random circuit sampling ("Google")

They apply a long circuit of random physical interactions on superconducting qubits.



Boixo et al., Nature Phys. 14 (2016)  
Bouland, Fefferman, Nirkhe, Vazirani,  
Nature Phys arXiv:1803.04402  
Arute, Nature, Vol 574, 505 (2019)

# New Scientist

WEEKLY 2 November 2019

SPECIAL REPORT

## QUANTUM SUPREMACY

What the big Google computer breakthrough means for you  
– and what it doesn't

What is a quantum computer? ✤ How will they change the world?

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Is the internet now broken? ✤ Beware quantum winter

### RIVERS IN THE SKY

These hidden marvels are vanishing with the rainforests

PLUS RATS DRIVING TINY CARS / CRYSTAL MUSH ON VENUS /  
RISE OF THE MAMMALS / NEW THEORY OF CONSCIOUSNESS

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SAVE OUR PARASITES!  
How nature's most hated  
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Einstein killed it. But now  
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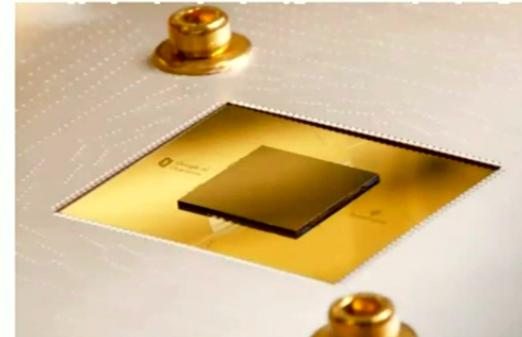


## Quantum supremacy has arrived – what happens to computing now?

The claim that a quantum computer has done something a classical machine can't has generated plenty of excitement, but true quantum computing will take time to appear



TECHNOLOGY | LEADER 30 October 2019



The New York Times

Opinion

## Why Google's Quantum Supremacy Milestone Matters

The company says its quantum computer can complete a calculation much faster than a supercomputer. What does that mean?

By Scott Aaronson

Dr. Aaronson is the founding director of the Quantum Information Center at the University of Texas at Austin.

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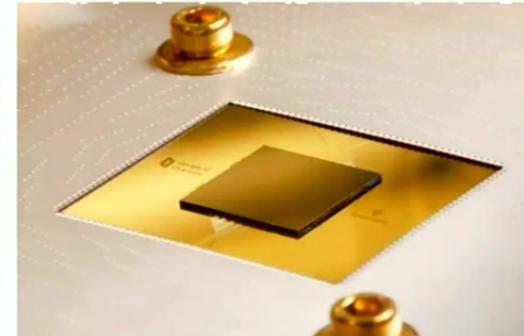


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TECHNOLOGY | LEADER 30 October 2019



IBM

IBM Research Blog Topics Labs About



October 21, 2019 | Written by: Edwin Pednault, John Gunnels & Dmitri Maslov, and Jay Gambetta

The New York Times

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Science

Contents News Careers Journals



Google researchers in Santa Barbara, California, say their advance may lead to near-term applications of quantum computers. GETTY IMAGES/JAVIER HURTADO

IBM casts doubt on Google's claims of quantum supremacy

By Adrian Cho | Oct. 21, 2019, 5:40 AM

# Our work

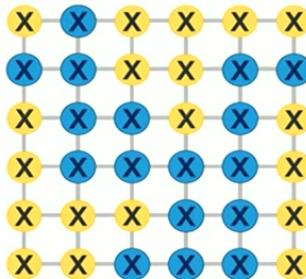
Two types of quantum advantages  
from quantum simulators

## Result: simple Hamiltonian evolutions are “horribly hard” to simulate classically

Approximate sampling from shallow (constant-time) evolutions of 2D translation-invariant Hamiltonians is *impossible* assuming plausible\* complexity-theoretic conjectures:

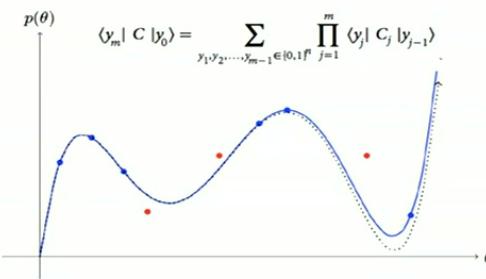
- 1) The Polynomial Hierarchy doesn't collapse
- 2) Anti-concentration  $\approx$  “fairly flat” outputs
- 3) Approximate average-case hardness

\*Identical to random circuit sampling, slightly better than boson sampling



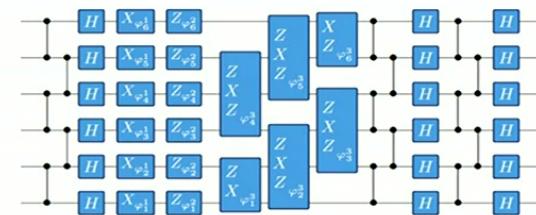
Protocols

Bermejo-Vega, Hangleiter, Schwarz,  
Raussendorf, Eisert, *Phys. Rev. X* 8  
(2018), arxiv:1703.00466



Proofs: anticoncentration & *exact* average case hardness

Bouland, Fefferman, Nirke, Vazirani, *Nature Phys* arXiv:1803.04402  
Hangleiter, Bermejo-Vega, Schwarz, Eisert, *Quantum* 2 (2018), arXiv:1706.03786  
Haferkamp, Hangleiter, Fefferman, Eisert, Bouland, Bermejo-Vega, Upcoming!



