

Title: CMB birefringence from axion strings

Speakers: Andrew Long

Series: Particle Physics

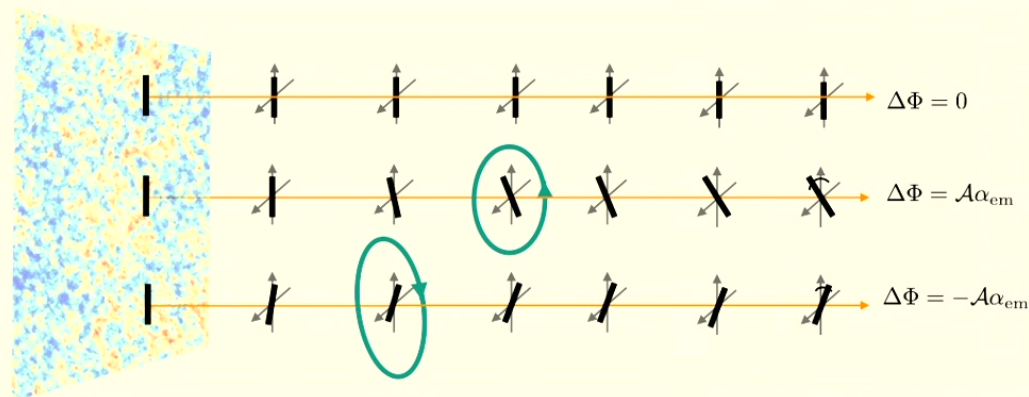
Date: March 26, 2024 - 1:00 PM

URL: <https://pirsa.org/24030125>

Abstract: A cosmological network of axion strings in our Universe today may leave its imprint on the polarization pattern of the cosmic microwave background radiation through the phenomenon of axion-string-induced birefringence. I will explain how this signal arises, discuss how it depends on the properties of the string network and the axion-photon coupling, describe how existing measurements of anisotropic birefringence place constraints on axion strings, and discuss how the non-Gaussian nature of this signal could be leveraged in searches with future data.

Zoom link

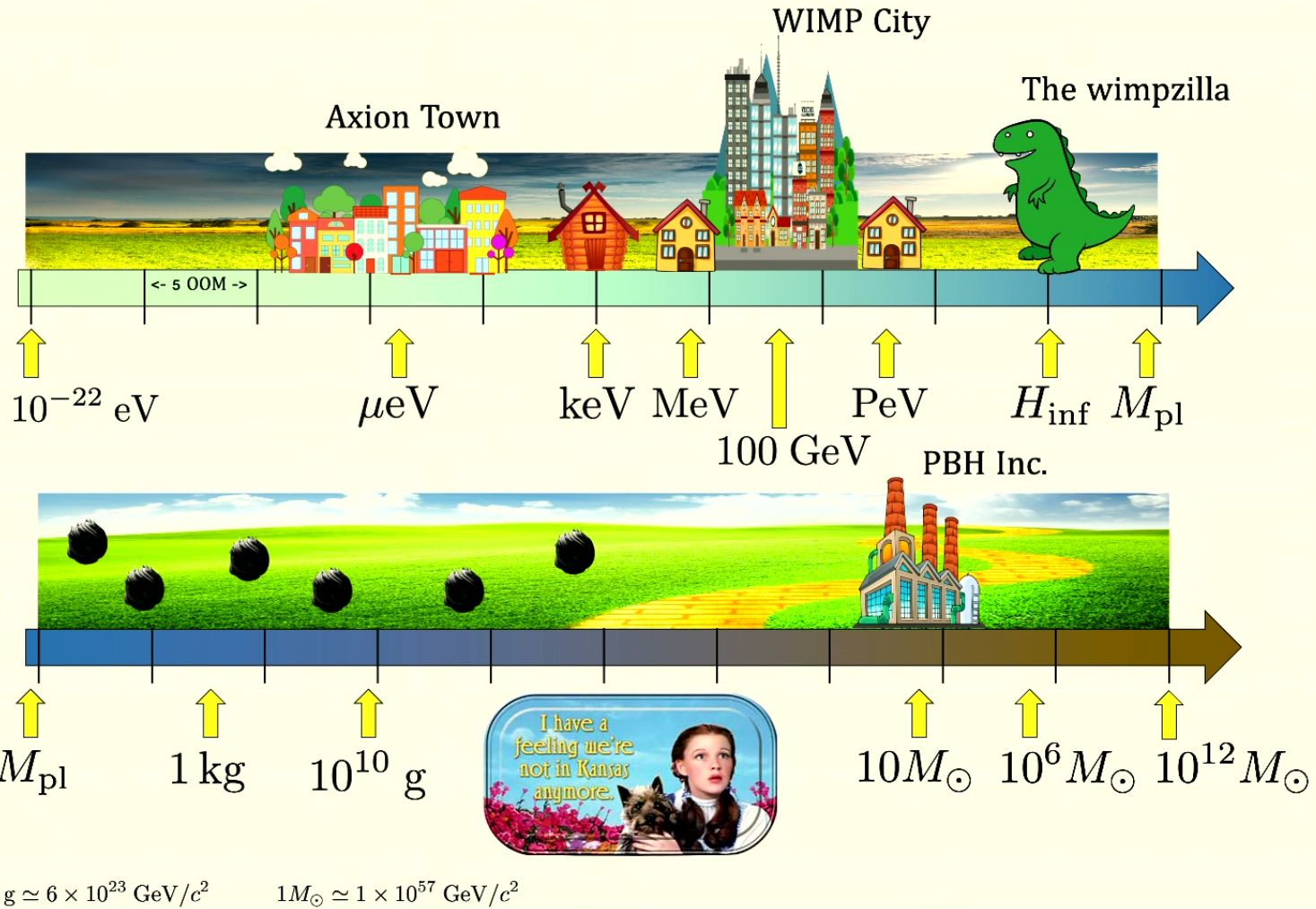
CMB Birefringence from Axion Strings



Andrew J. Long
Rice University
@ Perimeter Institute
March 26, 2024



NOT THIS TALK



Summary

- If a **hyper-light axion-like particle** exists in Nature, the associated cosmological **network of axion strings** can leave an imprint on **CMB polarization** through birefringence
- We use existing **measurements of anisotropic birefringence** (Planck, SPT, ...) to place constraints on this scenario. Next-generation telescopes (CMB-S4) will probe $O(1)$ electromagnetic anomaly coefficients and thereby probe the axion's UV embedding
- We find that it is difficult (but not impossible!) to reconcile the **detection of isotropic birefringence** with strong limits on anisotropic birefringence coming from axion strings
- We argue that measurements of anisotropic birefringence could not only reveal the presence of a hyper-light ALP in Nature, but also lead to a **measurement of its mass**
- Our ongoing work (very early stages) seeks to use machine learning techniques (spherical CNN) to detect the subtle signal of axion strings in CMB polarization data

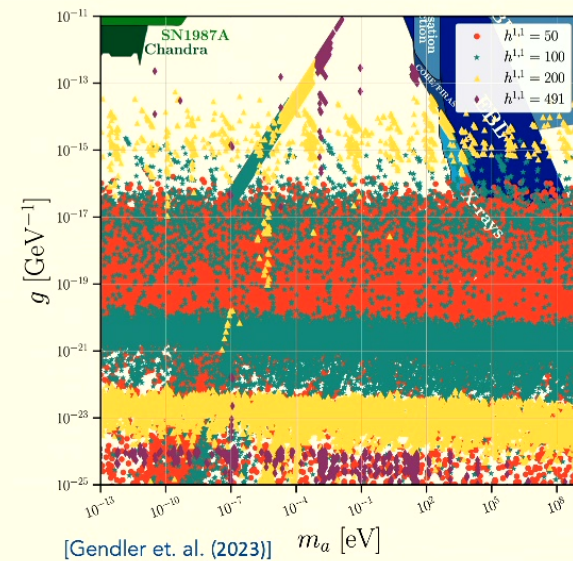
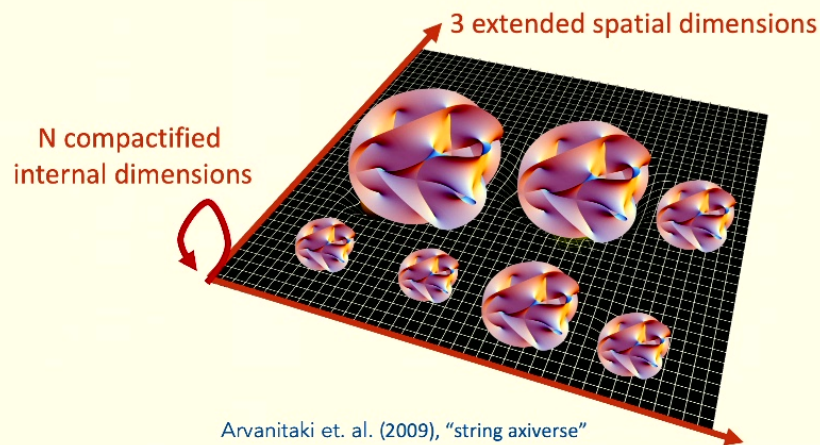
axion-like particles & cosmic axion strings

Theory landscape: axion-like particles

axion-like particles

$$\mathcal{L} \supset \frac{1}{2}(\partial a)^2 - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

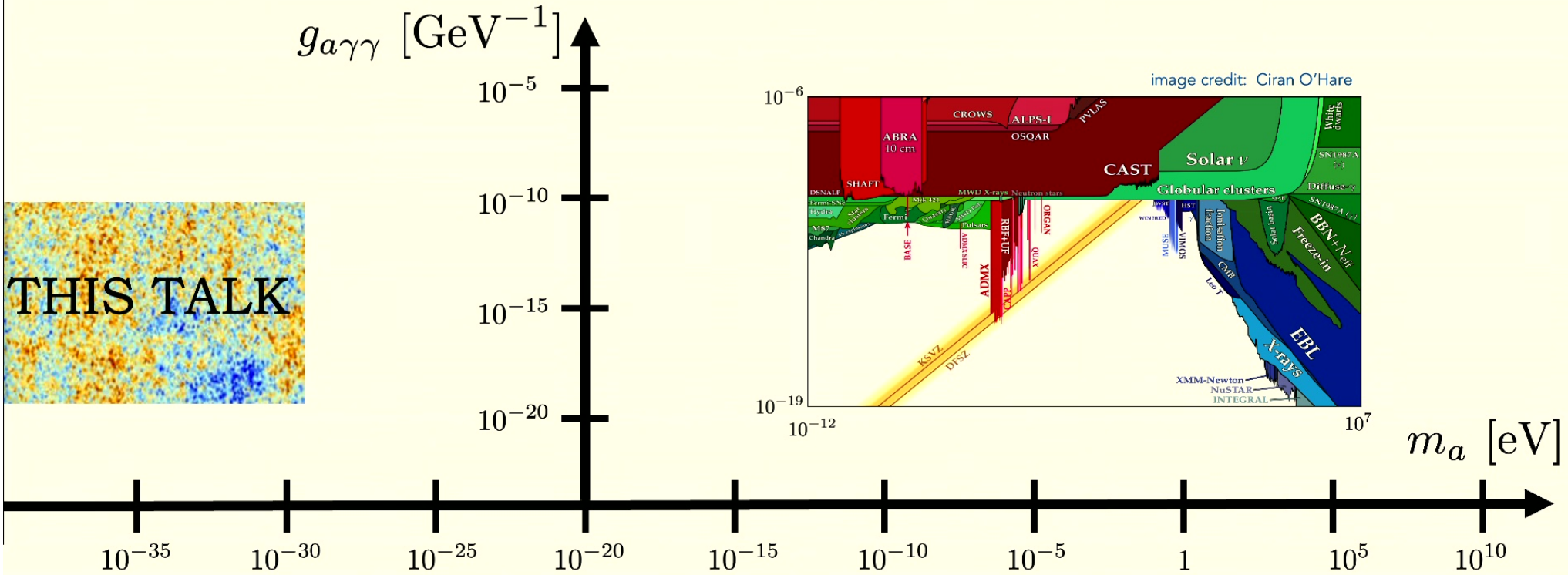
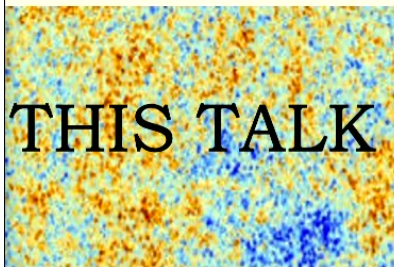
ALPs from extra dimensions
(such as string theory)



