

Title: The S8 tension in cosmology

Speakers: Mike Hudson

Collection: Quantum Spacetime in the Cosmos: From Conception to Reality

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Abstract: In addition to the now-well known "Hubble tension", in recent years a second tension has emerged: the S_8 tension. This is a measure of the homogeneity of the Universe. Specifically, S_8 is defined as $(\Omega_{\text{matter}}/0.3)^{0.5} \sigma_8$ where σ_8 is the standard deviation of the density fluctuation in an $8 h^{-1}$ Mpc radius sphere. As with the Hubble tension, there is disagreement, at greater than 4 σ significance between what is predicted by extrapolating the fluctuations in the Cosmic Microwave Background forward to the present day, and what is measured by multiple probes of the inhomogeneity in the nearby Universe. I will discuss the diverse lines of evidence for the tension, showing it is not restricted to one probe, but is seen in weak gravitational lensing, peculiar velocities and redshift-space distortions and cluster abundances. I will conclude by discussing prospects for future measurements.

Zoom Link: <https://pitp.zoom.us/j/99946149565?pwd=M2puMy9nSEtBZTg1MnRmSIIHeUE0UT09>

THE S_8 TENSION

MIKE HUDSON



UNIVERSITY OF
WATERLOO

WATERLOO CENTRE FOR
ASTROPHYSICS 

OUTLINE

- What is S_8 ?
- Ways to measure S_8
 - CMB
 - Weak lensing
 - Peculiar velocities and redshift-space distortions
 - Cluster abundances
- Solutions?

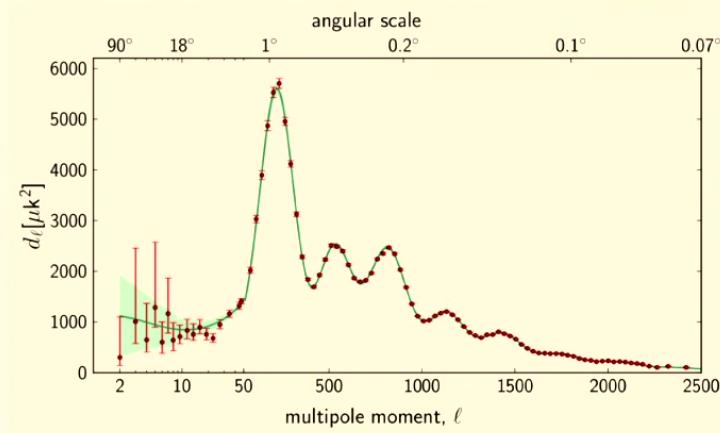
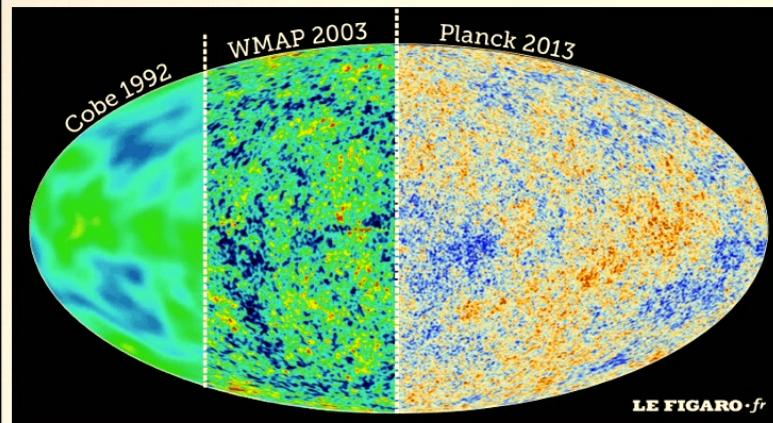
WHAT IS S_8 ?

- A measure of how *inhomogeneous* the Universe is.
- $\delta(\mathbf{r}) = \frac{\rho_m(\mathbf{r}) - \bar{\rho}_m}{\bar{\rho}_m}$
- Average δ over an 8 Mpc/h radius sphere
- σ_8 is the r.m.s. of such spheres measured (ideally) over the whole Universe
- $S_8 \equiv \left(\frac{\Omega_m}{0.3} \right)^{0.5}$ σ_8 is a combination of cosmological parameters close to the degeneracy "bananas" of different methods, esp. weak lensing.

WHAT IS S_8 ?

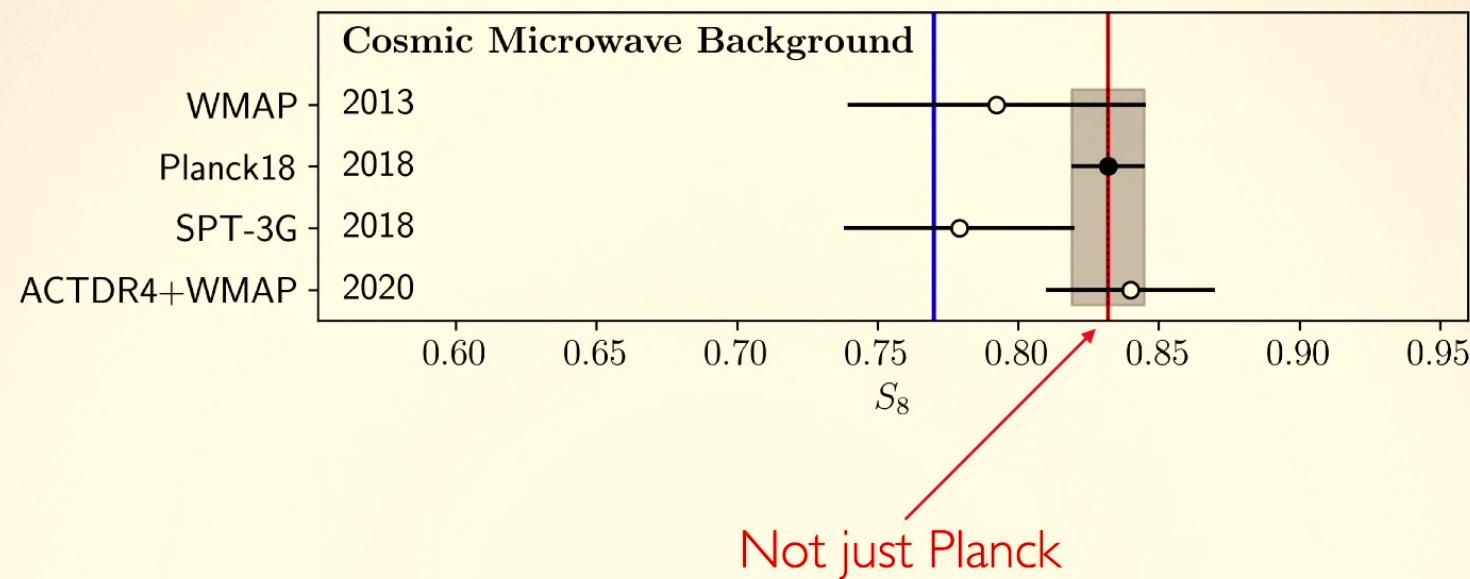
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- $S_8 \equiv \left(\frac{\Omega_m}{0.3} \right)^{0.5}$ σ_8 is a combination of cosmological parameters close to the degeneracy "bananas" of different methods, esp. weak lensing.
- By convention, extrapolated to redshift 0 assuming LCDM.

