

Title: Standard Model

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Lecture 3: Electroweak Theory & Tests

gauge theory

$$SU(2)_L \times U(1)_Y$$

$$W^1, W^2, W^3$$

$$B$$

hypercharge

Higgs field

$$H \rightarrow \text{doublet } (2)$$

$$Y = \frac{1}{2}$$

$$H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$$

↳ gets a VEV

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↳ gets a VEV

$$\langle H \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$$

SU(2) gauge theory

$$[T_R^a, T_R^b] = i \epsilon^{abc} T_R^c$$

reps: doublet
(fundamental) $T_F^a = \frac{1}{2} \sigma^a$ ← Pauli spin matrix

adjoint $(T_A^a)^{bc} = -i \epsilon^{abc}$

$$D_\mu = \partial_\mu - ig A_\mu^a T_R^a$$

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g \epsilon^{abc} A_\mu^b A_\nu^c$$

Gauge sector

$$D_\mu H = \partial_\mu H - ig_Y \left(\frac{1}{2}\right) B_\mu H - ig_W W_\mu^a T_F^a H$$

$$\mathcal{L}_H = |D_\mu H|^2 - V(H)$$

↑
hypercharge $\frac{1}{2}$

Replace $H \rightarrow \langle H \rangle$, pick out the mass terms. gauge field

$$D_\mu H \rightarrow -ig_Y \begin{pmatrix} B_\mu & 0 \\ 0 & B_\mu \end{pmatrix} \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix} - ig_W \begin{pmatrix} \frac{1}{2}W_\mu^3 & \frac{1}{2}(W_\mu^1 - iW_\mu^2) \\ \frac{1}{2}(W_\mu^1 + iW_\mu^2) & -\frac{1}{2}W_\mu^3 \end{pmatrix} \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}$$

$$= -i \begin{pmatrix} \frac{1}{2} g_Y B_\mu + \frac{1}{2} g_W W_\mu^3 & \frac{g_W}{2} (W_\mu^1 - iW_\mu^2) \\ \underbrace{\frac{g_W}{2} (W_\mu^1 + iW_\mu^2)}_{\text{multiplied by } 0} & \underbrace{\frac{1}{2} g_Y B_\mu - \frac{1}{2} g_W W_\mu^3}_{\text{multiplied by } \frac{V}{\sqrt{2}}} \end{pmatrix} \begin{pmatrix} 0 \\ \frac{V}{\sqrt{2}} \end{pmatrix}$$

3 linear combinations get mass.

$$W_\mu^\pm = \frac{1}{\sqrt{2}} (W_\mu^1 \mp iW_\mu^2)$$

$$M_W = \frac{g_W V}{2}$$

$$= -i \begin{pmatrix} \frac{1}{2} g_Y B_\mu + \frac{1}{2} g_W W_\mu^3 \\ \frac{g_W}{2} (W_\mu^1 + iW_\mu^2) \\ \frac{g_W}{2} (W_\mu^1 - iW_\mu^2) \\ \frac{1}{2} g_Y B_\mu - \frac{1}{2} g_W W_\mu^3 \end{pmatrix} \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}$$

multiplied by 0
multiplied by $\frac{v}{\sqrt{2}}$

$g_W = 0.65$
 $g_Y = 0.3$

3 linear combinations get mass.

$$W_\mu^\pm = \frac{1}{\sqrt{2}} (W_\mu^1 \mp iW_\mu^2)$$

$$Z_\mu = \cos\theta_W W_\mu^3 - \sin\theta_W B_\mu$$

$$\tan\theta_W = \frac{g_Y}{g_W}$$

$$M_W = \frac{g_W v}{2}$$

$$M_Z = \frac{M_W}{\cos\theta_W}$$

Last linear combination is massless:

$$A_\mu = \cos\theta_w B_\mu + \sin\theta_w W_\mu^3$$

↳ photon!

$$SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$$

3 eaten Goldstone bosons $\rightarrow H^\pm$ eaten by W^\pm

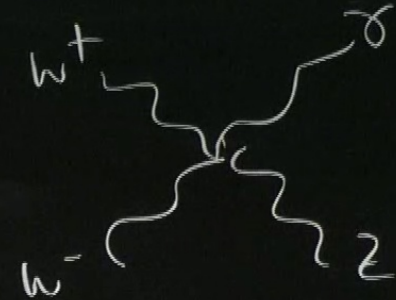
In unitary gauge, $H \rightarrow \begin{pmatrix} 0 \\ H^0 \\ \frac{1}{\sqrt{2}}(v+h) \end{pmatrix} = h + ia_0$, a_0 eaten by Z

CAUTION

Last linear combination is massless:

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In unitary gauge, $H \rightarrow \begin{pmatrix} 0 \\ \frac{1}{\sqrt{2}}(v+h) \end{pmatrix}$ $H^0 = h + ia_0$, a_0 eaten by Z

$$\text{Gauge boson prop: } \frac{-i \left(g_{\mu\nu} - \frac{k_\mu k_\nu}{M_W^2} \right)}{k^2 - M_W^2 + i\epsilon}$$

Matter content (1 gen)

• L , LH lepton doublet, $Y = -\frac{1}{2}$

$$L = \begin{pmatrix} \nu_L \\ e_L^- \end{pmatrix}$$

• e_R^- , RH lepton singlet under $SU(2)$, $Y = -1$

• Q , LH quark doublet, $Y = \frac{1}{6}$

$$Q = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$$

• u_R , RH up quark singlet, $Y = \frac{2}{3}$

• d_R , RH down quark singlet, $Y = -\frac{1}{3}$

Fermion masses (lepton)

Yukawa coupling for leptons

$$\mathcal{L}_{\text{mass}, e} = - y_e H^* e_R^+ L + \text{h.c.}$$

$Y: -\frac{1}{2} + |-\frac{1}{2}| = 0$

$SU(2): H^* = (H^- \bar{H}^0)$

unitary
gauge \rightarrow

$$= - \frac{y_e v}{\sqrt{2}} e_R^+ e_L + \text{h.c.}$$

$$m_e = \frac{y_e v}{\sqrt{2}}$$

v

$$H^* L = (H^- \bar{H}^0) \begin{pmatrix} \nu \\ e_L \end{pmatrix} = \frac{v}{\sqrt{2}} e_L$$

up quark: $\mathcal{L} = -y_u H U_R^+ Q + h.c.$

$$Y = \frac{1}{2} - \frac{2}{3} + \frac{1}{6} = 0$$

think of QM, spin $-\frac{1}{2}$: how do we get $S=0$ from $2 \times S=\frac{1}{2}$

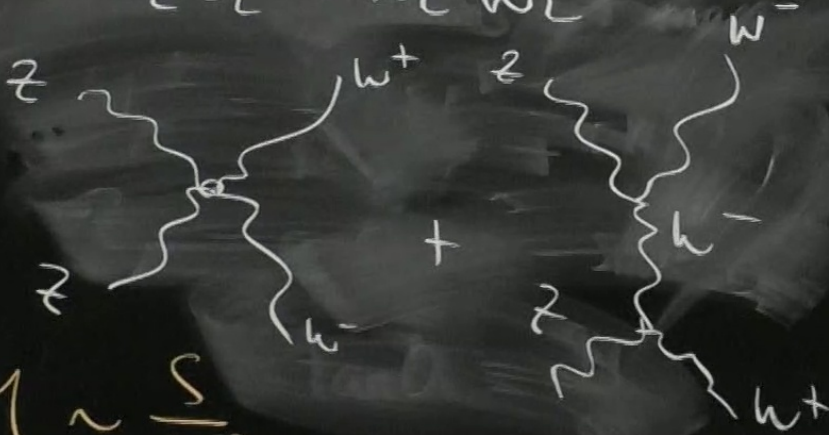
$$|H^+_{\downarrow}\rangle - |H^0_{\uparrow u}\rangle$$

$$|0\rangle = \frac{1}{\sqrt{2}}(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

High-Energy Limit

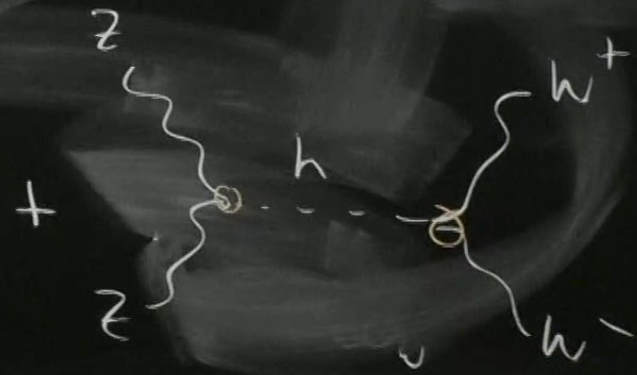
Vector boson scattering

$$Z_L Z_L \rightarrow W_L^+ W_L^-$$



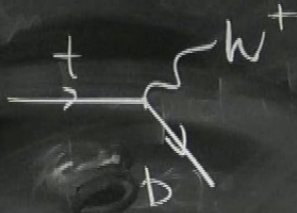
$$M \sim \frac{s}{m_W^2}$$

if no $m_h \leq 1 \text{ TeV}$,
violate perturbative
unitarity in $\sqrt{s} \gtrsim 1 \text{ TeV}$



