

Title: Piecing Together a Flat Hologram

Speakers: Sabrina Pasterski

Collection: Puzzles in the Quantum Gravity Landscape: viewpoints from different approaches

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Abstract: The Celestial Holography program encompasses recent efforts to understand the flat space hologram in terms of a CFT living on the celestial sphere. A key development instigating these efforts came from understanding how soft limits of scattering encode infinite dimensional symmetry enhancements corresponding to the asymptotic symmetry group of the bulk spacetime. Historically, the construction of the bulk-boundary dual pair has followed bottom up approach matching symmetries on both sides. Recently, however, there has been exciting progress in formulating top down descriptions using insights from twisted holography. We review salient aspects of the celestial construction, the status of the dictionary, and active research directions.



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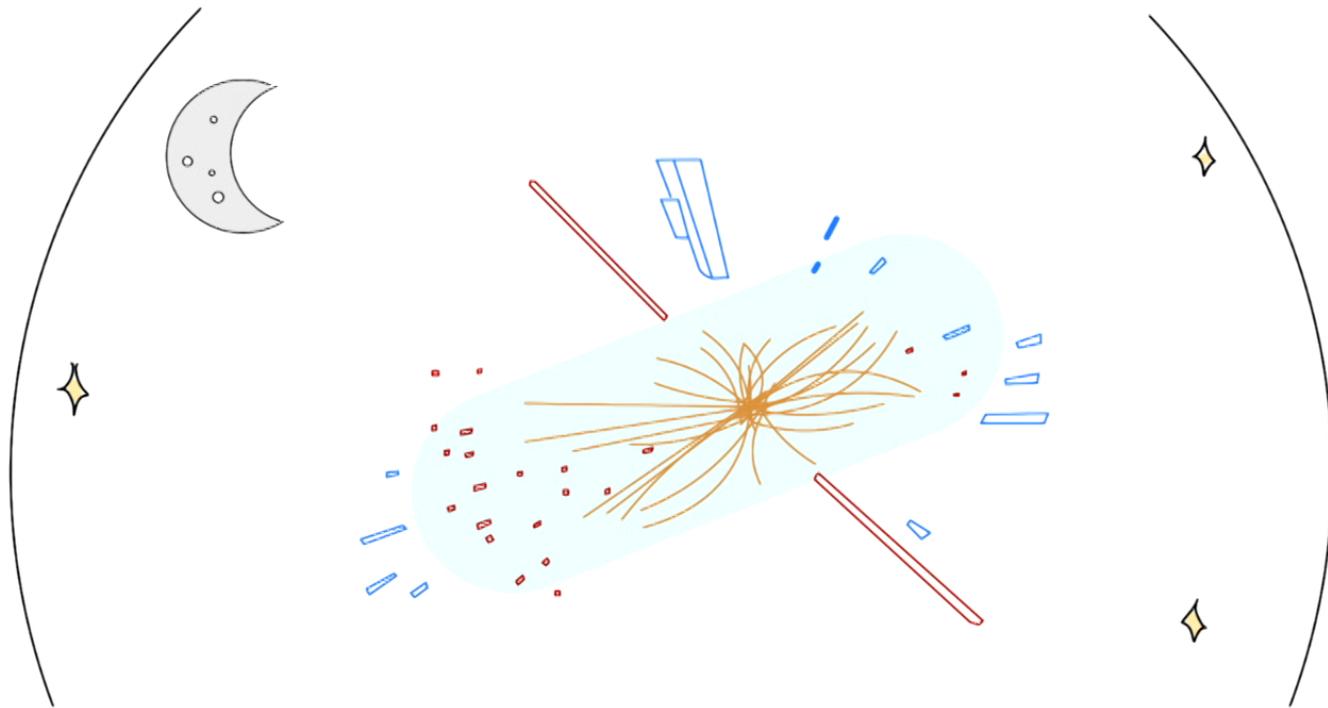
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Piecing Together a Flat Hologram

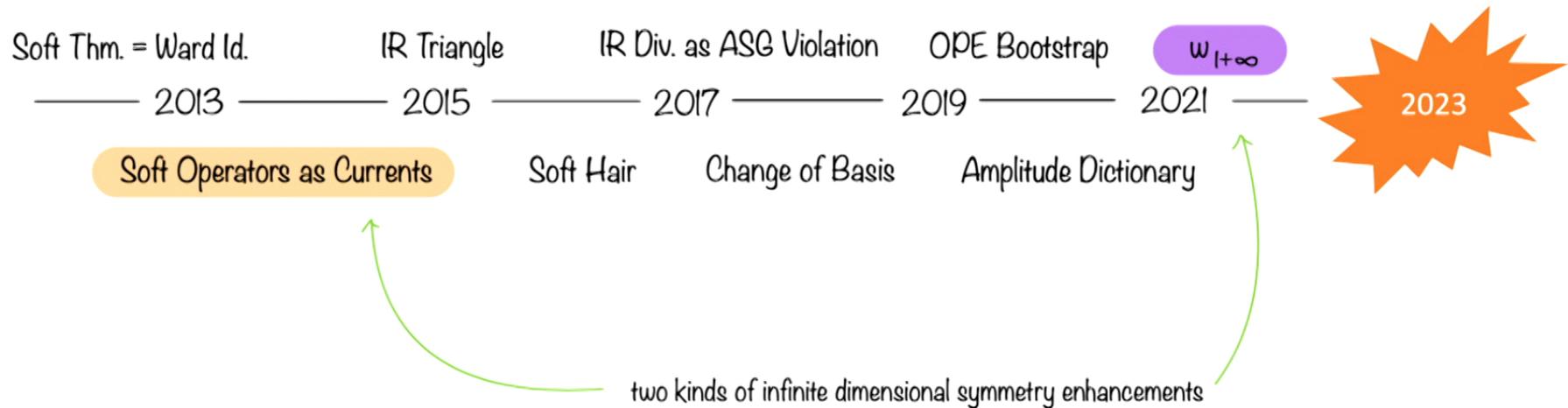
Sabrina Pasterski

The Celestial Conjecture:

scattering in asymptotically flat spacetimes is dual to a CFT living on the celestial sphere

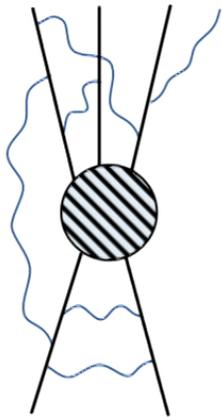


This program evolved from a **bottom-up** approach to flat holography...



