

Title: Standard Model Lecture

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$$B_1 = -1(T - k)$$

However what are Quantum numbers of ν_R ?

$$\begin{array}{cc} SU(2) & U(1) \\ 1 & 0 \end{array}$$

Singlet under all gauge groups in SM.

∴ its own antiparticle → Majorana field

$$\begin{pmatrix} 0 \\ 0 \\ m_{\nu_3} \end{pmatrix}$$

$$\Sigma = -\sigma_2$$

mass term $\nu_R \nu_R$ allowed

Neutrinos have mass!

$$\mathcal{L}_{SM} \Rightarrow m_{\nu_1} = m_{\nu_2} = m_{\nu_3} = 0$$

$$\text{Exp} \Rightarrow \Delta m_{12}^2 = 7.37 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{13/32}^2 = 2.5 \times 10^{-3} \text{ eV}^2$$

$$|V\rangle \rightarrow |V\rangle$$

Schwarz

$m_{\nu_L \nu_R}$ Dirac masses

$$[k_i, k_j] = -i \epsilon_{ijk} J_k$$

So how to make $\Delta m_{\nu_{12}}^2 \neq 0$, $\Delta m_{\nu_{13}}^2 \neq 0$

'Dirac Masses' - Add to SM $\rightarrow \mathcal{L}_{SM} - [\tilde{H}^\dagger \bar{V}_R Y_\nu \psi_L + h.c.]$

Higgs gets vev $\Rightarrow -\frac{v}{\sqrt{2}} \bar{V}_R Y_\nu V_L + h.c.$

Rotate to mass eigenstates $V_L \rightarrow U(V,L) V_L'$ $M_\nu = \frac{v}{\sqrt{2}} Y_\nu$
 $V_R \rightarrow U(V,R) V_R'$ (not diagonal to start)

$\Rightarrow A_L = \frac{1}{2} (J_0 + k)$

$[A_1, A_2] = i \delta_{12} A_k$

$(0,0) \rightarrow spin 0$

$[B, B] = 0$

$(1,0) \rightarrow spin 1$

Majorana masses vs Dirac masses

When fermion charged under $U(1)_Y$

$$H, \bar{\Psi}_L, \Psi_R \quad \text{Dirac masses}$$

$$\Sigma(x) \sim SU(2) \times SU(2)$$

$$= \exp(i\sigma \cdot \pi / v)$$

Recall Lorentz group \rightarrow rotations J_i
boosts K_i

$$[J_i, J_j] = i \epsilon_{ijk} J_k$$

$$[K_i, K_j] = -i \epsilon_{ijk} J_k$$

$$[J_i, K_j] = i \epsilon_{ijk} K_k$$

Hermitian
generators
 \Rightarrow

Denote a $(1/2, 0)$ Weyl spinor χ : $\chi \rightarrow e^{-i/2 \sigma \cdot \theta} \chi$ under rotation

$\chi \rightarrow e^{-1/2 \sigma \cdot \eta} \chi$ under boost

($\tanh \eta = \beta$)
↑
rapidity

$\mathcal{L} = \frac{1}{2} \chi^\dagger \epsilon \chi + \text{h.c.}$ is allowed

$$\epsilon = i\sigma_2$$

$\sigma \cdot \theta \chi$ under rotations

$\sigma \cdot n \chi$ under boosts

$(\tanh \eta = \beta)$
↑
rapidity

$\chi + h.c.$ is allowed

$= i\sigma_2$

Explicitly $\chi^T \epsilon \chi \rightarrow \chi^T M^T \epsilon M \chi$ where $M = e^{i/2 \sigma_1 \eta}$
or $e^{-i/2 \sigma_3 \eta}$

In components $(M^T)_{\alpha\beta} \epsilon_{\beta\gamma} M_{\gamma\delta} = \epsilon_{\alpha\delta} M_{\beta\gamma}$
 $= \epsilon_{\alpha\delta} \det M$
" "
 $= \epsilon_{\alpha\delta}$

Majorana mass term allowed
mass term $\bar{\nu}_R \nu_R$ allowed

Choice: $m \ll \ll y \nu$ Pираи miss

$m \gg \gg y \nu \rightarrow$ Seesaw model

$$p/m^2 \ll 1$$

Expect $\mathcal{L}_{SM} + \frac{\mathcal{L}^5}{M} + \frac{\mathcal{L}^6}{M^2} + \frac{\mathcal{L}^7}{M^3} \dots$
($m_\nu = 0$)

$$\mathcal{L}^5 = \frac{C_{mn}}{M}$$

$$\mathcal{L}^5 = \frac{C_{mn}}{\Lambda} \left[(\bar{\ell}_m^c \tilde{H}^*) (\tilde{H}^+ \ell^n) + \text{h.c.} \right] \quad \underline{\text{allowed}}$$