# Protocols

arXiv:1703.00466

Prepare  $N$  qubits on an  $n \times m$  square lattice in a product state

$$|\psi_\beta\rangle = \bigotimes_{i=1}^N (|0\rangle + e^{i\beta_i} |1\rangle)$$

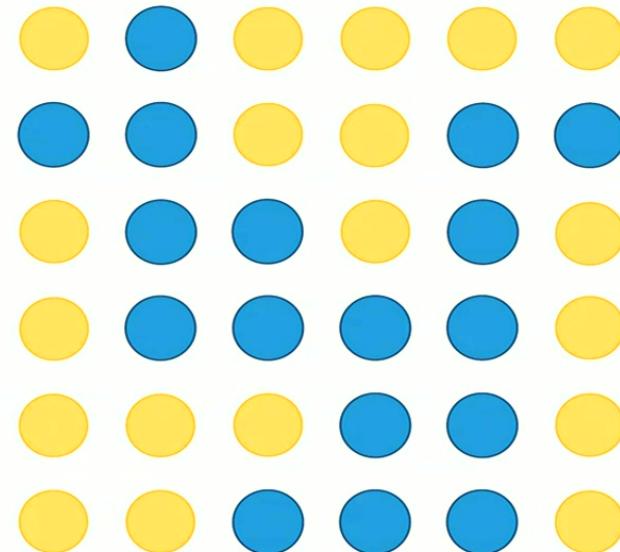
with  $\beta_i \in \{0, \pi/4\}$  randomly.

Quench to

$$H = \sum_{(i,j) \in E} \frac{\pi}{4} Z_i Z_j - \sum_{i \in V} \frac{\pi}{4} Z_i.$$

and evolve under  $U = e^{iH}$ .

Measure all qubits in the X basis.



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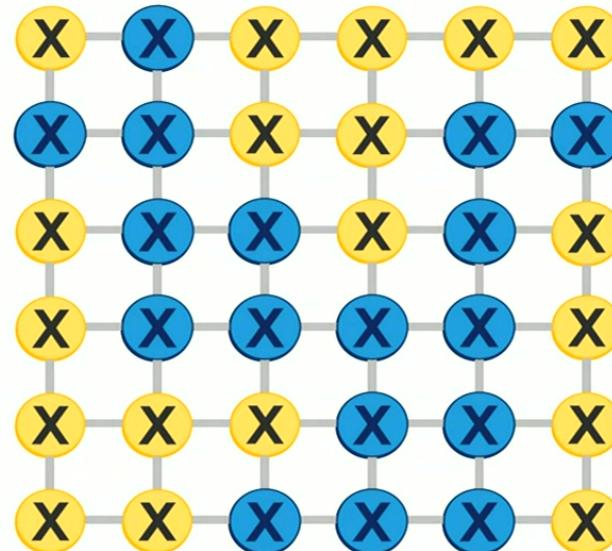
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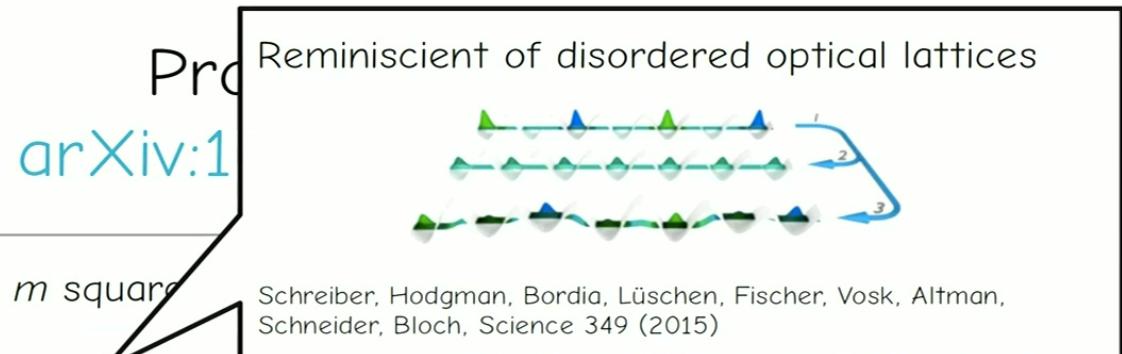
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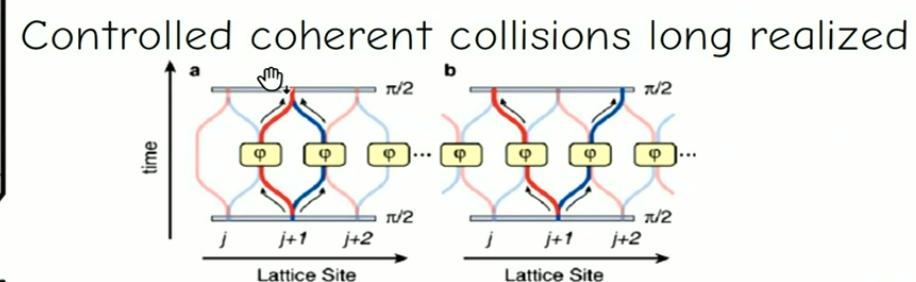




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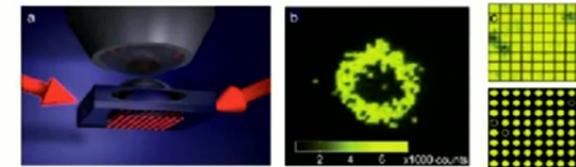


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and evolve under  $U = e^{iH}$ .

