

Title: The cosmology of electron scalars

Speakers: Zach Weiner

Series: Particle Physics

Date: November 28, 2023 - 11:00 AM

URL: <https://pirsa.org/23110081>

Abstract: The cosmic microwave background is a sensitive probe of early-Universe physics, and yet fundamental constants at recombination can differ from their present-day values due to degeneracies in the standard cosmological model. Such scenarios have been invoked to reconcile discrepant measurements of the present-day expansion rate, but even absent such motivation they raise the intriguing possibility of yet-undiscovered physics coupled directly to Standard Model particles. I will discuss theories in which a new scalar field shifts the electron's mass at early times; viable models are already stringently constrained by measurements of quasar absorption lines, the abundances of light elements, and the universality of free fall. I will show that the remaining parameter space is exactly that which allows not only the primary cosmic microwave background but also low-redshift distances to be consistent with observations. After presenting the results of parameter inference I will discuss additional cosmological and laboratory signatures of the model.

Zoom link <https://pitp.zoom.us/j/99705853481?pwd=MTZRWC9hREkvOXpiZkxCM3UvdnRNQT09>

The cosmology of electron scalars

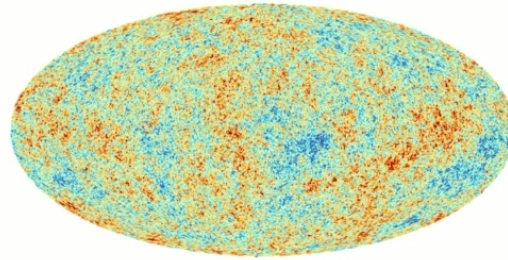
Zach Weiner • University of Washington

in collaboration with Masha Baryakhtar and Olivier Simon

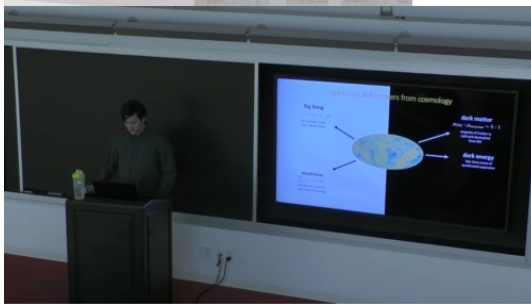
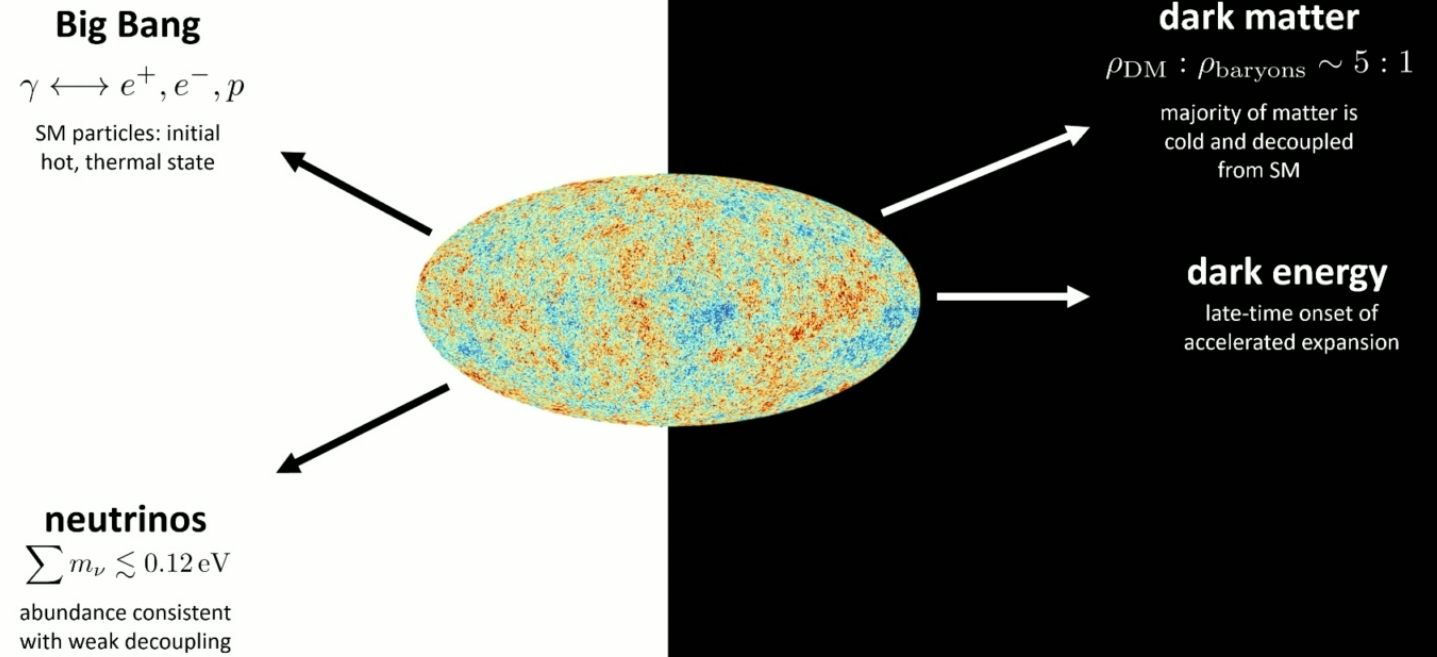
Perimeter Institute Particle Physics Seminar, 11/28/2023



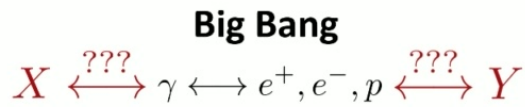
questions and answers from cosmology



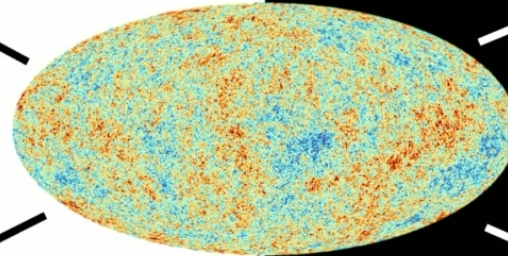
questions and answers from cosmology



questions and answers from cosmology



what else can we learn about (beyond) Standard Model particle physics?



dark matter

mass?
spin?
production mechanism?
connection to Standard Model?



dark energy

fundamental theory?
modified gravity?



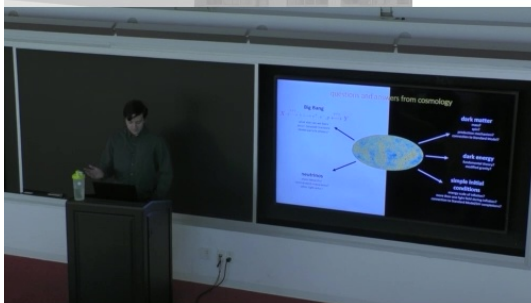
simple initial conditions

energy scale of inflation?
more than one light field during inflation?
connection to Standard Model/UV completions?



neutrinos

mass hierarchy?
nonstandard interactions?
other light relics?

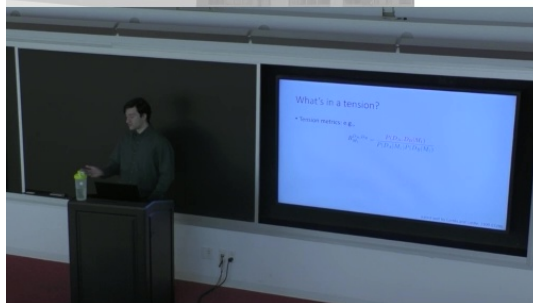


What's in a tension?

- Tension metrics: e.g.,

$$R_{M_1}^{D_A, D_B} = \frac{P(D_A, D_B | M_1)}{P(D_A | M_1)P(D_B | M_1)}$$

stated well by Cortès and Liddle, 2309.03286



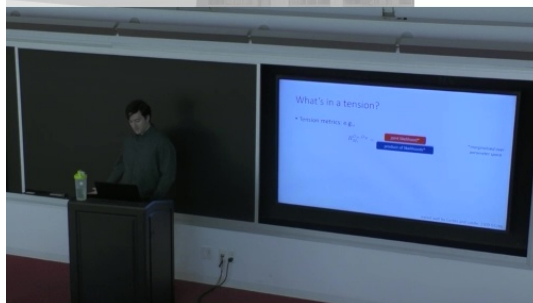
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$$R_{M_1}^{D_A, D_B} = \frac{\text{joint likelihood}^*}{\text{product of likelihoods}^*}$$

**marginalized over parameter space*

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What's in a tension?

- Tension metrics: e.g.,

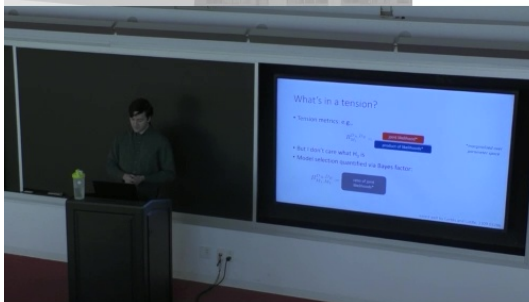
$$R_{M_1}^{D_A, D_B} = \frac{\text{joint likelihood}^*}{\text{product of likelihoods}^*}$$

**marginalized over parameter space*

- But I don't care what H_0 is
- Model selection quantified via Bayes factor:

$$B_{M_1, M_2}^{D_A, D_B} = \text{ratio of joint likelihoods}^*$$

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What's in a tension?

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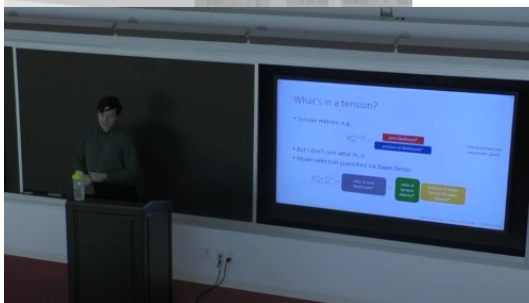
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$$B_{M_1, M_2}^{D_A, D_B} = \text{ratio of joint likelihoods}^* = \text{ratio of tension metrics}^* \text{ product of Bayes factors for each dataset}^*$$

stated well by Cortès and Liddle, 2309.03286



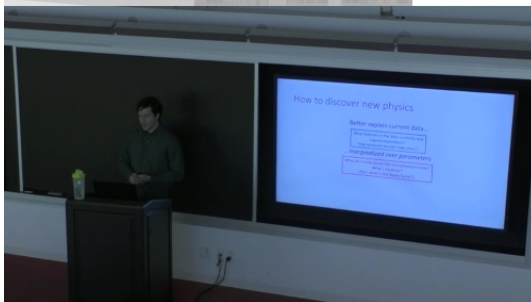
How to discover new physics

Better explain current data...

What features in the data currently lack
a good explanation?
How seriously should I take them?

...marginalized over parameters

What do I know about the microphysical model?
What's my prior?
(Also: what is the Bayes factor?)



How to discover new physics

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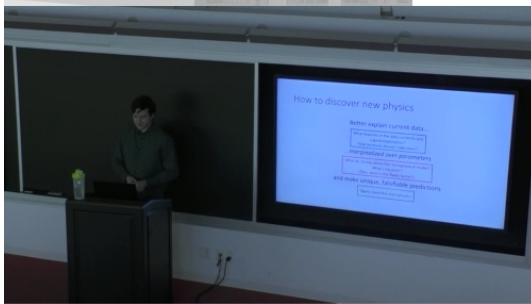
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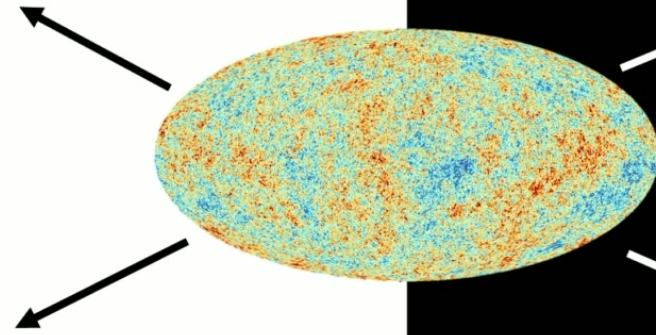
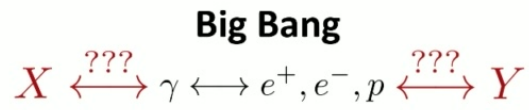
What do I know about the microphysical model?
What's my prior?
(Also: what is the Bayes factor?)

and make unique, falsifiable predictions

Again, need the microphysics



questions and answers from cosmology



first signature of
"beyond- Λ CDM"
dark sector?

dark matter
interactions with self/dark
energy/neutrinos/dark
radiation?

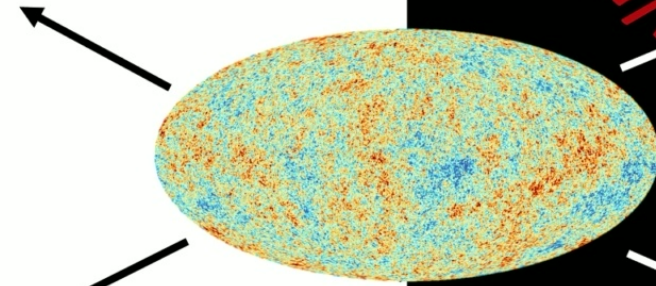
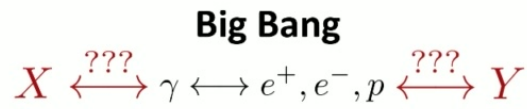
dark energy
dynamical?
interacting?

**complex initial
conditions**

neutrinos
simply add more radiation?
strong self-interactions?



questions and answers from cosmology



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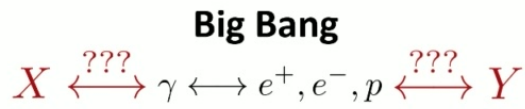
**another dark
component?...**

neutrinos
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strong self-interactions?

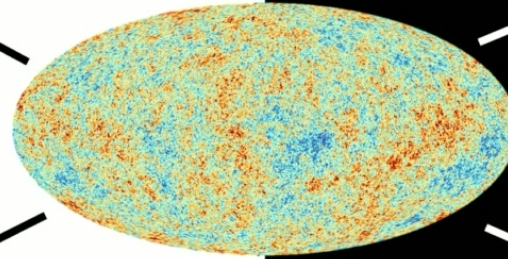
few/no independent probes



questions and answers from cosmology



opportunities beyond cosmology in laboratory, astrophysics!



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simply add more radiation?
strong self-interactions?

first signature of "beyond- Λ CDM" dark sector?

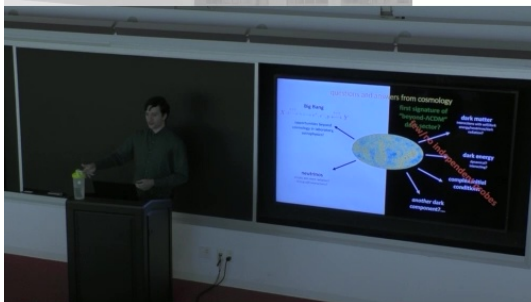
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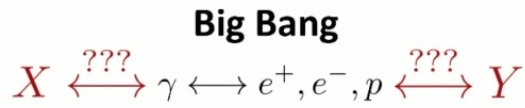
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another dark component?...