$E \sim M_{pl}$

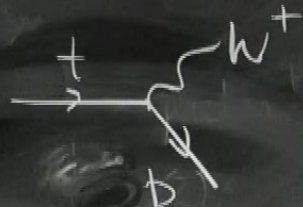
Example: top quark decay



$$iM = \frac{ig_w}{\sqrt{2}} \bar{u}_b \gamma^\mu P_L u_t \epsilon_\mu^*(W)$$

CAUTION
DO NOT TOUCH THE BOARD SURFACE
OR THE SURROUNDING AREA
IF YOU ARE NOT A MEMBER OF THE STAFF
OR A STUDENT OF THE UNIVERSITY OF TORONTO

Example: top quark decay



$$iM = i \frac{g_w}{\sqrt{2}} \bar{u}_b \gamma^\mu P_L u_t \epsilon_\mu^*(w)$$

$$\langle |M|^2 \rangle = \frac{g_w^2}{2} \text{Tr}[\dots] \left(-g_{\mu\nu} + \frac{P_{w\mu} P_{w\nu}}{m_w^2} \right)$$

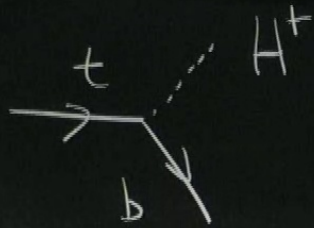
$$m_t = \frac{y_t v}{\sqrt{2}}, \quad m_w = \frac{g_w v}{2}$$

$$\Gamma_t = \frac{g_w^2 m_t^3}{64\pi m_w^2}$$

($m_t \gg m_w$)

$$= \frac{g_w^2 m_t}{64\pi} \left(\frac{2y_t^2}{g_w^2} \right) = \frac{y_t^2}{32\pi} m_t$$

CAUTION
 No work on ceiling and lighting should
 be done in the vicinity of the board.
 No work on the board should be done
 while the board is in use.



$$\Gamma_t = \frac{y_t^2 m_t}{32\pi}$$

At high energies, amplitudes involving $(E \gg m_\nu)$

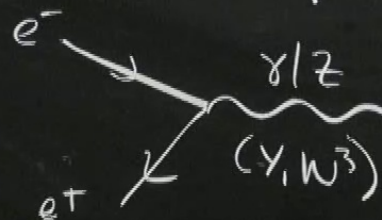
$$V_L \leftrightarrow \pi$$

Goldstone Boson Equivalence Theorem

$$M(X \rightarrow Y V_L) \cong M(X \rightarrow Y \pi) \text{ when } E_\nu \gg M_\nu$$

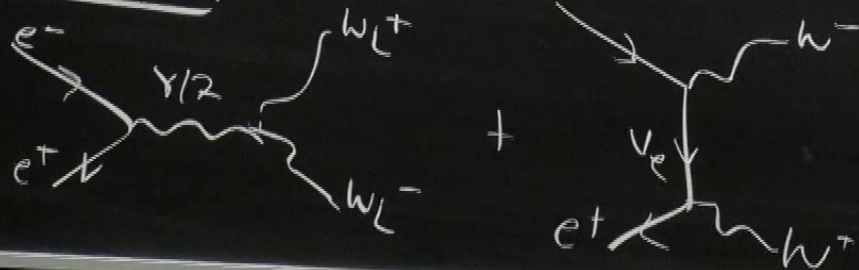
eg. $e^+e^- \rightarrow W_L^+ W_L^-$

GBET: $e^+e^- \rightarrow H^+ H^-$



$$y_e = \frac{m_e}{\sqrt{s}} \sqrt{2} \sim 10^{-6}$$

Gauge picture



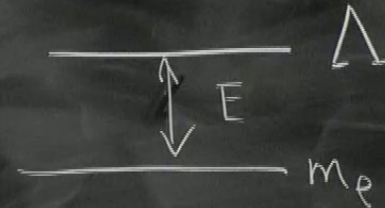
CAUTION
 Do not touch the surface of the blackboard
 unless instructed by the lecturer or your tutor
 Do not drink or eat on the blackboard
 Please respect the blackboard

'Another loophole theory with a cutoff Λ

vector mesons : ρ, ω, ϕ

$$m_\rho = 770 \text{ MeV}$$

• if vector mesons are "light"

