

Title: Building Quantum Simulators for QuFTs

Speakers: Jorg Schmiedmayer

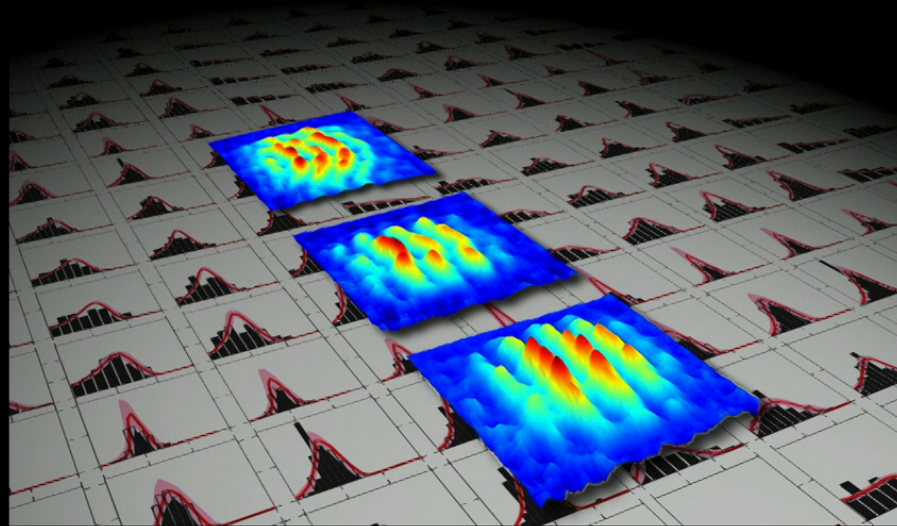
Collection: Quantum Simulators of Fundamental Physics

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Abstract: ZOOM: <https://pitp.zoom.us/j/95722860808?pwd=REYwSDdiK3pFamRJcjJwOW5FV1RPZz09>

# Quantum Simulators for QuFT



Jörg Schmiedmayer

Vienna Center for Quantum Science and Technology, TU-Wien





1982 **Richard Feynman:**

*other* quantum systems, assembled and manipulated under precisely controlled conditions following quantum laws, could simulate strongly correlated quantum systems.

*Simulating physics with computers,*  
R. Feynman, *Int. J. Theor. Phys.* 21, 467 (1982)

## Digital Quantum Simulators:

**Trotter-Suzuki's decomposition** of the many-body evolution operator into sequences of elementary quantum gates.

Example:

*Real-time dynamics of lattice gauge theories with a few-qubit quantum computer*  
E. A. Martinez et al. Nature 534, 516 (2016)

## Analog Quantum Simulators:

**Build** the desired Hamiltonian directly in the Lab and prepare the ground state, observe time evolution.

Example: Hubbard Model, ...

*Quantum simulation with ultracold atomic gases,*  
I. Bloch, et al. Nature Phys. 8, 267 (2012).

## Emergent Quantum Simulators

The **complexity** of the many body wave function **does not allow to 'observe'** all the details. Every **measurement** we do is a **'coarse graining'** which leads to an **emerging effective description** that is very different from the microscopic physics.

Example: relativistic quantum fields

Sine-Gordon model  $\leftrightarrow$  two tunnel coupled superfluids

emergent Hydrodynamics

....

Schweigler, et al. Nature 545, 323 (2017)

Zache et al. PRX 10, 011020 (2020)

Cataldini et al. arXiv:2111.13647

# Many Body Quantum Systems $\leftrightarrow$ QuFT description

Quantum Many Body systems are an ideal starting point to build QuFT's

- ✧ The complexity of the many body wave function does not allow to 'observe' all the details  
-> **We can only measure few body observables.**
- ✧ Measurement on a many body system is therefore a '**coarse graining**'.  
Within the RG framework this leads to an **effective description** of the system that can be very different from the microscopic physics.
- ✧ A natural way to describe quantum many body systems is then through these **emerging effective models** (field theories)

Question: how good are these emerging quantum simulators for QuFT  
When and how do they break down

A natural way to probe these models is through **correlation functions**.

Question: **which QuFT do we simulate?**  
**Can we extract the parameters for an effective field theory directly from experimental data?**

# Quantum Gas $\leftrightarrow$ QuFT

(Effective) Quantum Field Theories are a powerful tool to describe many body quantum systems.

Quantum Gases are ideal tools to quantum simulate QuFTs

$T=0$   $\leftrightarrow$  vacuum  
excitations  $\leftrightarrow$  particles  
energy density  $\leftrightarrow$  geometry

...

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Examples:

- 1d superfluid  $\leftrightarrow$  Luttinger liquid (relativistic QuFT)
- Tunnel coupled super fluid  $\leftrightarrow$  Sine-Gordon model
- ...

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Examples:

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- ...

Interesting questions:

- Microscopic Physics  $\leftrightarrow$  effective QuFT description
- Granularity of the MB system  $\leftrightarrow$  Planck scale?
- ...



## Sine Gordon Model

- Tunnel coupled 1d superfluids  $\leftrightarrow$  SG model
- Verifying Sine-Gordon model
- Extracting the 1PI vertices
- Some recent examples and old unpublished experiments
  - Area law of mutual information in a QuFT
  - Floquet engineering
  - Decay of self trapping

## Emerging Generalized Hydrodynamics (GHD)

- Generalized Hydrodynamics (GHD) for 1d systems
- Rapidities  $\leftrightarrow$  Luttinger Liquid Phonons
- Pauli blocking and the limit of integrability

## Outlook



# Sine-Gordon Model

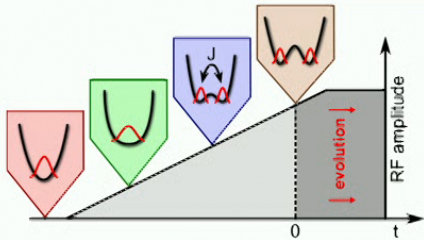
Emergent quantum simulator built from  
Two tunnel coupled  
1d super fluids

Exp: T. Schweiger, et al. (Vienna)  
Theory: S. Erne, V. Kasper, T. Zache et al. (HD)

Gritsev, Polkovnikov, Demler PRB 75, 174511 (2007)  
Schweigler et al. Nature 545, 323 (2017)  
Zache et al. PRX 10, 011020 (2020)

# Two tunnel coupled 1d super fluids

## Emergent quantum simulator for the Sine Gordon model



$$H = \sum_{j=1}^2 \int dz \left[ \frac{\hbar^2}{2m} \frac{\partial \psi_j^\dagger}{\partial z} \frac{\partial \psi_j}{\partial z} + \frac{g_{1D}}{2} \psi_j^\dagger \psi_j^\dagger \psi_j \psi_j + U(z) \psi_j^\dagger \psi_j - \mu \psi_j^\dagger \psi_j \right] - \hbar J \int dz \left[ \psi_1^\dagger \psi_2 + \psi_2 \psi_1^\dagger \right]$$

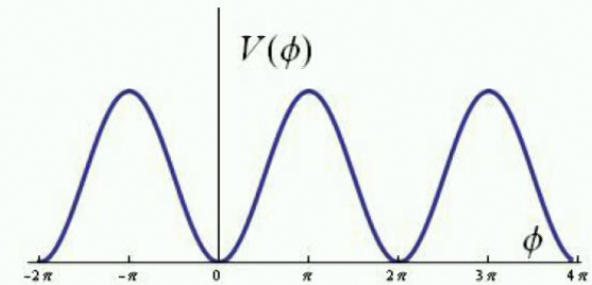
Following: Gritsev, Polkovnikov, Demler Phys. Rev. B 75, 174511 (2007)

- Density phase representation
- Expanding the Hamiltonian in density fluctuations  $\delta\rho_j$  and phase gradients  $\partial_z\phi_j$  up to second order and neglecting mixed terms separates  $H$  in symmetric and antisymmetric degrees of freedom
- Neglecting terms  $|\delta\rho/n_0| \ll 1$

One arrives at Quantum Sine-Gordon model:

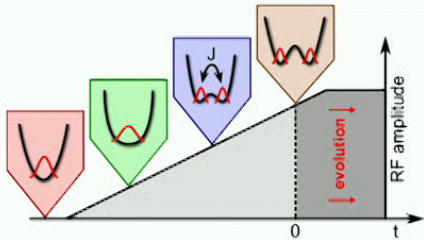
$$\hat{H}_{SG} = \int dz \left[ \frac{\hbar^2 n_{1D}}{4m} (\partial_z \hat{\phi})^2 + g \delta \hat{\rho}^2 \right] - \int dz 2J n_{1D} [1 - \cos \hat{\phi}]$$

"uncoupled harmonic oscillators"
anharmonic, non-gaussian, gapped,



# Two tunnel coupled 1d super fluids

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"uncoupled harmonic oscillators"

anharmonic, non-gaussian,  
gapped,

phase coherence length

$$\lambda_T = 2\hbar^2 n_{1D} / (mk_B T)$$

phase (spin) healing length

$$l_J = \sqrt{\hbar / (4mJ)}$$

Characteristic parameters

$$q = \lambda_T / l_J$$

# Quantum Sine Gordon Model

Theory of a massive scalar field  $\hat{\phi}$  in one space and time dimension with an interaction density proportional to  $\cos \beta \hat{\phi}$

$$H_{\text{SG}} = \frac{\hbar v_s}{2} \int dz \left[ (\partial_t \hat{\phi})^2 + (\partial_z \hat{\phi})^2 - \frac{2 M^2}{\beta^2} \cos \beta \hat{\phi} \right]$$

For the energy to be bounded  $\beta$  is limited to:  $0 < \beta < \sqrt{8\pi}$

$\beta$  plays the role of the Planck constant,  $\beta \ll 1$  being the (semi)-classical limit.

In our experiments:  $0.1 < \beta < 1$

# Sine Gordon Model

equivalent to (a few examples)

## Massive Thirring Model

S. Coleman *Phys. Rev. D* 217 11, 2088 (1975).

## Coulomb Gas

Polyakov, A. M. *Nuclear Physics B*, 120, 429-458 (1977).

Samuel, S. *Physical Review D*, 18, 1916 (1978).

## XY Model

José, J. V. et al., *Physical Review B*, 16, 1217 (1977).

## Half-integer spin chains and extended Hubbard models

Essler and Konik in: *From Fields to Strings*  
WORLD SCIENTIFIC, pp. 684-830 (2005)

## string breaking and entanglement in expanding Qu-fields

Berges et al., *Phys. Lett. B* 778, 442 (2018)

*Journal of High Energy Physics*, 2018(4), 145. (2018)



# Experiment

## Two tunnel coupled 1d super fluids

Exp: T. Schweiger, et al. (Vienna)  
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# AtomChip

Integrated Circuits for ultra-cold Quantum Matter

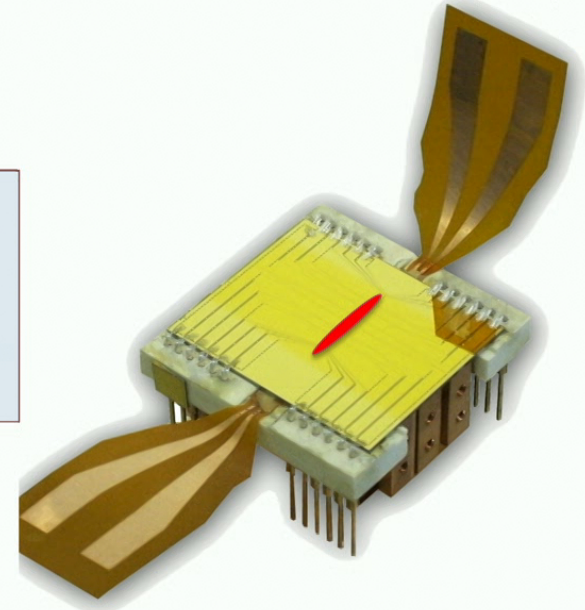
Combine the robustness of nano-fabrication on the quantum tools of atomic physics and quantum optics to build a toolbox for quantum experiments

Folman et al. PRL 84, 4749 (2000)

- 1d elongated traps
- Easy to create a BEC
- Very stable and reproducible laboratory for quantum experiments
- Fast operation
- Single atom detection with unit efficiency
- Well controlled splitting and interference
- experiment optimized by genetic algorithm

Rohringer et al. APL 93, 264101 (2008)

3000-10000 atoms  
 $T = 10-100$  nK  
 $\omega_R \sim 2\pi \times 2 - 3$  kHz  
 $\omega_L \sim 2\pi \times 5 - 10$  Hz  
 $k_B T \sim 0.1 - 0.7 \hbar \omega_R$   
 $k_B T \sim 0.1 - 1 \mu$