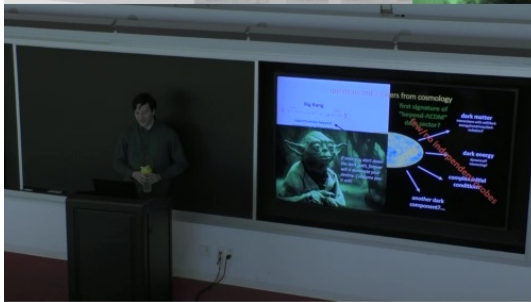
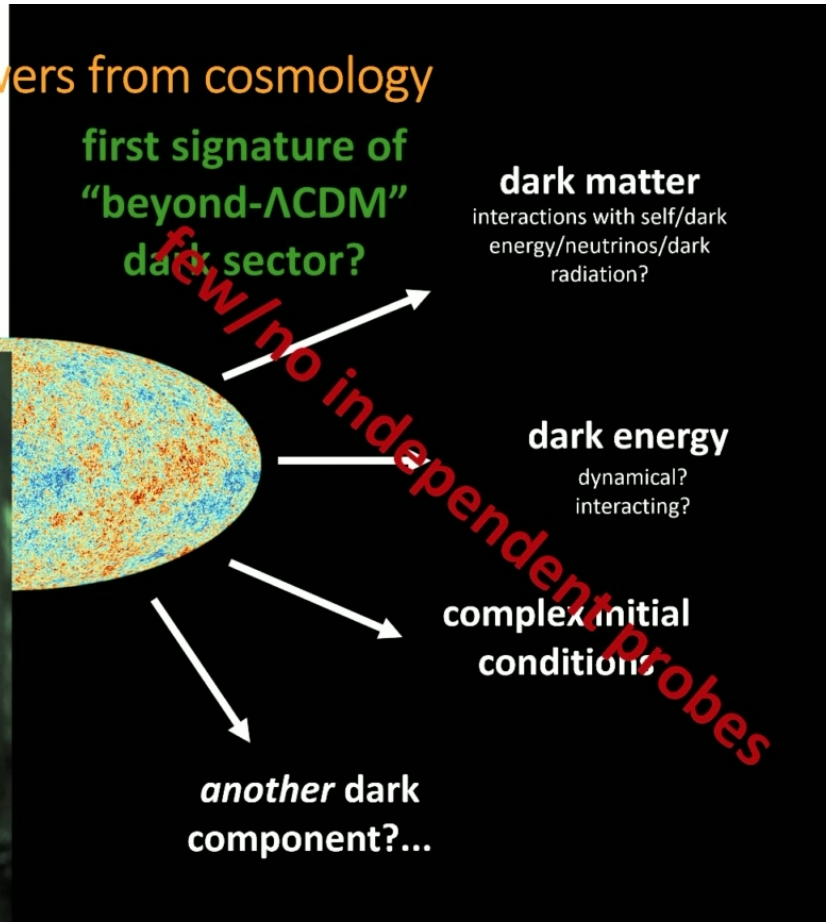
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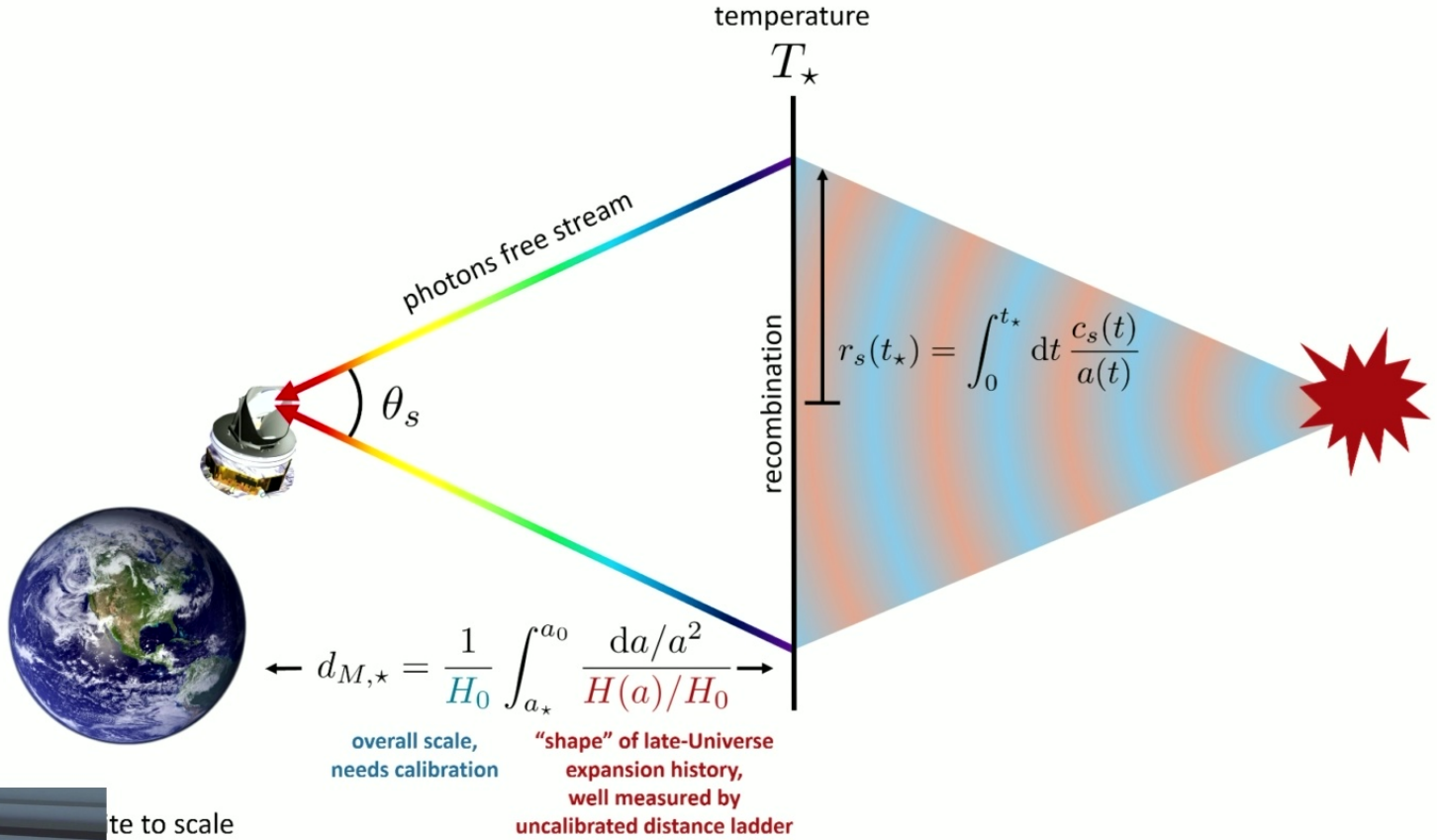
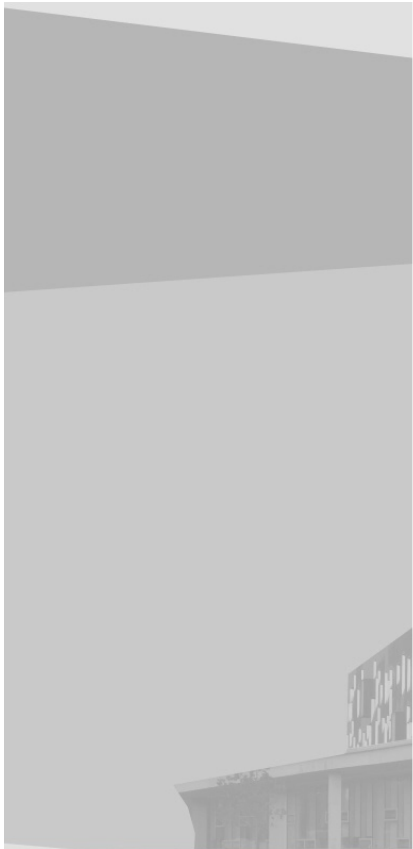


questions and answers from cosmology

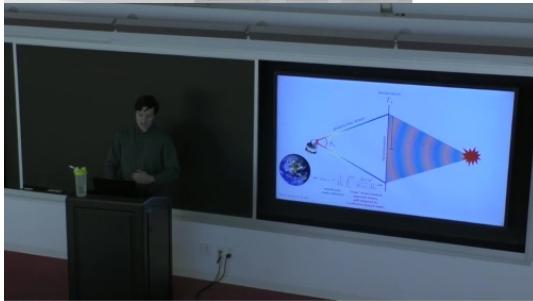


opportunities beyond cosmology in laboratory





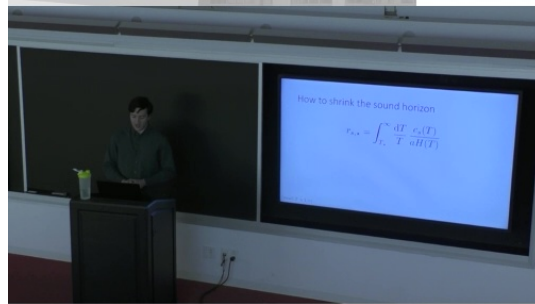
te to scale



How to shrink the sound horizon

$$r_{s,\star} = \int_{T_\star}^{\infty} \frac{dT}{T} \frac{c_s(T)}{aH(T)}$$

$T \propto 1/a$)



How to shrink the sound horizon

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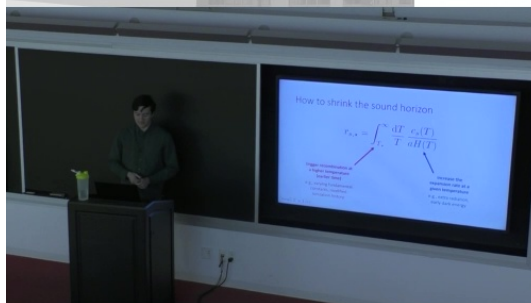
**trigger recombination at
a higher temperature
(earlier time)**

e.g., varying fundamental
constants, modified
ionization history

**increase the
expansion rate at a
given temperature**

e.g., extra radiation,
early dark energy

$T \propto 1/a$)



How to shrink the sound horizon

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(hard to imagine changing sound speed evolution without ruining CMB peaks)

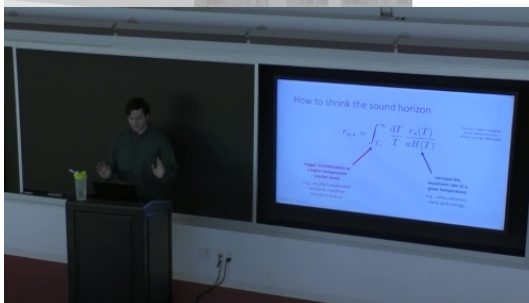
trigger recombination at a higher temperature (earlier time)

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Proposal: varying fundamental constants

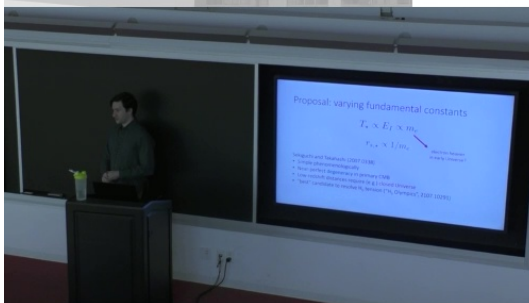
$$T_{\star} \propto E_I \propto m_e$$

$$r_{s,\star} \propto 1/m_e$$

electron heavier
in early Universe?

Sekiguchi and Takahashi (2007.0338)

- Simple phenomenologically
- Near-perfect **degeneracy** in primary CMB
- Low-redshift distances require (e.g.) **closed Universe**
- "best" candidate to resolve H_0 tension ("H₀ Olympics", 2107.10291)



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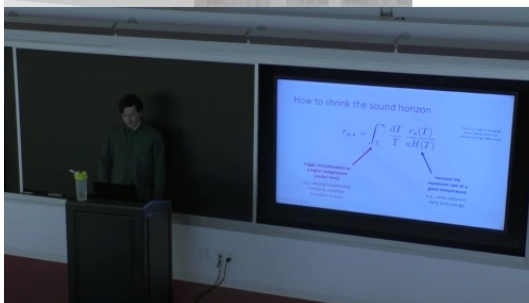
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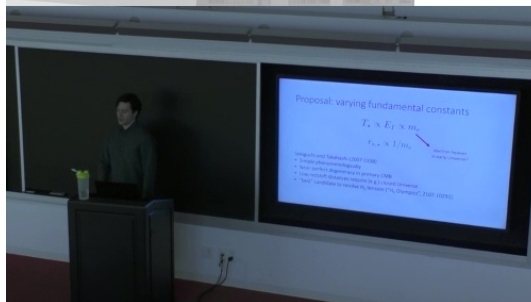
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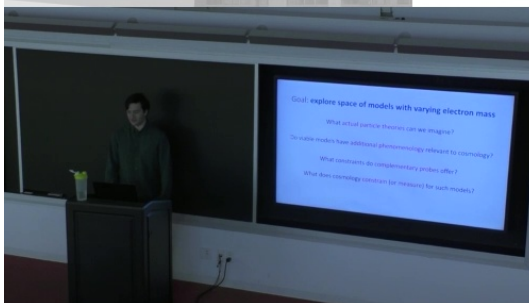
Goal: **explore space of models with varying electron mass**

What **actual particle theories** can we imagine?

Do viable models have **additional phenomenology** relevant to cosmology?

What constraints do **complementary probes** offer?

What does cosmology **constrain** (or **measure**) for such models?

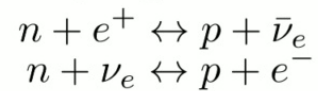


Varying electron mass: probes

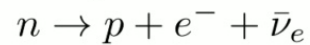
big bang nucleosynthesis

Altered rates of

- neutron \rightarrow proton reaction during weak decoupling



- neutron decay after



Heavier electron **increases neutron abundance** at ${}^4\text{He}$ formation

$$\frac{\Delta Y_p}{Y_p} = 0.42 \frac{\Delta m_e}{m_e}$$

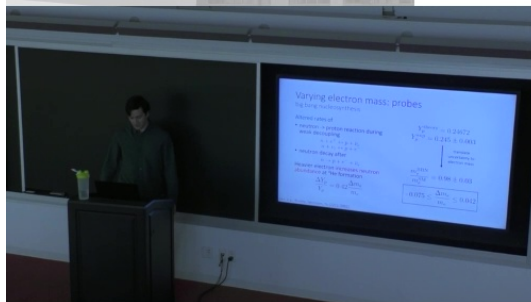
$$Y_p^{\text{theory}} = 0.24672$$
$$Y_p^{\text{exp}} = 0.245 \pm 0.003$$

translate
uncertainty to
electron mass

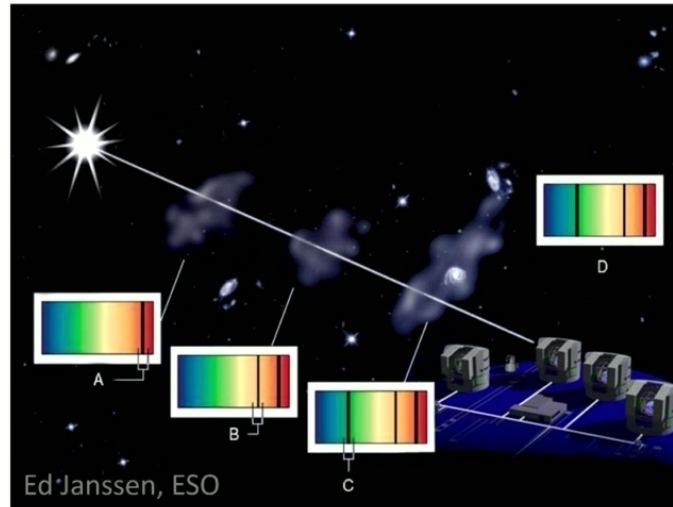
$$\frac{m_e^{\text{BBN}}}{m_e^{\text{SM}}} = 0.98 \pm 0.03$$

$$-0.075 \leq \frac{\Delta m_e}{m_e} \leq 0.042$$

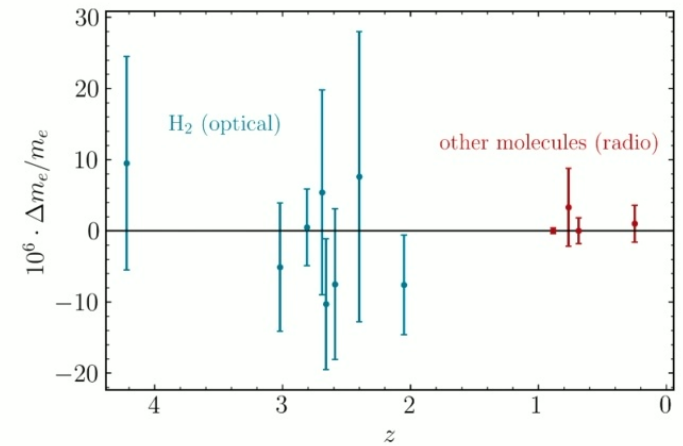
Bouley, Sørensen, Yu (2211.0982)



