

Title: Energy transport for thick holographic branes

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Series: Quantum Fields and Strings

Date: May 19, 2023 - 11:00 AM

URL: <https://pirsa.org/23050032>

Abstract: Universal properties of two-dimensional conformal interfaces are encoded by the flux of energy transmitted and reflected during a scattering process.

In this talk, I will develop a method that allows me to extend previous results based on thin-brane holographic models to smooth domain-wall solutions of 3-dimensional gravity.

As an application, I will compute the transmission coefficient of a Janus interface in terms of its deformation parameter.

Zoom link: <https://pitp.zoom.us/j/98684574364?pwd=WGdrQXhRcHRJZUZMYmNObUVZT1ZCZz09>

"ENERGY TRANSPORT FOR THICK HOLOGRAPHIC BRANES" [2212.14058]

- 1) MOTIVATIONS
- 2) 2D ICFT
- 3) THIN BRANE MODEL
- 4) THICK BRANE MODEL
- 5) CONCLUSIONS

- 1)
 - EXTENDED PROBES IN QFT
 - CONDENSED MATTER PHYSICS
 - DYNAMICAL BRANES IN AdS
 - QUANTUM INFORMATION

2)

CFT_L
 (T_L, \bar{T}_L)

CFT_R
 (T_R, \bar{T}_R)

$$T_{tot} = T_L + T_R$$

$$T_{2d} = C_R T_L - C_L T_R$$

$$\langle T_L(z) T_L(w) \rangle = \frac{C_L/2}{(z-w)^4}$$

$$\langle T_L(z) T_R(w) \rangle = \frac{C_{LR}/2}{(z-w)^4}$$

$$CFT_L \otimes \overline{CFT_R}$$

WES [2212.14058]

$$\begin{array}{c|c} \text{CFT}_L & \text{CFT}_R \\ (T_L, \bar{T}_L) & (T_R, \bar{T}_R) \end{array}$$

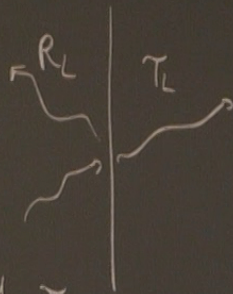
$$\boxed{\text{CFT}_L \otimes \text{CFT}_R}$$

$$T_R$$

$$L-C, T_R$$

$$\langle W \rangle = \frac{C_{LL}/2}{(z-w)^4}$$

$$\langle W \rangle = \frac{C_{RR}/2}{(z-w)^4}$$

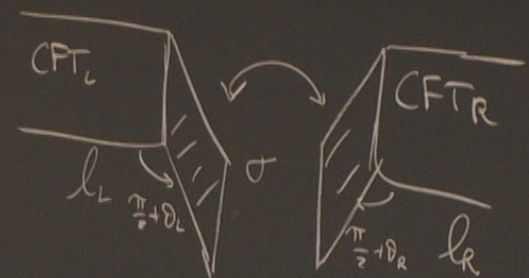


$$R_L = 1 - T_L$$

$$\langle T_L \rangle = \frac{C_{LR}}{C_L}$$

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[Quella et al., 07]
[Meyer et al., '19]

3)



$$S = \frac{1}{16\pi G_N} \int d^3x_L \sqrt{-g_L} \left(R_L + \frac{2}{L^2} \right) + (L \leftrightarrow R)$$

$$- \sigma \int d^2x \sqrt{-\gamma}$$

$$[K_{ij}] = K_{ij}^L - K_{ij}^R$$

ISRAEL MATCHING CONDITIONS

$$\gamma_{ij}^L = \gamma_{ij}^R$$

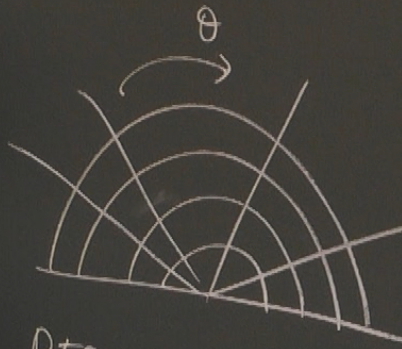
$$[K_{ij}] - [K] \gamma_{ij} = 8\pi G_N \sigma \gamma_{ij}$$

