

Title: BSM Theory

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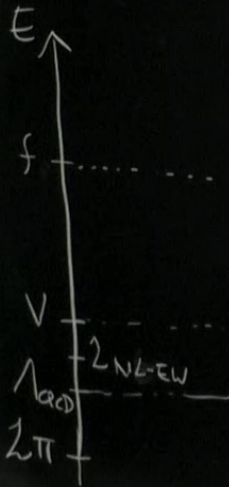
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SUMMARY

- SUPERSYMMETRY
- COMPOSITE HIGGS / EXTRA-DIMENSIONS
- (• ANTHROPIC / COSMOLOGICAL)



◦ COMPOSITE HIGGS / EXTRA-DIMENSIONS
(◦ ANTHROPIC / COSMOLOGICAL)

E

f

• Non-linear chiral Lagrangian
(Sigma model)

V

$2v$

Λ_{QCD}

$2\pi f$

2x2 MATRIX SCALARS

$$\mathcal{L} = \bar{\Psi} i \gamma^\mu \partial_\mu \Psi + g (\bar{\Psi}_L \Sigma \Psi_R + \bar{\Psi}_R \Sigma \Psi_L) \quad (+ \quad - \quad - \quad -)$$

$$\Sigma = \sigma \mathbb{1}_{2 \times 2} + i \vec{\pi} \cdot \vec{\sigma}$$

$$+ \frac{1}{2} (\partial_\mu \phi)^2 + \frac{1}{2} (\partial_\mu \pi)^2 - \frac{M^2}{2} (\phi^2 + \vec{\pi}^2) - \frac{\lambda}{4} (\phi^2 + \vec{\pi}^2)^2$$

$$U_{L,R} = e^{i \frac{1}{2} \alpha^a_{L,R} \sigma^a}$$

Σ transforms under $SU(2)_L \times SU(2)_R$ $\Sigma \rightarrow U_L \Sigma U_R$

$$\phi = \begin{pmatrix} \pi_1 \\ \pi_2 \\ \pi_3 \\ \phi \end{pmatrix} \quad V = \frac{M^2}{2} \phi^2 + \frac{\lambda}{4} \phi^4 \quad SO(4)$$

$$\bullet \langle \phi \rangle = f \Rightarrow \sigma^2 + \pi^2 = f^2 \quad \text{choose } \langle \sigma \rangle = f \quad \langle \pi \rangle = 0$$

$\begin{matrix} \nearrow \\ -\frac{\pi^2}{f} \\ \nearrow \end{matrix}$

shift $\sigma \rightarrow \sigma - f$

$$\mathcal{L} = \bar{\Psi} i \gamma^\mu \partial_\mu \Psi + g f \bar{\Psi} \Psi - \lambda f^2 \sigma^2 + g \bar{\Psi} (\sigma + i \vec{\sigma} \cdot \vec{\pi}) \Psi$$

$$- \frac{\lambda}{4} (\sigma^2 + \pi^2)^2 - \lambda f \sigma (\sigma^2 + \pi^2)$$

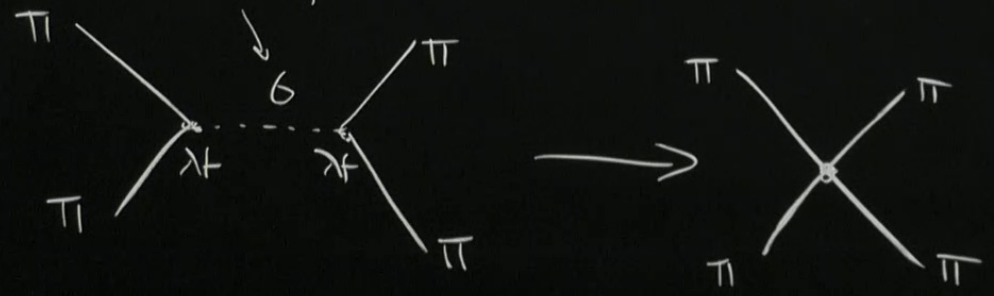
$\frac{-\sqrt{3}}{2}$

shift $\sigma \rightarrow \sigma - f$

$$\mathcal{L} = \bar{\Psi} i \gamma^\mu \partial_\mu \Psi + g \bar{\Psi} \Psi - \lambda f^2 \sigma^2 + g \bar{\Psi} (\sigma + i \vec{\sigma} \cdot \vec{\pi}) \Psi$$

$$- \frac{\lambda}{4} (\sigma^2 + \vec{\pi}^2)^2 - \lambda f \sigma (\sigma^2 + \vec{\pi}^2)$$