... recognizing **soft theorems as Ward Identities** for asymptotic symmetries and recasting the **soft operators as currents** in a codimension 2 CFT.

Soft Thm = Ward Id



\Leftrightarrow

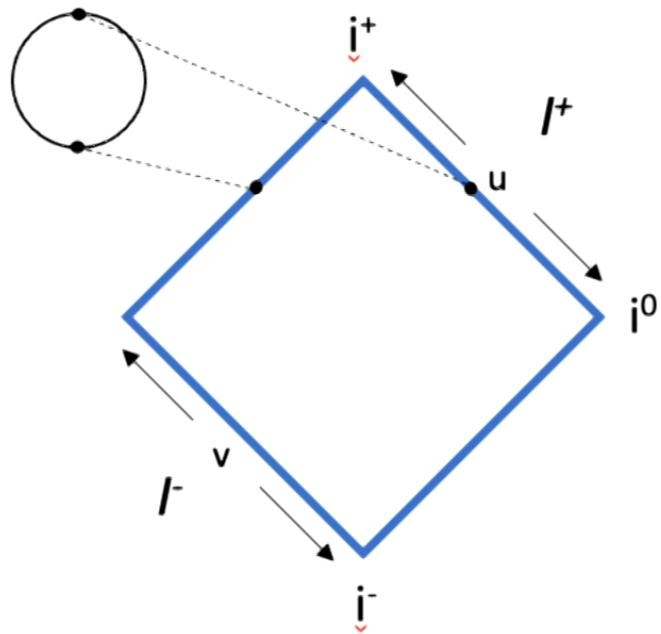
$$\langle out | Q^+ [Y] \mathcal{S} - \mathcal{S} Q^- [Y] | in \rangle = 0$$



$$ds^2 = -dt^2 + dx^2 + dy^2 + dz^2$$

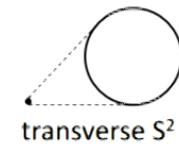


$$G_{\mu\nu} = 8\pi G T_{\mu\nu}$$



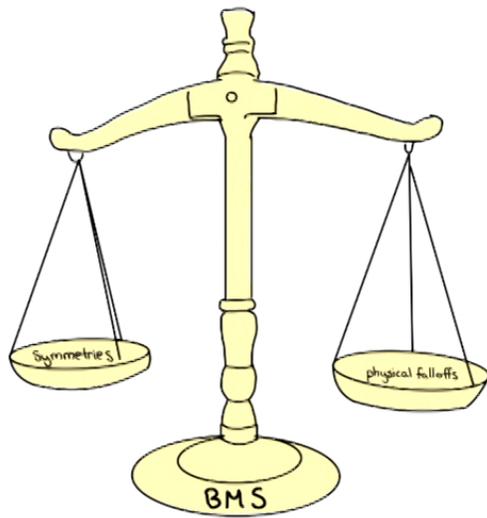
time

light
rays



$$u = t - r$$

$$v = t + r$$



$$\text{ASG} = \frac{\text{allowed gauge symmetries}}{\text{trivial gauge symmetries}}$$

In Bondi gauge the metric near future null infinity takes the form

$$ds^2 = -du^2 - 2dudr + 2r^2\gamma_{z\bar{z}}dzd\bar{z} + 2\frac{m_B}{r}du^2 + (rC_{zz}dz^2 + D^z C_{zz}dudz + \frac{1}{r}(\frac{4}{3}N_z - \frac{1}{4}\partial_z(C_{zz}C^{zz}))dudz + c.c.) + \dots$$

Radiative Data

which is preserved by the residual diffeomorphisms

$$\xi^+ = \underbrace{(1 + \frac{u}{2r})Y^{+z}\partial_z - \frac{u}{2r}D^{\bar{z}}D_z Y^{+z}\partial_{\bar{z}} - \frac{1}{2}(u+r)D_z Y^{+z}\partial_r + \frac{u}{2}D_z Y^{+z}\partial_u + c.c.}_{\text{Supertranslations}} + \underbrace{f^+\partial_u - \frac{1}{r}(D^z f^+\partial_z + D^{\bar{z}} f^+\partial_{\bar{z}}) + D^z D_z f^+\partial_r}_{\text{Superrotations}}$$

$$8\pi G Q^+[Y] = \int_{I^+} \sqrt{\gamma} d^2 z du \left[\underbrace{-\frac{1}{2} D_z^3 Y^z u \partial_u C^{zz}}_{\text{blue line}} + \underbrace{Y^z T_{uz} + u D_z Y^z T_{uu}}_{\text{green line}} + h.c. \right]$$

$$Q^+[Y] = Q_S^+[Y] + Q_H^+[Y]$$

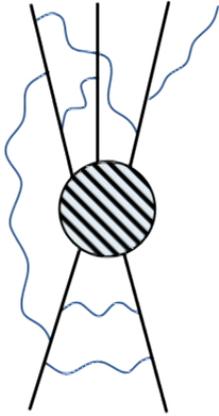
radiative mode 

$$h_{\mu\nu}(x) = \sum_{\alpha=\pm} \int \frac{d^3q}{(2\pi)^3} \frac{1}{2\omega_q} [\epsilon_{\mu\nu}^{\alpha*}(\vec{q}) a_\alpha(\vec{q}) e^{iq\cdot x} + \epsilon_{\mu\nu}^\alpha(\vec{q}) a_\alpha(\vec{q})^\dagger e^{-iq\cdot x}]$$