$$\Rightarrow \frac{l_L}{\cos \theta_L} = \frac{l_R}{\cos \theta_R} = \frac{\tan \theta}{2}$$

$$ds^2 = -dt^2 + dr^2 + r^2 d\Omega^2$$

$$z \cos \theta$$

$$z \sin \theta$$



$$AdS_2(z, t)$$

PERTURBATION

FG COORDINATES

$$ds^2 = \frac{l^2}{z^2} \left(d\tilde{s}^2 + \left(g_{\alpha\beta}^{(2)} + \frac{g_{\alpha\beta}^{(2)}}{l^2} g^{(2)} + \frac{g^{(4)}}{4l^2} g_{\alpha\beta}^{(4)} \right) dW^\alpha dW^\beta \right)$$

$$W^\pm = u \pm t$$

$$g^{(2)} = 4l G_N \langle T_{\alpha\beta} \rangle$$

$$g^{(4)} = g^{(2)} (g^{(2)})^{-1} g^{(2)}$$

$$\begin{aligned} dW^\alpha dW^\beta \langle T_{\alpha\beta}^L \rangle &= \mathcal{E} \left[e^{i\omega(t_L - u_L)} d(t_L - u_L)^2 \right. \\ &\quad \left. + R_L e^{i\omega(t_L + u_L)} d(t_L + u_L)^2 \right] \\ \langle T_{\alpha\beta}^R \rangle dW^\alpha dW^\beta &= \mathcal{E} \left[T_L e^{i\omega(t_R - u_R)} d(t_R - u_R)^2 \right] \end{aligned}$$

• IMPOSE ISRAL MATCHING

• IMPOSE NO-OUTGOING WAVE CONDITIONS (IN THE IR)

$$\hat{K}_{ij} = K_{ij} - K \gamma_{ij}$$

EMPTY ADS: $\sigma = 0$
 $l_L = l_R \Rightarrow T_L = 1$

$$T_L = \frac{2}{l_L} \left(\frac{1}{l_L} + \frac{1}{l_R} + 8\pi G_N \sigma \right)^{-1}$$

$$\Rightarrow \frac{C_R}{C_L + C_R} \leq T_L \leq \min\left(1, \frac{C_R}{C_L}\right)$$

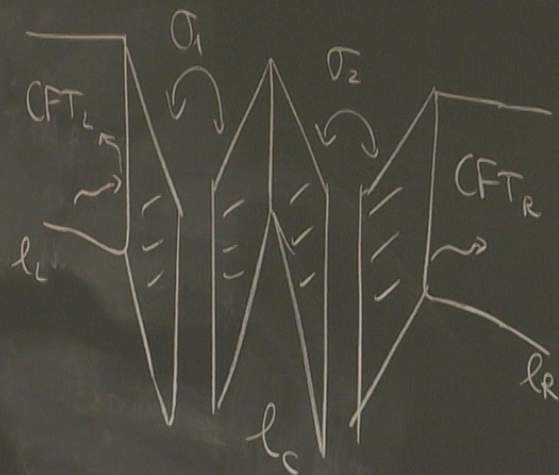
$$\left| \frac{1}{l_L} - \frac{1}{l_R} \right| \leq 8\pi G_N \sigma \leq \frac{1}{l_L} + \frac{1}{l_R}$$

ANEC: $0 \leq T_L \leq \min\left(1, \frac{C_R}{C_L}\right)$

$$\frac{C_R}{C_L} \rightarrow 0$$

$$\log g \sim \sigma$$

"ENERGY TRANSPORT FOR THICK HOLOGRAPHIC BRANES" [2212.14058]



$$\tau_L = \frac{2}{l_L} \left(\frac{1}{l_L} + \frac{1}{l_R} + 8\pi G_N (\sigma_1 + \sigma_2) \right)^{-1}$$

$$\log \times (\sigma_1 + \sigma_2)$$

N BRANES

$$\tau_L = \frac{2}{l_L} \left(\frac{1}{l_L} + \frac{1}{l_R} + 8\pi G_N \sum_i \sigma_i \right)^{-1}$$

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$$\left(G_N (\sigma_1 + \sigma_2) \right)^{-1}$$

$$\left(\sum_i \sigma_i \right)^{-1}$$

4) THICK BRANE MODEL

EINSTEIN GRAVITY + DILATION

$$S = \frac{1}{16\pi G_N} \int d^{m+1}x \sqrt{-g} \left(R - \partial_\mu \phi \partial^\mu \phi - 2V(\phi) \right)$$

