

Title: A measured approach toward long-range entangled matter

Speakers: Timothy Hsieh

Series: Colloquium

Date: November 08, 2023 - 2:00 PM

URL: <https://pirsa.org/23110055>

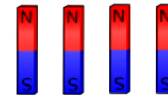
Abstract: Long-range entangled quantum matter encompasses a wealth of fascinating phenomena including fractionalization and criticality. I will show how quantum dynamics involving measurements can both enable new kinds of long-range entangled states and facilitate their realization on quantum simulators. In the first part, I will illustrate how competing measurements along with unitary time evolution can give rise to distinct universality classes of non-equilibrium criticality. In the second part, I will show how measurements and unitary evolution conditioned on the measurement outcomes ("adaptive quantum circuits") enable efficient preparation of long-range entangled matter. Finally, I will demonstrate how environmental measurement (decoherence) can remarkably enrich quantum critical pure states, giving rise to renormalization group flows between quantum channels with important implications on the entanglement structure of the resulting critical mixed states.

Zoom link <https://pitp.zoom.us/j/97087115629?pwd=NHdlWG9oM0xHUDIzU05sUWRKdWlFdz09>

Long-range entangled quantum matter

Long-range entangled quantum matter

“Far” from classical product-like state



Example 1: quantum critical states

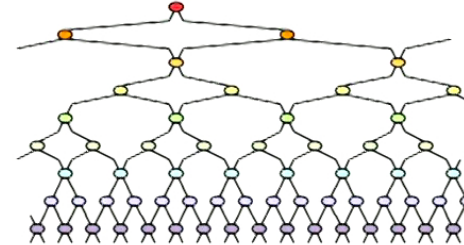
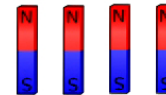


Fig. adapted from Vidal

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Example 1: quantum critical states

Phase transitions between competing quantum orders (e.g. ferromagnet and paramagnet)

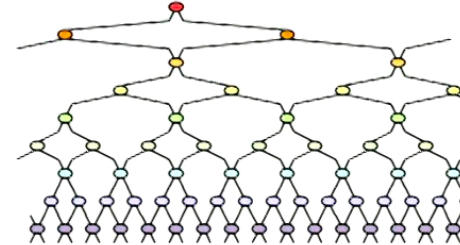
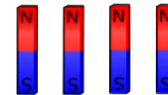


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Example 1: **quantum critical states**

Phase transitions between competing quantum orders (e.g. ferromagnet and paramagnet)

Quantum correlations at all length scales

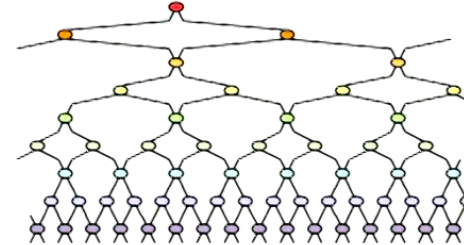
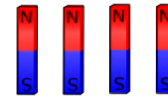


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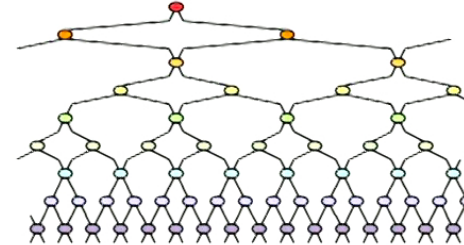
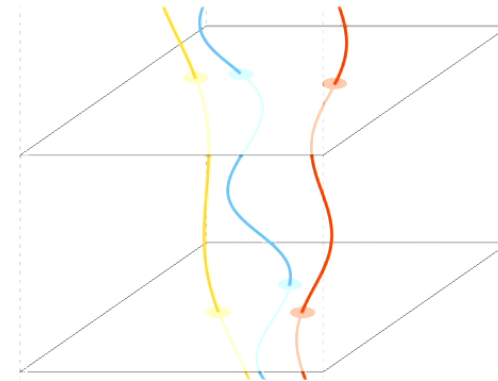


Fig. adapted from Vidal

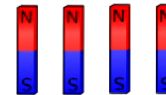
Example 2: **topological order**

No local order parameter



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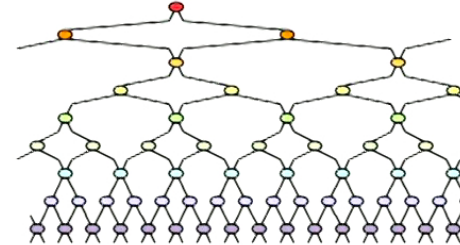
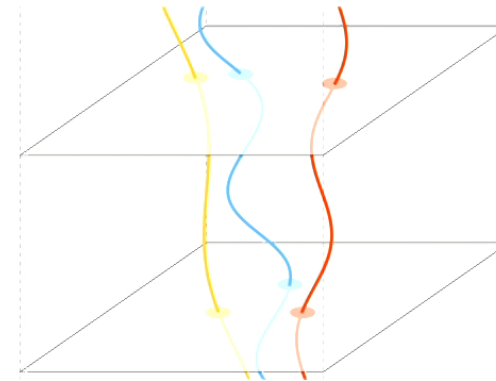


Fig. adapted from Vidal

Example 2: **topological order**

No local order parameter

Fractionalized excitations “anyons”

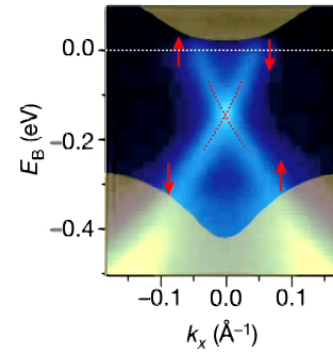


Topological quantum materials

Topological
insulators



Bi₂Se₃



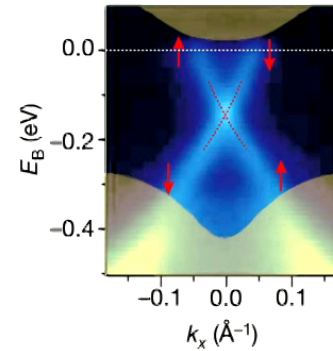
D. Hsieh et.al. (2009)

Topological quantum materials

Topological insulators

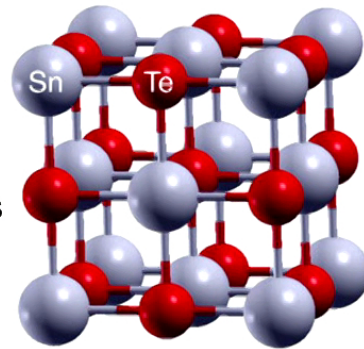


Bi₂Se₃

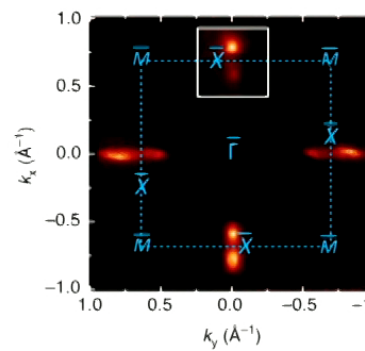


D. Hsieh et.al. (2009)

Topological crystalline insulators



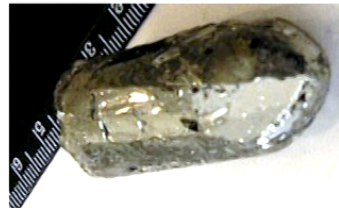
TH, H. Lin, J. Liu, W. Duan, A. Bansil, and L. Fu (2012)



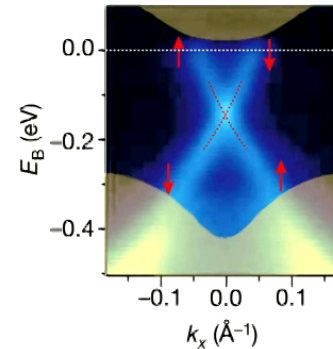
S. Xu et.al. (2012)

Topological quantum materials

Topological insulators

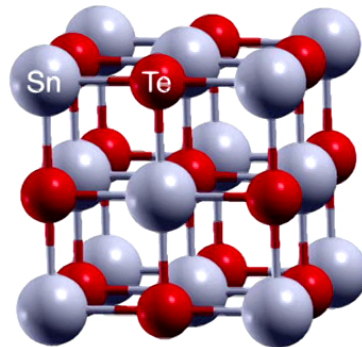


Bi_2Se_3

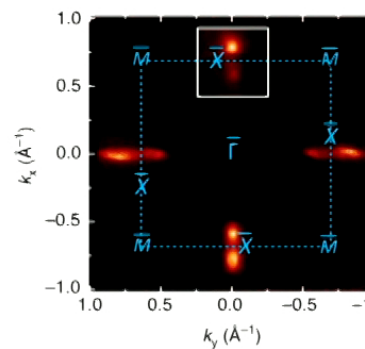


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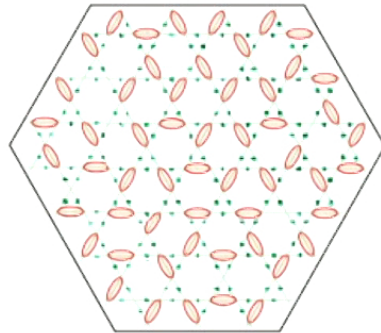
S. Xu et.al. (2012)

But long-range entangled matter much more elusive

Rise of the (Quantum) Machines

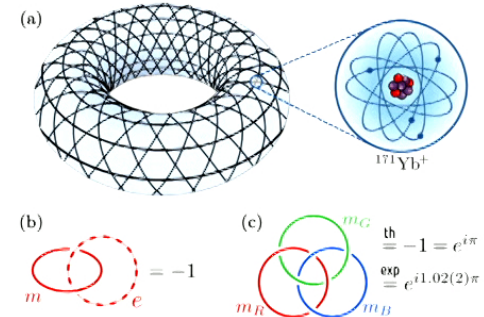
Rydberg array

Semeghini, et.al.
(2021)



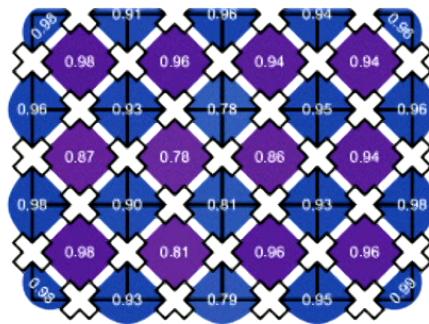
Trapped ions

Iqbal, et.al.
(2023)

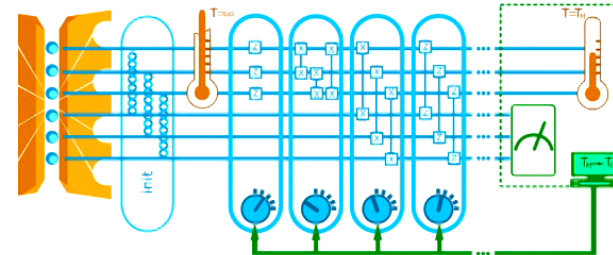


Superconducting qubits

Satzinger, et.al.
(2021)



Quantum critical and thermofield double states on trapped ion computer:



Zhu, Johri, Linke, Landsman, Alderete,
Nguyen, Matsuura, TH, and Monroe (2020)