$m_\sigma \sim \sqrt{\lambda} f$



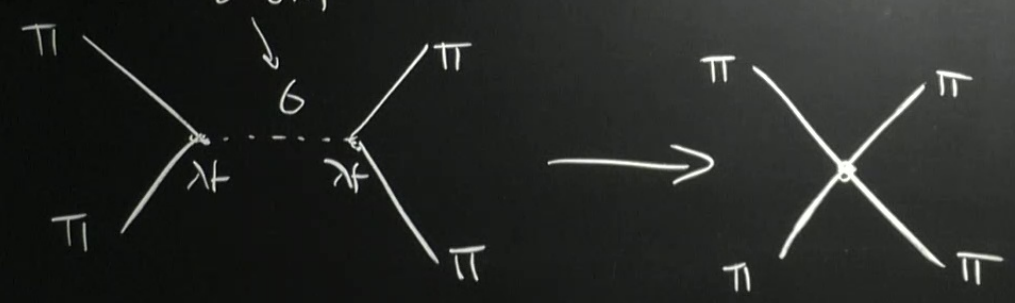
$-\frac{\lambda^2}{f}$

$\rightarrow \sigma - f$

$$\mathcal{L} = \bar{\Psi} i \gamma^\mu \partial_\mu \Psi + g \bar{\Psi} \Psi - \lambda f^2 \sigma^2 + g \bar{\Psi} (\sigma + i \vec{\sigma} \cdot \vec{\pi}) \Psi$$

$$- \frac{\lambda}{4} (\sigma^2 + \vec{\pi}^2)^2 - \lambda f \sigma (\sigma^2 + \vec{\pi}^2)$$

$m_\sigma \sim \sqrt{\lambda} f$



But As $f \rightarrow \infty$ coupling $\lambda f \rightarrow \infty$

• How to decouple heavy σ in a symmetry-respecting way!

$$\underbrace{\phi^2}_{\sigma^2 + \vec{\pi}^2} = f^2 \Rightarrow \sigma = \sqrt{f^2 - \vec{\pi}^2} \simeq f \left(1 - \frac{1}{2} \frac{\vec{\pi}^2}{f^2} + \dots \right)$$

$$\mathcal{L}_\pi \equiv \frac{1}{2} \left[(\partial_\mu \vec{\pi})^2 + \frac{(\vec{\pi} \cdot \partial_\mu \vec{\pi})^2}{f^2 - \vec{\pi}^2} \right] + g \bar{\Psi} \left[\sqrt{f^2 - \vec{\pi}^2} + i \vec{\sigma} \cdot \vec{\pi} \right] \Psi$$

• Use a different parametrisation of 4 scalar d.o.f.:

$$\Sigma = \rho U \quad U = e^{i \vec{\pi} \cdot \vec{\sigma} / f}$$

$\vec{\sigma}$
Singlet under full $SU(2)_L \times SU(2)_R$ triplet

$$\rho^2 = \frac{1}{2} \text{Tr}(\Sigma^\dagger \Sigma) = G^2 + \pi^2 = f^2 \quad \text{shift } \rho \rightarrow \rho - f$$

$$\mathcal{L} = \frac{f^2}{4} \text{Tr}(\partial_\mu U^\dagger \partial^\mu U) + \bar{\Psi} i \gamma^\mu \partial_\mu \Psi + g t (\bar{\Psi}_L U \Psi_R + \bar{\Psi}_R U^\dagger \Psi_L)$$

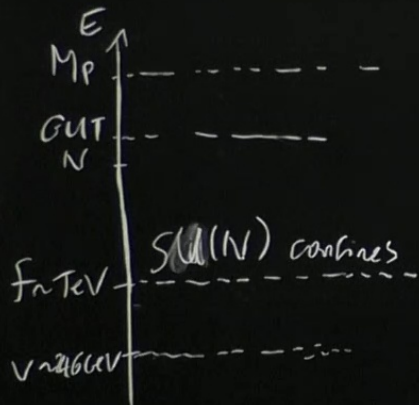
• $\vec{\xi}$ transforms non-linearly under $SU(2)_L \times SU(2)_R$: $LU R^\dagger \Rightarrow \xi' = f(\xi)$