Theory landscape: axion-like particles

$$\mathcal{L} \supset \frac{1}{2}(\partial a)^2 - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$g_{a\gamma\gamma}$ [GeV⁻¹]



CMB birefringence from axion strings

5

Andrew Long (Rice University)

Axion strings from ALPs

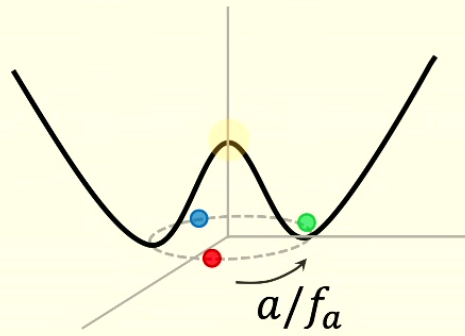
[Kibble (1976)]
[Vilenkin & Vachaspati (1987)]

string formation:
early-universe phase transition

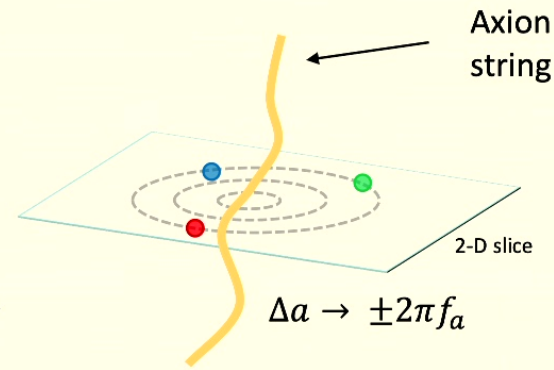
Field space

$$\mathcal{L} = |\partial\Phi|^2 - \lambda(|\Phi|^2 - f^2/2)^2$$

$$\Phi(x) = \frac{f+s(x)}{\sqrt{2}} e^{ia(x)/f}$$



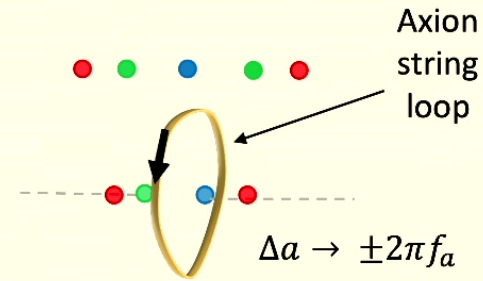
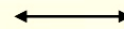
Physical space



Axion string

string thickness = microscopic

string length = cosmological



Axion string loop

"post-inflation scenario"
assume: $T_{RH} > f_a$

Clockwise (+); or
anti-clockwise (-)

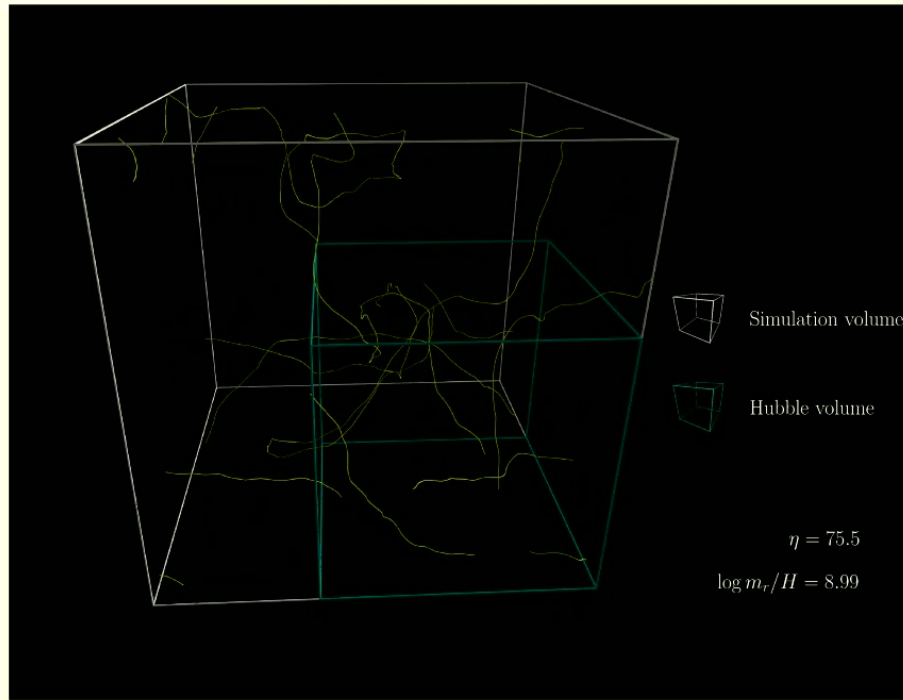
image credit: Mudit Jain (2021)

A cosmic string network

[Buschmann et. al. (2022)]

see also: [Saikawa et. al. (2024)]

string network simulation:



things we have learned:

- the network contains long strings & string loops
- string tension pulls bent string segments ($L < d_H$)
- string segments cross & reconnect
- reconnections forms new loops
- loops ($L < d_H$) emit axions and collapse
- distribution over loop lengths tracks Hubble
- average energy density tracks Hubble

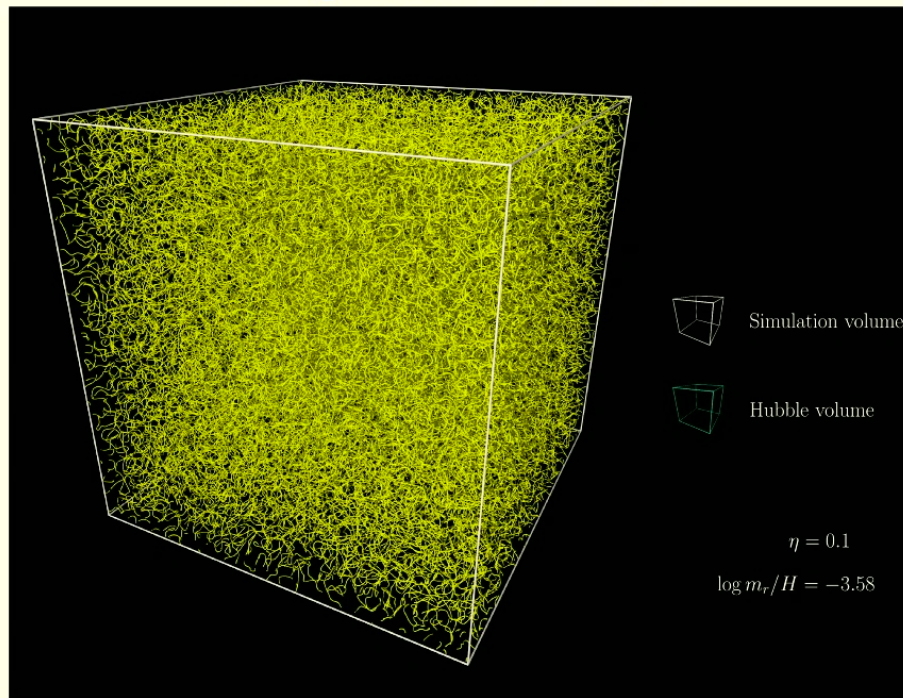
things we want to know:

- what's the energy spectrum of axion emission?
- how many strings in the universe today?
 - does the network maintain scaling?
 - should be $O(10)$ strings per Hubble volume
- distribution over loop lengths

A cosmic string network

[Buschmann et. al. (2022)]
see also: [Saikawa et. al. (2024)]

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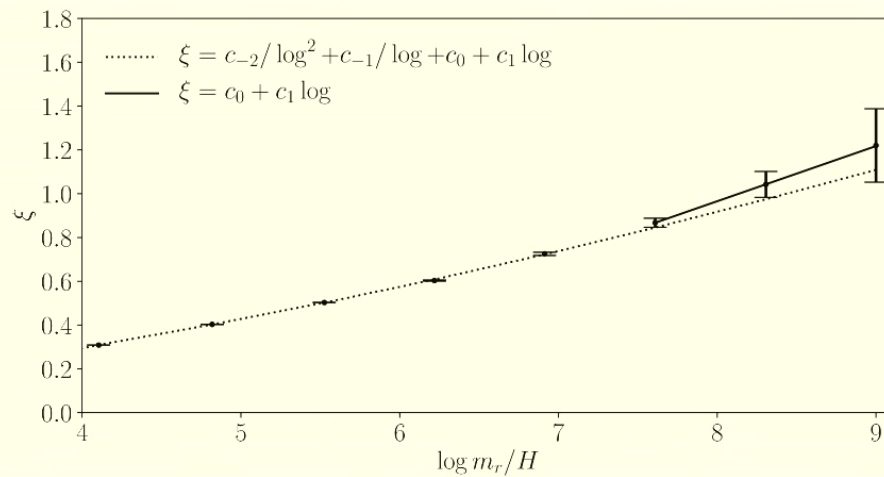
- what's the energy spectrum of axion emission?
- how many strings in the universe today?
 - does the network maintain scaling?
 - should be $O(10)$ strings per Hubble volume
- distribution over loop lengths

To scale or not to scale?