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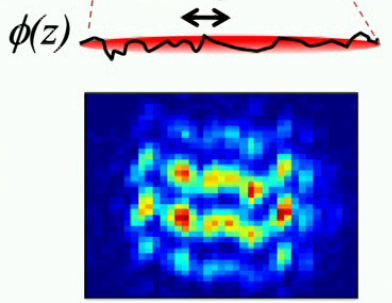
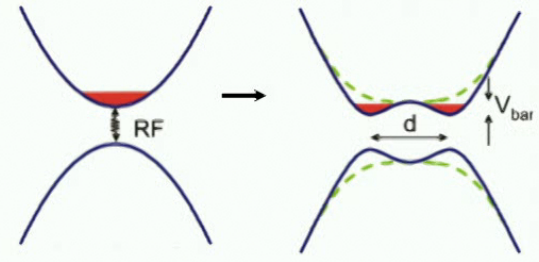
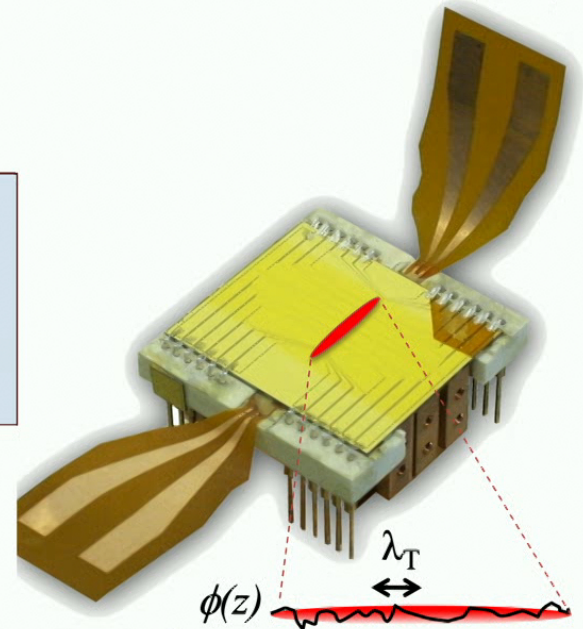
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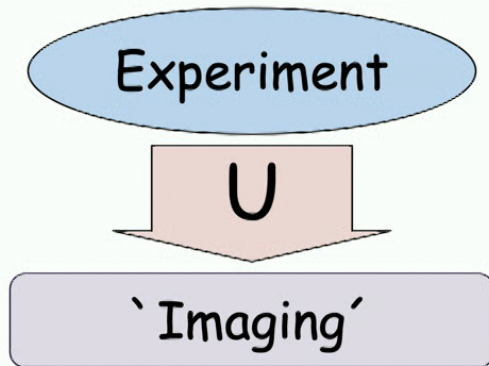
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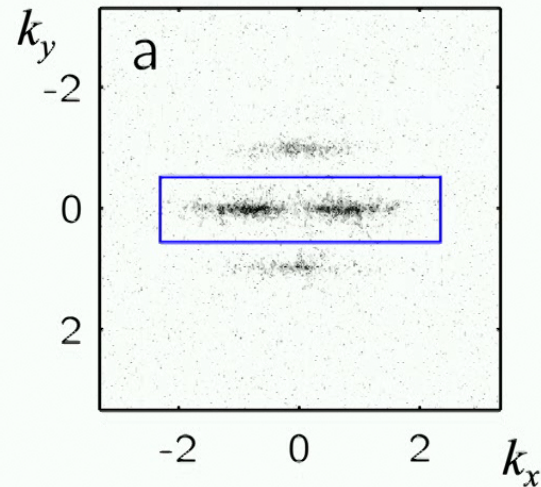
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# Experiment $\leftrightarrow$ read out

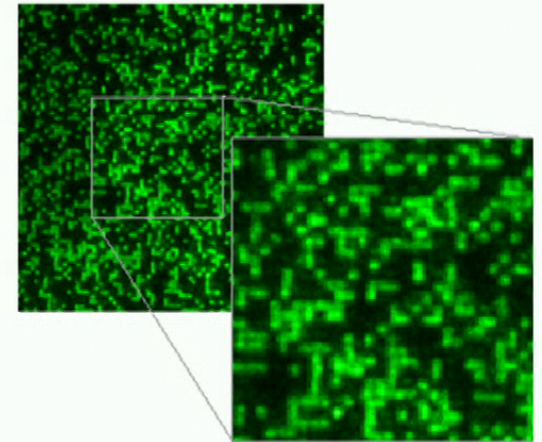


time of flight  $\rightarrow$  momentum



R. Bücker et al. NJP 11, 103039 (2009)  
 R. Bücker et al. Nature Physics 7, 608 (2011)

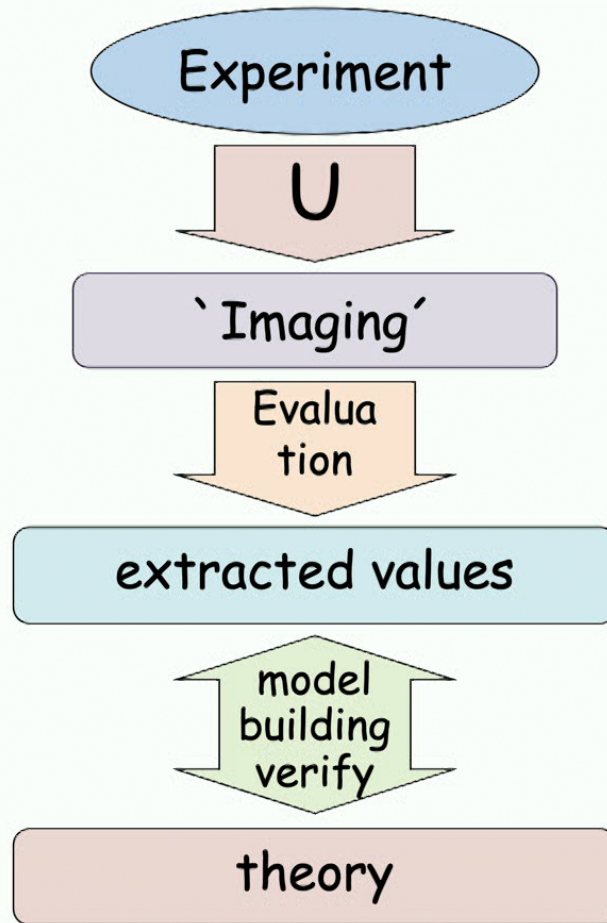
in situ  $\rightarrow$  position



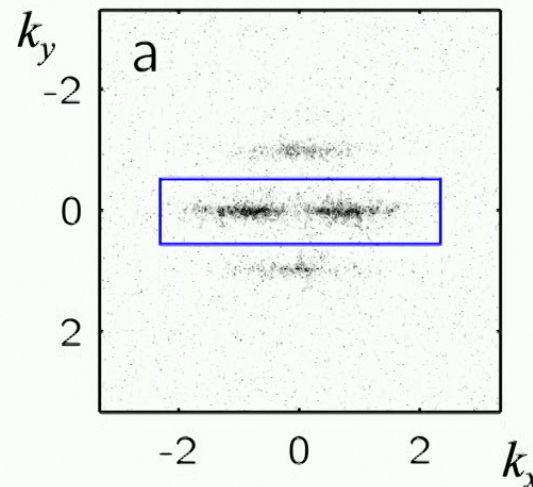
W. S. Bakr, et al., Nature 462, 74 (2009)  
 J. F. Sherson, et al. Nature 467, 68 (2010)

single shot projective measurements of the many body wavefunction: **n-point function**

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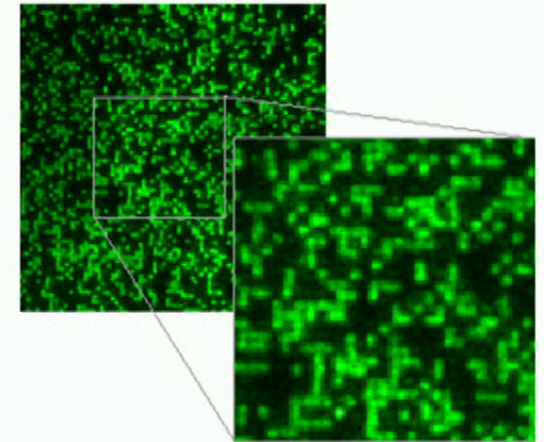


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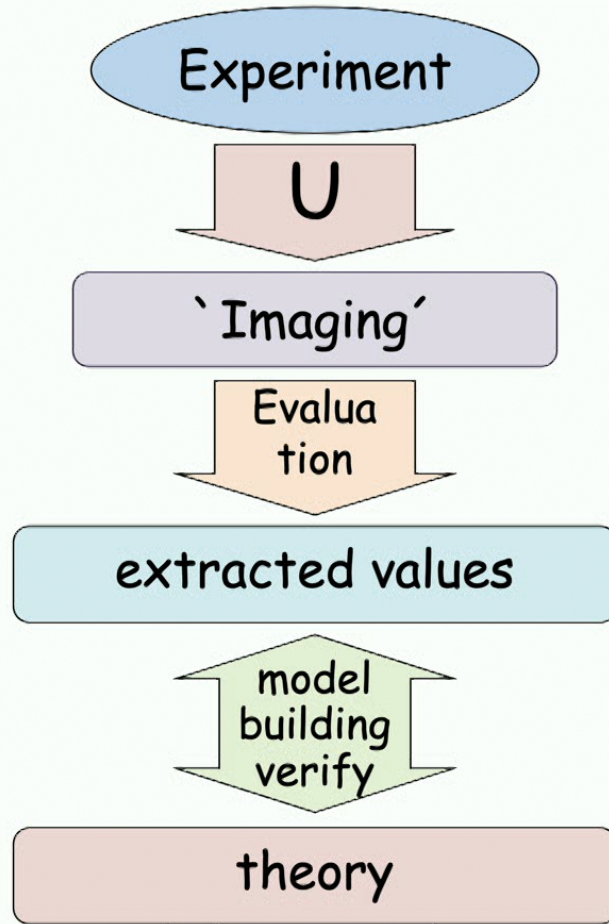


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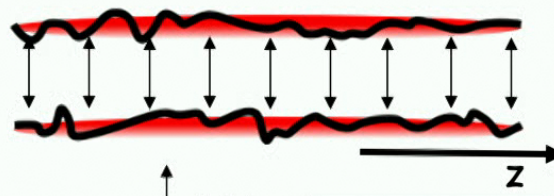
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Schweigler et al. Nature 545, 323 (2017)



1D gas of  $^{87}\text{Rb}$  atoms

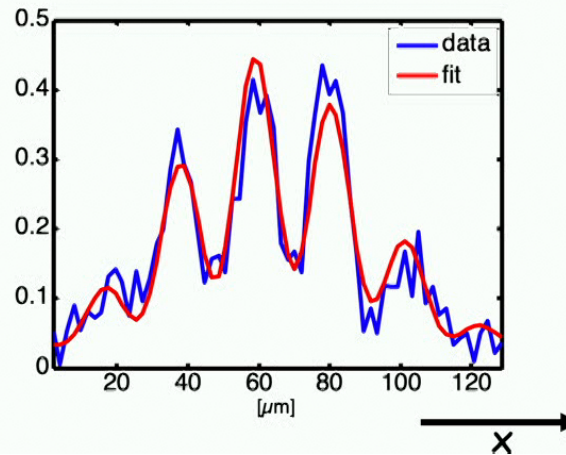
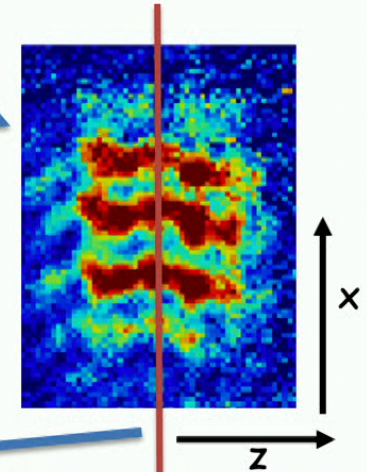


adjustable tunnelling  $J$

$$\psi(z) = e^{i\hat{\Theta}(z)} \sqrt{\rho_0(z) + \delta\hat{\rho}(z)}$$

Tunnel coupling lead to **phase locking** characterized by  $\langle \cos(\varphi) \rangle$

time of flight



fit

$\Rightarrow$  phase difference between condensates  $\varphi(z) = \theta_1(z) - \theta_2(z)$

Quantum field of SG model



# Verifying the Sine-Gordon Model

## Correlation functions

Exp: T. Schweiger, et al. (Vienna)  
Theory: S. Erne, V. Kasper, T. Zache et al. (HD)

Schweigler et al. arXiv:1505.03126  
Schweigler et al. Nature **545**, 323 (2017)  
Zache et al. PRX **10**, 011020 (2020)

# Correlation functions

## excitations $\leftrightarrow$ phase

in experiment we measure the phase  $\varphi(z)$  directly  
 $\rightarrow$  look at phase correlators

$$C^{(2)}(z_1, z_2) = \langle [\varphi(z_1) - \varphi(z_2)]^2 \rangle = \langle [\Delta\varphi(z_1, z_2)]^2 \rangle$$

with  $\Delta\varphi(z_1, z_2) = \varphi(z_1) - \varphi(z_2)$  **Note:  $\Delta\varphi$  is NOT restricted to  $2\pi$**

using 
$$\varphi(z) = \frac{1}{\sqrt{L}} \sum_{k \neq 0} \left[ (-i) \sqrt{\frac{\pi}{|k|K}} (b_k^\dagger - b_{-k}) e^{ikz} \right]$$

$$\longrightarrow \langle [\varphi(z_1) - \varphi(z_2)]^2 \rangle = \sum_{k_1, k_2} \frac{\pi}{K \sqrt{|k_1 k_2|}} b_{k_1}^\dagger b_{-k_2} e^{ik_1 z_1 + ik_2 z_2} + \dots$$

$\rightarrow$  phase correlators are related to the quasi particles

4<sup>th</sup> order

$$C^{(4)}(z_1, z_2, z_3, z_4) = \langle [\varphi(z_1) - \varphi(z_2)]^2 [\varphi(z_3) - \varphi(z_4)]^2 \rangle$$

$$\propto b_{k_1}^\dagger b_{k_2}^\dagger b_{-k_3} b_{-k_4} + \dots$$

$\rightarrow$  quasi particle scattering

# Correlation Functions

The  $N^{\text{th}}$  order Correlation function

$$G^{(N)}(\mathbf{z}) = \langle \mathcal{O}(z_1) \mathcal{O}(z_2) \dots \mathcal{O}(z_N) \rangle$$

Characterizes the propagation and the interactions of the degrees of freedom connected to the operators  $\mathcal{O}(z_i)$

