

Title: The H_0 tension and sample variance

Speakers: Will Percival

Collection: Quantum Spacetime in the Cosmos: From Conception to Reality

Date: May 11, 2023 - 11:00 AM

URL: <https://pirsa.org/23050128>

Abstract: Local measurements of the expansion rate of the local universe differ from predictions of simple models fitted to large-scale cosmological measurements, at a statistically significant level. Sample variance (often called cosmic variance) is a key component of errors placed on measurements made from a small data set. For the Hubble constant, which parametrises the expansion rate, the size of the patch of the Universe covered by recent supernovae observations has a radius of 300Mpc. The smaller the patch, the larger the patch-to-patch fluctuations and the larger the error on the measured value of H_0 from sample variance. Using the H_0 measurement from supernovae as an example, I will consider a number of different ways to estimate sample variance using techniques developed for multiple uses, and show that they all approximately agree. The sample variance error on H_0 measurements from the recent Pantheon supernovae sample is $\pm 1 \text{ kms}^{-1}\text{Mpc}^{-1}$, insufficient to explain the Hubble tension in a standard Λ -CDM universe. This will demonstrate methods for comparing variations in expansion rate in the universe and what we mean by saying the universe is expanding (on average), or that galaxies move apart with particular velocities.

Zoom Link: <https://pitp.zoom.us/j/99946149565?pwd=M2puMy9nSEtBZTg1MnRmSlIHeUE0UT09>

The H_0 tension and sample variance

Will Percival

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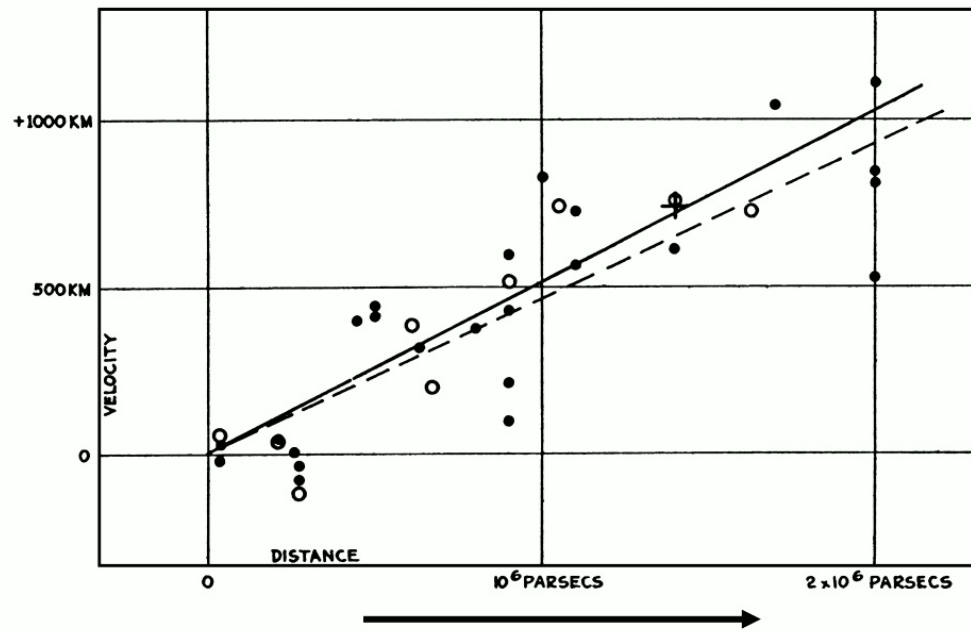
University of Waterloo / Perimeter Institute

Sample variance discussion based
on work with Zhongxu Zhai

arXiv:2207.02373



Long history of incorrect measurements!

