

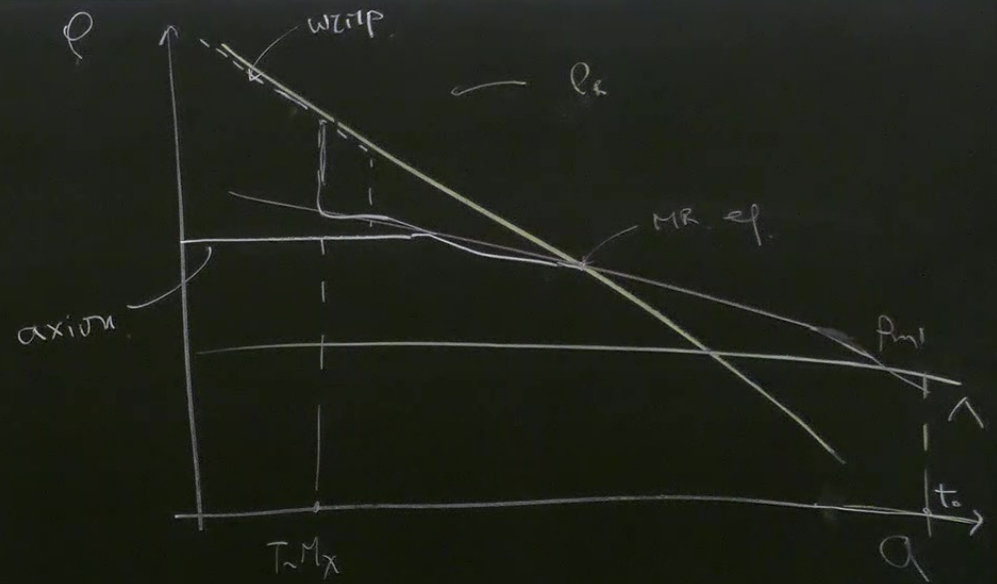
Title: Particle Physics Lecture

Speakers: Junwu Huang

Collection: Particle Physics

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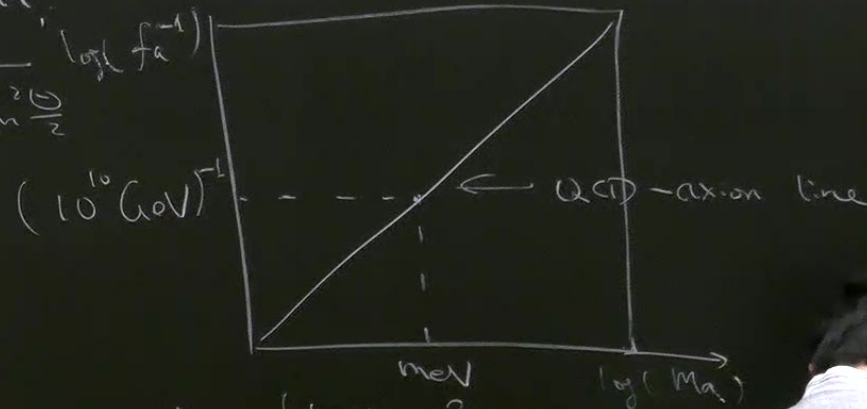
Lecture 11. Axions & Misalignment

$$E(\theta) = -m_\pi^2 f_\pi^2 \sqrt{\cos^2 \frac{\theta}{2} - \left(\frac{m_u - m_d}{m_u + m_d}\right)^2 \sin^2 \frac{\theta}{2}}$$

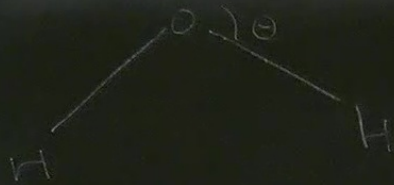
$\theta = 0$ Minimum

$$\theta \rightarrow \frac{a}{f_a} \quad \theta \rightarrow \theta + 2\pi \quad a \rightarrow a + 2\pi f_a$$

$$E''(a) = \frac{1}{f_a^2} \left(\frac{m_u m_d}{(m_u + m_d)^2} \right) m_\pi^2 f_\pi^2 = m_a^2$$



$$M_a \sim \frac{(100 \text{ MeV})^2}{10^{10} \text{ GeV}} \sim 10^{-12} \text{ GeV}$$