CMB



Fit the cosmological parameters at $z \sim 1100$
extrapolate to $z \sim 0$ assuming LCDM and linear perturbation theory

CMB



COSMIC SHEAR

Correlations between the shapes of background galaxies (that are close to each other on the sky) due to foreground mass

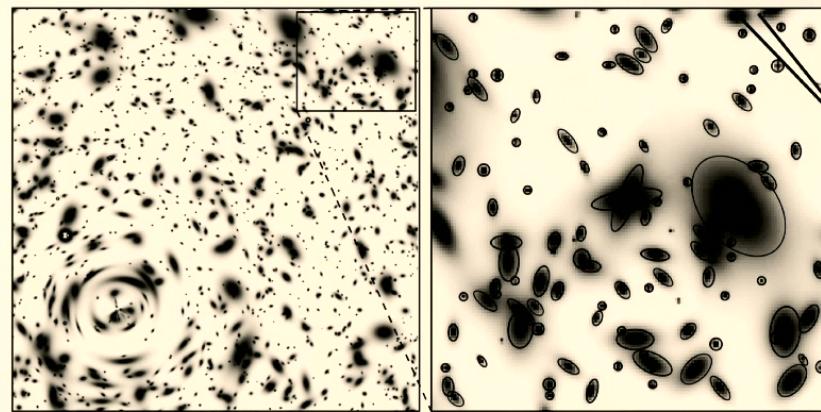
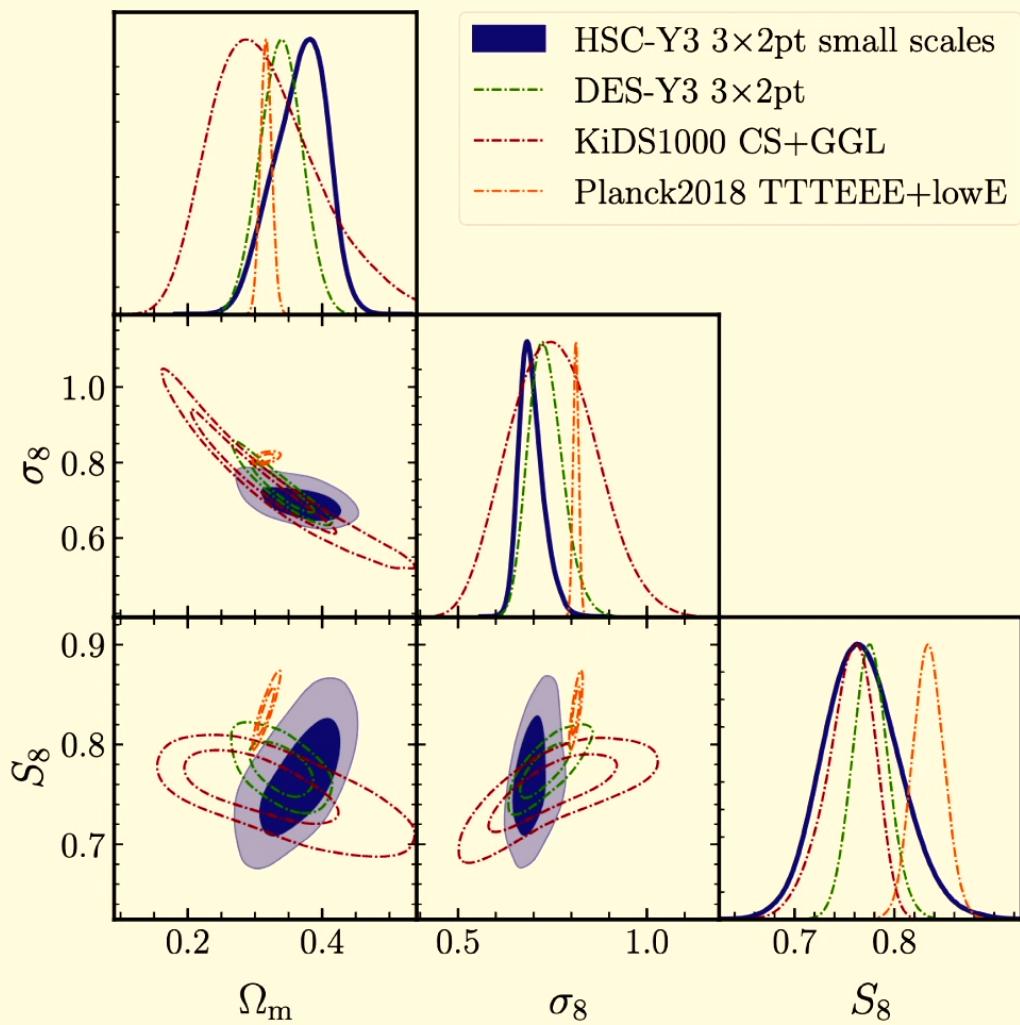


Image credit: Mellier 99

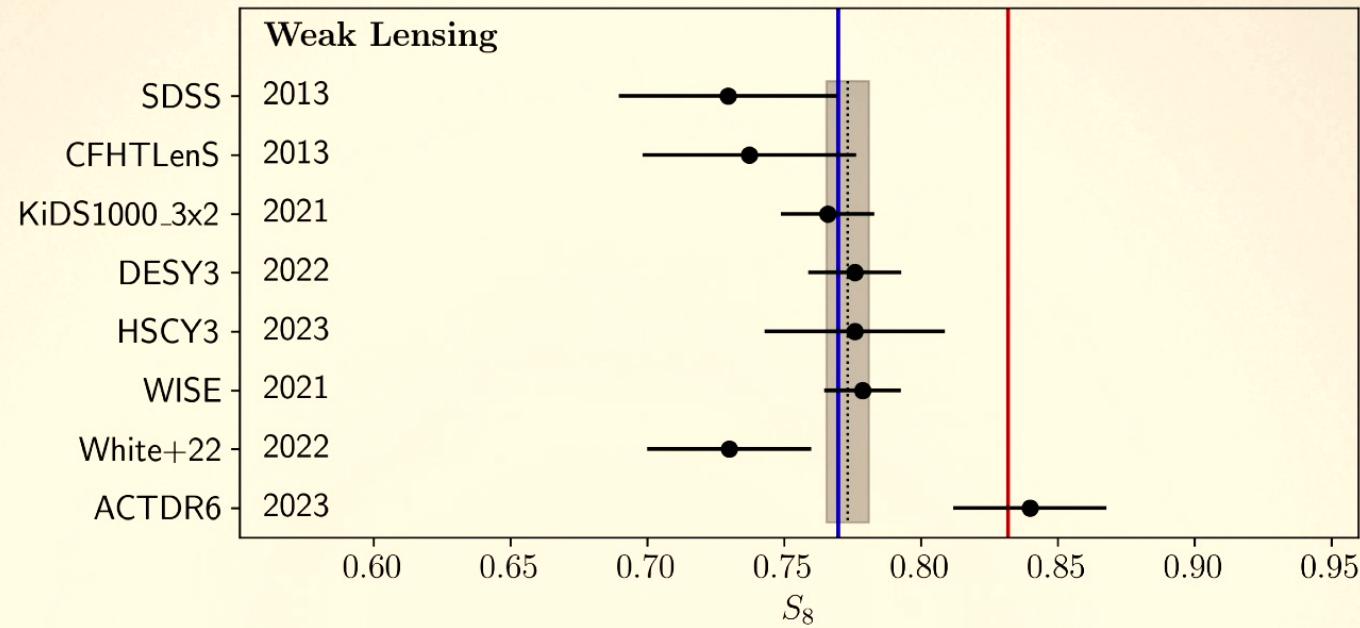
Technically challenging:

cosmic shear distortion ~ 0.001

atmospheric distortion ~ 0.1

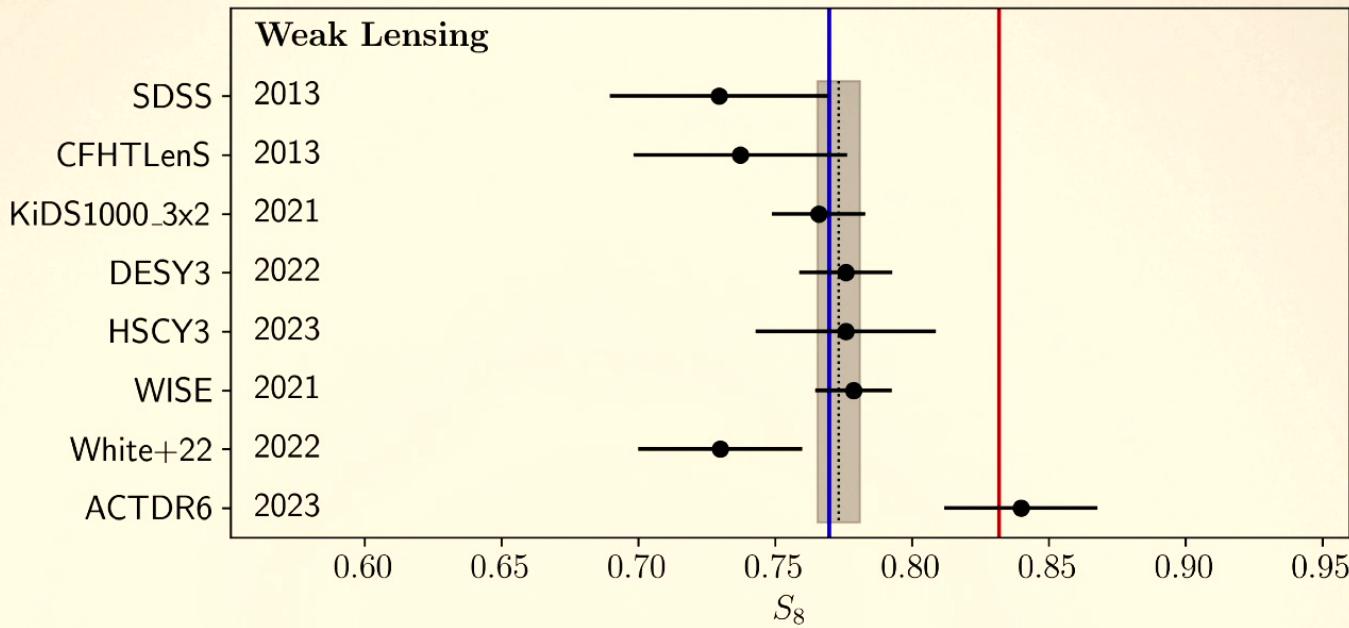


Weak lensing S_8 measurements since 2010



Galaxy lensing

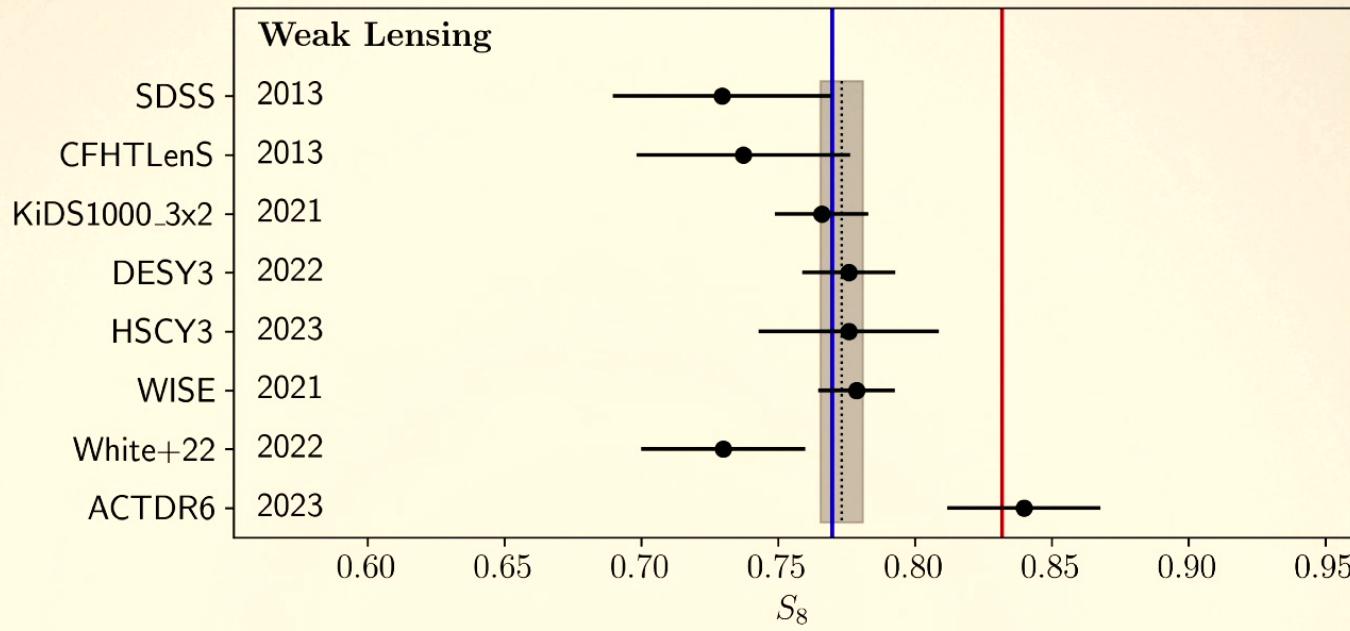
Weak lensing S_8 measurements since 2010