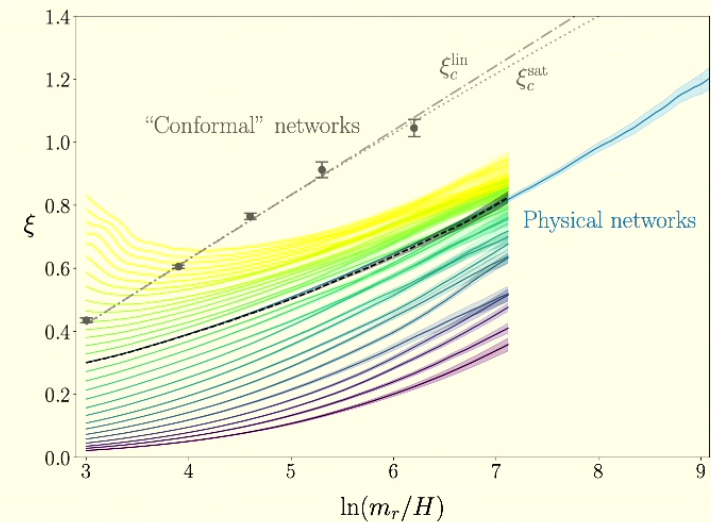
see also: [Gorghetto et. al. (2021)]

string abundance parameter: $\xi \equiv l_s t^2 / \mathcal{V}$ so $\rho_s \sim \xi \mu H^2$

Buschmann et. al. (2022)
adaptive mesh refinement



Saikawa et. al. (2024)
fixed lattice 11264^3 sites



extrapolating till today: $\log \sim 120$ and $\xi \sim 25$

Cosmological probes of axion strings

How can we detect axion strings in the Universe today?

Gravitational Probes

Kaiser-Stebbins effect → CMB

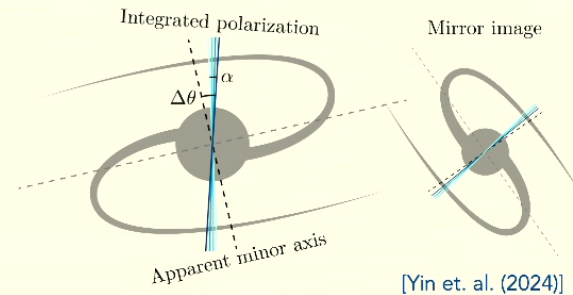
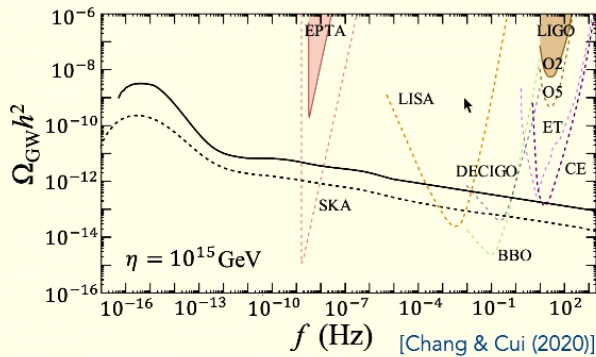
string wakes → LSS

grav wave emission → PTA, LVK, LISA

Non-Gravitational Probes

particle emission → dark radiation ... BBN ... cosmic rays ... CMB effects

birefringence → CMB ... galaxy polarization/shape



birefringence from axion strings

How could we detect an axion string?

[Harvey & Naculich (1989)], [Carroll, Field, Jackiw (1990,91)], [Harari, Sikivie (1992)]
 [Fedderke, Graham, Rajendran (2019)], [Agrawal, Hook, Huang (2019)]
 [Yin, Dai, Ferraro (2021) & (2023)]

assume interaction
 with electromagnetism:
 standard Chern-Simons coupling

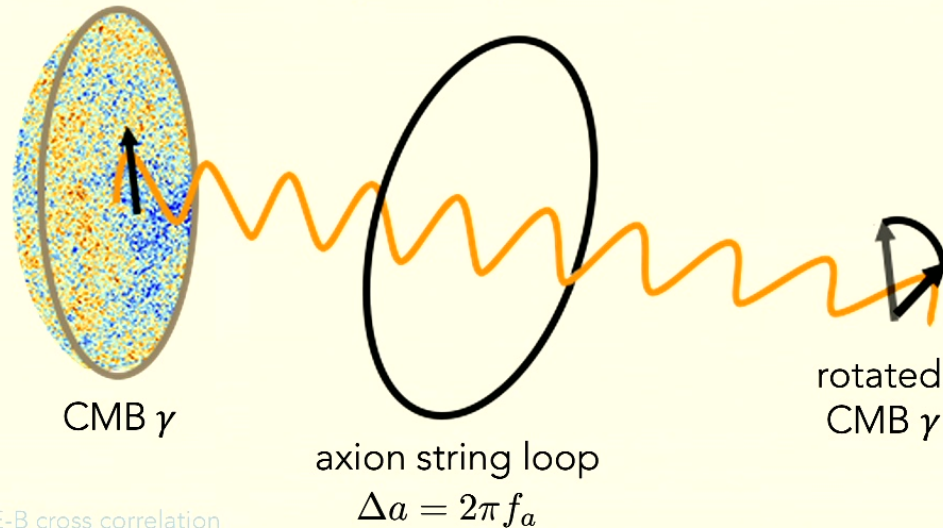
$$\mathcal{L}_{\text{int}} = -\frac{1}{4} g_{a\gamma\gamma} a F \tilde{F}$$

$$g_{a\gamma\gamma} = -\mathcal{A} \frac{\alpha_{\text{em}}}{\pi f_a}$$

$$\mathcal{A} = \sum Q_{\text{PQ}} Q_{\text{em}}^2 \sim \# / 9$$

axion-induced birefringence:
 an electromagnetic wave
 traveling through a varying axion field
 has its plane of polarization rotated

$$\alpha = \frac{1}{2} g_{a\gamma\gamma} \int_C dX^\mu \partial_\mu a(X)$$



rotation angle

$$\alpha = g_{a\gamma\gamma} \pi f_a$$

$$\equiv -\mathcal{A} \alpha_{\text{em}}$$

$$\approx -0.42^\circ \mathcal{A}$$

* birefringence can be measured through E-B cross correlation

The loop-crossing model

Assumptions

- All strings are circular loops
- Randomize loop orientation
- Randomize loop location in space
- All loops same radius at any time
- Loop radius tracks Hubble

$$R(t) = \zeta_0 / H(t)$$

- Number of loops tracks Hubble

$$\rho(t) = \xi_0 \mu(t) H(t)^2$$

Model Parameters

$$\{m_a, \mathcal{A}, \zeta_0, \xi_0\} \quad g_{a\gamma\gamma} = -\mathcal{A} \frac{\alpha_{em}}{\pi f_a}$$

loop-crossing model

$$\zeta_0 = 1.0$$

$$\xi_0 = 1.0$$



early time -> small loops
late time -> large loops

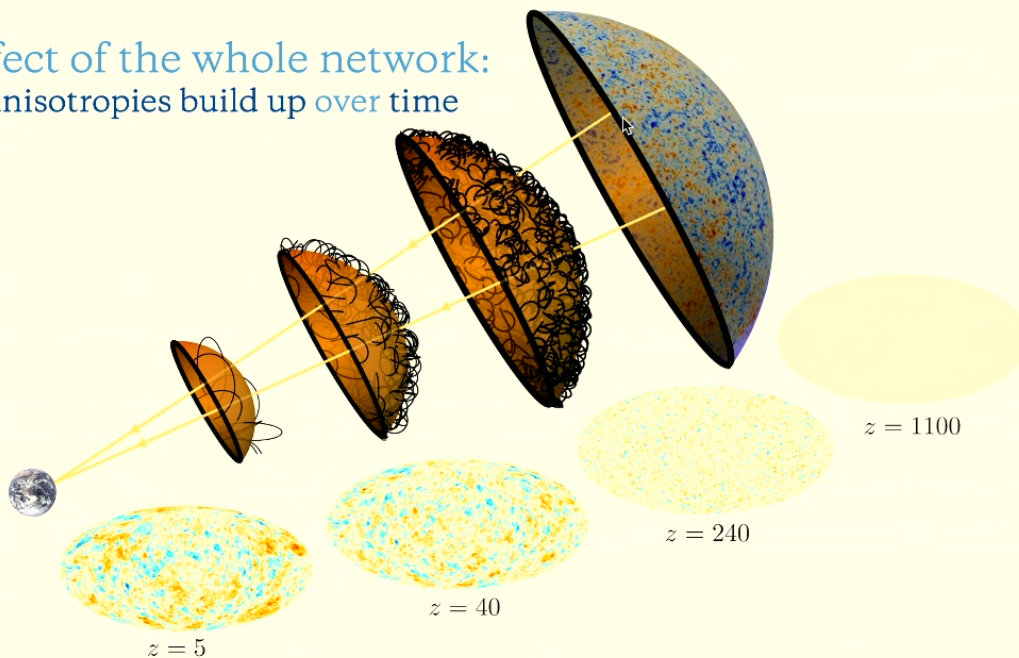
Expected birefringence signal

[Jain, AL, Amin, arXiv:2103.10962]
[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

loop-crossing model:
a network of circular loops

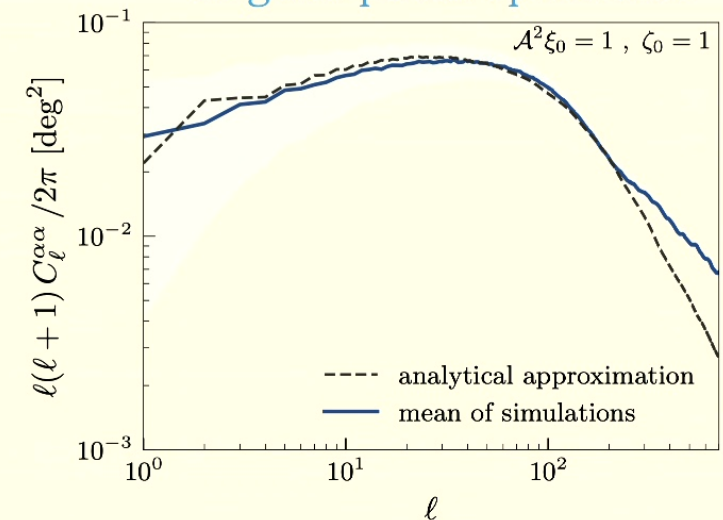
\mathcal{A} = dimensionless axion-photon coupling
 ξ_0 = dimensionless loop density (Hubble units)
 ζ_0 = dimensionless loop length (Hubble units)

effect of the whole network:
anisotropies build up over time



* need $m_a \lesssim 3H_{\text{cmb}} \approx 10^{-28}$ eV for the network to survive until after recombination

angular power spectrum:



approx. scale invariant up to $l \sim 100$

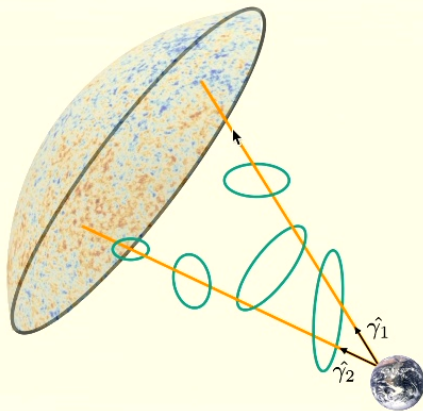
degeneracy: $\langle \alpha \alpha \rangle \sim \mathcal{A}^2 \xi_0$