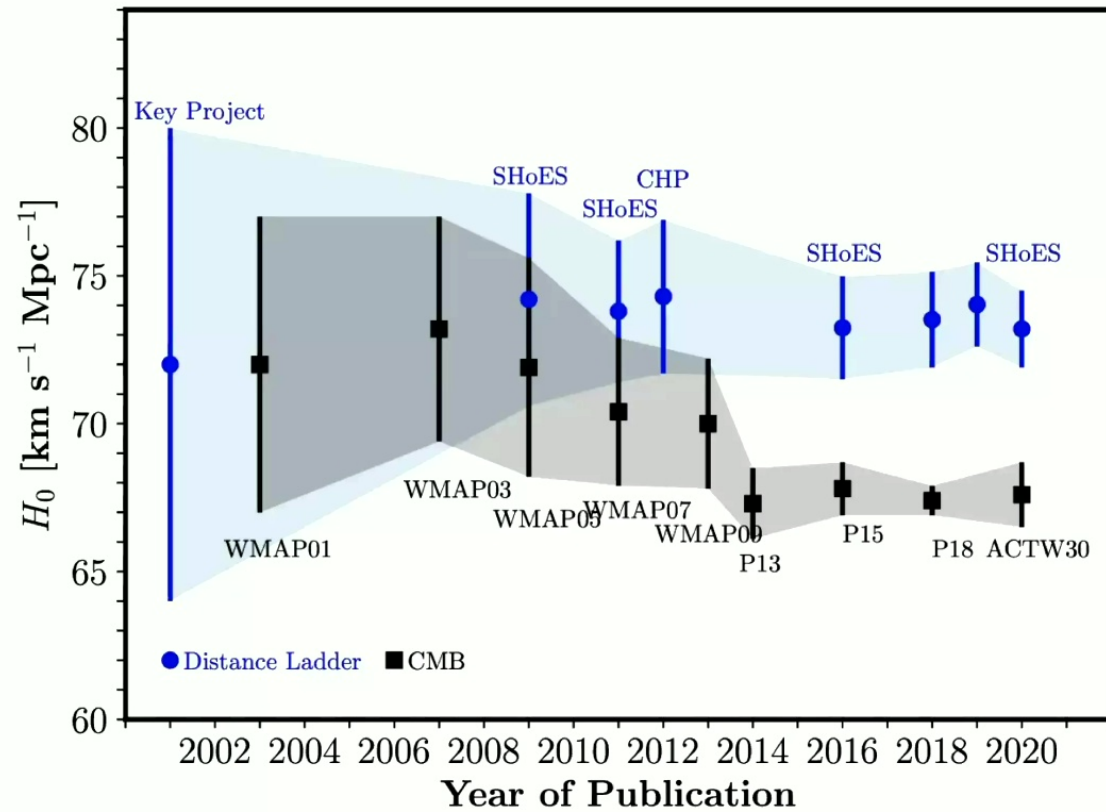


Modern estimates move galaxy distances by a factor 7

$$H_0 = \frac{\text{velocity}}{\text{distance}}$$

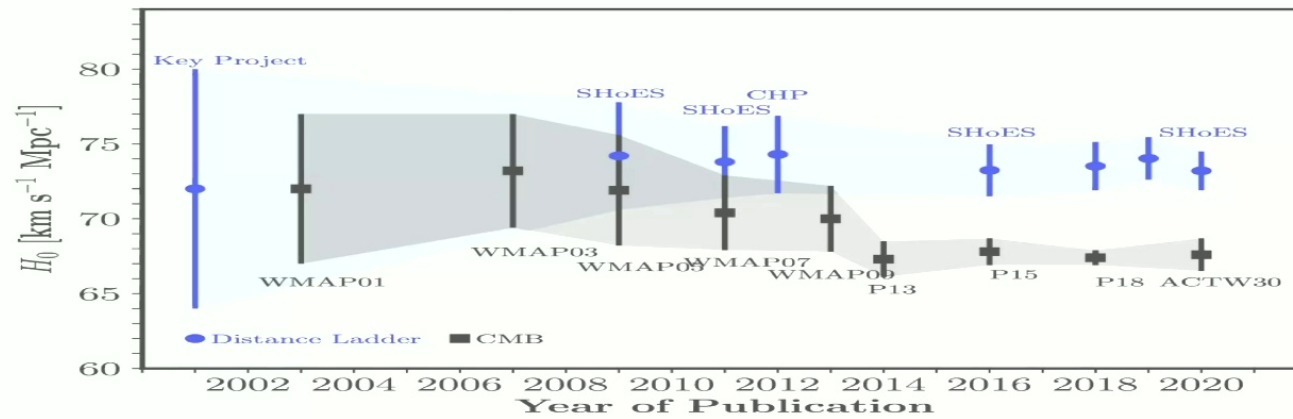
Hubble 1929

The emergence of the “current” Hubble tension

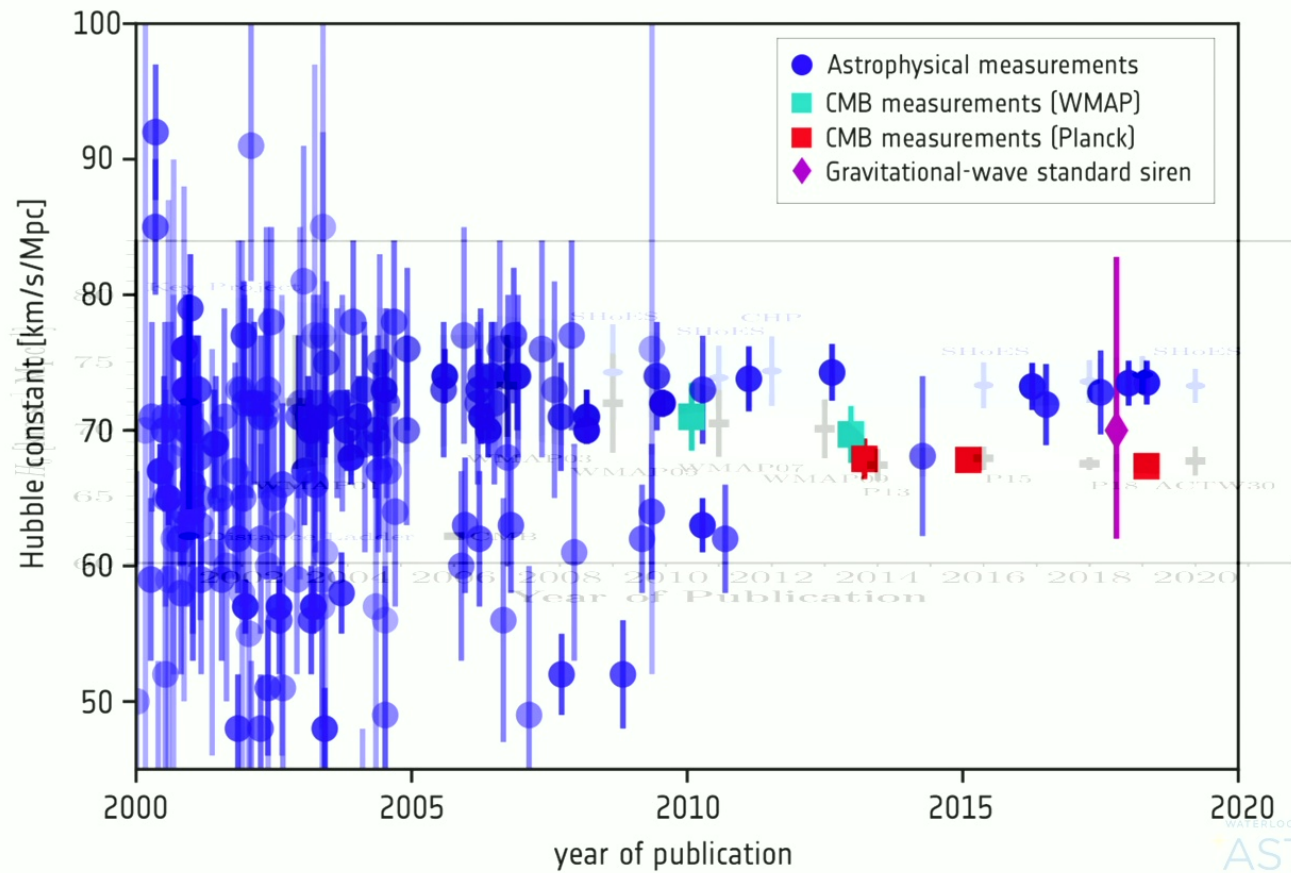


Freedman 2021

Other measurements

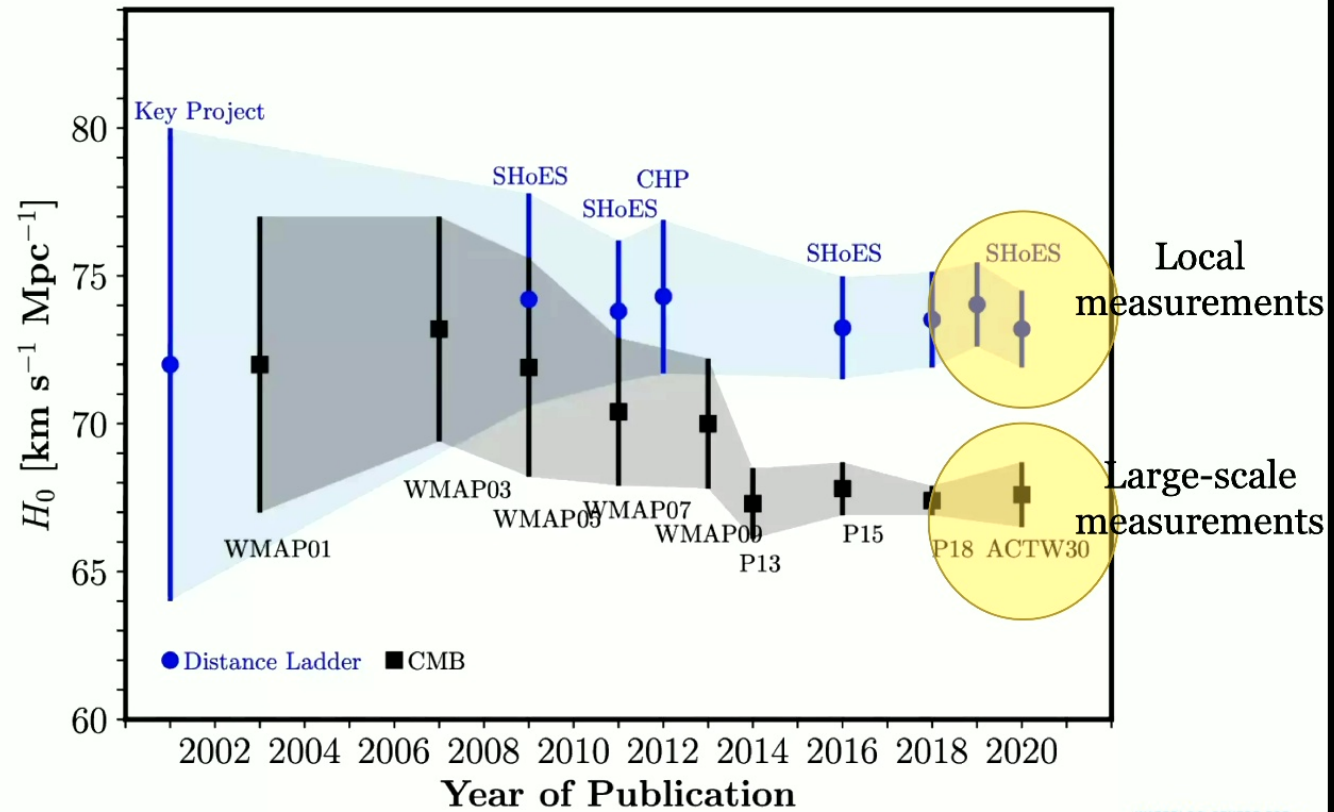


Other measurements



https://www.esa.int/ESA_Multimedia/Images/2018/07/Measurements_of_the_Hubble_constant

The emergence of the “current” Hubble tension



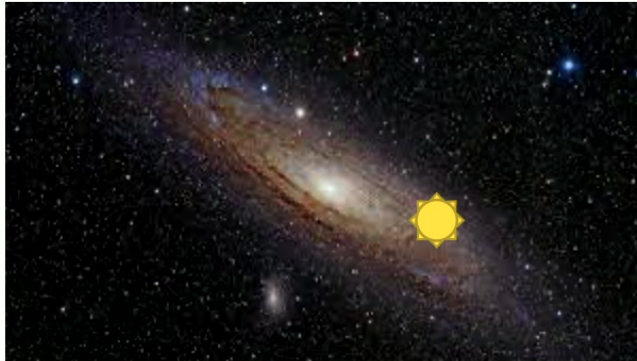
Freedman 2021

H_0 from local measurements

