

Title: Kinetic decoupling and the matter distribution at high redshift

Speakers: Benjamin Lehmann

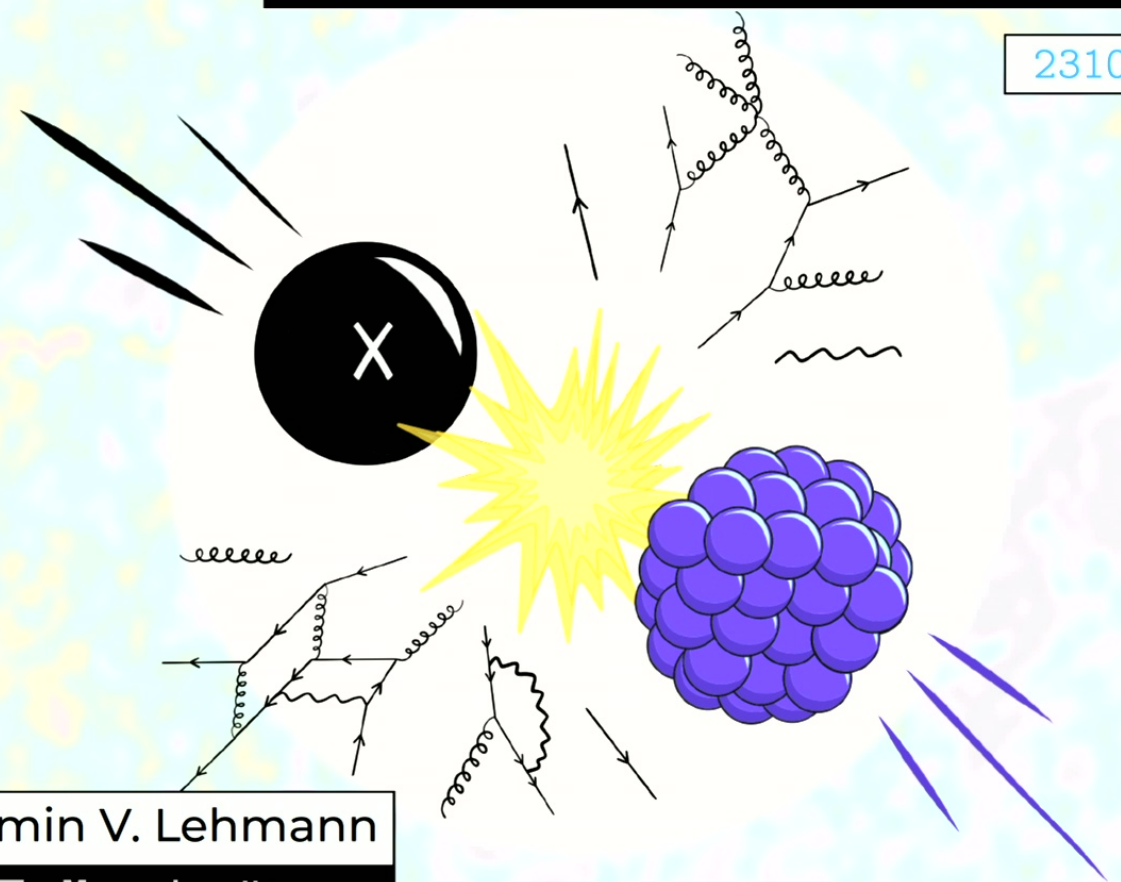
Collection: Dark Matter, First Light

Date: February 28, 2024 - 11:00 AM

URL: <https://pirsa.org/24020083>

Kinetic recoupling of dark matter


2310.20513



Benjamin V. Lehmann



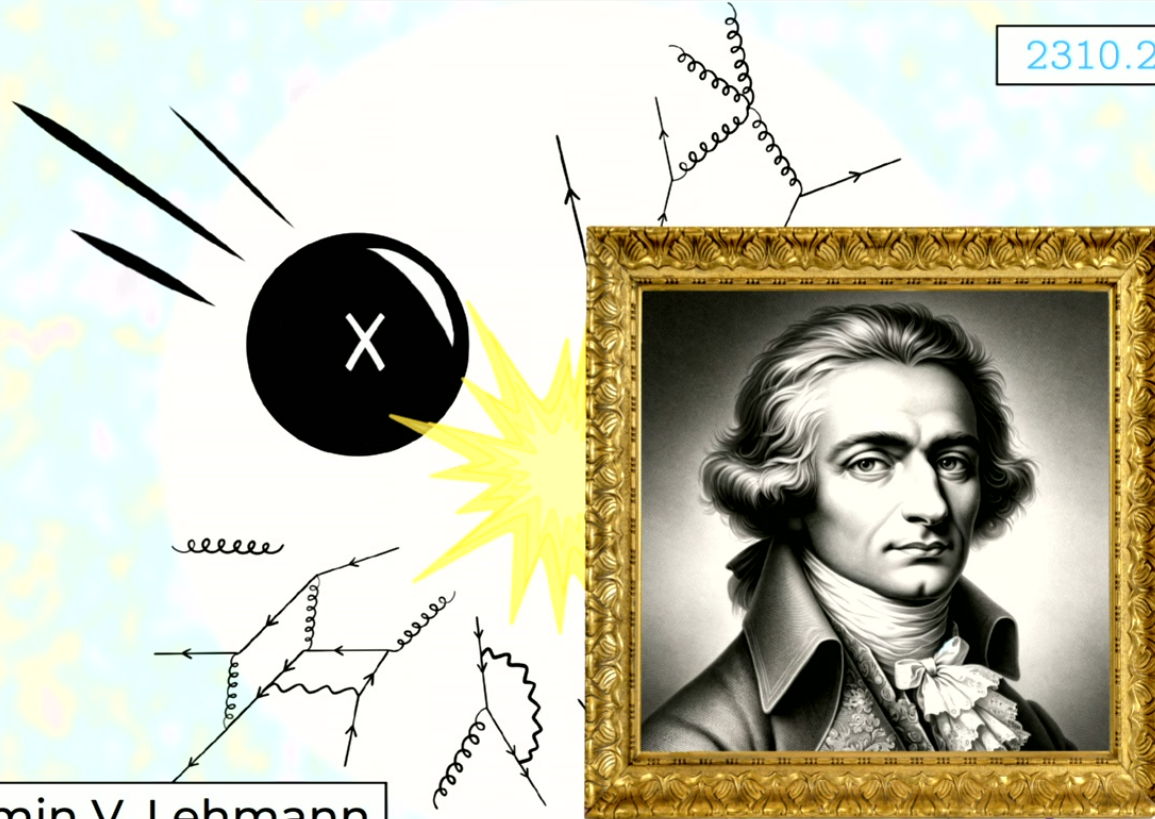
Massachusetts
Institute of
Technology



with Stefano Profumo, Nolan Smyth, & Logan Morrison

Kinetic recoupling of dark matter

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Massachusetts
Institute of
Technology



→ Ciela Inst. ∈ Montreal!

with Stefano Profumo, **Nolan Smyth**, & Logan Morrison

This talk in one slide

1. A new thermal history

Kinetic decoupling? Kinetic recoupling!

3. Implementation

Possible origins for a kinetic recoupling

1

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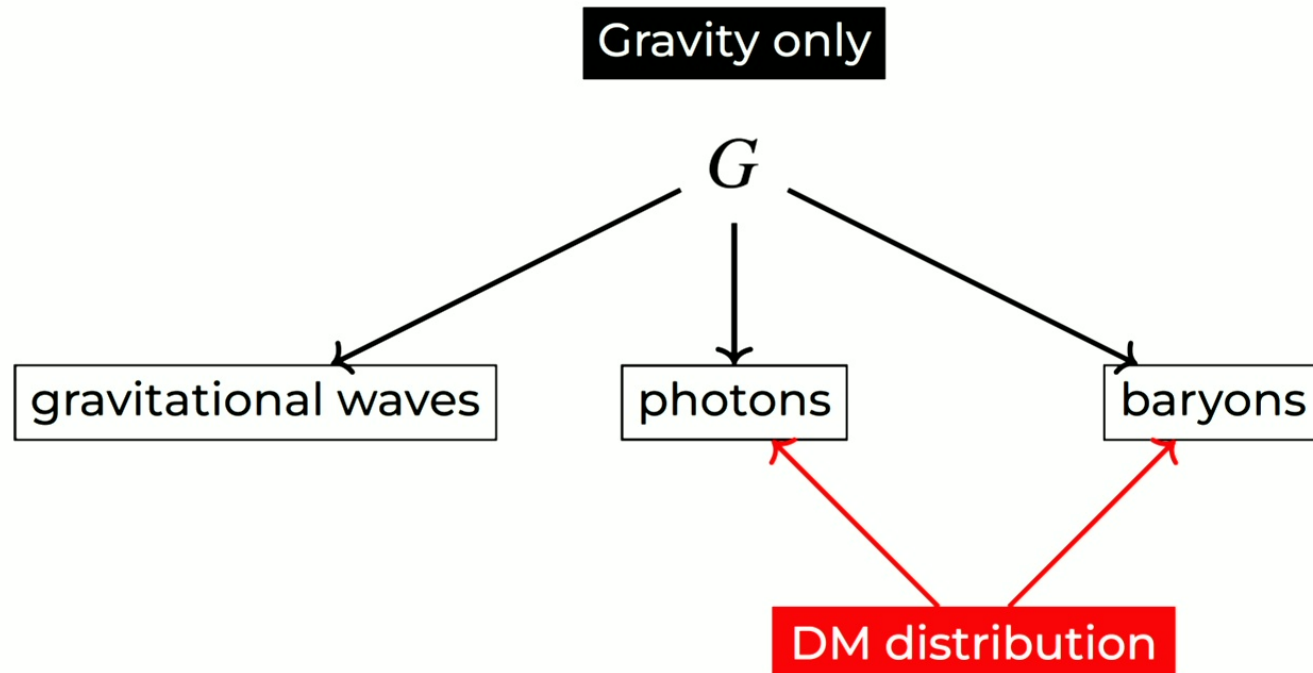
Possible origins for a kinetic recoupling

2. The DM distribution

Implications for the matter power spectrum

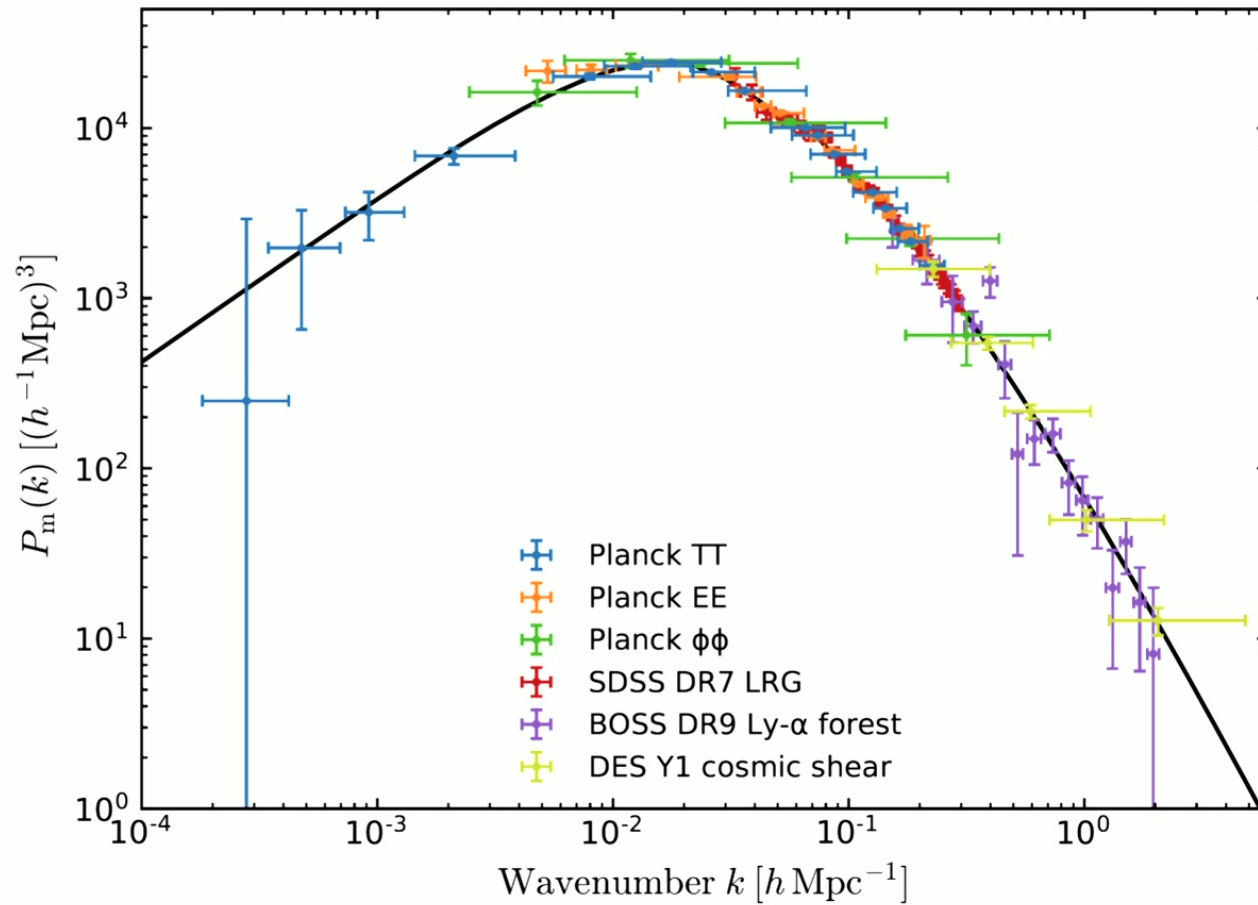
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Probing sequestered dark sectors