1. Minimum at the right \odot

2. Dynamical variable. Know its dynamics

$$\ddot{\theta} + \gamma \dot{\theta} + \omega_0^2 (\theta - \theta_{min}) = 0$$

Axion $\square a + m_a^2 a = 0$

$$\Rightarrow \ddot{a} + H \dot{a} + m_a^2 a = \text{radiation}$$

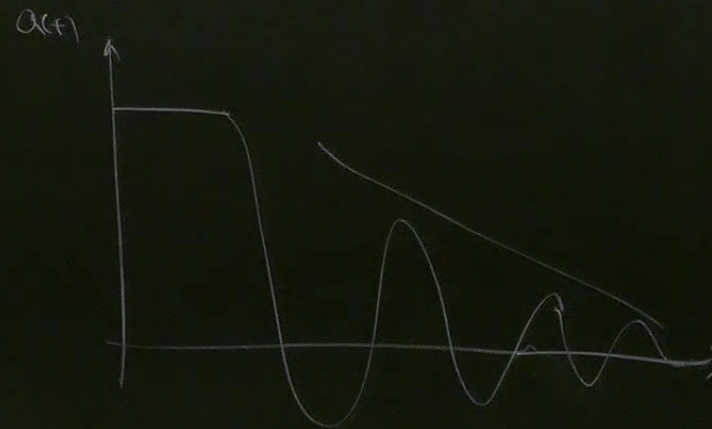
$$\ddot{\theta} + \gamma \dot{\theta} + \omega_0^2 (\theta - \theta_{min}) = 0$$

Axiom $\square a + m_a^2 a = 0$

$$\Rightarrow \ddot{a} + 3H \dot{a} + m_a^2 a = 0$$

in radiation domination $H = \frac{1}{2t}$

- $H > m_a$ $\underline{a \sim \text{constant}}$
- $H \sim m_a$
- $m_a \gg H$



$$\ddot{\theta} + \gamma \dot{\theta} + \omega_0^2 (\theta - \theta_{min}) = 0$$

pa

Axion $\square a + m_a^2 a = 0$

$$\Rightarrow \ddot{a} + 3H\dot{a} + m_a^2 a = 0$$

in radiation domination $H = \frac{1}{2t}$

axion dynamics

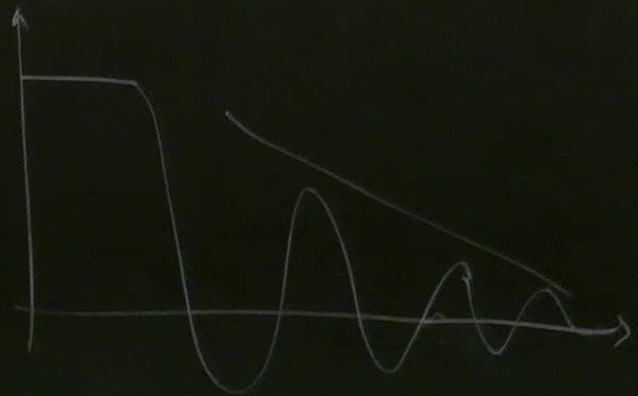
$$H > m_a$$

$$a \sim \text{constant}$$

$$H \sim m_a$$

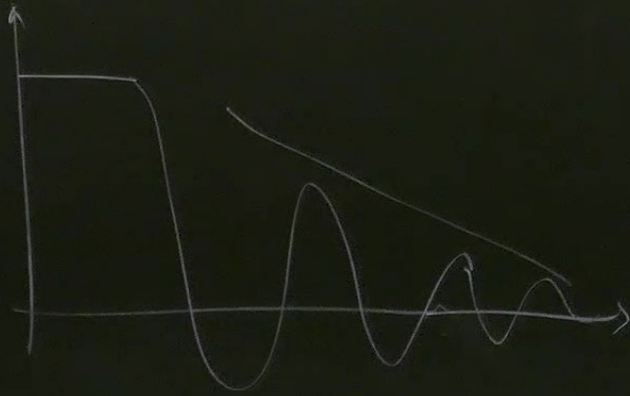
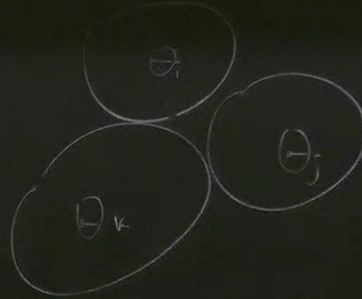
$$m_a \gg H$$