- Start with a local (absolute) calibrator to a galaxy
 - Parallax (sun-earth distance)
 - Detached eclipsing binaries (period)
 - Masers (acceleration)
- Use these to calibrate objects viewed further out
 - Cepheid variables (luminosity-period relation)
 - TRGB observations (universality of Helium flash)
- Use this to calibrate SN1a in cosmological volume (e.g. the Pantheon SN1a sample)
 - Measure H_0

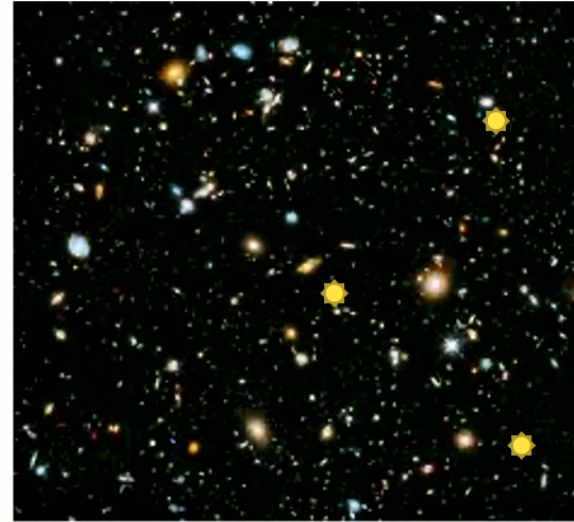
H_0 from local measurements

Example calibrator galaxy



Use calibration to determine M_{sn}
if SN1a goes off

e.g. Riess et al. (20XX); Freedman et al. (20xx)