CONTINUOUS GEOMETRY

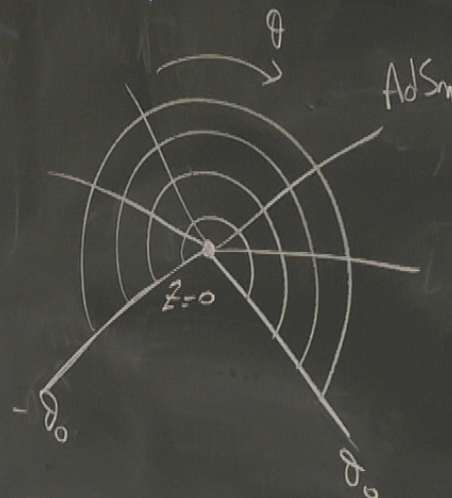
$$ds^2 = a^2(\theta) (d\theta^2 + \gamma_{\alpha\beta} dx^\alpha dx^\beta)$$

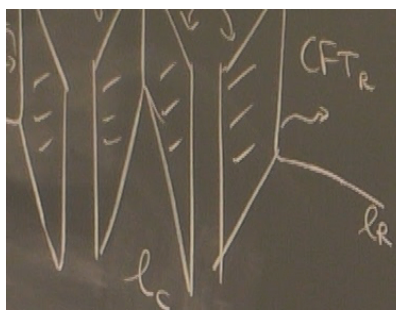
$$\phi = \phi(\theta)$$

JANUS AdS_3

$AdS_3 \times S^3 \times M_4$

TYPE IIB SUPER





$$\tau_L = \frac{2}{l_L} \left(\frac{1}{l_L} + \frac{1}{l_R} + 8\pi G_N (\tau_1 + \tau_2) \right)^{-1}$$

$$l_{gg} \propto (\tau_1 + \tau_2)$$

N BRANES

$$\tau_L = \frac{2}{l_L} \left(\frac{1}{l_L} + \frac{1}{l_R} + 8\pi G_N \sum_i \tau_i \right)^{-1}$$

$$\sum_i \tau_i \rightarrow \int_a^b dy \frac{d\tau}{dy}$$

4) THICK BRANE MODEL

EINSTEIN GRAVITY + DILATON

$$S = \frac{1}{16\pi G_N} \int d^{n+1}x \sqrt{-g} \left(R - \partial_\mu \phi \partial^\mu \phi - 2V(\phi) \right)$$