• $SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$ in QCD: confinement of quarks
 $\langle \bar{q}_L q_R \rangle \sim \langle \bar{q}_L q_R \rangle$

• $SU(3)_L \times SU(3)_R \rightarrow SU(3)_V$

• explicit breaking from quark masses

COMPOSITE HIGGS



Global symmetry G broken to H

$$SO(5) \rightarrow SO(4) \Rightarrow \text{no. of Goldstones} = 4$$

\Rightarrow Higgs as a pNGB

$$\vec{\phi} = \begin{pmatrix} \phi_1 \\ \phi_2 \\ \phi_3 \\ \phi_4 \end{pmatrix}$$

$$\Phi = \begin{pmatrix} \phi_1 \\ \phi_2 \\ \phi_3 \\ \phi_4 \\ \sigma \end{pmatrix}$$

$$\Rightarrow \phi^2 + \sigma^2 = f^2 \Rightarrow \sigma = \sqrt{f^2 - \phi^2}$$

2x2 MATRIX SCALARS

$$\mathcal{L} = \bar{\Psi} i \gamma^\mu \partial_\mu \Psi + g (\bar{\Psi}_L \Sigma \Psi_R + \bar{\Psi}_R \Sigma \Psi_L) \quad (+ \dots)$$

$$\Sigma = \sigma \mathbb{1}_{2 \times 2} + i \vec{\pi} \cdot \vec{\sigma}$$

$$+ \frac{1}{2} (\partial_\mu \sigma)^2 + \frac{1}{2} (\partial_\mu \vec{\pi})^2 - \frac{M^2}{2} (\sigma^2 + \vec{\pi}^2) - \frac{\lambda}{4} (\sigma^2 + \vec{\pi}^2)^2$$

$$U_{L,R} = e^{-\frac{i}{2} \alpha^a_{L,R} \sigma^a}$$

Σ transforms under $SU(2)_L \times SU(2)_R$ $\Sigma \rightarrow U_L \Sigma U_R^\dagger$

$SU(2)_L \times SU(2)_R \rightarrow SO(4)$

$$\phi = \begin{pmatrix} \pi_1 \\ \pi_2 \\ \pi_3 \\ \sigma \end{pmatrix}$$

$$V = \frac{M^2}{2} \phi^2 + \frac{\lambda}{4} \phi^4$$

$$\mathcal{L} = \frac{1}{2} D_\mu \Phi^\dagger D^\mu \Phi + (2m - ig W_\mu^a T_L^a - g' B T_R^3)$$

$$= (2ph)^2 + (2m \sqrt{f^2 - (h+v)^2})^2$$

$$H = \begin{pmatrix} h_u \\ h_d \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_2 + i\phi_1 \\ \phi_4 - i\phi_3 \end{pmatrix}$$

$$= \begin{pmatrix} 0 \\ \frac{1}{\sqrt{2}}(v+h) \end{pmatrix}$$

$$\Phi = \begin{pmatrix} 0 \\ 0 \\ 0 \\ v+h \\ \sqrt{f^2 - (h+v)^2} \end{pmatrix}$$

$$\begin{aligned}
 \mathcal{L} &= \frac{1}{2} D_\mu \Phi^\dagger D^\mu \Phi + (\partial_\mu - ig W_\mu^a T_L^a - g' B_\mu^3) \\
 &= (\partial_\mu h)^2 + (\partial_\mu \sqrt{f^2 - (h+v)^2})^2 \\
 &\approx (\partial_\mu h)^2 \left(1 + \frac{v^2}{f^2}\right)
 \end{aligned}$$

$$\begin{aligned}
 H &= \begin{pmatrix} h_u \\ h_d \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_2 + i\phi_1 \\ \phi_4 - i\phi_3 \end{pmatrix} \\
 &= \begin{pmatrix} 0 \\ \frac{1}{\sqrt{2}}(v+h) \end{pmatrix} \\
 \Phi &= \begin{pmatrix} 0 \\ 0 \\ 0 \\ \frac{v+h}{\sqrt{f^2 - (h+v)^2}} \end{pmatrix}
 \end{aligned}$$