W. Ho and TH (2019)

J. Wu and TH (2019)

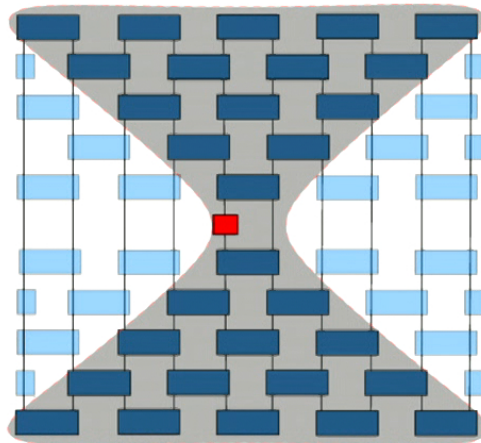
Long-range entangled quantum matter

Far from classical product-like state

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Far from classical product-like state

Cannot be prepared from trivial product states using
local unitary quantum circuits of constant depth



Finite speed at which correlations can propagate

Figure from Xu, Swingle (2020)

Long-range entangled quantum matter

Far from classical product-like state

Cannot be prepared from trivial product states using
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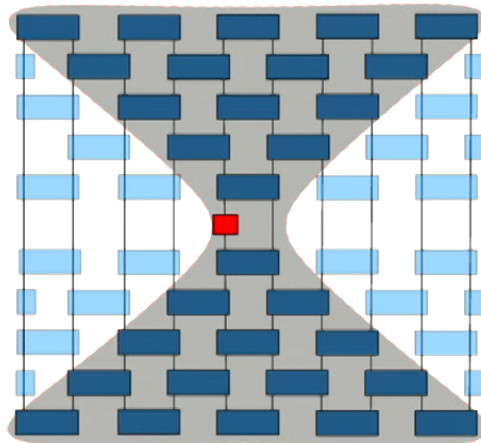


Figure from Xu, Swingle (2020)

Finite speed at which correlations can propagate

Need depth / time **scaling with system size** to produce
requisite long range correlation

Long-range entangled quantum matter

Far from classical product-like state

Cannot be prepared from trivial product states using

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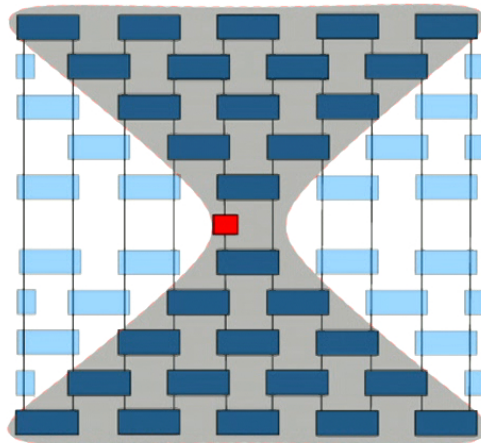


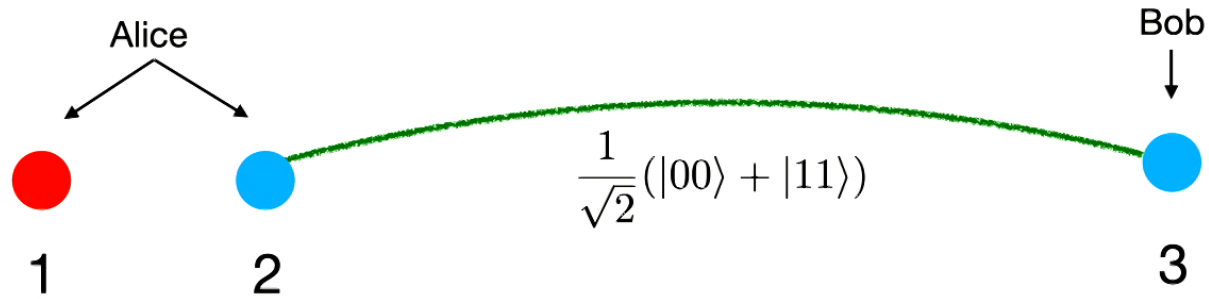
Figure from Xu, Swingle (2020)

Finite speed at which correlations can propagate

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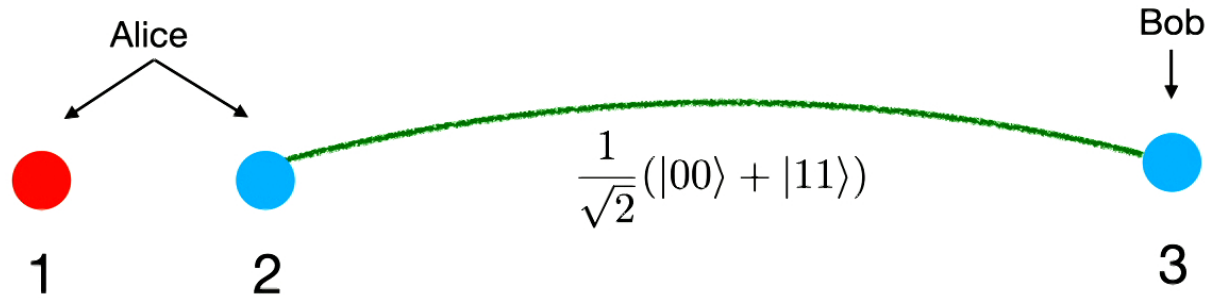
Use local **measurements**
(and possibly non-local classical communication)

Quantum Teleportation



Bennett, Brassard, Crepeau,
Jozsa, Peres, Wootters (1993)

Quantum Teleportation



Bennett, Brassard, Crepeau,
Jozsa, Peres, Wootters (1993)

Alice performs Bell pair (ZZ, XX) measurement on her qubits

Quantum Teleportation



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Quantum Teleportation

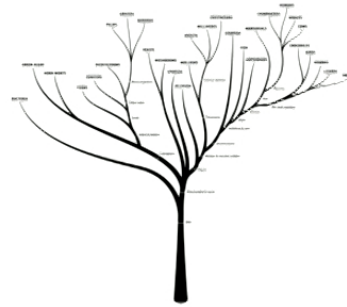


Bennett, Brassard, Crepeau,
Jozsa, Peres, Wootters (1993)

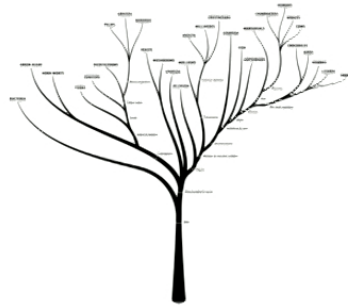
Alice performs Bell pair (ZZ, XX) measurement on her qubits

After Alice tells Bob which outcome (classical info), Bob can apply Pauli operator to recover Alice's qubit

This talk: measurements in many-body systems



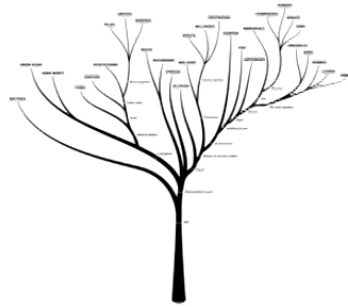
This talk: measurements in many-body systems



Part I: Competition between different **measurements** can give rise to novel long-range entangled states

Part II: **Measurement + feedback** can prepare many classes of long-range entangled states more efficiently than local unitary protocols

This talk: measurements in many-body systems



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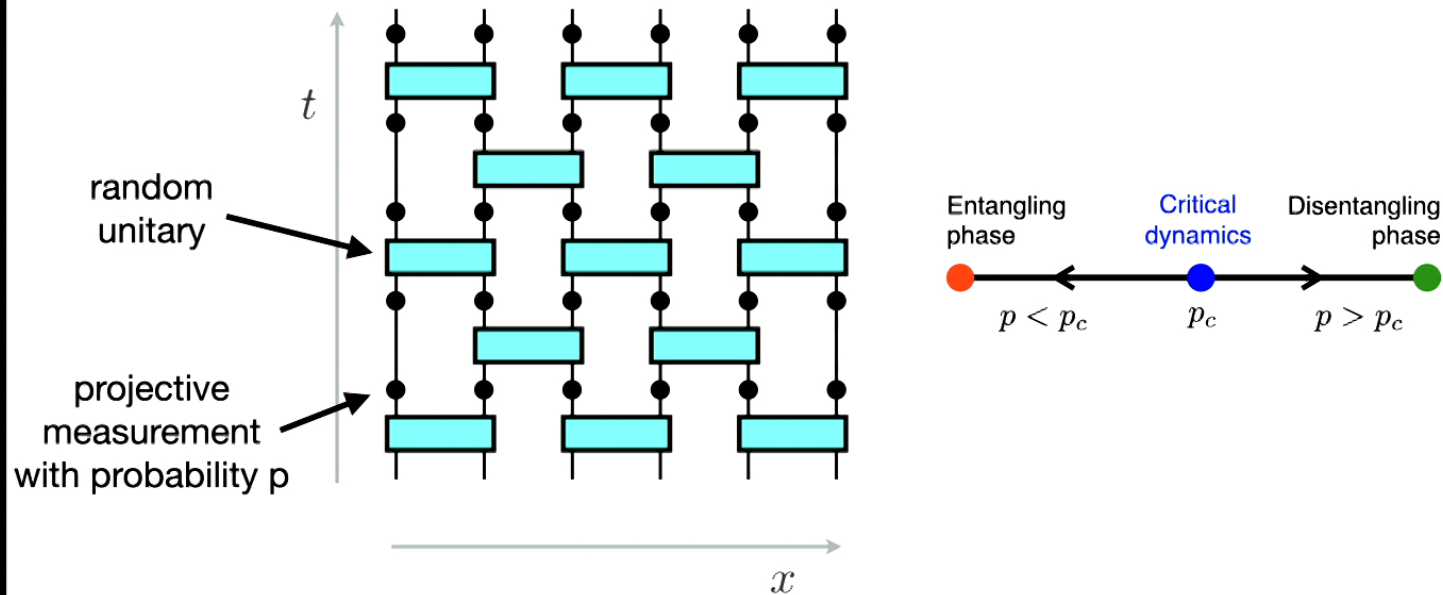
Part III: **Noise (measurement + forgetting outcome)** can transform existing long-range entanglement