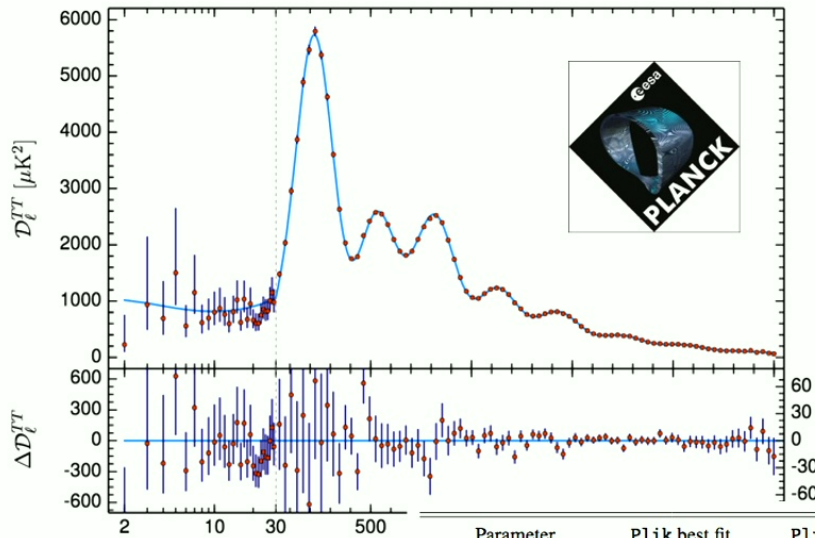


Measure apparent brightness of distant SN
To estimate distances

$$\mu = m - M = 5 \log(d_L / \text{Mpc}) + 25$$

$$d_L \simeq \frac{cz}{H_0} + O(z^2)$$

H₀ from the CMB



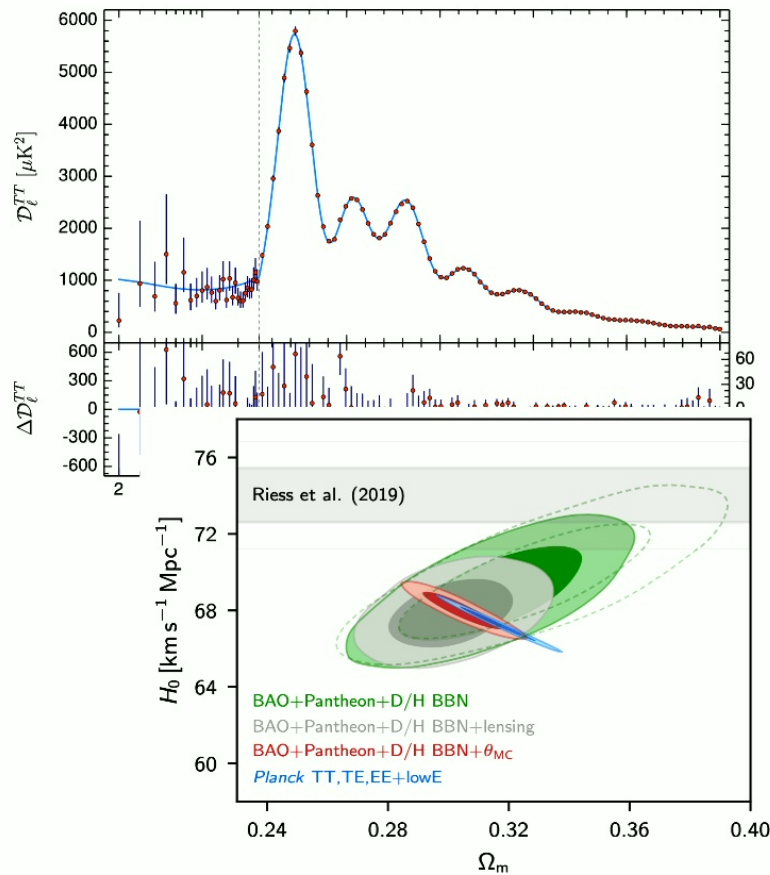
To measure H_0 we need an absolute calibration

For the CMB this is the temperature $T=2.7255\text{K}$

The projected peak positions, together with the theory for their intrinsic position gives H_0

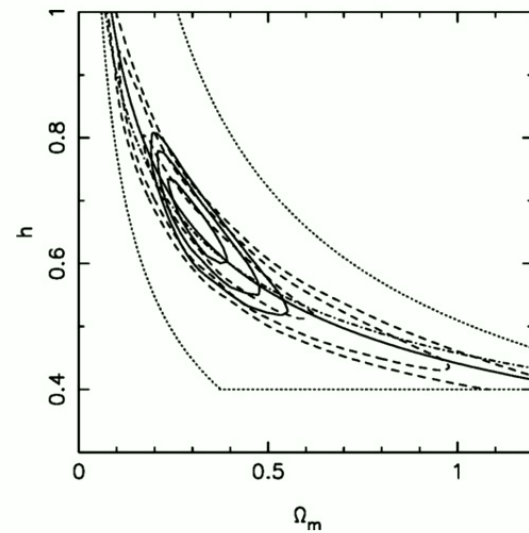
Parameter	Plik best fit	Plik [1]	CamSpec [2]	$([2] - [1])/\sigma_1$	Combined
$\Omega_b h^2$	0.022383	0.02237 ± 0.00015	0.02229 ± 0.00015	-0.5	0.02233 ± 0.00015
$\Omega_c h^2$	0.12011	0.1200 ± 0.0012	0.1197 ± 0.0012	-0.3	0.1198 ± 0.0012
$100\theta_{\text{MC}}$	1.040909	1.04092 ± 0.00031	1.04087 ± 0.00031	-0.2	1.04089 ± 0.00031
τ	0.0543	0.0544 ± 0.0073	$0.0536^{+0.0069}_{-0.0077}$	-0.1	0.0540 ± 0.0074
$\ln(10^{10} A_s)$	3.0448	3.044 ± 0.014	3.041 ± 0.015	-0.3	3.043 ± 0.014
n_s	0.96605	0.9649 ± 0.0042	0.9656 ± 0.0042	+0.2	0.9652 ± 0.0042
$\Omega_m h^2$	0.14314	0.1430 ± 0.0011	0.1426 ± 0.0011	-0.3	0.1428 ± 0.0011
H_0 [km s ⁻¹ Mpc ⁻¹] ...	67.32	67.36 ± 0.54	67.39 ± 0.54	+0.1	67.37 ± 0.54
Ω_m	0.3158	0.3153 ± 0.0073	0.3142 ± 0.0074	-0.2	0.3147 ± 0.0074
Age [Gyr]	13.7971	13.797 ± 0.023	13.805 ± 0.023	+0.4	13.801 ± 0.024
σ_8	0.8120	0.8111 ± 0.0060	0.8091 ± 0.0060	-0.3	0.8101 ± 0.0061
$S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5}$..	0.8331	0.832 ± 0.013	0.828 ± 0.013	-0.3	0.830 ± 0.013
z_{re}	7.68	7.67 ± 0.73	7.61 ± 0.75	-0.1	7.64 ± 0.74
$100\theta_*$	1.041085	1.04110 ± 0.00031	1.04106 ± 0.00031	-0.1	1.04108 ± 0.00031
r_{drag} [Mpc]	147.049	147.09 ± 0.26	147.26 ± 0.28	+0.6	147.18 ± 0.29