Varying electron mass: probes quasar absorption lines



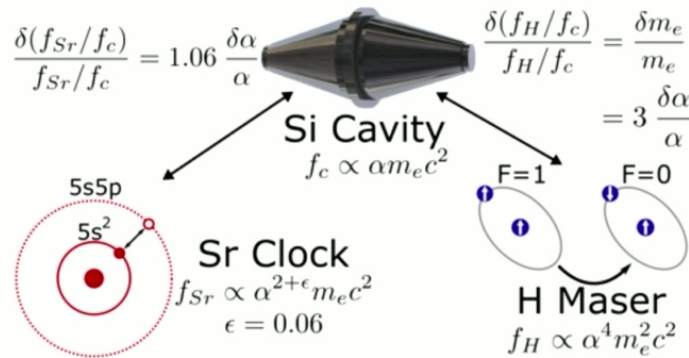
Measure molecular absorption lines along quasar sight lines



PPM measurements of
fundamental constants



Varying electron mass: probes atomic clocks and pulsar timing

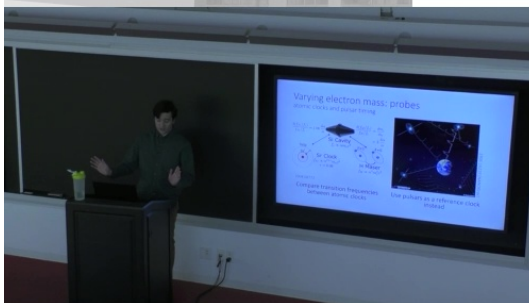


2008.08773

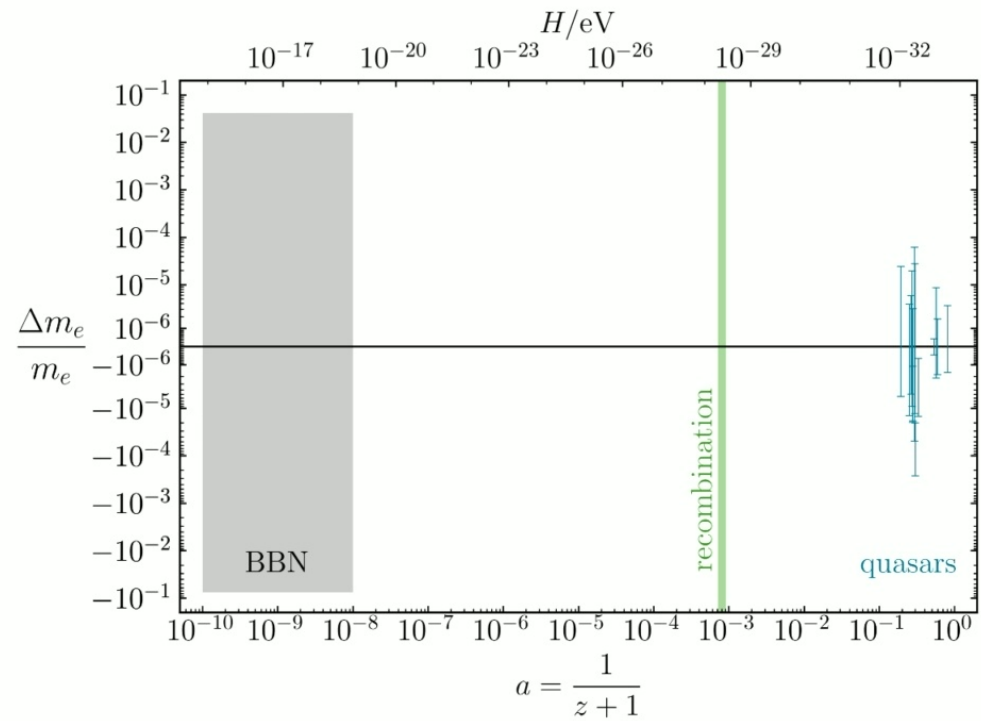
Compare transition frequencies
between atomic clocks



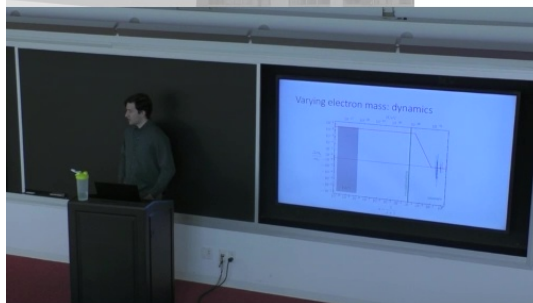
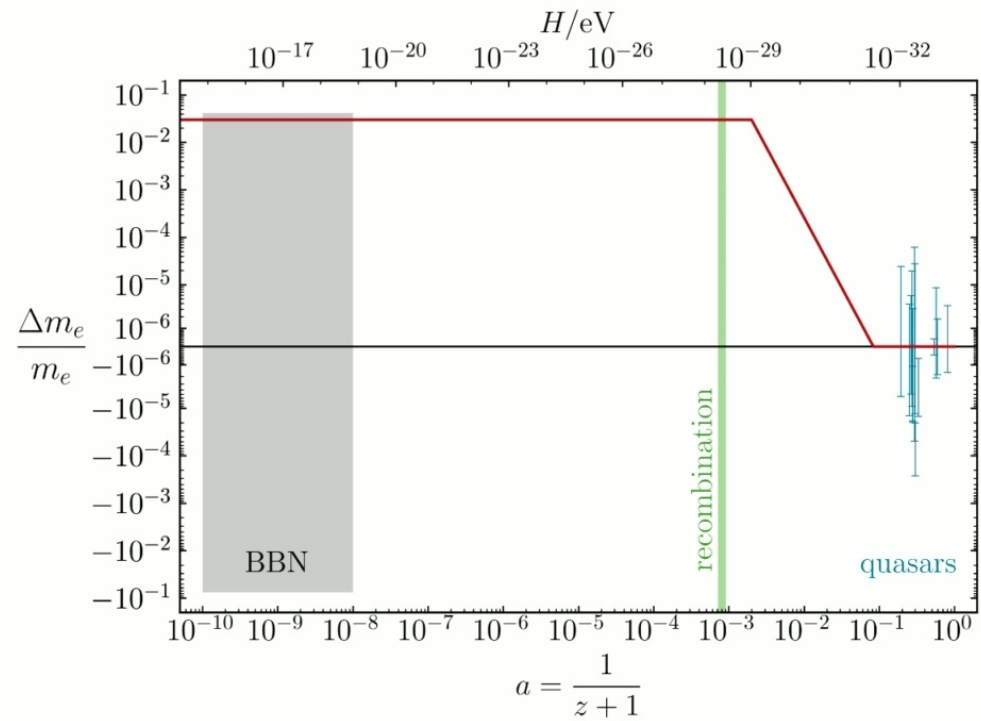
Use pulsars as a reference clock
instead



Varying electron mass: dynamics



Varying electron mass: dynamics



Varying electron mass: scalar models

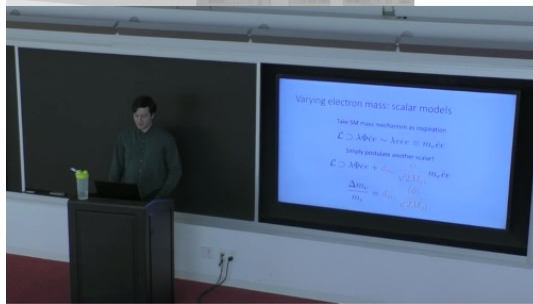
Take SM mass mechanism as inspiration

$$\mathcal{L} \supset \lambda \Phi \bar{e} e \sim \lambda v \bar{e} e \equiv m_e \bar{e} e$$

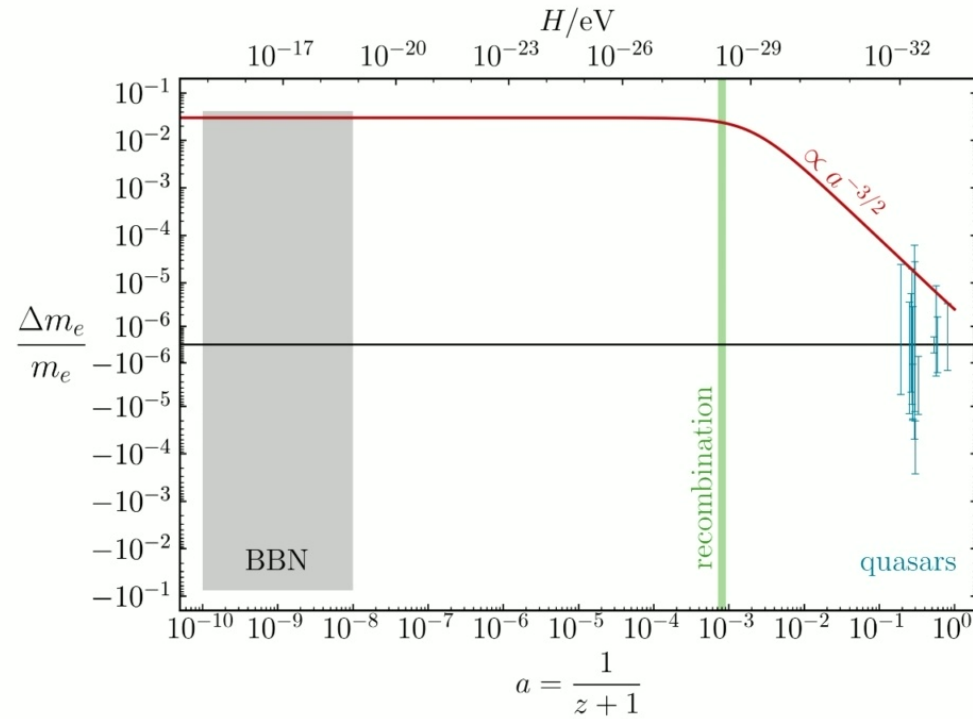
Simply postulate another scalar!

$$\mathcal{L} \supset \lambda \Phi \bar{e} e + d_{m_e} \frac{\phi}{\sqrt{2} M_{\text{pl}}} m_e \bar{e} e$$

$$\frac{\Delta m_e}{m_e} = d_{m_e} \frac{\langle \phi \rangle}{\sqrt{2} M_{\text{pl}}}$$



Varying electron mass: scalar models



Klein-Gordon equation
 $\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$
 $H > m: \phi(t) \text{ constant}$
 $H < m: \phi(t) \propto a^{-3/2}$

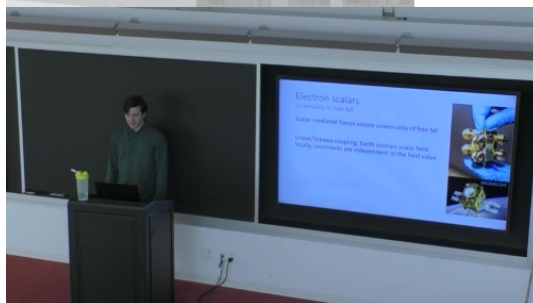


Electron scalars

universality of free fall

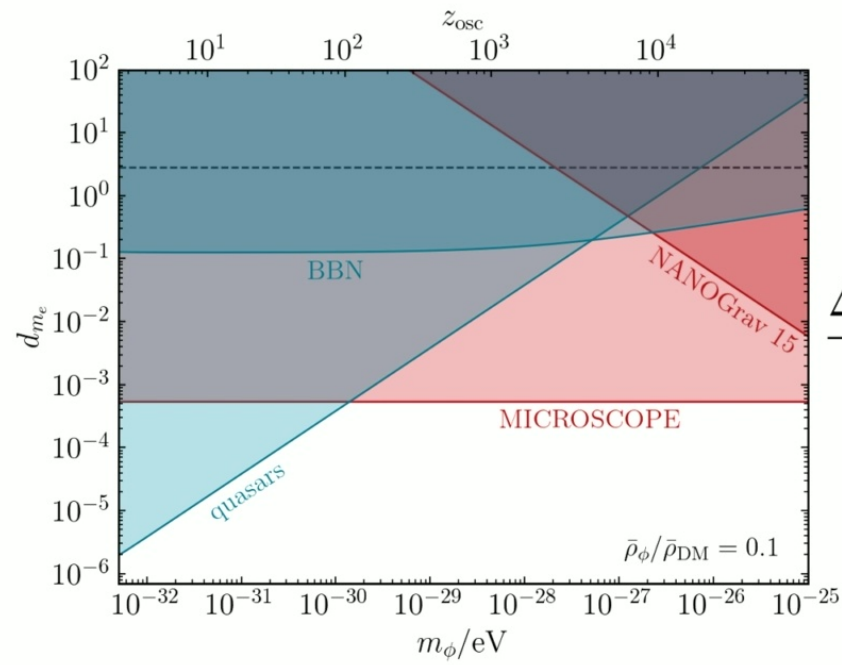
Scalar-mediated forces violate universality of free fall

Linear/Yukawa coupling: Earth sources scalar field locally, constraints are independent of the field value