$$C_{\bar{z}\bar{z}} = 2 \lim_{r \rightarrow \infty} \frac{1}{r} \partial_{\bar{z}} x^\mu \partial_{\bar{z}} x^\nu \sum_{\alpha=\pm} \int \frac{d^3q}{(2\pi)^3} \frac{1}{2\omega_q} [\epsilon_{\mu\nu}^{\alpha*}(\vec{q}) a_\alpha(\vec{q}) e^{-i\omega_q u - i\omega_q r(1-\cos\theta)} + h.c.]$$

saddle 

$$C_{\bar{z}\bar{z}} = -\frac{i}{4\pi^2} \hat{\epsilon}_{\bar{z}\bar{z}}^+ \int_0^\infty d\omega_q [a_-(\omega_q \hat{x}) e^{-i\omega_q u} - a_+(\omega_q \hat{x})^\dagger e^{i\omega_q u}]$$



$$\langle out|a_-(q)\mathcal{S}|in\rangle = \left(S^{(0)-} + S^{(1)-}\right) \langle out|\mathcal{S}|in\rangle + \mathcal{O}(\omega)$$

$$S^{(0)-} = \sum_k \frac{(p_k \cdot \epsilon^-)^2}{p_k \cdot q}$$

$$S^{(1)-} = -i \sum_k \frac{p_{k\mu} \epsilon^{-\mu\nu} q^\lambda J_{k\lambda\nu}}{p_k \cdot q}$$

Soft Thm = Ward Id

$$\langle out | Q^+[Y] \mathcal{S} - \mathcal{S} Q^-[Y] | in \rangle = 0$$

$$Q^+[Y] = Q_S^+[Y] + Q_H^+[Y]$$

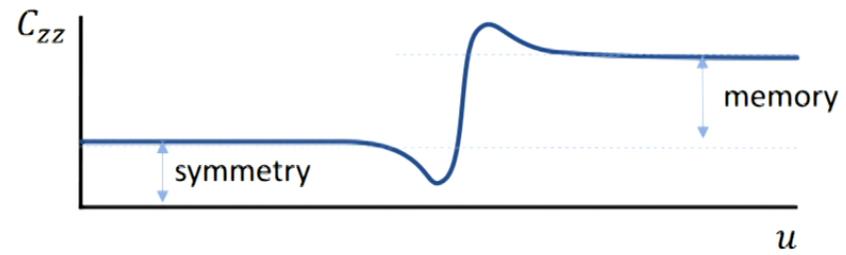
$$Q_S^+[Y] = \frac{1}{2} \int_{\mathcal{I}^+} du d^2z D_z^3 Y^z u \partial_u C_{\bar{z}}$$

$$Q_H^+[Y] = \lim_{\Sigma \rightarrow \mathcal{I}^+} \int_{\Sigma} d\Sigma \xi^\mu n_\Sigma^\nu T_{\mu\nu}^M$$

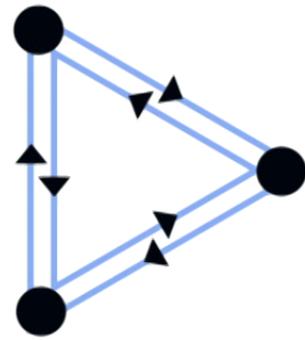
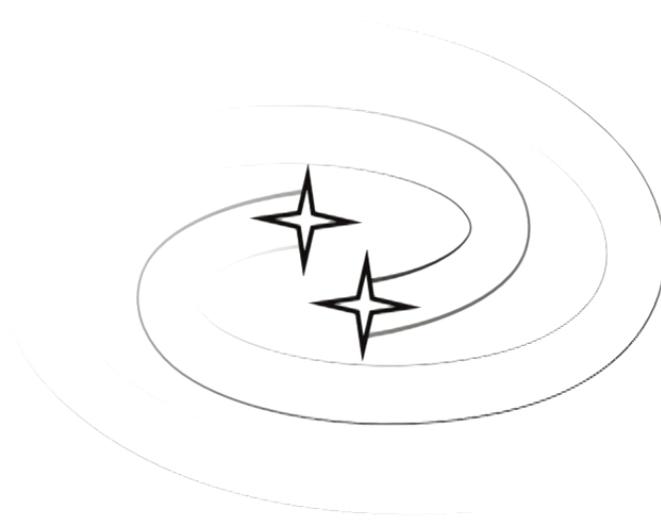
$$\langle out | a_-(q) \mathcal{S} | in \rangle = (S^{(0)-} + S^{(1)-}) \langle out | \mathcal{S} | in \rangle + \mathcal{O}(\omega)$$

$$S^{(1)-} = -i \sum_k \frac{p_{k\mu} \epsilon^{-\mu\nu} q^\lambda J_{k\lambda\nu}}{p_k \cdot q}$$

Soft Thm = Memory



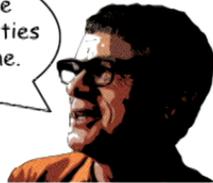
Soft Thm = Memory



IR Triangle

Our story starts with Strominger's suggestion that...

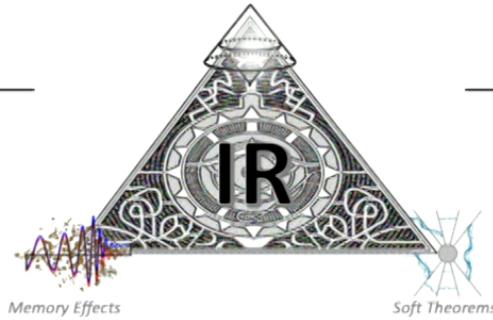
...a series of separate studies from the sixties are secretly the same.



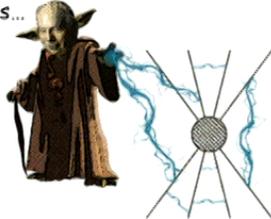
The relativists were systematizing what happens at long distances...