# Correlation Functions

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Characterizes the propagation and the interactions of the degrees of freedom connected to the operators  $\mathcal{O}(z_i)$

It can be decomposed:  $G^{(N)}(\mathbf{z}) = G_{\text{dis}}^{(N)}(\mathbf{z}) + G_{\text{con}}^{(N)}(\mathbf{z})$

- The **disconnected** part  $G_{\text{dis}}^{(N)}$  is fully determined through lower order correlations
- The **connected** part  $G_{\text{con}}^{(N)}$  contains **genuine new information about the system** at order  $N$



# 4<sup>th</sup> order correlations

## Connected and disconnected part

Schweigler et al. Nature 545, 323 (2017)

to study factorization of correlation functions we look at:

$$G^{(2)}(z_1, z_2) = \langle [\varphi(z_1) - \varphi(z_2)]^2 \rangle$$

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$$\Delta\varphi(z_1, z_2) = \varphi(z_1) - \varphi(z_2)$$

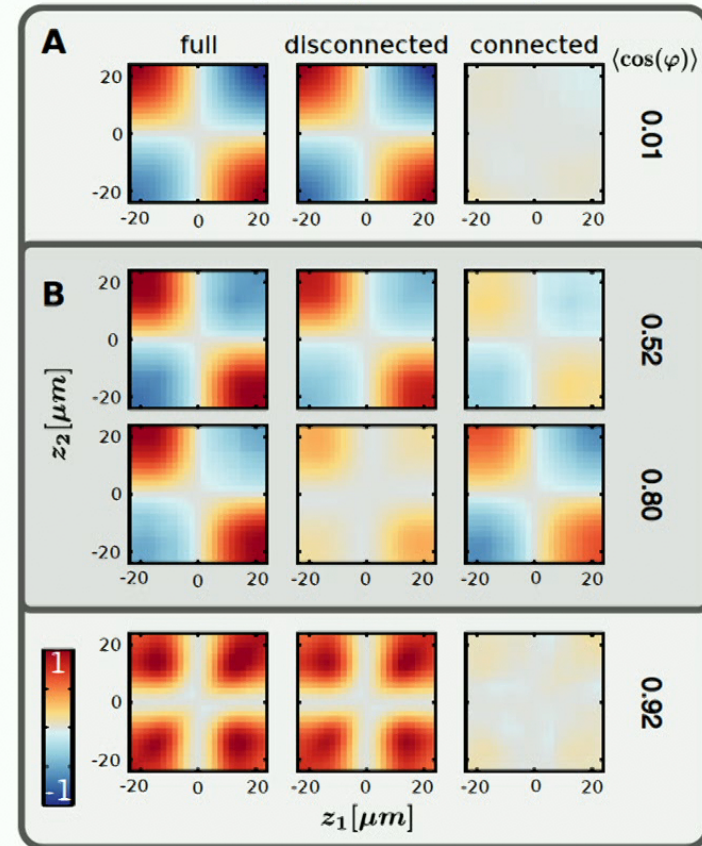
$\Delta\varphi$  is NOT restricted to  $[-\pi, \pi)$

Connected/Disconnected part

$$G^{(N)}(\mathbf{z}) = G_{\text{con}}^{(N)}(\mathbf{z}) + G_{\text{dis}}^{(N)}(\mathbf{z})$$

J. Schmiedmayer: Quantum Simulators for QuFT

$$C^{(4)}(z_1, z_2, -15, 15)$$



# Characterizing Connected Correlations

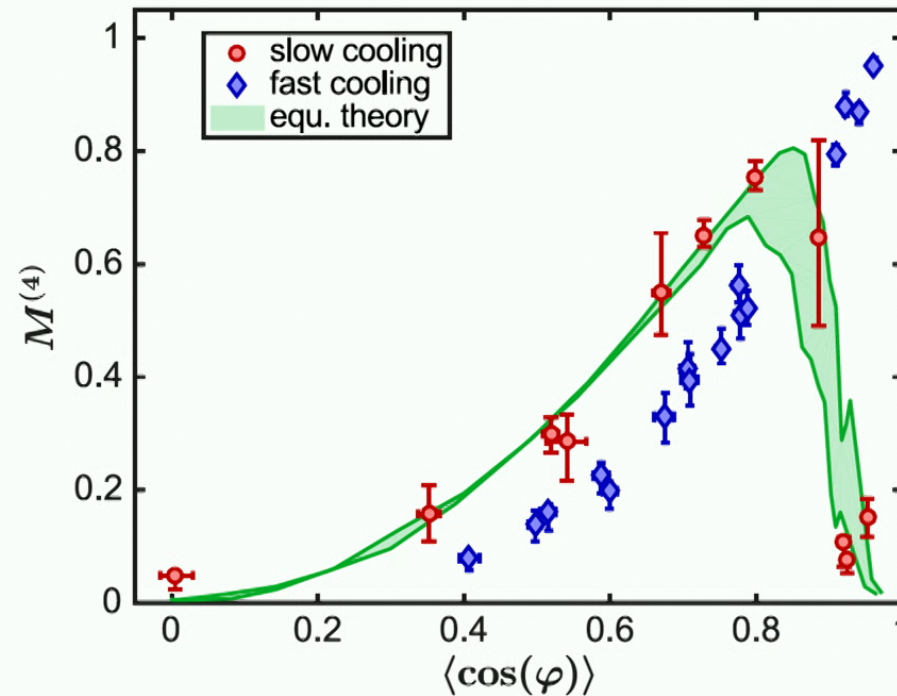
Schweigler et al. Nature 545, 323 (2017)

## 4<sup>th</sup> order correlations

Integrated measure

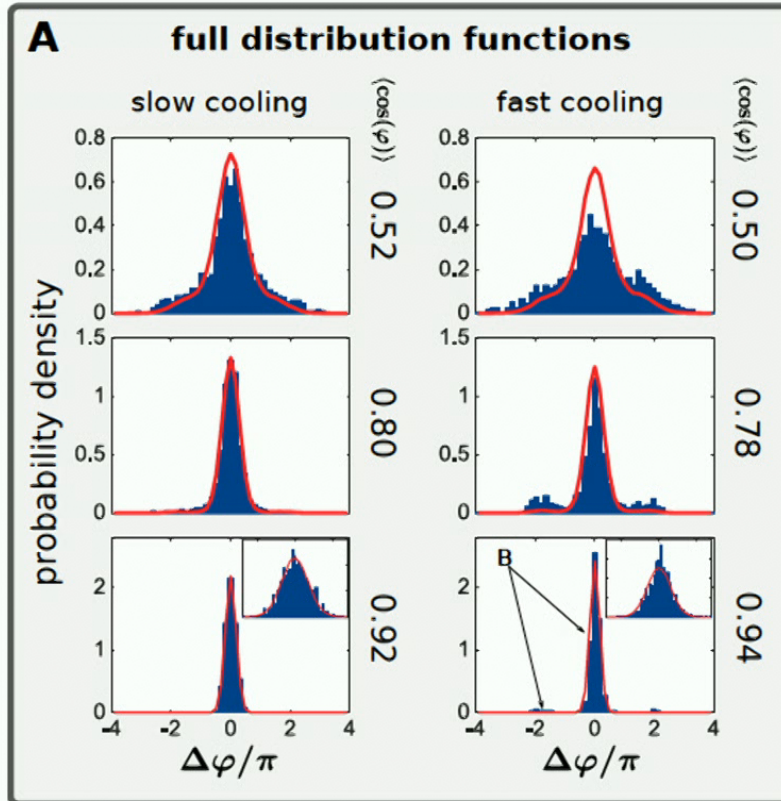
$$M^{(N)} = \frac{\sum_{\mathbf{z}} |G_{\text{con}}^{(N)}(\mathbf{z}, 0)|}{\sum_{\mathbf{z}} |G^{(N)}(\mathbf{z}, 0)|}$$

Compared to predictions for a thermal equilibrium state of the sine-Gordon model



# Quantifying factorization of correlation functions

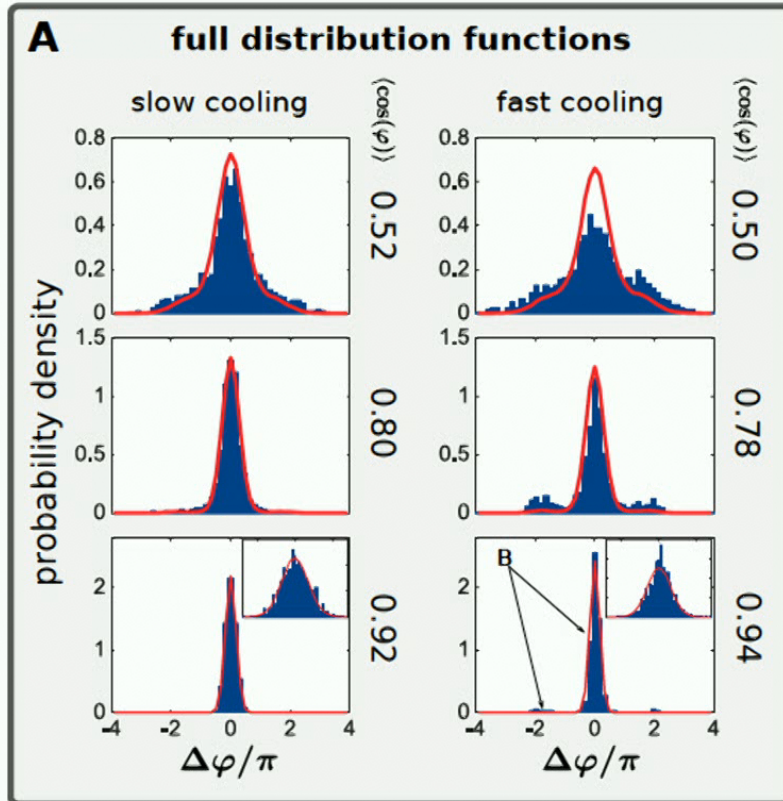
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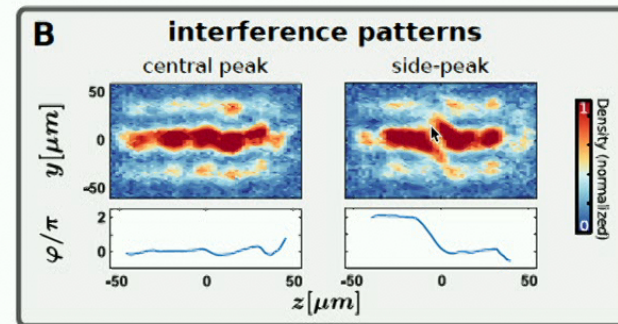
- the breakdown of factorization is evident in the full distribution functions of the phase by new peaks at multiples of  $2\pi$
- caused by the  $2\pi$  *periodic* SG Hamiltonian  $\rightarrow 2\pi$  phase jumps, 'kinks' = SG solitons

# Quantifying factorization of correlation functions

Schweigler et al. Nature 545, 323 (2017)



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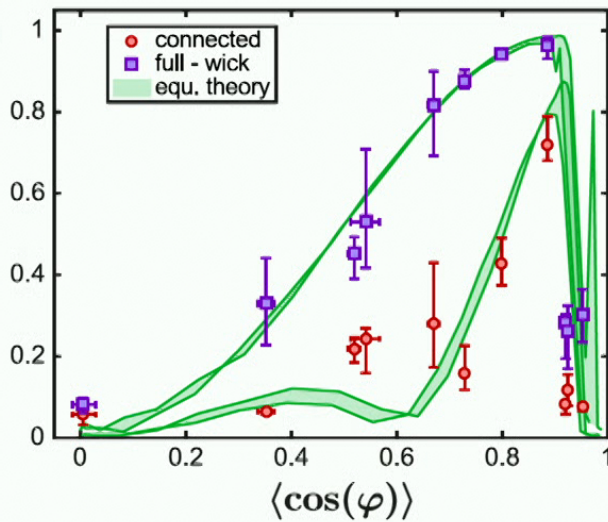


- SG Solitons are topological excitations
- Phase fluctuations around *topologically different Vacua*

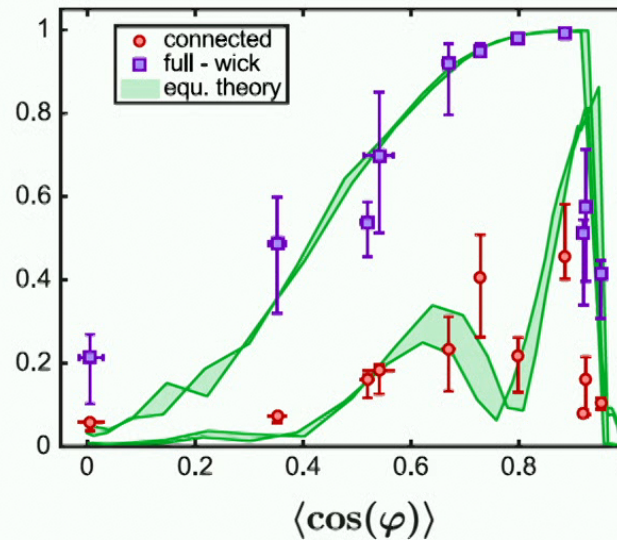
# Higher order connected correlations

Schweigler et al. Nature 545, 323 (2017)