Electron scalars

linear coupling

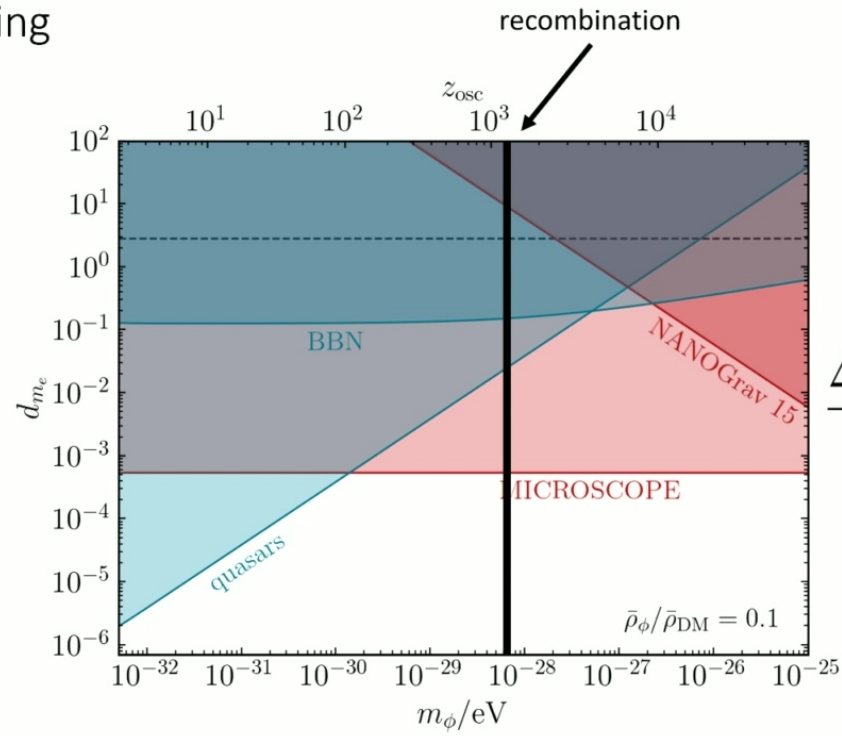


$$\frac{\Delta m_e}{m_e} = d_{m_e} \frac{\langle \phi \rangle}{M_{\text{pl}}}$$

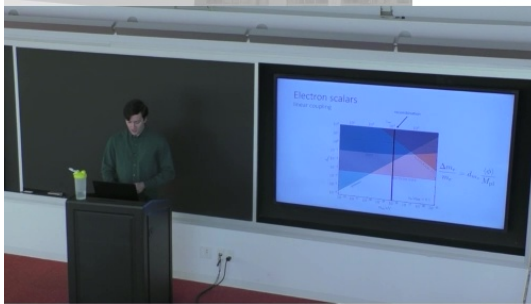


Electron scalars

linear coupling

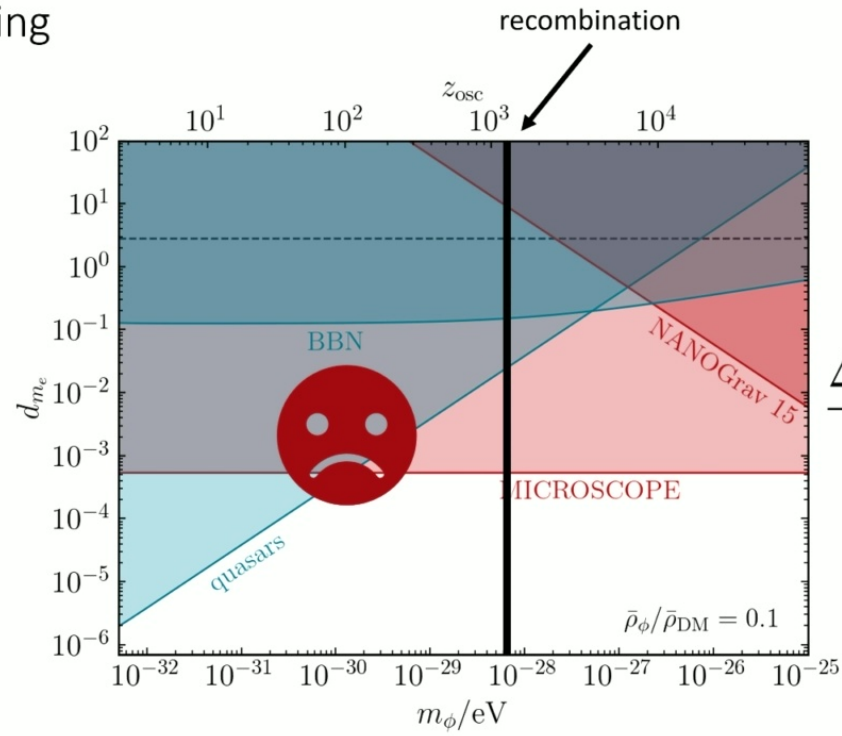


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Electron scalars

linear coupling



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What about an axion(like particle)?

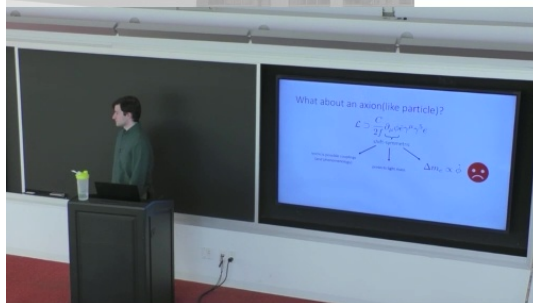
$$\mathcal{L} \supset \frac{C}{2f} \partial_\mu \phi \bar{e} \gamma^\mu \gamma^5 e$$

shift-symmetric

restricts possible couplings
(and phenomenology)

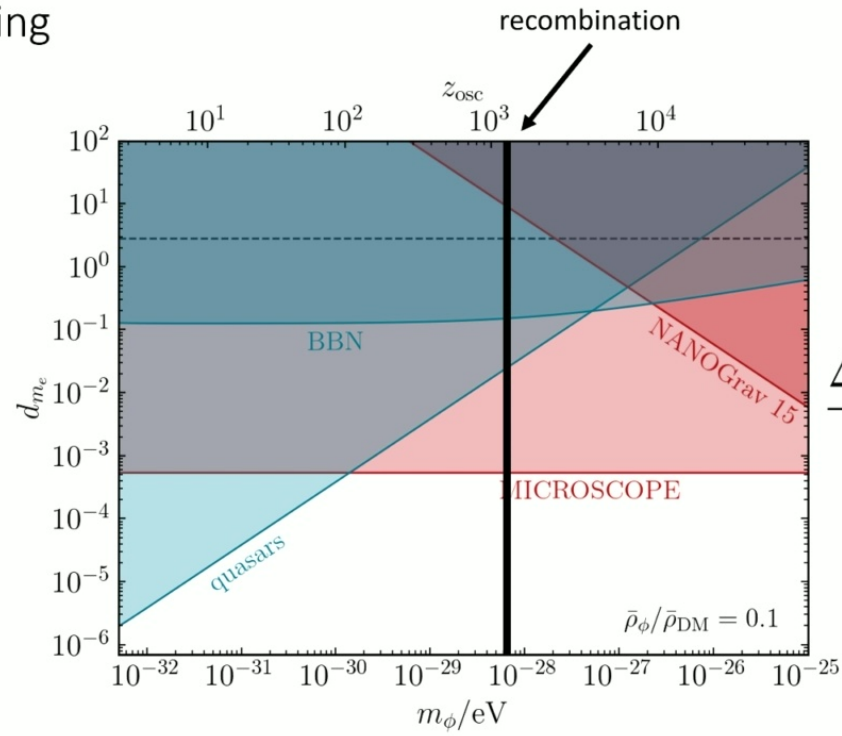
protects light mass

$$\Delta m_e \propto \dot{\phi}$$

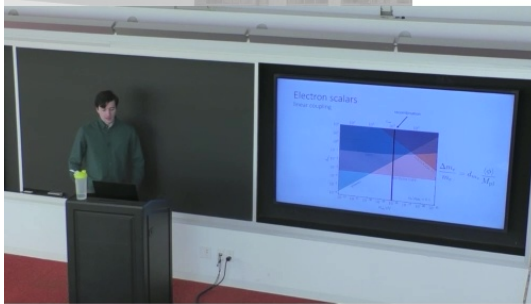


Electron scalars

linear coupling



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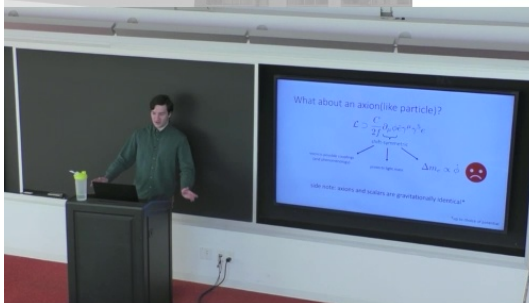
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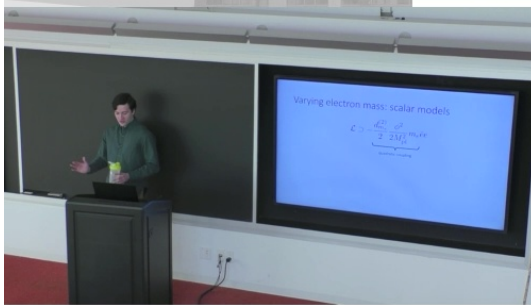
side note: axions and scalars are gravitationally identical*

*up to choice of potential

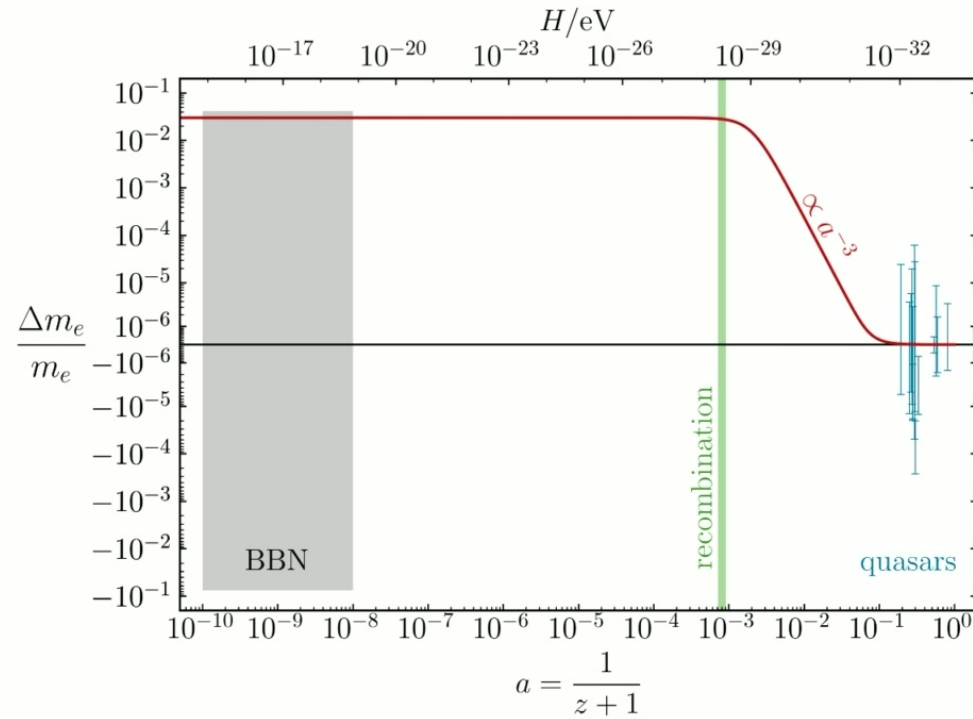


Varying electron mass: scalar models

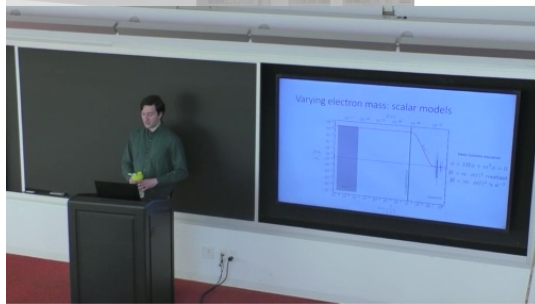
$$\mathcal{L} \supset - \underbrace{\frac{d_{m_e}^{(2)}}{2} \frac{\phi^2}{2M_{\text{pl}}^2}}_{\text{quadratic coupling}} m_e \bar{e}e$$



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 $H < m: \phi(t)^2 \propto a^{-3}$



Electron scalars

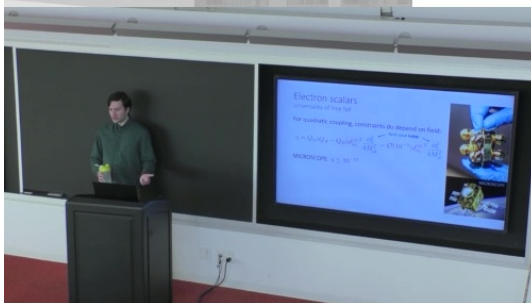
universality of free fall

For quadratic coupling, constraints do depend on field:

$$\eta \approx Q_{\oplus}(Q_A - Q_B)d_{m_e}^{(2)2} \frac{\phi_0^2}{4M_{\text{pl}}^2} = \mathcal{O}(10^{-9})d_{m_e}^{(2)2} \frac{\phi_0^2}{4M_{\text{pl}}^2}$$

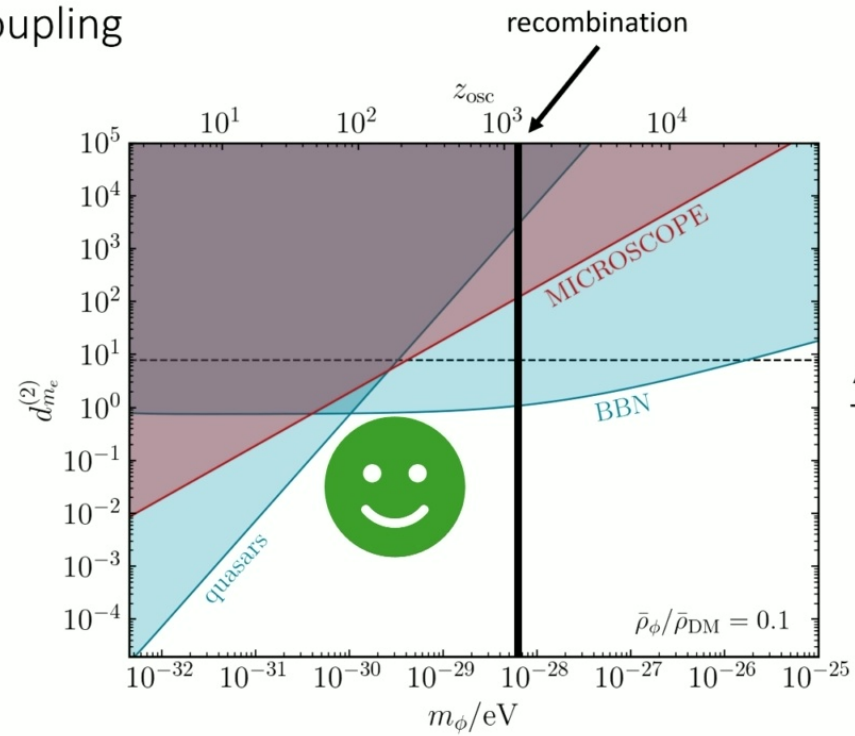
← field value today →

MICROSCOPE: $\eta \lesssim 10^{-15}$



Electron scalars

quadratic coupling



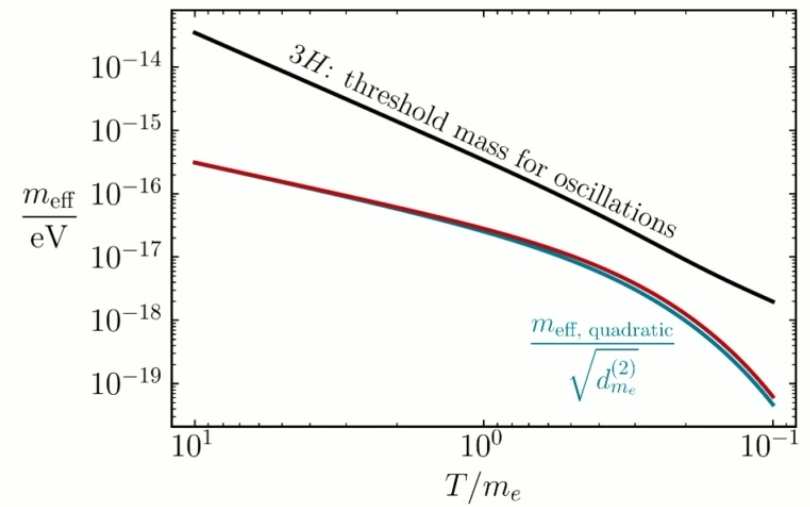
$$\frac{\Delta m_e}{m_e} = d_{m_e}^{(2)} \frac{\langle \phi \rangle^2}{4M_{pl}^2}$$