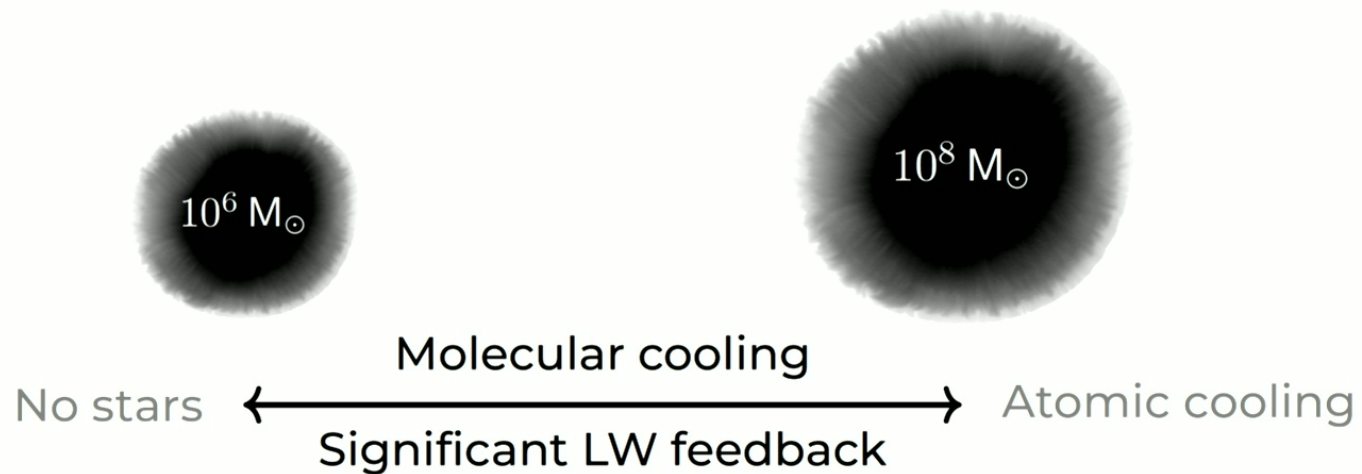
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Experimental progress



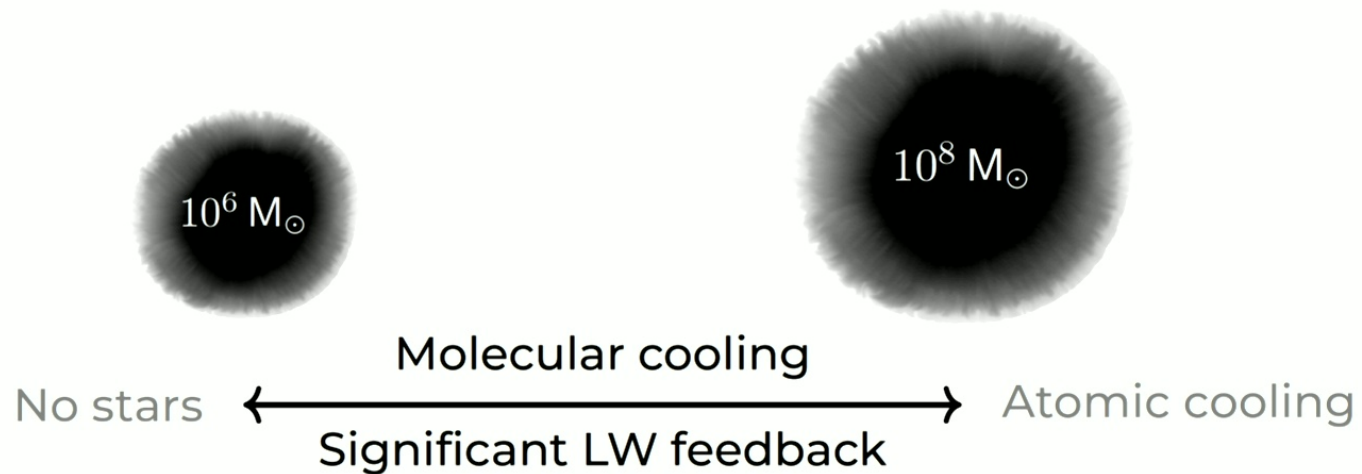
3 Planck Collaboration 2018

Suppression of small structure delays 21 cm evolution



SFR probes $40 \text{ Mpc}^{-1} < k < 100 \text{ Mpc}^{-1}$ ($12 < z < 15$)

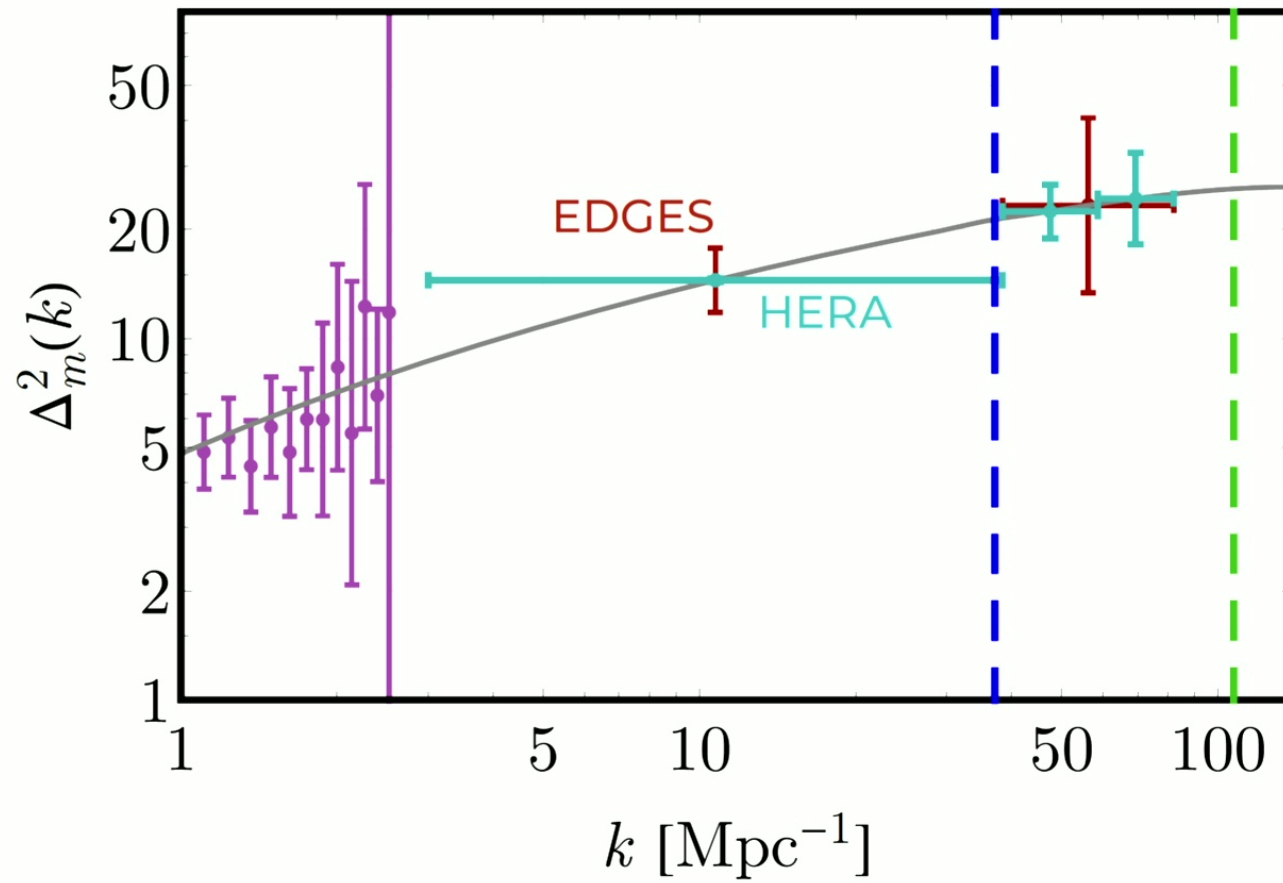
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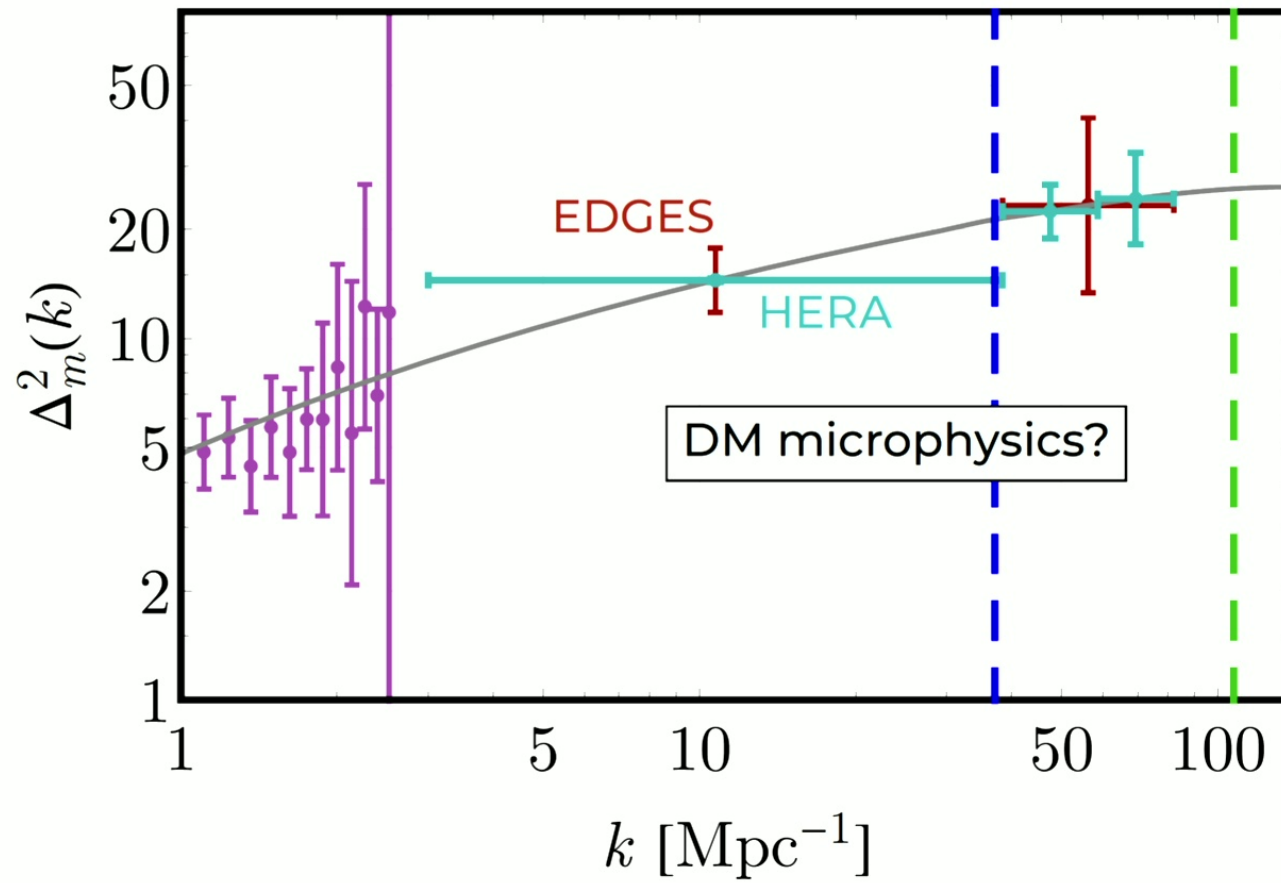
Caveats: baryons and nonlinearity