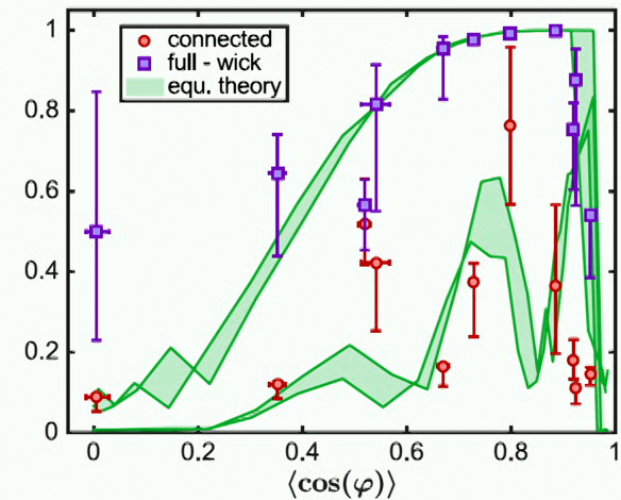
6<sup>th</sup> order



8<sup>th</sup> order



10<sup>th</sup> order



Limit is NOT the data but the computational complexity of data analysis for strongly fields

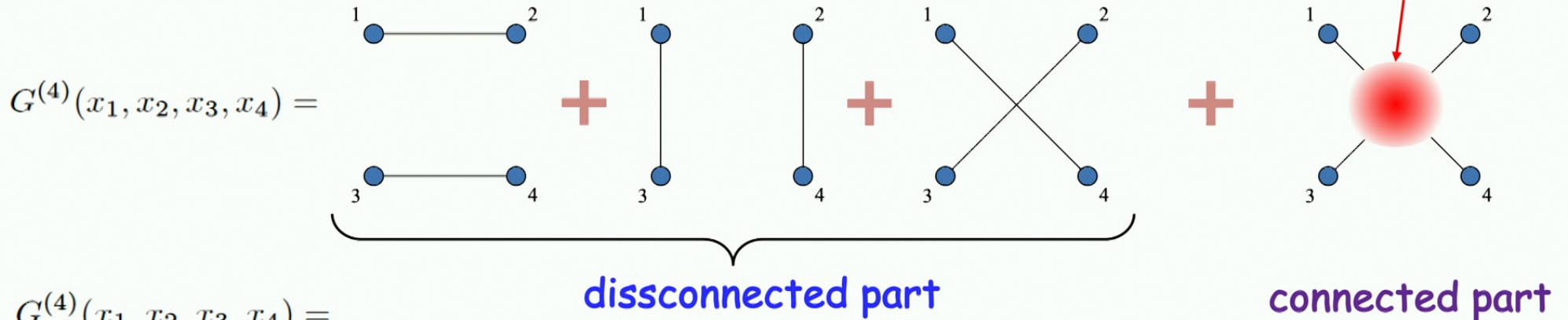


# Verifying the Sine-Gordon Model

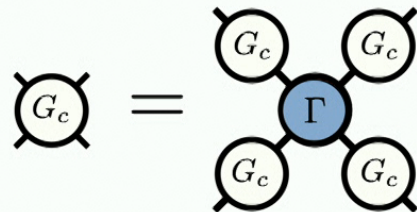
extracting the parameters of the  
effective theory from experiment

Zache et al. PRX 10, 011020 (2020)

# Diagrammatics: one-particle irreducible - 1PI



$$\begin{aligned}
 G^{(4)}(x_1, x_2, x_3, x_4) = & G^{(2)}(x_1, x_3)G^{(2)}(x_2, x_4) + G^{(2)}(x_1, x_2)G^{(2)}(x_3, x_4) + G^{(2)}(x_1, x_4)G^{(2)}(x_2, x_3) \\
 & + \int d^D y_1 \dots d^D y_4 G^{(2)}(x_1, y_1)G^{(2)}(x_2, y_2)G^{(2)}(x_3, y_3)G^{(2)}(x_4, y_4) \Gamma^{(4)}(y_1, y_2, y_3, y_4)
 \end{aligned}$$



**1PI correlators:**  
*building blocks of all correlations!*

# Equal-Time QuFT

Standard formulation of QuFT is with **non-equal time** correlators

**Experiment:** **equal time** correlations are much more accessible (extracted from the pictures)

→ **Equal time formulation of QuFT**

State  $\hat{\rho}_t$  is completely characterized by **all equal-time correlation** functions

quantum dynamics leads to a hierarchy of coupled evolution equations

*Wetterich Phys. Rev. E56, 2687 (1997)*

$$i\partial_t \text{---} \Gamma_t \text{---} = \dots$$



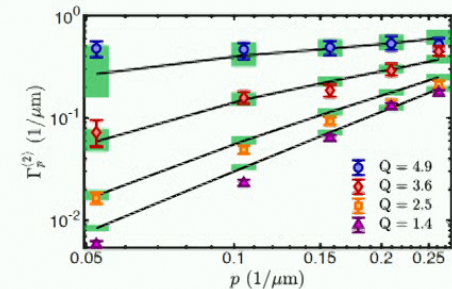
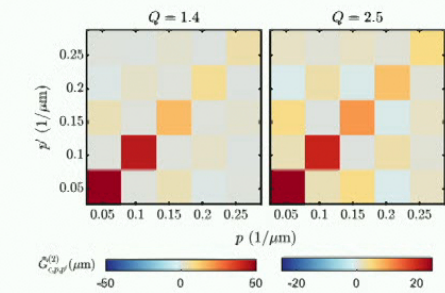
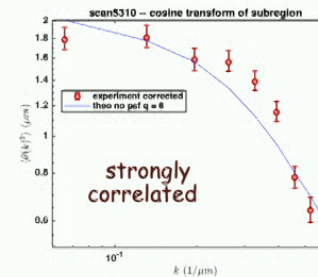
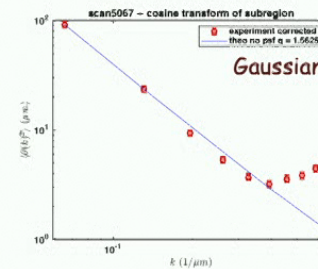
# Extracting the Coupling Constants

- The measured connected correlators contain contributions from the propagators (the 'legs')
- To extract the information about the coupling constants in the scattering vertices one has to 'amputate' the correlators
- Best done in momentum representation.
- In our finite system we have a discrete momentum spectrum (the modes of the system)
- Transform the correlators to the space of the modes

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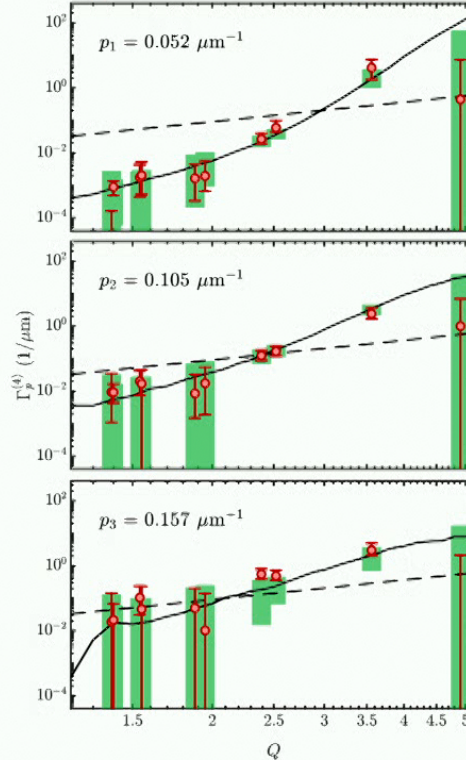
transformed  
2-point correlator  
(1/propagator)



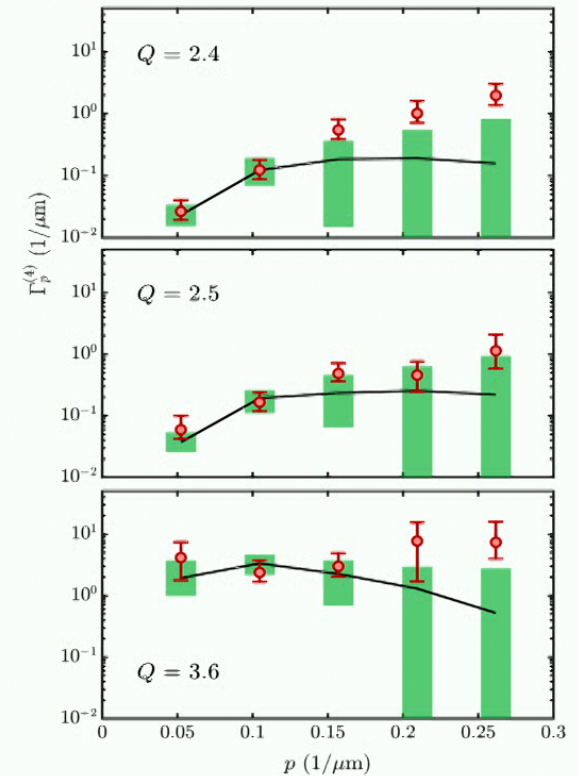
# Extracting the Coupling Constants

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'amputated' connected 4-point correlator (vertex)



running coupling in SG model



# Some recent applications

Area Law of Mutual Information in QuFT

Curved light cones

Floquet engineering a QuFT

Gaussification after a quench

M. Tajik et al. Nature Physics (2023)

M. Tajik et al. PNAS 120, 21 (2023)

Si-Cong Ji et al. PRL 129, 080402 (2022)

Scheigler et al. Nature Physics, 17, 559 (2021)

# Mutual information

Shared information content between two subsystems

• Definition:

$$I(A : B) = S_A + S_B - S_{A \cup B}$$



von Neumann entropy for subsystem A

$$S_A = -\text{Tr}(\rho_A \ln \rho_A) \quad \text{with} \quad \rho_A = -\text{Tr}_B(\rho_{A \cup B})$$

• Motivation:

- Captures the total amount of information of a subsystem about another one.
- It gives the entanglement entropy in the limit of zero temperature.
- Shows an area law for gapped Hamiltonians.
- Can the area law be verified experimentally for a system with decaying correlations?

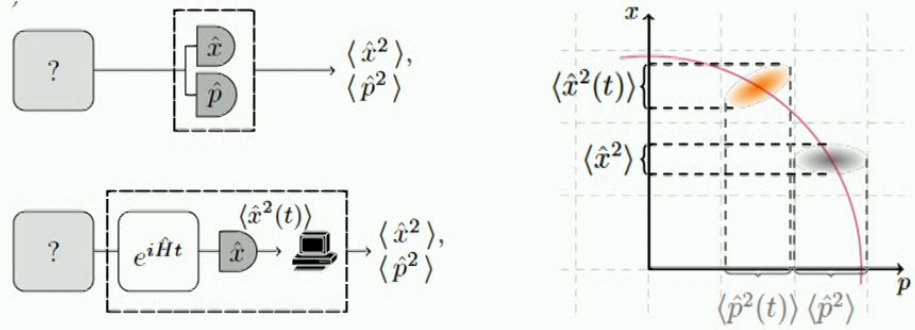
# Many Body Tomography

In interference experiments we measure phase quadrature

M. Gulza et al. Communications Physics 3, 12 (2020)  
arXiv:1807.04567

**Idea:**  
'free evolution' **rotates** the Wigner function of the modes in the low energy effective field theory

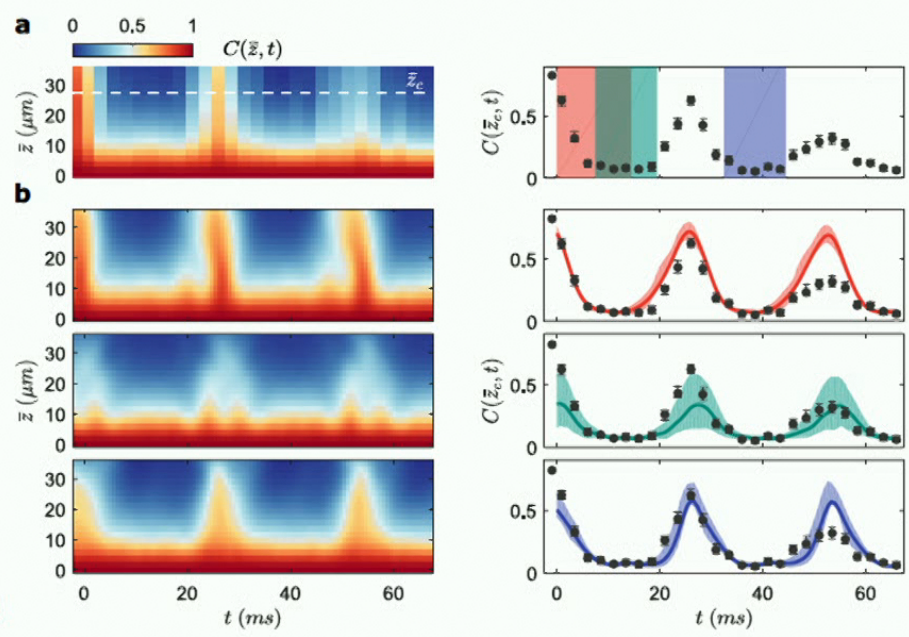
**Example:**  
data from recurrence experiment



Repeated measurement  $\Rightarrow$  tomographic slicing

**➔** allows reconstruction of the density matrix

Will give excess to v. Neumann entropy, mutual information and entanglement etc ...