$$\approx (\partial_\mu h)^2 \left(1 + \frac{v^2}{f^2}\right)$$

$$\Phi = \begin{pmatrix} 0 \\ 0 \\ v+h \\ \sqrt{f^2 - (h+v)^2} \end{pmatrix}$$

redefine $h \rightarrow h \sqrt{1 - \frac{v^2}{f^2}}$ for canonical kinetic term

$$(\partial_\mu \Phi)^2 \Rightarrow \mathcal{L} \supset \frac{g^2 v^2}{4} \left(|W|^2 + \frac{1}{2} |Z|^2 \right) 2 \sqrt{1 - \frac{v^2}{f^2}} \frac{h}{v}$$

$$\phi = \begin{pmatrix} \pi_1 \\ \pi_2 \\ \pi_3 \\ \phi \end{pmatrix}$$

$$V = \frac{M^2}{2} \phi^2 + \frac{\lambda}{4} \phi^4 \quad (5014)$$

$$\approx (\partial_\mu h) \left(1 + \frac{v^2}{f^2}\right)$$

$$\left(\frac{v+h}{\sqrt{f^2 - (h+v)^2}}\right)$$

redefine $h \rightarrow h \sqrt{1 - \frac{v^2}{f^2}}$ for canonical kinetic term

$$(D_\mu \Phi)^2 \Rightarrow \mathcal{L} \supset \frac{g^2 v^2}{4} \left(|W|^2 + \frac{1}{c_W^2} Z^2 \right) 2 \sqrt{1 - \frac{v^2}{f^2}} \frac{h}{v}$$

Generic consequence: suppression of hVV couplings $\sim \sqrt{1 - \frac{v^2}{f^2}}$

$$V = \frac{M^2}{2} \phi^2 + \frac{\lambda}{4} \phi^4 \quad SO(4)$$



fermion masses: SM fermions

$$\mathcal{L} \supset -y_L \bar{\Psi}_L \chi_R + \text{h.c.} + \tilde{m}_* \bar{\chi}_L \chi_R$$

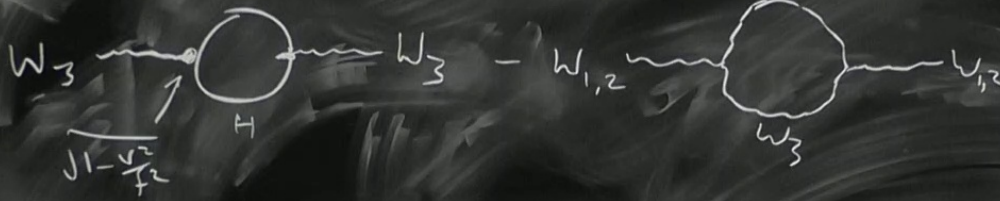
composite field
from new strong sector

$$y_* \bar{\chi} H \chi \rightarrow \underbrace{(y_* \sin\theta_L \sin\theta_R)}_{y_{SM}} \bar{\Psi}_L H \Psi_R$$

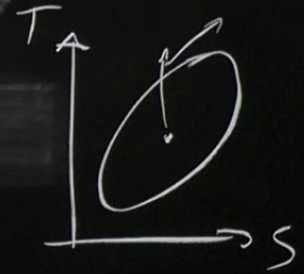
EWPT at LEP: $\rho = \frac{M_W^2}{M_Z^2 \cos^2 \theta_W} \approx 1$
 Quigg's textbook

$\frac{c_0}{\Lambda^2} |H^\dagger D_\mu H|^2 \sim T$ parameter

$T = \rho - 1$



S parameter



CAUTION
 Do not touch the detector when it is on. Do not touch the detector when it is on.