21 cm forecasts



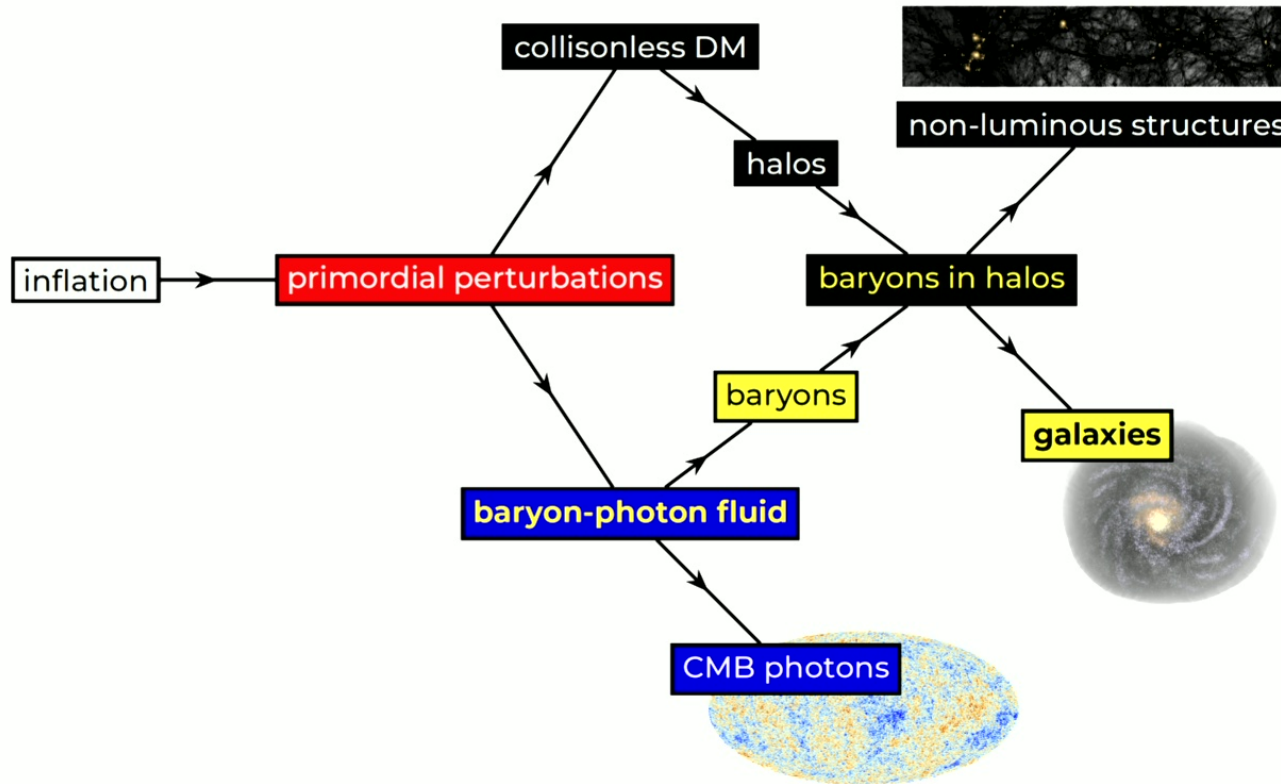
5 Muñoz, Dvorkin, & Cyr-Racine 1911.11144

21 cm forecasts



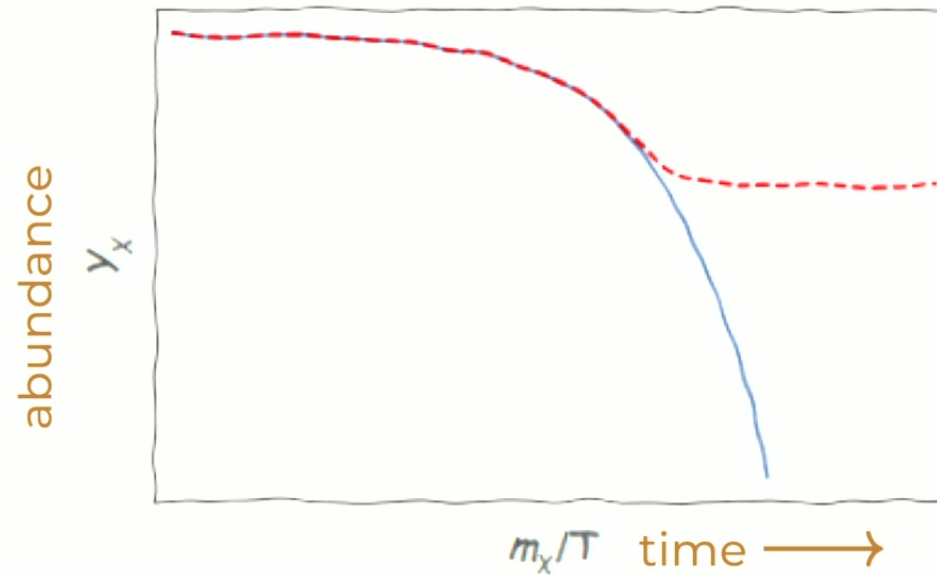
5 Muñoz, Dvorkin, & Cyr-Racine 1911.11144