Measurement-driven quantum phases and transitions



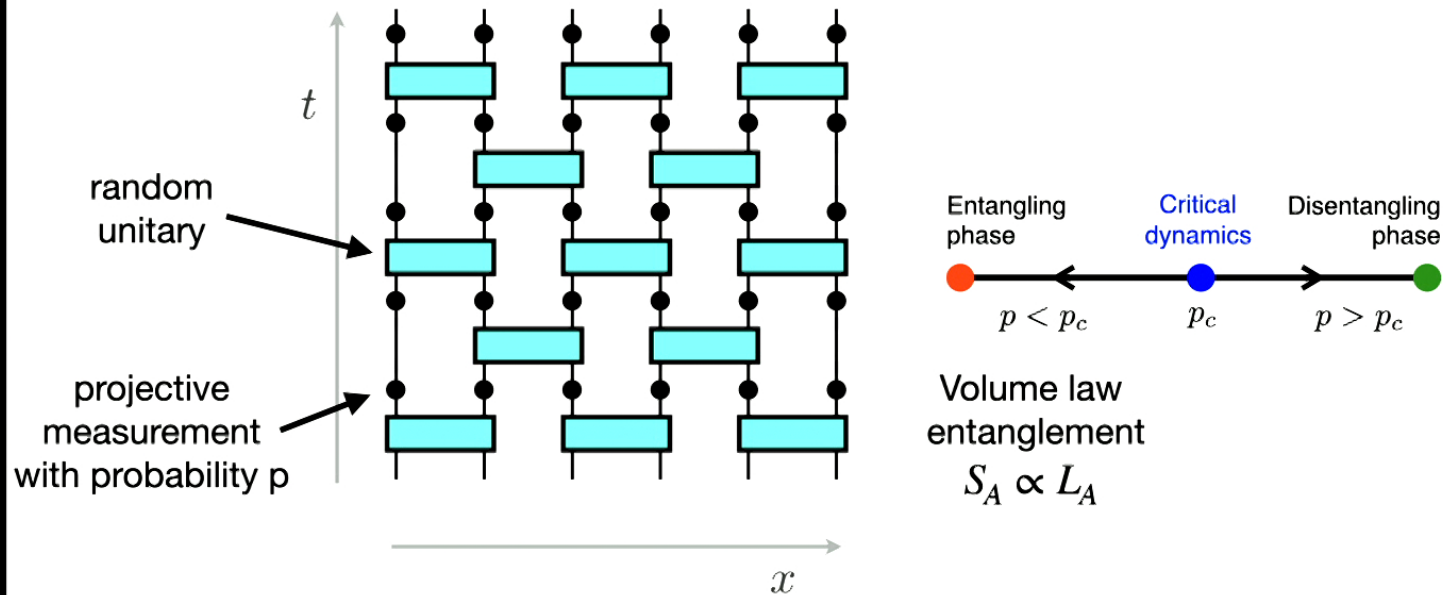
Shengqi Sang and TH
Phys. Rev. Research 3, 023200 (2021)

Hybrid Quantum Circuits



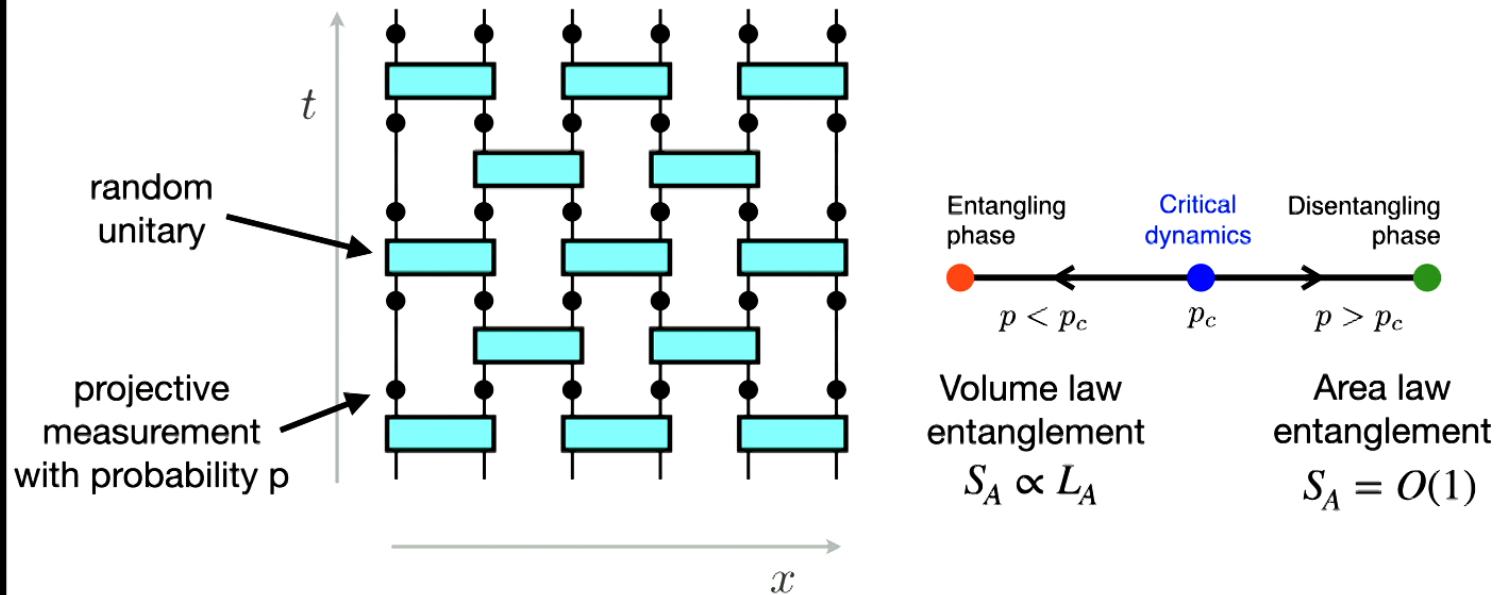
Y. Li, X. Chen, MPA Fisher PRB 98, 205136 (2018)
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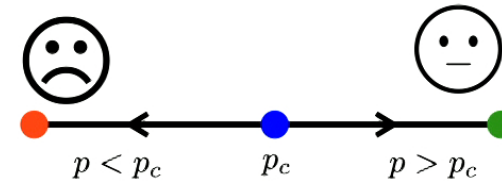
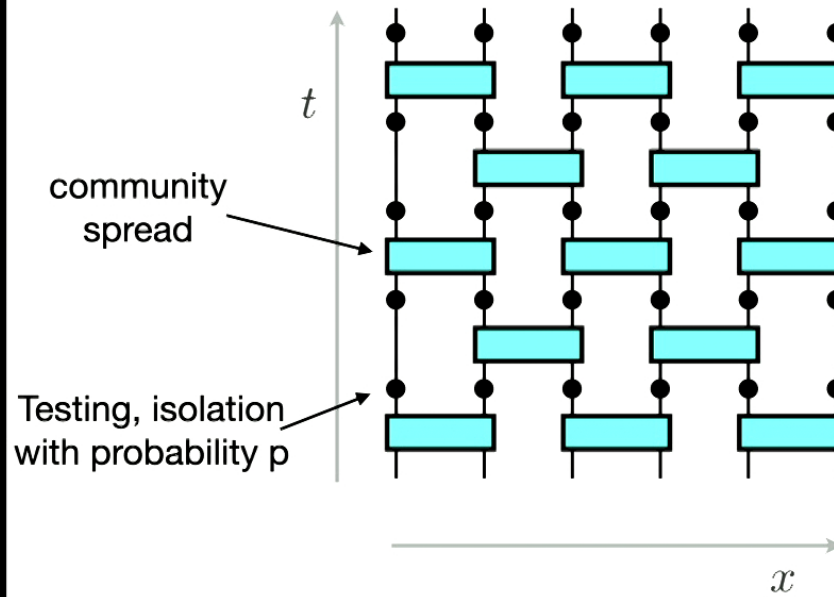
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Hybrid Quantum Circuits



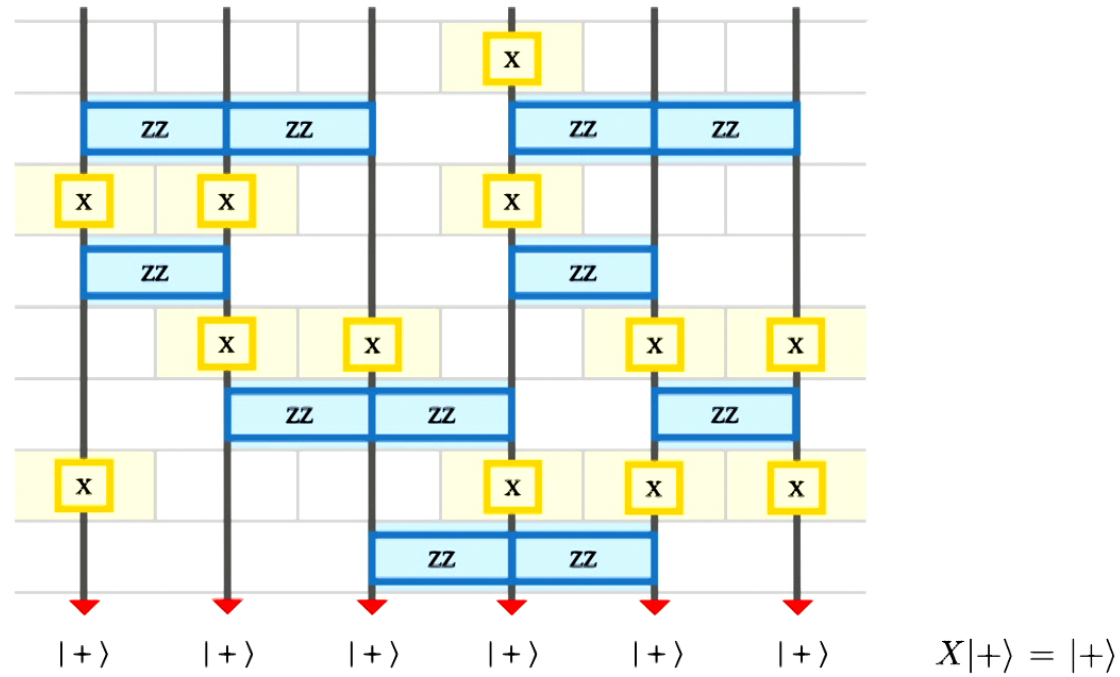
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Practical Relevance



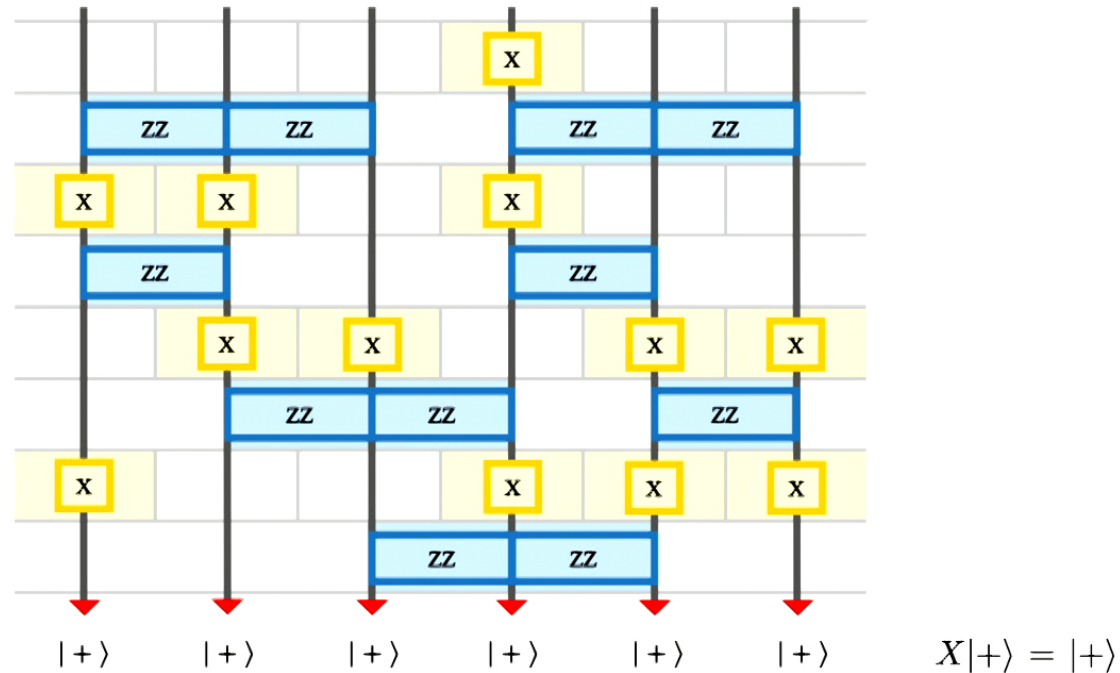
Measurement-only dynamics: a toy model

Measurement-only dynamics: a toy model



See also
Skinner and Nahum,
Ippoliti, et.al.
Lavasani, et.al.
for related models

Measurement-only dynamics: a toy model



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Randomly measure ZZ and X; competition drives criticality