Galaxy lensing

CMB lensing

Weak lensing S_8 measurements since 2010



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- What is S_8 ?
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 - **Peculiar velocities and redshift-space distortions**
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MEASURING PECULIAR VELOCITIES

$$v \sim cz - H_0 r$$

1. Direct distance estimates

- cz is easy to measure
- $H_0 r$ is difficult. Need a standard candle or rod:
 - Supernovae (5-10%), Tully-Fisher (20%), Fundamental Plane (20%)

sparse and noisy, only works at low $z \lesssim 0.1$

2. Statistically, via "redshift-space distortions": cosmic variance limited

3. Kinetic Sunyaev-Zeldovich effect : very weak signal, but exciting prospects

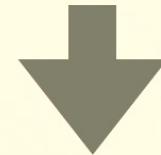
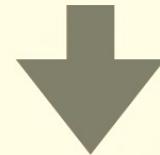
PECULIAR VELOCITIES AND GRAVITY

$$\rho_m(\mathbf{r}) \rightarrow \mathbf{a}(\mathbf{r}) = G \int d^3\mathbf{r}' \rho_m(\mathbf{r}') \frac{(\mathbf{r}' - \mathbf{r})}{|\mathbf{r}' - \mathbf{r}|^3}$$

In linear perturbation theory, **peculiar** velocity is proportional to **peculiar** acceleration generated by the **perturbed** density

PECULIAR VELOCITIES AND GRAVITY

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$$\delta_m(\mathbf{r}) = \frac{\rho_m(\mathbf{r}) - \overline{\rho_m}}{\overline{\rho_m}} \rightarrow \mathbf{v}(\mathbf{r}) = \frac{f H_0}{4\pi} \int d^3\mathbf{r}' \delta_m(\mathbf{r}') \frac{(\mathbf{r}' - \mathbf{r})}{|\mathbf{r}' - \mathbf{r}|^3}$$

Lifshitz 1946, Bonner 1957, Doroshkevich and Zel'dovich 1964, Peebles, 1976

$$f \equiv \frac{d \ln D_+}{d \ln a} \simeq \Omega_m^\gamma \quad \Upsilon = 0.55 \text{ in flat } \Lambda \text{CDM}$$

PECULIAR VELOCITIES TEAM



Supranta Boruah
Waterloo → Arizona



Guilhem Lavaux
Paris



Amber Hollinger
Waterloo → Technion

PECULIAR VELOCITY COMPARISONS

Observed
peculiar velocity data

Predicted peculiar velocity
from the galaxy density field and
linear perturbation theory

$$\mathbf{v}(\mathbf{r}) = \frac{\beta}{b} \frac{f H_0}{4\pi} \int_0^{R_{\max}} d^3 \mathbf{r}' \delta_g(\mathbf{r}') \frac{(\mathbf{r}' - \mathbf{r})}{|\mathbf{r}' - \mathbf{r}|^3} + \mathbf{V}_{\text{ext}}$$

$$v(\mathbf{r}) = \frac{\beta}{b} \frac{f(\Omega_m)}{4\pi} H_0 \int_0^{R_{\max}} \delta_g(\mathbf{r}') \frac{(\mathbf{r}' - \mathbf{r})}{|\mathbf{r}' - \mathbf{r}|^3} d^3 r' + V_{\text{ext}}$$