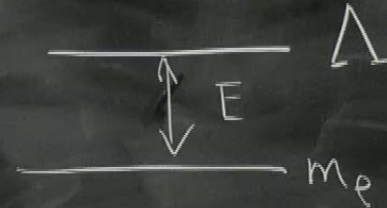


'Another loophole' theory with a cutoff Λ

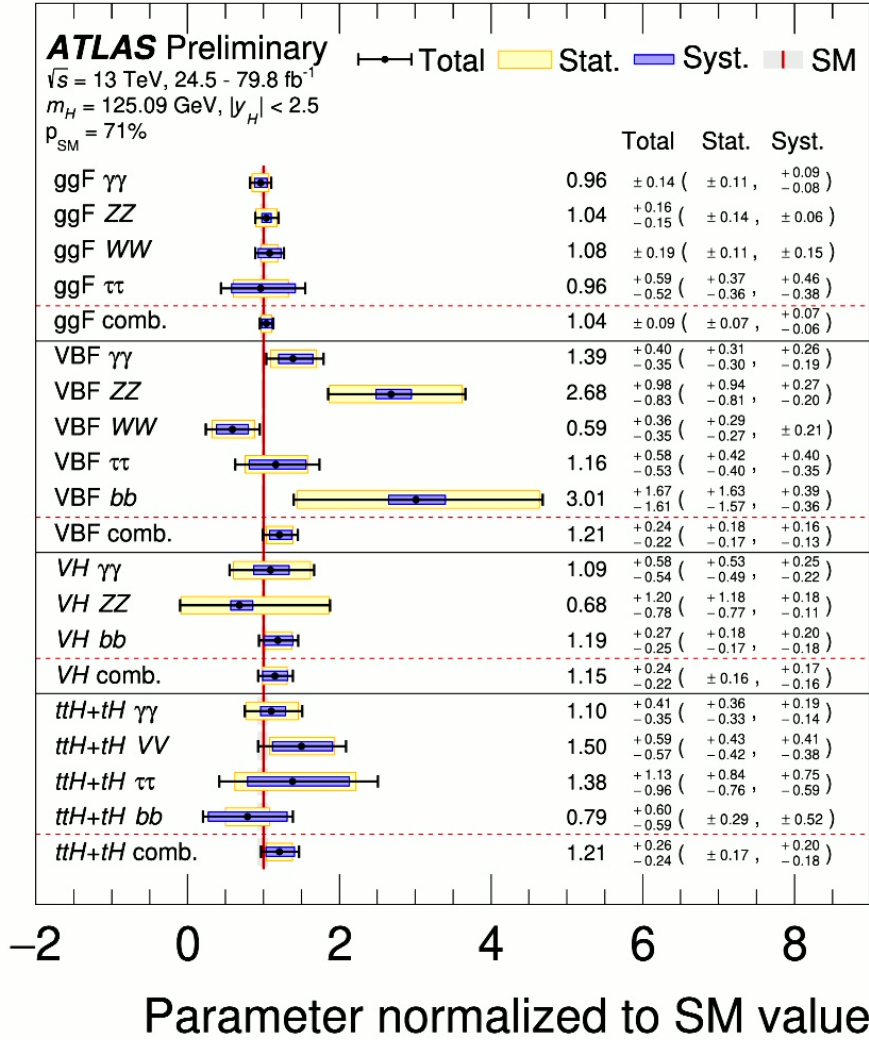
vector mesons : ρ, ω, ϕ

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- if vector mesons are "light"
- two interrelated ideas
 - \rightarrow vector meson dominance



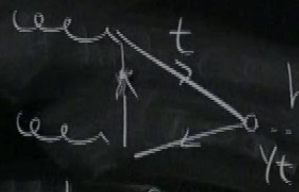
All results from ATLAS-CONF-2019-005



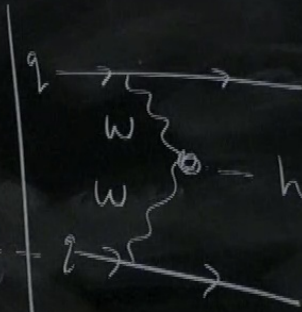
$$\frac{\sigma \times \text{BF}}{\sigma_{\text{SM}} \times \text{BF}_{\text{SM}}}$$