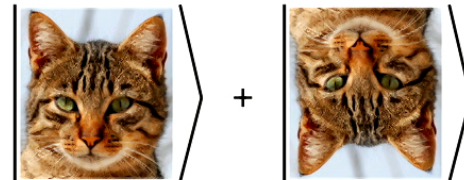
Extreme limits

ZZ measurement only: steady state has random $Z_i Z_{i+1} = \pm 1$ for every pair of qubits

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“random cat state” $\frac{1}{\sqrt{2}}(|\uparrow\downarrow\downarrow\dots\uparrow\rangle + |\downarrow\uparrow\uparrow\dots\downarrow\rangle)$



X measurement only: remains a paramagnetic product state

Order Parameter and Phase Diagram

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Random cat aka **spin glass**: $\frac{1}{\sqrt{2}}(|\uparrow\downarrow\downarrow \dots \uparrow\rangle + |\downarrow\uparrow\uparrow \dots \downarrow\rangle)$

Order Parameter and Phase Diagram

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Quantify long-range order using spin glass or Edwards Anderson type order parameter:

$$O = \frac{1}{L} \sum_{i,j=1}^L \langle \psi | Z_i Z_j | \psi \rangle^2$$

or **Constant (paramagnet)**
or **linear with system size L (spin glass)?**

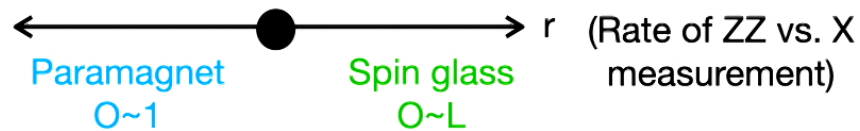
Order Parameter and Phase Diagram

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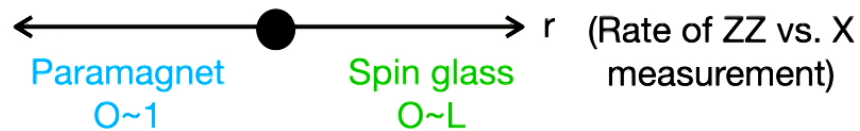
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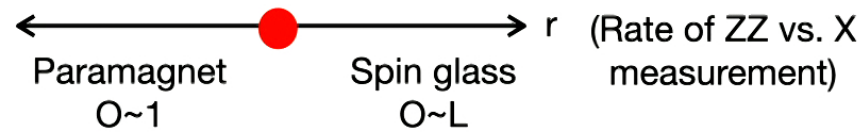
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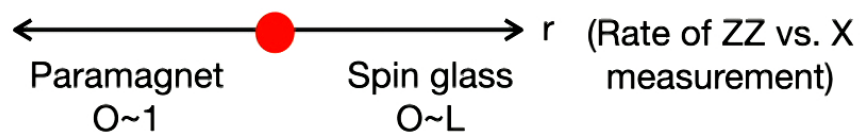
Ising symmetry essential for stability of spin glass (e.g. Z measurement would collapse cat)

Measurement-only phase transition

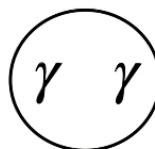


Represent each spin as pair of Majorana fermions (“Jordan-Wigner transformation”)

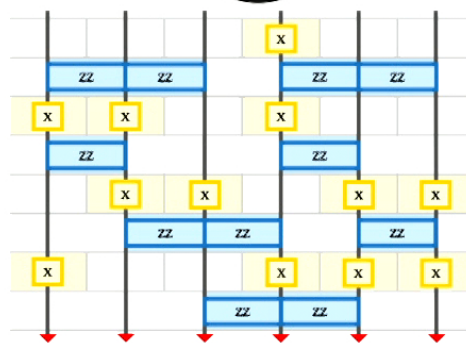
Measurement-only phase transition



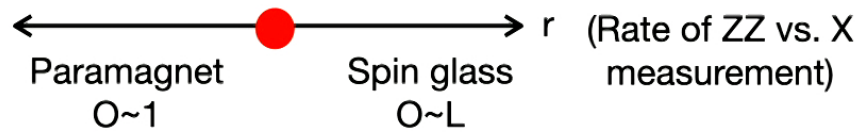
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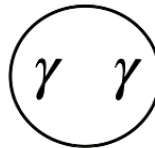
Majorana picture		Qubit picture	
$iY_{2k-1}Y_{2k}$ measurement		X measurement	
$iY_{2k}Y_{2k+1}$ measurement		ZZ measurement	
identity gate		identity gate	



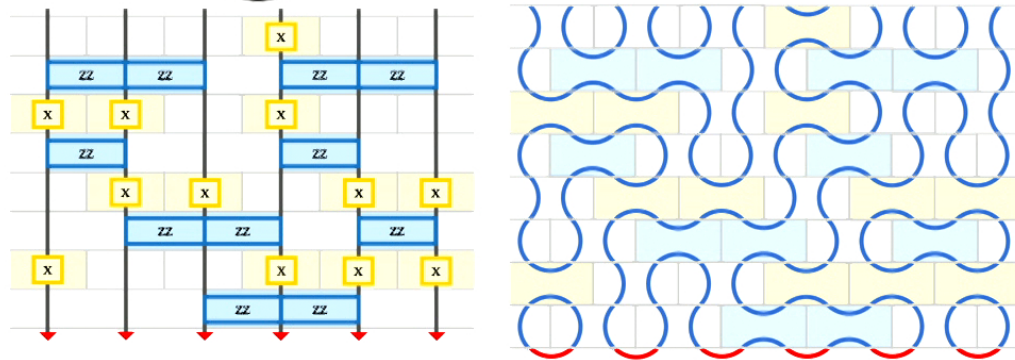
Measurement-only phase transition



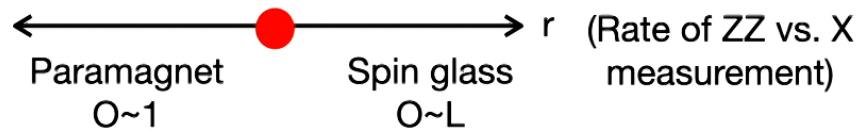
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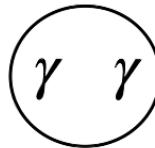
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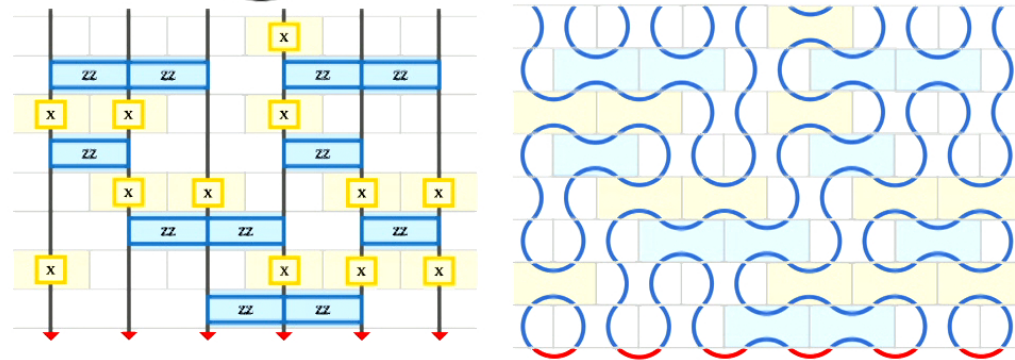
Measurement-only phase transition



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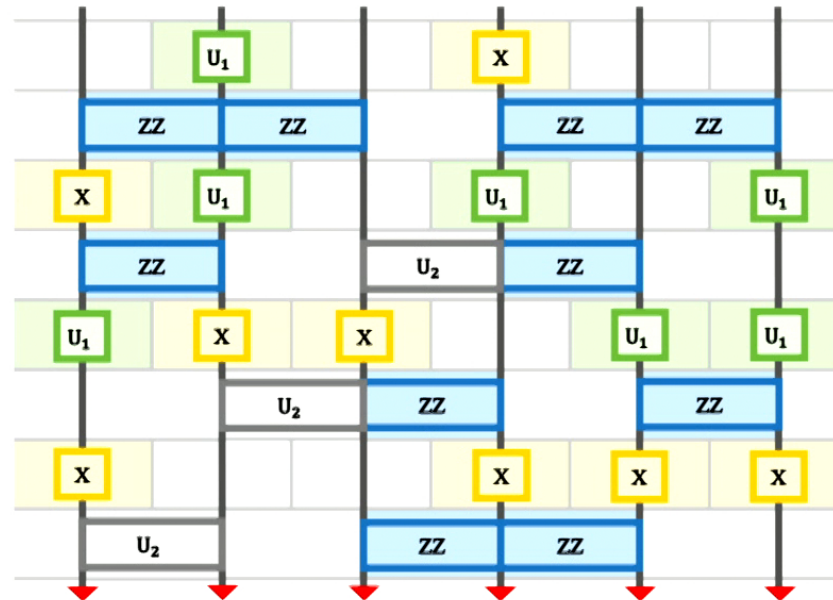
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Classical loop model in critical percolation universality class [Skinner, Nahum \(2019\)](#)

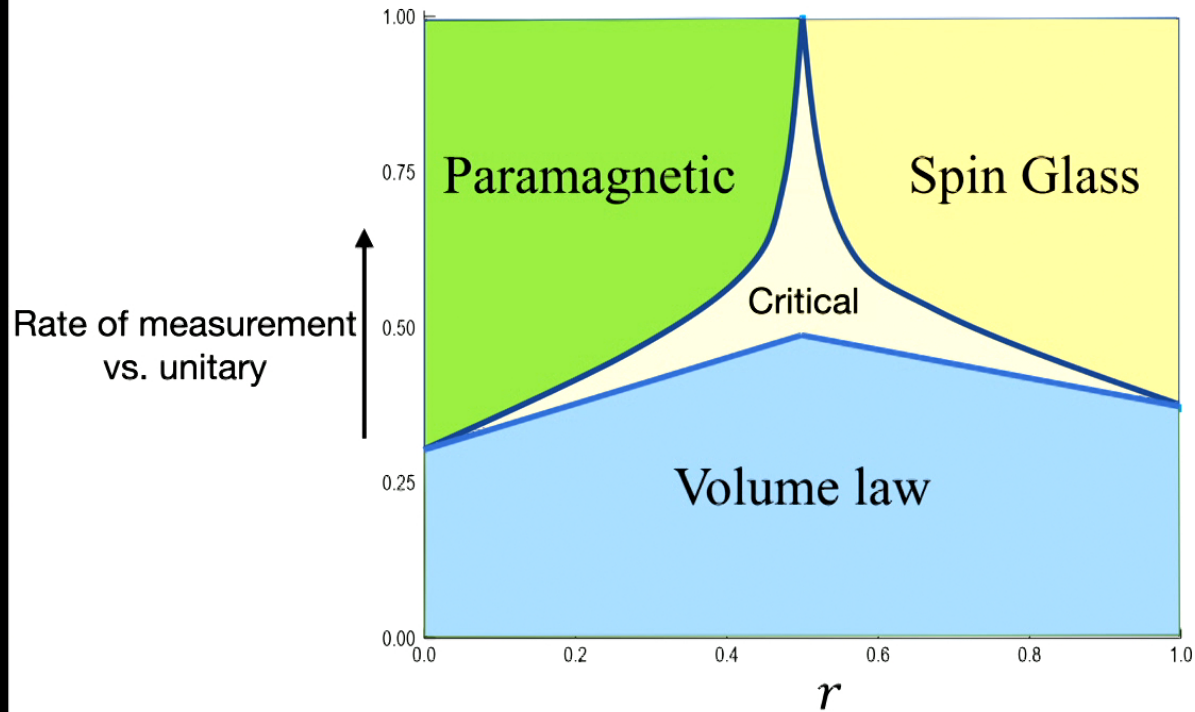
$$\text{Entanglement of subregion of size } L_A \sim \frac{\sqrt{3}}{2\pi} \log L_A$$