$$\delta_g = b\delta_m$$

$$\sigma_{8,g} = b\sigma_8$$

$$\beta\sigma_{8,g} = \left(\frac{f}{b}\right) b\sigma_8 = f\sigma_8$$

↓ ↓
 Measurable Measurable
 from fit from δ_g

REDSHIFT-SPACE DISTORTIONS

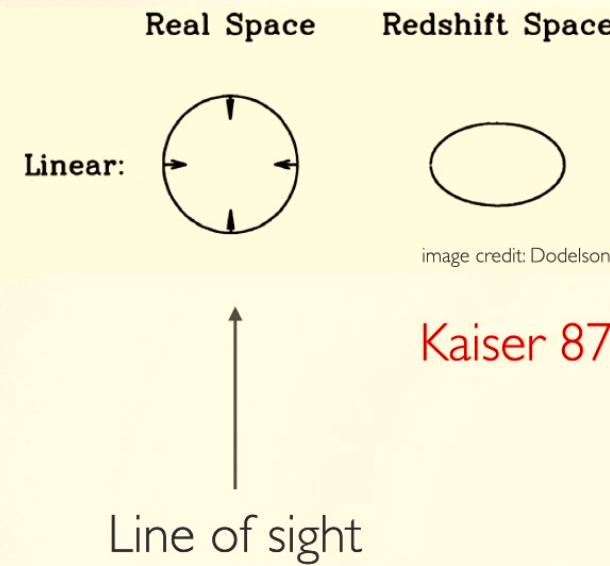
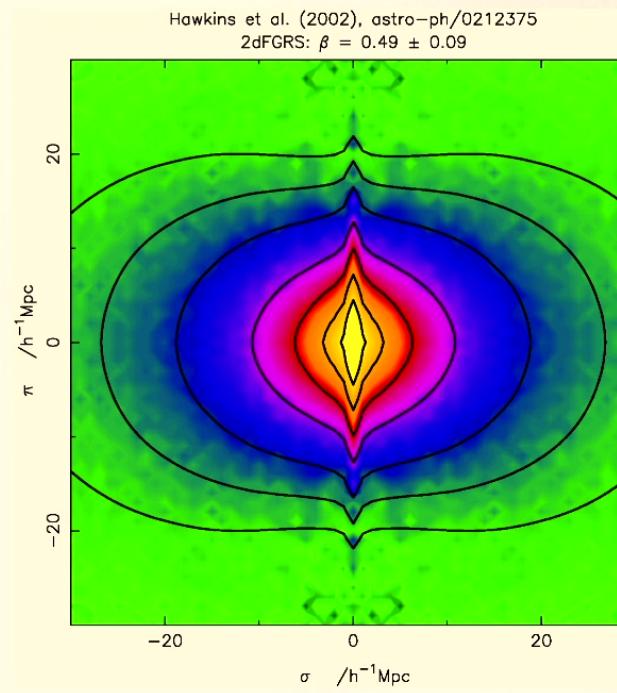
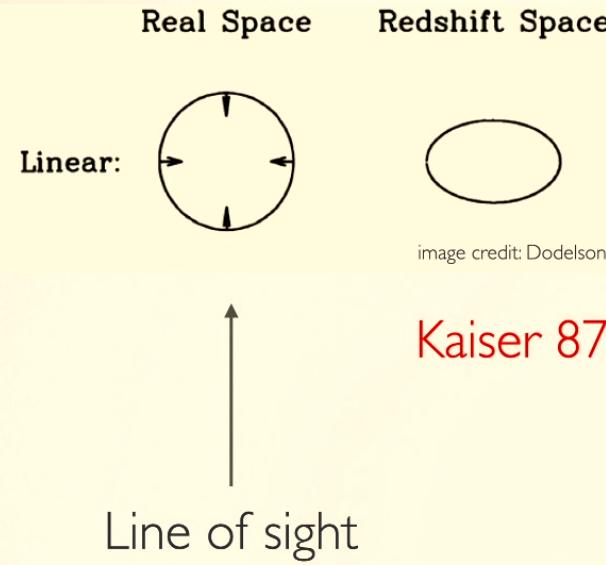
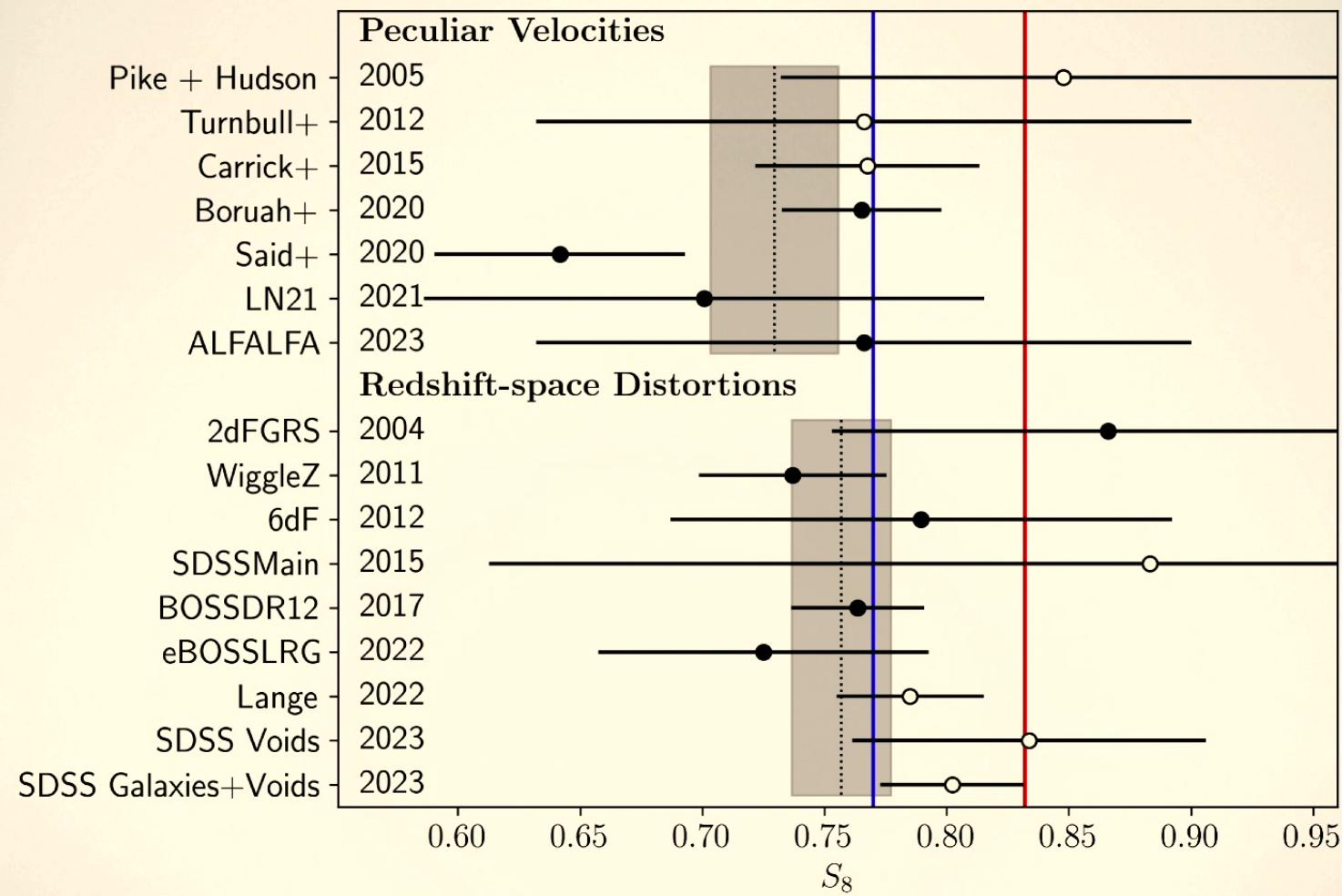
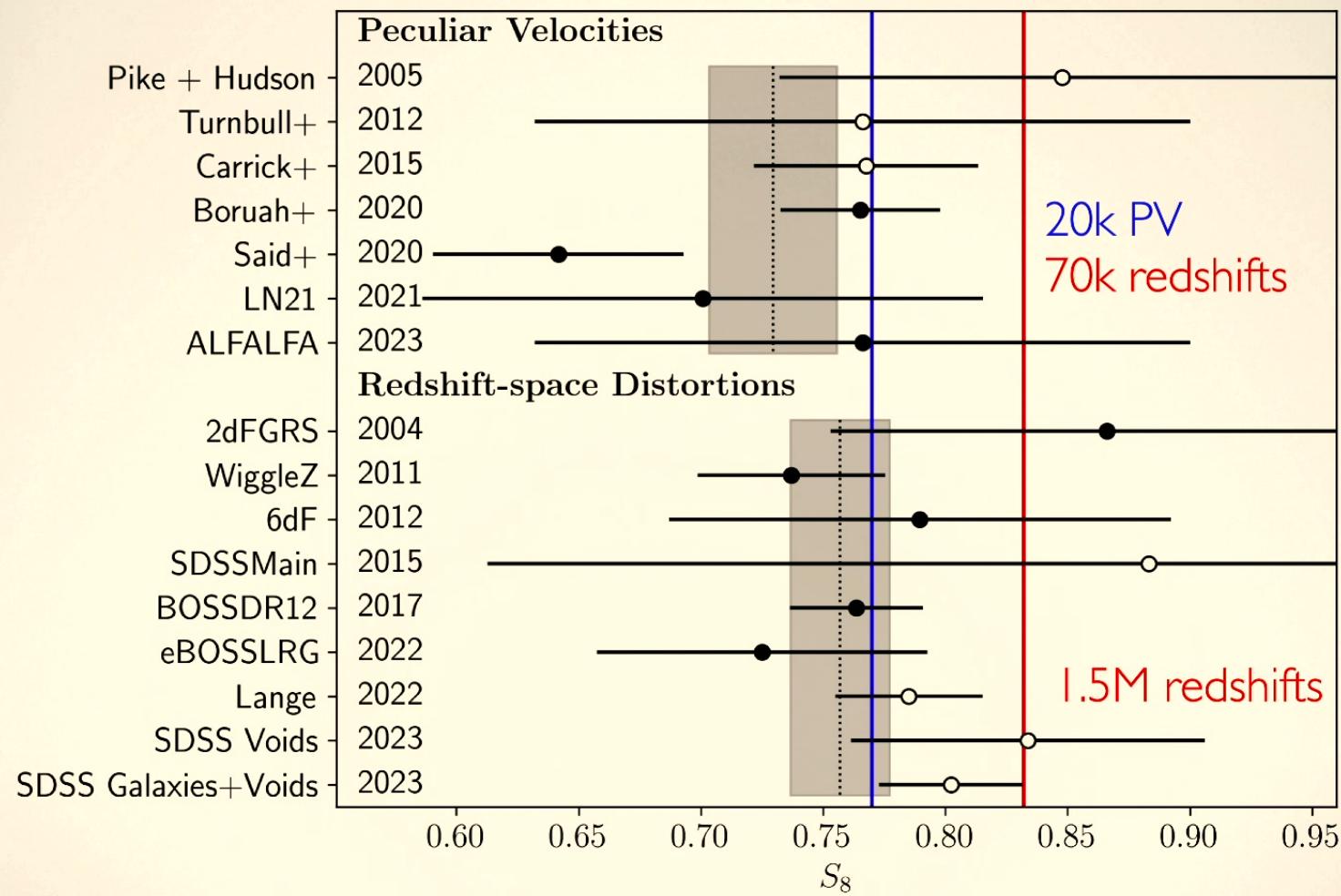


image credit: Dodelson

REDSHIFT-SPACE DISTORTIONS







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CLUSTER ABUNDANCES

- Count clusters of galaxies per unit volume per unit mass
more inhomogeneity : more clusters
- In practice, cannot measure masses of large numbers of clusters.
 - Use a mass proxy and calibrate the proxy, usually with weak lensing