Higgs physics

production



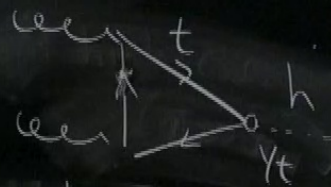
gluon fusion



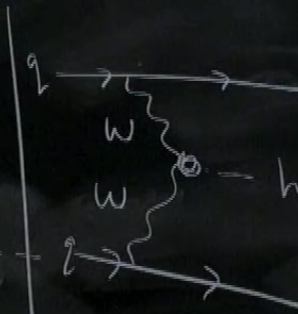
vector boson
fusion

Higgs physics

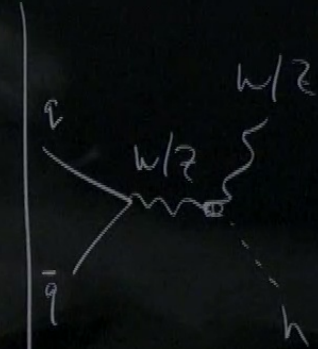
production



gluon fusion

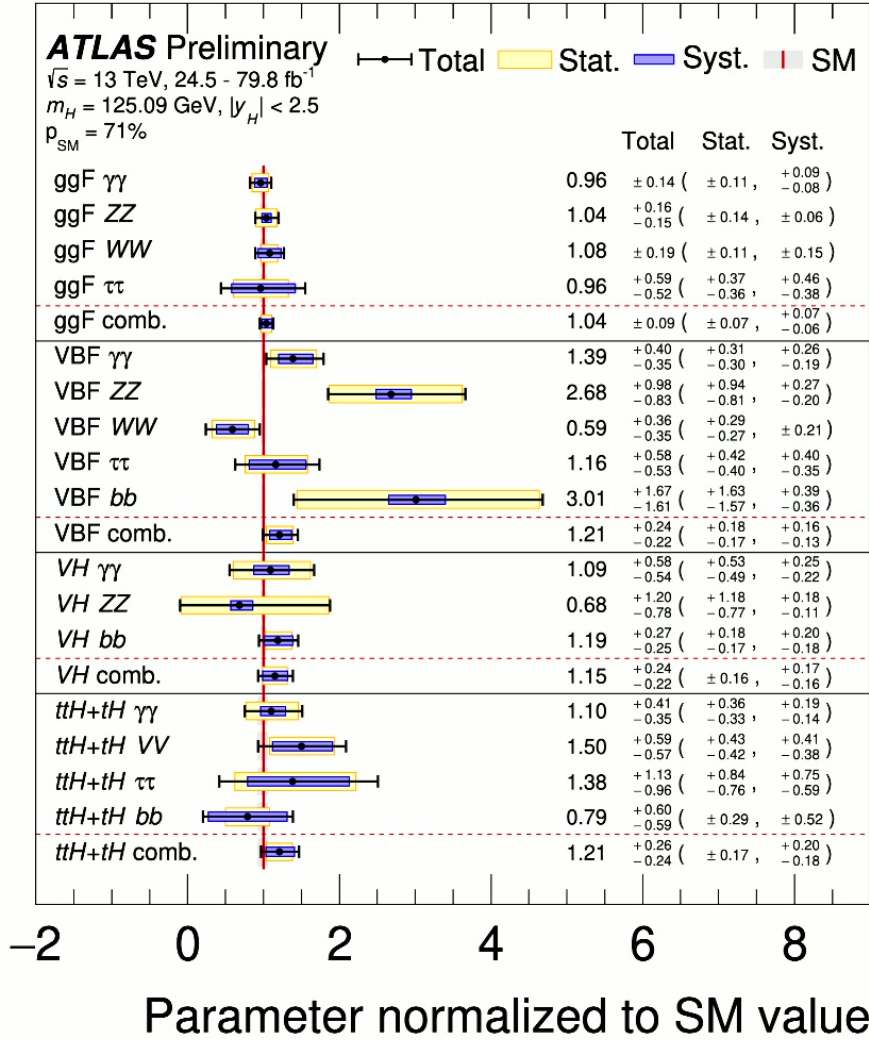


vector boson
fusion



Higgsstrahlung

All results from ATLAS-CONF-2019-005



$$\frac{\sigma \times \text{BF}}{\sigma_{\text{SM}} \times \text{BF}_{\text{SM}}}$$