The story of structure



6

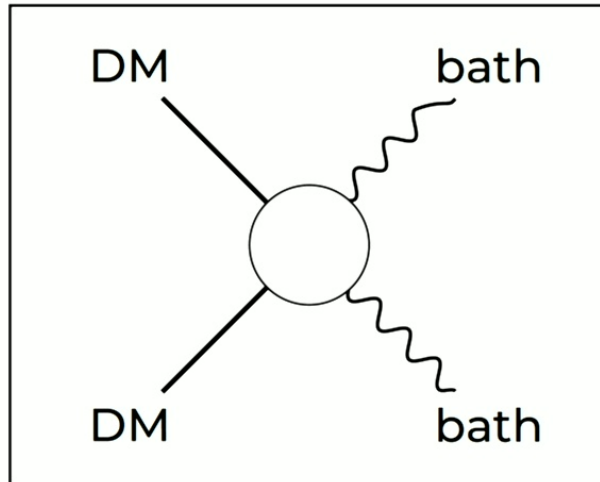
WIMPs and decoupling



Conditions set at **decoupling**

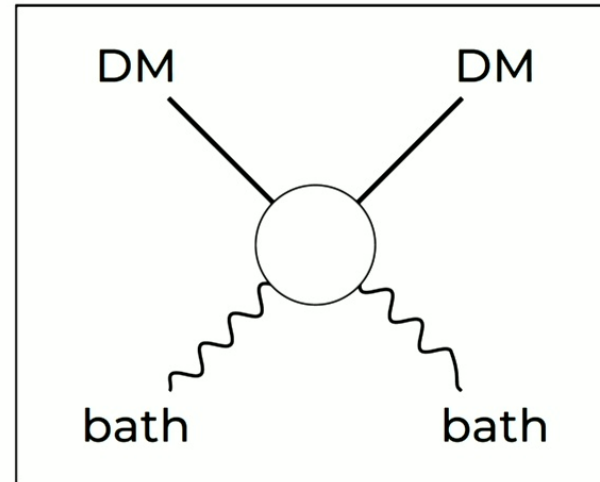
Decoupling: chemical vs. kinetic

Chemical equilibrium



Fast number-changing

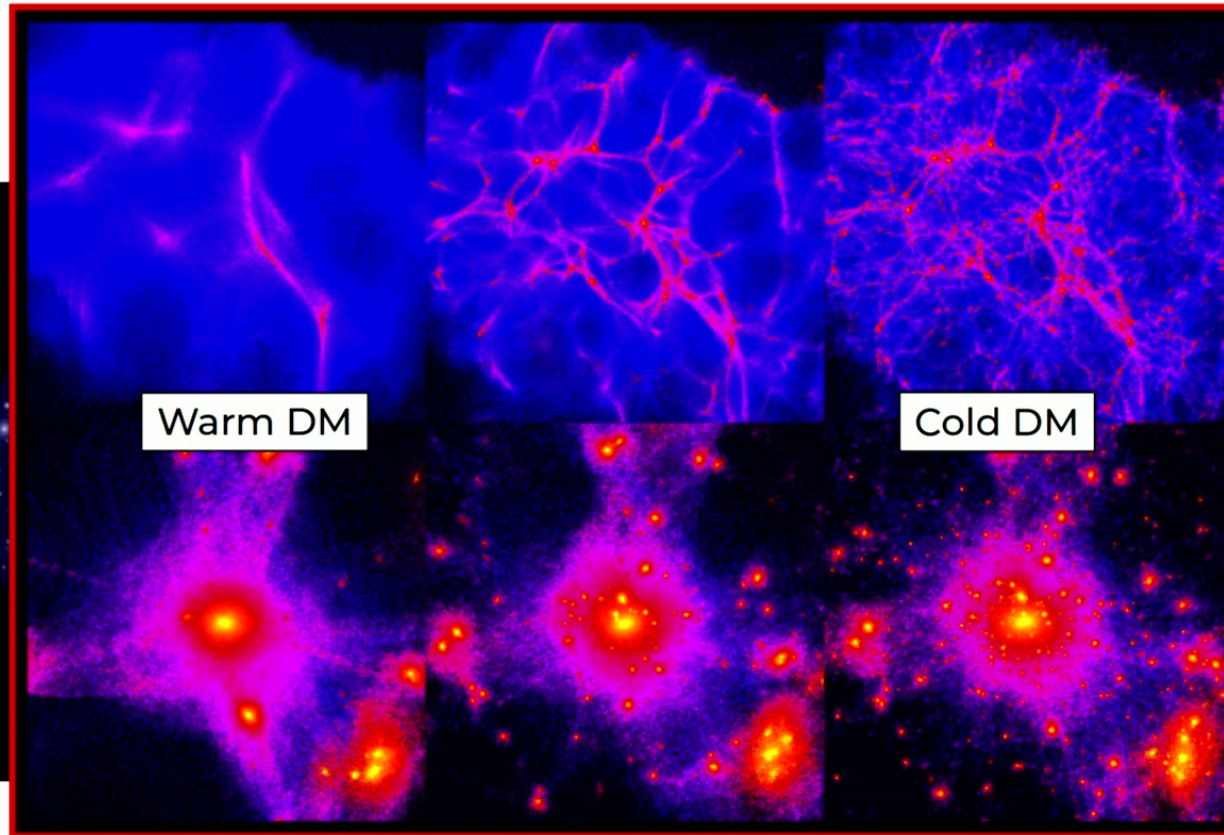
Kinetic equilibrium



Fast momentum-changing

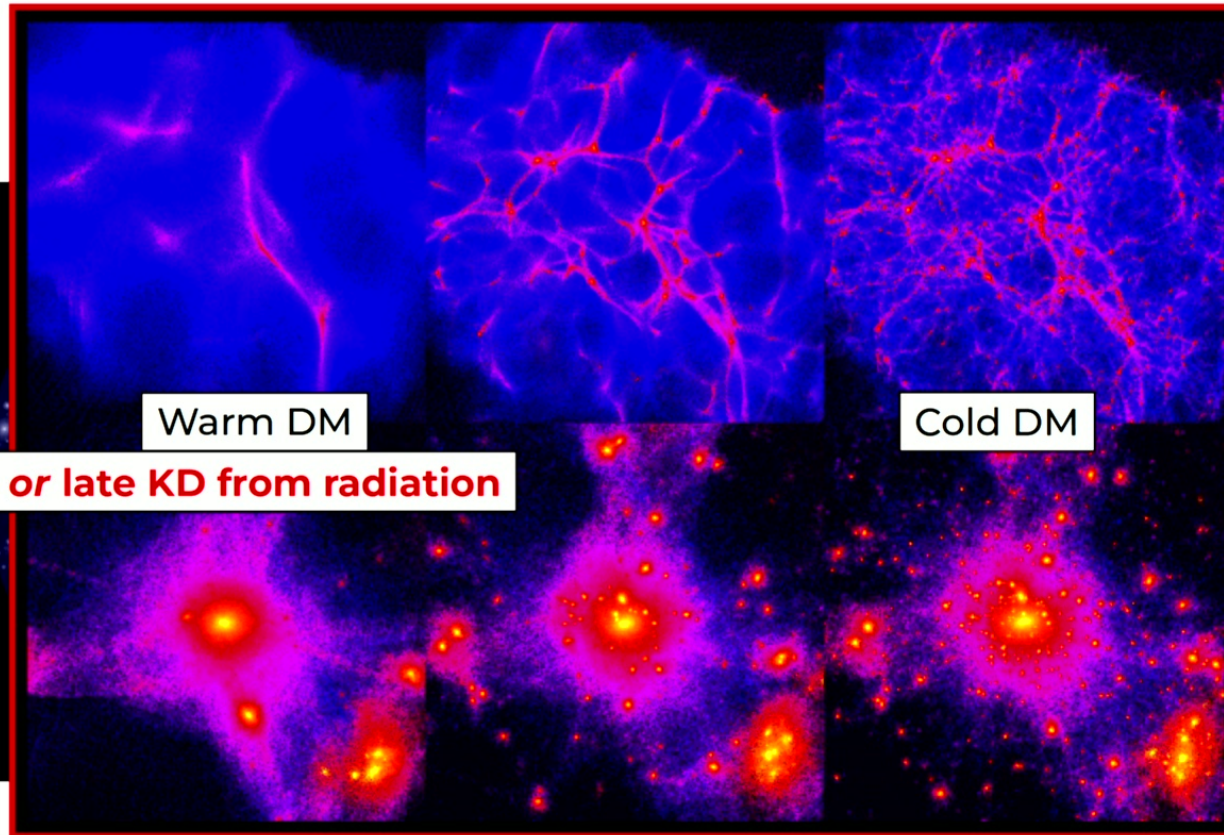
(Left diagram also maintains kinetic equilibrium!)

Nonminimal kinetic decoupling



9 Bullock & Boylan-Kolchin 1707.04256

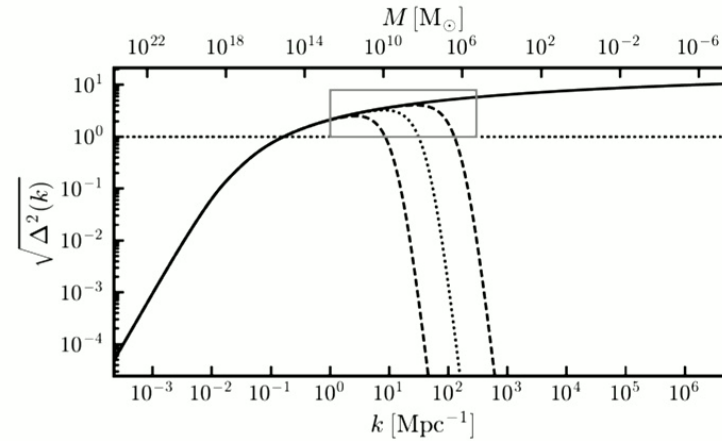
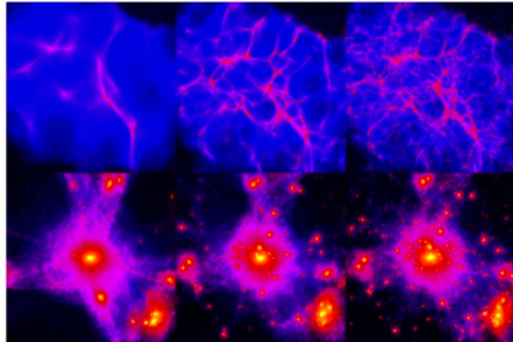
Nonminimal kinetic decoupling



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Bullock & Boylan-Kolchin 1707.04256

Decoupling and the power spectrum



warm or late decoupling

Structured dark sectors → complicated decoupling

Generic predictions

PHYSICAL REVIEW D **88**, 015027 (2013)

Kinetic decoupling and small-scale structure in effective theories of dark matter

Jonathan M. Cornell,^{1,2,3,*} Stefano Profumo,^{2,3,†} and William Shepherd^{2,3,‡}

¹*Department of Physics, Oskar Klein Centre for Cosmoparticle Physics, Stockholm University, SE-106 91 Stockholm, Sweden*

²*Department of Physics, University of California, 1156 High Street, Santa Cruz, California 95064, USA*

³*Santa Cruz Institute for Particle Physics, Santa Cruz, California 95064, USA*

(Received 20 May 2013; published 24 July 2013)

The size of the smallest dark matter collapsed structures, or protohalos, is set by the temperature at which dark matter particles fall out of kinetic equilibrium. The process of kinetic decoupling involves elastic scattering of dark matter off of Standard Model particles in the early universe, and the relevant cross section is thus closely related to the cross section for dark matter scattering off of nuclei (direct detection) but also, via crossing symmetries, for dark matter pair production at colliders and for pair annihilation. In this study, we employ an effective-field-theoretic approach to calculate constraints on the kinetic decoupling temperature, and thus on the size of the smallest protohalos, from a variety of direct, indirect and collider probes of particle dark matter.

Generic predictions

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³*Santa Cruz Institute for Particle Physics, Santa Cruz, California 95064, USA*

The size of the small-scale structure which dark matter particles form is determined by the temperature at which dark matter particles kinetically decouple from the radiation bath. Kinetic decoupling involves elastic scattering of dark matter particles off of nuclei (direct detection) but also, via annihilation. In this study we calculate constraints on the kinetic decoupling temperature from a variety of direct, indirect and collider probes.

$$\mathcal{O}_S = \frac{m_f}{\Lambda_S^3} \bar{\chi} \chi \bar{f} f, \quad (1)$$

$$\mathcal{O}_P = \frac{m_f}{\Lambda_P^3} \bar{\chi} \gamma^5 \chi \bar{f} \gamma^5 f, \quad (2)$$

$$\mathcal{O}_V = \frac{1}{\Lambda_V^2} \bar{\chi} \gamma^\mu \chi \bar{f} \gamma_\mu f, \quad (3)$$

$$\mathcal{O}_A = \frac{1}{\Lambda_V^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{f} \gamma_\mu \gamma^5 f, \quad (4)$$

$$\mathcal{O}_T = \frac{m_f}{\Lambda_T^3} \bar{\chi} \sigma^{\mu\nu} \chi \bar{f} \sigma_{\mu\nu} f, \quad (5)$$

indirect and collider probes. Kinetic decoupling involves elastic scattering of dark matter particles off of nuclei (direct detection) but also, via annihilation. In this study we calculate constraints on the kinetic decoupling temperature from a variety of direct, indirect and collider probes.

Generic predictions

PHYSICAL REVIEW D **93**, 123527 (2016)

ETHOS—an effective theory of structure formation: From dark particle physics to the matter distribution of the Universe

Francis-Yan Cyr-Racine,^{1,2,*} Kris Sigurdson,^{3,4} Jesús Zavala,⁵ Torsten Bringmann,⁶
Mark Vogelsberger,⁷ and Christoph Pfrommer⁸

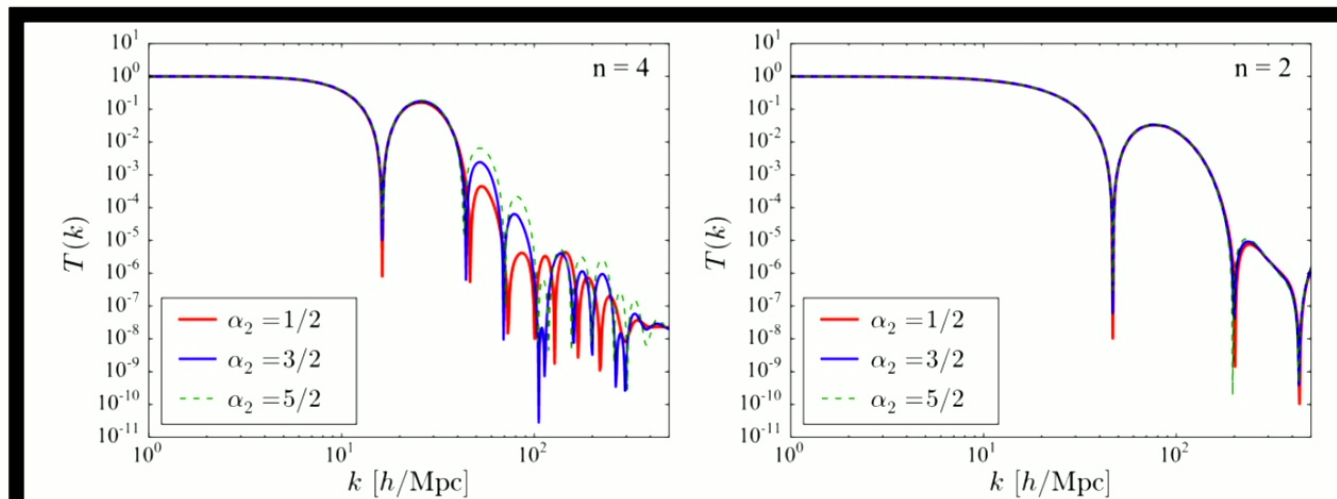
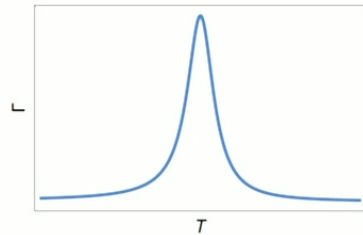
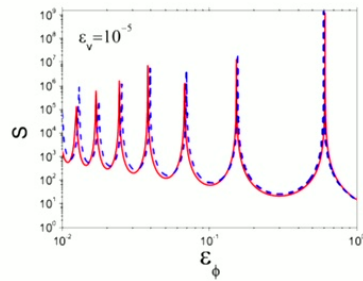


FIG. 2. Left panel: Transfer function for three different values of α_2 for a model characterized by a nonvanishing value of a_4 . The model shown here assumes fermionic DP with $a_1 = 0.73 \times 10^3 \text{ Mpc}^{-1}$, $\xi = 0.5$, $m = 2 \text{ TeV}$, $n_1 = n_2 = 2$, $h = 0$, and $\alpha_1 = 1$.

