

Title: Tutorial 1A: Introduction to simpleboot. 3D Ising Island with Delaunay search

Speakers: Ning Su

Collection: Mini-Course of Numerical Conformal Bootstrap

Date: April 24, 2023 - 1:30 PM

URL: <https://pirsa.org/23040137>

```

File Edit Insert Format Cell Graphics Evaluation Palettes Window Help
  "VBlock$Identity" \[Rule] {{Fp[eps, eps, eps, eps, 0], Fp[eps, eps, eps, eps, 0]}, {0, Fp[sig, sig, eps, eps, 0], Hp[sig, sig, eps, eps, 0]}}, (* crossing vector for Videntity=(1 1).Veven (\[Delta]=0, \[Theta]=0).{{1, 0}, {0, 1}} *)
  "VBlock$Deriv" \[Rule] {{odd, odd, odd, odd, even}}, (* indicate the 5 components are even/odd under u<->v exchange *)
  "VBlock$External" \[Rule] {"sig", "eps"} (* the name of external operators as String *)
};


```

Block specifications

```

In[10]:= (* conformal block specifications : spacetime dimension, derivative order, pole keeping order, r_* order, spins *)
blockconfobj = {"dim" \[Rule] 3, "Amax" \[Rule] 11, "\[Kappa]" \[Rule] 12, "rN" \[Rule] 48, "lset" \[Rule] Range[0, 20] \[Intersection] Complement[Range[49, 52], {4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 29, 30, 33, 34, 37, 38, 41, 42, 45, 46, 49, 50}]};

dim = 3;
Lambda = 27;
AutoCB3$BlockSetting["DSD"] [dim, Lambda] (* some presetting in simpleboot *)
{dim \[Rule] 3, Amax \[Rule] 27, \[Kappa] \[Rule] 20, rN \[Rule] 80, lset \[Rule] {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 29, 30, 33, 34, 37, 38, 41, 42, 45, 46, 49, 50}}

```



```
"VBlock$External"→{"sig","eps"} (* the name of external operators as String *)
};
```

Block specifications

```
In[10]:= (* conformal block specifications : spacetime dimension, derivative order, pole keeping order, r, order, spins *)
blockconfobj={"dim"→3,"Δmax"→11,"κ"→12,"rN"→48,"lset"→Range[0,20]~Join~{49,52}};
```

```
In[30]:= dim = 3;
Lambda = 19;
AutoCB3$BlockSetting["DSD"] [dim, Lambda] (* some presetting in simpleboot *)
```

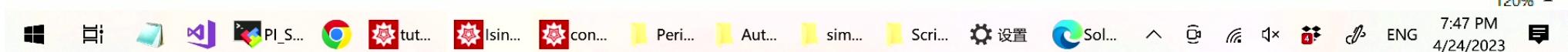
```
Out[32]= {dim → 3, Δmax → 19, κ → 14, rN → 56,
lset → {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 49, 50}}
```

Initialize simpleboot

```
In[11]:= (* tell simpleboot about the crossing vectors and block specs *)
AutoCB3$Init[crossvecobj,blockconfobj];
```

AutoCB3\$Init[crossvecobj,blockconfobj] : this function tells simpleboot about the crossing vectors and block specs.

Gaps



AutoCB3\$Init[crossvecobj,blockconfobj] : this function tells simpleboot about the crossing vectors and block specs.

Gaps

Format :

GapConfiguration is a List of element in one of the following format:

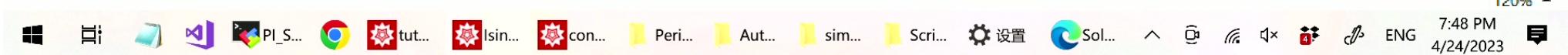
```
{channel,gap,spins}           // this means demand  $\alpha \cdot V_{\text{channel}} \geq 0$  for  $\Delta > \text{gap}$  and L in spins.  spins can be a integer or set of integers.
{channel,IndividualOperator[\Delta0],spin} // this means demand  $\alpha \cdot (V_{\text{channel},\Delta0,\text{spin}}) \geq 0$ 
{channel,IndividualOperator[\Delta0,ope_List],spin} // this means demand  $\alpha \cdot (\text{ope}.V_{\text{channel},\Delta0,\text{spin}}.\text{ope}) \geq 0$ 
{channel,IntervalPositivity[\Deltamin,\Deltamax],spin} // this means demand  $\alpha \cdot V_{\text{channel},\Delta,\text{spin}} \geq 0$  for  $\Delta_{\text{min}} < \Delta < \Delta_{\text{max}}$ 
```

```
In[12]:= Clear@GapConfiguration;
GapConfiguration[dim_, lset_]:={
  {op[op, "0", 1, 1], 3, 0}, (*  $\alpha \cdot V_{\text{odd}} > 0$  for  $\Delta > 3$  and L=0 *)
  {op[op, "E", 1, 1], 3, 0}, (*  $\alpha \cdot V_{\text{even}} > 0$  for  $\Delta > 3$  and L=0 *)

  {op[op, "E", 1, 1], \[Delta]unitary[dim, #], Select[lset, EvenQ[#] && # > 0 & ]}, (*  $\alpha \cdot V_{\text{even}} > 0$  for  $\Delta > \Delta_{\text{unitary}}$  and L=2, 4, ... *)
  {op[op, "0", 1, -1], \[Delta]unitary[dim, #], Select[lset, OddQ ]}, (*  $\alpha \cdot V_{\text{odd}} > 0$  for  $\Delta > \Delta_{\text{unitary}}$  and L=1, 3, ... *)
  {op[op, "0", 1, 1], \[Delta]unitary[dim, #], Select[lset, EvenQ[#] && # > 0 & ]} (*  $\alpha \cdot V_{\text{odd}} > 0$  for  $\Delta > \Delta_{\text{unitary}}$  and L=2, 4, ... *)
};

/: place holder for spin
```

SDP template



Gaps

Format :

GapConfiguration is a List of element in one of the following format:

```
{channel,gap,spins}           // this means demand  $\alpha \cdot V_{\text{channel}} \geq 0$  for  $\Delta > \text{gap}$  and L in spins.  spins can be a integer or set of integers.
{channel,IndividualOperator[\Delta0],spin}  // this means demand  $\alpha \cdot (V_{\text{channel},\Delta0,\text{spin}}) \geq 0$ 
{channel,IndividualOperator[\Delta0,ope_List],spin} // this means demand  $\alpha \cdot (\text{ope}.V_{\text{channel},\Delta0,\text{spin}}.\text{ope}) \geq 0$ 
{channel,IntervalPositivity[\Deltamin,\Deltamax],spin} // this means demand  $\alpha \cdot V_{\text{channel},\Delta,\text{spin}} \geq 0$  for  $\Delta_{\text{min}} < \Delta < \Delta_{\text{max}}$ 
```

```
In[12]:= Clear@GapConfiguration;
GapConfiguration[dim_, lset_]:={
  {op[op, "0", 1, 1], 3, 0}, (*  $\alpha \cdot V_{\text{odd}} > 0$  for  $\Delta > 3$  and L=0 *)
  {op[op, "E", 1, 1], 3, 0}, (*  $\alpha \cdot V_{\text{even}} > 0$  for  $\Delta > 3$  and L=0 *)

  {op[op, "E", 1, 1], \[Delta]unitary[dim, #], Select[lset, EvenQ[#] && # > 0 & ]}, (*  $\alpha \cdot V_{\text{even}} > 0$  for  $\Delta > \Delta_{\text{unitary}}$  and L=2, 4, ... *)
  {op[op, "0", 1, -1], \[Delta]unitary[dim, #], Select[lset, OddQ ]}], (*  $\alpha \cdot V_{\text{odd}} > 0$  for  $\Delta > \Delta_{\text{unitary}}$  and L=1, 3, ... *)
  {op[op, "0", 1, 1], \[Delta]unitary[dim, #], Select[lset, EvenQ[#] && # > 0 & ]}} (*  $\alpha \cdot V_{\text{odd}} > 0$  for  $\Delta > \Delta_{\text{unitary}}$  and L=2, 4, ... *)
};
```