Measurements and Unitaries

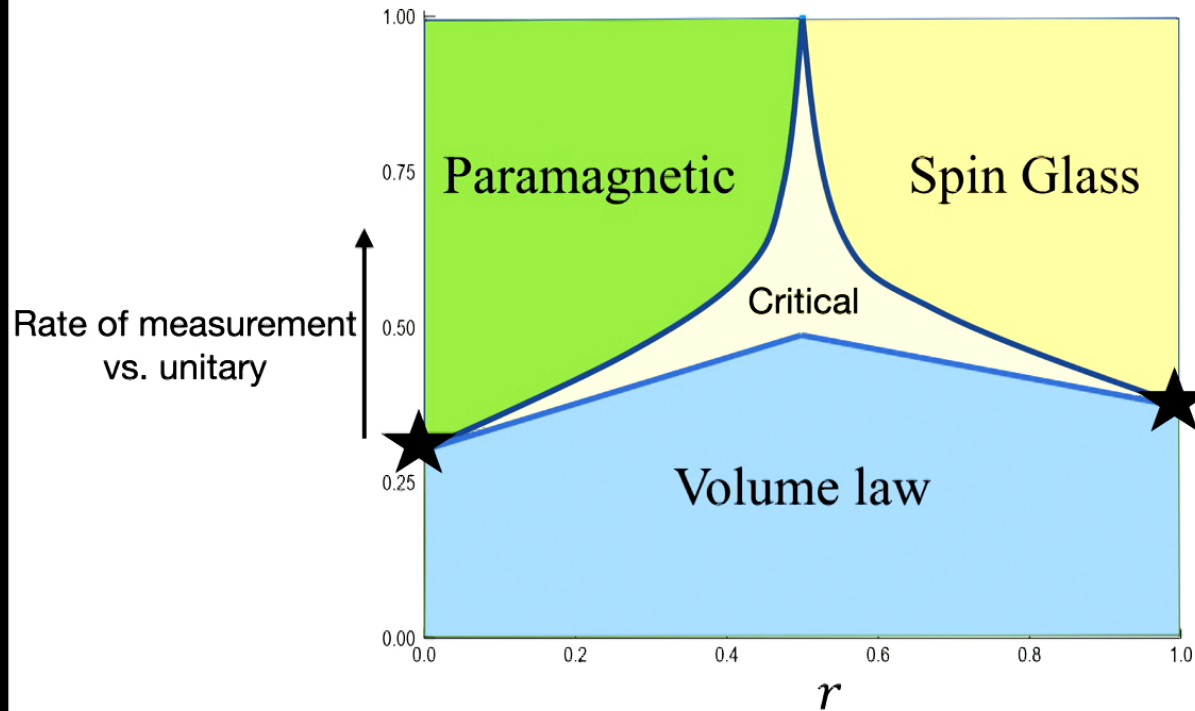


Random unitary gates
preserving Ising symmetry

Phase Diagram

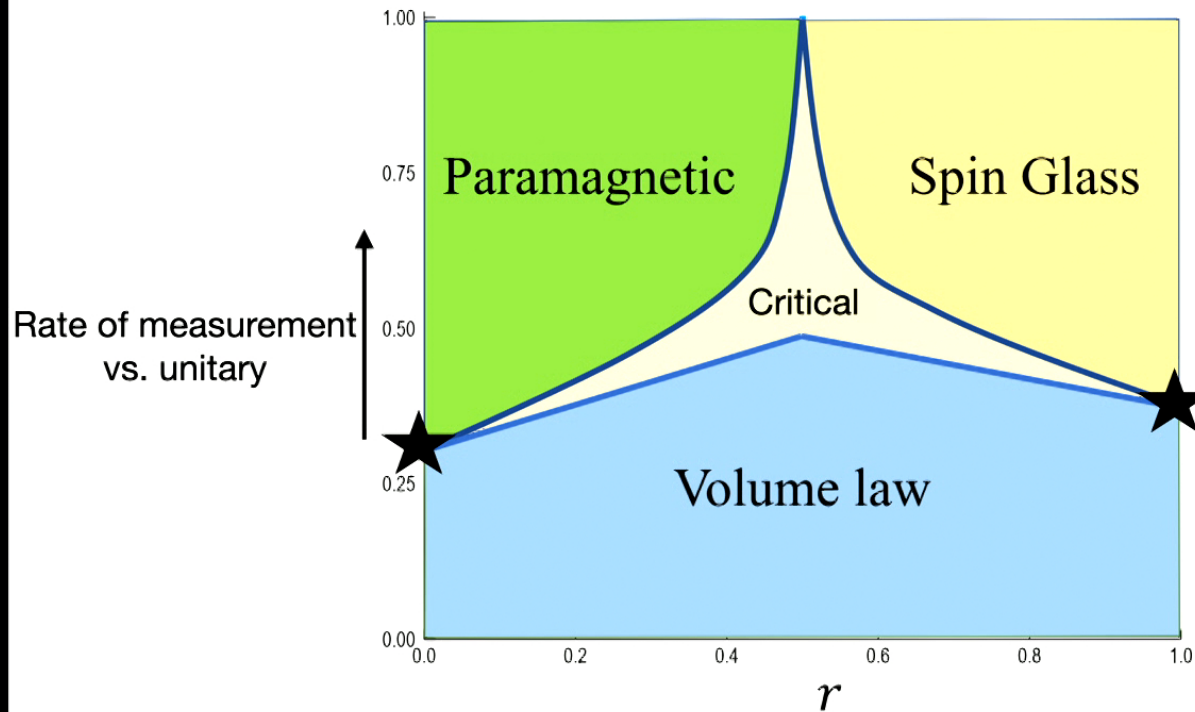


Phase Diagram



New non-equilibrium
universality classes
enabled by measurements

Phase Diagram



New non-equilibrium
universality classes
enabled by measurements

Measurement as a shortcut to long-range entangled matter



Tsung-Cheng (Peter) Lu
(Perimeter)



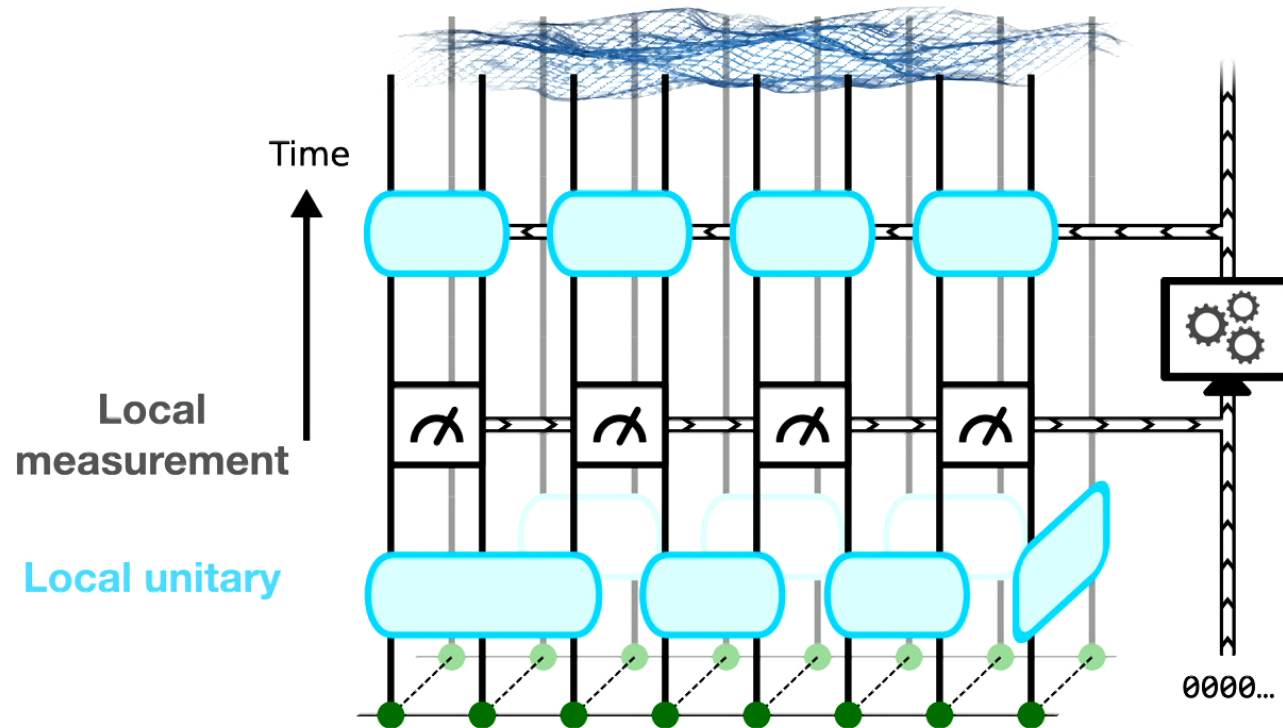
Leonardo Lessa
(Perimeter)



Isaac Kim
(UC Davis)

[PRX Quantum 3, 040337 \(2022\)](#)

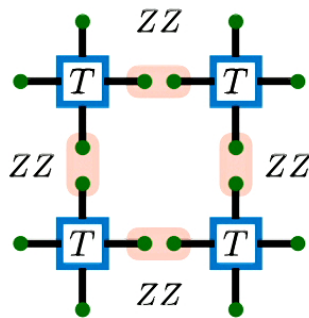
Local adaptive circuit



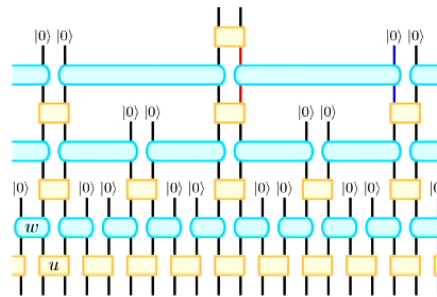
Local adaptive circuits for long-range entangled states