Asymptotic Symmetries



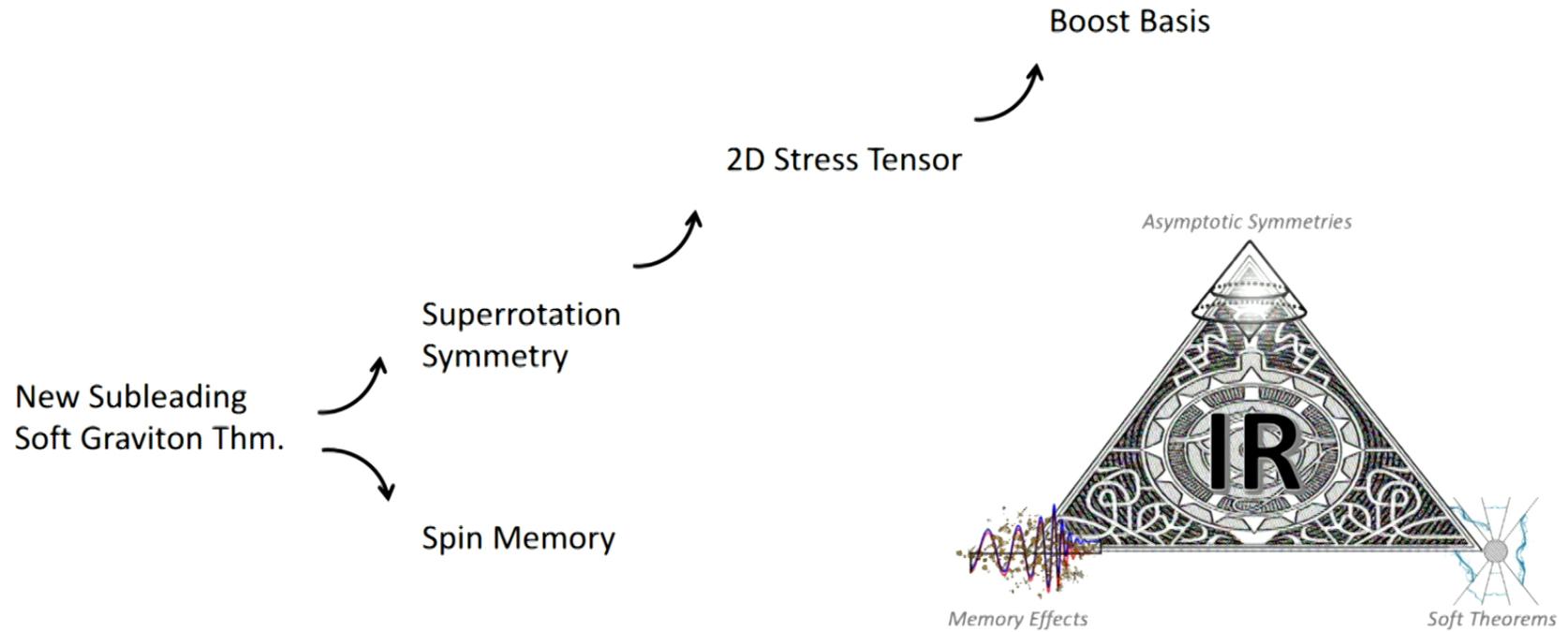
The quantum field theorists were worried about what was going on at low energies...



And, a little later, someone remembered there was a physical observable attached to each of these things....



IR Triangle



4D Soft Mode = 2D Current

For a particular choice of Y

$$T_{zz} = 2iQ_S^+ (Y^w = \frac{1}{z-w}, Y^{\bar{w}} = 0)$$

the superrotation Ward Id takes the form of a 2D stress tensor Ward Id.

$$\langle T_{zz} \mathcal{O}_1 \cdots \mathcal{O}_n \rangle = \sum_{k=1}^n \left[\frac{h_k}{(z-z_k)^2} + \frac{\Gamma_{z_k z_k}^{z_k}}{z-z_k} h_k + \frac{1}{z-z_k} (\partial_{z_k} - |s_k| \Omega_{z_k}) \right] \langle \mathcal{O}_1 \cdots \mathcal{O}_n \rangle$$