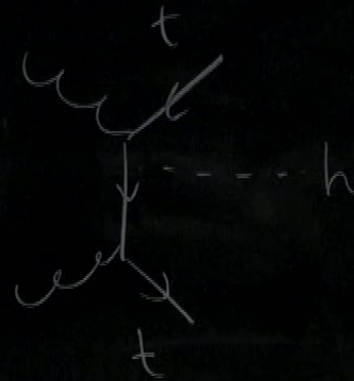
another loophole. theory with

vector mesons - ρ

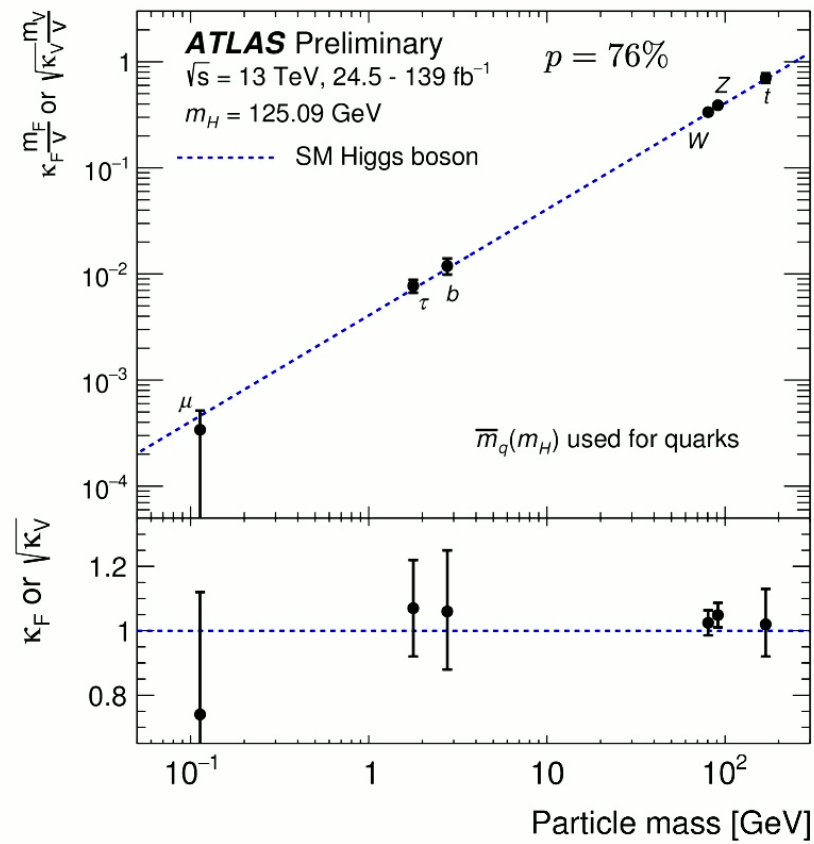
$$m_\rho = 770 \text{ MeV}$$

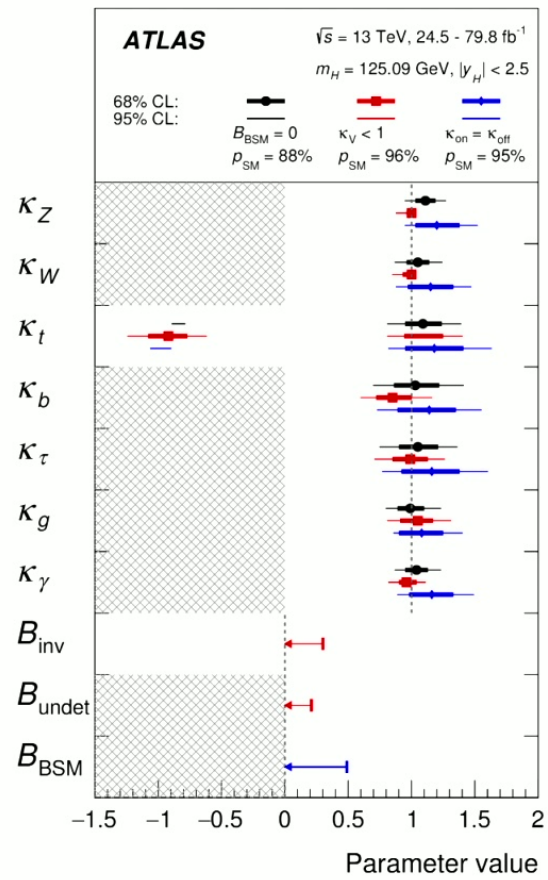
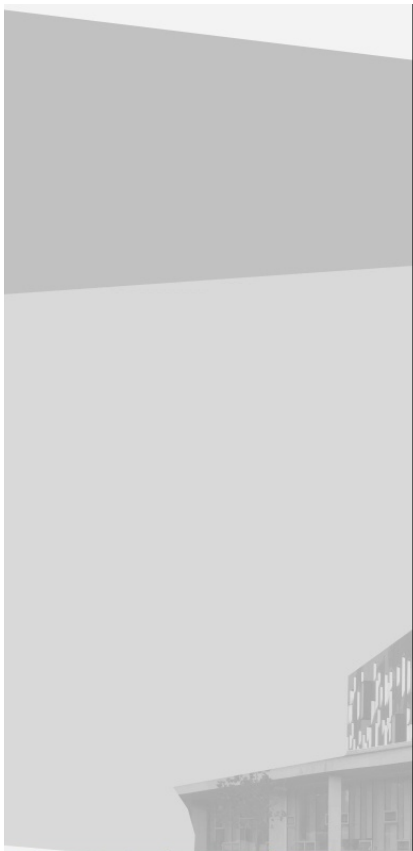
if vector mesons

- interrelated ideas
- vector meson dominance
- hidden local symmetry (p. a)