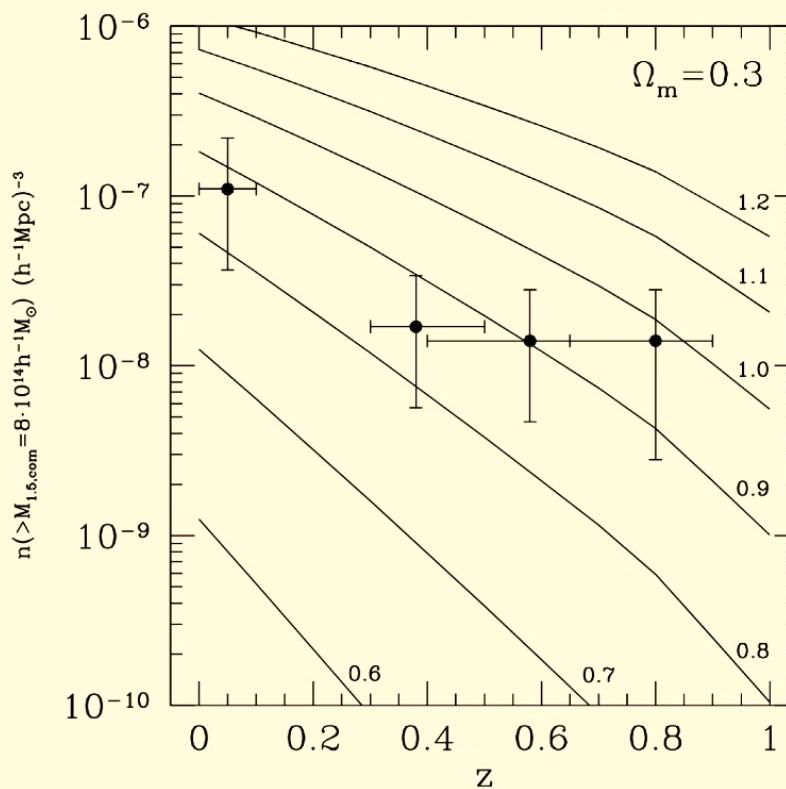
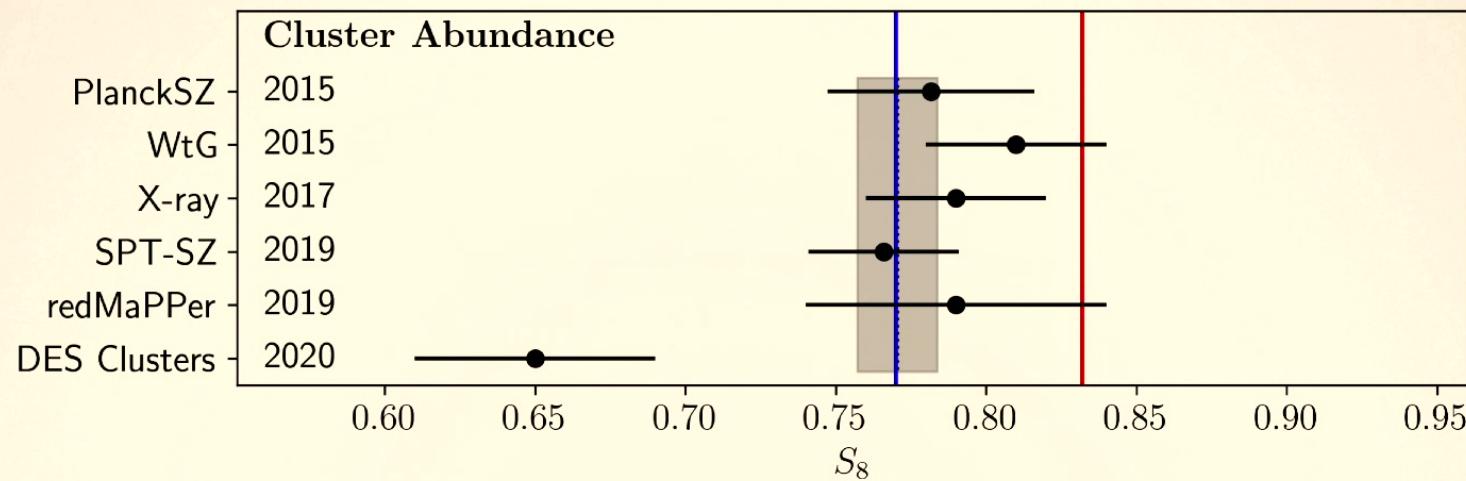
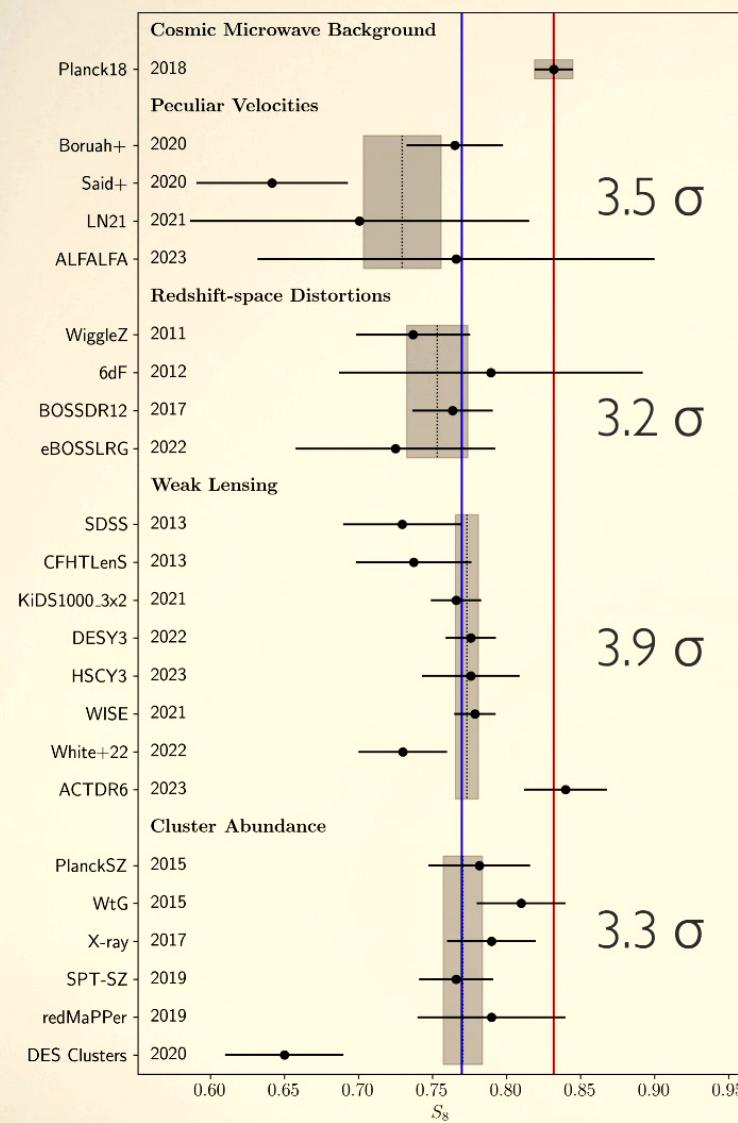