subleading soft
graviton theorem

=

Ward identity for
4D superrotations

=

Ward identity for
2D stress tensor



the asymptotic symmetry is physical

subleading soft
graviton theorem

=

Ward identity for
4D superrotations

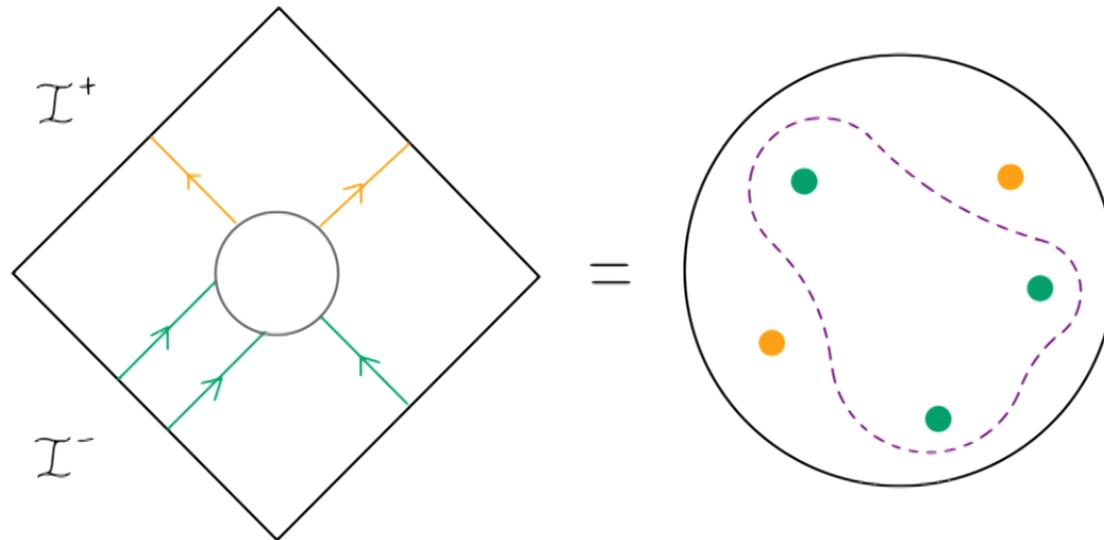
=

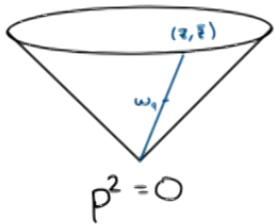
Ward identity for
2D stress tensor



we should look for a 2D dual CFT

4D Soft Mode = 2D Current



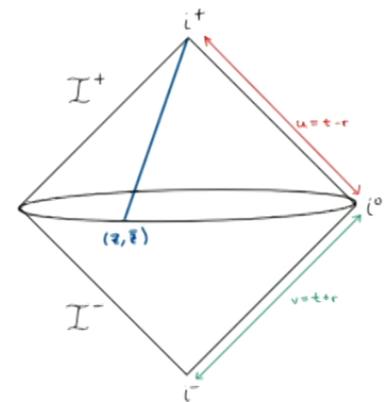


4D Amplitude = 4D Correlator

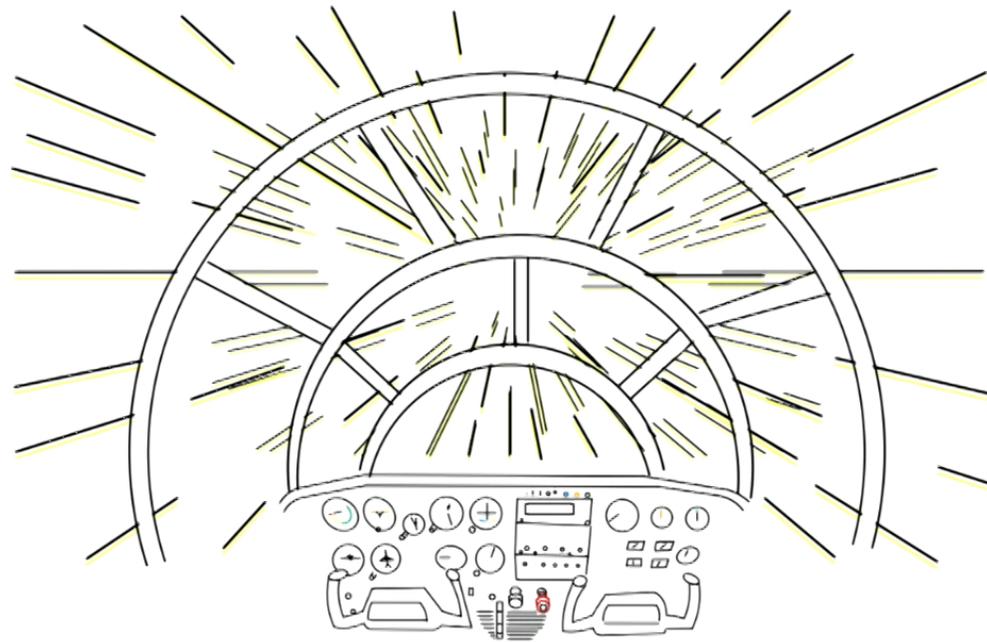
LSZ \Leftrightarrow Extrapolate Dict.

$$\langle out|S|in\rangle_{boost} = \prod_i \lim_{r \rightarrow \infty} \int_{-\infty}^{\infty} d\nu_i \nu_i^{-\Delta_i} \langle r\Phi(\nu_1, r, z_1, \bar{z}_1) \dots r\Phi(\nu_n, r, z_n, \bar{z}_n) \rangle$$

$$\nu = \{u, v\}$$



4D Amplitude = 2D Correlator

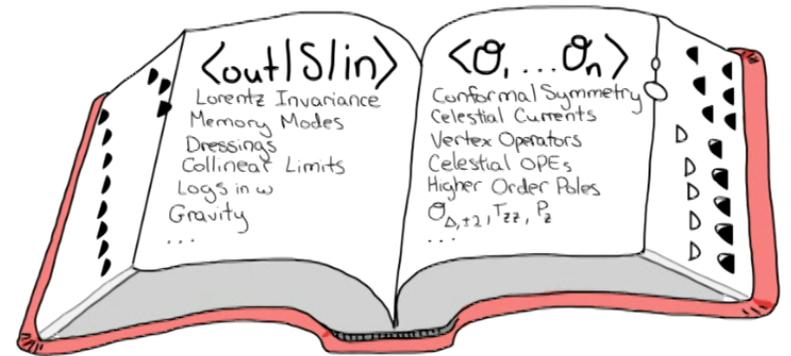


4D Amplitude = 2D Correlator

4D Lorentz invariance = 2D global conformal symmetry

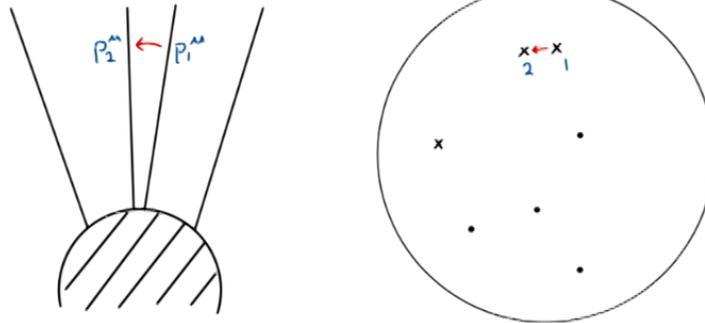
$$\langle \mathcal{O}_{\Delta_1}^{\pm}(z_1, \bar{z}_1) \dots \mathcal{O}_{\Delta_n}^{\pm}(z_n, \bar{z}_n) \rangle = \prod_{i=1}^n \int_0^{\infty} d\omega_i \omega_i^{\Delta_i - 1} \langle out | \mathcal{S} | in \rangle$$

If we go to a boost basis, amplitudes transform as CFT correlators under the Lorentz group.