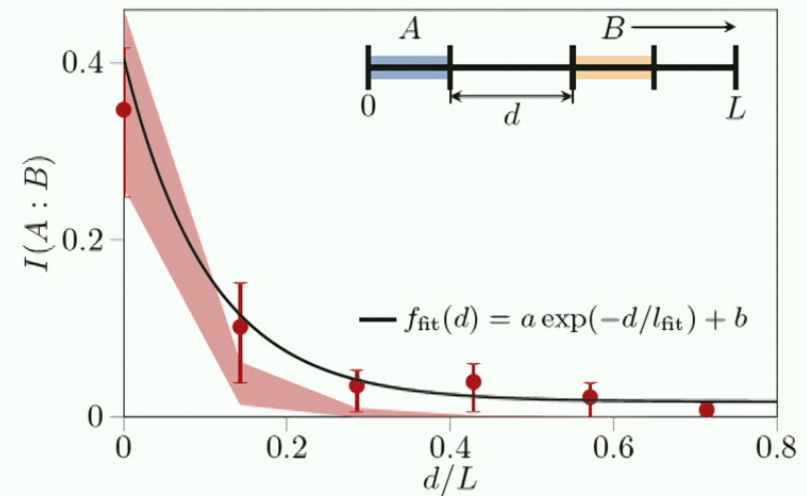
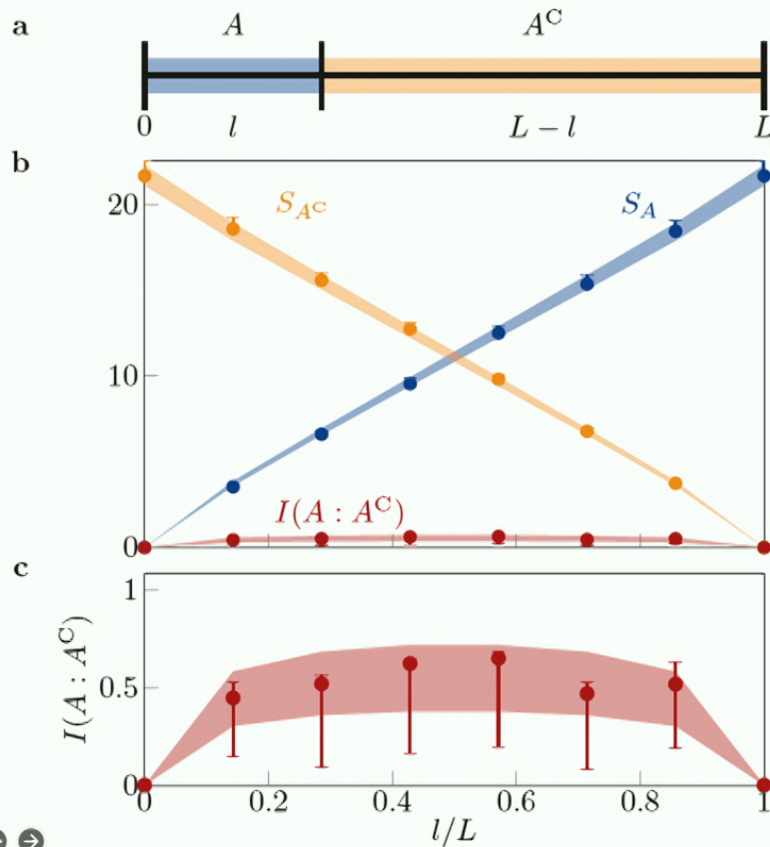


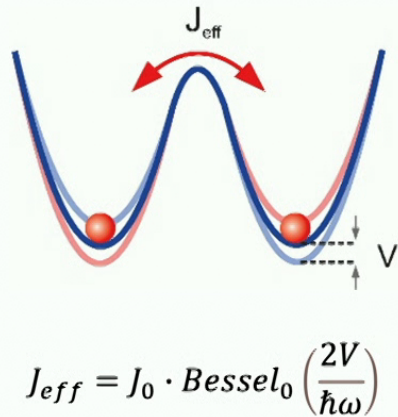
# V. Neumann $\leftrightarrow$ Mutual Information

## Experiment in Klein-Gordon

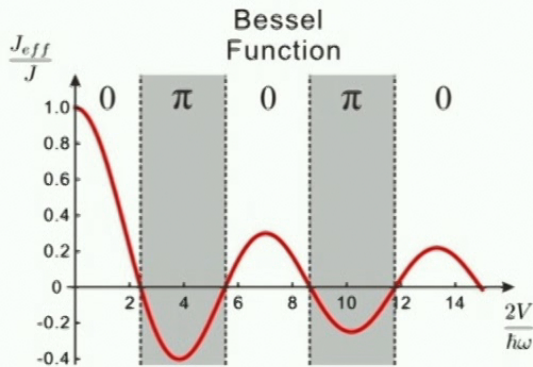
$$I(A : B) = S_A + S_B - S_{A \cup B}$$

M. Tajik et al. Nature Physics (2023)  
arXiv:2206.10563

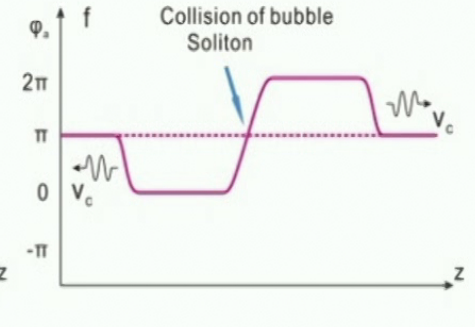
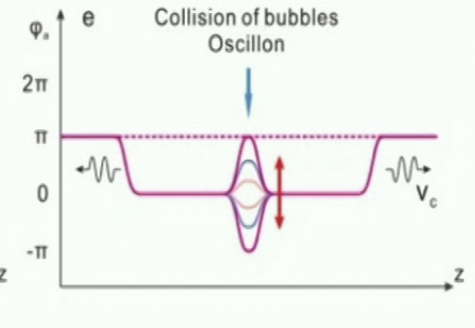
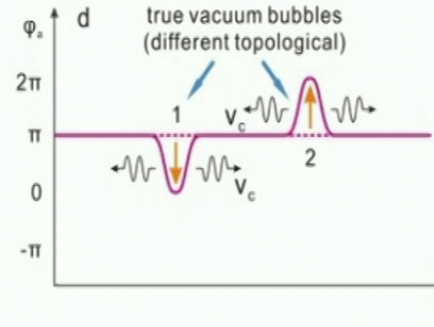
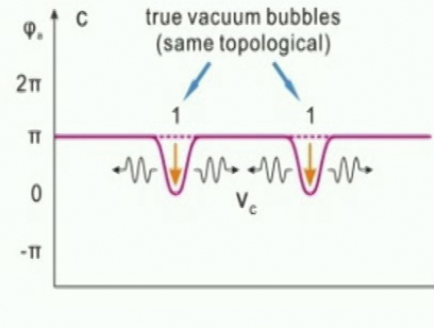
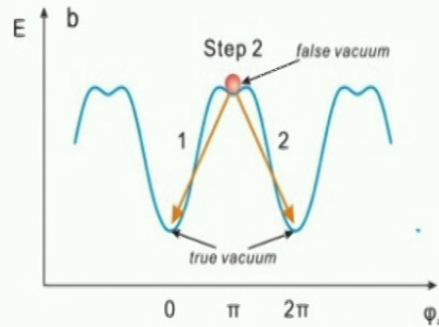
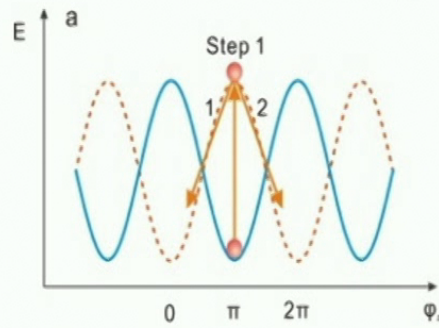




$$J_{\text{eff}} = J_0 \cdot \text{Bessel}_0\left(\frac{2V}{\hbar\omega}\right)$$



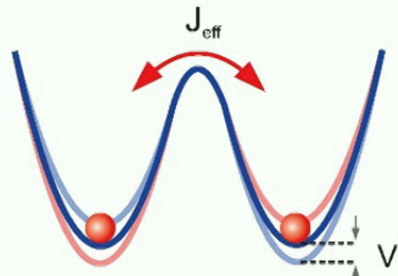
## Floquet Engineering a Sine Gordon QuTF



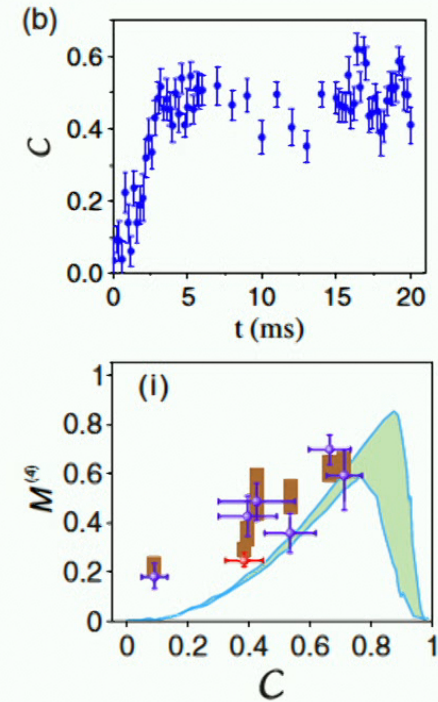
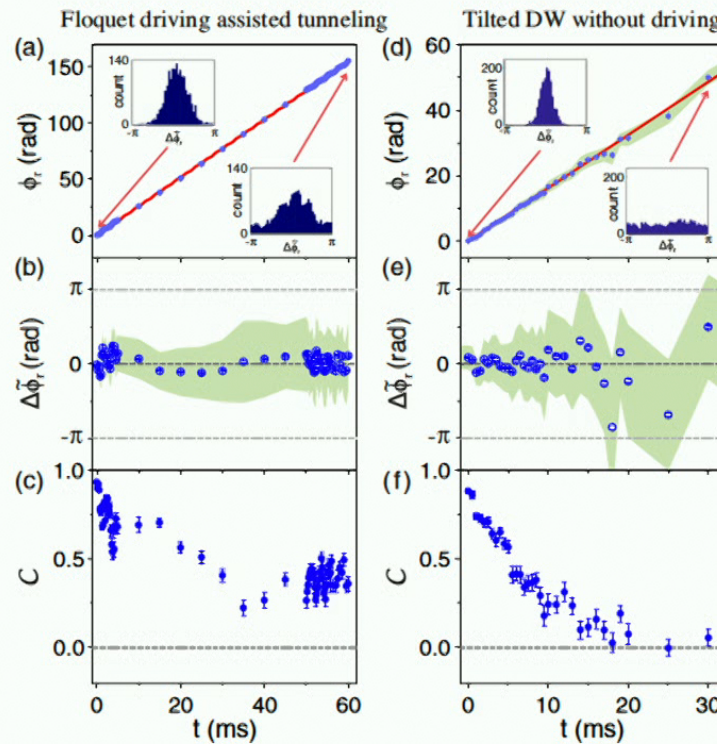
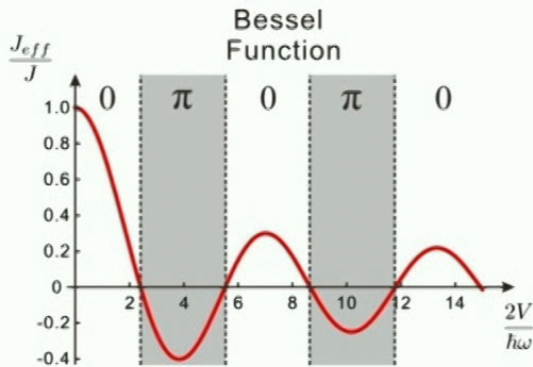
☹️ observed too much heating ☹️



## Floquet Engineering a Sine Gordon QuTF

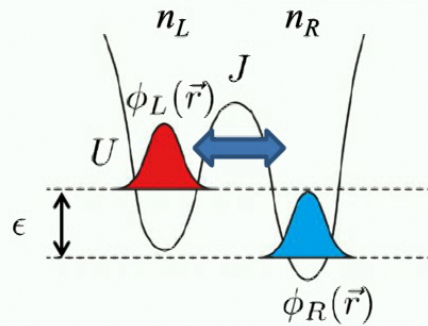


$$J_{eff} = J_0 \cdot \text{Bessel}_0\left(\frac{2V}{\hbar\omega}\right)$$

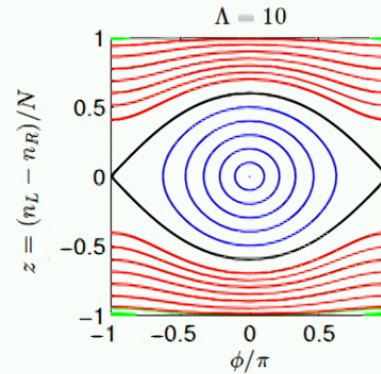


# Decay of Self-Trapping

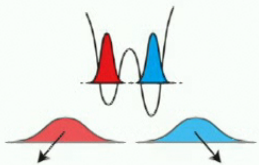
? Decay of false vacuum in a 1d bosonic Josephson Junction ?