Analytical understanding

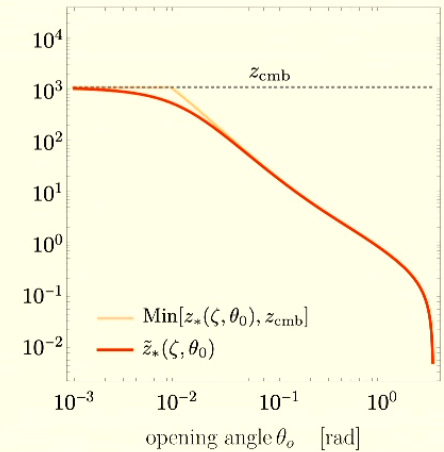
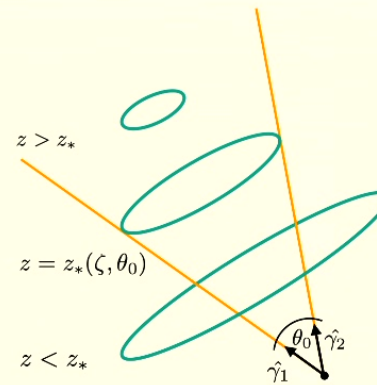
[Jain, AL, Amin, arXiv:2103.10962]

correlations accumulate
when both photons pass
through the same loops

$$\langle \alpha(\hat{\gamma}_1) \alpha(\hat{\gamma}_2) \rangle = (\mathcal{A} \alpha_{\text{em}})^2 N_{\text{both}}(\hat{\gamma}_1 \cdot \hat{\gamma}_2)$$



large-angle correlations are
established later (small z)

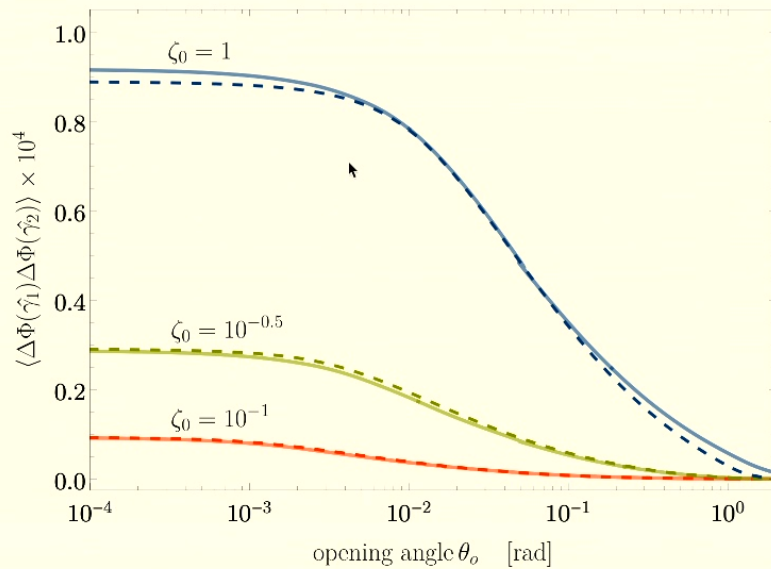


Analytical understanding

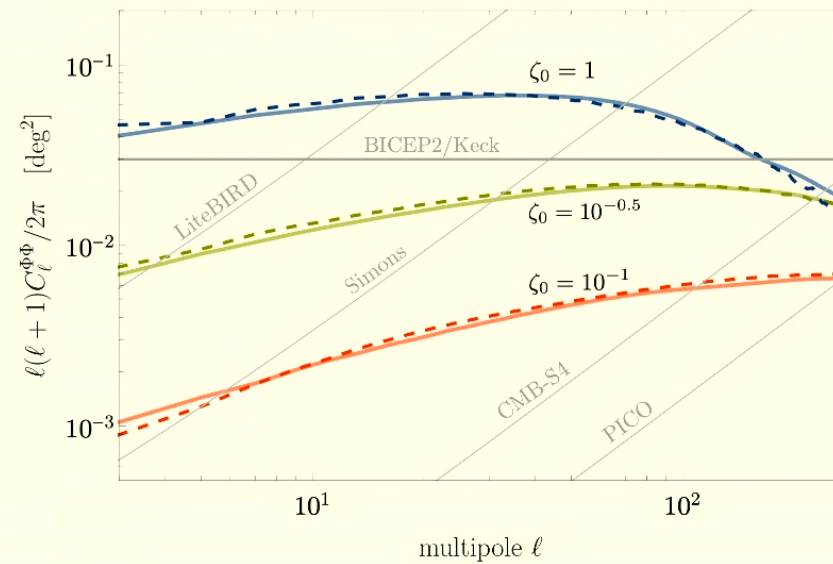
[Jain, AL, Amin, arXiv:2103.10962]

vary the loop radius: $R(t) = \zeta_0/H(t)$

correlation function



angular power spectrum



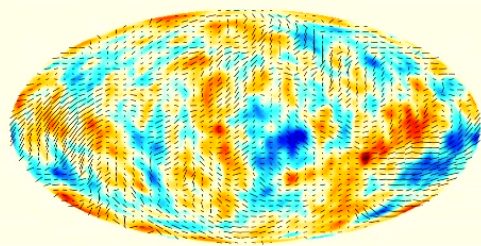
Effect on CMB polarization

How does birefringence affect the CMB's temperature and polarization?

$$T(\hat{n}) \rightarrow T(\hat{n})$$

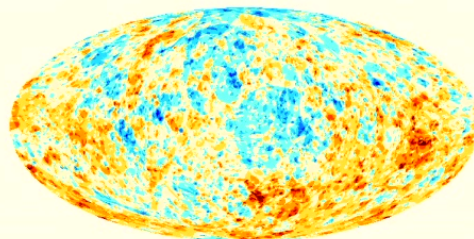
$$[Q \pm iU](\hat{n}) \rightarrow [(Q \pm iU)e^{\pm 2i\Delta\Phi}](\hat{n})$$

primordial CMB sky



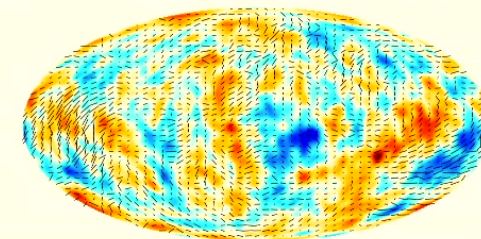
-160 160

axion string-induced birefringence angle



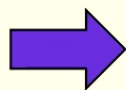
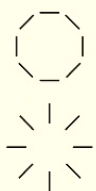
-60 60
α [deg]
(exaggerated by ~30x)

Planck's CMB sky

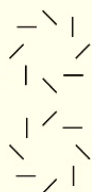


-160 160

E - mode
pol pattern



B - mode
pol pattern



Signal of axion string-induced cosmological birefringence

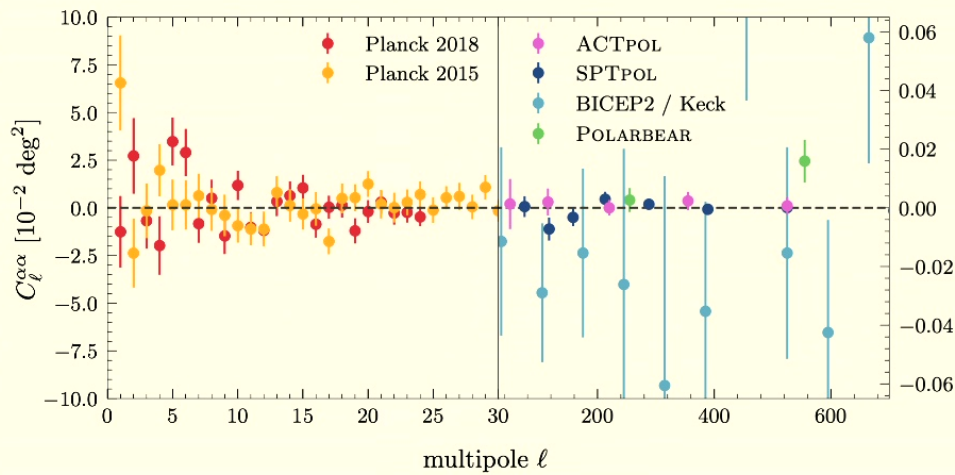
$$\begin{cases} \langle TB \rangle \neq 0 \\ \langle EB \rangle \neq 0 \end{cases}$$

$$C_\ell^{\text{EB}} \sim \sin(4\Delta\Phi)(C_\ell^{\text{EE}} - C_\ell^{\text{BB}})$$

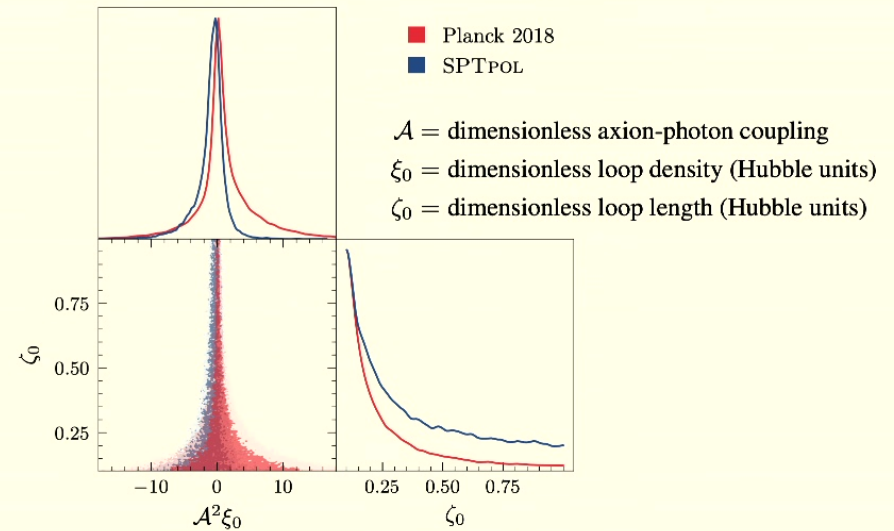
Constraints from anisotropic birefringence