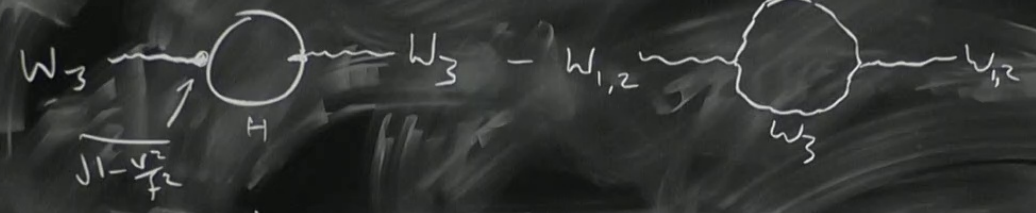
CAUTION

Quigg, textbook

$$M_Z^2 \cos^2 \theta_W$$

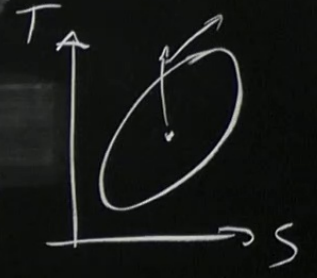
$$\frac{c_6}{\Lambda^2} |H^\dagger D_\mu H|^2 \sim T \text{ parameter}$$

$$T = \rho - 1$$



S parameter

$$T = \frac{g'^2}{16\pi^2} \log\left(\frac{\Lambda}{M_H}\right) - \frac{g'^2}{16\pi^2} \log\left(\frac{\Lambda}{M_Z}\right) = -\frac{g'^2}{16\pi^2} \log\left(\frac{M_H}{M_Z}\right) \text{ in SM}$$



CAUTION
DO NOT TOUCH THE BOARD SURFACE
OR THE BOARD OR THE BOARD SURFACE
IF AN EMERGENCY OCCURS
CALL THE FACULTY OFFICE

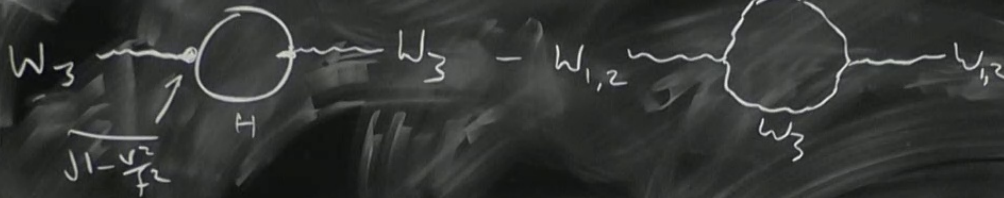
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Quigg, textbook

$$M_Z^2 \cos^2 \theta_W$$

$$\frac{c_6}{\Lambda^2} |H^\dagger D_\mu H|^2 \sim T \text{ parameter}$$

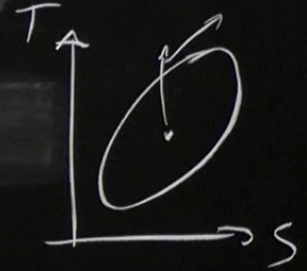
$$T = \rho - 1$$



S parameter

$$T = \frac{g'^2}{16\pi^2} \log\left(\frac{\Lambda}{M_H}\right) - \frac{g'^2}{16\pi^2} \log\left(\frac{\Lambda}{M_Z}\right) = -\frac{g'^2}{16\pi^2} \log\left(\frac{M_H}{M_Z}\right) \text{ in SM}$$

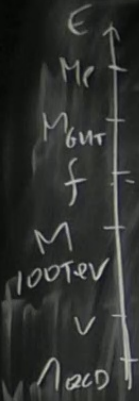
$$\text{in CHM} \Rightarrow \log\left(\frac{M_H^{\text{eff}}}{M_Z}\right) \quad M_H^{\text{eff}} = M_H \left(\frac{\Lambda}{M_H}\right)^{\frac{\sqrt{2}}{5}}$$



CAUTION
DO NOT OPEN THE DOOR UNTIL THE LIGHTS ARE OFF
IF A WARNING LIGHT GOES ON, STOP WORK IMMEDIATELY
PLEASE REPORT ANY