Electron scalars

thermal effects in early Universe

Electron/positron plasma induces
a **temperature-dependent mass**
for the scalar

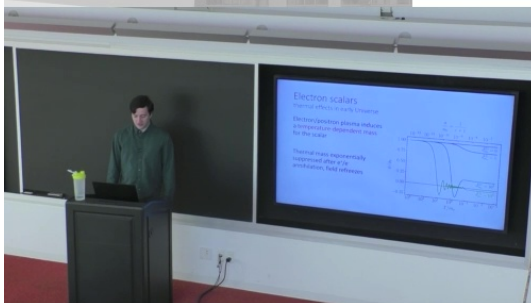
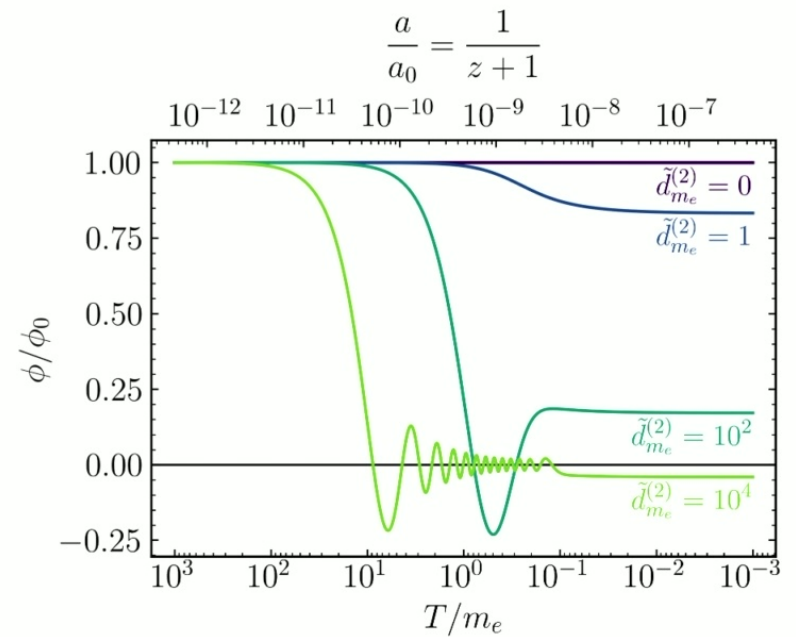


Electron scalars

thermal effects in early Universe

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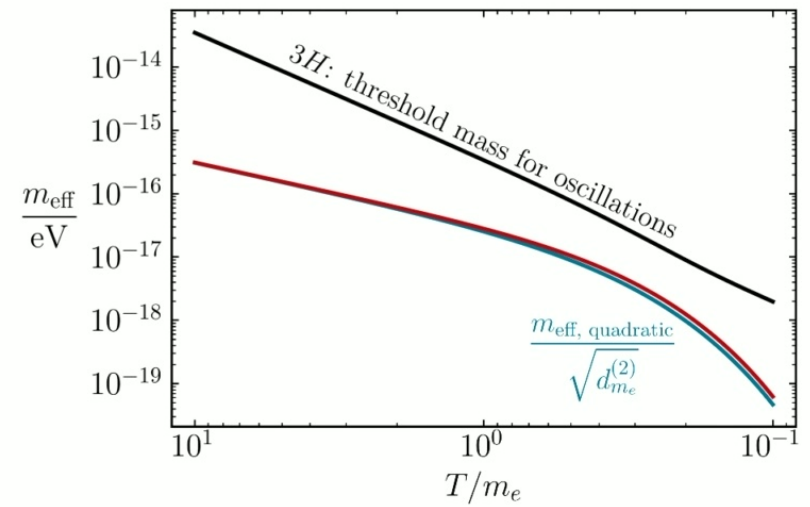
Thermal mass exponentially suppressed after e^+/e^- annihilation, field refreezes



Electron scalars

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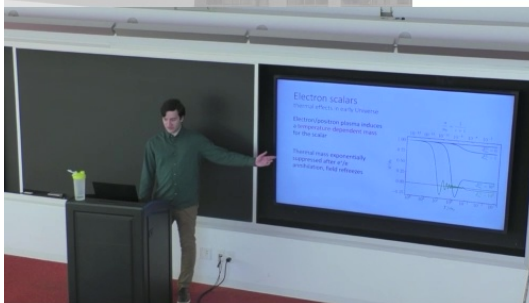
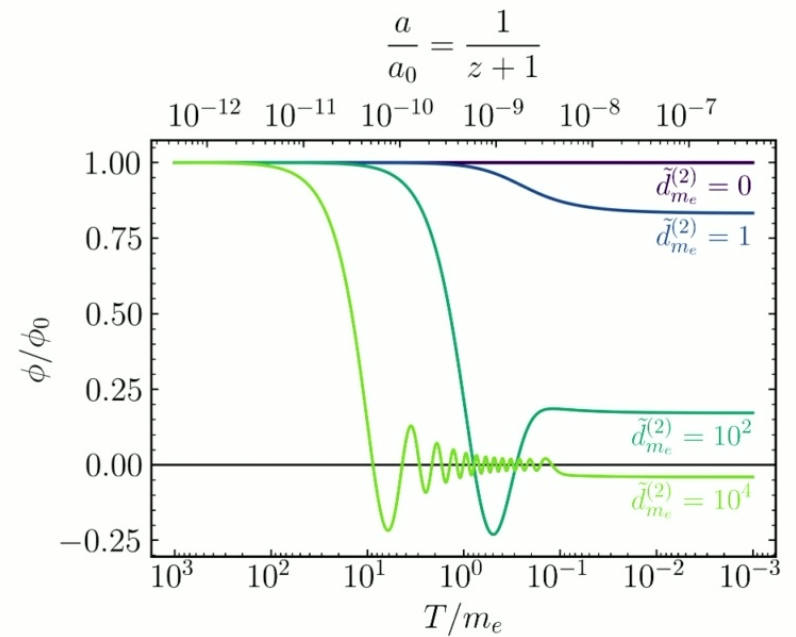


Electron scalars

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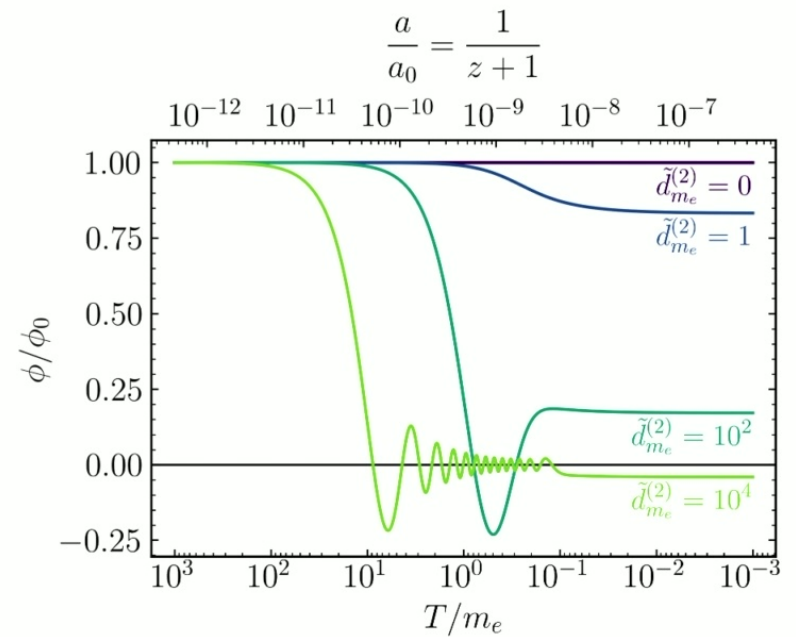
Electron scalars

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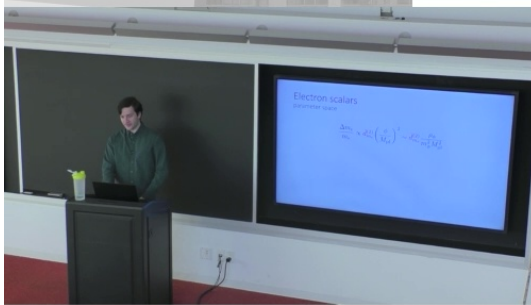
Avoid with **couplings \lesssim few**



Electron scalars

parameter space

$$\frac{\Delta m_e}{m_e} \propto \tilde{d}_{m_e}^{(2)} \left(\frac{\phi}{M_{\text{pl}}} \right)^2 \sim \tilde{d}_{m_e}^{(2)} \frac{\rho_\phi}{m_\phi^2 M_{\text{pl}}^2}$$



Electron scalars

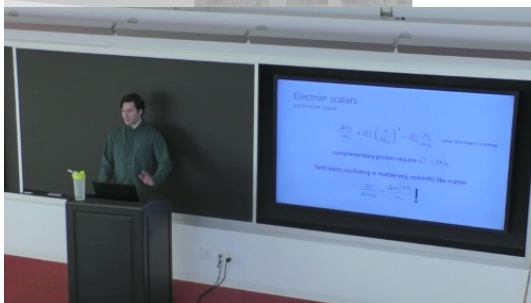
parameter space

$$\frac{\Delta m_e}{m_e} \propto \tilde{d}_{m_e}^{(2)} \left(\frac{\phi}{M_{\text{pl}}} \right)^2 \sim \tilde{d}_{m_e}^{(2)} \frac{\rho_\phi}{\rho_{\text{tot}}} \quad (\text{when field begins oscillating})$$

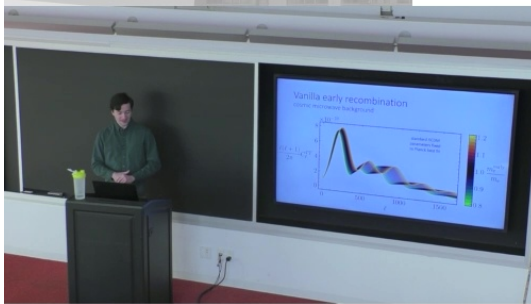
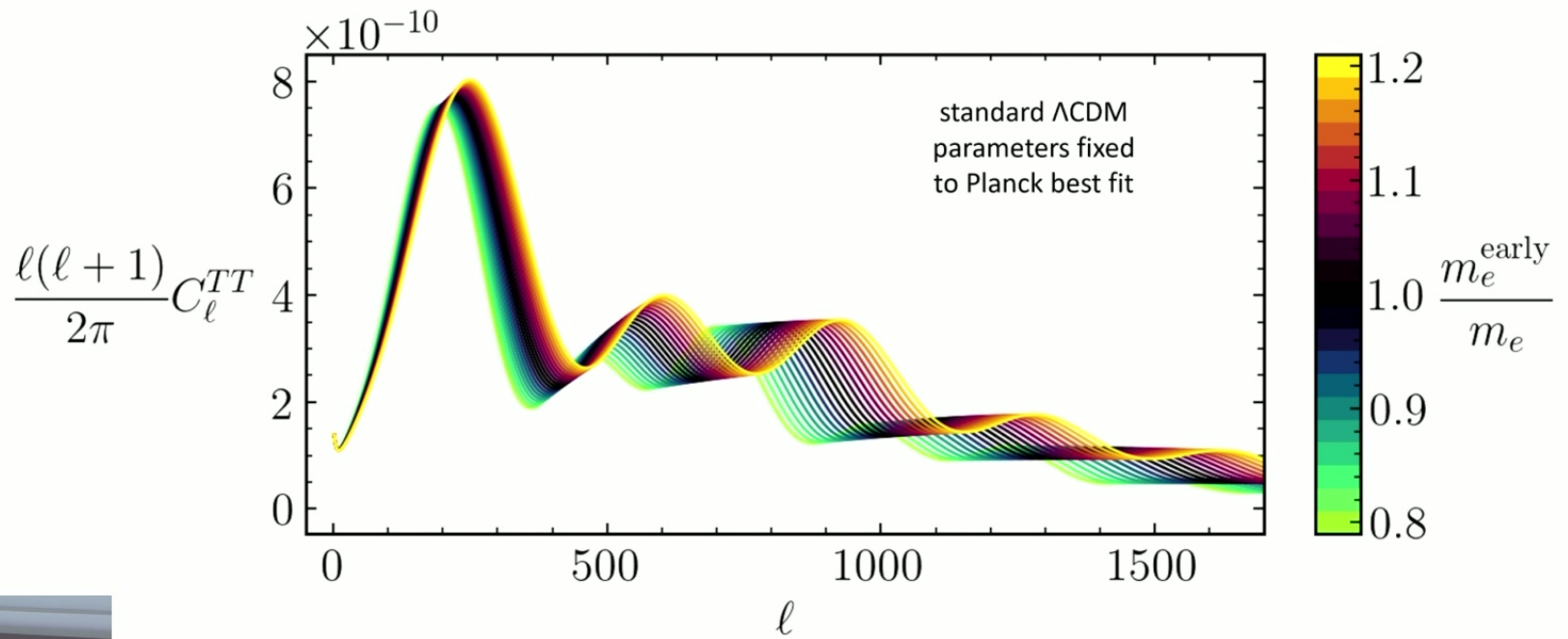
complementary probes require $\tilde{d}_{m_e}^{(2)} \lesssim \mathcal{O}(1)$

field starts oscillating in matter era, redshifts like matter

$$\frac{\rho_\phi}{\rho_{\text{CDM}}} \sim \frac{\Delta m_e^{\text{early}}}{m_e} \quad !$$



Vanilla early recombination cosmic microwave background



Vanilla early recombination sound horizon

angle subtended
by acoustic
oscillations at
recombination

$$\theta_s =$$

$$\theta_s = \frac{r_{s,*}}{d_{M,*}} = \frac{\frac{1}{H_0} \int_0^{a_*} \frac{da}{a^2} \frac{c_s(a)}{H(a)/H_0}}{\frac{1}{H_0} \int_{a_*}^{a_0} \frac{da/a^2}{H(a)/H_0}}$$

“sound horizon”
comoving distance propagating sound
waves traveled by recombination

overall scale

“shape” of early-Universe
expansion history

= $(1.0411 \pm 0.0003) \times 10^{-2}$

overall scale

comoving distance traveled
after recombination

“shape” of late-Universe
expansion history



Vanilla early recombination

sound horizon

$$c_s^2 = \frac{1}{3(1+R)}$$

$$R = \frac{3\omega_b}{4\omega_\gamma} \frac{a}{a_0}$$

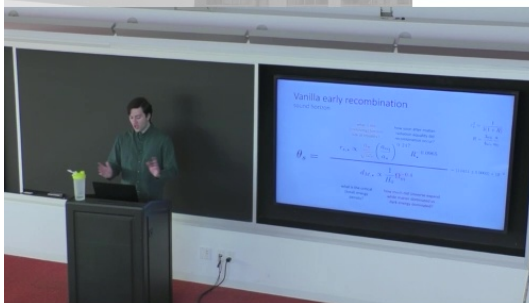
what is the
(comoving) horizon
size at equality?

how soon after matter-
radiation equality did
recombination occur?

$$\theta_s = \frac{r_{s,\star} \propto \frac{a_\star}{\sqrt{\omega_r}} \left(\frac{a_{\text{eq}}}{a_\star} \right)^{0.247} R_\star^{-0.0965}}{d_{M,\star} \propto \frac{1}{H_0} \Omega_m^{-0.4}} = (1.0411 \pm 0.0003) \times 10^{-2}$$

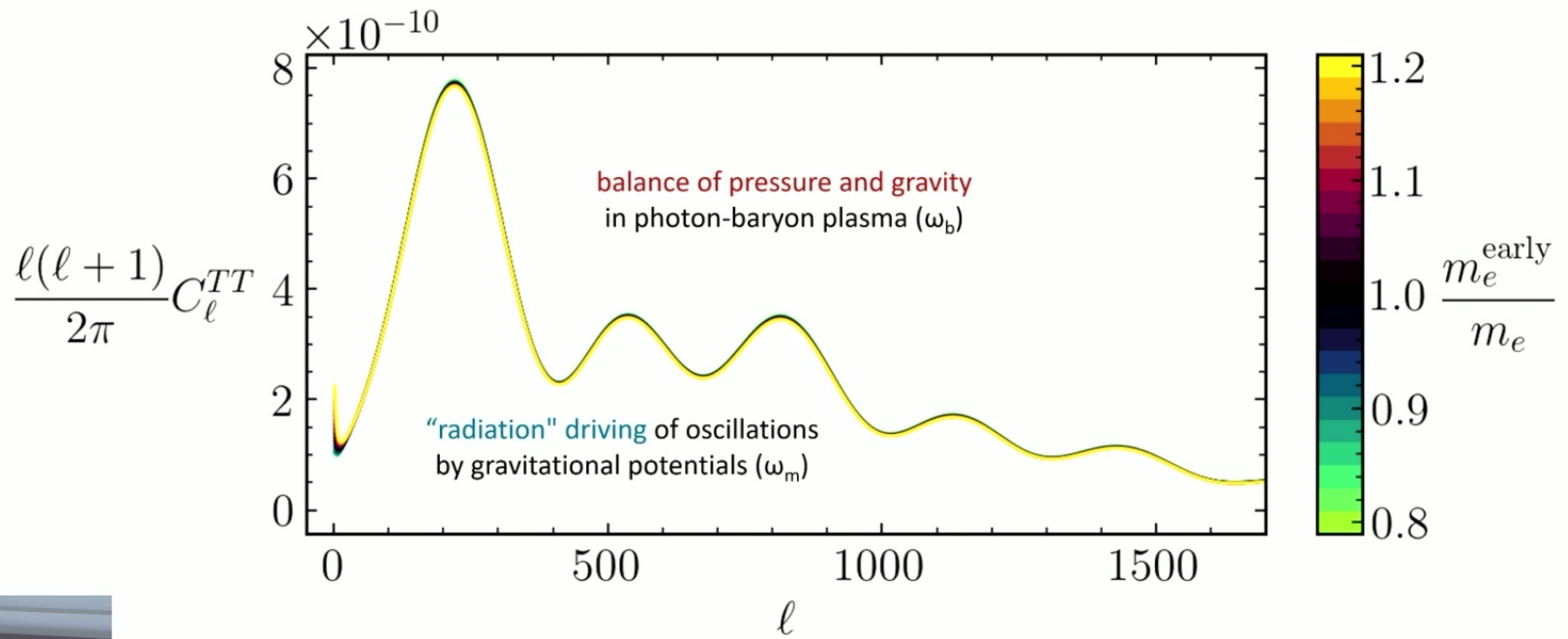
what is the critical
(total) energy
density?

how much did Universe expand
while matter dominated vs.
dark-energy dominated?