[Jain, AL, Amin, arXiv:2103.10962]
 [Jain, Hagimoto, AL, Amin, arXiv:2208.08391]
 see also: Yin, Dai, & Ferraro (2021)

measurements of CMB polarization:
 no evidence for anisotropic birefringence



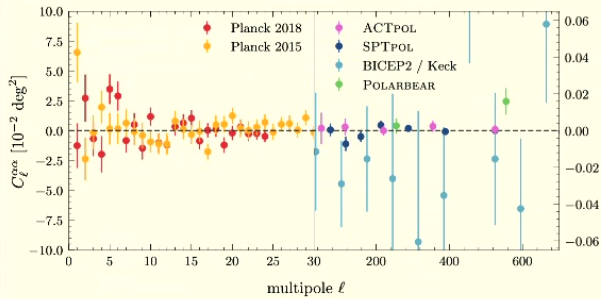
a constraint on axion strings networks
 & their coupling to electromagnetism:



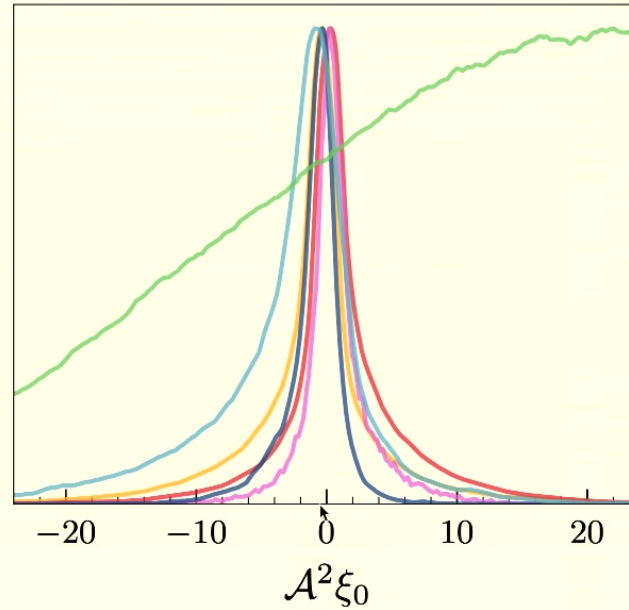
constraints:

$$\text{SPTPOL: } \mathcal{A}^2 \xi_0 < 3.7 \text{ at 95\% CL}$$

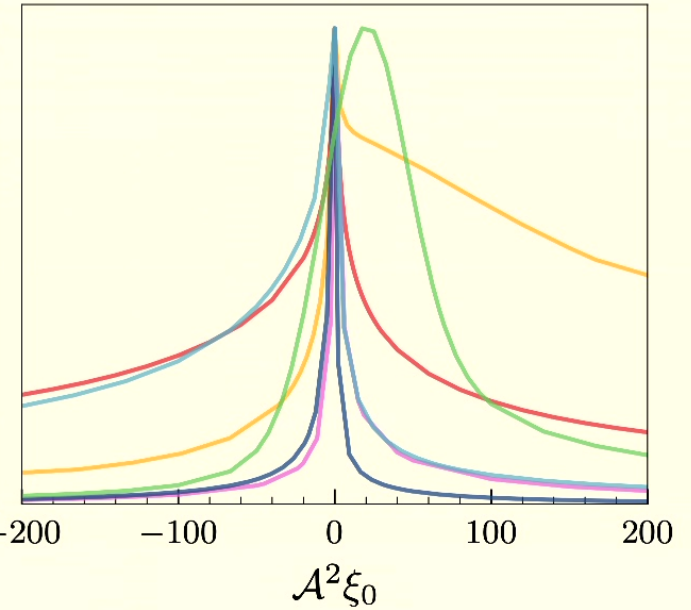
Constraints from anisotropic birefringence



stable string network



collapsing string-wall network



■ Planck 2015
 ■ Planck 2018
 ■ ACTPOL
 ■ SPTPOL
 ■ BICEP2 / Keck
 ■ POLARBEAR

Implications

CMB observations constrain:

$$\text{SPTPOL: } \mathcal{A}^2 \xi_0 < 3.7 \text{ at 95\% CL}$$

Typical axion-photon coupling:

$$\mathcal{A} = 1/3$$

Typical loop abundance:

$$\xi_0 = 30$$

The diagram consists of two arrows pointing downwards and inwards from the typical values to the resulting product. The arrow from $\mathcal{A} = 1/3$ points to the right, and the arrow from $\xi_0 = 30$ points to the left. They meet at the equation $\mathcal{A}^2 \xi_0 \approx 3.3$.

$$\mathcal{A}^2 \xi_0 \approx 3.3$$

... already probing an $O(1)$ anomaly coefficient!
... but still large uncertainties in ξ_0 (from sims)

Projected sensitivity

Pogosian et. al. (2019)

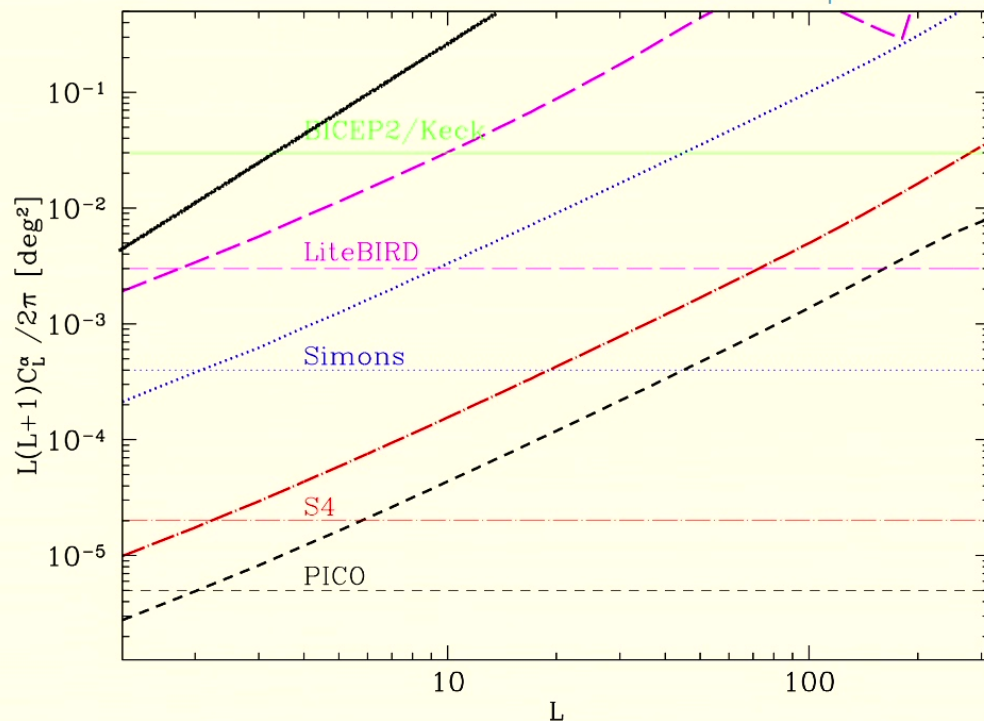
future telescopes
probes of isotropic + aniso. birefringence

Current			LiteBIRD			SO			CMB-S4-like			PICO		
α	A_α	$\sqrt{\frac{C_\alpha^\alpha}{4\pi}}$	α	A_α	$\sqrt{\frac{C_\alpha^\alpha}{4\pi}}$	α	A_α	$\sqrt{\frac{C_\alpha^\alpha}{4\pi}}$	α	A_α	$\sqrt{\frac{C_\alpha^\alpha}{4\pi}}$	α	A_α	$\sqrt{\frac{C_\alpha^\alpha}{4\pi}}$
-	10^{-2}deg^2	-	-	10^{-3}deg^2	-	-	10^{-4}deg^2	-	-	10^{-5}deg^2	-	-	10^{-5}deg^2	-
-	-	-	1.3	2.7	0.9	0.56	3	0.29	0.1	1.4	0.065	0.05	0.4	0.035
-	-	-	1.5	3.3	1.0	0.66	4	0.35	0.11	2.0	0.08	0.06	0.5	0.04
-	-	-	1.4	3.5	1.0	0.64	5.0	0.4	0.13	2.5	0.09	0.08	1.2	0.06
30	2	3	1.6	4.0	1.1	0.71	5.5	0.4	0.15	3.3	0.1	0.09	1.4	0.065

BLE II. Current and forecasted 68% CL bounds on the uniform and the anisotropic CPR parameters.

$$A_\alpha = L(L+1)C_L^\alpha / 2\pi$$

diagonal = allows multipoles to vary independently
horizontal = restricts to a scale invariant spectrum



what about
isotropic
birefringence

Are strings responsible for isotropic birefringence?

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

reported detection of isotropic birefringence:

same rotation angle across the whole sky
(using *Planck* & *WMAP* data)

$$\alpha_{00} = -1.21^{\circ} {}^{+0.33^{\circ}}_{-0.32^{\circ}} \text{ (68\% CL)}$$

[Minami & Komatsu (2020)]

[Diego-Palazuelos et. al. (2022)]

[Eskilt (2022)], [Eskilt & Komatsu (2022)]

[Eskilt et. al. (2023)]

note that: $\beta = -\alpha_{00}/\sqrt{4\pi} \approx 0.34^{\circ}$

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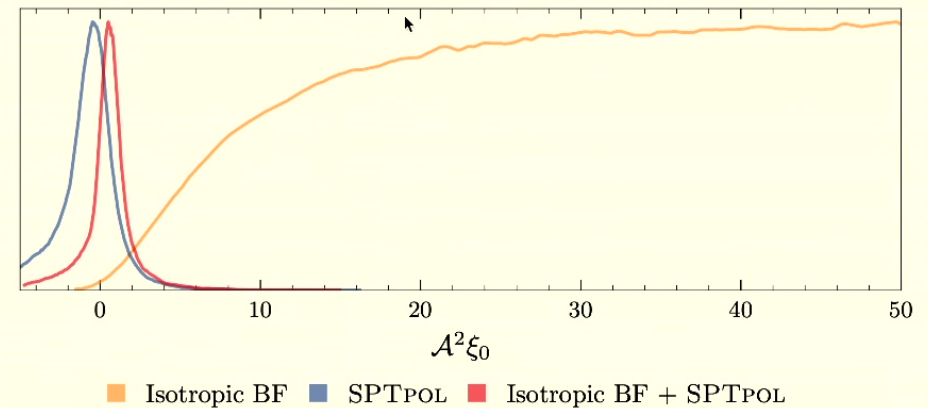
[Minami & Komatsu (2020)]

[Diego-Palazuelos et. al. (2022)]

[Eskilt (2022)], [Eskilt & Komatsu (2022)]

[Eskilt et. al. (2023)]

our conclusion: the isotropic signal is in tension
with limits on anisotropic BF if they both arise
from axion-string induced birefringence



note that: $\beta = -\alpha_{00}/\sqrt{4\pi} \approx 0.34^{\circ}$

Are strings responsible for isotropic birefringence?