Collinear Limit = OPE

$$\begin{aligned} \mathcal{O}_{\Delta_1,+2}(z_1, \bar{z}_1) \mathcal{O}_{\Delta_2,+2}(z_2, \bar{z}_2) &\sim -\frac{\kappa \bar{z}_{12}}{2 z_{12}} B(\Delta_1 - 1, \Delta_2 - 1) \mathcal{O}_{\Delta_1+\Delta_2,+2}(z_2, \bar{z}_2) + \dots, \\ \mathcal{O}_{\Delta_1,+2}(z_1, \bar{z}_1) \mathcal{O}_{\Delta_2,-2}(z_2, \bar{z}_2) &\sim -\frac{\kappa \bar{z}_{12}}{2 z_{12}} B(\Delta_1 - 1, \Delta_2 + 3) \mathcal{O}_{\Delta_1+\Delta_2,-2}(z_2, \bar{z}_2) \\ &\quad - \frac{\kappa z_{12}}{2 \bar{z}_{12}} B(\Delta_1 + 3, \Delta_2 - 1) \mathcal{O}_{\Delta_1+\Delta_2,+2}(z_2, \bar{z}_2) + \dots, \end{aligned}$$



2D Radial Quantization → More Symmetries

For special weights, the $SL(2, \mathbb{C})$ multiplets have primary descendants.

$$H^k(z, \bar{z}) := \lim_{\epsilon \rightarrow 0} \epsilon \mathcal{O}_{k+\epsilon, 2}(z, \bar{z}), \quad \Delta = k = 2, 1, 0, -1, \dots$$

Assuming these multiplets shorten, we have

$$H^k(z, \bar{z}) = \sum_{m=\frac{k-2}{2}}^{\frac{2-k}{2}} \bar{z}^{-\frac{k-2}{2}-m} H_m^k(z), \quad w_n^p = \frac{1}{\kappa} (p-n-1)!(p+n-1)! H_n^{-2p+4}$$

2D Radial Quantization → More Symmetries

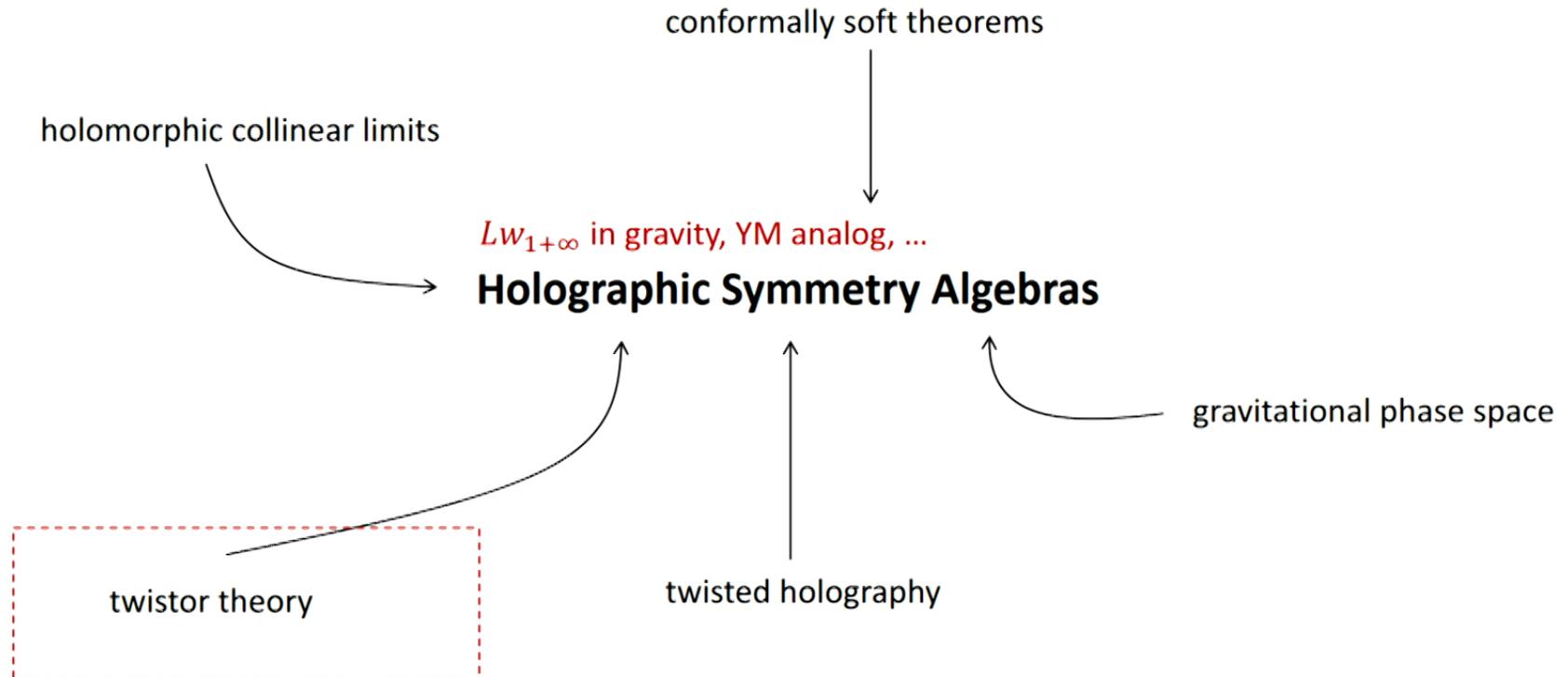
Complexifying the celestial sphere variables and defining a holomorphic commutator

$$[A, B](z) = \frac{1}{2\pi i} \oint_z dw A(w)B(z)$$

gives a $Lw_{1+\infty}$ symmetry algebra for appropriately rescaled modes

$$\left[w_n^p, w_m^q \right](z) = \left[n(q-1) - m(p-1) \right] w_{m+n}^{p+q-2}(z)$$