Vanilla early recombination

net result



Vanilla early recombination

diffusion damping

$$r_{D,*}^2 = \frac{1}{6} \int_0^{a_*} \frac{R^2 + \frac{16}{15}(1+R)}{(1+R)^2} \frac{1}{a^2 H} da/a$$

length scale below which photons diffuse

already fixed function of a/a_* when increasing baryon density $\propto m_e$

$\propto a_*^{-3} \omega_b \propto a_*^{-4} R_*$

$n_e \sigma_T \propto 1/m_e^2$

already fixed function of a/a_* when increasing net matter density $\propto m_e$



Vanilla early recombination

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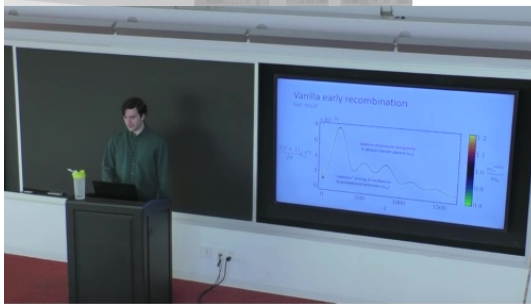
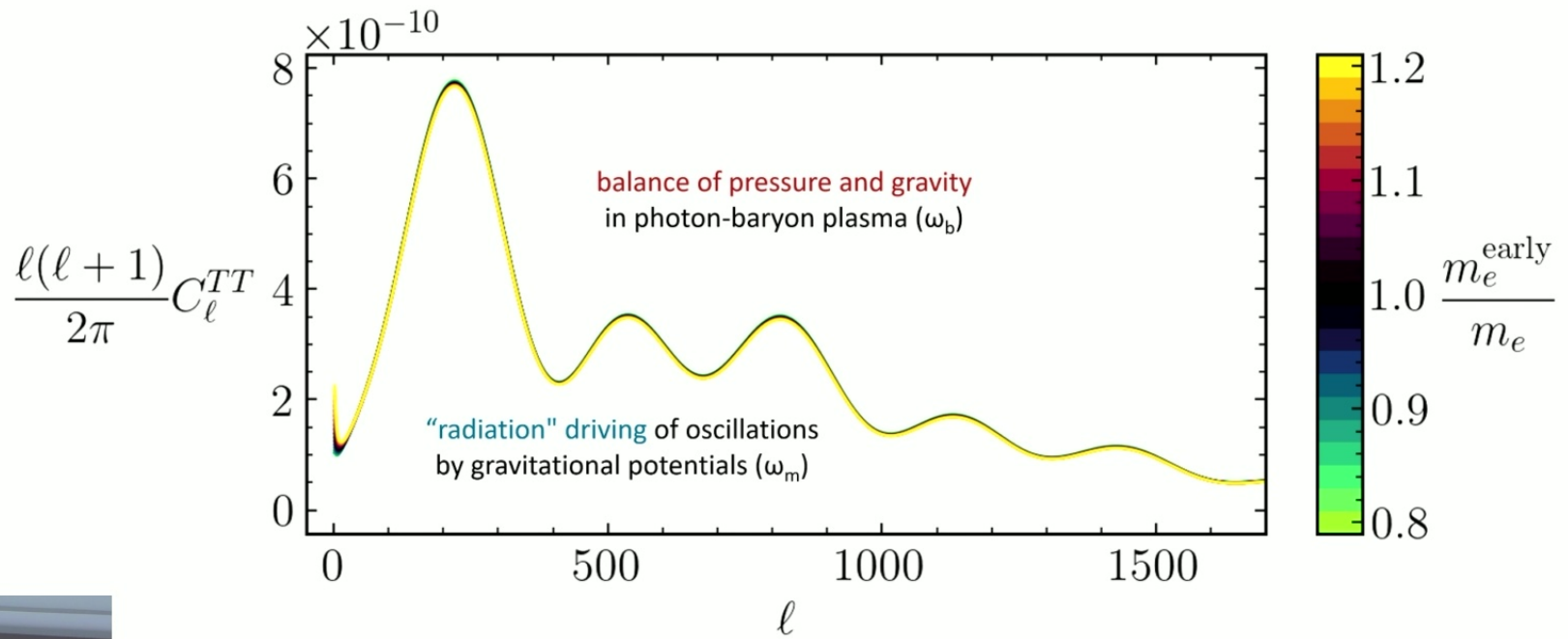
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$r_{D,\star} \propto a_\star$
 $r_{D,\star} \propto r_{s,\star}$ for free!



Vanilla early recombination

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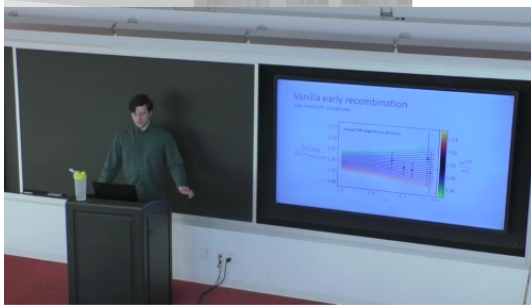
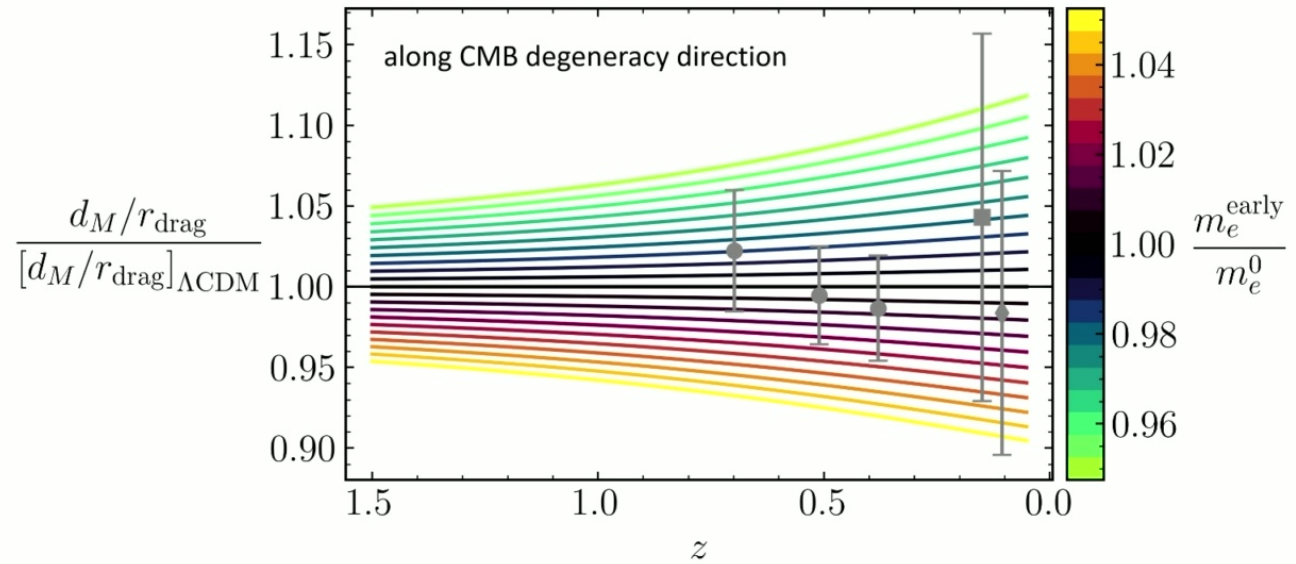
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Vanilla early recombination

low-redshift distances



Vanilla early recombination

low-redshift distances

$$d_M^{\text{flat}}(a) = \frac{1}{H_0} \int_a^{a_0} \frac{da'/a'^2}{H(a')/H_0}$$

overall scale, needs calibration **"shape" of late-Universe expansion history**

Original proposal (2007.0338): add curvature

recall: complementary probes require

$$d_M^{\text{curved}}(a) = \frac{\sin [\sqrt{-\Omega_k} H_0 d_M^{\text{flat}}(a)]}{\sqrt{-\Omega_k} H_0}$$

$$\frac{\rho_\phi}{\rho_{\text{CDM}}} \sim \frac{\Delta m_e^{\text{early}}}{m_e}$$

matching CMB **misbalanced matter and dark energy**



Vanilla early recombination

low-redshift distances

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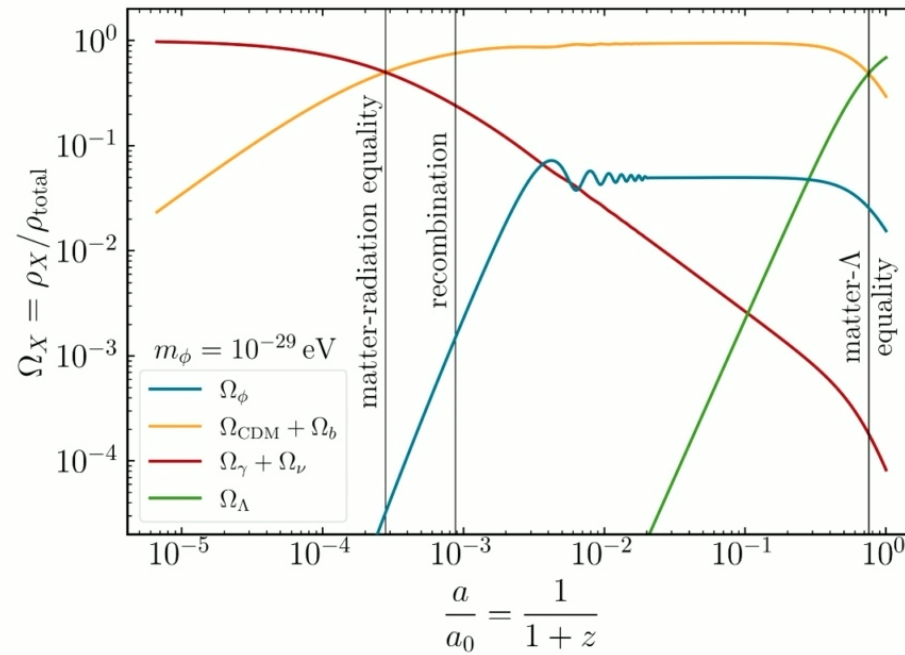
matching CMB **misbalanced matter and dark energy**

but scalar field becomes matterlike when it starts oscillating



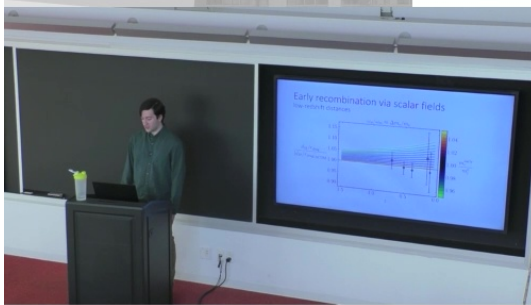
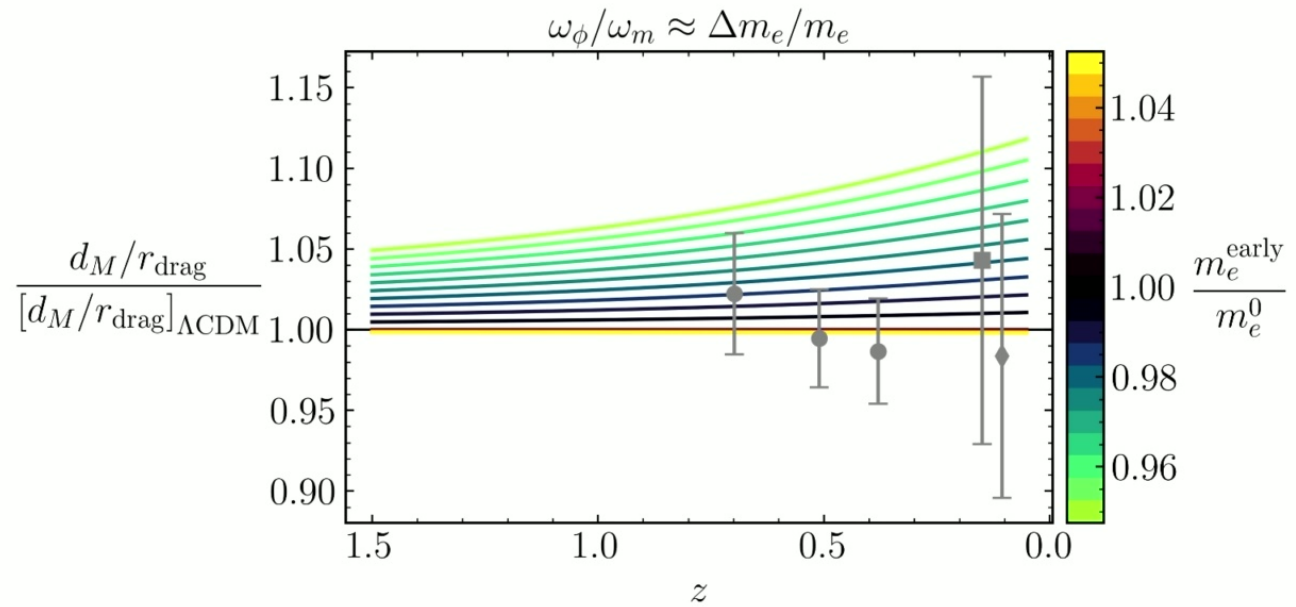
Early recombination via scalar fields