H₀ from the CMB



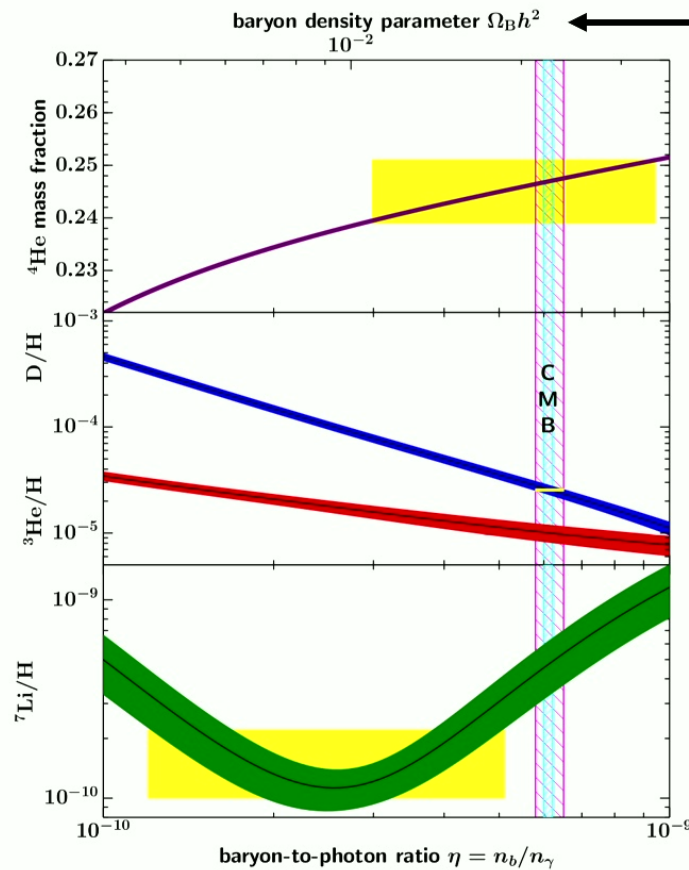
Planck 2018; arXiv:1807.06209

For flat Λ CDM models,
there is a degeneracy
between Ω_m and H_0

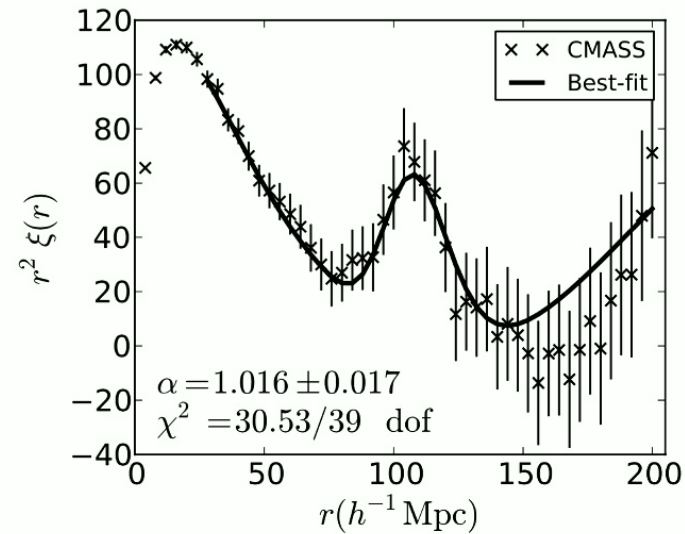


Percival et al 2002; arXiv:0206256

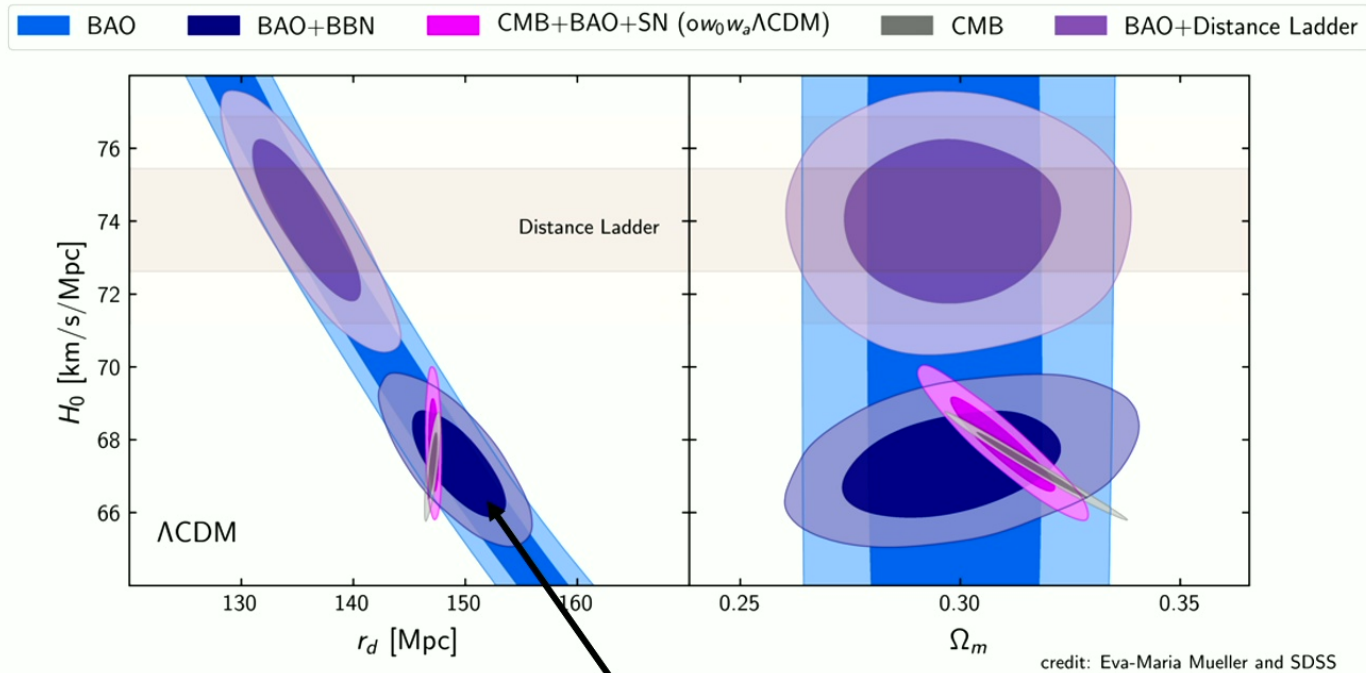
H₀ from BBN + BAO



BAO peak position measured from galaxy surveys tells us the projected position of the sound horizon along and across line of sight and depends on Ω_b , Ω_c , h