Fig. 1.— Evolution of cluster abundance with redshift, for clusters with mass $M_{1.5,com} \geq 8 \times 10^{14} h^{-1} M_\odot$ (within a comoving radius of $1.5 h^{-1} \text{Mpc}$). Dots with error bars are the data as described in the text. The lines are the predicted number density assuming a flat $\Omega_m = 0.3$ cosmology; each line is labeled with the σ_8 used.

Bahcall and Bode 02

CLUSTER ABUNDANCES





$$S_8 = 0.768 \pm 0.006$$

4.4σ from CMB

THEORETICAL EXPLANATIONS?

H_0 tension

Table B2. Models solving the H_0 tension with R20 within 1σ , 2σ and 3σ considering *Planck* in combination with additional cosmological probes. Details of the combined datasets are discussed in the main text.

Tension $\leq 1\sigma$ ‘excellent models’	Tension $\leq 2\sigma$ ‘good models’	Tension $\leq 3\sigma$ ‘promising models’
Early dark energy [228, 235, 240, 250]	Early dark energy [212, 229, 236, 263] Rock ‘n’ roll [242]	DE in extended parameter spaces [289] Dynamical dark energy [281, 309]
Exponential acoustic dark energy [259]		
Phantom crossing [315]	New early dark energy [247]	Holographic dark energy [350]
Late dark energy transition [317]	Acoustic dark energy [257]	Swampland conjectures [370]
Metastable energy [314]	Dynamical dark energy [309]	MEDE [399]
PEDE [394]	Running vacuum model [332]	Coupled DM—dark radiation [534]
Vacuum metamorphosis [402]	Bulk viscous models [340, 341]	Decaying ultralight scalar [538]
Elaborated vacuum metamorphosis [401, 402]	Holographic dark energy [350]	BD- Λ CDM [852]
Sterile neutrinos [433]	Phantom braneworld DE [378]	Metastable dark energy [314]
Decaying dark matter [481]	PEDE [391, 392]	Self-interacting neutrinos [700]
Neutrino–Majoron interactions [509]	Elaborated vacuum metamorphosis [401]	Dark neutrino interactions [716]
IDE [637, 639, 657, 661]	IDE [659, 670]	IDE [634–636, 653, 656, 663, 669]
DM–photon coupling [685]	Interacting dark radiation [517]	Scalar–tensor gravity [855, 856]
$f(T)$ gravity theory [812]	Decaying dark matter [471, 474]	Galileon gravity [877, 881]
BD- Λ CDM [851]	DM–photon coupling [686]	Nonlocal gravity [886]
Über-gravity [59]	Self-interacting sterile neutrinos [711]	Modified recombination [986]
Galileon gravity [875]	$f(T)$ gravity theory [817]	Effective electron rest mass [989]
Unimodular gravity [890]	Über-gravity [871]	Super Λ CDM [1007]
Time varying electron mass [990]	Λ CDM [893]	Axi-Higgs [991]
Λ CDM [995]	Primordial magnetic fields [992]	Self-interacting dark matter [479]
Ginzburg–Landau theory [996]	Early modified gravity [859]	
Lorentzian quintessential inflation [979]	Bianchi type I spacetime [999]	Primordial black holes [545]
Holographic dark energy [351]	$f(T)$ [818]	

Di Valentino et al. 2021, CQGr. 1000 references!

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H₀+S₈ tension

Dissecting the H_0 and S_8 tensions with Planck + BAO + supernova type Ia in multi-parameter cosmologies

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⁴Institute for Particle Physics Phenomenology, Department of Physics, Durham University, Durham DH1 3LE, UK

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⁶Department of Physics, Liaoning Normal University, Dalian, 116029, P. R. China

The mismatch between the locally measured expansion rate of the universe and the one inferred from observations of the cosmic microwave background (CMB) assuming the canonical Λ CDM model has become the new cornerstone of modern cosmology, and many new-physics set ups are rising to the challenge. Comitant with the so-called H_0 problem, there is evidence of a growing tension between the CMB-preferred value and the local determination of the weighted amplitude of matter fluctuations S_8 . It would be appealing and compelling if both the H_0 and S_8 tensions were resolved at once, but as yet none of the proposed new-physics models have done so to a satisfactory degree. Herein, we adopt a systematic approach to investigate the possible interconnection among the free parameters in several classes of models that typify the main theoretical frameworks tackling the tensions on the universe expansion rate and the clustering of matter. Our calculations are carried out using the publicly available Boltzmann solver *CAMB* in combination with the sampler *CosmoMC*. We show that even after combining the leading classes of models sampling modifications of both the early and late-time universe a simultaneous solution to the H_0 and S_8 tensions remains elusive.

Anchordoqui et al. 2021, JHEP

CHANGING γ ?