$\frac{3}{2} \quad 1 \quad 1 \quad \frac{3}{2}$

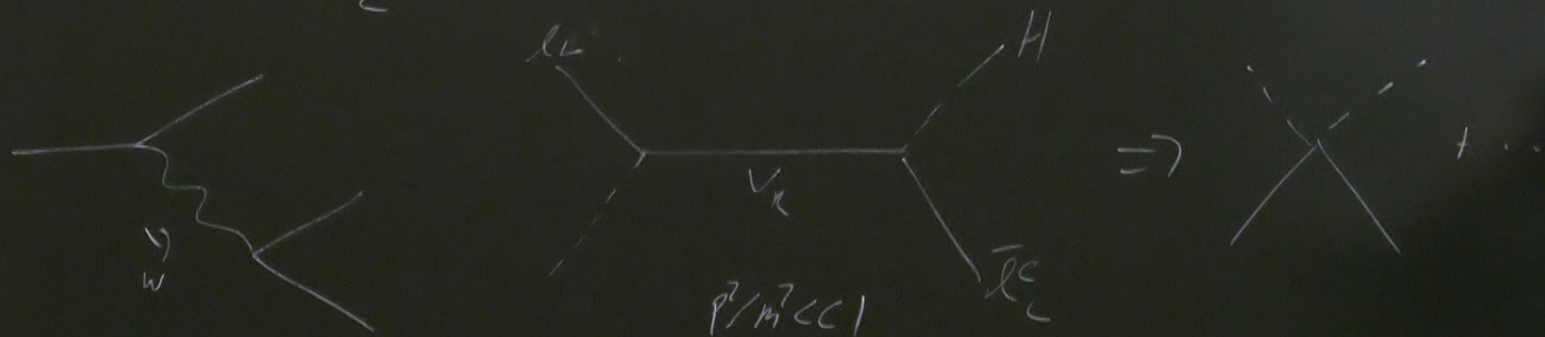
$$|H\rangle = \begin{pmatrix} 0 \\ v/\sqrt{2} \end{pmatrix} \Rightarrow -\frac{m_{\nu, k}}{2} \bar{V}_L^{c, k} V_L^k + \text{h.c.}$$

By absorption $\Lambda \gg v$

$$m_{\nu, k} = -\frac{v^2}{2\Lambda} U^T(v, L) C_{mn} U(v, L)$$

Seesaw Model: $\psi^c = C \bar{\psi}^T$, $C = -i\gamma_2\gamma_0$

$$\mathcal{L}_{SM} + \frac{1}{2} \bar{V}_R^P (i\not{\partial} - m_P) V_R^P - \bar{\ell}_L^B \widehat{H} (Y_{\nu}^{\dagger})_{PP} V_R^P + h.c.$$



Baryon number violation

Preserved lightest Baryon
(proton)

$$\text{Baryon number} \equiv \frac{1}{3} (n_u - n_{\bar{u}})$$

\mathcal{L}_{SM} classically preserved

Global

$$\psi_q \rightarrow e^{i\alpha_2} \psi_q$$

Symmetry

$$\psi_{\bar{q}} \rightarrow e^{-i\alpha_2} \psi_{\bar{q}}$$

violation

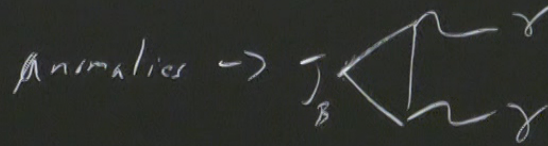
Preserved lightest Baryon stable
(proton)