Our work: three general approaches based on distinct physical insights

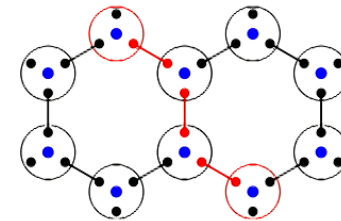
Tensor networks



Renormalization



Partons

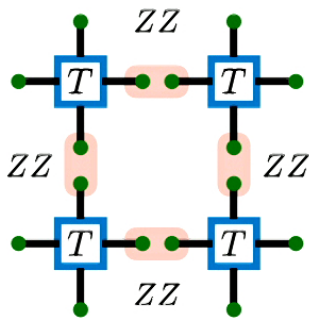


Prior work with similar motivation: Briegel and Raussendorf (2001), Piroli, Styliaris, Cirac (2021), Tantivasadakarn, Thorngren, Vishwanath, Verresen (2021)

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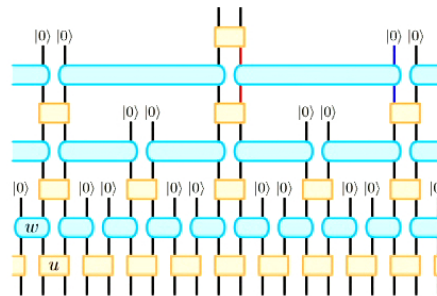
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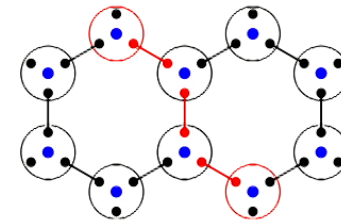
Modular, experiment-friendly

Renormalization



Quantum critical states
and non-abelian topological order

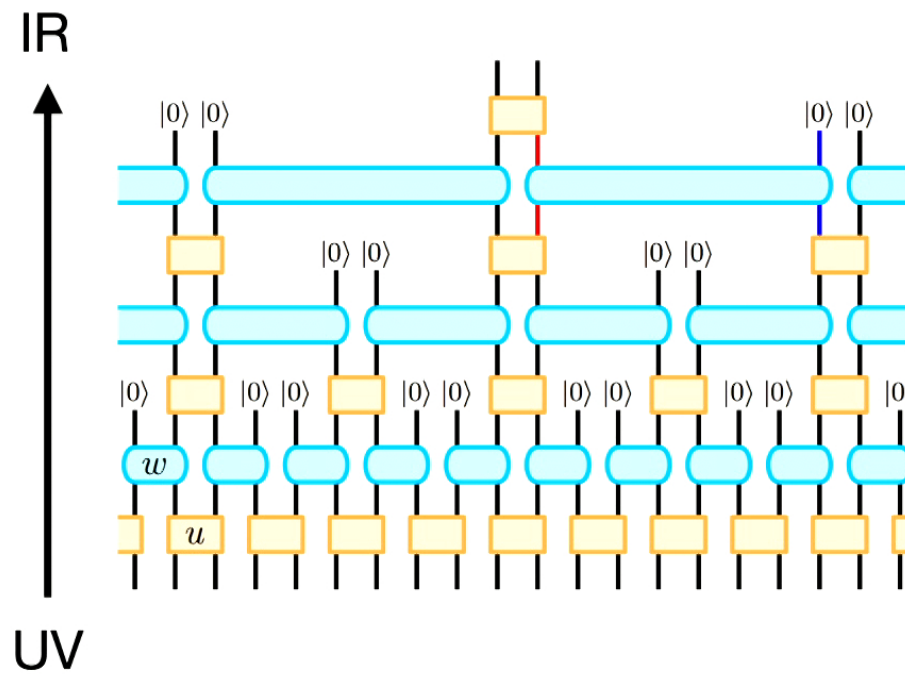
Partons



Chiral topological order

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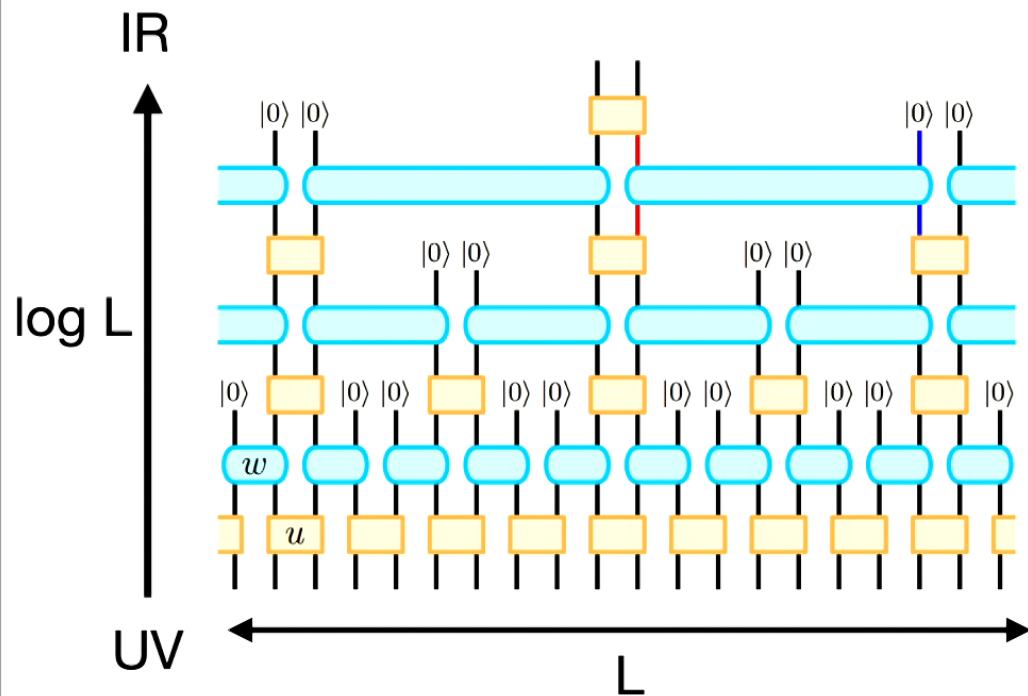
Entanglement Renormalization



Multiscale entanglement renormalization ansatz (MERA)

Vidal (2007)

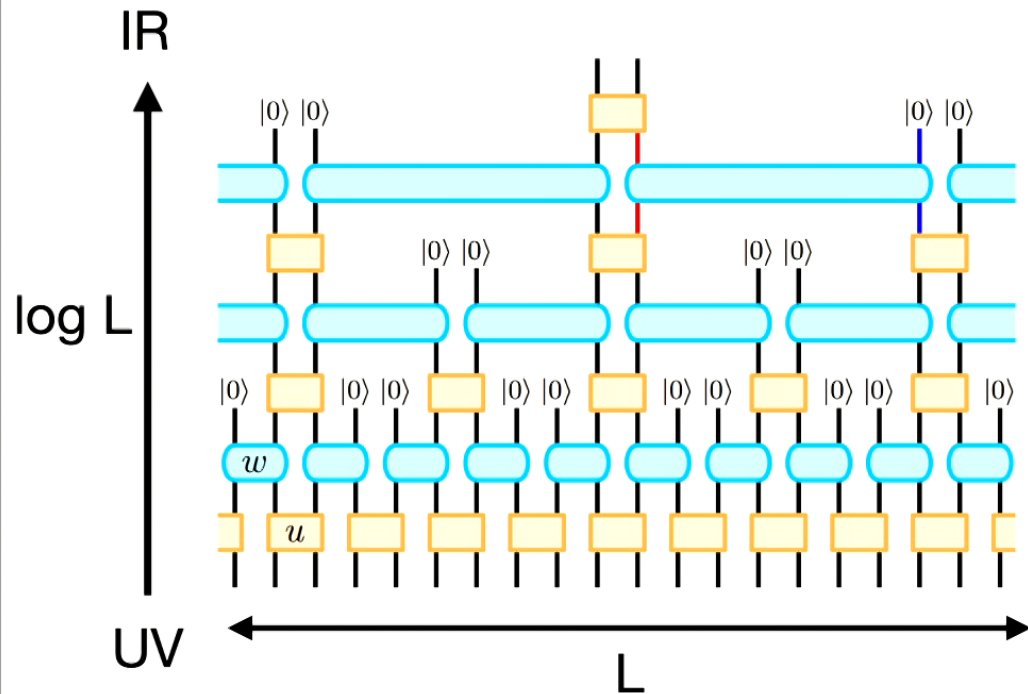
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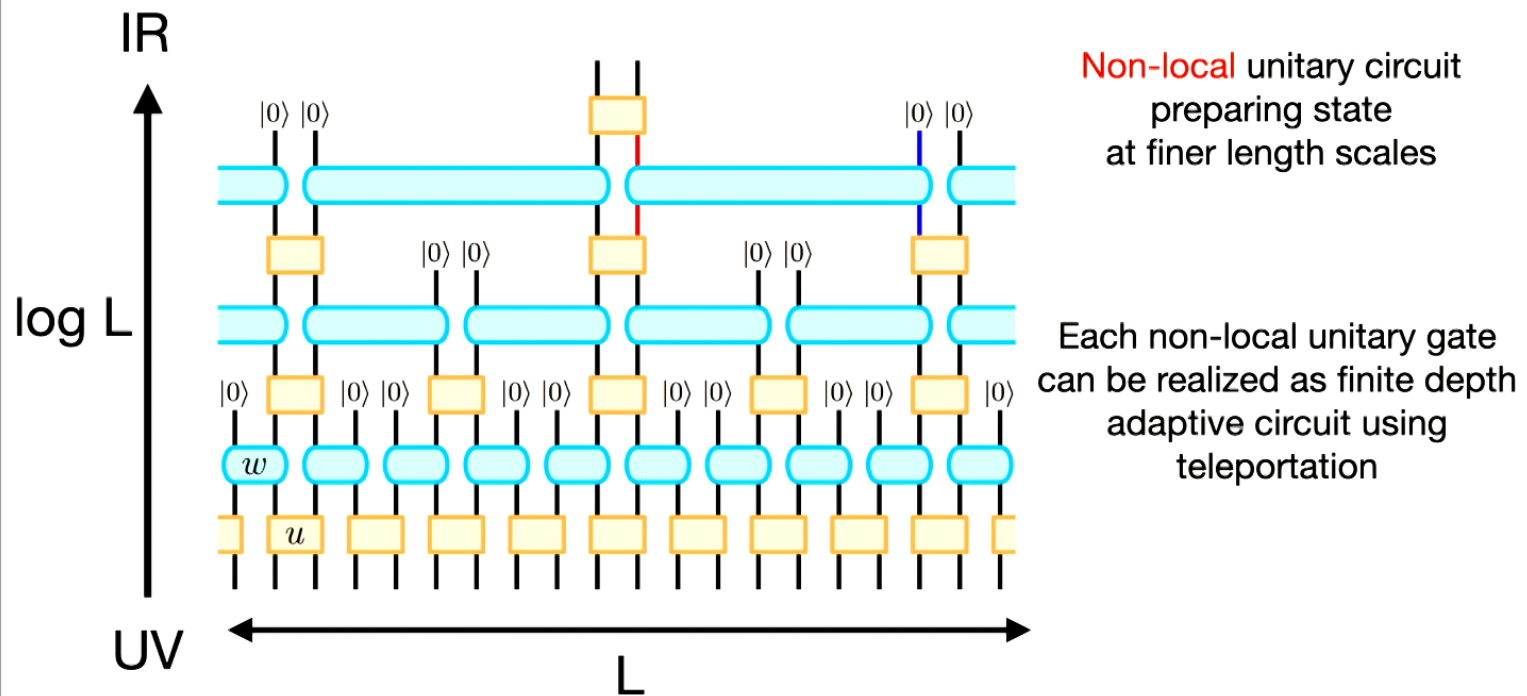