[Ferreira, Gasparotto, Hiramatsu, Obata, & Pujolas (2023)]

reported detection of isotropic birefringence:
same rotation angle across the whole sky
(using *Planck* & *WMAP* data)

$$\alpha_{00} = -1.21^{\circ} {}^{+0.33^{\circ}}_{-0.32^{\circ}} \text{ (68\% CL)}$$

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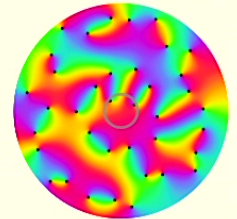
note that: $\beta = -\alpha_{00}/\sqrt{4\pi} \approx 0.34^{\circ}$

loopholes allowing large iso-BF

(1) environmental effects
a nearby loop in our Hubble volume
would dominate the isotropic signal

(2) Hubble-scale gradients
the massless axion field is expected to be
inhomogeneous on the Hubble scale

(3) late-forming network
if the string network is not present just after
recombination, the small-scale BF is suppressed



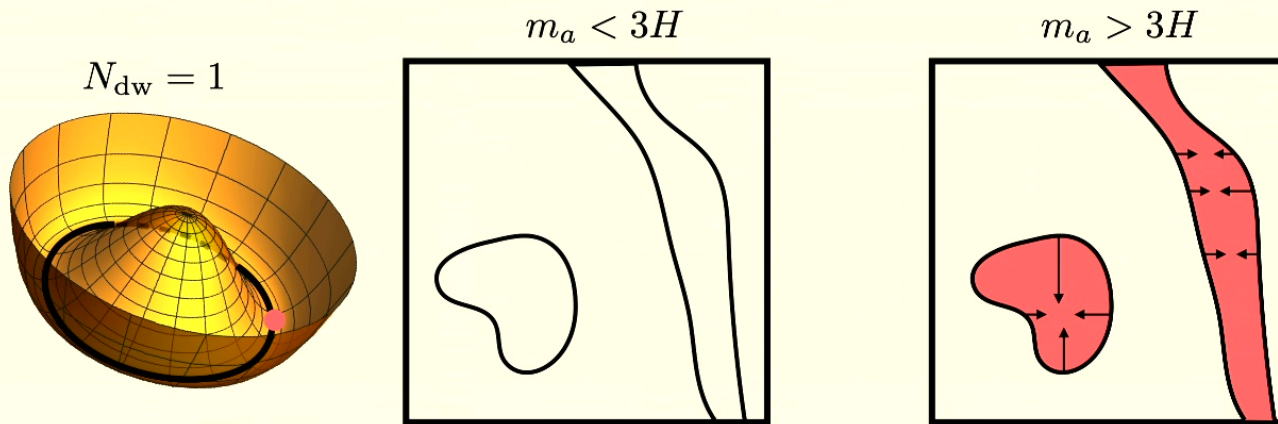
effect of varying ALP mass

Collapse of the string-wall network

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

Axion strings become connected together by domain walls

... the string-wall network collapses (for $N_{\text{dw}} = 1$)



let's consider: $\begin{cases} m_a \lesssim 3H_{\text{CMB}} \simeq 3 \times 10^{-29} \text{ eV} & \text{(string network survives until after recombination)} \\ m_a \gtrsim 3H_0 \simeq 5 \times 10^{-33} \text{ eV} & \text{(string network collapses before today)} \end{cases}$

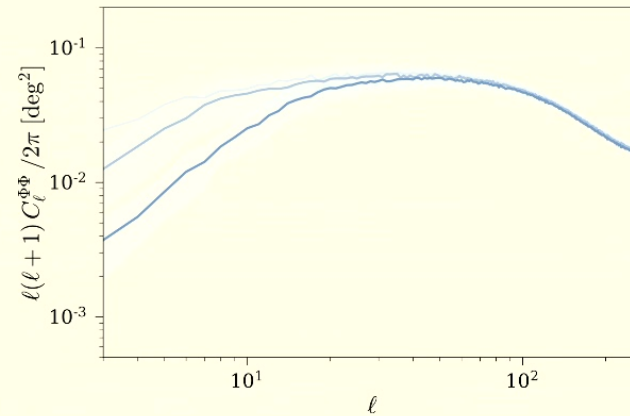
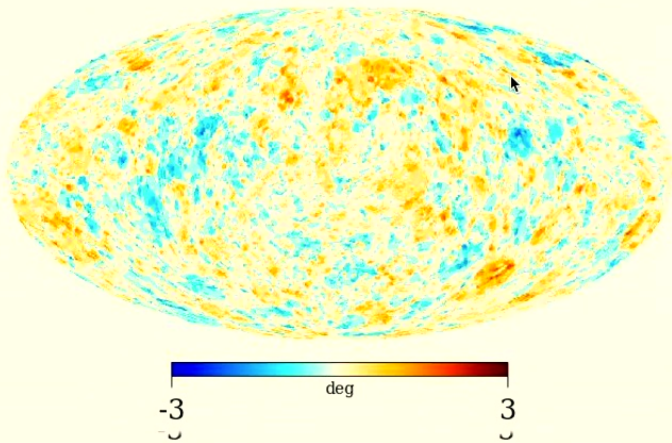
Impact on birefringence

(assuming $N_{\text{DW}} = 1$)

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

raise the ALP mass
(network collapses earlier)

$$m_a = 2 \times 10^{-31} \text{ eV} \quad (z_c = 19)$$



after the network collapses at redshift z_c the accumulation of birefringence is shut off

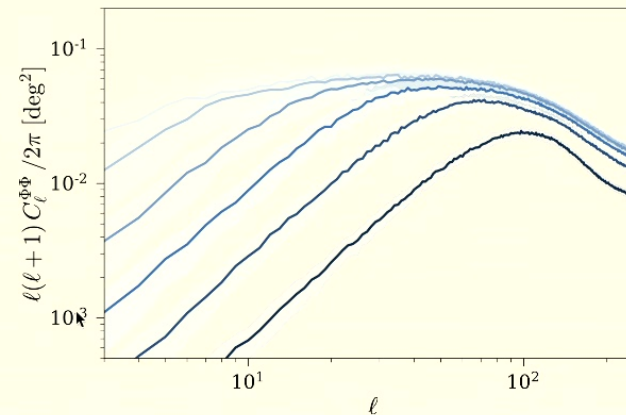
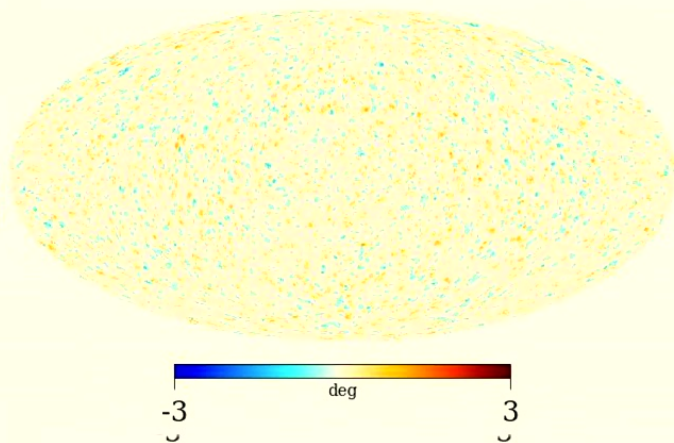
Impact on birefringence

(assuming $N_{\text{DW}} = 1$)

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

raise the ALP mass
(network collapses earlier)

$$m_a = 2 \times 10^{-29} \text{ eV} \quad (z_c = 404)$$



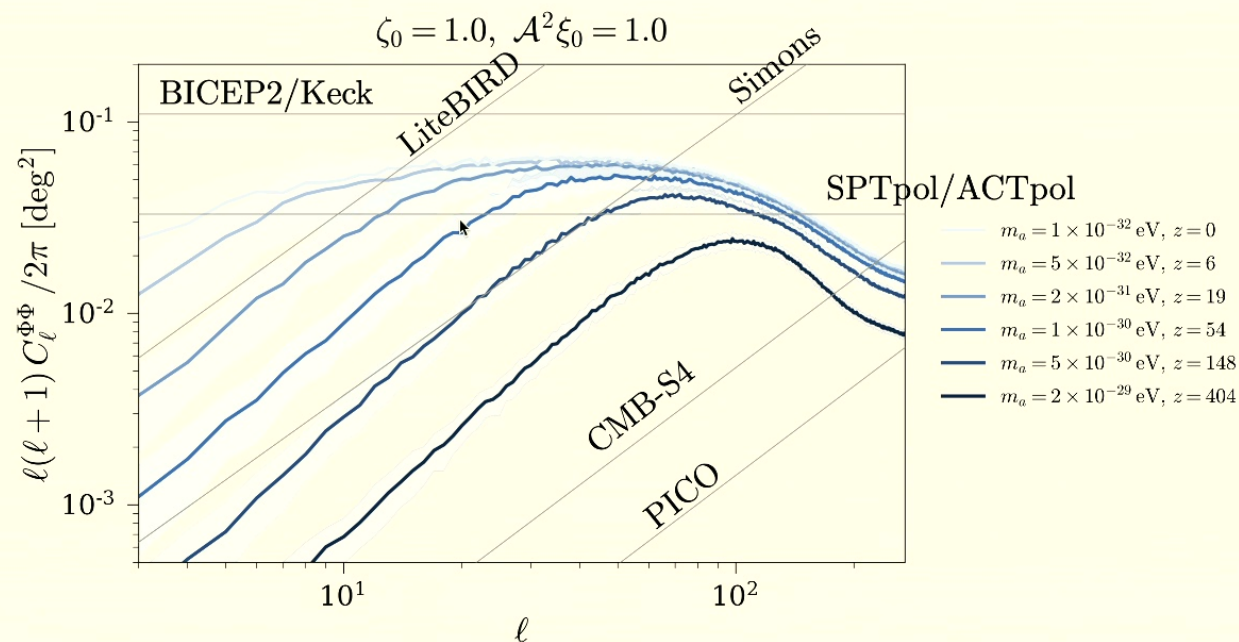
after the network collapses at redshift z_c the accumulation of birefringence is shut off

Implications

(assuming $N_{\text{DW}} = 1$)

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

raise the ALP mass
(network collapses earlier)



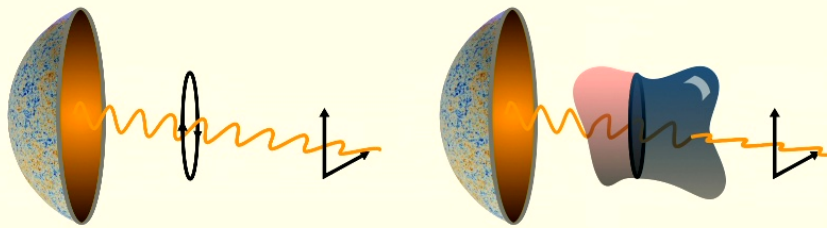
strong scale dependence \rightarrow possible to measure m_a

