

Title: QFT1 Lecture - 102723

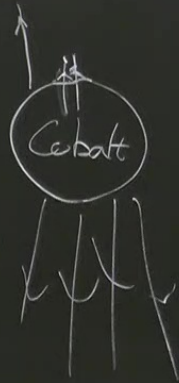
Speakers: Gang Xu

Collection: Quantum Field Theory 1 2023/24

Date: October 27, 2023 - 10:45 AM

URL: <https://pirsa.org/23100053>

Interaction Lagrangian
parallel universe
CS Wu's puzzle



beta decay
electrons
photons

angian.

• which interaction is responsible?

conclusion: Parity is not a symmetry.

$$\begin{cases} x \rightarrow -x \\ y \rightarrow -y \\ z \rightarrow -z \end{cases} \rightarrow \pi, \pi \text{ rotation}$$

+ flip z

① mirror symmetry.

②

tion is responsible?
vity is not a symmetry.

② momentum flip
L :

→ π rotation
+ flip z

① mirror symmetry

② choose directions
→ perpendicular

tion is responsible?
vity is not a symmetry.

→ xy, π rotation
+ flip z

① mirror symmetry

② choose directions
→ perpendicular

③ momentum flip
 L : not flip

④ helicity : flip

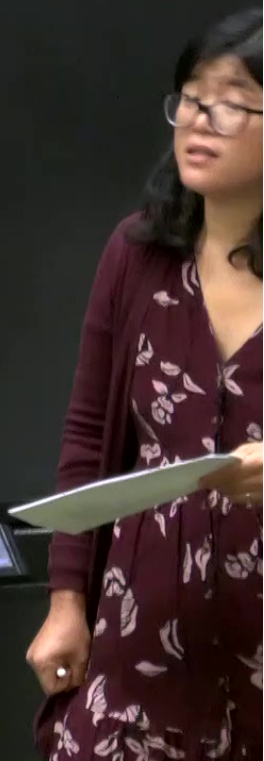
⑤ right handed Weyl spinor

mirror → left handed Weyl spinor

$$\psi_+ \xleftrightarrow{\text{Mirror}} \psi_-$$

$$\begin{pmatrix} w_+ \\ w_- \end{pmatrix} \leftrightarrow \begin{pmatrix} w_- \\ w_+ \end{pmatrix}$$

$$P\psi(t, x)P = \underline{\gamma}^0 \psi(t, -x)$$
$$P\psi^+(t, x)P = \psi^+(t, -x)\underline{\gamma}^0$$
$$\underline{\gamma}^0 = \begin{pmatrix} 1 & \\ & 1 \end{pmatrix} \quad \underline{\gamma}^i = \begin{pmatrix} & \sigma^i \\ -\sigma^i & \end{pmatrix}$$



γ^0) List of suspects (a thorough search) $\rightarrow \sum \Lambda_n \phi^n$

$\mathcal{L}_{\text{Free}} = \bar{\psi} (i \gamma^\mu \partial_\mu - m) \psi$

- $\bar{\psi} \psi$ — mass term \rightarrow Yukawa
- $\bar{\psi} \gamma^\mu \psi$ — kinetic term \rightarrow QED
- $\bar{\psi} \gamma^\mu \gamma^5 \psi$ — $\bar{\psi} \gamma^\mu \psi$ — weak interaction
- $\bar{\psi} \gamma^\mu \gamma^5 \psi$ — $\bar{\psi} \gamma^5 \psi$ — spoiler, this is the one
- $\bar{\psi} \gamma^\mu \gamma^5 \psi$ — $\bar{\psi} \gamma^5 \psi$
- ~~$\bar{\psi} \gamma^\mu \gamma^5 \psi$~~

$$\begin{aligned}
& P \bar{\psi} \psi P \\
&= P \psi^\dagger \gamma^0 \psi P \\
&= P \psi^\dagger P \gamma^0 P \psi P \\
&= \underbrace{\psi^\dagger(t, -x) \gamma^0 \gamma^0 \gamma^0}_{\bar{\psi}(t, -x)} \underbrace{\psi(t, -x)}_{\psi(t, -x)} \\
&= \bar{\psi}(t, -x) \psi(t, -x)
\end{aligned}$$