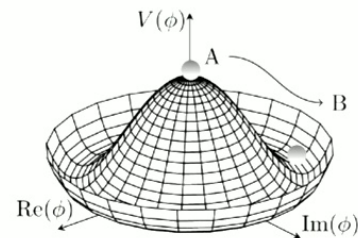
Nontrivial time dependence c.f. chemical decoupling



Resonant interaction

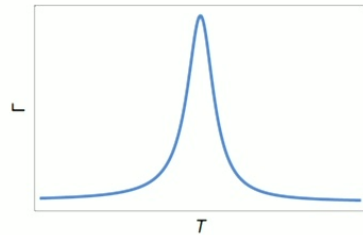


Sommerfeld enhancement

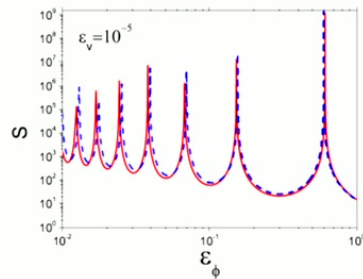


Phase transition

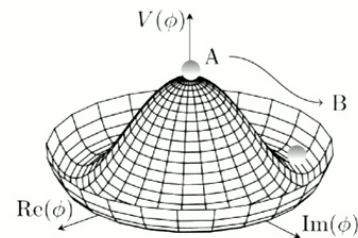
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Resonant interaction



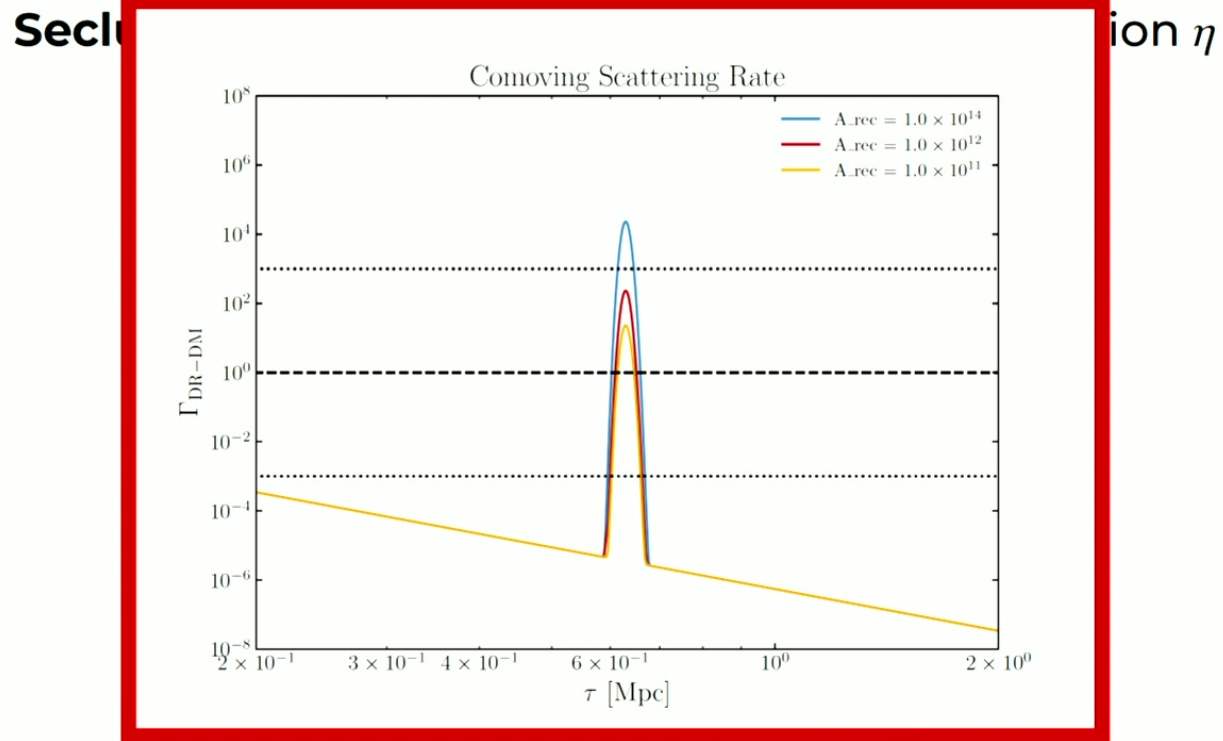
Sommerfeld enhancement



Phase transition

New possibility: kinetic recoupling

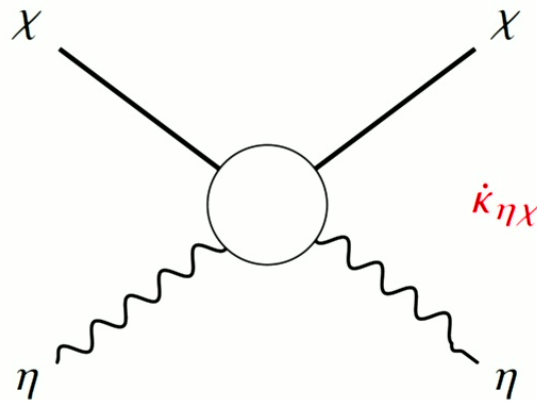
Kinetic recoupling: basic picture



DM-DR decouple normally, and then briefly **recouple**

Kinetic recoupling: basic picture

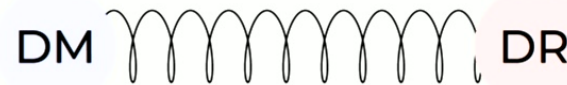
Secluded dark sector with matter χ and radiation η



Non-monotonic opacity $\dot{\kappa}_{\eta\chi}$
DM-DR decouple normally, and then briefly **recouple**

Kinetic decoupling and structure

Consider a coupled matter–radiation fluid



DM perturbations are damped by:

- 1 DM free-streaming
- 2 Collisional (acoustic) damping
- 3 Induced (Silk / diffusion) damping from DR

$$\ell_{\text{fs}} \simeq \bar{v}_{\text{kd}} a_{\text{kd}} \int_{\tau_{\text{kd}}}^{\tau} \frac{d\tau'}{a(\tau')} \longrightarrow \left(\frac{m_{\chi}}{T_{\text{kd}}} \right)^{1/2} \frac{a_{\text{eq}}/a_{\text{kd}}}{\log(4a_{\text{eq}}/a_{\text{kd}})} a_{\text{eq}} H_{\text{eq}}$$

Damping scales for kinetic recoupling

A *tight* recoupling introduces two new scales:

$$\Delta\tau_{\text{dec}} = \tau_{\text{rec}} - \tau_{\text{kd1}}$$

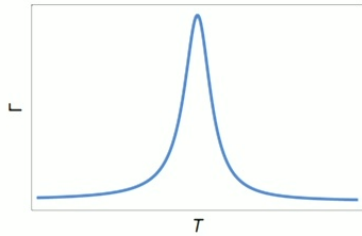
$$\Delta\tau_{\text{rec}} = \tau_{\text{kd2}} - \tau_{\text{rec}}$$

Three differences for DM perturbations:

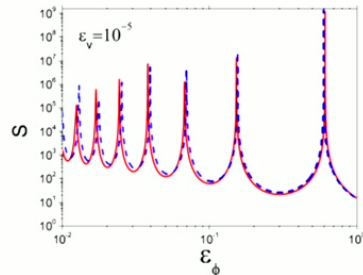
- 1 DM **free-streaming** is **interrupted** $\sim \Delta\tau_{\text{dec}}$
- 2 **Collisional** damping on **smaller scale** $r_s^{\text{rec}} \sim \Delta\tau_{\text{rec}}$
- 3 Induced damping: **DR** perturbations **evolve** $\sim \Delta\tau_{\text{dec}}$

Implementing kinetic recoupling

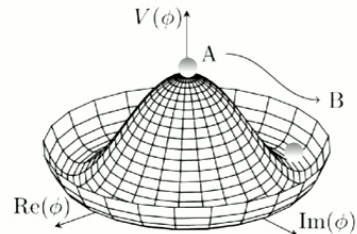
Implementation



Resonant interaction

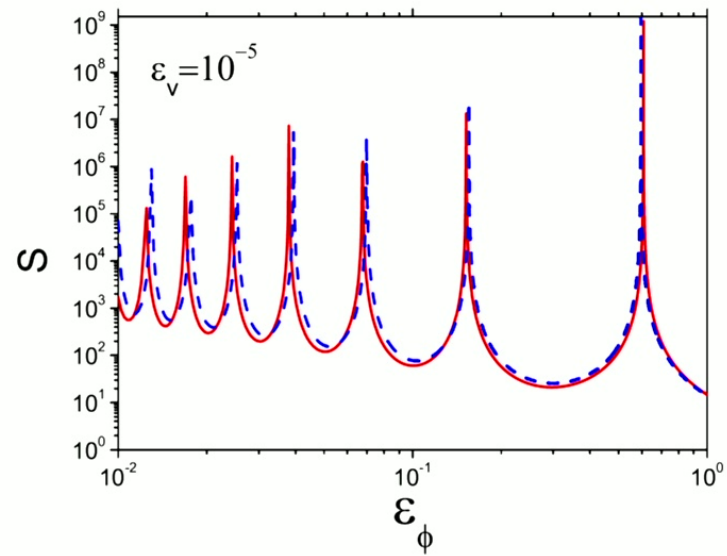


Sommerfeld enhancement



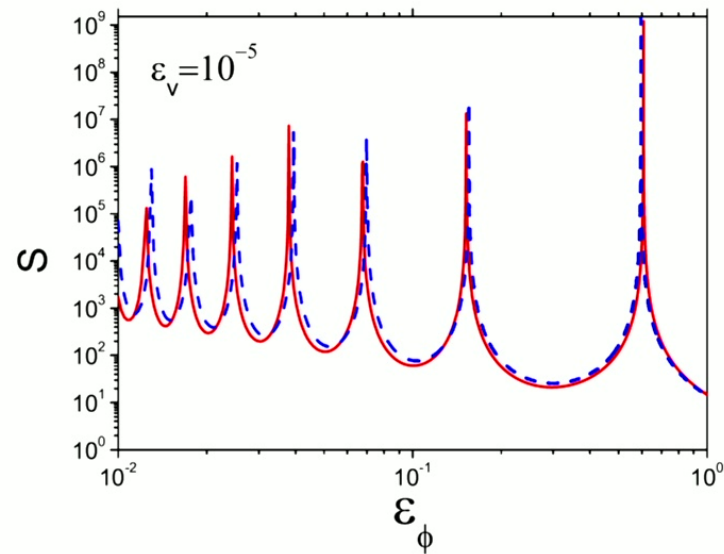
Phase transition

Sommerfeld enhancement



Intrinsically nonrelativistic

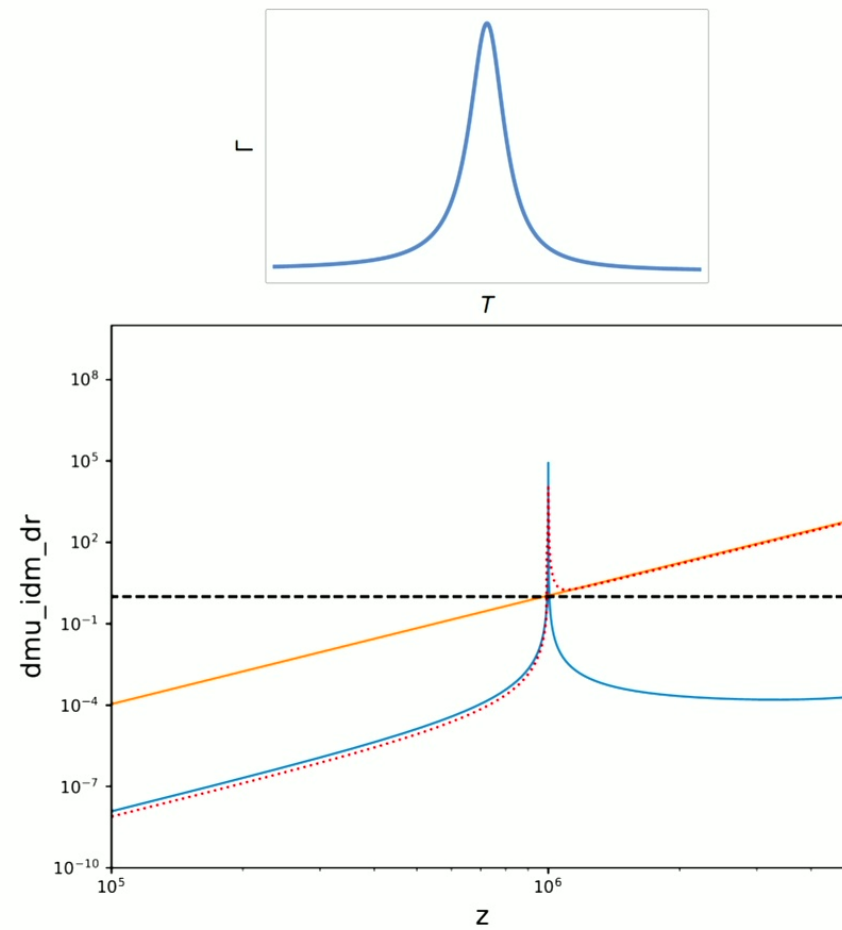
Sommerfeld enhancement



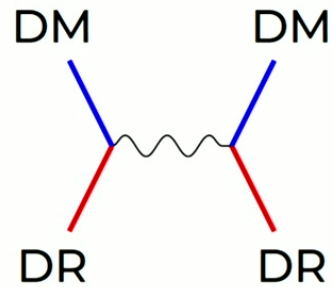
Intrinsically nonrelativistic

(Possible, but requires mediator bath)

Resonance



Do resonances recouple?