Similar results for stable string-wall networks

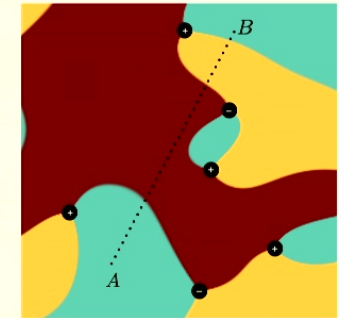
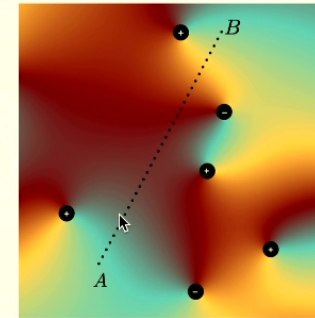
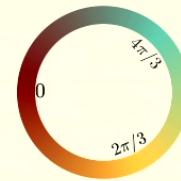
[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

(assuming $N_{\text{DW}} > 1$)

birefringence
due to string versus string-wall

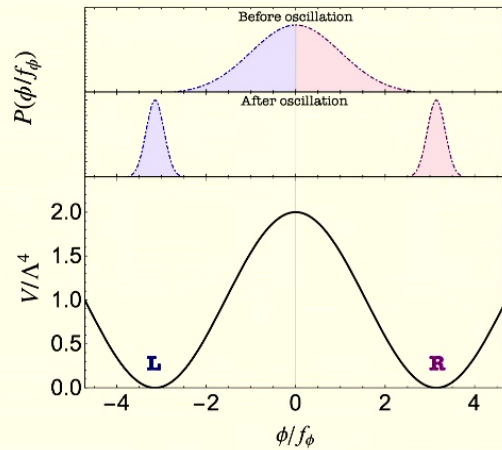


birefringence builds up across many defects
similar behavior to string network



Complementary studies: stable axion domain walls

domain walls without strings
expected if $H_{\text{inf}} \sim f_a$



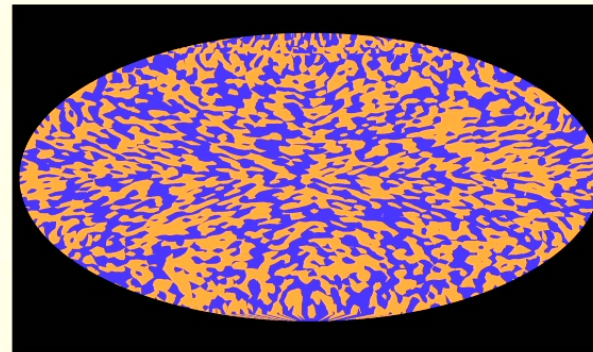
possible to evade DW problem
imposes bound on mass & decay constant

$$\sigma_{\text{DW}} \simeq 8f_\phi^2 m_\phi \lesssim (1 \text{ MeV})^3,$$

$$f_\phi \lesssim 4 \times 10^9 \text{ GeV} \sqrt{\frac{10^{-20} \text{ eV}}{m_\phi}}.$$

[Takahashi & Yin (2020)]
[Nakagawa, Takahashi, & Yamada (2021)]
[Kitajima, Kozai, Takahashi, & Yin (2022)]
[Gonzalez, Kitajima, Takahashi, & Yin (2022)]

birefringence signal
independent of propagation



$$\Delta\Phi = 0 \quad \text{if LS}\gamma \text{ is from the vacuum } R$$

$$\Delta\Phi = c_\gamma \alpha \quad \text{if LS}\gamma \text{ is from the vacuum } L.$$

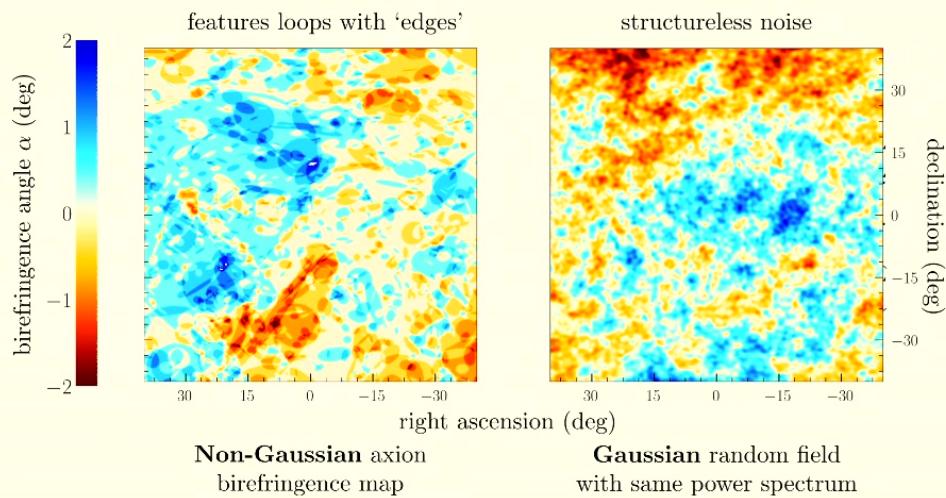
**possible to accommodate detection of
isotropic BF and evade limits on anisotropic BF
(no random-walk enhancement)**

signatures of non-Gaussianity

non-Gaussianity in birefringence maps

[Hagimoto & AL, arXiv:2306.07351]
see also: Yin, Dai, Ferraro (2305.02318)

axion-string induced birefringence:
loop-like features are visibly non-Gaussian

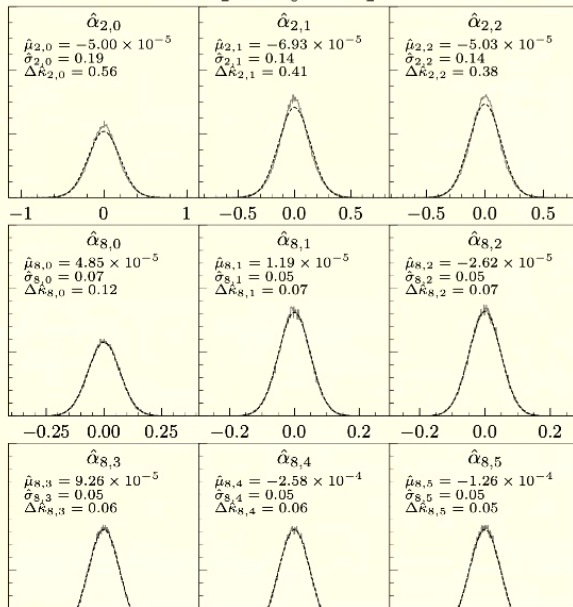
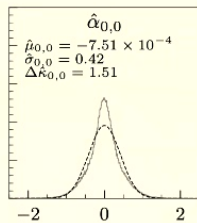


How to best quantify the non-Gaussian birefringence and develop tests to extract these features from the data?

Measures of NG 1: kurtosis

[Hagimoto & AL, arXiv:2306.07351]

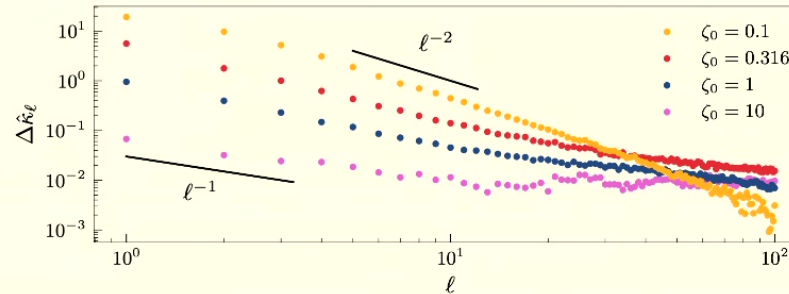
distribution over $\hat{a}_{\ell m}$'s
less Gaussian at lower ℓ



kurtosis
a measure of Gaussianity

$$\kappa_{\ell m} = \frac{\langle |\hat{a}_{\ell m} - \langle \hat{a}_{\ell m} \rangle|^4 \rangle}{\langle |\hat{a}_{\ell m} - \langle \hat{a}_{\ell m} \rangle|^2 \rangle^2} = 3 \text{ for Gaussian}$$

scaling with multipole index
more Gaussian on smaller scales



analytical model
~ inverse with # loops

$$\Delta\hat{\kappa}_\ell \sim \frac{\zeta_0}{8\xi_0} \left(1 + \frac{\pi}{\lambda\zeta_0\ell} \right)^2$$

recall: $R(t) = \zeta_0/H(t)$

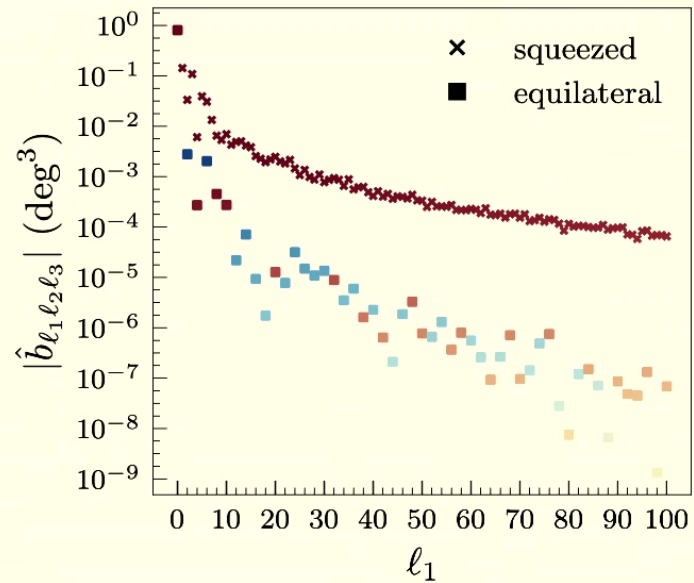
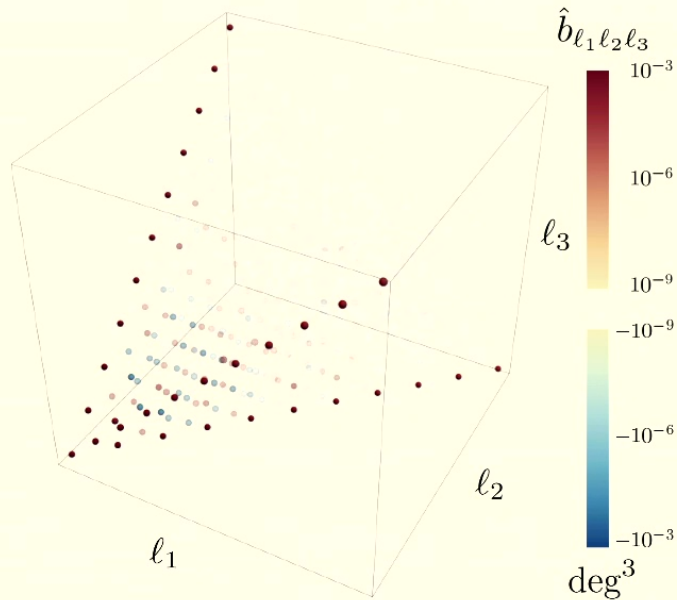
Measures of NG 2: bispectrum