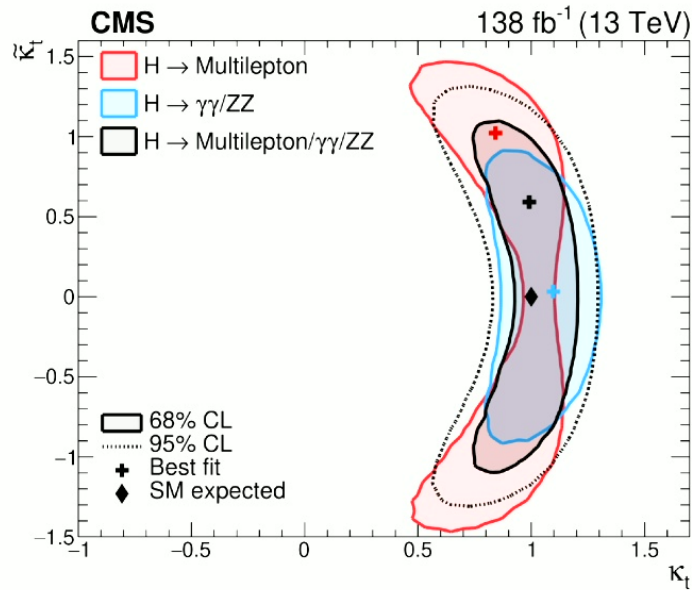


Higgs Coupling Measurements

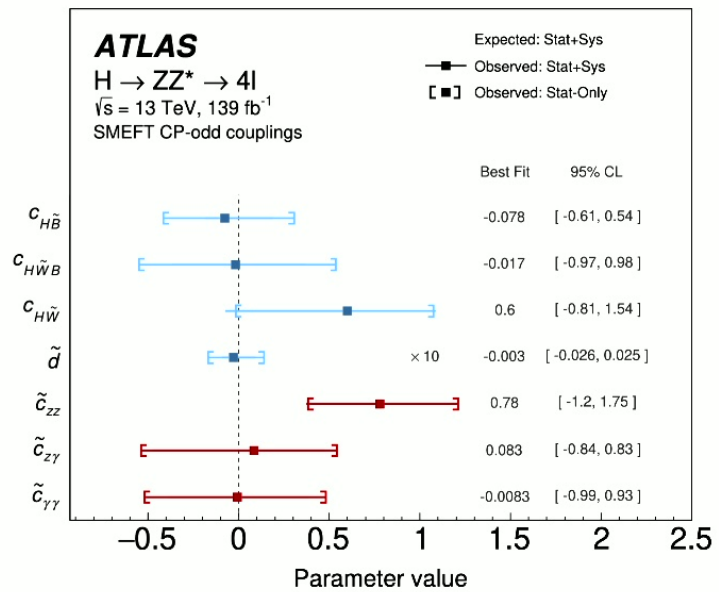




CP-violating couplings



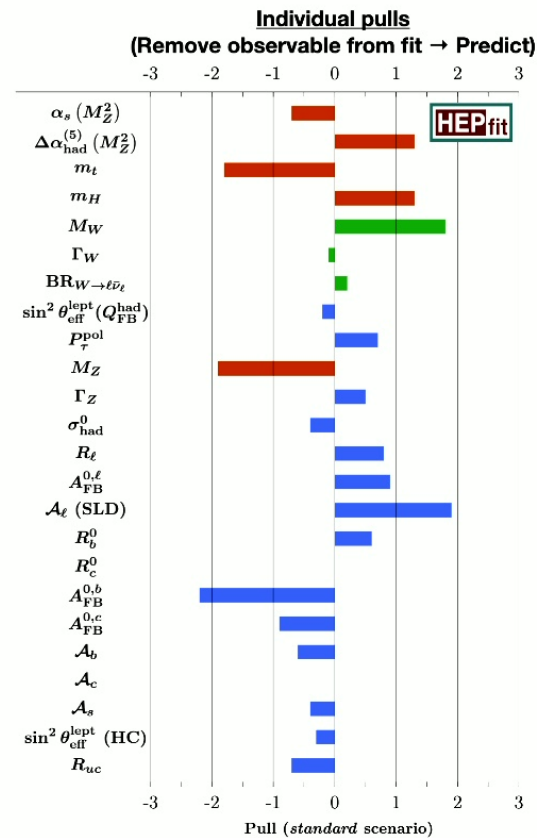
arXiv:2208.02686



arXiv:2304.09612

Electroweak Precision Fits

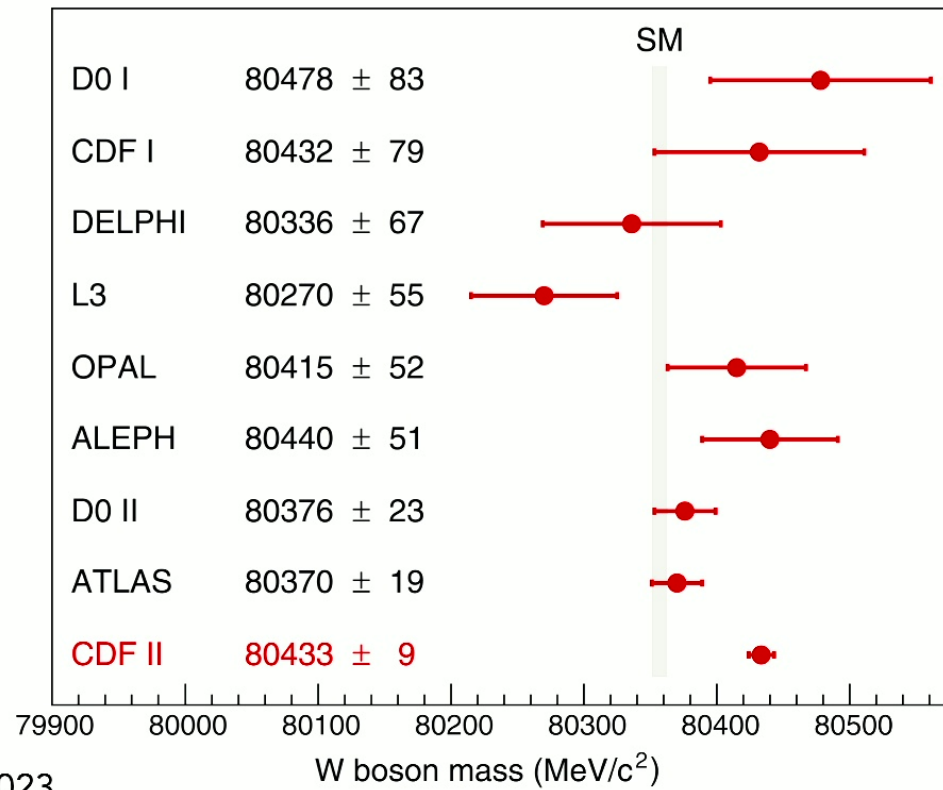
