

Title: BSM Theory

Speakers: Tiann-Tevong You

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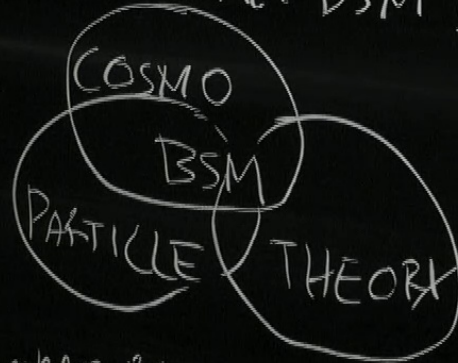
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BSM

• ULTIMATE GOAL: BSM?



• LITERATURE:

• McCullough: inspirehop/literature/1684708

• Walzer: 1901.01017

• Murayama: 0002232

OUTLINE

1. SM is an EFT
 2. NATURALNESS
 3. SUPERSYMMETRY
 4. COMPOSITE HIGGS / EXTRA-DIMENSIONS
 5. AXION \rightarrow RELAXION
-

1. SM is an EFT

• OLD UNDERSTANDING OF QFT:

• Misconception: renormalisability is key for sensible theories

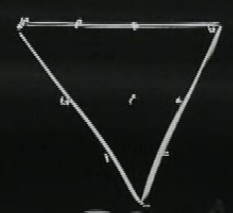
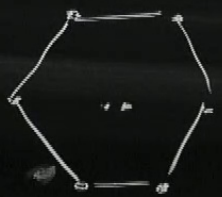
• 't-Hooft's proof of renormalisability of SM: start of acceptance

1. SM is an EFT

- OLD UNDERSTANDING OF QFT:
 - Misconception: renormalisability is key for sensible theories
 - 't-Hooft's proof of renormalisability of SM: start of acceptance
- MODERN UNDERSTANDING (Wilson, Weinberg, ...)
 - QFTs are EFTs
 - Once particle contents and quantum numbers are fixed write down all possible terms allowed by symmetries including higher-dimensional terms

- Gell-Mann's 'totalitarian' principle ← QM
 Anything that is not forbidden is compulsory

- 8-fold way



1964

$\Omega?$

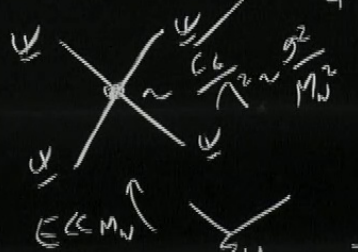
- QFTs are not fundamental but low-energy approximations to underlying ^{UV} theory

- QED EFT:

$$\mathcal{L}_{\text{QED}}^{\text{EFT}} = \bar{\Psi} i \gamma D_{\mu} \Psi - m \bar{\Psi} \Psi - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{C_6}{\Lambda^2} (\bar{\Psi} \Gamma \Psi)^2 + \dots$$

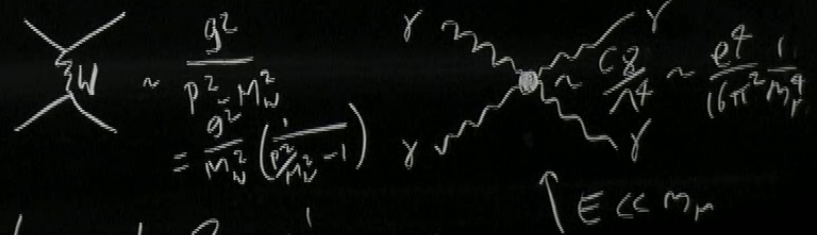
Wilson coefficients $\Gamma = \{1, \gamma^{\mu}, \gamma_5, \gamma^{\mu} \gamma_5, \sigma_{\mu\nu}\}$