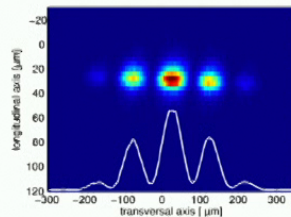
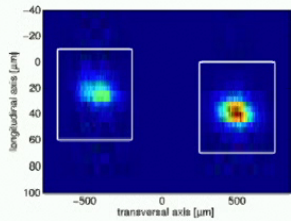
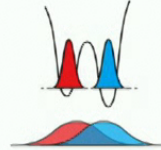
**0D:** self trapping  
**1D:** Decay of self trapped state



population imbalance measurement

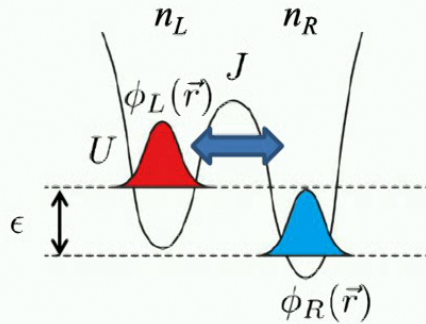


relative phase measurement

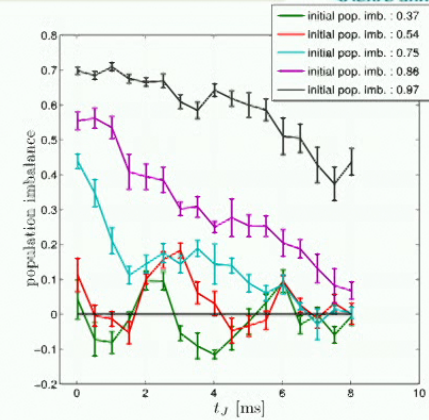
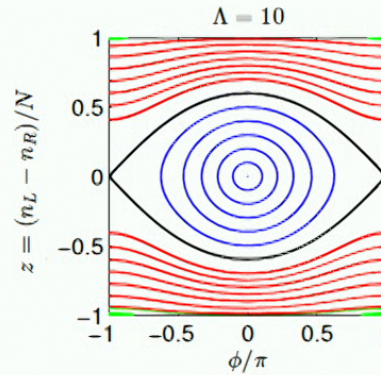


# Decay of Self-Trapping

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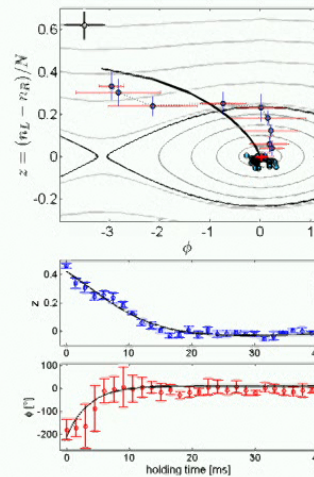
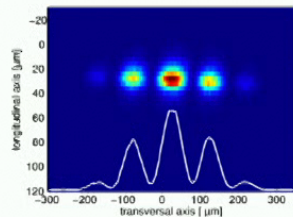
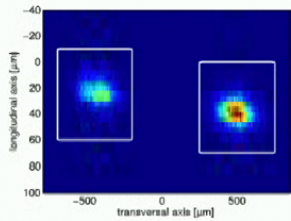
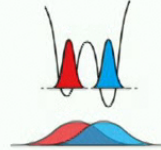
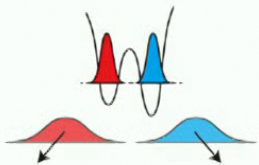


**0D:** self trapping  
**1D:** Decay of self trapped state

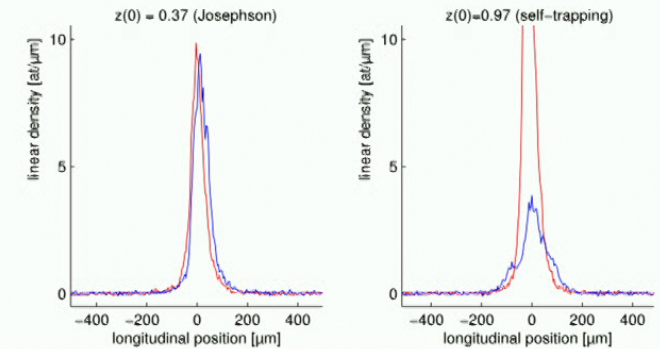


population imbalance measurement

relative phase measurement



**longitudinal momentum**



# Older quantum simulations of QuFT physics

Relaxation in isolated system:

Pre-thermalization:

Light cone spreading of correlations:

Generalized Gibbs Ensemble:

Recurrences in QuFT:

Universality in non-equilibrium:

Hofferberth et al Nature 449, 324 (2007)

Gring et al., Science 337, 1318 (2012)

Kuhnert et al., PRL 110, 090405 (2013)

Langen et al., Nature Physics 9, 460 (2013)

Langen et al., Science 348, 207 (2015)

Rauer et al. Science 360, 307 (2018)

Erne et al., Nature 563, 225 (2018)

# Outlook Sine Gordon

Hamiltonian learning  
SG close to quantum vacuum  
SG out of equilibrium  
Decay of self trapping

...

Pokrovsky-Talapov model  
Other SG models

[www.AtomChip.org](http://www.AtomChip.org)

# Emergent description of 1d systems

Luttinger Liquid

$\leftrightarrow$

Generalized Hydro Dynamics

Møller et al. SciPost Physics 8, 041 (2020)

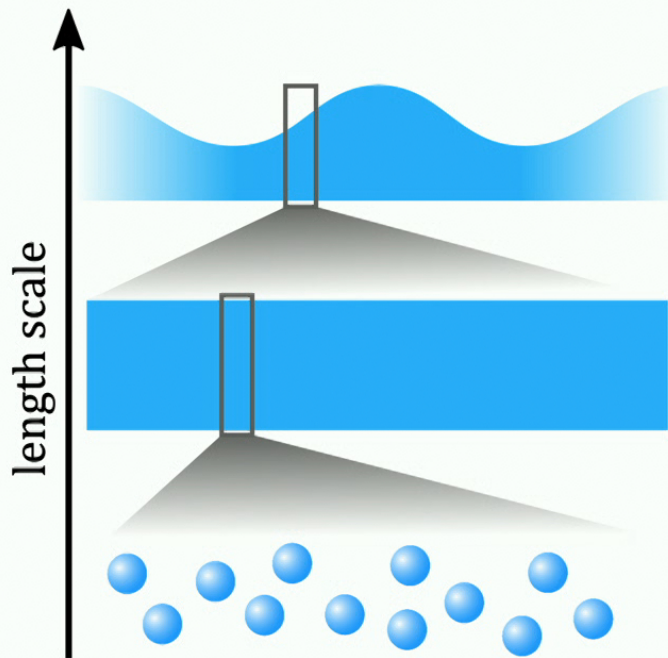
Møller et al. PRL 126, 090602 (2021)

Cataldini et al. Phys. Rev. X 12, 041032 (2022)

# Emergence of hydrodynamics in 1d systems

B. Bertini  
JS Caux  
B. Doyon,  
J. Dubai

....



Macroscopic: Slow variations

**Thermodynamic Bethe Ansatz**

Mesoscopic: Homogeneous  
Local equilibrium

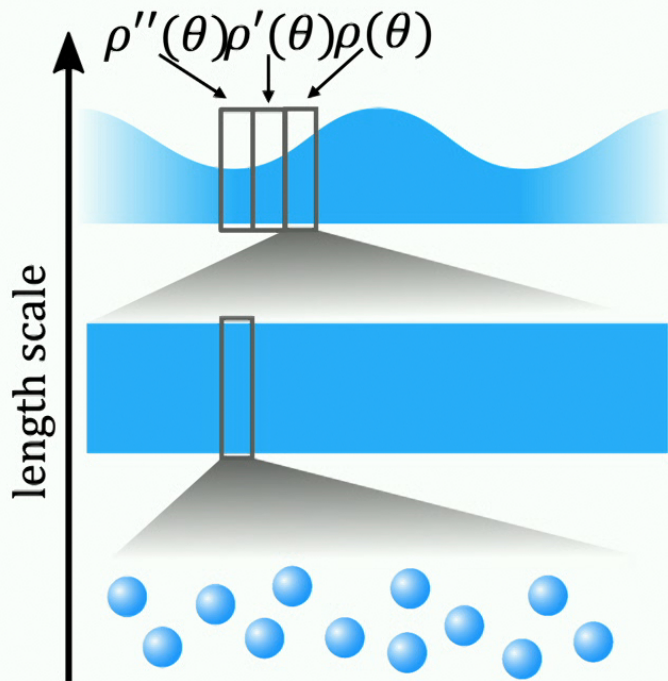
Microscopic: Atoms

Generalized Hydro Dynamics (GHD)  
OA. Castro-Alvaredo et al., PRX 6, 041065 (2016)  
B. Bertini et al., PRL. 117, 207201 (2016)  
+ very many papers since then

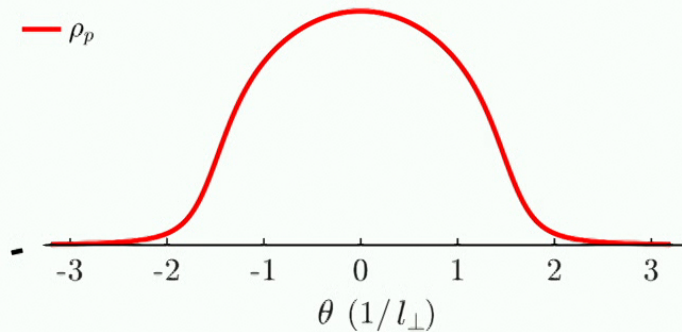
# Emergence of hydrodynamics

B. Bertini  
 JS Caux  
 B. Doyon,  
 J. Dubai  
 ....

$$\partial_t \rho(\theta, t, z) + \partial_z (v^{\text{eff}}(\theta, t, z) \rho(\theta, t, z)) = 0$$



Thermodynamic state fully characterised by distribution of quasi-momenta (rapidities  $\theta$ )

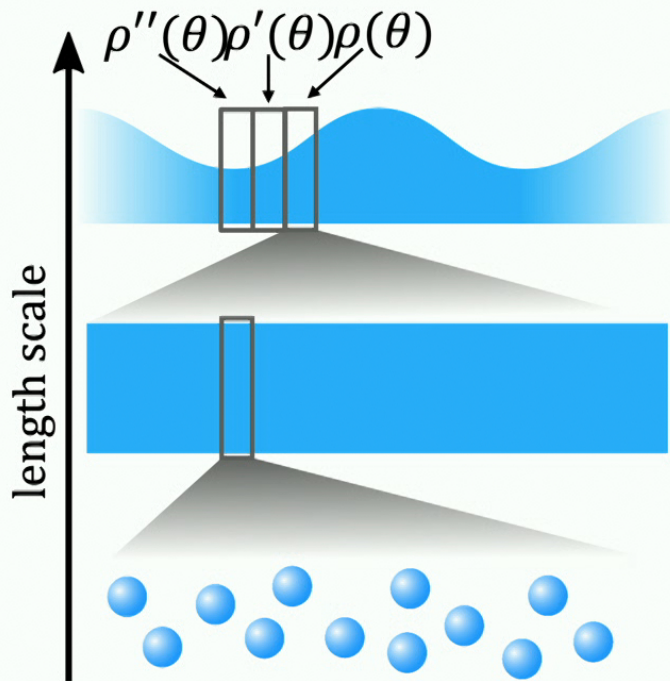




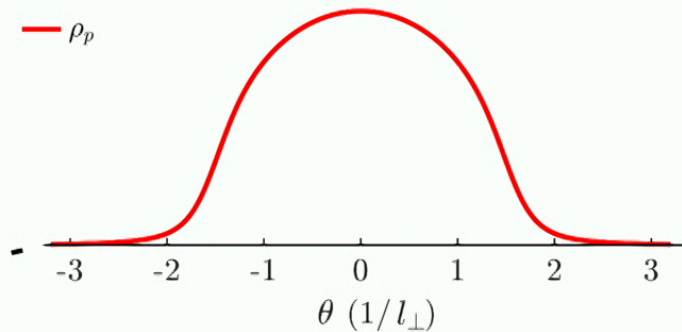
# Emergence of hydrodynamics

B. Bertini  
 JS Caux  
 B. Doyon,  
 J. Dubai  
 ....

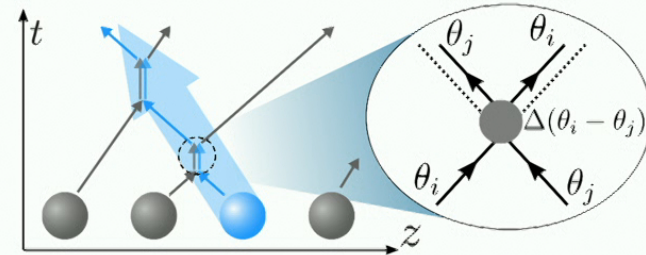
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Thermodynamic state fully characterised by distribution of quasi-momenta (rapidities  $\theta$ )