Axion

QCD axion obtains potential from QCD confinement

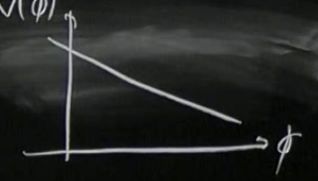


$U(1)_{PQ}$

$$V(\phi) = -\Lambda_{QCD}^4 \cos\left(\frac{\phi}{f}\right)$$

$$\mathcal{L} \supset \frac{1}{2} \partial_\mu \phi \partial^\mu \phi + \frac{1}{4} \tilde{G}_{\mu\nu} \tilde{G}^{\mu\nu} \quad S = \int d^4x \mathcal{L}$$

g parameter
 ext. gt
 breaking shift symmetry

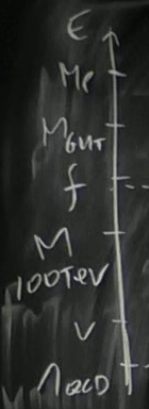


Relation

$$\mathcal{L} \equiv \underbrace{(-M^2 + g\phi)}_{\text{effective Higgs mass}} |H|^2 + gM^2 \phi + g^2 \phi^2 + \dots +$$

CAUTION

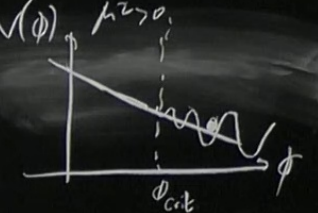
QCD axion obtains potential from QCD



$U(1)_{PQ}$

$$V(\phi) = -\frac{\Lambda_{QCD}^4}{f} \cos\left(\frac{\phi}{f}\right)$$

$$\mathcal{L} = \frac{1}{2} \partial_\mu \phi \partial^\mu \phi + \frac{1}{4} G_{\mu\nu}^a G^{\mu\nu a} \quad S = \int d^4x \mathcal{L}$$



Relaxion

g parameter explicit breaking of shift symmetry

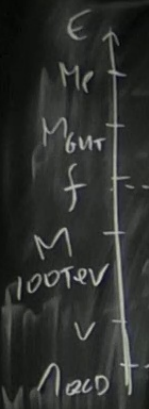
$$\mathcal{L} = \frac{1}{2} (\underbrace{-M^2 + g\phi}_{\text{effective Higgs mass } \mu^2}) |H|^2 + gM^2 \phi + g^2 \phi^2 + \dots - \frac{\Lambda_{QCD}^4}{f} \cos\left(\frac{\phi}{f}\right)$$

$\mu^2 < m_\pi^2 \ll v^2$

$$V = \begin{cases} 0 & \mu^2 > 0 \\ \mu^2 \phi & \mu^2 < 0 \end{cases} \quad V \ll M$$

CAUTION
DO NOT TOUCH THE BOARD SURFACE
IF NECESSARY TO CLEAN THE BOARD SURFACE
PLEASE CONTACT THE STAFF OF THE BOARD

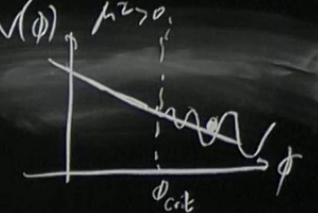
QCD axion obtains potential from QCD color anomaly



Λ_{QCD}

$$V(\phi) = -\frac{\Lambda_{QCD}^4}{f} \cos\left(\frac{\phi}{f}\right)$$

$$\mathcal{L} = \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{4} G_{\mu\nu}^a G^{a\mu\nu} \quad S = \int d^4x \mathcal{L}$$



Relaxion

g parameter
explicit
breaking of shift symmetry

$$\mathcal{L} = \underbrace{(-M^2 + g\phi)}_{\text{effective Higgs mass } \mu^2} |H|^2 + gM^2 \phi + g^2 \phi^2 + \dots - \frac{\Lambda_{QCD}^4}{f} \cos\left(\frac{\phi}{f}\right)$$

$\mu^2 > 0$
 $\mu^2 < 0$

effective Higgs mass μ^2

$$V = \begin{cases} 0 & \mu^2 > 0 \\ \mu^2 \phi & \mu^2 < 0 \end{cases}$$

$$\frac{\Lambda_{QCD}^4}{f} \ll M^2$$

$$gM^2 \sim \frac{\Lambda_{QCD}^4(v)}{f}$$

CAUTION
DO NOT TOUCH THE BOARD SURFACE
IT IS PROHIBITED TO APPLY
HEAVY OBJECTS TO THE BOARD