Single-site addressing possible (within limits)



Bakr, Gillen, Peng, Foelling, Greiner, Nature 462, (2009)  
Weitenberg, Endres, Sherson, Cheneau, Schauß, Fukuhara, Bloch, Kuhr, Nature (2011)

Measure all qubits in the X basis

## Quantum Verification/Benchmarking: How can we check if the quantum computation is working?

### Challenges:

1. Tomographic methods exponentially costly, no fault-tolerant solutions
2. Classical efficient verification of sampling problems is hard

Hangleiter, Kliesch, Eisert, Gogolin, arXiv:1812.01023

### Approach I

With additional noise/complexity assumptions, a few quantum samples + exponential classical processing is enough

Cross-entropy, HOG, BOG

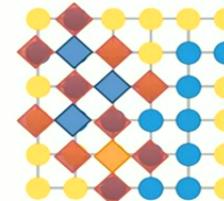
Boixo et al., Nature Phys. 14 (2016)

Bouland, Fefferman, Nirkhe, Vazirani, Nature Phys arXiv:1803.04402

Aaronson, Chen, CCC 17

### Approach II

With reliable single-qubit measurements, the fidelity of the prepared final state can be efficiently estimated



$$F(\rho_0, \rho) \geq 1 - \frac{\langle H \rangle_\rho}{\Delta}$$

Hangleiter, Kliesch, Schwarz, Eisert, Quant. Sc. Tech. 2, (2017)  
Bermejo-Vega, Hangleiter, Schwarz, Raussendorf, Eisert, Phys. Rev. X 8 (2018), arxiv:1703.00466

# Experimental demonstration (arXiv:2307.14424v1)

## Verifiable measurement-based quantum random sampling with trapped ions

Martin Ringbauer,<sup>1</sup> Marcel Hinsche,<sup>2</sup> Thomas Feldker,<sup>1,3</sup> Paul K. Faehrmann,<sup>2</sup> Juani Bermejo-Vega,<sup>2,4,5</sup> Claire Edmunds,<sup>1</sup> Lukas Postler,<sup>1</sup> Roman Stricker,<sup>1</sup> Christian D. Marciak,<sup>1</sup> Michael Meth,<sup>1</sup> Ivan Pogorelov,<sup>1</sup> Rainer Blatt,<sup>1,3,6</sup> Philipp Schindler,<sup>1</sup> Jens Eisert,<sup>2,7,8</sup> Thomas Monz,<sup>1,3</sup> and Dominik Hangleiter<sup>9,10</sup>

<sup>1</sup>Universität Innsbruck, Institut für Experimentalphysik, Technikerstrasse 25, 6020 Innsbruck, Austria

<sup>2</sup>Dahlem Center for Complex Quantum Systems, Freie Universität Berlin, 14195 Berlin, Germany

<sup>3</sup>Alpine Quantum Technologies GmbH, 6020 Innsbruck, Austria

<sup>4</sup>Departamento de Electromagnetismo y Física de la Materia,  
Avenida de la Fuente Nueva, 18071 Granada, Universidad de Granada, Granada, Spain

<sup>5</sup>Institute Carlos I for Theoretical and Computational Physics,  
Campus Universitario Fuentenueva, Calle Dr. Severo Ochoa, 18071, Granada, Spain.

<sup>6</sup>Institut für Quantenoptik und Quanteninformation, Österreichische Akademie  
der Wissenschaften, Otto-Hittmair-Platz 1, 6020 Innsbruck, Austria

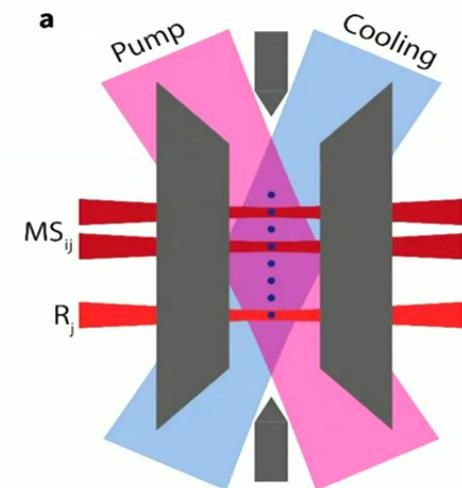
<sup>7</sup>Helmholtz-Zentrum Berlin für Materialien und Energie, 14109 Berlin, Germany

<sup>8</sup>Fraunhofer Heinrich Hertz Institute, 10587 Berlin, Germany

<sup>9</sup>Joint Center for Quantum Information and Computer Science (QuICS), University of Maryland & NIST, College Park, MD 20742, USA

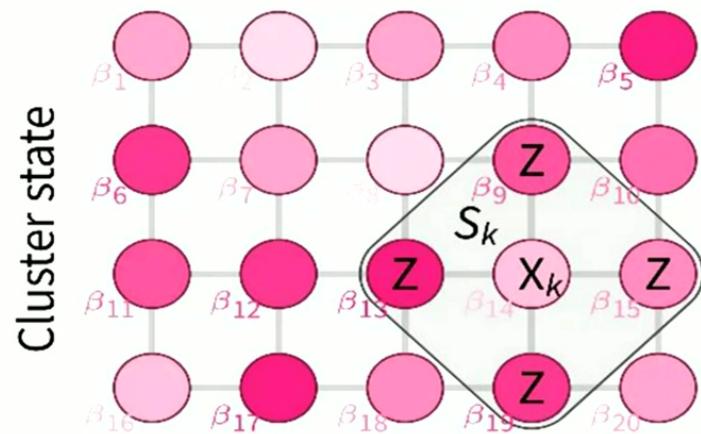
<sup>10</sup>Joint Quantum Institute (JQI), University of Maryland & NIST, College Park, MD 20742, USA

(Dated: July 28, 2023)



## Direct fidelity estimation

$$F = \frac{1}{2^N} \sum_{s \in \mathcal{S}} \langle s \rangle_{\rho} = \frac{1}{2^N} \sum_{s \in \mathcal{S}} \sum_{\sigma=\pm 1} \langle \pi_s^{\sigma} \rangle_{\rho} \cdot \sigma,$$