Rapidities  
 behave like  
 Fermions

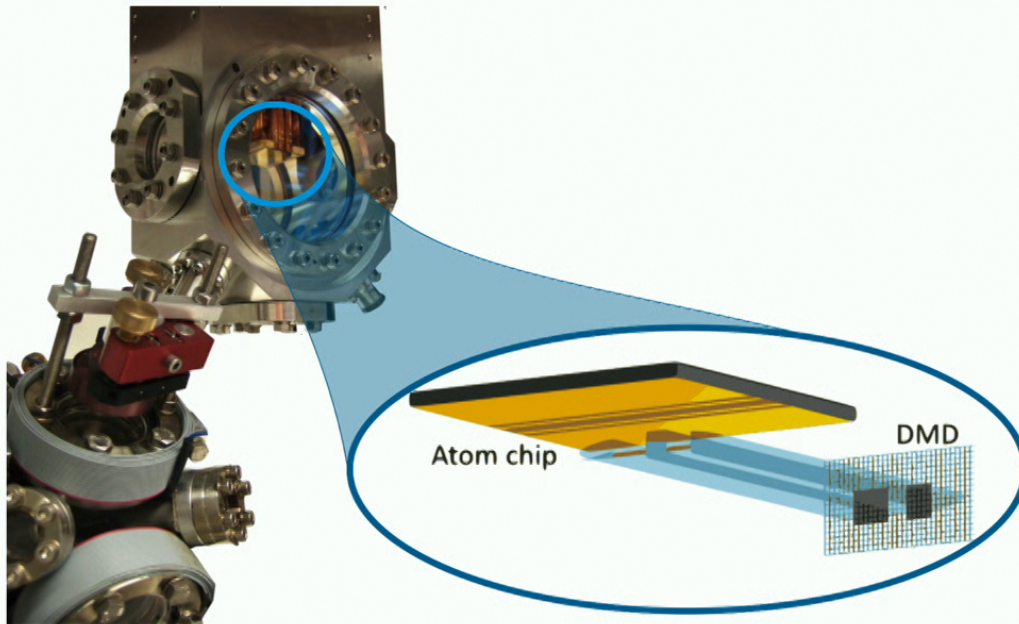


# Excitating a single mode in a 1d quantum gas

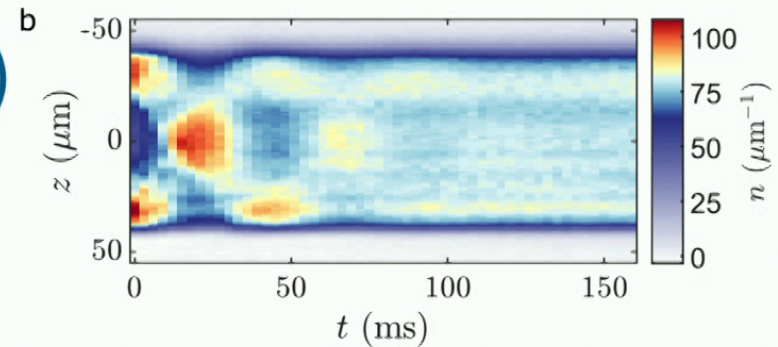
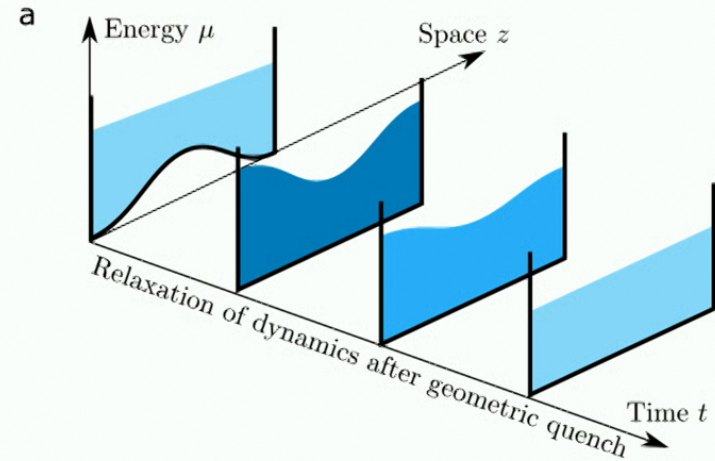
F. Cataldini, F. Möller

Cataldini et al. Phys. Rev. X 12, 041032 (2022)

## 1. Imprint cosine-shaped density perturbation.



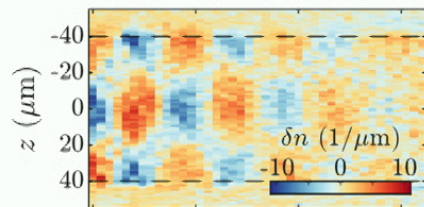
Tajik et al. Optics Express, 27, 33474 (2019)



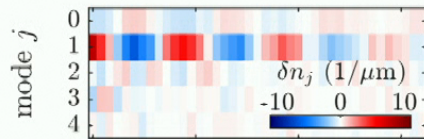
# Relaxation dynamics

low temperature  
small amplitude

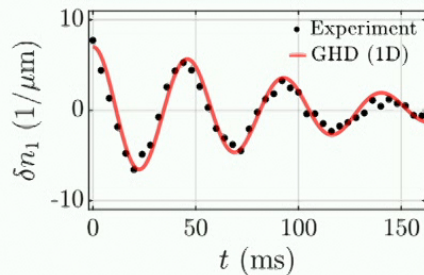
$$T = 46(4)\text{nK} [0.69(6)\hbar\omega_{\perp}]$$



Long lived dynamics!



(Almost) single mode excitation!



Fast damping of the phonon mode

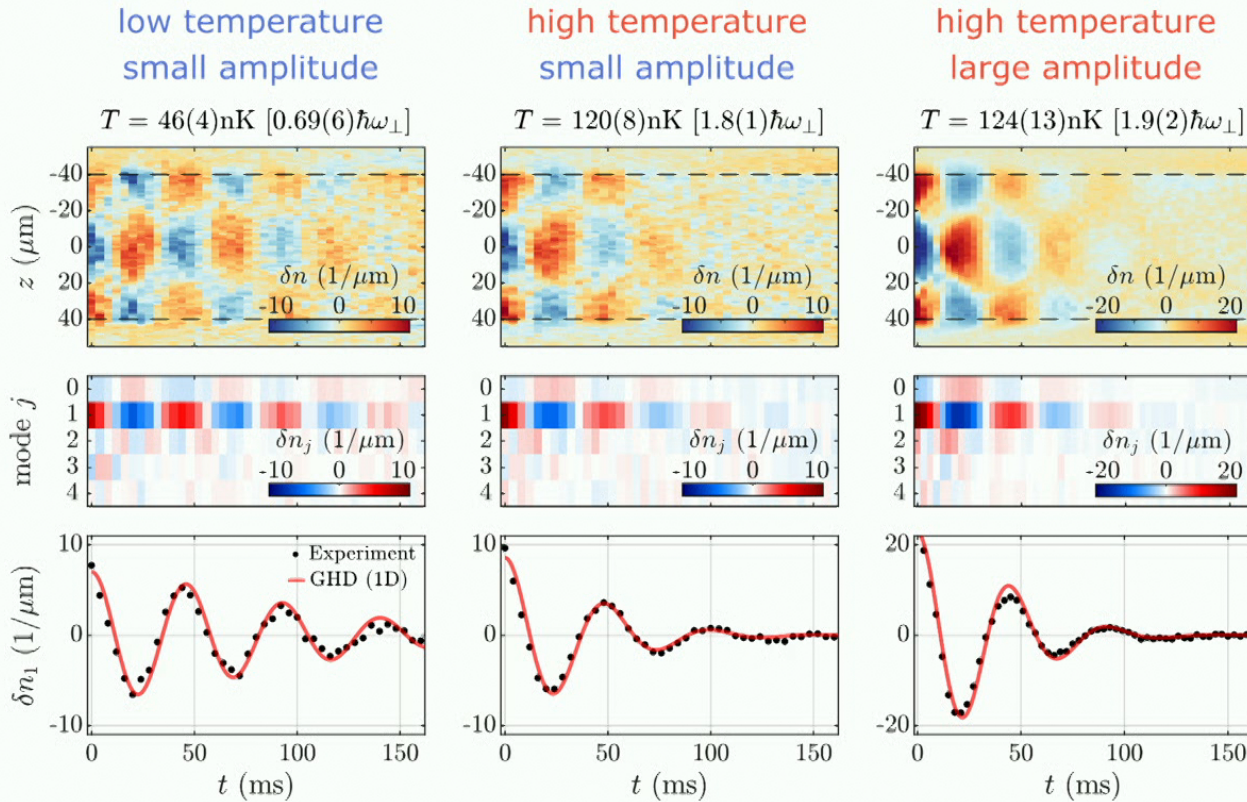
GHD gives a perfect description of the damping  
no free parameters

# Relaxation dynamics

Cataldini et al. Phys. Rev. X 12, 041032 (2022)

Standard 1D condition:

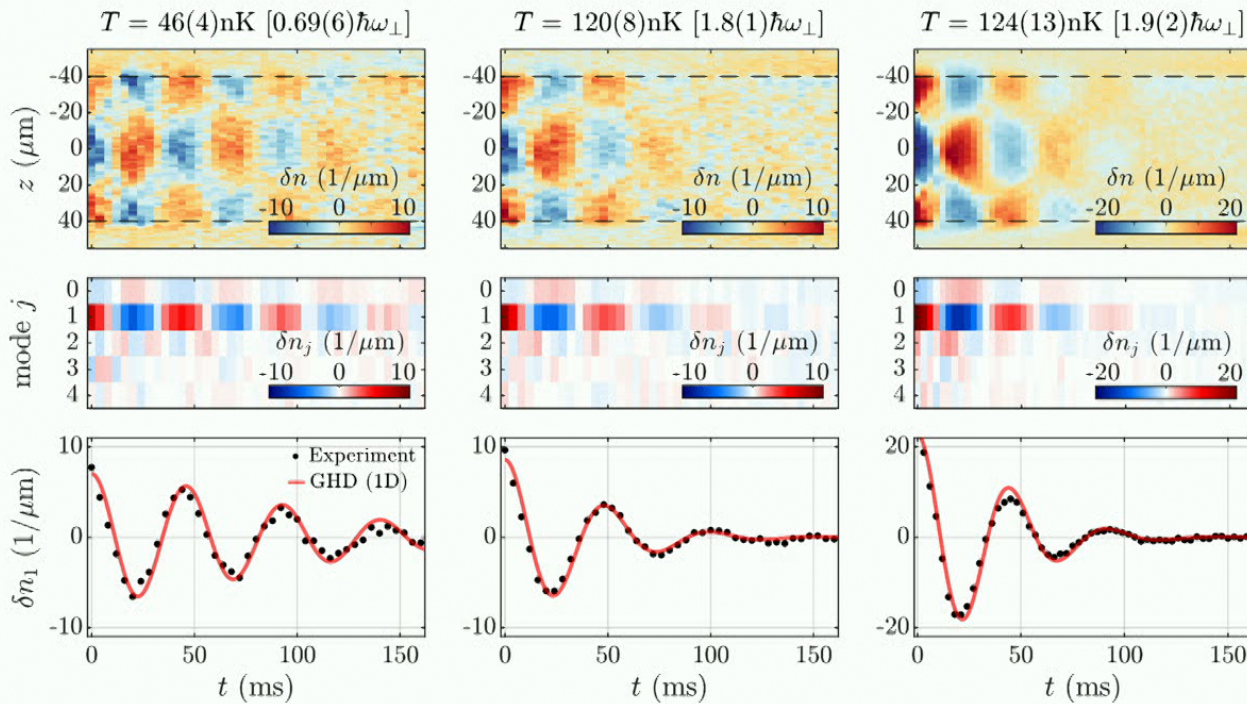
$$\mu, k_B T \ll \hbar \omega_{\perp}$$



low temperature  
small amplitude

high temperature  
small amplitude

high temperature  
large amplitude



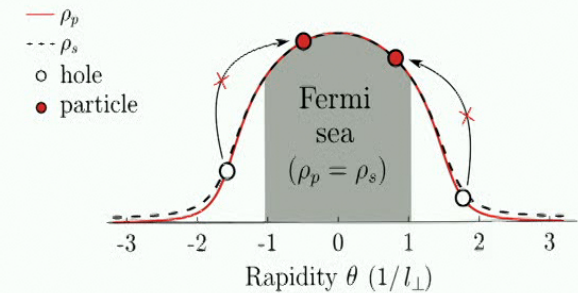
Standard 1D condition:

$$\mu, k_B T \ll \hbar\omega_{\perp}$$

Even far above this condition, the observed relaxation is consistent with 1D GHD theory!

Interpretation:

In a box the rapidities fill the complete Fermi sea and thereby prevent thermalizing collisions much longer.

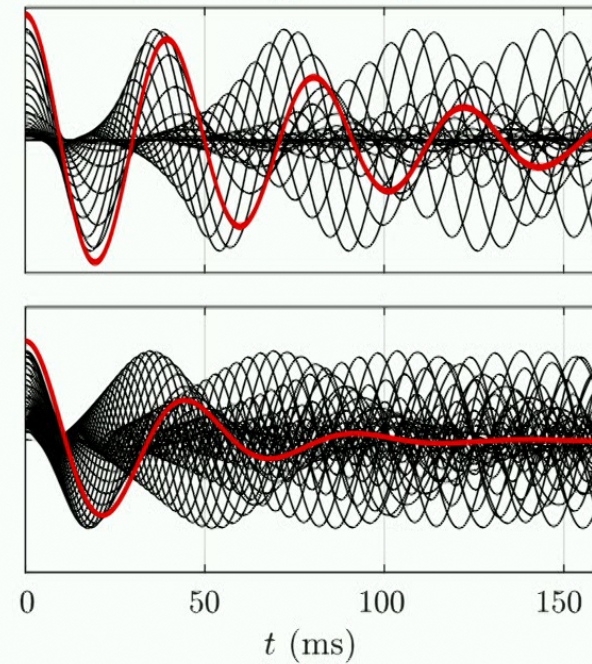
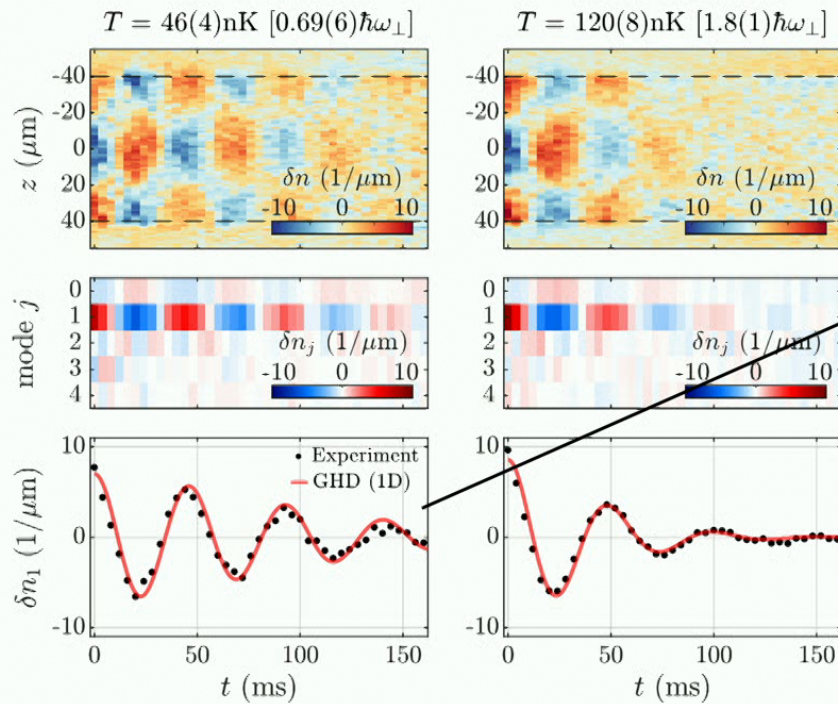