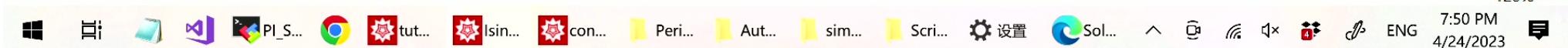
/ : place holder for spin

SDP template

normalization:

$$\alpha \cdot (V_{\text{identity}}) = 1 \text{ with } V_{\text{identity}} = (1 \ 1) \cdot V_{\text{even}}(\Delta = 0, / = 0) \cdot \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

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$$\alpha \cdot (V_{\text{identity}}) = 1 \text{ with } V_{\text{identity}} = (1 \ 1) \cdot V_{\text{even}}(\Delta = 0, l = 0) \cdot \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

positivity condition:

$$\alpha \cdot V_{\text{even}}(\Delta, l) \geq 0 \text{ for } \Delta \geq 3, l = 0$$

$$\alpha \cdot V_{\text{odd}}(\Delta, l) \geq 0 \text{ for } \Delta \geq 3, l = 0$$

$$\alpha \cdot V_{\text{even}}(\Delta, l) \geq 0 \text{ for } \Delta \geq \Delta_{\text{unitary}}, l = 2, 4, 6, \dots$$

$$\alpha \cdot V_{\text{odd}}(\Delta, l) \geq 0 \text{ for } \Delta \geq \Delta_{\text{unitary}}, l = 1, 2, 3, 4, \dots$$