### Requirements:

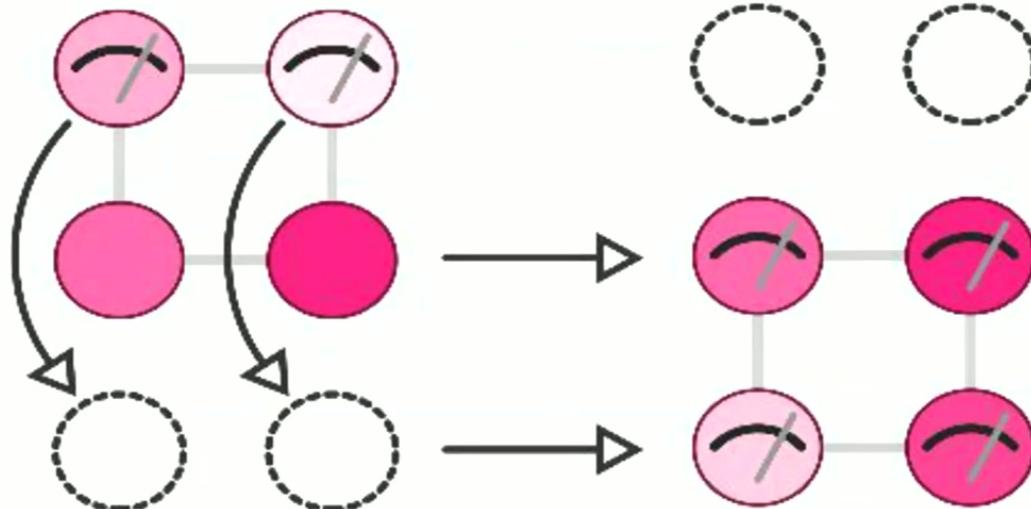
- single qubit measurements

### Advantages (over XEB approaches):

- efficient in terms of both sample and computational complexity
- knowledge only of the measurement noise
- bounds the quality of the samples from a fixed quantum state
- system size efficient: estimates  $F$  with error  $\epsilon$  using  $1/\epsilon^2$  measurements

S. T. Flammia and Y.-K. Liu, Phys. Rev. Lett. 106, 230501 (2011).

## Qubit recycling (non-adaptive MBQC with ions)



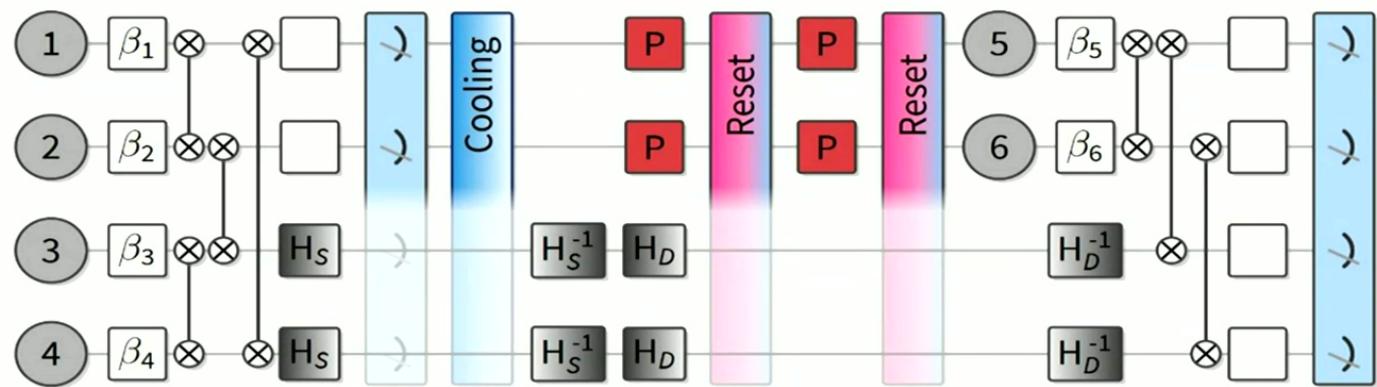
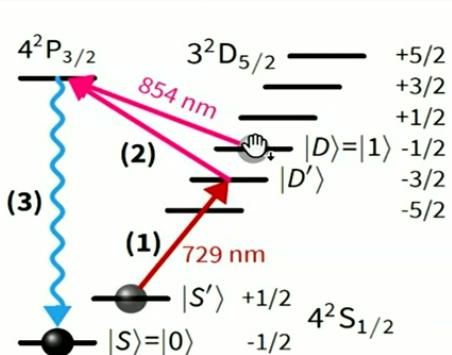
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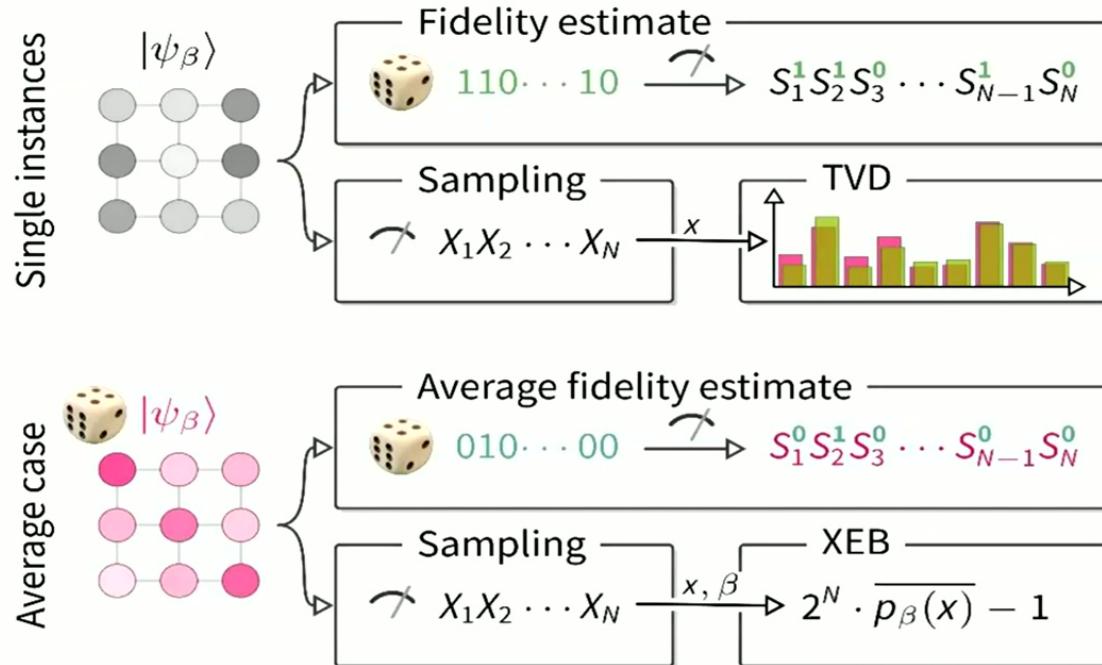
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# Qubit recycling (non-adaptive MBQC with ions)