Celestial Algebra = Sym of SDG



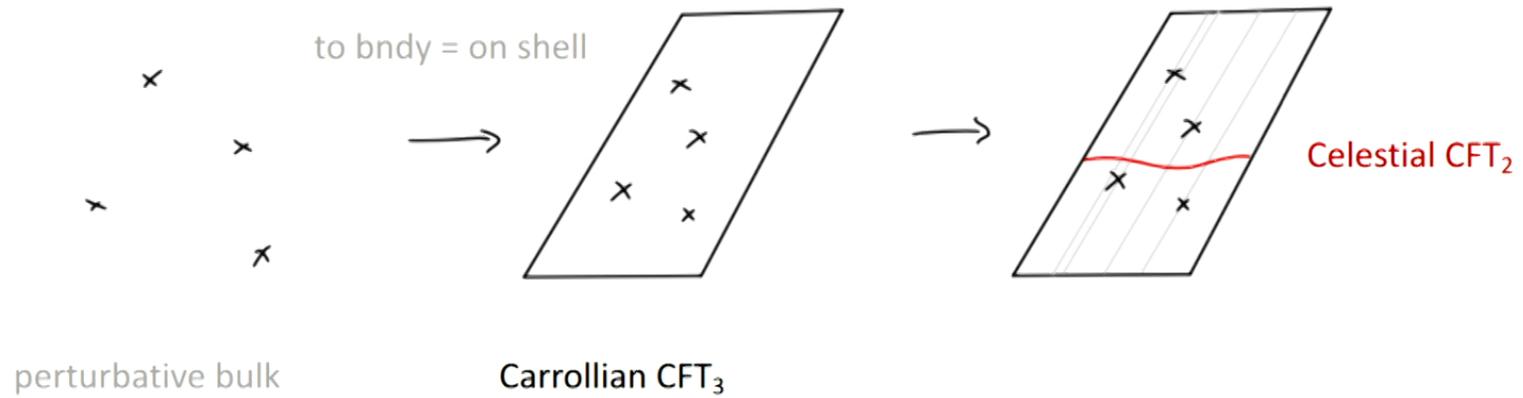
Do these symmetries beyond tree level, or the self-dual sector?

Can we realize them in the matter sector?

Can we really complexify the celestial sphere to define these currents?



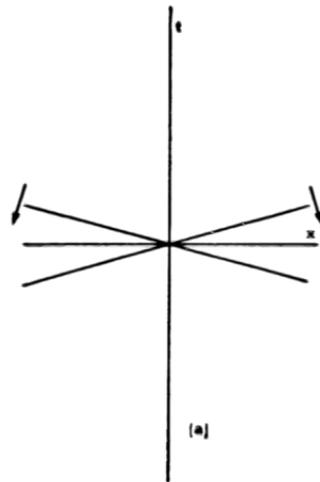
Celestial = Carrollian



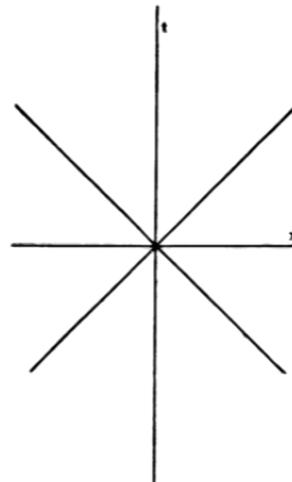
Celestial = Carrollian

$$ds^2 = -c^2 dt^2 + d\vec{x}^2$$

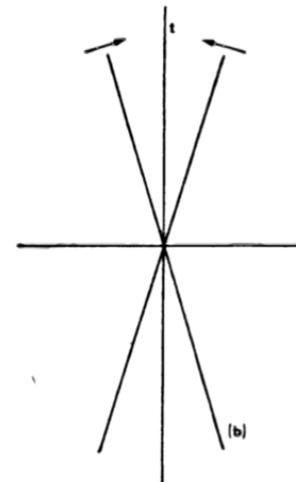
$c \rightarrow \infty$
Galilean



$c = 1$
Lorentzian



$c \rightarrow 0$
Carrollian

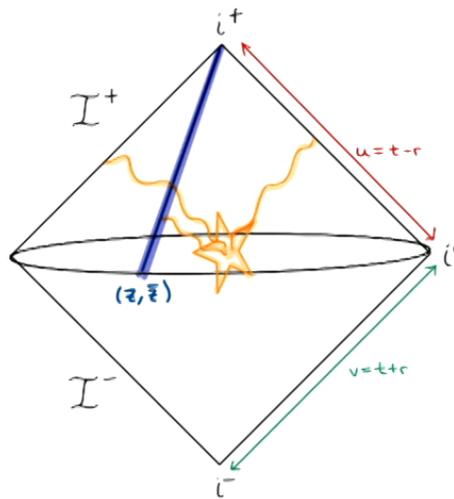


Hard Charges = Light Ray Operators

$$Q_{H,matter}^{\mathcal{J}^+}$$



$$\mathcal{E}(z, \bar{z}) = \lim_{r \rightarrow \infty} r^2 \int du T_{uu}(u, r, z, \bar{z})$$



Hard Charges = Light Ray Operators

CCFT

$$\langle \mathcal{O}_{\Delta_1}^{\pm}(z_1, \bar{z}_1) \dots \mathcal{O}_{\Delta_n}^{\pm}(z_n, \bar{z}_n) \rangle$$

Single Particle

Exclusive

vs

Conformal Colliders

$$\frac{\langle 0 | \mathcal{O}^{\dagger} \mathcal{E}(\theta_1) \dots \mathcal{E}(\theta_n) \mathcal{O} | 0 \rangle}{\langle 0 | \mathcal{O}^{\dagger} \mathcal{O} | 0 \rangle}$$

2-Particle

Inclusive

Hard Charges = Light Ray Operators

CCFT

$$\langle \mathcal{O}_{\Delta_1}^{\pm}(z_1, \bar{z}_1) \dots \mathcal{O}_{\Delta_n}^{\pm}(z_n, \bar{z}_n) \rangle$$