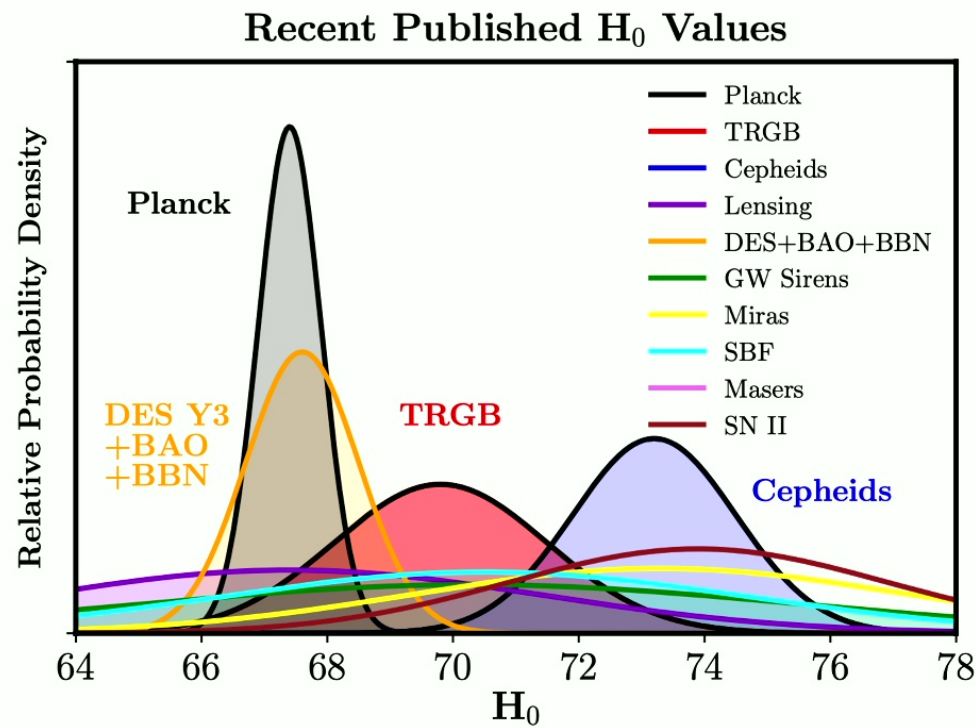
H_0 from BBN + BAO



Alam et al. (2020), arXiv:2007.08991

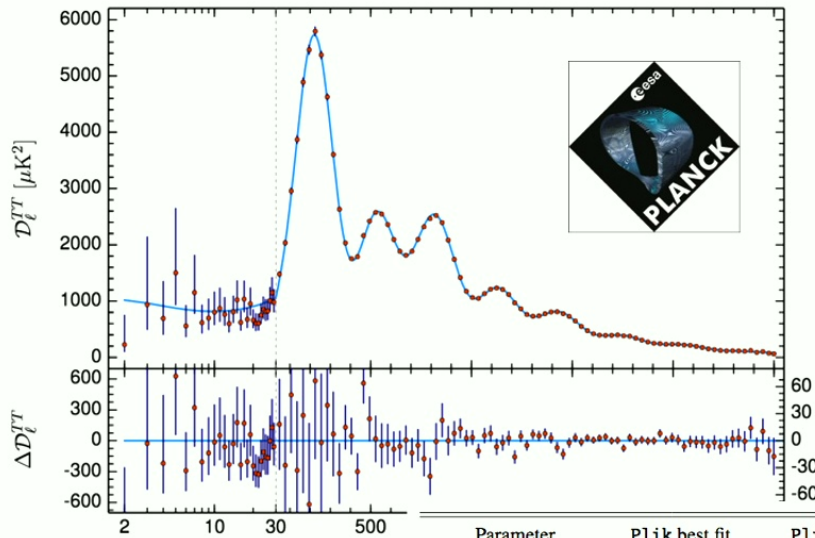
Measurement of H_0
independent of CMB

Recent measurements



Freedman et al. (2021), arXiv:2106.15656

H₀ from the CMB



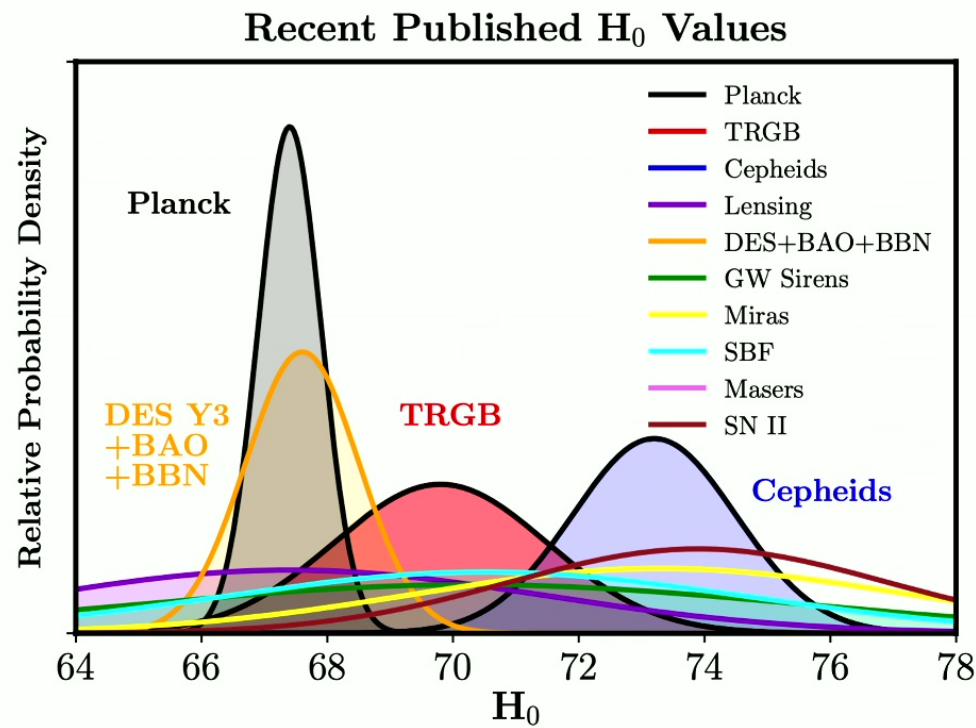
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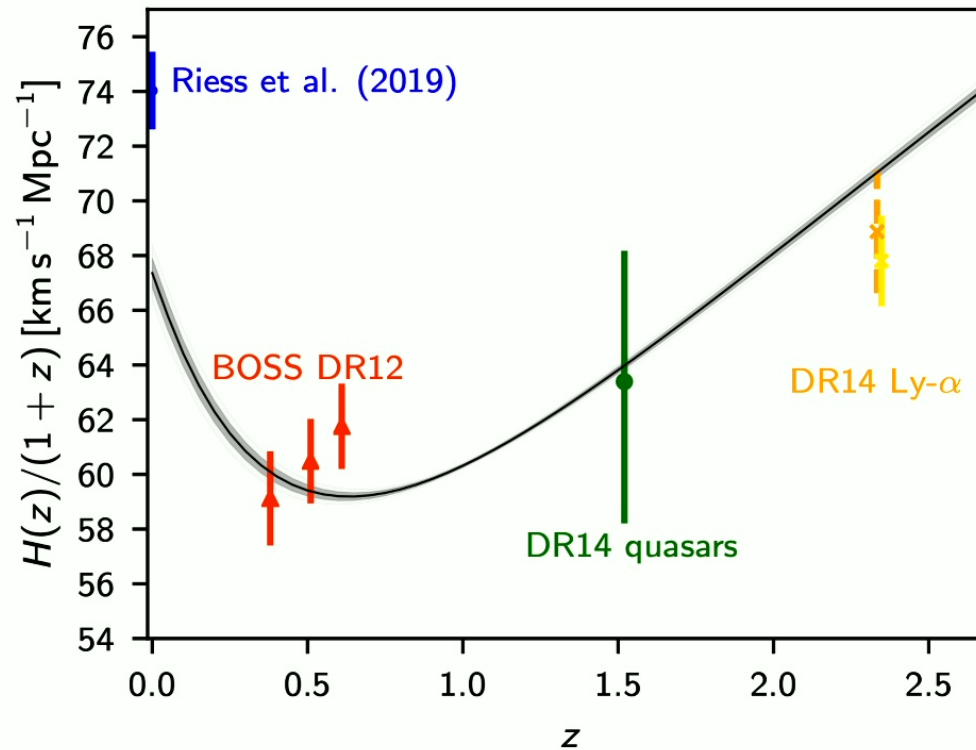
All techniques calibrate distances