- Measurement ( $P \leftrightarrow S$ )
- $P = \text{Cooling Reset } (S' \rightarrow D')$
- $H_S = \text{Recycling } (S \rightarrow D' \text{ transition})$
- $H_D(D \rightarrow S')$

# Measuring the fidelity and XEB for our setup



## Requirements:

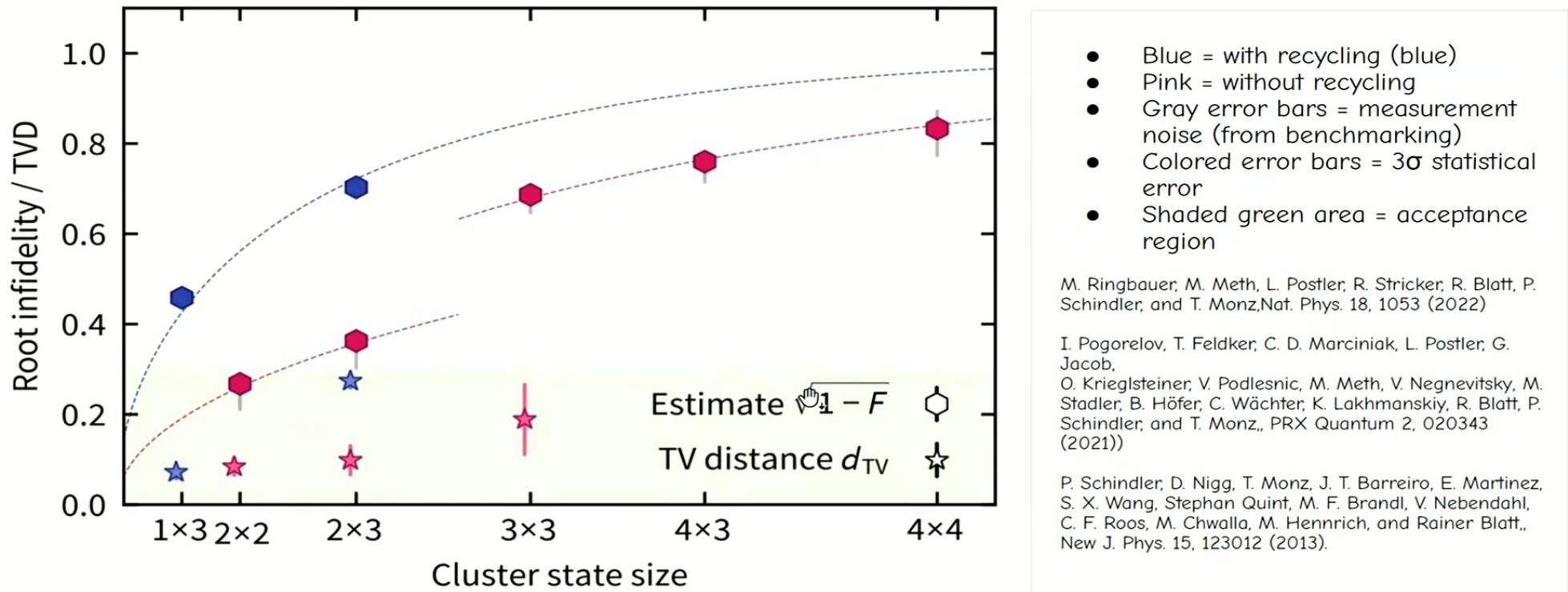
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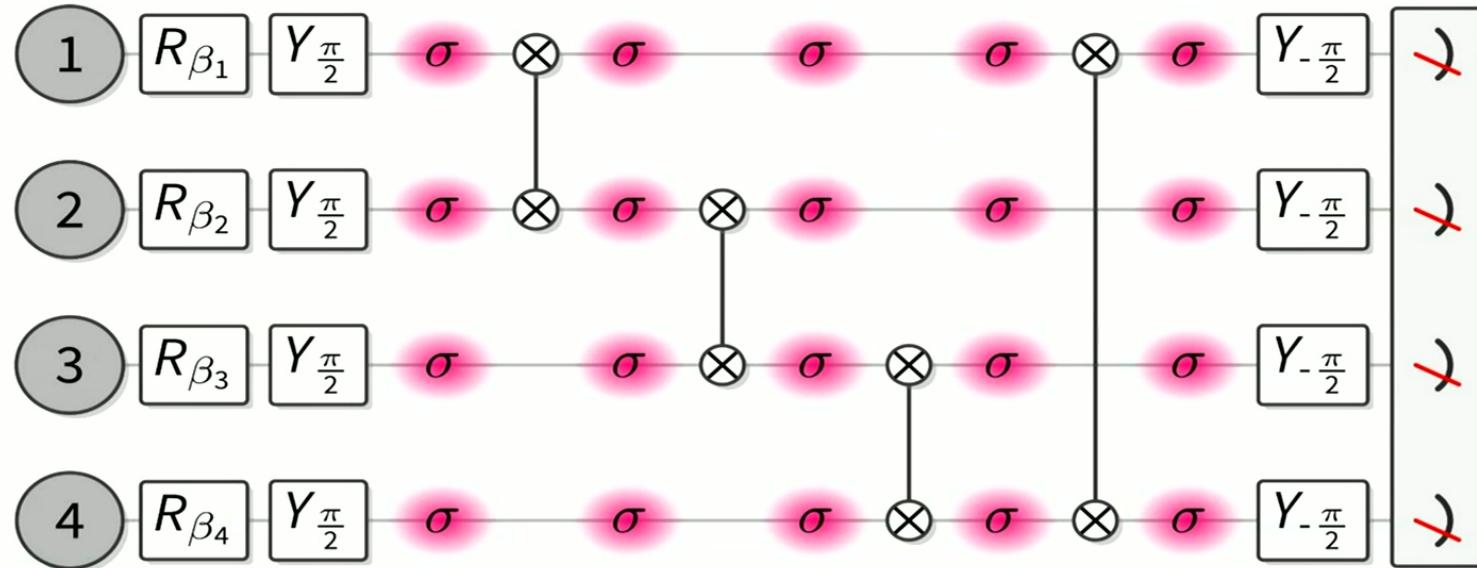
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S. T. Flammia and Y.-K. Liu, Phys. Rev. Lett. 106, 230501 (2011).