$a(t)$



$$L \propto \left(\frac{a}{r} \right)^2 \frac{1}{1 - \frac{2M}{r}} \left(\frac{a}{r} \right)$$

radiation domination $H = \frac{1}{2t}$



$ma \gg H$

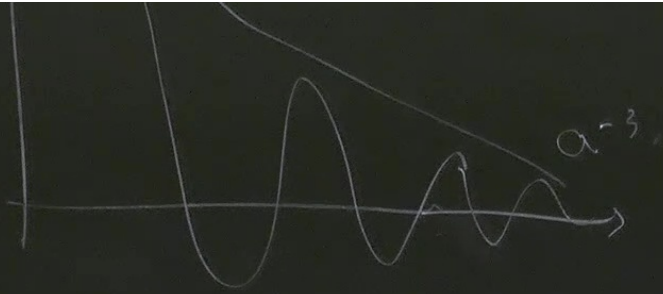
$$\phi(t) \propto \exp(-\Gamma(t) dt) \cos mat$$

1) $O(m_a^2)$ $\ddot{\phi} \rightarrow -m_a^2 \cos mat$

2) $O(ma \frac{d}{dt}, maH)$ $\ddot{\phi} \rightarrow 2\Gamma(t) \sin mat \cdot ma$

$\dot{\phi} \rightarrow -3H(t) \sin mat \cdot ma = 0$

$$\Rightarrow \Gamma = \frac{3}{2}H \Rightarrow \int \Gamma dt = \int \frac{3}{2} \frac{da}{a}$$



$$\phi(t) = \left(\frac{a(H=m_a)}{a(t)} \right)^{3/2} \phi_0 \cos m_a t$$

$$\begin{aligned} \rho_\phi &= (\partial_t \phi)^2 + m_a^2 \phi^2 \\ &= \left(\frac{a(H=m_a)}{a(t)} \right)^3 \cdot \frac{\rho_0}{m_a^2 \phi_0^2} \end{aligned}$$

This behavior is DM.

What is the density?

$$\phi \rightarrow \phi + 2\pi f a$$



$$\frac{[\theta_i - \theta_{\min}]}{2\pi} \sim 1 = \bar{\theta}_i$$

Initial condition persist until $\frac{m_a H}{m_p}$

$$\rho_p = m_a^2 f a^2 \bar{\theta}_i^2 \quad \text{vs} \quad \rho_H = m_a f a^2 \bar{\theta}_i^2 \cdot \left(\frac{T_{(+)}}{T_{(H=m_a)}} \right)^3$$

$\rho_H = \rho_p$ @ MR equality.

$$\frac{\rho_p}{\rho_H} \Big|_{T=T_{\text{eq}}} = \frac{(M_p)^{-1} m_p}{(m_p)^{-1} T_{\text{eq}}} = \frac{M_a^{1/2} f a^2 \bar{\theta}_i^2}{m_p^{1/2} T_{\text{eq}}} \sim 1$$

Lecture 11. Axions & Misalignment

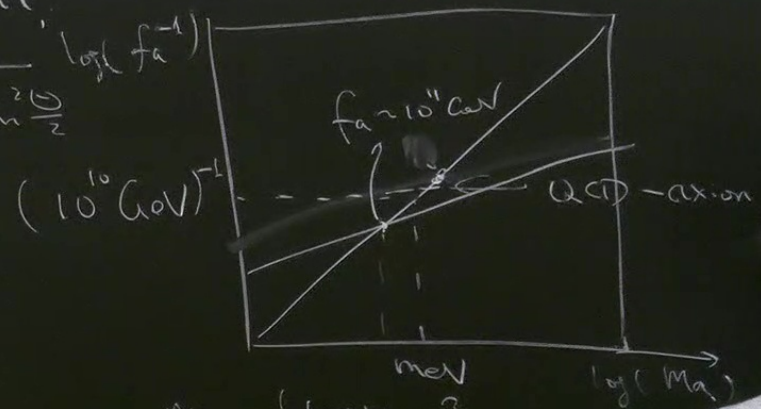
$$E(\theta) = -m_\pi^2 f_\pi^2 \sqrt{\cos^2 \frac{\theta}{2} - \left(\frac{m_u - m_d}{m_u + m_d}\right)^2 \sin^2 \frac{\theta}{2}}$$

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$$E''(a) = \frac{1}{f_a^2} \left(\frac{m_u m_d}{(m_u + m_d)^2} \right) m_\pi^2 f_\pi^2 = M_a^2$$

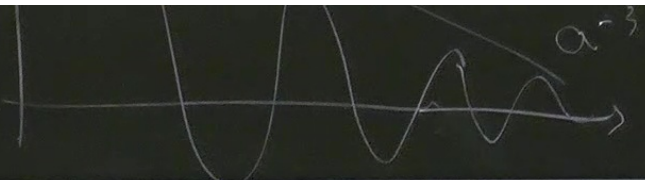
$M_a \gg H$



$$M_a \sim \frac{(100 \text{ MeV})^2}{10^{10} \text{ GeV}} \sim 10^{-12} \text{ GeV}$$