$$\alpha \cdot V_\theta \geq 0 \text{ where } V_\theta = V_{\text{even}}(\Delta = \Delta_\varepsilon, l = 0) + V_{\text{odd}}(\Delta = \Delta_\sigma, l = 0) \otimes \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$$

```
In[14]:= Clear@SDPTemplate$IsingOE;
SDPTemplate$IsingOE[]:=Module[
{BC$normalization, BC$objective, BC$condition, sdp, v$theta,
GFFnormalization},

BC$normalization=AutoCB3$Vector[CrossVec["identity"]]; (* α.V_identity=1 *)
BC$objective=AutoCB3$Vector[CrossVec["zero"]];
BC$conditions=AutoCB3$Condition[1,CrossVec["v$theta"],0,{0}]~Join~(* α.V_θ>0 *)
AutoCB3$Condition[GapConfiguration]; (* the rest positivity conditions *)

sdp=SDPData[BC$objective,BC$normalization,BC$condition];

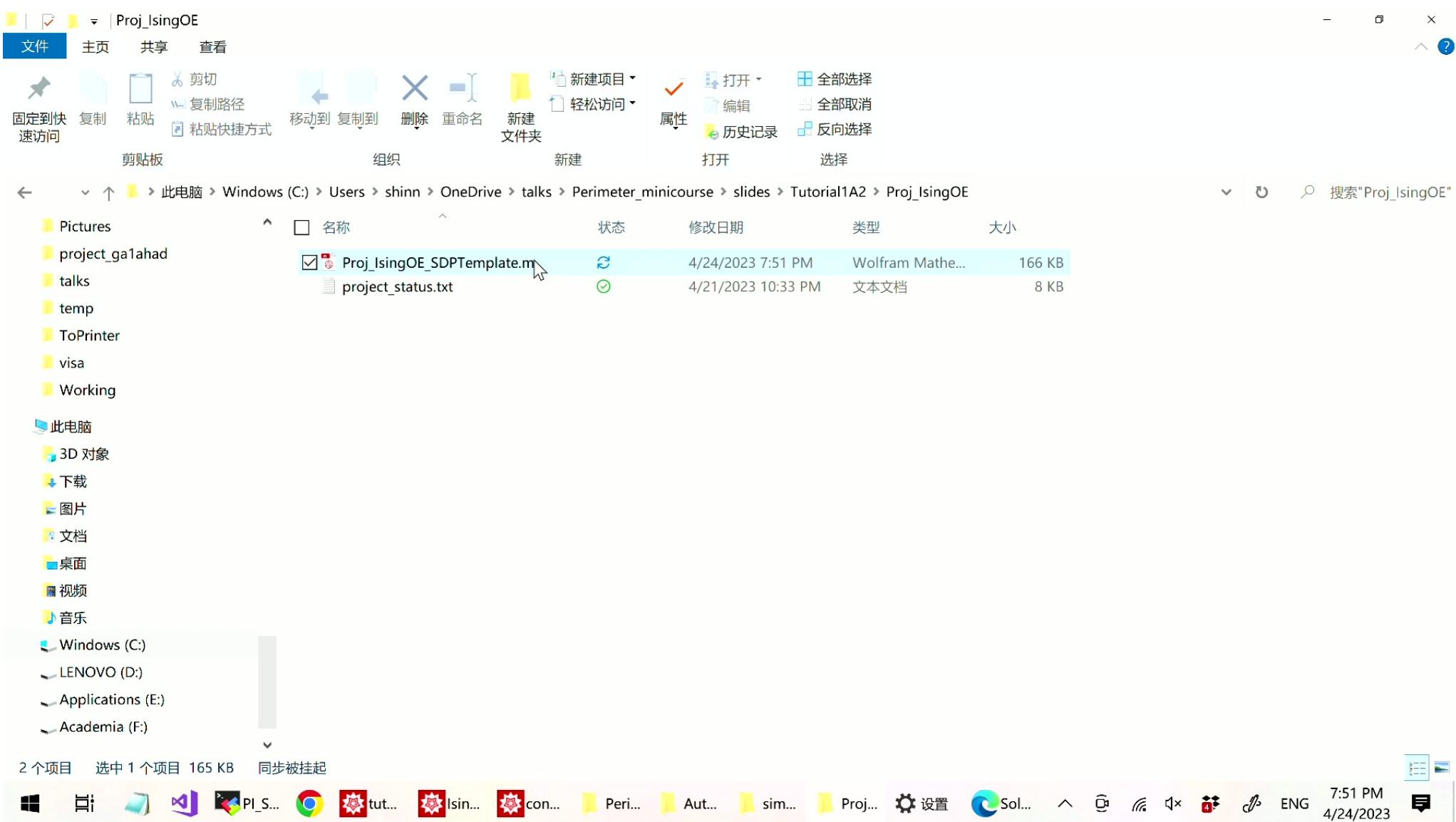
sdp
];
```

~Join~ : see the note

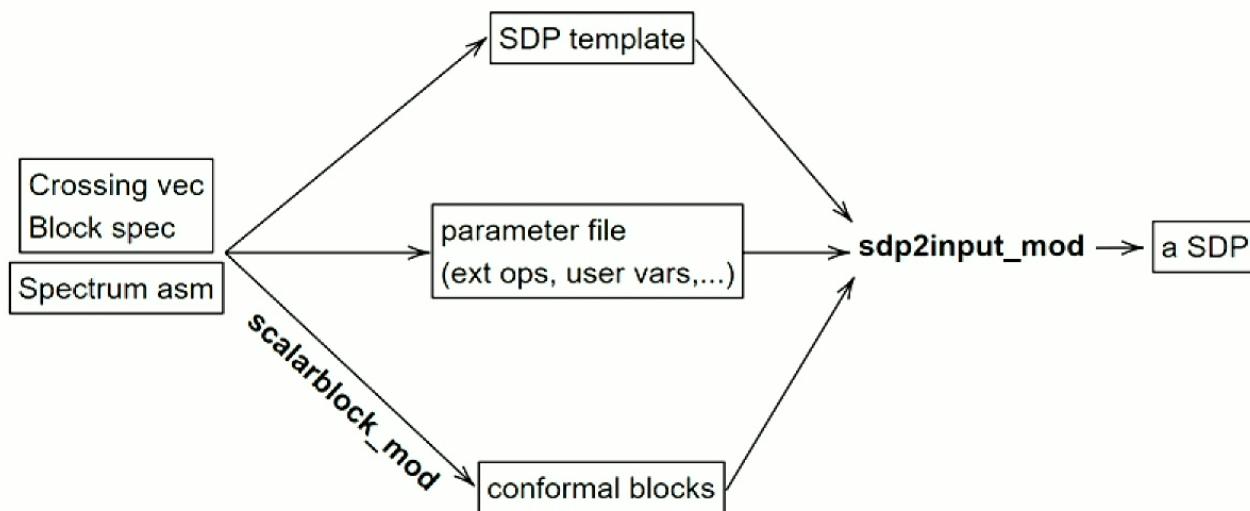
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4/24/2023