- SM is an over constrained system - perform many measurements and do a global fit!
- Fit from early 2022 data, p-value 0.45



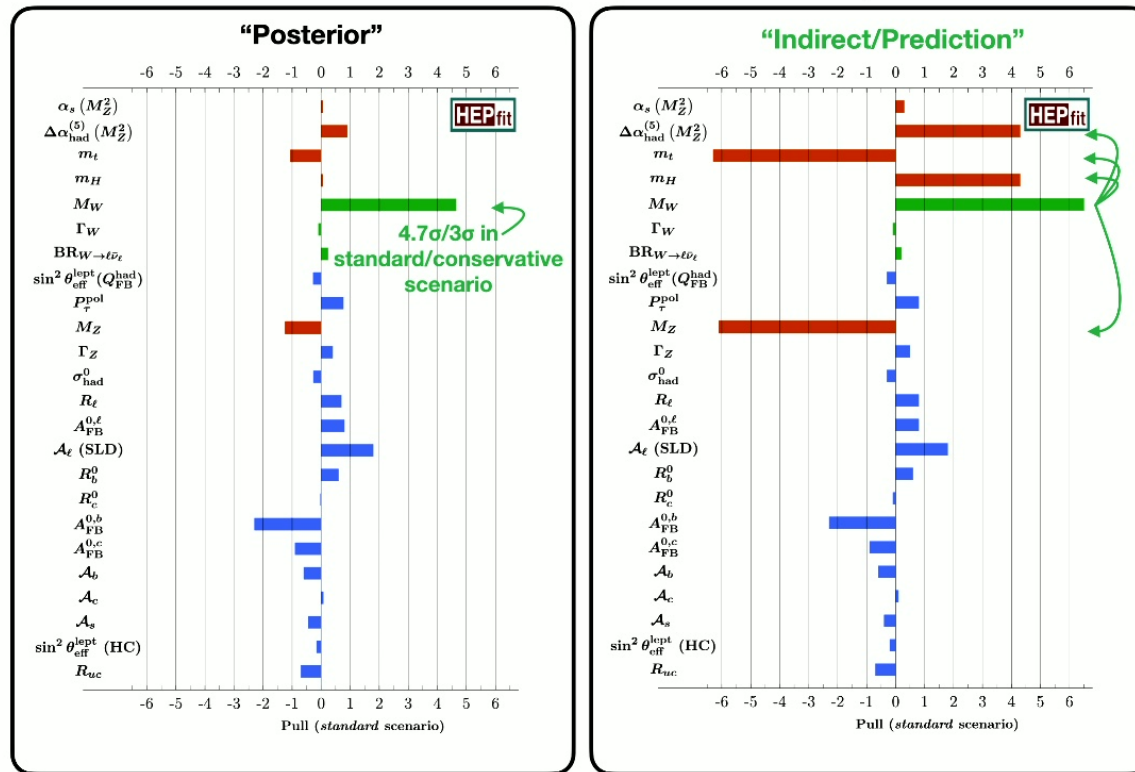
de Blas et al., arXiv:2204.04204

W Mass Anomaly

- Then, in April 2022:



Updated EW Fits



de Blas et al., arXiv:2204.04204