Non-local unitary circuit
preparing state
at finer length scales

Multiscale entanglement renormalization ansatz (MERA)

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Entanglement Renormalization



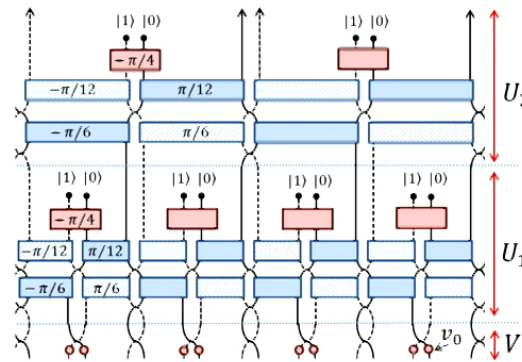
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Adaptive circuits via renormalization

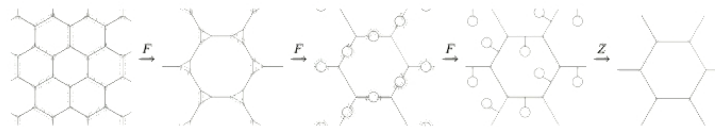
MERA:

approximates 1d quantum critical states



Evenbly, White (2016)

exactly captures many topological orders (all string net models, quantum doubles)



Aguado, Vidal (2008)
Konig, Reichardt, Vidal (2009)

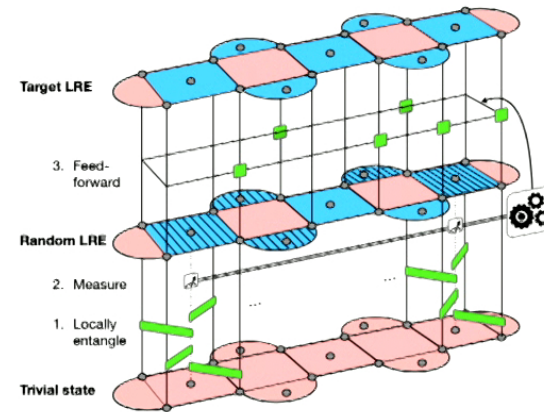
Local adaptive circuits with only depth $\sim \log L$ for preparing all of the above!
(contrast with $\sim L$ typically required using local unitary circuit)

Adaptive Circuits: Experiments and Mixed States

Adaptive Circuits: Experiments and Mixed States

Experimental realization
with Quantinuum (trapped ion quantum computing)

[arXiv:2302.03029](https://arxiv.org/abs/2302.03029) (2023)



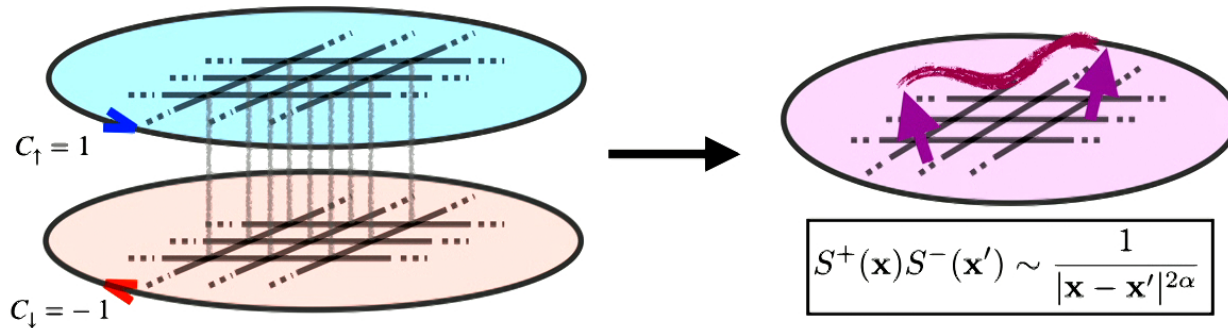
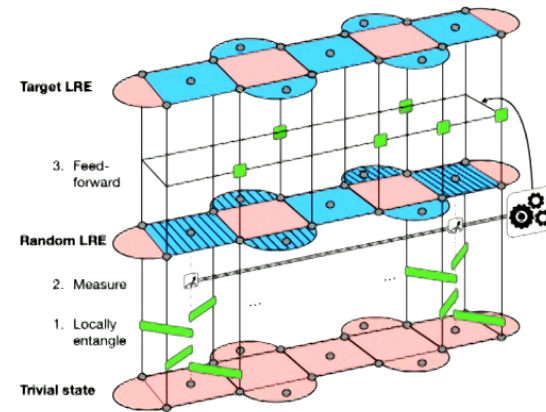
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Control trajectories
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T-C. Lu, Z. Zhang, S. Vijay, and TH
PRX Quantum 4, 030138 (2023)



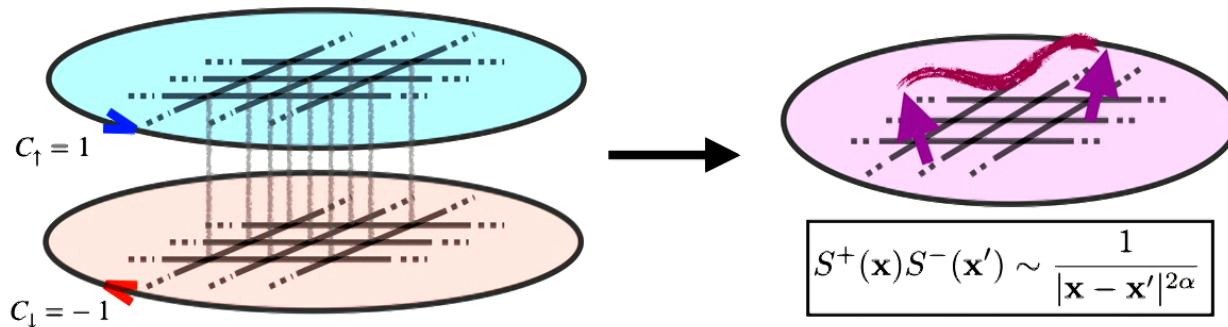
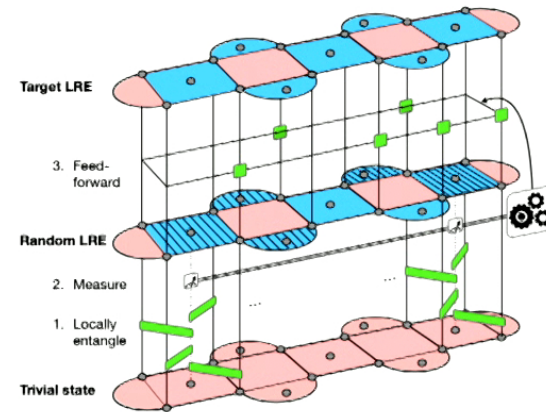
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Channeling Quantum Criticality



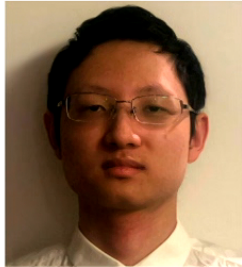
Yijian Zou
(Perimeter)



Shengqi Sang
(Perimeter)

[PRL 130, 250403 \(2023\)](#)

Channeling Quantum Criticality



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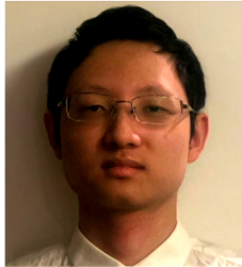


Shengqi Sang
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[PRL 130, 250403 \(2023\)](#)

How is the long-range entanglement in quantum critical states affected by noise?

Channeling Quantum Criticality



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Renormalization group (RG) flows for quantum channels describing noise

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How is the long-range entanglement in quantum critical states affected by noise?

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Dictate entanglement structure / separability of resulting mixed states

Setup

Local quantum channel $\mathcal{N} = \bigotimes_{j=1}^L \mathcal{N}_j$

Dephasing in \vec{v} direction with strength p :

$$\mathcal{D}_{p,\vec{v}}(\rho) = \left(1 - \frac{p}{2}\right) \rho + \frac{p}{2} \sigma_{\vec{v}} \rho \sigma_{\vec{v}}$$

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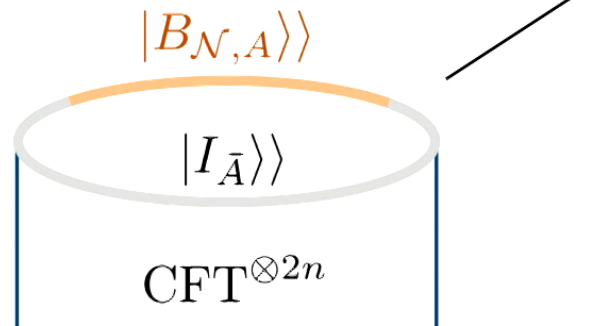
$$\rho = \mathcal{N}(|\psi\rangle \langle \psi|)$$

Critical state described by conformal field theory

Mapping channels to boundary conditions of $CFT^{\otimes 2n}$

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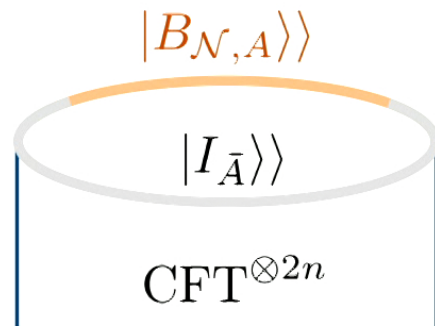
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$$\text{Tr}(\rho_A^n) = \text{Tr}(\rho^{\otimes n} \tau_{n,A}) = \text{Tr}(\mathcal{N}(|\psi\rangle\langle\psi|)^{\otimes n} \tau_{n,A}) = \text{Tr}((|\psi\rangle\langle\psi|)^{\otimes n} B_{N,A})$$

Permutation operator \nearrow

\uparrow
 $\mathcal{N}^{*\otimes n}(\tau_{n,A})$

$$= \langle\langle (\psi \otimes \psi^*)^{\otimes n} | B_{N,A} I_{\bar{A}} \rangle\rangle$$

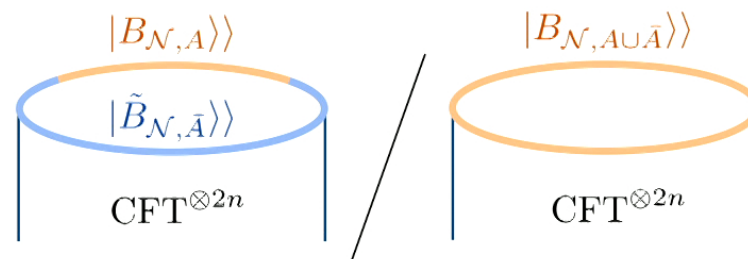
Operators as states
in doubled Hilbert space