simpleboot : run a SDP (high efficiency mode)



Advantage : very fast. All heavy computations are done in C++ programs

Disadvantage : simpleboot doesn't access to explicit SDP data (such as explicit crossing vectors $V_{\Delta,\ell}$).



```
sdp
];
```

~Join~ : see the note

```
In[33]:= (* save the template as default template for this project *)
AutoCB3$SaveSDPTemplate@SDPTemplate$IsingOE[];
```

Generate SDP

This function generate a SDP. It will be used by the Delaunay search scanner.

Input : a point to scan

Output : filename of the SDP

```
In[16]:= SDP$IsingOE[point_List, filename_:Automatic]:=Module[
{Δσ, Δε},
{Δσ, Δε}=SetPrec[point];

AutoCB3$GenerateSDP[{Δσ, Δε}, {}, filename]
];
```

AutoCB3\$GenerateSDP[externalOperatorList, userDefinedVariables, paramFilename]

AutoCB3\$GenerateSDP call C++ programs to generate blocks (if the block data is not generated) and generate an actual SDP based on the template and user-defined variables



Input:

externalOperatorList: the values of the external operators. The order should match with "VBlock\$External"

userDefinedVariables: user-defined variable in the template. Format : {"variable1"→value1, "variable2"→value2, ...}

paramFilename: SDP filename. Automatic : AutoCB3\$GenerateSDP will choose a proper name automatically.

Output:

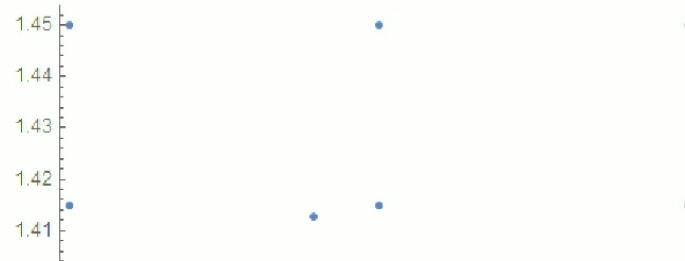
SDP filename

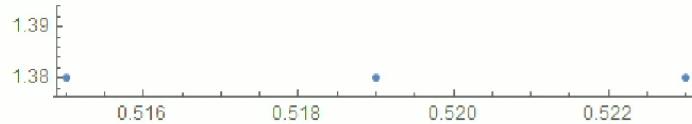
Delaunay Search

```
SSH$UploadCurrentNotebook[] (* save and upload current notebook as package (.m) to the cluster *)
```

```
initpts = {{0.5181489, 1.412625}} ~Join~ GeneratePointsInRectangular[{0.515, 0.523}, {1.38, 1.45}, 3, 3] // SetPrec;
initpts // ListPlot
```