modiv-

$$\text{number} \equiv \frac{1}{3} (n_L - n_{\bar{L}})$$

\mathcal{L}_{SM} classically preserves global sym for B

$$\rightarrow e^{i\alpha} \psi_q$$



$$\rightarrow e^{-i\alpha} \psi_{\bar{q}}$$

$$J_B^M = (\bar{u} \gamma^M u + \bar{d} \gamma^M d + \dots \text{quarks})$$

Motivation to $P \rightarrow \gamma \gamma \pi$

KEK Japan

$$\tau_{\text{proton}} = 8.2 \times 10^{33} \text{ years}$$

$$2_n J_B^{\wedge} \neq 0$$

for B

$$= \frac{g^2}{16\pi^2} F_{\mu\nu} \hat{F}_{\mu\nu}$$

$$\hat{F}_{\mu\nu} = \sum_{\alpha < \beta} F^{\alpha\beta}$$

Baryon number violating ops

Dim 6 $Q_{prst}^{dnql} = \sum_{\alpha\beta\gamma} \sum_{ij} \left(d_p^\alpha C u_r^\beta \right) \left(q_s^{i\gamma} C l_t^j \right)$

charge conjugation

↑ Flavor ↑ SU(3) ↑ SU(2) Flavor-prst

Q^{qqe}

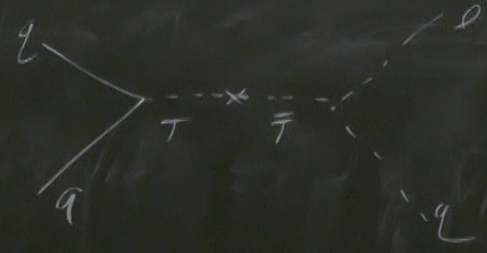
Q^{qqql}

Q^{dne}

$$\Gamma_p \sim C \frac{m_p^5}{\Lambda^4} \rightarrow \Lambda \sim 10^{16} \text{ GeV}$$

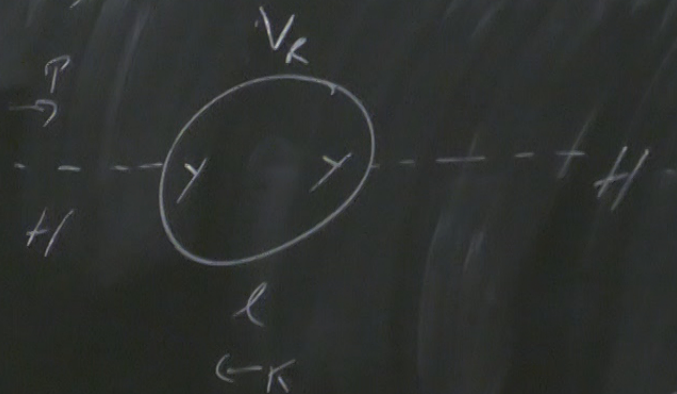
$\tau > 10^{33} \text{ years}$

SM \rightarrow extend to SU(5)



SU(2) triplet
 $T(3, 1)_{-1/3}$

Necessarily $\rightarrow k+p$



$$\Pi_{H^+H^-}^{(p)} = \frac{1}{2} |Y_V^r|^2 \int \frac{d^4k}{(2\pi)^4}$$

Neutrino mass $M_\nu > 10^{16} \text{ GeV}$

Progen number conservation

~~Ad=0~~

$$M_V \gg M_{\text{GL}}$$

$$= 2 |y_V|^2 \int \frac{d^4 \ell}{(2\pi)^4} \int_0^1 dx \frac{\ell^2 - p^2 x(1-x)}{[\ell^2 - \Delta]^2}$$

$$\Delta = m_V^2 (1-x) + m_\chi^2 x - p^2 x(1-x)$$

Motivation to $P \rightarrow \gamma\gamma\pi$

KEK Japan

$$\tau_{\text{proton}} = 8.2 \times 10^{33} \text{ years}$$

$$= -\frac{|Y_V|^2}{16\pi^2 \epsilon} (2m_\chi^2 + 2m_\nu^2 - p^2)$$

Sh. Higgs

$$L_V =$$

$$- \frac{|Y_V|^2}{48\pi^2} (3m_\chi^2 + 3m_\nu^2 - p^2)$$

(D.H.)[†](D.H.)

=> -

+ log terms

$$(2m_u^2 + 2m_d^2 - p^2)$$

Shift higg mass

$$\mathcal{L}_V = \frac{\lambda}{4} (H^\dagger H - v^2/2)^2$$

$$(3m_u^2 + 3m_d^2 - p^2)$$

$$(D_\mu H)^\dagger (D_\mu H)$$

$$\Rightarrow -\frac{\lambda}{4} v^2 H^\dagger H - \frac{|Y_V|^2 m_p^2}{8\pi^2} H^\dagger H$$

$$H^\dagger H \left[-\frac{\lambda}{4} v^2 - \frac{|Y_V|^2 m_p^2}{8\pi^2} \right]$$