CONTINUOUS GEOMETRY

$$ds^2 = a^2(\theta) (d\theta^2 + \gamma_{\alpha\beta} dx^\alpha dx^\beta)$$

$$\phi = \phi(\theta)$$

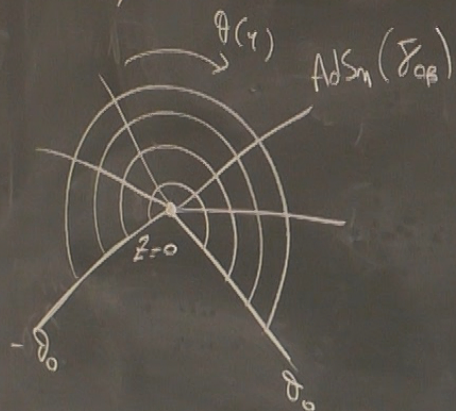
$$dy = a(\theta) d\theta$$

JANUS AdS_3

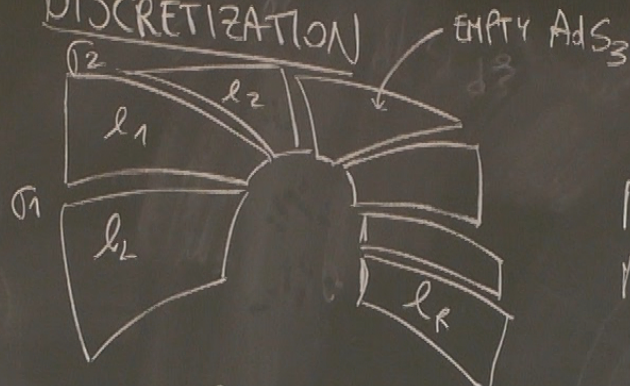
$AdS_3 \times S^3 \times M_4$

TYPE IIB SUPER

$$R - \partial_\mu \phi \partial^\mu \phi - 2V(\phi)$$



DISCRETIZATION



EMPTY AdS_3

N BRANES

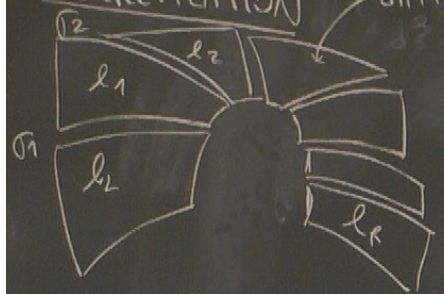
$N \rightarrow \infty$

$$l(y)$$

$$\frac{dr}{dy}$$

DISCRETIZATION

EMPTY AdS_3

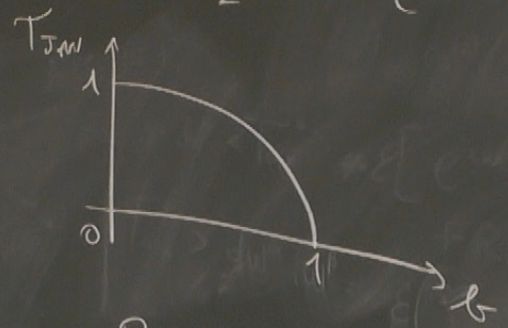


N BRANES
 $N \rightarrow \infty$

$$l(y)$$

$$\frac{dr}{dy}$$

$$\tau_{JAN} = \frac{1}{2} \sqrt{b(2-b)} \left[\operatorname{arctanh} \left(\sqrt{\frac{b}{2-b}} \right)^{-1} \right]$$



$$b=0 \Rightarrow \tau_{JAN}=1$$

$$b=1 \Rightarrow \tau_{JAN}=0$$

$$0 \leq \tau_L \leq \min \left(1, \frac{c_R}{c_L} \right)$$

• IMPOSE ISRAL

• IMPOSE NO-OUTGOING

$$\hat{K}_{ij} = K_{ij} -$$

$$\tau_L = \frac{2}{l_L} \left(\frac{1}{l} \right)$$

$$\left| \frac{1}{l_L} - \frac{1}{l_R} \right| \leq$$

$$\log g \sim \sigma$$

4) THICK BRANE MODEL

EINSTEIN GRAVITY + DILATON

$$b = 1 - \sqrt{1 - 2\gamma^2}$$

$$S = \frac{1}{16\pi G_N} \int d^{d+1}x \sqrt{-g} \left(R - \partial_\mu \phi \partial^\mu \phi - 2V(\phi) \right)$$

CONTINUOUS GEOMETRY

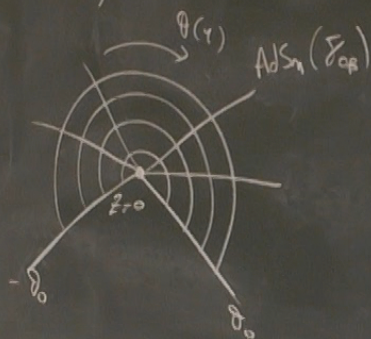
$$ds^2 = a^2(\theta) (d\theta^2 + \gamma_{\alpha\beta} dx^\alpha dx^\beta)$$

$$\phi = \phi(\theta)$$

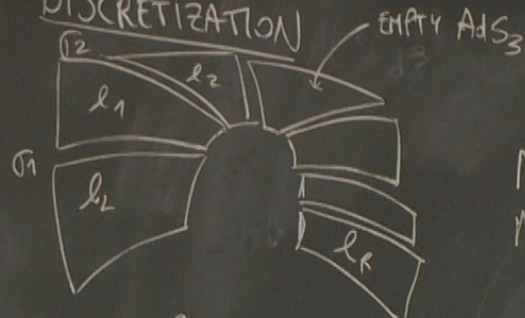
$$dy = a(\theta) d\theta$$

JANUS AdS_3

$AdS_3 \times S^3 \times M_4$
TYPE IIB SUPER



DISCRETIZATION



$$l(y) \frac{dr}{dy}$$

N BRANES
 $N \rightarrow \infty$

T_{JAN}