Λ EFT cutoff \rightarrow GeV



$$+ \frac{C_8}{\Lambda^4} (F_{\mu\nu} F^{\mu\nu})^2 + \dots$$

Euler-Heisenberg 1933

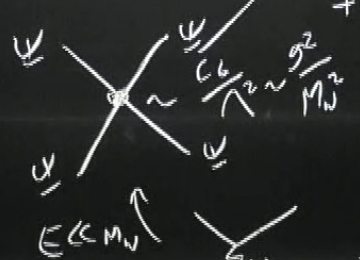


• SM as an EFT
 $SU(3)_c \quad SU(2)_L \quad U(1)_Y$

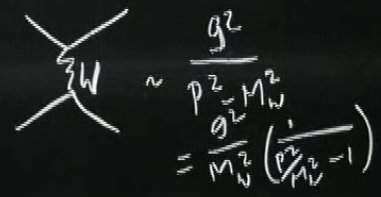
$$\mathcal{L}_{\text{QED}}^{\text{EFT}} = \bar{\Psi} i \not{D} \Psi - m \bar{\Psi} \Psi - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{c_6}{\Lambda^2} (\bar{\Psi} \Gamma \Psi)^2 + \frac{c_8}{\Lambda^4} (F_{\mu\nu} F^{\mu\nu})^2 + \dots$$

← Wilson coefficients
 $\Gamma = \{1, \gamma^\mu, \gamma_5, \gamma^\mu \gamma_5, \sigma_{\mu\nu}\}$

Λ EFT cutoff \rightarrow GeV



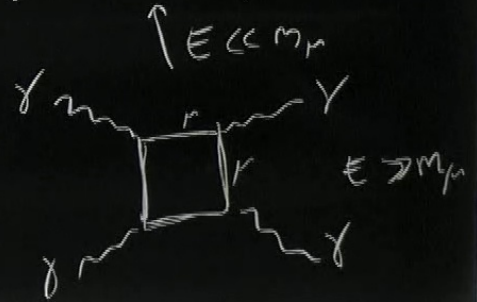
Euler-Herzenberg 1933



• SM as an EFT

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
Q_L	3	2	$1/6$
u_R	3	1	$2/3$
d_R	3	1	$-1/3$

L_L	1	2	$-1/2$
e_R	1	1	-1
H	1	2	$1/2$



- $d < 4$: 'relevant'
- $d = 4$: marginal
- $d > 4$: 'irrelevant'

$\theta < 10^{-9}$
 \ominus strong CP problem

$$\begin{aligned}
 \mathcal{L}_{SM}^{EFT} = & \bar{Q}_L i \gamma^\mu D_\mu Q_L + \bar{q}_R i \gamma^\mu D_\mu q_R + \bar{L}_L i \gamma^\mu D_\mu L_L + \bar{l}_R i \gamma^\mu D_\mu l_R \quad \checkmark \\
 & - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} W_{\mu\nu}^a W^{\mu\nu a} - \frac{1}{4} G_{\mu\nu}^i G^{\mu\nu i} + \frac{\theta}{16\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu} \\
 & (D_\mu H)^\dagger (D^\mu H) - V(H) + y_d \bar{Q}_L H u_R + y_u \bar{Q}_L H^c u_R + y_l \bar{L}_L H l_R + h.c. \\
 & + \mathcal{L}_5 + \mathcal{L}_6 + \mathcal{L}_7 + \dots
 \end{aligned}$$

Walter: 1901.01017

Murayama: 0002232

dim-5 = $\frac{c_5}{\Lambda} (L_L H^c)(L_L H) \sim \frac{c_5 v^c}{\Lambda} \nu \nu$

(see-saw) $\longrightarrow c_5 \sim O(1) \Rightarrow \Lambda \sim 10^{14} \text{ GeV}$

Violation of lepton number: "accidental" symmetries

B-violation at dim-6: $\frac{c_B}{\Lambda^2} q q q l$ $c_B \sim O(1)$

$\Lambda \gtrsim 10^{15} \text{ GeV}$

59 dim-6 CP-even operators

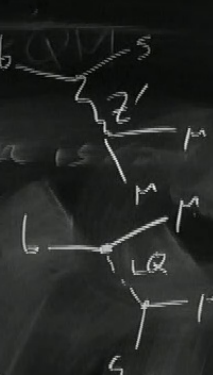
$\frac{c_R}{\Lambda^2} H^\dagger \overleftrightarrow{D}_\mu H \bar{l}_R \gamma^\mu l_R \rightarrow \bar{l}_R \gamma^\mu l_R$ $\Lambda \gtrsim 10^3 - 10^5 \text{ GeV}$