... N: Requested precision 16 is smaller than \$MinPrecision. Using \$MinPrecision instead.





```
ClusterAsyn$Evaluate[  
  AutoCB3$SaveSDPTemplate@SDPTemplate$IsingOE[]]; ]  
  
initpts = {{0.5181489, 1.412625}} ~Join~ GeneratePointsInRectangular[{0.515, 0.523}, {1.38, 1.45}, 3, 3] // SetPrec;  
  
SB$FeasibilityScanner[  
  SDP$IsingOE, (* function that generates a SDP *)  
  initpts, (* initial points to scan *)  
  "--maxIterations=1000 --dualityGapThreshold=1e-25 --primalErrorThreshold=1e-15 --dualErrorThreshold=1e-15  
  --precision=765 --initialMatrixScalePrimal=1e+20 --initialMatrixScaleDual=1e+20 --maxComplementarity=1e+70  
  --detectPrimalFeasibleJump --detectDualFeasibleJump ", (* SDPB parameters *)  
  
  {"Delaunay"}, (* scan method *)  
  200, (* maximal points to scan *)  
  False (* initial checkpoint. False means no initial checkpoint. *)  
 ]  
 ]
```

408919

```
(* Check the job output. Input : job ID *)  
ClusterAsyn$JobOutput["408581"]
```



PI_Symmetry (nsu2)

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Session Servers Tools Games Sessions View Split

MultiExec Tunneling Packages Settings Help

X server Exit

Quick connect...

Sessions Macros Sftp Tools

/gpfs/nsu2/simpleboot4_tutorial1A/Proj_IsingOE/

Name .. btjob-409897.out

btjob-409897.out

System information as of Mon Apr 24 11:35:52 EDT 2023

```
System load: 0.58          Users logged in: 14
Usage of /: 41.7% of 99.94GB  IP address for eno1np0: 10.10.21.98
Memory usage: 37%          IP address for eno3: 172.16.2.250
Swap usage: 31%            IP address for ib0: 192.168.2.250
Processes: 1109             IP address for docker0: 172.17.0.1
```

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16 of these updates are standard security updates.
To see these additional updates run: apt list --upgradable

66 additional security updates can be applied with ESM Apps.
Learn more about enabling ESM Apps service at <https://ubuntu.com/esm>

Your Hardware Enablement Stack (HWE) is supported until April 2023.

Last login: Mon Apr 24 01:51:32 2023 from 10.40.1.224

```
nsu2@mn003:~$ squeue -u nsu2
      JOBID PARTITION      NAME      USER ST      TIME  NODES NODELIST(REASON)
      409850    debugq RunMMA_j    nsu2 R      48:56      1 cn070
nsu2@mn003:~$ cd /gpfs/nsu2/simpleboot4_tutorial1A/
nsu2@mn003:/gpfs/nsu2/simpleboot4_tutorial1A$ rm -r *.m
nsu2@mn003:/gpfs/nsu2/simpleboot4_tutorial1A$ squeue -u nsu2
      JOBID PARTITION      NAME      USER ST      TIME  NODES NODELIST(REASON)
      409897    debugq RunMMA_j    nsu2 R      0:06      1 cn071
nsu2@mn003:/gpfs/nsu2/simpleboot4_tutorial1A$
```

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8:01 PM 4/24/2023

PI_S... tut... lsin... con... Peri... Aut... sim... Proj... Sol... ENG

Function : SB\$AddPoints

Cluster control

Function : ClusterLoginNode\$Evaluate

Function : ClusterAsyn\$Evaluate, ClusterAsyn\$JobOutput, ClusterAsyn\$JobOutput\$ToExpression

Function : ClusterAsyn\$SDPBOutput

Function : ClusterSRUN\$ReloadJobs

Miscellaneous

Function : ObjSet, ObjGet

I

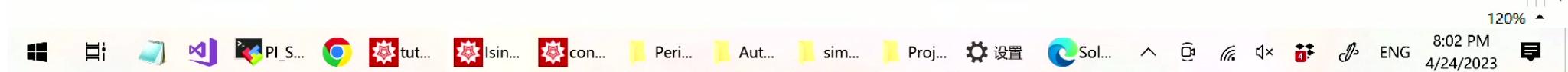
Function : RunShell

Function : CheckDirectory

Simpleboot operation mode

To use full functionality, simpleboot need automatic SSH login and SLURM cluster.

Automatic SSH login : SSH can be configured to passwordless login based RSA keys. See .