## Experimental results for single-instance verification of random cluster states



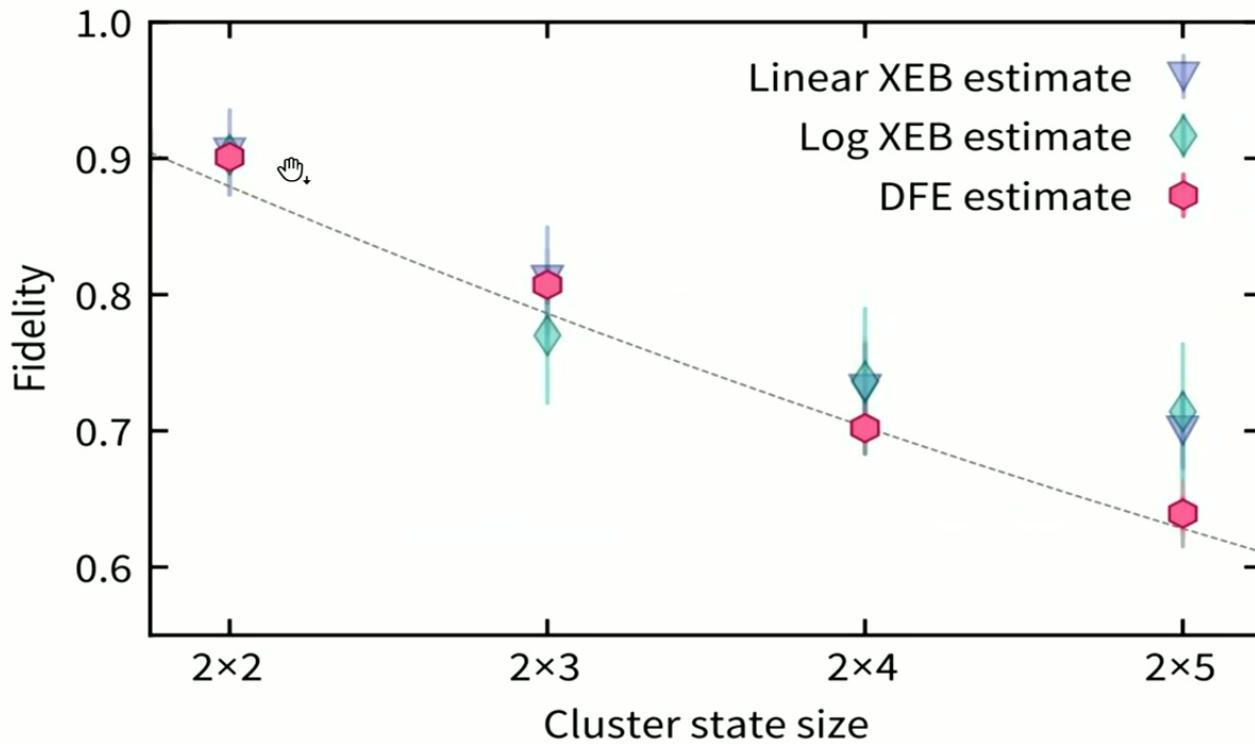
## Estimating the noise strength: verification with artificially induced phase noise



We add dephasing noise on all qubits after initial state preparation and each MS gate.

Rotation angles of Z rotations are drawn from normal distribution with zero mean and standard deviation  $\sigma \in [0, 0.2\pi]$  every 50 shots. For correlated noise, the parameters in each time step are chosen equally and for uncorrelated noise, they are chosen independently.