Mapping channels to boundary conditions of $CFT^{\otimes 2n}$

Renyi entanglement negativity (a measure of quantum correlations for mixed states)

$$N_A^{(n)}(\rho) := \frac{1}{1-n} \log \frac{\text{Tr}(\{\rho^{T_A}\}^n)}{\text{Tr}(\rho^n)}$$

$$N_A^{(n)}(\rho) = \frac{1}{1-n} \log \frac{\langle\langle (\psi \otimes \psi^*)^{\otimes n} | B_{\mathcal{N},A} \tilde{B}_{\mathcal{N},\bar{A}} \rangle\rangle}{\langle\langle (\psi \otimes \psi^*)^{\otimes n} | B_{\mathcal{N},A \cup \bar{A}} \rangle\rangle}$$



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g plays similar role for boundary RG flow as central charge c for bulk RG flow

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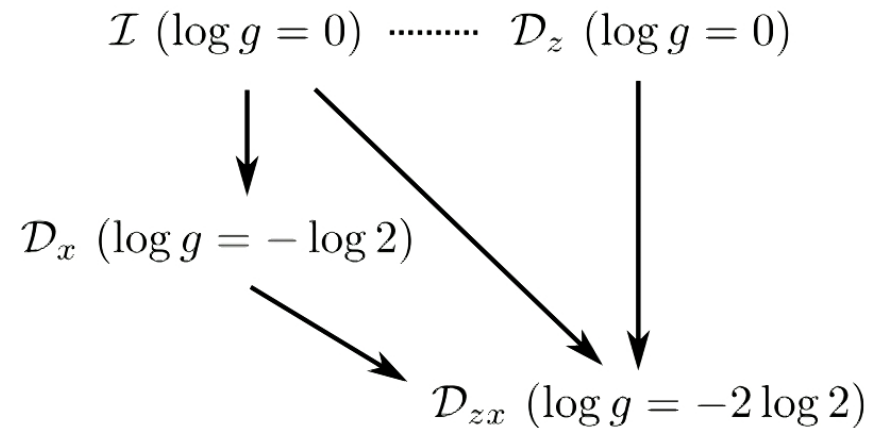
Channel with larger g can flow to channel with smaller g

RG flows for dephased 1d critical transverse-field Ising model

$$H = - \sum_{i=1}^L \sigma_{x,i} \sigma_{x,i+1} - \sum_{i=1}^L \sigma_{z,i}$$

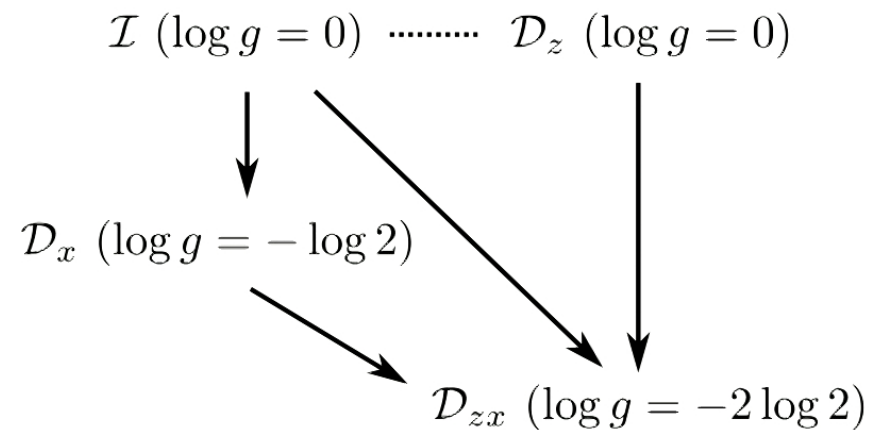
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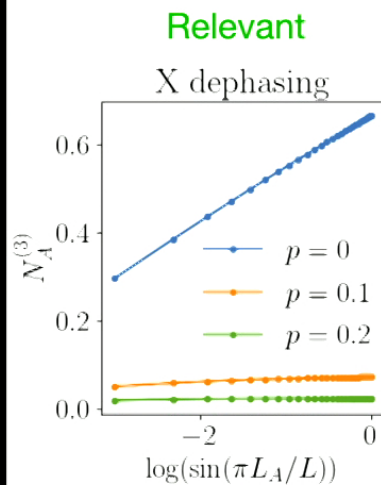


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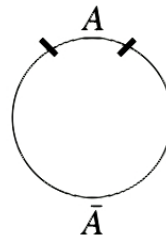
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(Renyi) Entanglement Negativity

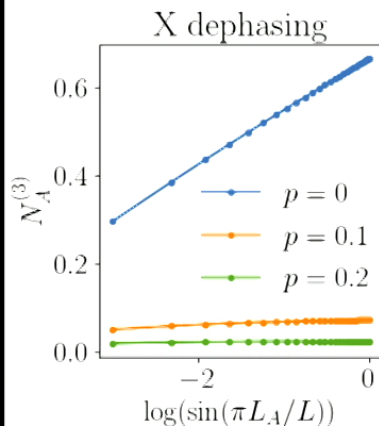


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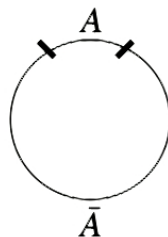


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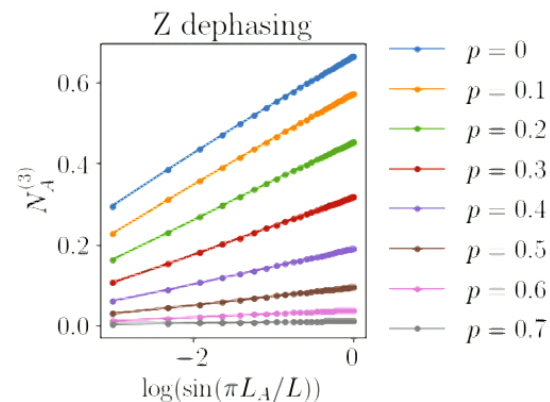
Relevant



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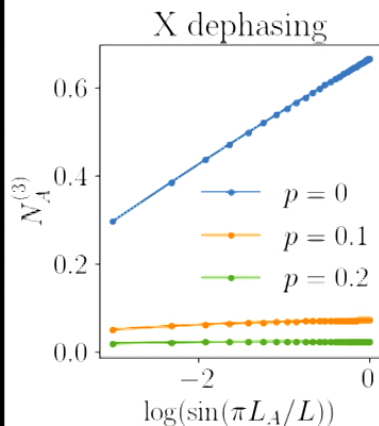


Marginal

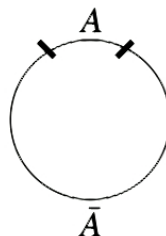


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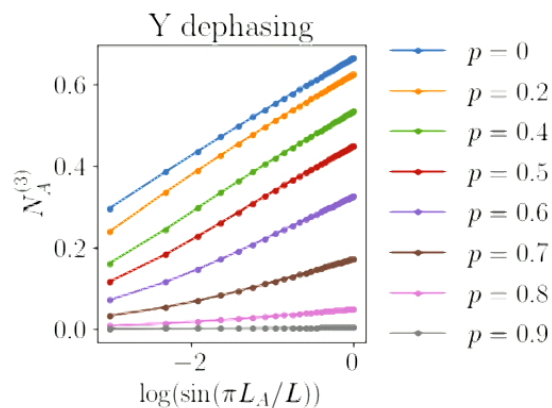
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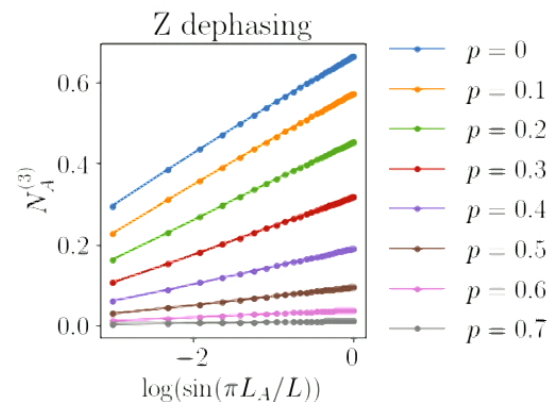
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Irrelevant

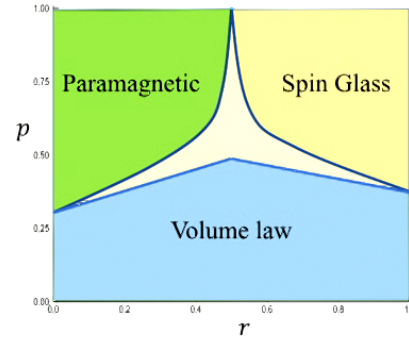
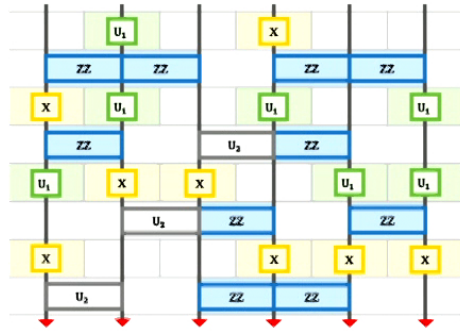


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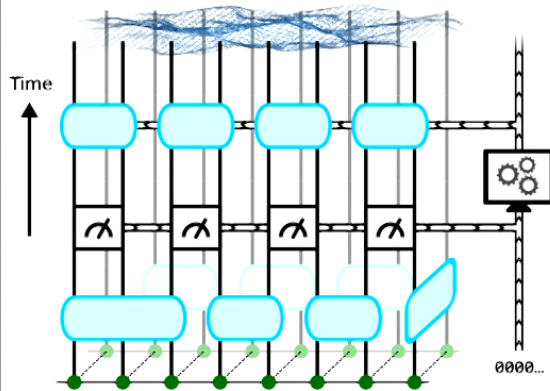


Continuously varying
log coefficient

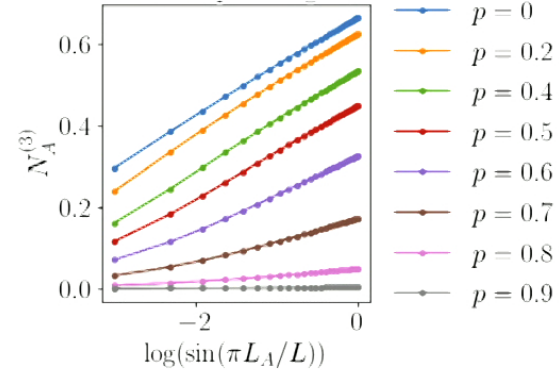
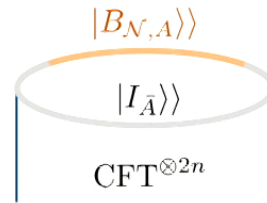
Measurement-enabled long range entangled matter



Sang and TH
 Phys. Rev. Research 3, 023200 (2021)



Lu, Lessa, Kim, and TH
 PRX Quantum 3, 040337 (2022)



Zou, Sang, and TH
 PRL 130, 250403 (2023)

The open quantum frontier

Measurement and decoherence driven
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The open quantum frontier

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Li, Zou, TH (2019)

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Dynamics involving measurement and feedback (quantum-classical interfaces)
for generating novel mixed states?

Thanks



Shengqi Sang
(Perimeter)



Yijian Zou
(Perimeter)



Tsung-Cheng (Peter) Lu
(Perimeter)



Leonardo Lessa
(Perimeter)



Isaac Kim
(UC Davis)