Near resonance; $M = m_\chi + \epsilon$

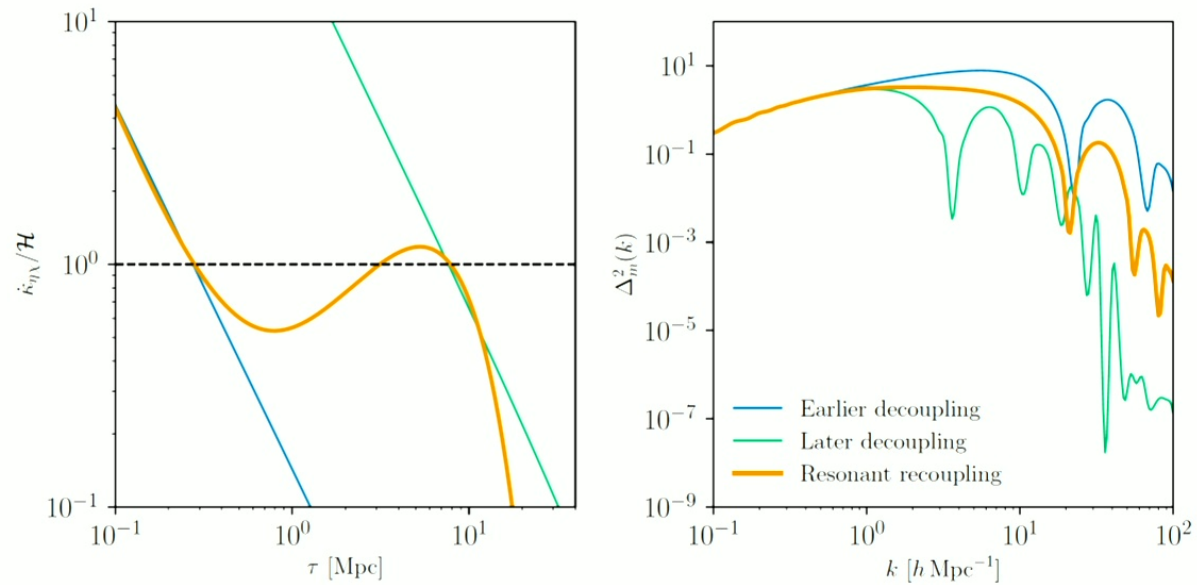
$$\begin{aligned} \mathcal{M} &\simeq \frac{\mathcal{M}_s}{s - M^2 + iM\Gamma} \\ &= -\frac{iM\Gamma}{(s - M^2)^2 + M^2\Gamma^2} \mathcal{M}_s + \mathcal{M}_{\text{regular}} \end{aligned}$$

$$\begin{aligned} \frac{\dot{k}_{\eta\chi}^{\text{res}}(T)}{\mathcal{H}} &\sim \frac{1}{a} \int \frac{dz}{2m_\chi} \frac{(M\Gamma)^2}{(z^2 + (M\Gamma))^2} \left(-k^4 \frac{df_\eta}{d\omega} \langle |\mathcal{M}_s|^2 \rangle_t \right) \\ &\sim \begin{cases} \left\{ \begin{array}{l} e^{-\epsilon/T}, & T \ll \epsilon \\ 1, & T \gg \epsilon \end{array} \right. & \text{bosonic DR} \\ \left\{ \begin{array}{l} e^{-\epsilon/T}, & T \ll \epsilon \\ \frac{4T^2}{\epsilon^2}, & T \gg \epsilon. \end{array} \right. & \text{fermionic DR} \end{cases} \end{aligned}$$

Does the rate actually increase?

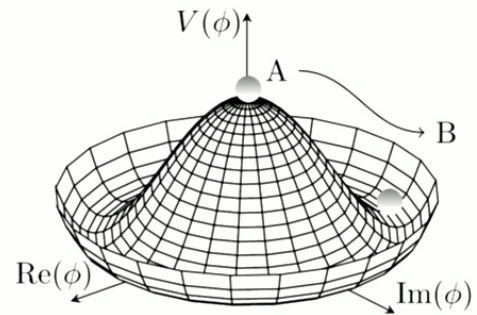
Recoupling through resonance

Does the rate actually increase?

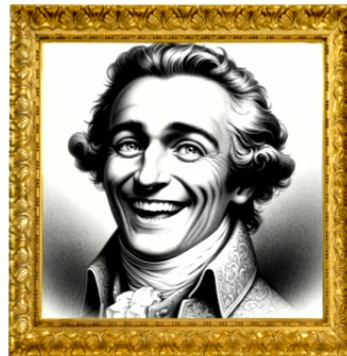


Yes, with tuning

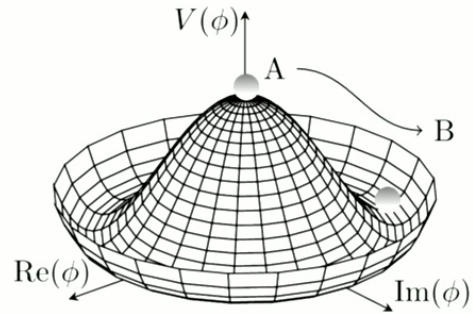
Phase transition



e.g., $\mathcal{L} \supset g_1 \chi \eta \varphi_1 + g_2 \chi \eta \varphi_1 \varphi_2$ acquiring large $\langle \varphi_2 \rangle$



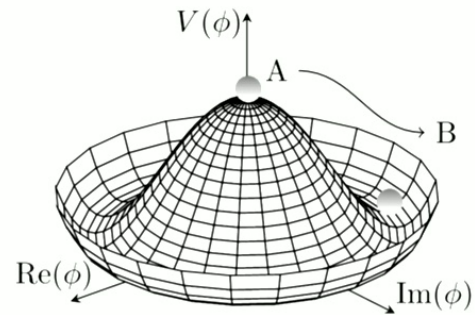
Phase transition



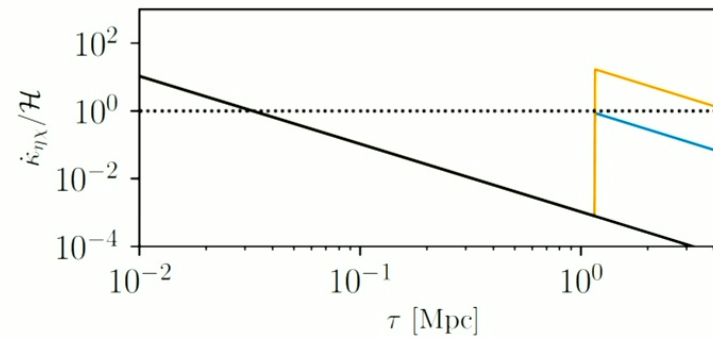
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Phase transition



e.g., $\mathcal{L} \supset g_1 \chi \eta \varphi_1 + g_2 \chi \eta \varphi_1 \varphi_2$ acquiring large $\langle \varphi_2 \rangle$



The power spectrum with kinetic recoupling

Coupled DM-DR perturbations

Linear evolution in conformal Newtonian gauge

DM perturbations:

$$\Delta\theta \equiv \theta_\eta - \theta_\chi, \quad S \equiv \frac{4\rho_\chi}{3\rho_\eta}$$

$$\begin{cases} \dot{\delta}_\chi + \theta_\chi - 3\dot{\phi} = 0, \\ \dot{\theta}_\chi - c_\chi^2 k^2 \delta_\chi + \mathcal{H}\theta_\chi - k^2\psi = -S\dot{\kappa}_{\eta\chi}\Delta\theta \end{cases}$$

DR perturbations:

$$\begin{cases} \dot{\delta}_\eta + \frac{4}{3}\theta_\eta - 4\dot{\phi} = 0, \\ \dot{\theta}_\eta + k^2(\sigma_\eta - \frac{1}{4}\delta_\eta) - k^2\psi = \dot{\kappa}_{\eta\chi}\Delta\theta \end{cases}$$

$\theta \sim$ divergence of velocity field

$\phi \simeq \psi \sim$ total potential

Perturbations in a tight recoupling

“Strong” recoupling ($\dot{k}/\mathcal{H} \gg 1$) \rightarrow matter–radiation fluid

$$\theta_\chi \simeq \theta_\eta, \quad \delta_\chi \simeq \frac{3}{4}\delta_\eta, \quad \sigma_\eta \simeq c_\chi \simeq 0$$

Where do θ_χ, θ_η meet? Careful: $\dot{k}_{\eta\chi}\Delta\theta$ is not small!

$$\delta_\eta(\tau) \equiv \frac{4}{3}\delta_\chi(\tau) [1 + \epsilon(\tau)], \quad \dot{k}_{\eta\chi} \equiv \gamma(\tau)/\epsilon(\tau), \quad \Delta\theta \equiv \Omega(\tau)/\epsilon(\tau)$$

$$\theta_\chi + \dot{\delta}_\chi - 3\dot{\phi} \simeq 0, \quad \dot{\theta}_\chi \simeq k^2\psi - \mathcal{H}\theta_\chi - \Omega S\gamma, \quad -\mathcal{H}\theta_\chi \simeq \frac{1}{3}k^2\delta_\chi + (1+S)\Omega\gamma$$

Estimate θ after recoupling: linearize $\theta_i(\tau) = \theta_i(\tau_0) + \dot{\theta}_i(\tau_0)\Delta\tau$ after recoupling. Rapid evolution stops when $\Delta\theta = 0$.

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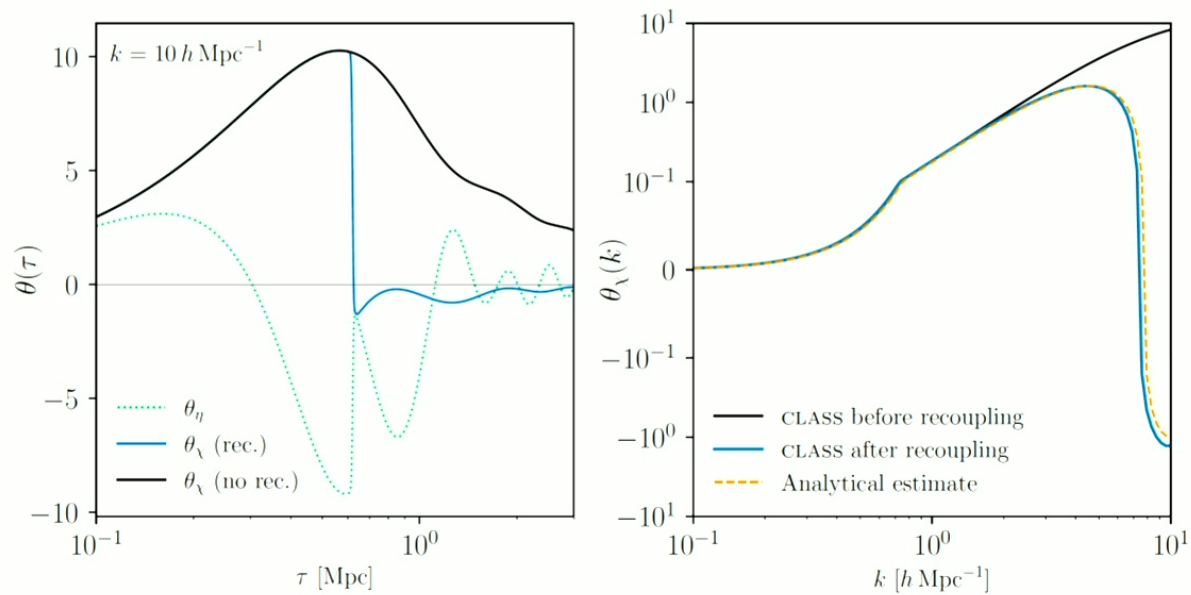
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Estimate θ after recoupling: linearize $\theta_i(\tau) = \theta_i(\tau_0) + \dot{\theta}_i(\tau_0)\Delta\tau$ after recoupling. Rapid evolution stops when $\Delta\theta = 0$.