① $m_a f_a = \left(\frac{m_u m_d}{(m_u + m_d)^2} \right)^{1/2}$

② $M_a^{1/2} f_a^2 \approx M_{\text{pl}}^{3/2} T_{\text{eff}}$

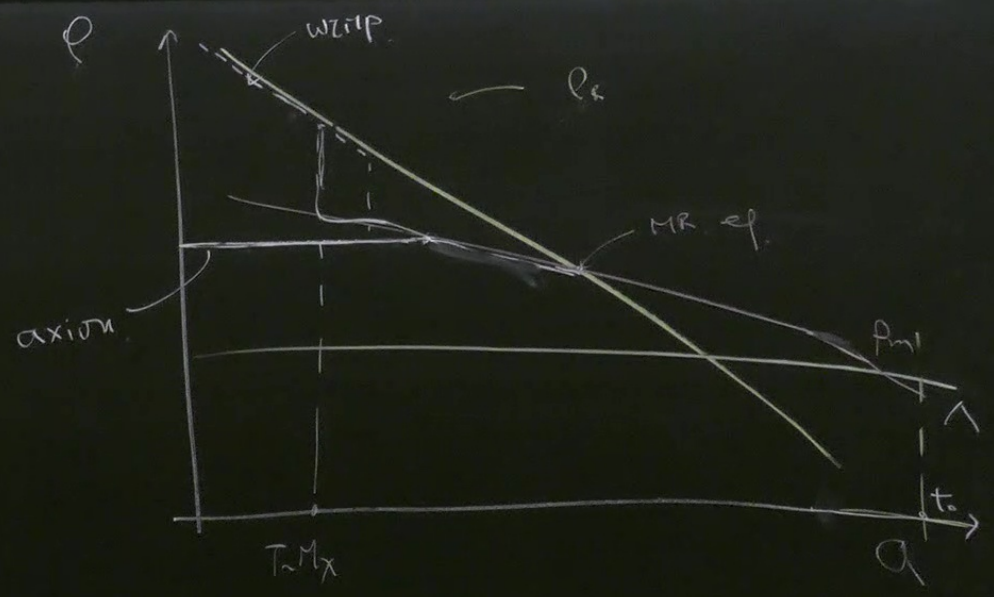


Axion DM.

$$\begin{cases} m_a \sim 100 \mu\text{eV} \\ f_a \sim 10^{16} \text{ GeV} \end{cases}$$

$$100 \text{ MeV} \sim \frac{1}{\text{fm}}$$

$$\lambda_a \sim \text{mm}$$



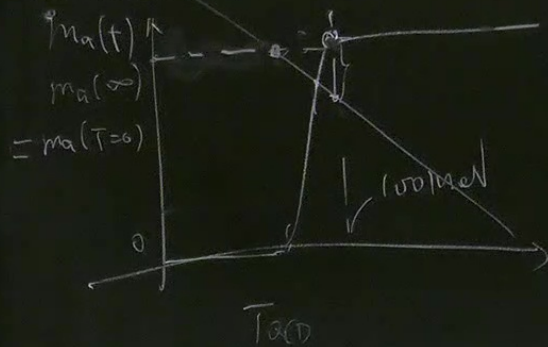
In reality m_a is not a constant
if it is from QCD.

$$m_a \sim \frac{T_{\text{QCD}}^2}{f_a} \sim \frac{m_{\pi}^2}{f_a}$$

$$H = \frac{T_{\text{QCD}}^2}{M_{\text{pl}}}$$

$$T_{\text{universe}} > \Lambda_{\text{QCD}}$$

QCD axion, precisely.



$\rho \sim 1/T = \rho_{eff}$ $\rho_{eff} \sim 1/T_{eff}$ $\rho \sim 1/T$

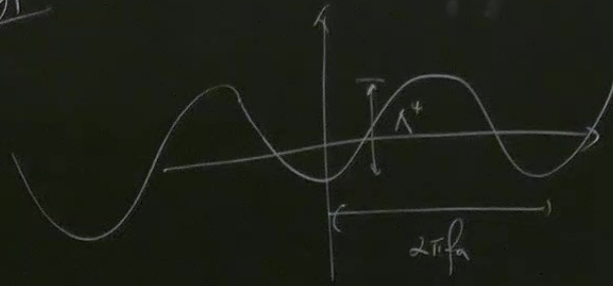
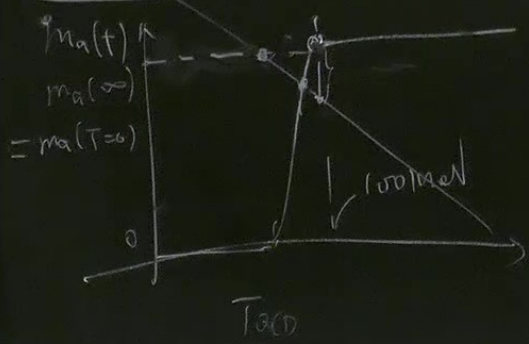
In reality m_a is not a constant.
if it is from QCD.