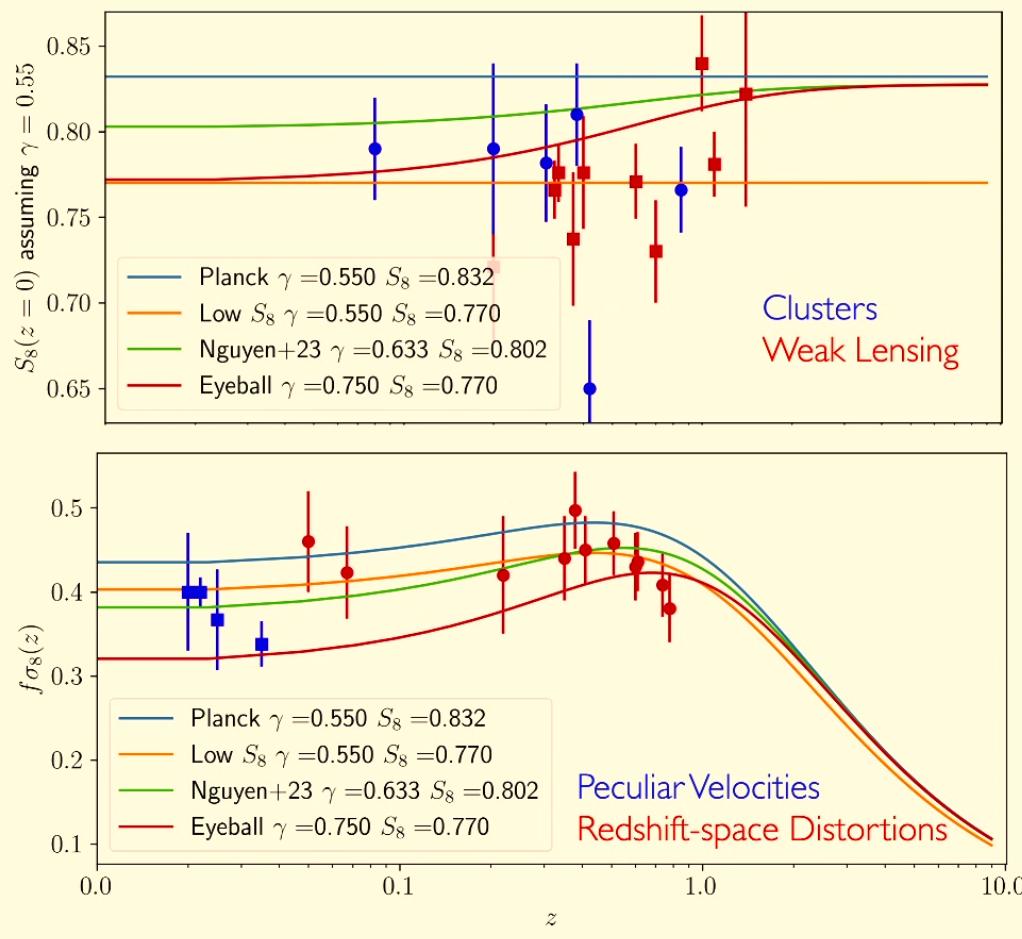
$$\cdot f \equiv \frac{d \ln D_+}{d \ln a} \simeq \Omega_m^\gamma$$

- LCDM: $\gamma = 0.55$... but modified gravity theories predict different γ .
- Nesseris & Perivolaropoulos (2008), di Porto & Amendola (2008), MH & Turnbull (2012), Samushia et al. (2013, 2014), Rapetti et al (2013), Beutler et al. (2014), Mantz et al (2015), Said et al. (2020)
- Nguyen, Huterer, Wen (2023) find $\gamma = 0.633 \pm 0.025$, 3.7σ different from LCDM.

Test by looking at redshift dependence,

comparing S8 from lensing with $f\sigma_8$ from peculiar velocities

REDSHIFT DEPENDENCE?



SCALE DEPENDENCE?

Another possibility is to look for a possible dependence on the comoving scales probed by each experiment

Weak lensing → Clusters → Peculiar velocities → RSD

UPCOMING SURVEYS/ MISSIONS

Weak Lensing

- **UNIONS** (ongoing), **Euclid** (launching in 7 weeks!), **Rubin/LSST**, **Roman**

Redshift-space Distortions

- **DESI**, **Euclid**, **4MOST**

Peculiar Velocities

- **DESI** and **4MOST** (Fundamental Plane, Tully-Fisher), **Rubin/LSST** (Supernovae), **Euclid** (Surface Brightness Fluctuations)

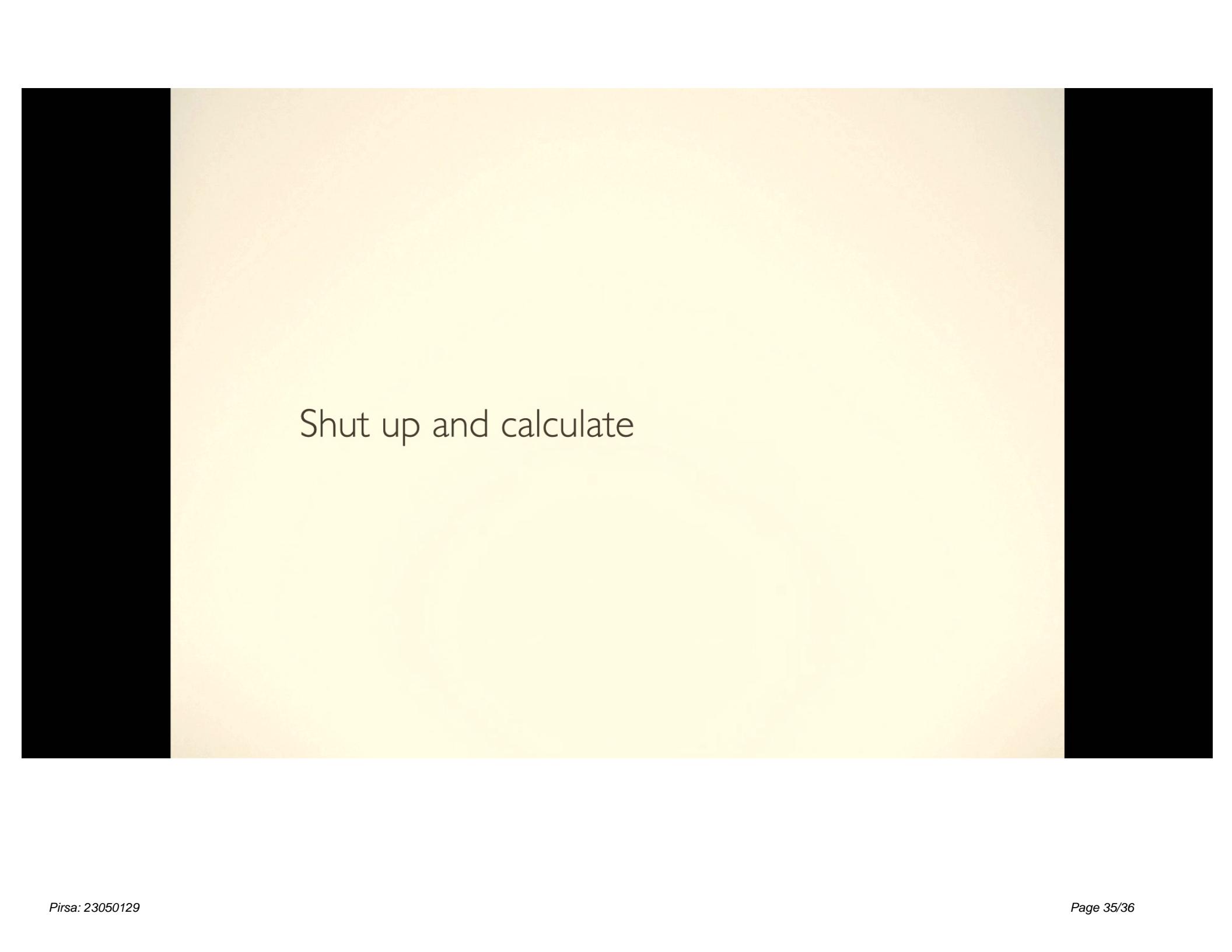
Clusters

- Finding: X-ray (**eROSITA**), Sunyaev-Zel'dovich effect (**ACT/SPT/Simons**), Optical Surveys
- Weighing: **Euclid**, **Rubin/LSST**, **Roman**

ground

or

space



Shut up and calculate



Shut up and ~~calculate~~-measure!