- Need an absolute measurement (H_0 is absolute)
 - CMB temperature
 - Earth-sun distance
- Theoretically link these to observed physical quantity
 - BBN, CMB physics, BAO position
 - Parallax, Cepheid period-luminosity relation, universality of SN1a
- Make projected distance observations (with errors)
 - CMB / BAO peak positions
 - Distance ladder up to SN1a brightness observations

Each component could be wrong!

And most have been carefully examined without finding a solution

Difficult to change evolution at low redshifts

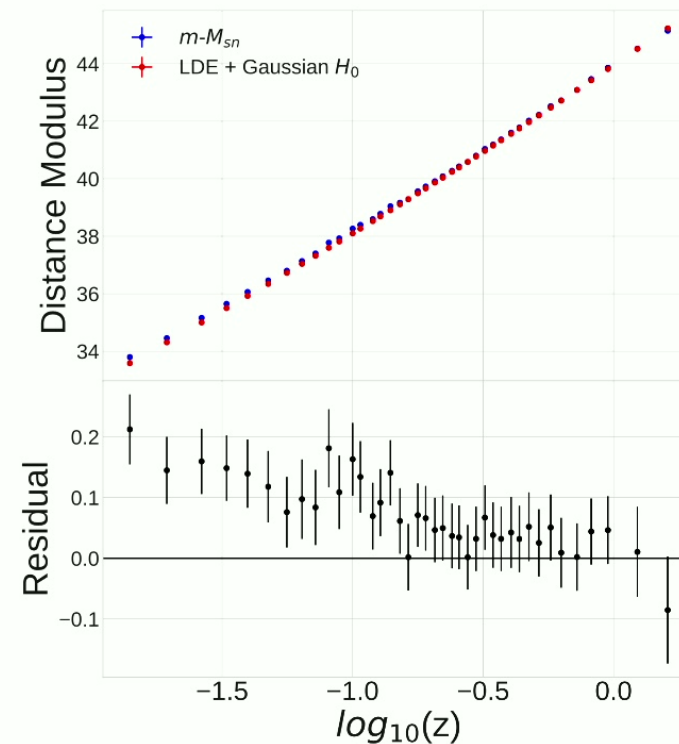


Planck 2018; arXiv:1807.06209

Difficult change evolution at very low redshift

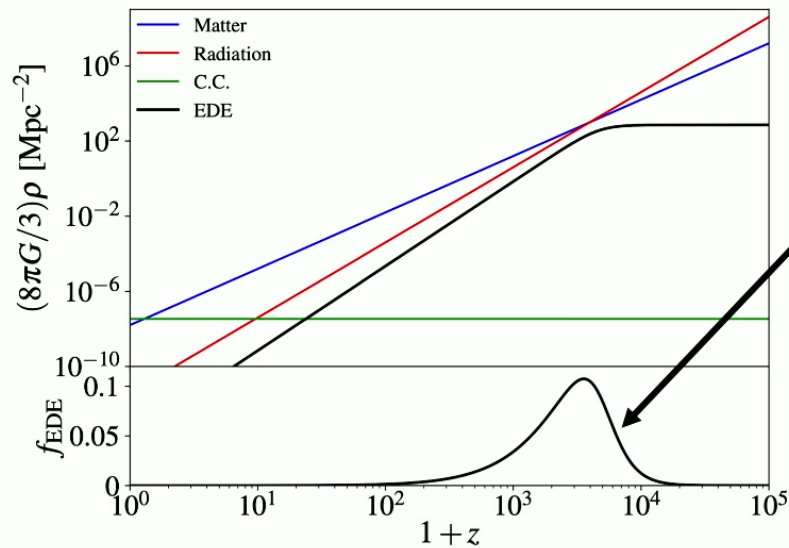
Suppose you add in extra acceleration
at $z < 0.1$ to get a higher H_0

The distance ladder gets messed up
– you're measuring distances from us



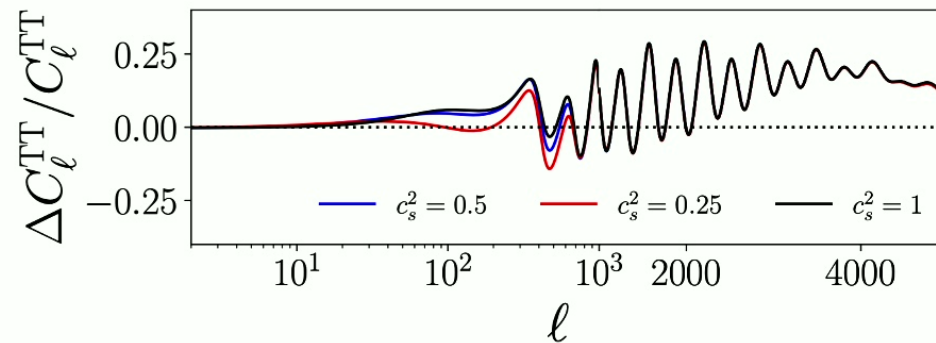
Greene & Cyr-Racine 2022; arXiv:2112.11567