$T_{universe} > \Lambda_{QCD}$
QCD axion, precisely.

$$m_a \sim \frac{T_{QCD}}{f_a} \sim \frac{m_{\pi} f_{\pi}}{f_a}$$

$$H = \frac{T_{QCD}}{M_{pl}}$$

$$\begin{aligned} \Lambda^4(h) &= m_{\pi}^2 f_{\pi}^2 - \overbrace{G_N}^{60 \text{ MeV}} \rho \\ &= (100 \text{ MeV})^4 - (60 \text{ MeV}) \cdot \frac{\rho}{G_N} \\ &= (100 \text{ MeV})^4 - 0.06 \cdot \rho \end{aligned}$$



$\rho =$ {
 earch. $\rightarrow R = \left[\frac{1}{2 m_e} \right]$
 sum

$\frac{m_{\pi} c^2}{f_a}$

$$\Lambda^4(h) = m_{\pi}^4 f_a^2 - \overset{60 \text{ MeV}}{G_N} \rho$$

$$= (100 \text{ MeV})^4 - (60 \text{ MeV}) \cdot \frac{\rho}{G_N}$$

$$= (100 \text{ MeV})^4 - 0.06 \cdot \rho$$

$\rho =$

eared. $\rightarrow R = \frac{1}{\alpha m_{\pi}} \sim \frac{1}{\text{keV}}$ nm

$\rho \sim (\text{keV})^3 \cdot G_N \cdot \text{nm}$

$\rho \sim (\text{keV})^3$

$\rho \sim (\text{keV})^3 \cdot G_N \cdot \text{nm}$

$(100 \text{ MeV})^4$

50 MeV

n

$$-(60 \text{ MeV}) \cdot \frac{\rho}{G_0 N}$$

$$= 0.06 \cdot \rho$$

$$R = \left[\frac{1}{\alpha m_e} \right] \sim \left(\frac{1}{\text{keV}} \right) \sim \text{nm}$$

earth

sun

NS

$$R \sim \frac{1}{m_\pi} \Rightarrow n \sim m_\pi^3$$

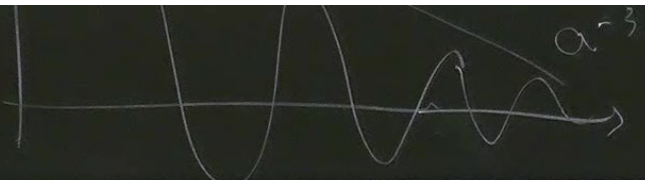
$$\rho = (60 \text{ MeV}) \cdot m_\pi^3$$

$$n \sim (\text{keV})^3$$

$$\rho \sim (\text{keV})^3 \cdot G_0 N$$

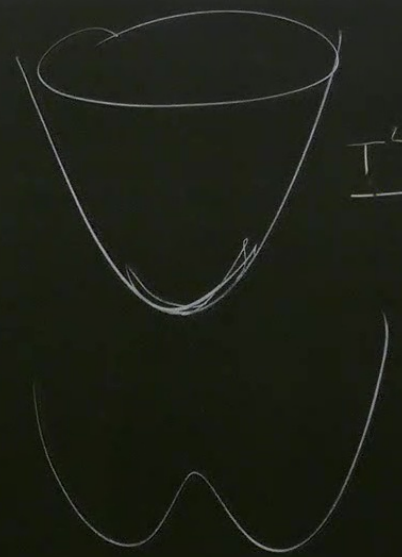
$$(100 \text{ MeV})^4 = \frac{(\text{keV})^3 \cdot 0.05 \times G_0 N}{10^8 \cdot 10^9 \cdot 50}$$





Axion DM:
 $m_a \sim 100 \mu\text{eV}$
 $f_a \sim 10^{16} \text{GeV}$

$100 \text{ MeV} \sim \frac{1}{f_m}$
 $\lambda_a \sim \text{mm}$



$T^2 \phi^2$