$$P \not\psi^t \gamma^0 \gamma^\mu \gamma^5 \not\psi P$$

$$= \not\psi^t(t, -x) \cancel{\gamma^0} \gamma^\mu \gamma^5 \not\psi(t, -x)$$

$$\left\{ \begin{array}{l} \mu=0 \\ \mu=i \end{array} \right. \quad - \not\psi(t, -x) \cdot \gamma^0 \cdot \gamma^5 \not\psi(t, -x)$$

$$\left\{ \begin{array}{l} \mu=0 \\ \mu=i \end{array} \right. \quad + \not\psi(t, -x) \gamma^i \gamma^5 \not\psi(t, -x)$$

$$\underbrace{\gamma^0 \not\psi(t, -x)}$$

$$\gamma^0 \gamma^5 \gamma^0$$

$$-\gamma^0 \gamma^0 \gamma^5$$

Parity: time same
space flipped $\rightarrow p^\mu$ vector

$(t, -x)$ time flipped

$$\begin{pmatrix} 1 & & & \\ & -1 & & \\ & & -1 & \\ & & & -1 \end{pmatrix}$$

$(t, -x)$ space same \rightarrow axial-vector

first try

$$\bar{\psi} \gamma^\mu \psi A_\mu \rightarrow \bar{\psi} \gamma^\mu \psi A_\mu + \bar{\psi} \gamma^\mu \psi \partial_\mu \alpha$$

resolution

$$\psi \rightarrow \psi e^{-ie\alpha(x)}$$

$$\psi^\dagger \rightarrow \psi^\dagger e^{ie\alpha(x)}$$

mass term ✓

$$\bar{\psi} i \gamma^\mu \partial_\mu \psi$$

$$\rightarrow \bar{\psi} e^{+ie\alpha(x)} i \gamma^\mu (\partial_\mu \psi e^{-ie\alpha(x)} + \psi (-ie \partial_\mu \alpha(x)) e^{-ie\alpha(x)})$$

$$= \bar{\psi} i \gamma^\mu \partial_\mu \psi + \bar{\psi} i \gamma^\mu \psi (-ie \partial_\mu \alpha(x))$$

vector field - photo
 $A_\mu \rightarrow A_\mu - \partial_\mu \alpha$

first try
 $\bar{\psi} \gamma^\mu \psi A_\mu \rightarrow \bar{\psi} \gamma^\mu \psi A_\mu - (\bar{\psi} \gamma^\mu \psi) \partial_\mu \alpha$

resolution
 $\psi \rightarrow \psi e^{-ie\alpha(x)}$
 $\psi^\dagger \rightarrow \psi^\dagger e^{ie\alpha(x)}$

mass term ✓

$$e \bar{\psi} \gamma^\mu \psi A_\mu + \bar{\psi} i \gamma^\mu \partial_\mu \psi$$

$\psi \rightarrow \psi e^{-ie\alpha(x)}$
 $\bar{\psi} \rightarrow \bar{\psi} e^{ie\alpha(x)}$
 $i \gamma^\mu (\partial_\mu \psi e^{-ie\alpha(x)} + \psi (-ie \partial_\mu \alpha) e^{-ie\alpha(x)})$

$$= \bar{\psi} i \gamma^\mu \partial_\mu \psi + \bar{\psi} i \gamma^\mu \psi (-ie \partial_\mu \alpha)$$

$e \left(\bar{\psi} \gamma^\mu \psi \partial_\mu \alpha \right)$

$$\bar{\psi} i (\underbrace{\partial_\mu + ieA_\mu}_{D_\mu}) \gamma^\mu \psi$$

$$\bar{\Phi}^+ \Phi$$

$$= \bar{\psi} (iD_\mu \gamma^\mu - m) \psi$$

$$- \int \bar{D}_\mu \Phi^+ D^\mu \Phi$$

apple . rotate
eat apple skin
has a stem
red