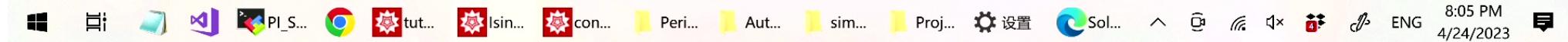
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```
primalErrorThreshold = 1e-15
dualErrorThreshold = 1e-15
initialMatrixScalePrimal = 1e+20
initialMatrixScaleDual = 1e+20
feasibleCenteringParameter = 0.1
infeasibleCenteringParameter = 0.3
stepLengthReduction = 0.7
maxComplementarity = 1e-70
initialCheckpointDir = "./Proj_IsingOE/SDPBFiles/0.518148900000_1.41262500000_Apr24_14h03m21s.ck"
checkpointDir = "./Proj_IsingOE/SDPBFiles/0.518148900000_1.41262500000_Apr24_14h03m21s.ck"
noFinalCheckpoint = false
writeSolution = x,y
procsPerNode = 64
procGranularity = 1
verbosity = 1
```

Performing a timing run

	time	mu	P-obj	D-obj	gap	P-err	p-err	D-err	P-step	D-step	beta
<hr/>											
1	0	1.0e+40	+0.00	+0.00	0.00	+1.00e+20	+0.00	+1.80e+24	0.446	0.383	0.300
2	0	7.1e+39	-1.29e+20	+0.00	1.00	+5.54e+19	+5.24e-195	+1.11e+24	0.366	0.398	0.300
3	1	5.5e+39	-2.27e+20	+0.00	1.00	+3.51e+19	+4.91e-195	+6.69e+23	0.292	0.257	0.300
4	1	4.6e+39	-2.84e+20	+0.00	1.00	+2.49e+19	+5.94e-195	+4.98e+23	0.323	0.358	0.300
5	2	3.7e+39	-3.22e+20	+0.00	1.00	+1.68e+19	+7.24e-195	+3.20e+23	0.355	0.291	0.300
6	2	2.9e+39	-3.84e+20	+0.00	1.00	+1.09e+19	+1.06e-194	+2.27e+23	0.439	0.339	0.300
7	3	2.1e+39	-5.00e+20	+0.00	1.00	+6.09e+18	+5.39e-195	+1.50e+23	0.371	0.324	0.300

120%

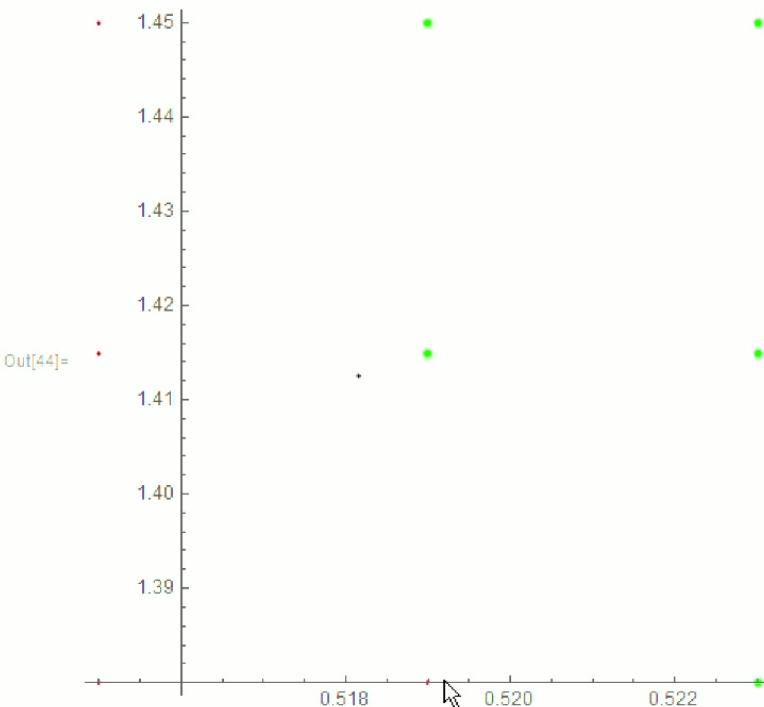


IsingOE.nb - Wolfram Mathematica 11.1

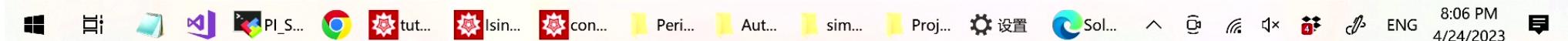
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```
In[42]:= SSH$DownloadFile@SB$Proj$FileName; (* download current project data from the cluster *)
          SB$LoadProject[]; (* load current project data *)
```

```
In[44]:= SB$DelaunayPlot[] (* plot the scan result *)
```



```
SB$RawPlot[]
```