## Experimental results for average performance verification



- Gray error bars = measurement noise (from benchmarking)
- Colored error bars =  $3\sigma$  statistical error
- Gray shaded area = Fidelity prediction from calibration data gate fidelities of single-qubit gates  $f_{1Q} = 99.8\%$ , twoqubit gates  $f_{2Q} = 97.5 \pm 0.5\%$ , and measurements  $f_M = 99.85\%$ ,
- Dotted line: effective local Pauli error probability of 1.7%

M. Ringbauer, M. Meth, L. Postler, R. Stricker, R. Blatt, P. Schindler, and T. Monz, Nat. Phys. 18, 1053 (2022)

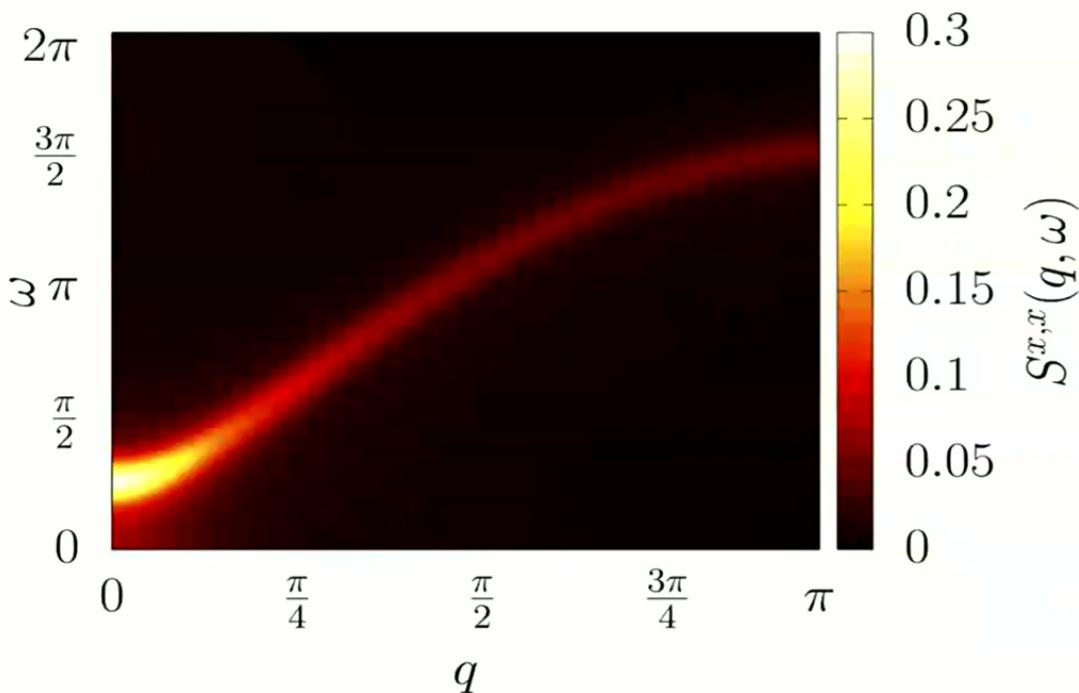
I. Pogorelov, T. Feldker, C. D. Marciniak, L. Postler, G. Jacob, O. Kriegelsteiner, V. Podlesnic, M. Meth, V. Negnevitsky, M. Stadler, B. Höfer, C. Wächter, K. Lakhmankiy, R. Blatt, P. Schindler, and T. Monz, PRX Quantum 2, 020343 (2021))

P. Schindler, D. Nigg, T. Monz, J. T. Barreiro, E. Martinez, S. X. Wang, Stephan Quint, M. F. Brandl, V. Nebendahl, C. F. Roos, M. Chwalla, M. Hennrich, and Rainer Blatt, New J. Phys. 15, 123012 (2013).

Direct fidelity estimation provides an efficient and scalable means of certifying both single instances and the average quality of MBQCS

Sample efficient: Larger systems can be verified with the same number of experiments as we have performed (30k -100 k shots)

# Practical quantum advantage for measuring dynamical structure factors



ML Baez, M Goihl, J Haferkamp, J Bermejo-Vega, M Gluza, J Eisert

Proceedings of the National Academy of Sciences 117 (42), 26123-26134

Direct fidelity estimation provides an efficient and scalable means of certifying both single instances and the average quality of MBQCS

Sample efficient: Larger systems can be verified with the same number of experiments as we have performed (30k -100 k shots)

Applications: tool for verifying NISQ devices and quantum advantages based on sampling problems in MBQC

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jbermejovega@go.ugr.es

## WHAT? DYNAMICAL STRUCTURE FACTOR FOR SPIN SYSTEMS

$$S^{a,b}(\mathbf{q}, \omega) = \frac{1}{N} \sum_{ij} \int_{-\infty}^{\infty} dt e^{-i\mathbf{q} \cdot (\mathbf{r}_i - \mathbf{r}_j)} e^{i\omega t} C_{i,j}^{a,b}(t), \quad C_{i,j}^{a,b}(t) = \langle \sigma_i^a(0) \sigma_j^b(t) \rangle$$

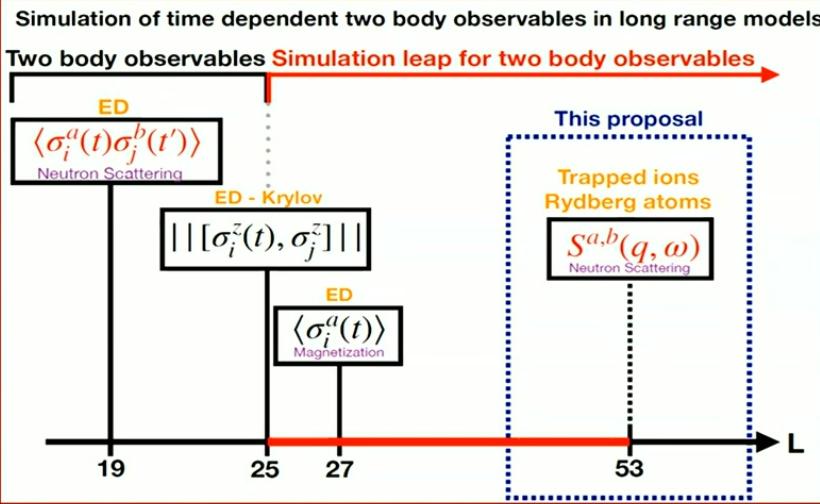
**Approximating the dynamical structure factor  $S_{t_0, t_1}^{\alpha, \beta}(q, \omega)$  within a constant error  $\epsilon \leq 1/8$  over an interval of time  $[t_0, t_1]$  is BQP-hard.**