# Relaxation dynamics

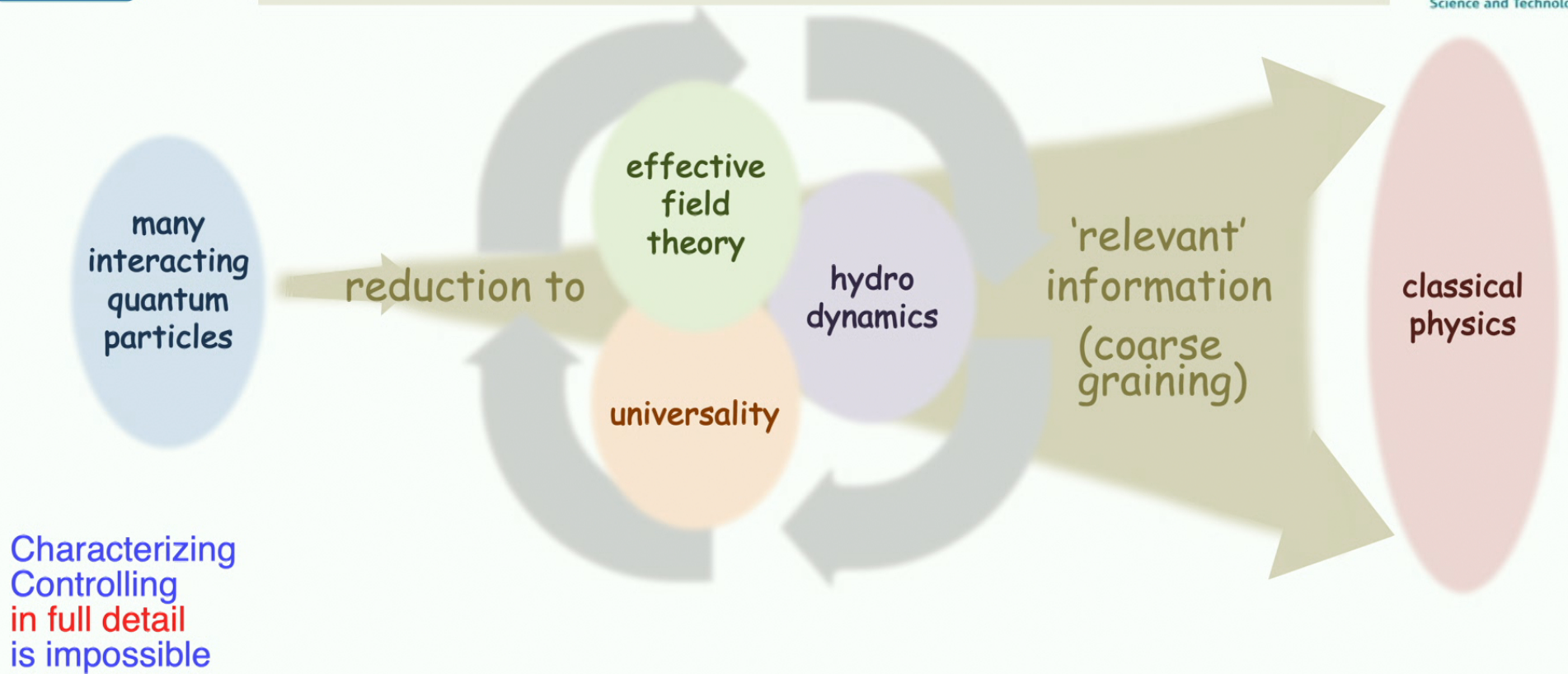
low temperature  
small amplitude

high temperature  
small amplitude

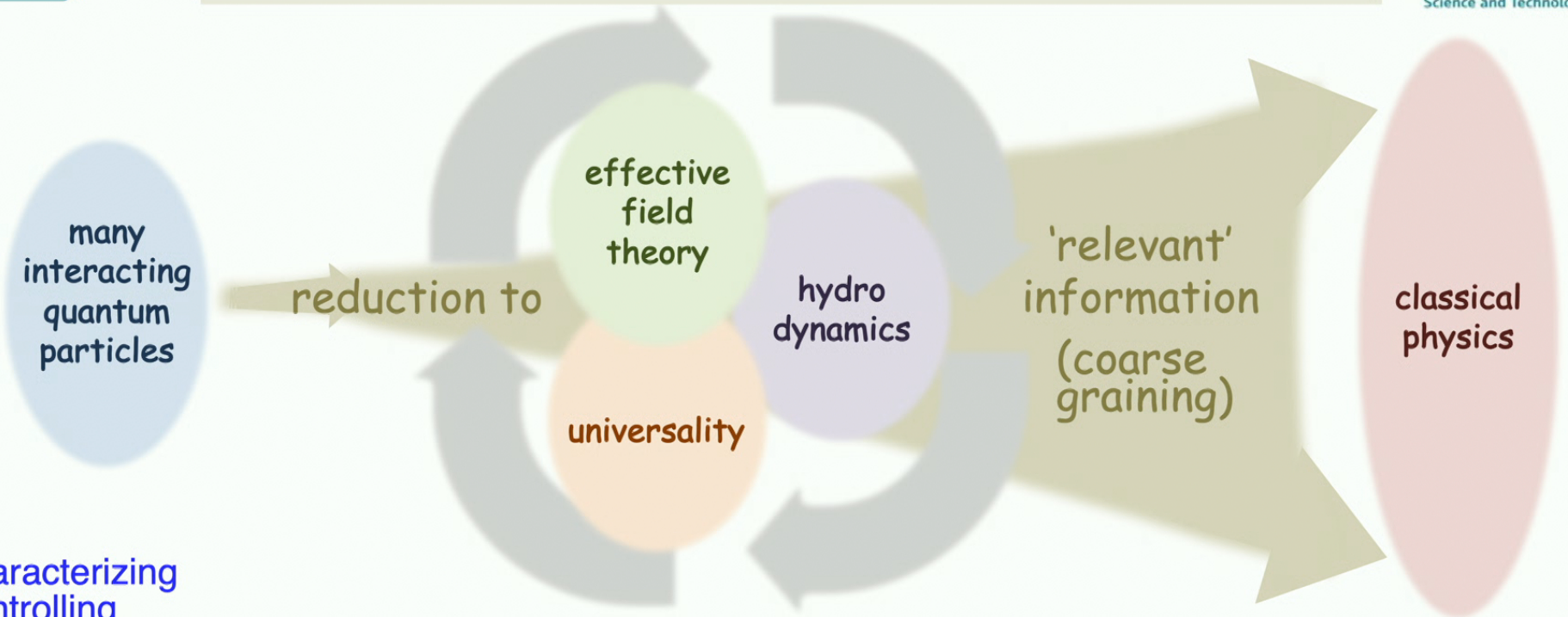
Relaxation is caused by  
dephasing of rapidities!



# Emergence in Quantum Physics



# Emergence in Quantum Physics



Characterizing  
Controlling  
in full detail is impossible ⇒ "Loss" of information  
⇒ Reduction to "relevant" information  
⇒ Emergence of novel descriptions

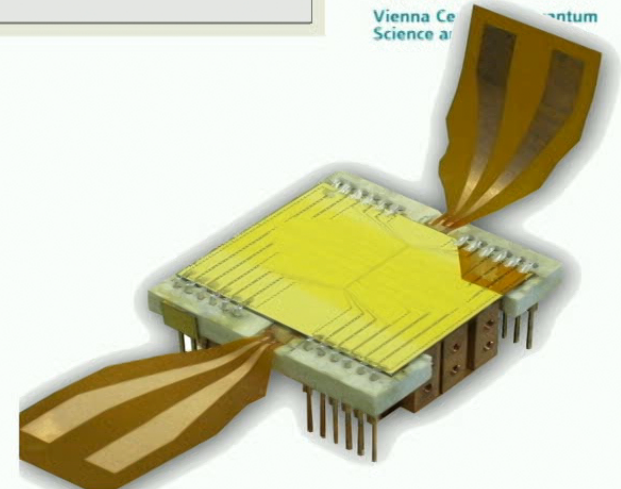
Experiments with **ultra cold quantum gases**:  
Measure each constituent with unit efficiency  
Computational complexity of data analysis is limitation !  
Choose which part of the information to retain/analyse  
**Experimentally** study emergence in detail



# What have we learned

- Higher order correlation functions (full distribution functions) and the question if they factorize gives insight in the effective quantum field theories describing the many body system.
- Verified Sine-Gordon model as emergent from the microscopic physics of two tunnel coupled super fluids
- Identified the topological excitations in the SG model.
- Extracted parameters of the model from experimental data
- Compared two emerging descriptions of 1d systems: Luttinger Liquid  $\leftrightarrow$  GHD (emerging fermionic excitations)
- Building and probing quantum field theories in the lab as emergent quantum simulators
- Verify and probe emergent models

Schweigler et al., Nature 545, 323 (2017)      arxiv: 1505.03126  
 Zache et al. PRX, 10, 011020 (2020)  
 Cataldini et al. Phys. Rev. X 12, 041032 (2022)  
 Tajik et al. Nature Physics (2023)



## Quantum Field Simulator Experiments:

Hofferberth et al. Nature 449, 324 (2007)  
 Gring et al., Science 337, 1318 (2012)  
 Kuhnert et al., PRL 110, 090405 (2013)  
 Smith et al., NJP 15, 075011 (2013)  
 Langen et al., Nature Physics 9, 460 (2013)  
 Berrada, et al., Nat. Comm 4, 2077 (2013)  
 Geiger et al., NJP 16 053034 (2014)  
 Van Frank, et al., Nat. Comm 5, 4009 (2014)  
 Langen et al., Science 348, 207 (2015)  
 Steffens, et al., Nature Comm. 6, 7663 (2015)  
 Rauer, et al., PRL 116, 030402(2016)  
 Rauer et al. Science 360, 307 (2018)  
 Erne et al., Nature 563, 225 (2018)  
 Schweigler et al. Nature Physics, 17, 559 (2021)  
 Si-Cong Ji et al. PRL 129, 080402 (2022)  
 Tajik et al. PNAS 120, 21 (2023)

## Atom Chip Experiment

R. Bücke, T. Berrada, S. vanFrank, M. Pigneur, M. Bonneau, F. Borselli,  
M. Maiwöger, TianTian Zhou, Y Kuratnikov, M. Prüfer

F. Cataldini, F. Moller, B. Rauer, Th. Schweigler, M. Tajik, S. Erne, M. Prüfer

## Atom Chip Fabrication

D. Fischer, M. Trinker, M. Schamböck (ATI)  
S. Groth (HD), Israel Bar Joseph (WIS)

## Theory Collaboration

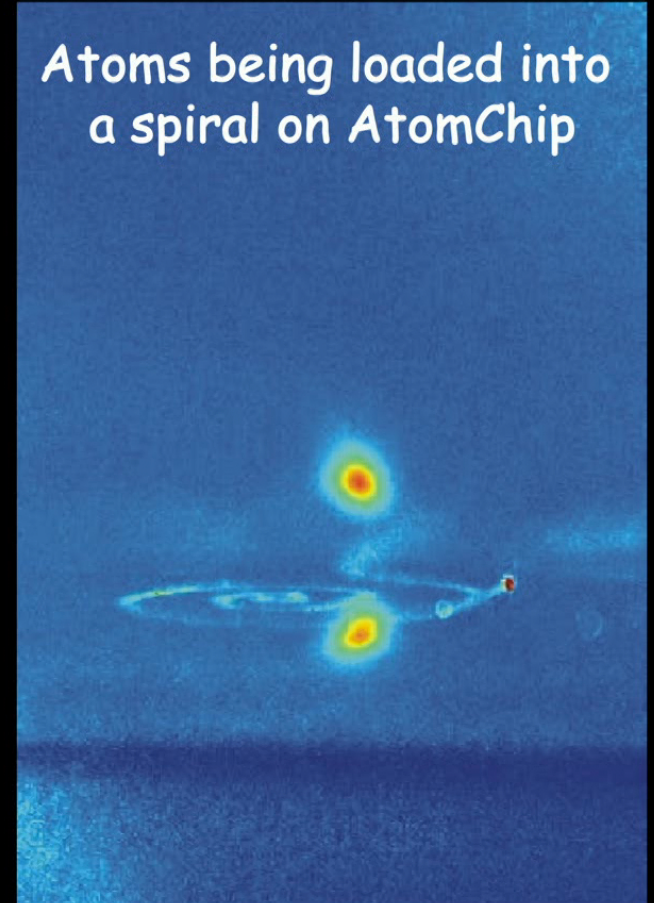
I. Mazets, P. Grisins (ATI)  
J. Grond, U. Hohenester (Univ. Graz)  
T. Calarco, S. Montanegro + ... (Univ. Ulm)  
E. Demler, T. Kitagawa + ... (Harvard->ETHZ)  
J. Berges, T. Gasenzer, V. Kasper, T. Zache + ... (Heidelberg)  
J. Eisert, S. Sotiriadis + ... (FU-Berlin)  
I. Kukuljan (MPQ)  
D. Seles (Flat Iron and NYU)  
P. Zoller, T. Zache, (Innsbruck)

EU: SIQS, QIBEC, AQuS, ...

AT: FWF, CoQuS, Wittgenstein, Stadt Wien

ERC AdG: QuantumRelax + EmQ

Atoms being loaded into  
a spiral on AtomChip



[www.AtomChip.org](http://www.AtomChip.org)