Expect a kick: a sudden change in $\dot{\delta}$

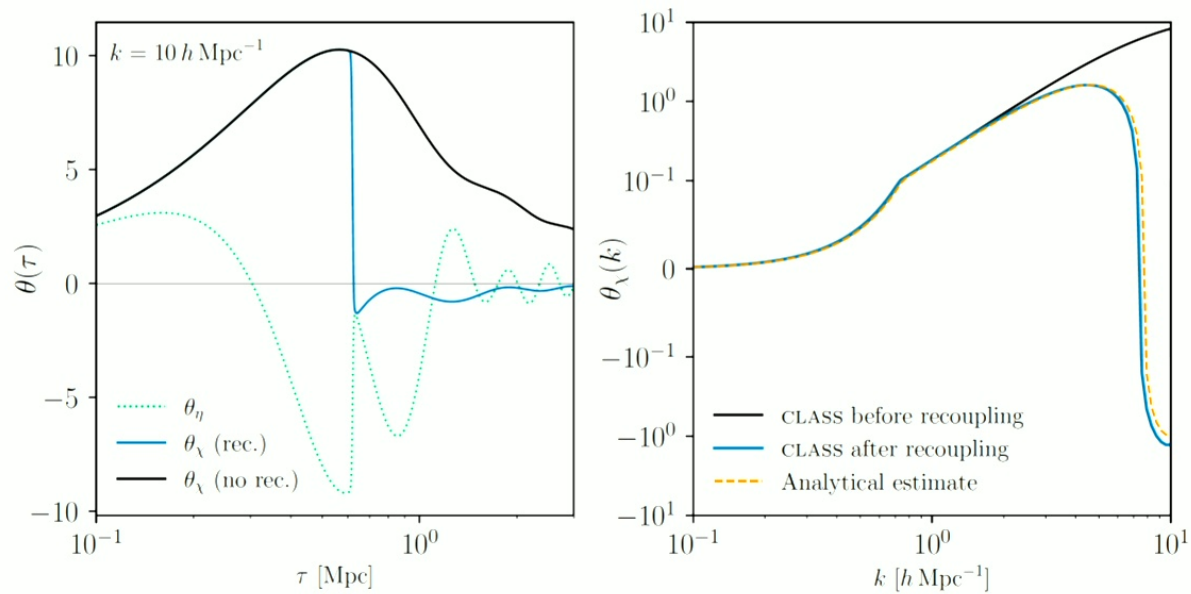
Check: brief recoupling in CLASS

$$\theta(\text{after}) \simeq \frac{k^2 \delta_\eta \theta_\chi - 4k^2 \psi \Delta\theta + 4\mathcal{H}\theta_\chi \theta_\eta + 4\Delta\theta (\theta_\chi + S\theta_\eta) \dot{k}_{\eta\chi}}{k^2 \delta_\eta + 4\mathcal{H}\theta_\chi + 4(1+S)\Delta\theta \dot{k}_{\eta\chi}} \Big|_{\tau=\tau_0}$$



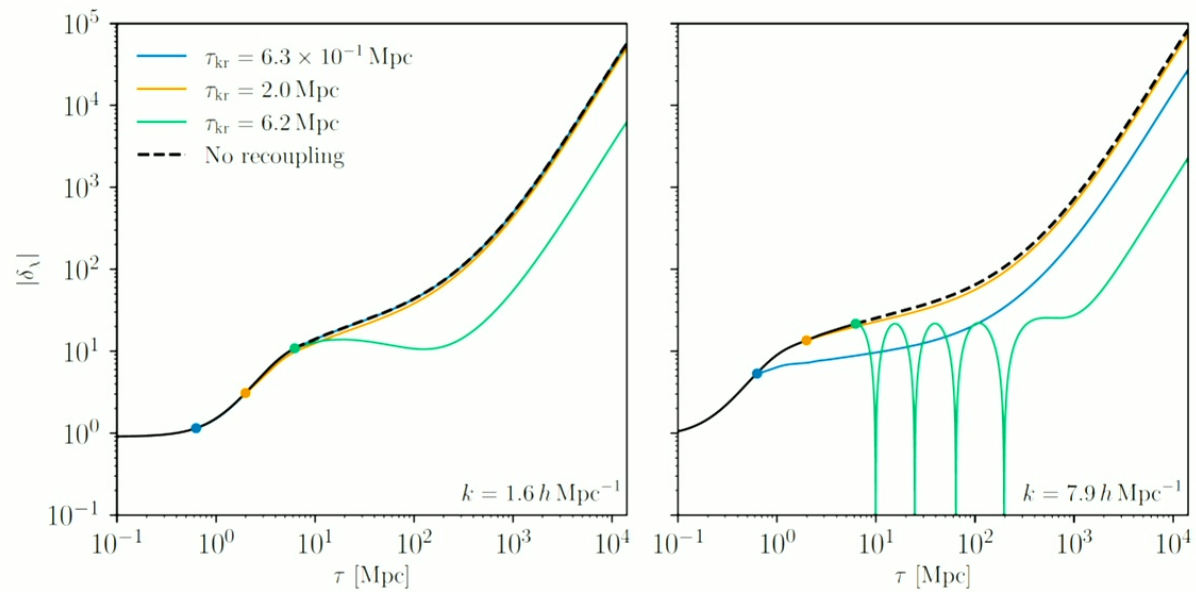
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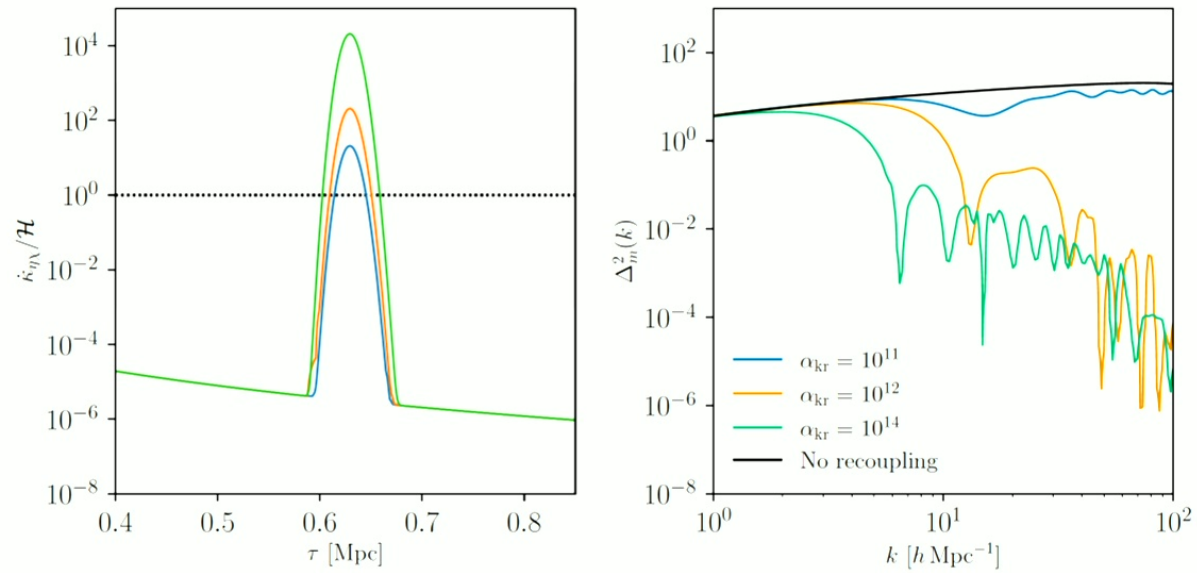
The kick is predictable