Early Dark Energy



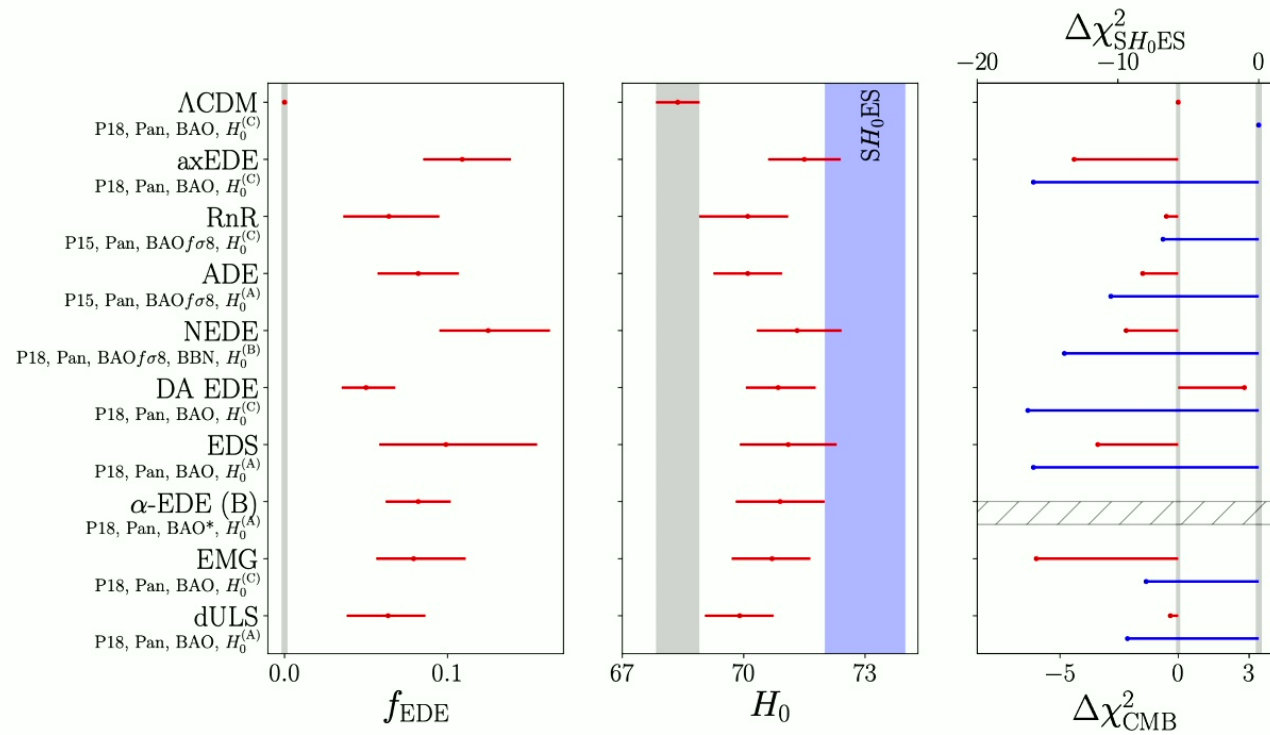
Introduce another period of acceleration after matter-radiation equality, before recombination. Component evolves to different w at later times, stopping acceleration

Extra expansion decreases r_s requiring a larger H_0 to fit the same peak positions



Poulin et al. 2023; arXiv:2302.09032

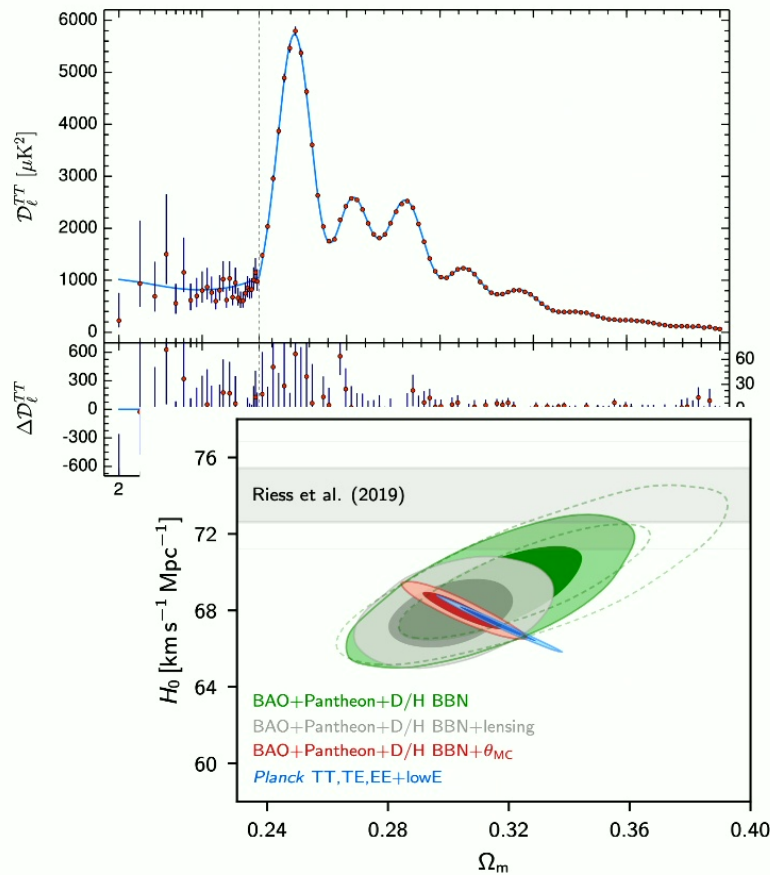
Early Dark Energy



Generic prediction of EDE model is to increase S_8 – see next talk

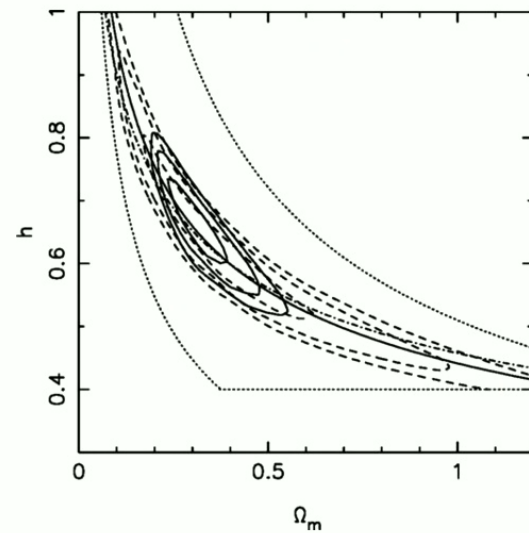
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