**For polynomially large ( $t_1 - t_0 = \text{poly}(n)$ ) then it is BQP-hard to approximate  $S_{t_0, t_1}^{\alpha, \beta}(q, \omega)$  within an error  $\epsilon = \text{poly}^{-1}(n)$ .**

arXiv: 1912.0607

$$\hat{H}(J, B) = \sum_i B_z \sigma_i^z - \sum_{i < j} \frac{J}{|r_i - r_j|^\alpha} \sigma_i^x \sigma_j^x$$

J. Haferkamp, J. Bermejo-Vega, J. Eisert



PHYSICAL REVIEW LETTERS 122, 150601 (2019)

### Confined Quasiparticle Dynamics in Long-Range Interacting Quantum Spin Chains

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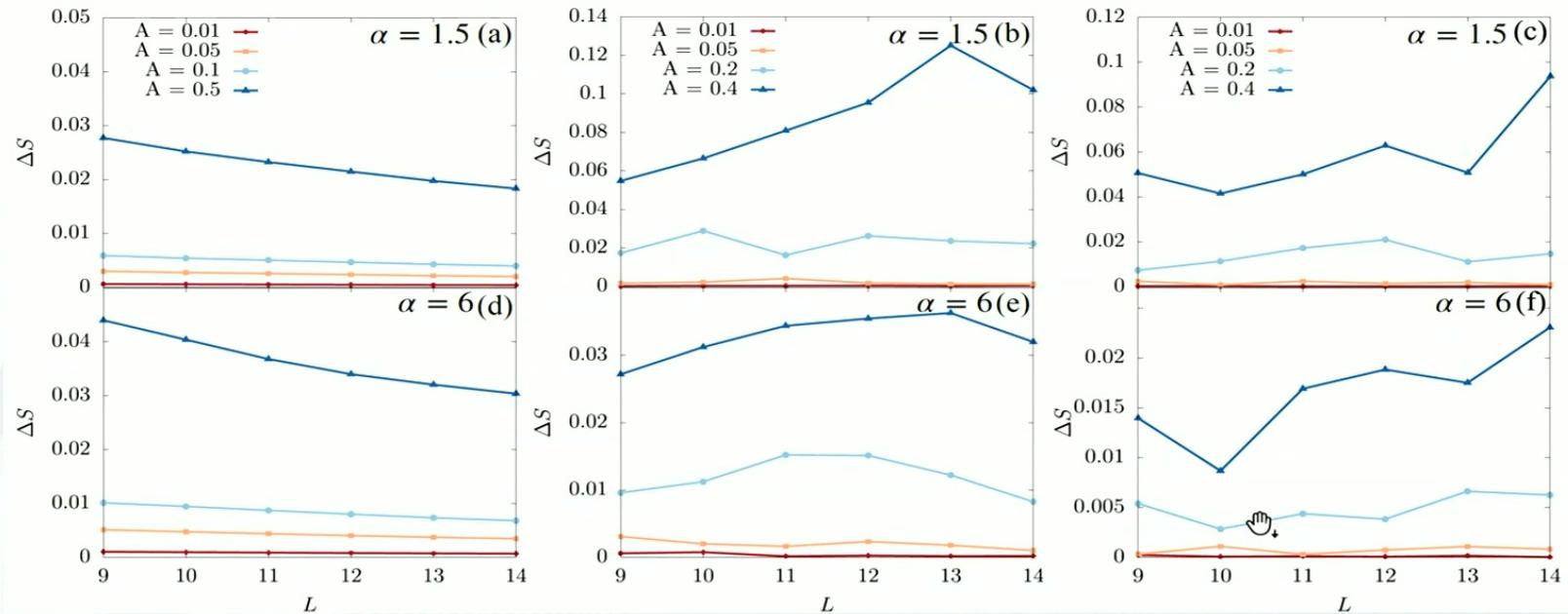
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We study the quasiparticle excitation and quench dynamics of the one-dimensional transverse-field Ising model with power-law ( $1/r^\alpha$ ) interactions. We find that long-range interactions give rise to a confining potential, which couples pairs of domain walls (kinks) into bound quasiparticles, analogous to mesonic states in high-energy physics. We show that these quasiparticles have signatures in the dynamics of order parameters following a global quench, and the Fourier spectrum of these order parameters can be exploited as a direct probe of the masses of the confined quasiparticles. We introduce a two-kink model to qualitatively explain the phenomenon of long-range-interaction-induced confinement and to quantitatively predict the masses of the bound quasiparticles. Furthermore, we illustrate that these quasiparticle states can lead to slow thermalization of one-point observables for certain initial states. Our work is readily applicable to current trapped-ion experiments.

Long range scaling up to  $L = 14$

Experiments have control up to  $A \propto 0.01$

$$\Delta S = \frac{1}{L^2 N_\omega} \sum_q \sum_\omega S(q, \omega)$$



Globally fluctuating Ising  
couplings

Random Ising interactions

Random transverse field

Imperfection effects are negligible and scale in a controlled way up to  $A \propto 0.05$

Existing quantum computers are entering a hard-to-simulate regime but demonstrating quantum advantages is still very challenging

Complexity theoretic proposal based on sampling problems of short Hamiltonian evolutions with advantages for quantum verification

Practical quantum advantage proposal for measuring dynamical quantum advantage in quantum simulators

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