Understanding the kick

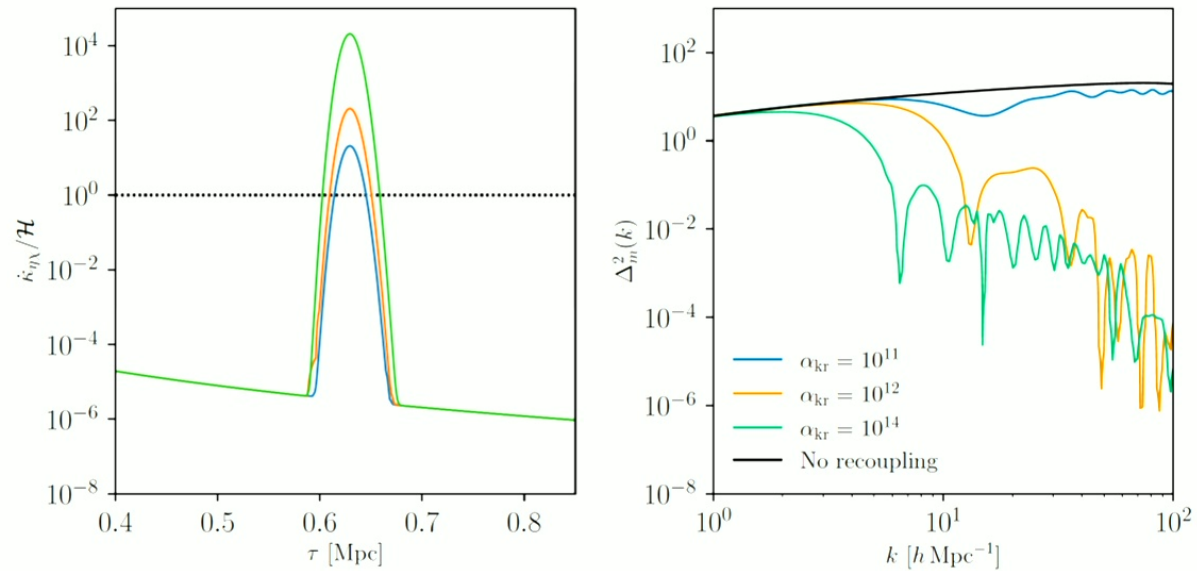


Scale-dependent delay to structure formation

The matter power spectrum



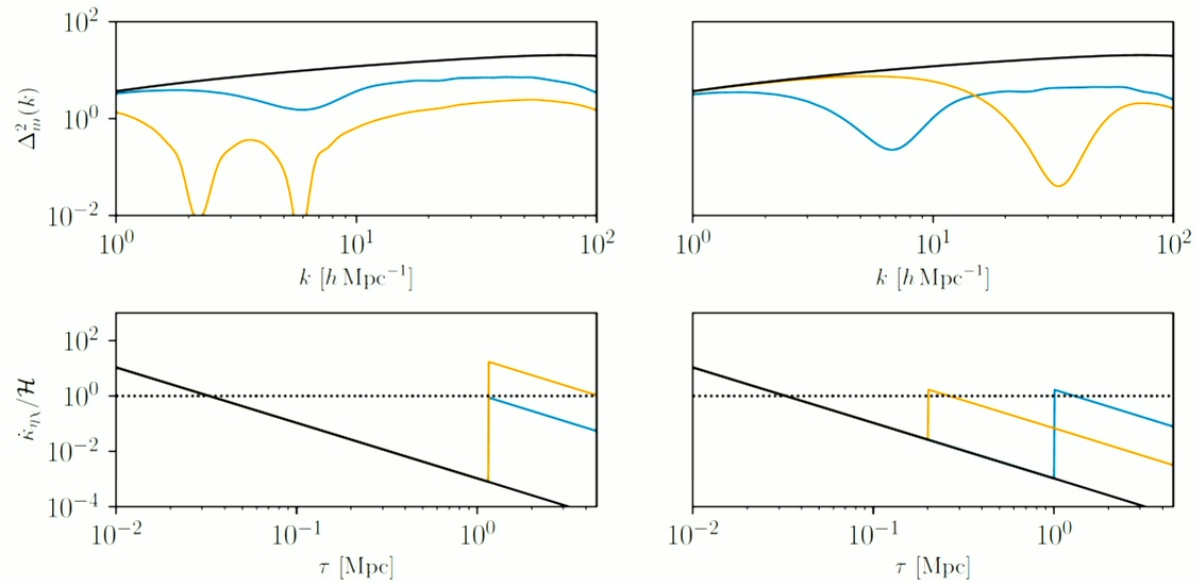
The matter power spectrum



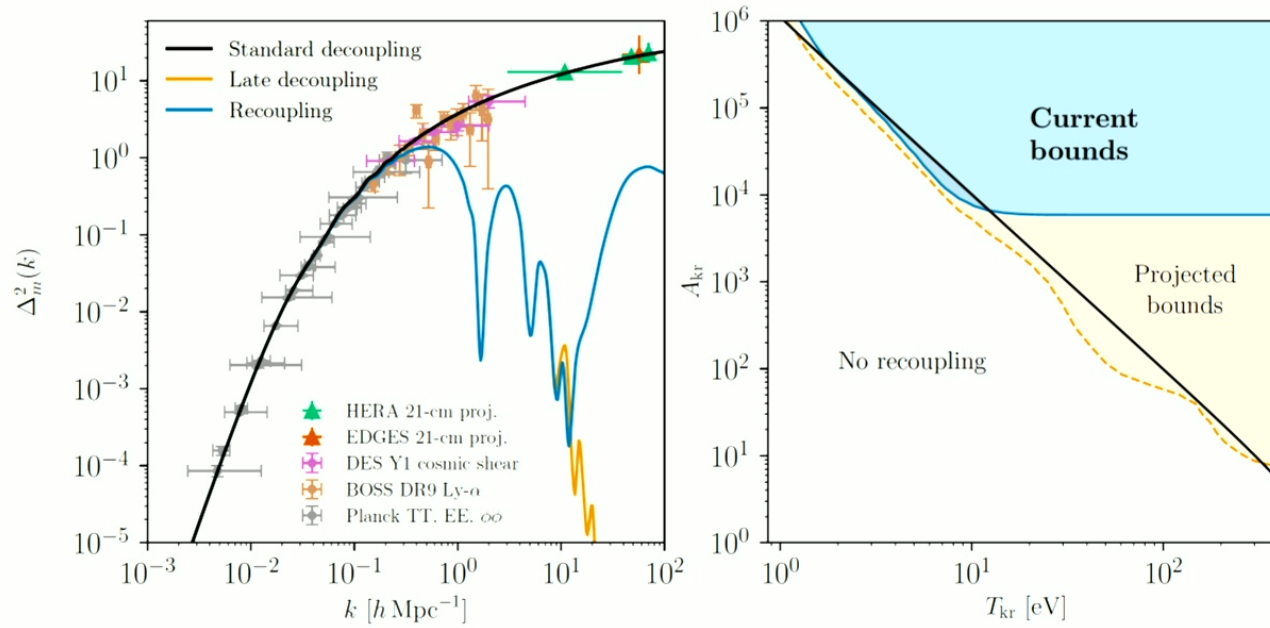
How can we interpret this?

Recoupling time and duration

Step-function enhancement (like phase transition)



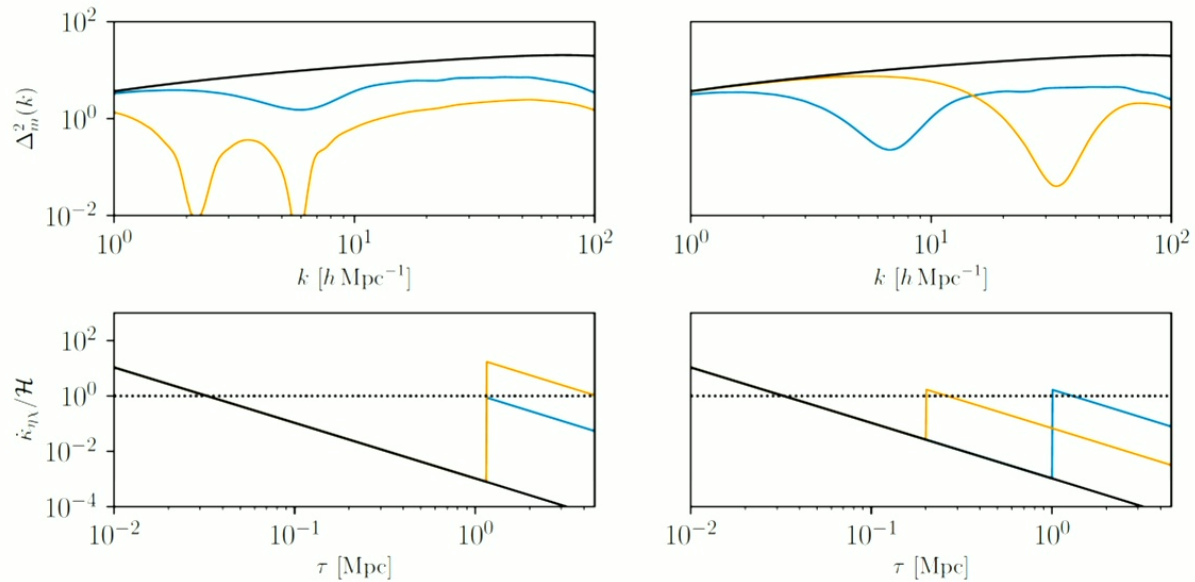
Interpretable constraints



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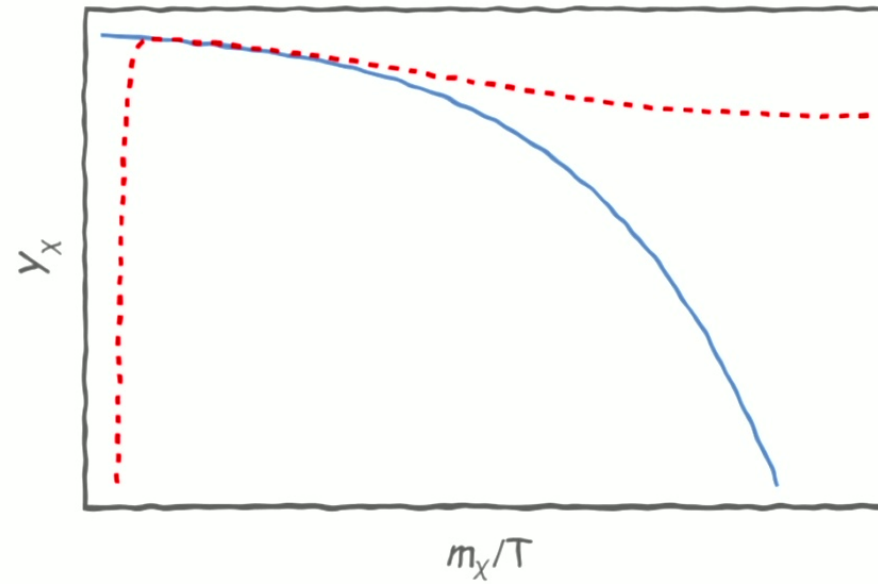
Recoupling time and duration

Step-function enhancement (like phase transition)

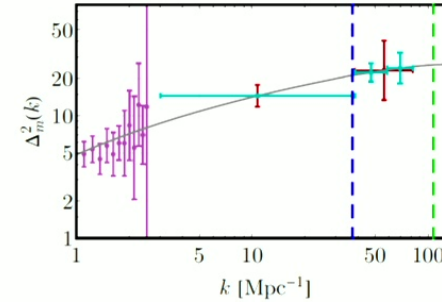
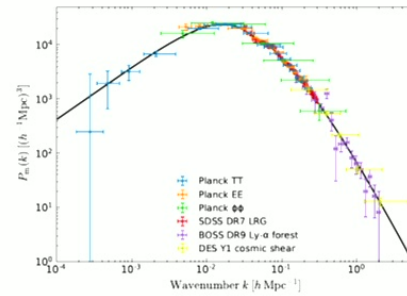
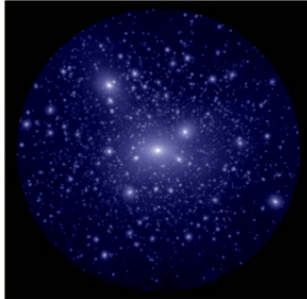


- Recoupling time \leftrightarrow feature scale
- Recoupling duration \leftrightarrow feature depth

Next: freeze-in!

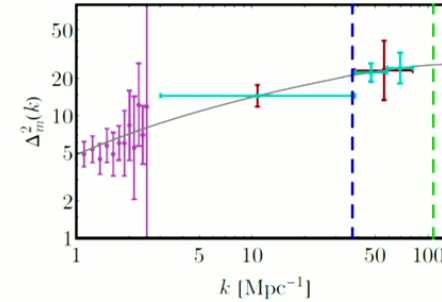
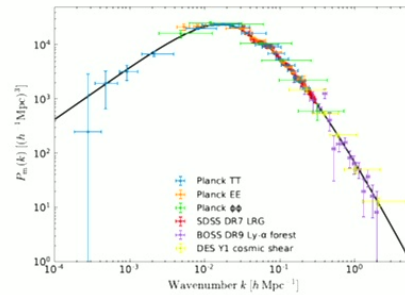
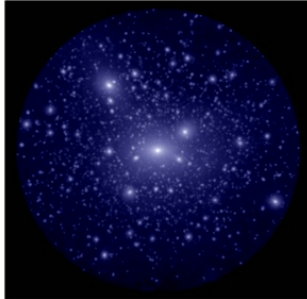


Conclusions



- 1 DM can kinetically *recouple*
- 2 Nontrivial time evolution in *kinetic* decoupling
- 3 Nonminimal observable for dark sectors

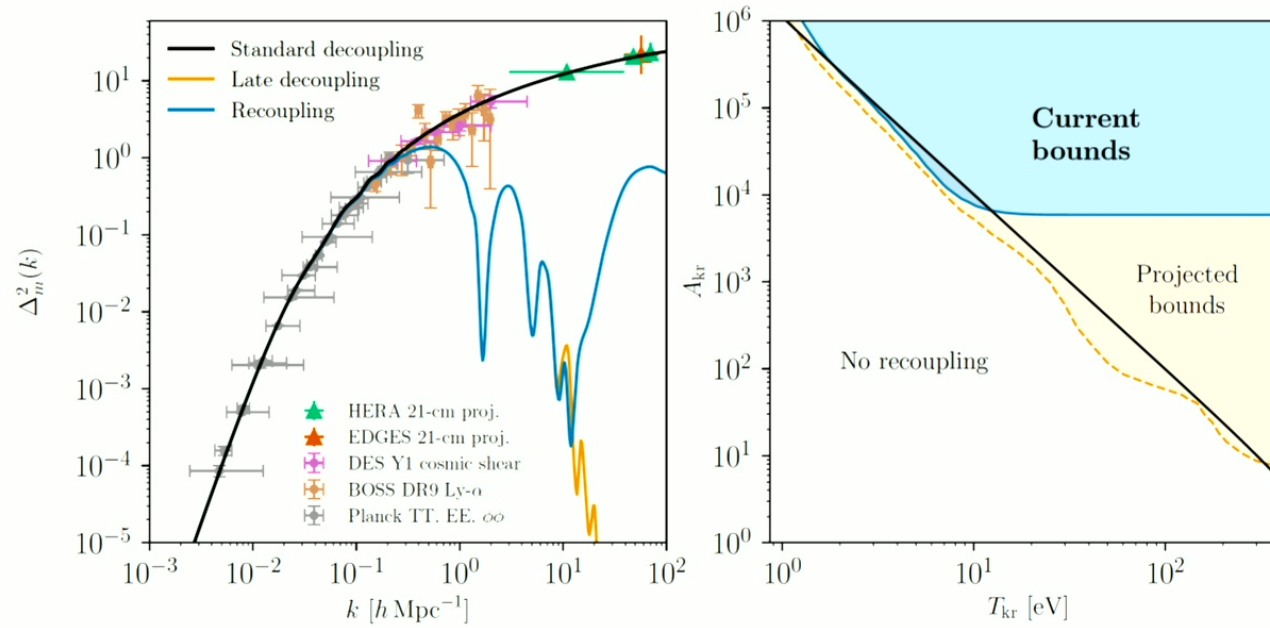
Conclusions



- 1 DM can kinetically *recouple*
- 2 Nontrivial time evolution in *kinetic* decoupling
- 3 Nonminimal observable for dark sectors

Goes beyond a cutoff in the power spectrum

Interpretable constraints



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Check: brief recoupling in CLASS

$$\theta(\text{after}) \simeq \frac{k^2 \delta_\eta \theta_\chi - 4k^2 \psi \Delta\theta + 4\mathcal{H}\theta_\chi \theta_\eta + 4\Delta\theta (\theta_\chi + S\theta_\eta) \dot{k}_{\eta\chi}}{k^2 \delta_\eta + 4\mathcal{H}\theta_\chi + 4(1+S)\Delta\theta \dot{k}_{\eta\chi}} \Big|_{\tau=\tau_0}$$