low-redshift distances

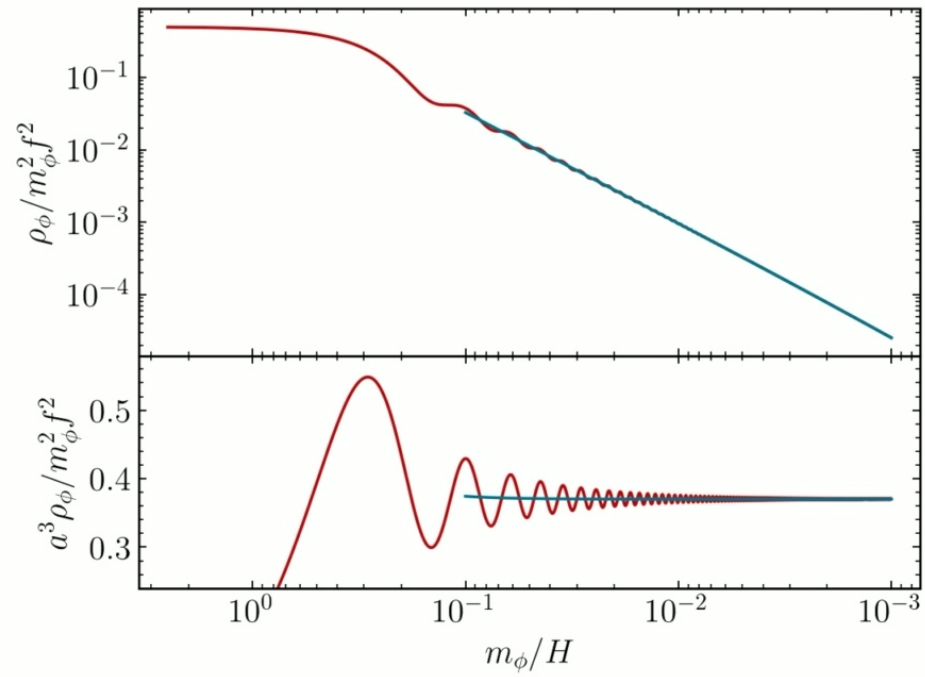


Early recombination via scalar fields

low-redshift distances



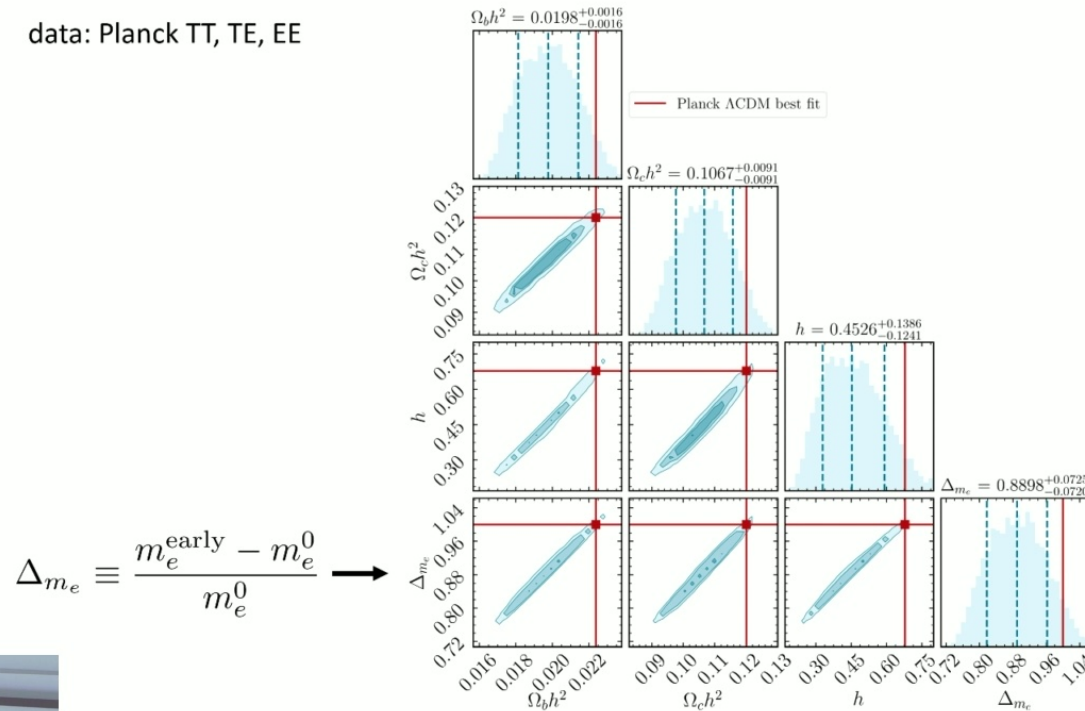
Scalar fields as fluids



The CMB prefers... late recombination???

data: Planck TT, TE, EE

Note: results effectively identical in vanilla early recombination

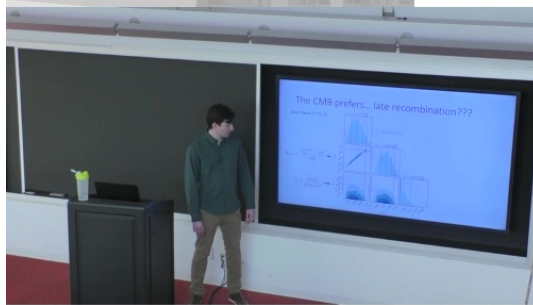
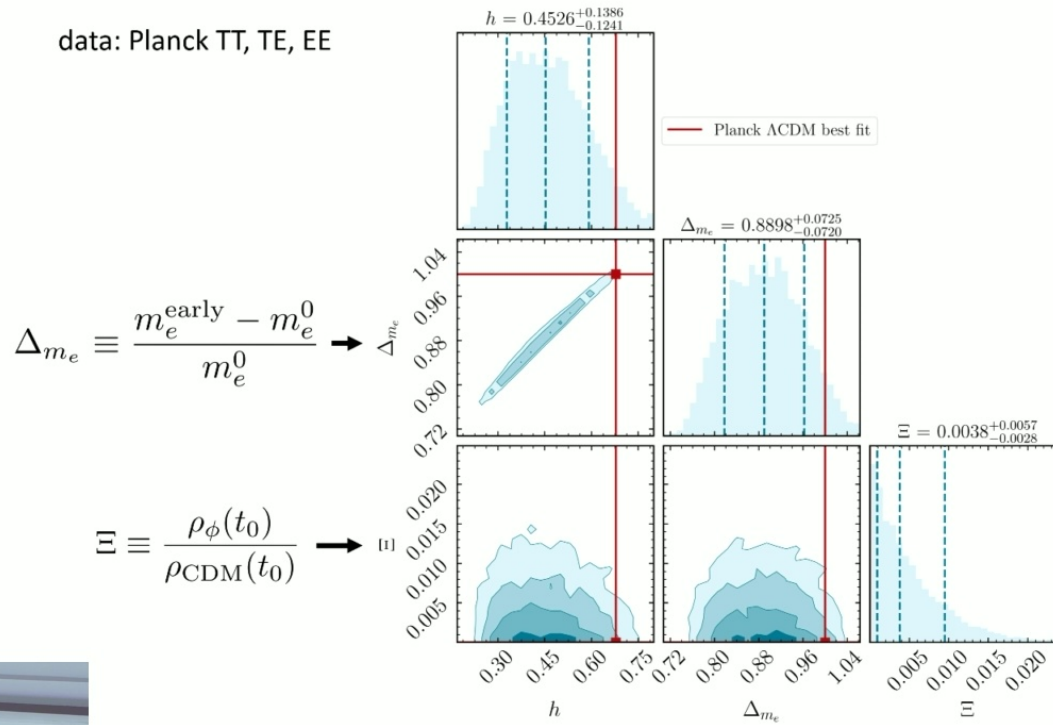


$$\Delta m_e \equiv \frac{m_e^{\text{early}} - m_e^0}{m_e^0} \rightarrow$$



The CMB prefers... late recombination???

data: Planck TT, TE, EE

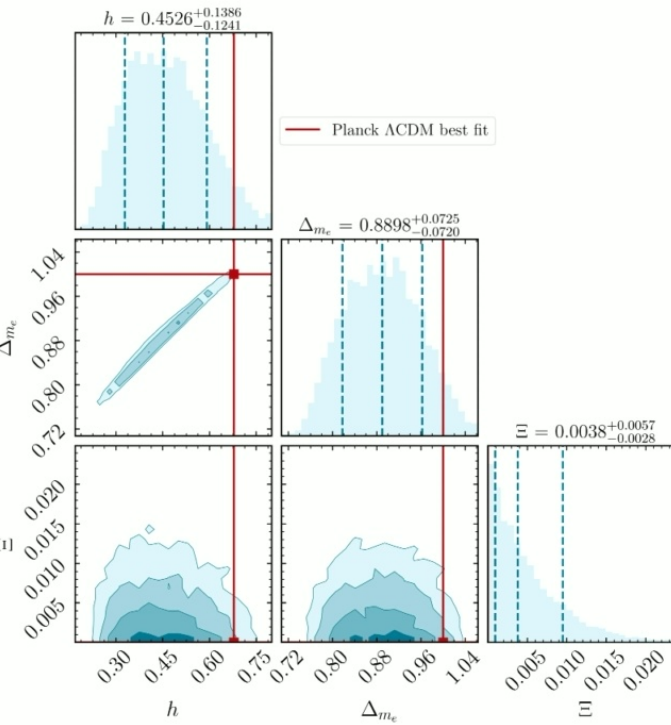


The CMB prefers... late recombination???

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$$\Delta m_e \equiv \frac{m_e^{\text{early}} - m_e^0}{m_e^0} \rightarrow \Delta m_e$$

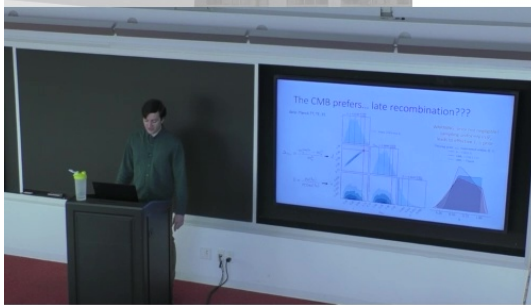
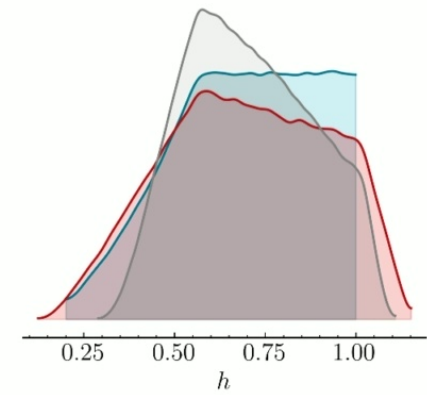
$$\Xi \equiv \frac{\rho_\phi(t_0)}{\rho_{\text{CDM}}(t_0)} \rightarrow \Xi$$



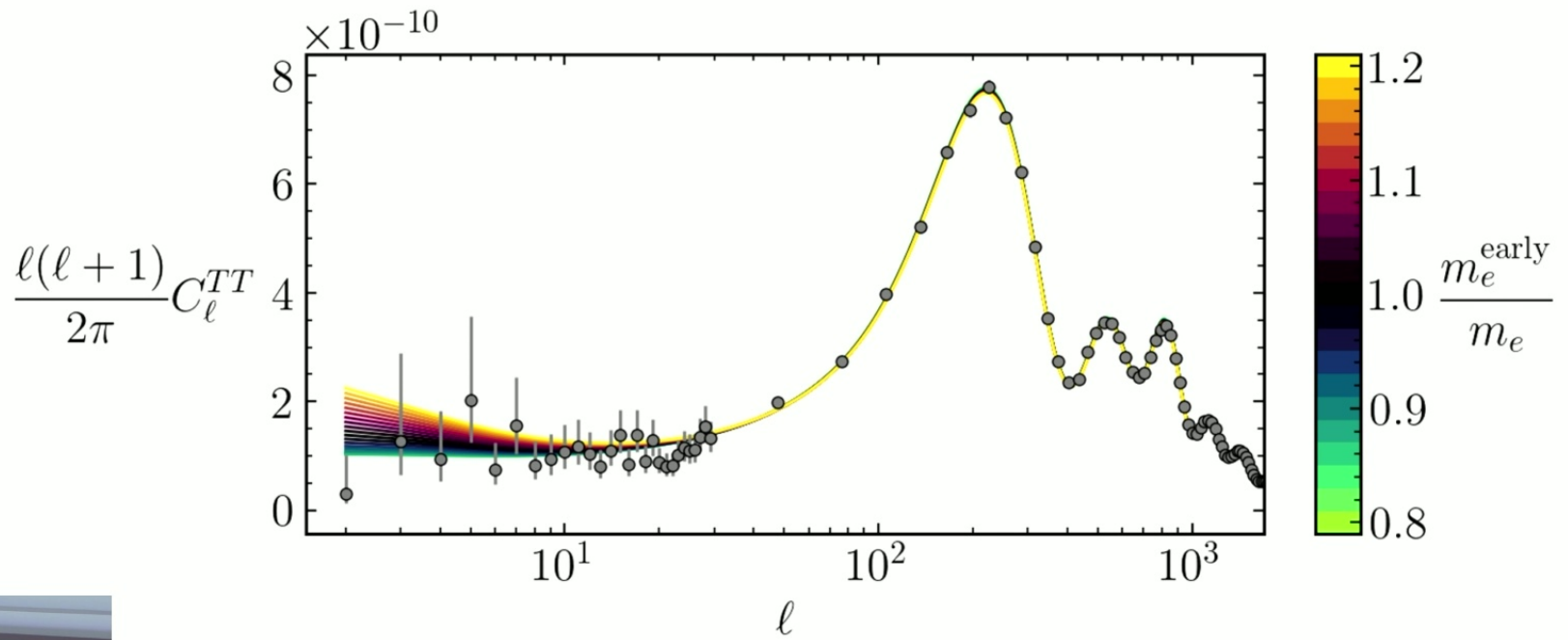
WARNING: prior not negligible!
 sampling uniformly in θ_s
 leads to effective $1/h$ prior

Varying prior, ω_Λ constrained within $[0, 1]$

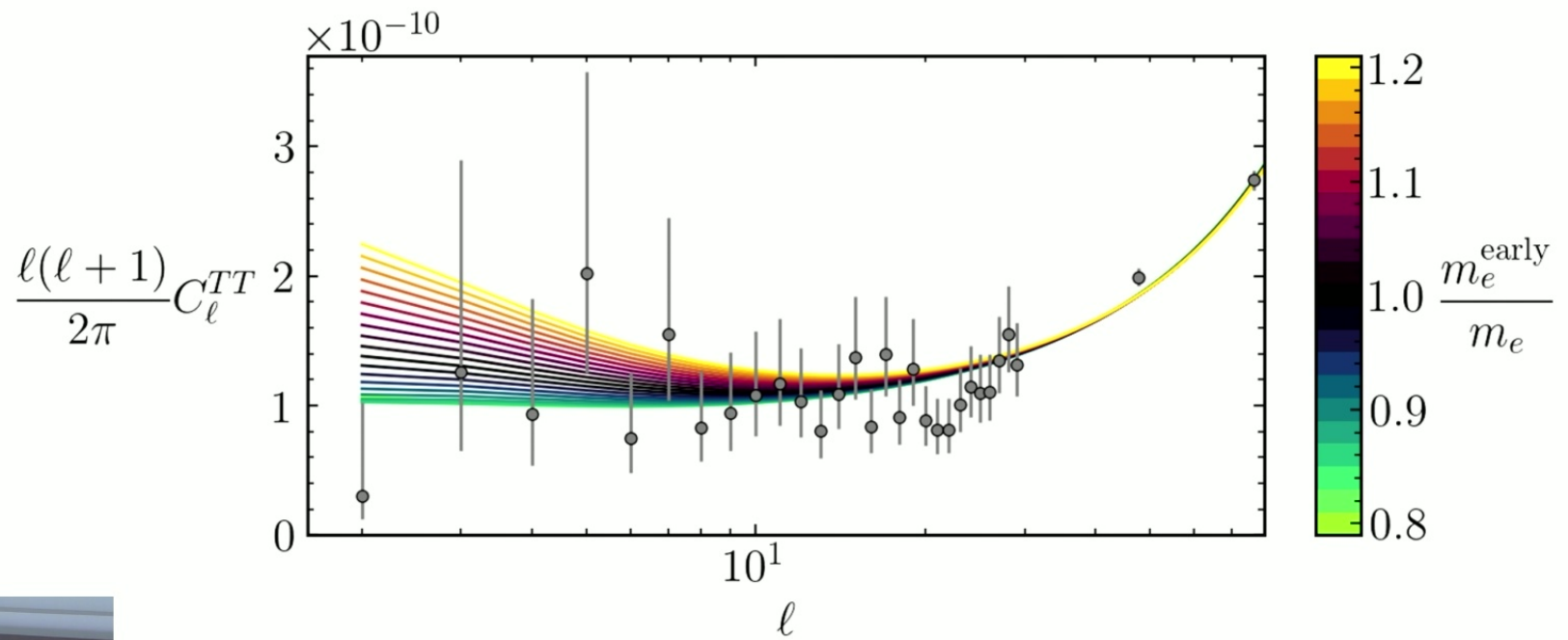
- $h \sim U(0.2, 1)$
- $100\theta_s \sim U(0.5, 1.5)$
- $100\theta_s \sim \text{Planck}$