[Hagimoto & AL, arXiv:2306.07351]

bispectrum
3-point correlations

$$\hat{b}_{\ell_1 \ell_2 \ell_3} = h_{\ell_1 \ell_2 \ell_3}^{-1} \sum_{m_1=-\ell_1}^{\ell_1} \sum_{m_2=-\ell_2}^{\ell_2} \sum_{m_3=-\ell_3}^{\ell_3} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ m_1 & m_2 & m_3 \end{pmatrix} \hat{\alpha}_{\ell_1 m_1} \hat{\alpha}_{\ell_2 m_2} \hat{\alpha}_{\ell_3 m_3}$$

single realization
largest in squeezed triangle form



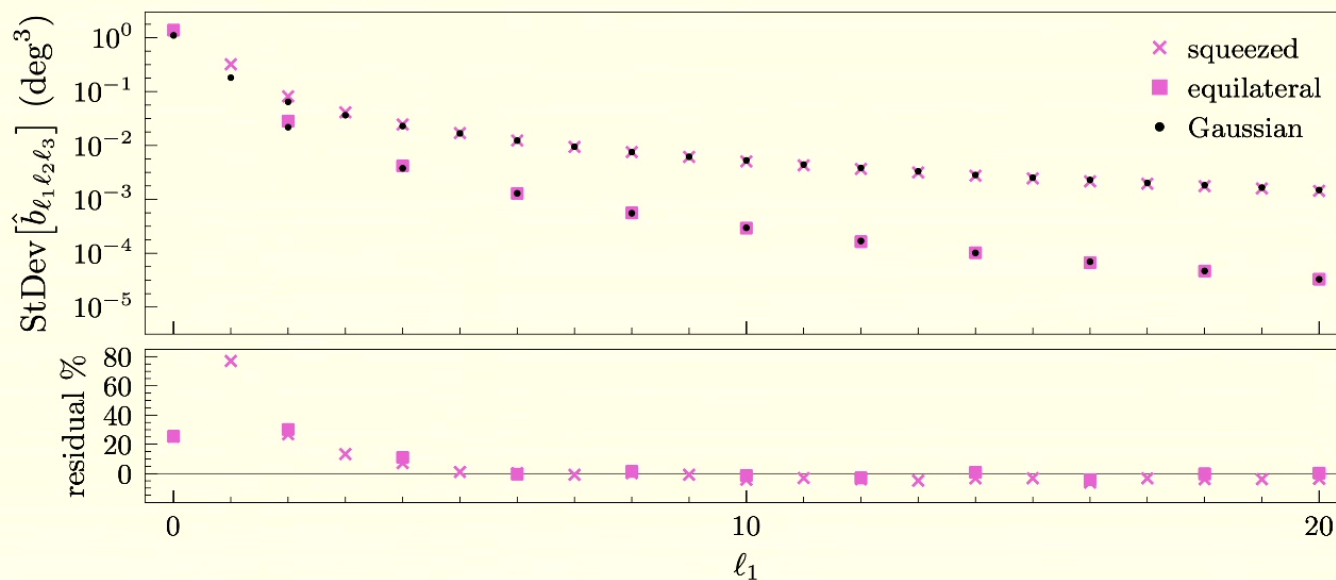
Measures of NG 2: bispectrum

[Hagimoto & AL, arXiv:2306.07351]

bispectrum
3-point correlations

$$\hat{b}_{\ell_1 \ell_2 \ell_3} = h_{\ell_1 \ell_2 \ell_3}^{-1} \sum_{m_1=-\ell_1}^{\ell_1} \sum_{m_2=-\ell_2}^{\ell_2} \sum_{m_3=-\ell_3}^{\ell_3} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ m_1 & m_2 & m_3 \end{pmatrix} \hat{\alpha}_{\ell_1 m_1} \hat{\alpha}_{\ell_2 m_2} \hat{\alpha}_{\ell_3 m_3}$$

average bispectrum
and comparison with Gaussian random field



Measures of NG 3: scattering transform

Yin, Dai, Ferraro (2023)

std. method
power spectrum

signal: $I_0(\mathbf{x})$

plane wave: $\phi_{\mathbf{k}}(\mathbf{x})$

$$P_{\mathbf{k}}(\mathbf{x}) = \langle |I_0 * \phi_{\mathbf{k}}|^2 \rangle(\mathbf{x})$$

new method
scattering transform

wavelet: $\psi^{j,l}(\mathbf{x})$

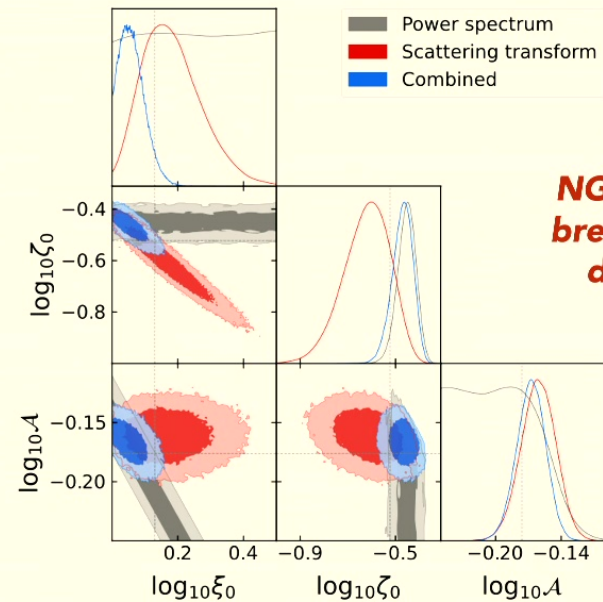
$$I_1^{j,l}(\mathbf{x}) = \langle |I_0 * \psi^{j,l}|^2 \rangle(\mathbf{x})$$

$$I_2^{j_1,l_1,j_2,l_2}(\mathbf{x}) = \langle |I_1^{j_1,l_1} * \psi^{j_2,l_2}|^2 \rangle(\mathbf{x})$$

$$s_1^j = \langle I_1^{j,l} \rangle_{\mathbf{x},l}$$

$$s_2^{j_1,j_2} = \langle I_2^{j_1,l_1,j_2,l_2} \rangle_{\mathbf{x},l_1,l_2}$$

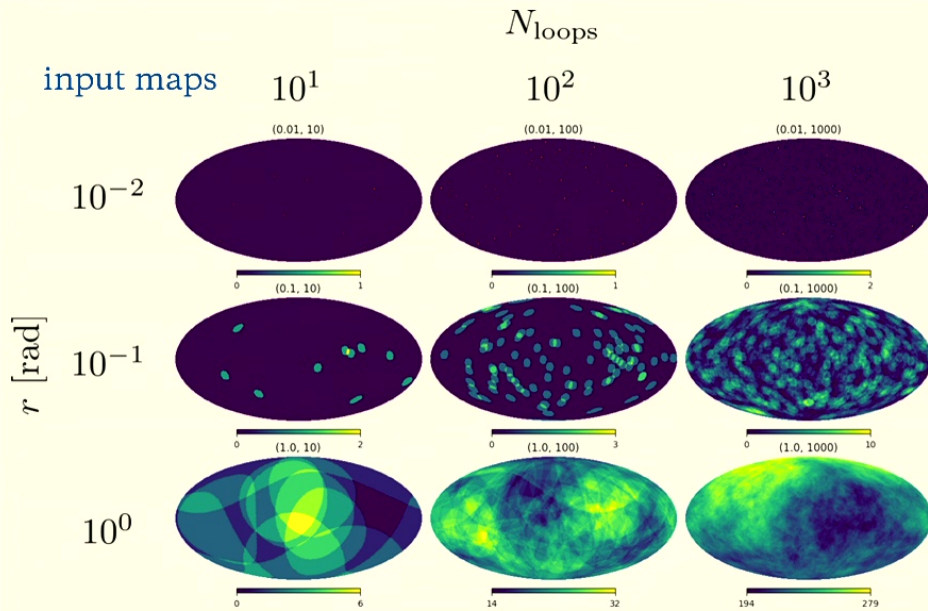
comparison
pow-spec vs. scatt-transform



(b) $\mathcal{A}^2 \xi_0 = 0.6$, $\mathcal{A} = 2/3$, $\zeta_0 = 0.3$

Machine learning for axion strings

--- early stages ---

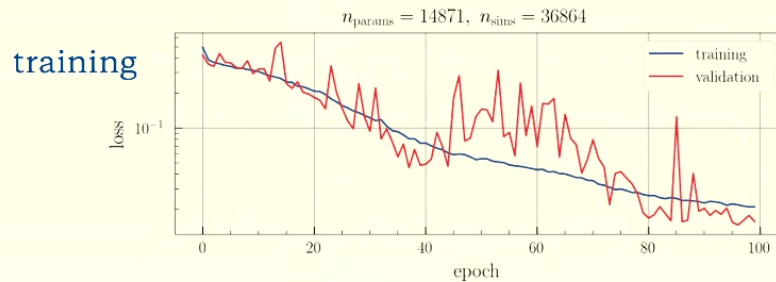


package: DeepSphere (Python)
architecture: 3 conv+pool layers

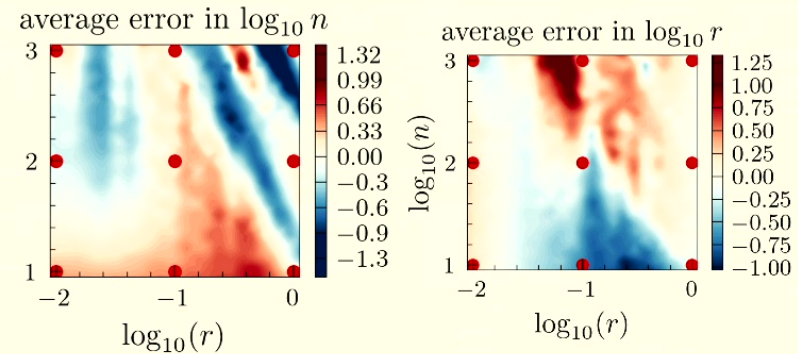
goal: to train an AI to identify features of axion strings in CMB polarization maps



Ray Hagimoto
(Rice U grad)



how well is it working? ... not bad!



summary & conclusion

Summary

- If a **hyper-light axion-like particle** exists in Nature, the associated cosmological **network of axion strings** can leave an imprint on **CMB polarization** through birefringence
- We use existing **measurements of anisotropic birefringence** (Planck, SPT, ...) to place constraints on this scenario. Next-generation telescopes (CMB-S4) will probe $O(1)$ electromagnetic anomaly coefficients and thereby probe the axion's UV embedding
- We find that it is difficult (but not impossible!) to reconcile the **detection of isotropic birefringence** with strong limits on anisotropic birefringence coming from axion strings
- We argue that measurements of anisotropic birefringence could not only reveal the presence of a hyper-light ALP in Nature, but also lead to a **measurement of its mass**
- Our ongoing work (very early stages) seeks to use machine learning techniques (spherical CNN) to detect the subtle signal of axion strings in CMB polarization data