$\frac{c_G}{\Lambda} g_3 H^2 G_{\mu\nu} G^{\mu\nu} \rightarrow h G_{\mu\nu} G^{\mu\nu}$ $\Lambda \gtrsim 10^7 \text{ GeV}$
 $c_G \sim \frac{1}{16\pi^2}$

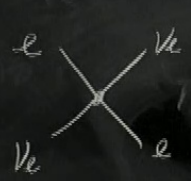
$\frac{c_g}{\Lambda^2} \bar{q} q \bar{l} l$



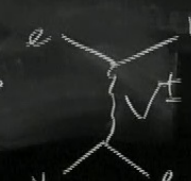
Nothing that is not μ -hidden is $\Rightarrow \Lambda \gtrsim 10^3 - 10^5 \text{ GeV}$



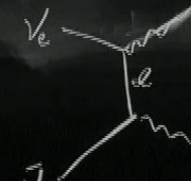
• BFM (Beyond Ferm. theory)



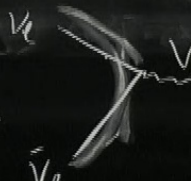
$A \sim E^2$



$A \sim \text{finite}$



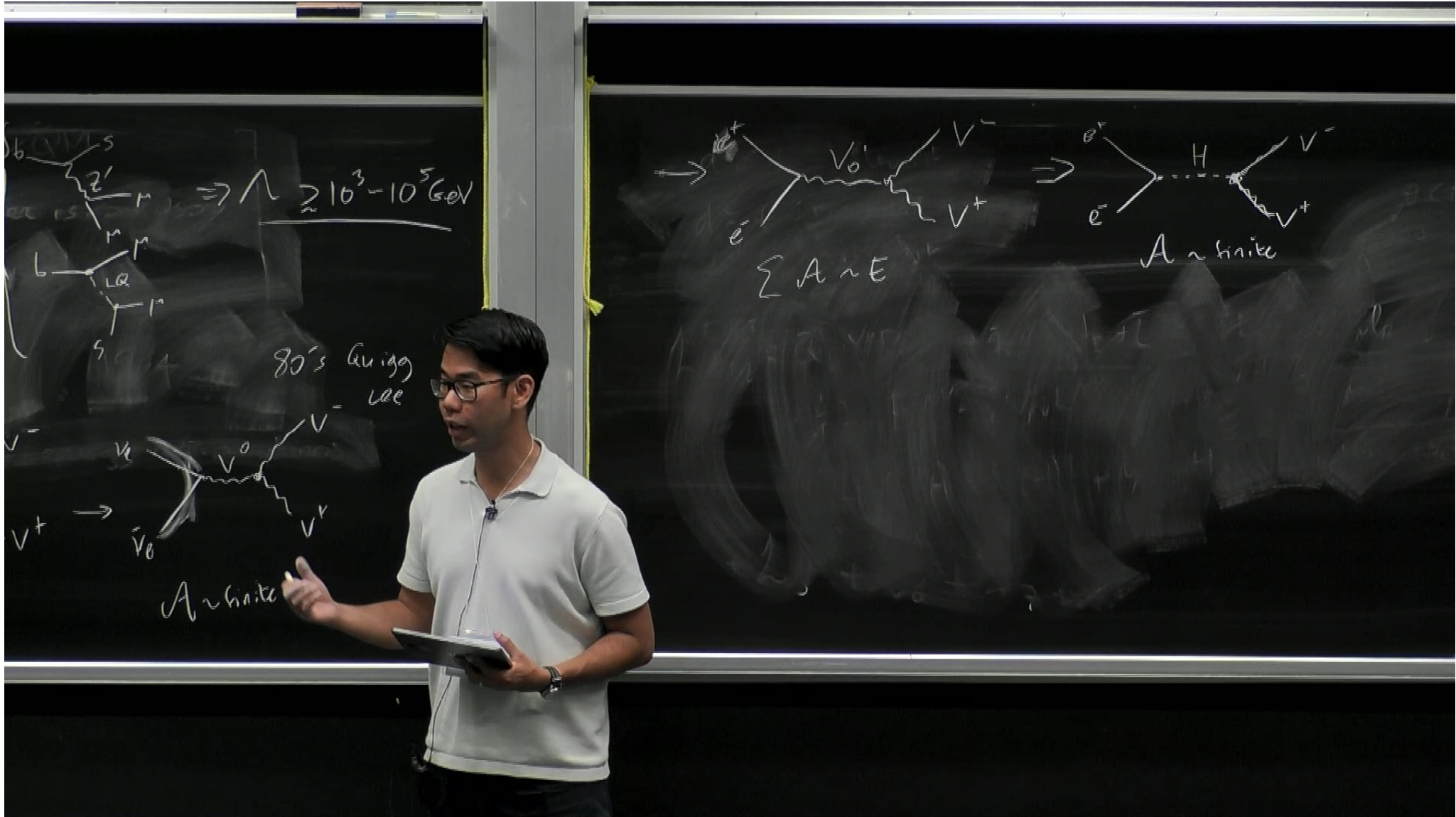
$A \sim E^2$



$A \sim \text{finite}$

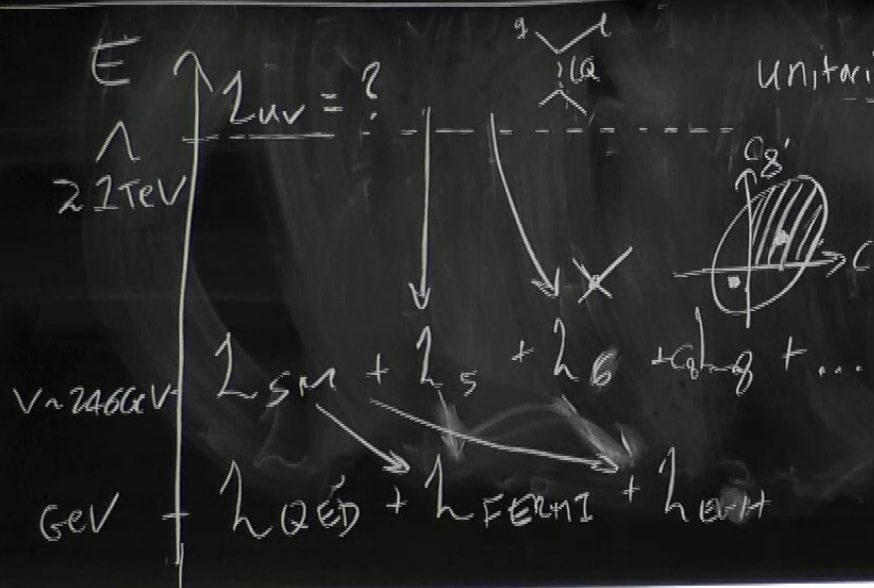
10^5 GeV
 6 GeV
 GeV

CAUTION



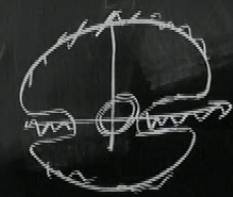
$$\sum A \sim E$$

$A \sim \text{finite}$



Unitarity, causality, locality

$$A(s, t=0) = \sum_n c_n s^{2n} \quad c_n = \frac{1}{2\pi i} \oint ds \frac{A}{s^3}$$



$$\begin{aligned} & \downarrow \frac{s^2}{\Lambda^4} \\ & = \int_{UV} + \int_{\text{branch cuts}} \\ & = A(s+i\epsilon) - \frac{A(s-i\epsilon)}{A^*(s+i\epsilon)} \\ & = 2\text{Im}A = G > 0 \end{aligned}$$