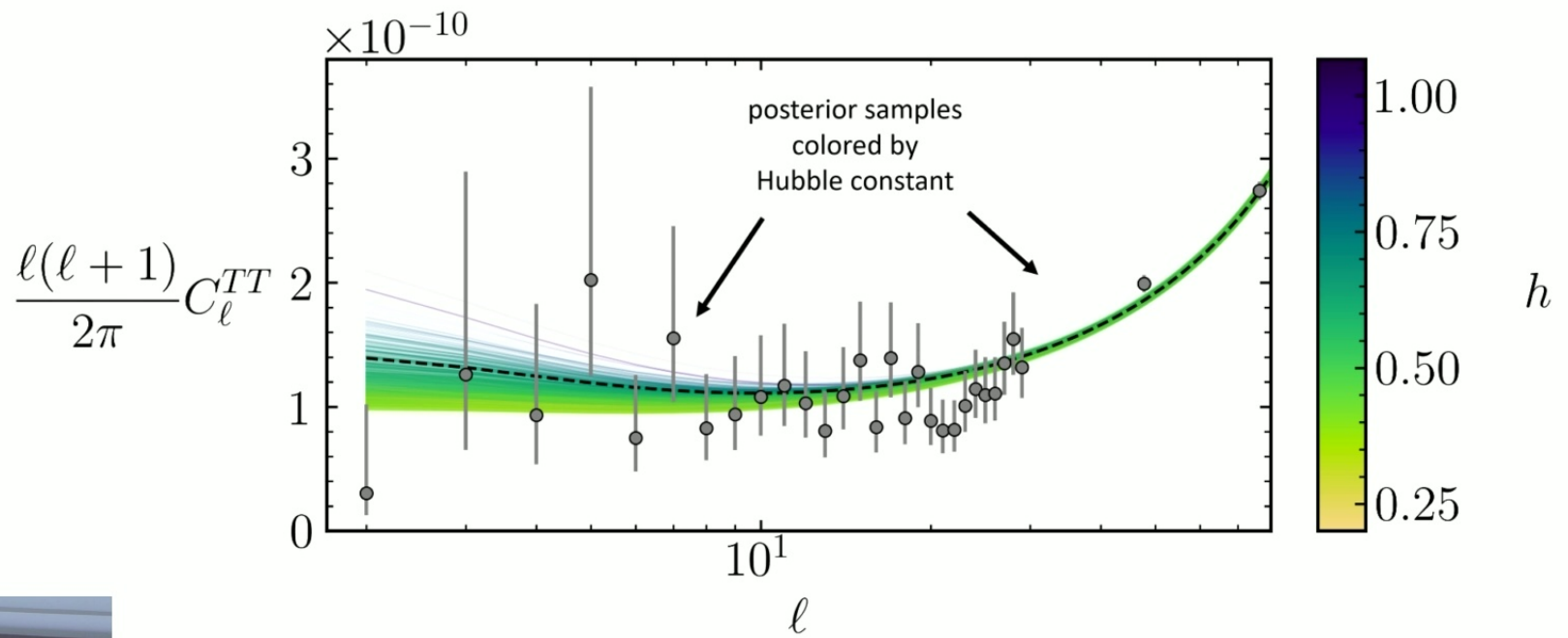
ISW effect



ISW effect



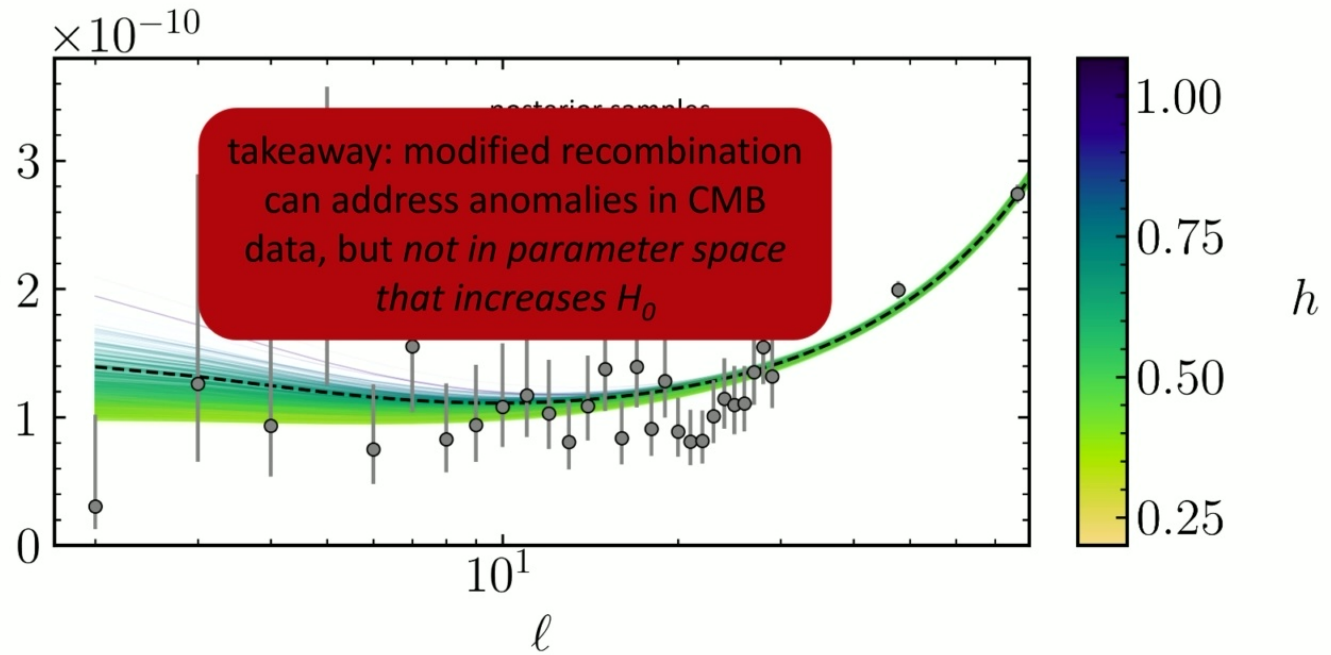
ISW effect



ISW effect



$$\frac{\ell(\ell + 1)}{2\pi} C_{\ell}^{TT}$$

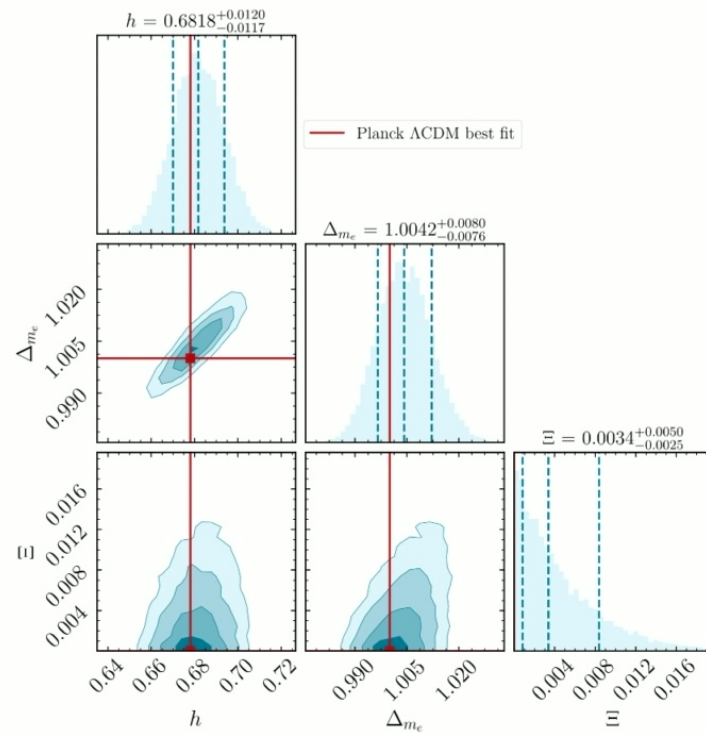


Adding BAO distances

- data: Planck TT, TE, EE
 + BAO scale from
- eBOSS LRG DR16
 - SDSS DR7 MGS
 - 6dFGS

$$\Delta m_e \equiv \frac{m_e^{\text{early}} - m_e^0}{m_e^0} \rightarrow$$

$$\Xi \equiv \frac{\rho_\phi(t_0)}{\rho_{\text{CDM}}(t_0)} \rightarrow$$

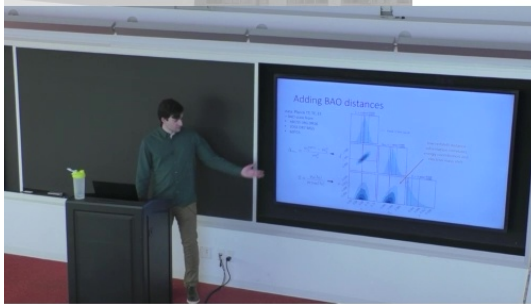
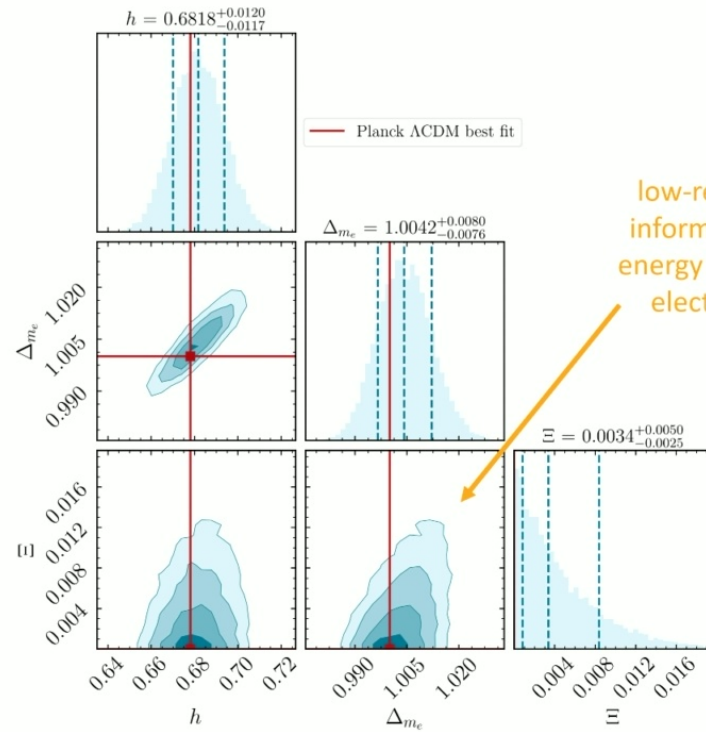


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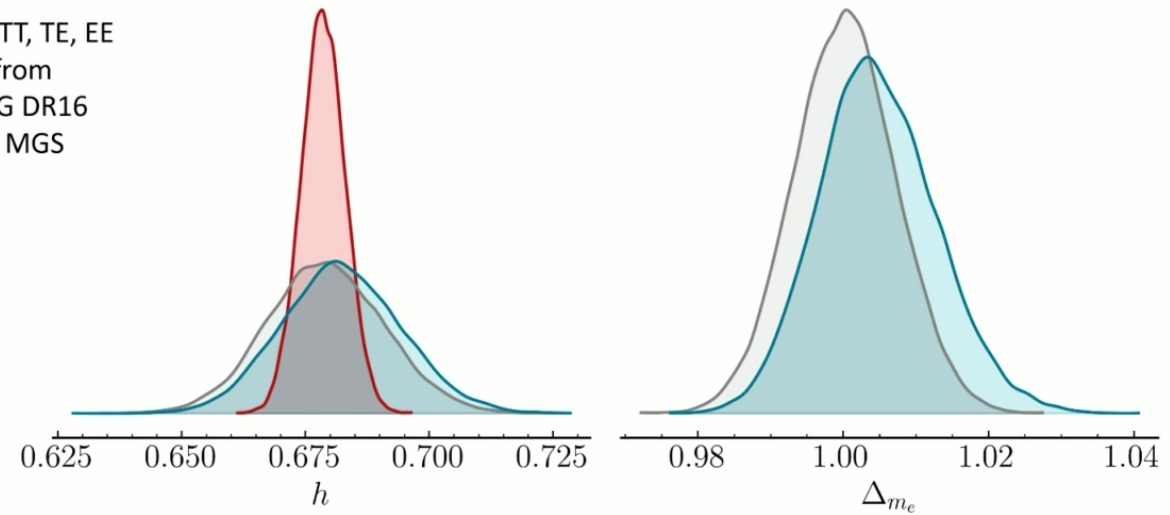
$$\Xi \equiv \frac{\rho_\phi(t_0)}{\rho_{\text{CDM}}(t_0)} \rightarrow$$



Showdown

— ACDM — Vanilla early recombination — Early recombination via 10^{-29} eV scalar

- data: Planck TT, TE, EE
+ BAO scale from
- eBOSS LRG DR16
 - SDSS DR7 MGS
 - 6dFGS



Additional phenomenology

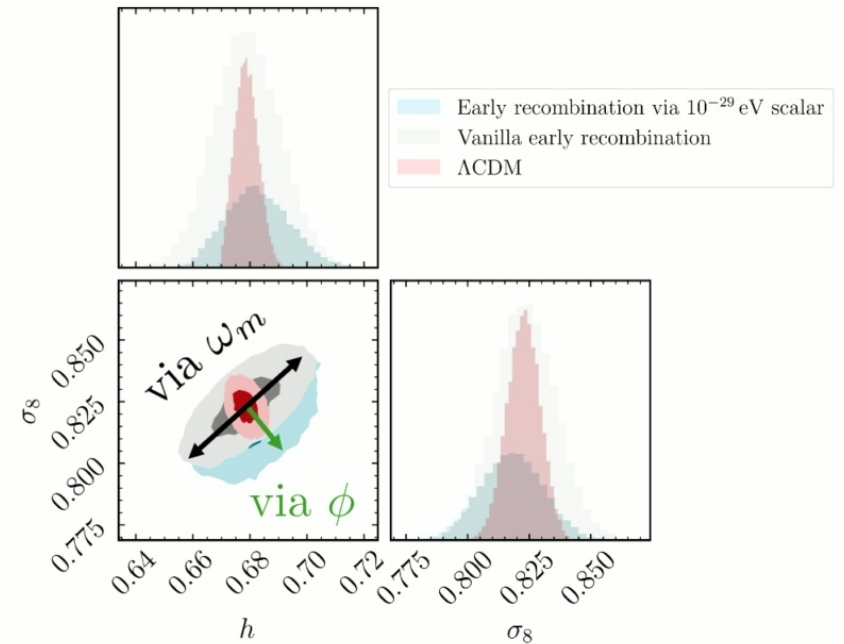
structure growth

Scalars field perturbations oscillate below Jeans scale and **free stream!**

$$k_{\text{fs}} \propto \sqrt{m_\phi}$$

Free-streaming subcomponent of DM **suppress growth of structure**

Can offset increase in matter density



Conclusion

Theory learns much from cosmology, but cosmology also stands to learn much from theory!