Single Particle

Exclusive

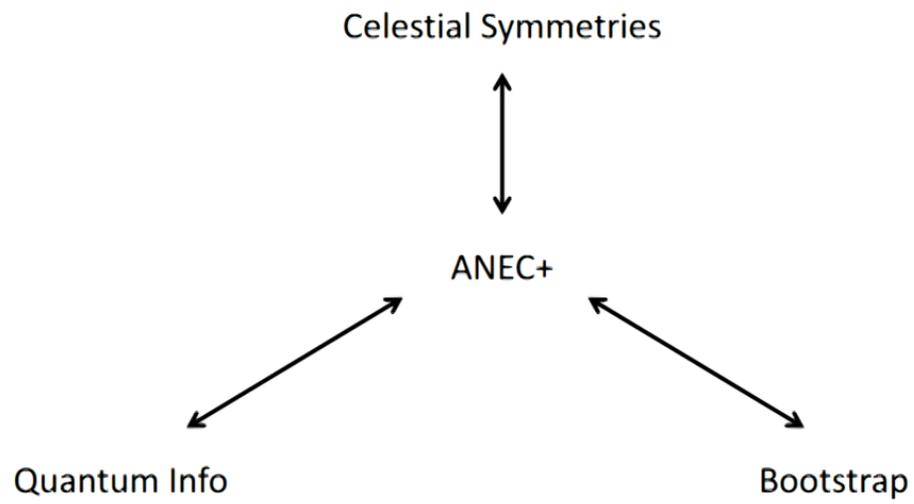
vs

Conformal Colliders

$$\frac{\langle 0 | \mathcal{O}^{\dagger} \mathcal{E}(\theta_1) \dots \mathcal{E}(\theta_n) \mathcal{O} | 0 \rangle}{\langle 0 | \mathcal{O}^{\dagger} \mathcal{O} | 0 \rangle}$$

2-Particle

Inclusive



Amplitudes

It From Qubit

soft and collinear factorization

conformal field theory

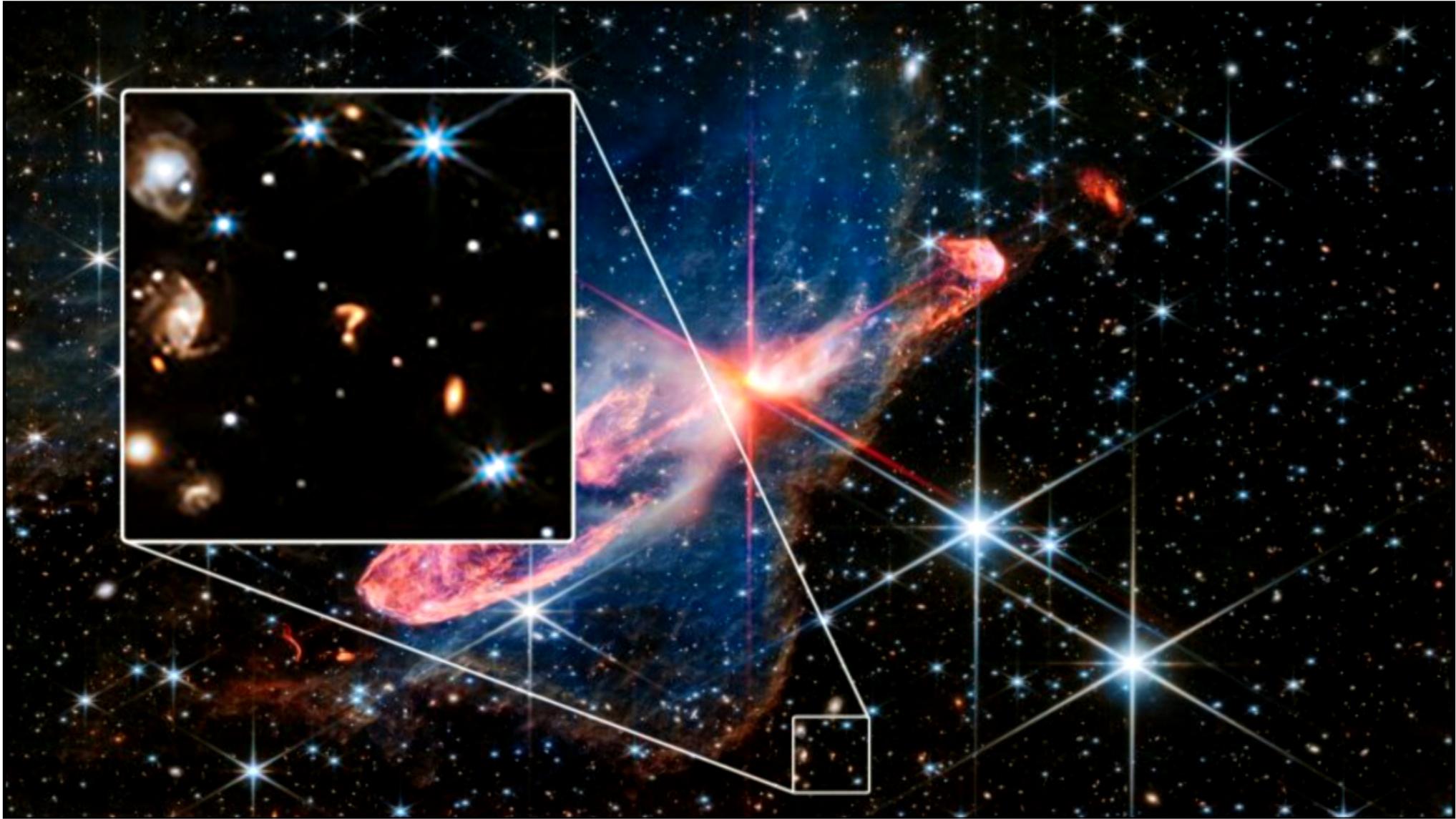
finite S-matrix

detector operators

complex spin

light ray operators

Bootstrap





Kevin Costello



Laurent Freidel



Sabrina Pasterski

Perimeter Institute for Theoretical Physics



Monica Pate

NYU



Nima Arkani-Hamed

IAS



Tim Adamo

University of Edinburgh



Lionel Mason

Oxford



Natalie Paquette

University of Washington



Andrew Strominger



Jordan Cotler

Harvard University



Tomasz Taylor

Northeastern



Andrea Puhm

École Polytechnique



David Skinner

Cambridge