PI_Symmetry (nsu2)

Terminal Sessions View X server Tools Games Settings Macros Help

Session Servers Tools Games Sessions View Split

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Quick connect...

Sessions

Name

- ..
- SDPBFiles
- BlockData
- project_status.txt
- Proj_IsingOE_SDPTemplate.m
- btjob-409910.out
- btjob-409897.out

6. login.rc.fas 2. PI_Symmet 8. PI_Symmet 11. login.rc.fas 13. PI_Symmet 15. localui.pi.in 17. vpn.caltech

```

defq*      up 1-00:00:00      64 alloc cn[004-059,061-068]
debugq     up 1:00:00        2 resv cn[003,060]
debugq     up 1:00:00        72 alloc cn[004-059,061-076]
ehtq       up infinite      0 n/a
preq       up 1-00:00:00      2 resv cn[003,060]
preq       up 1-00:00:00      2 mix cn[001-002]
preq       up 1-00:00:00      72 alloc cn[004-059,061-076]
reservedq  up infinite      1 drain* cn095
reservedq  up infinite      18 drain cn[093-094,096-110],mn004
reservedq  up infinite      2 resv cn[003,060]
reservedq  up infinite      2 mix cn[001-002]
reservedq  up infinite      82 alloc cn[004-059,061-076,079-086,089-090]
reservedq  up infinite      6 idle cn[077-078,087-088,091-092]
sharedq    up 7-00:00:00      2 mix cn[001-002]
gpuq      up 1-00:00:00      1 idle cn078
gpudebugq up 1:00:00        2 idle cn[077-078]
longq     up 7-00:00:00      1 resv cn060
longq     up 7-00:00:00      15 alloc cn[053-059,061-068]
amdq      up 1-00:00:00      1 drain* cn095
amdq      up 1-00:00:00      18 drain cn[093-094,096-110],mn004
amdq      up 1-00:00:00      10 alloc cn[079-086,089-090]
amdq      up 1-00:00:00      2 idle cn[087-088]
amddebugq up 1:00:00        1 drain* cn095
amddebugq up 1:00:00        18 drain cn[093-094,096-110],mn004
amddebugq up 1:00:00        10 alloc cn[079-086,089-090]
amddebugq up 1:00:00        4 idle cn[087-088,091-092]
amdpreq   up 1-00:00:00      1 drain* cn095
amdpreq   up 1-00:00:00      18 drain cn[093-094,096-110],mn004
amdpreq   up 1-00:00:00      10 alloc cn[079-086,089-090]
amdpreq   up 1-00:00:00      4 idle cn[087-088,091-092]
gpupreq  up 1-00:00:00      2 idle cn[077-078]
actq      up infinite      0 n/a
nsu2@mn003:/gpfs/nsu2/simpleboot4_tutorial1A$ squeue -u nsu2
          JOBID PARTITION      NAME      USER ST      TIME  NODES NODELIST(REASON)
          409910  amddebugq RunMMA_j  nsu2  R      0:05      1 cn087
nsu2@mn003:/gpfs/nsu2/simpleboot4_tutorial1A$ 
```

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8:06 PM
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Windows Taskbar icons: File Explorer, Task View, Taskbar settings, Sol... (Solitaire), ENG (English), Date/Time.

IsingOE.nb - Wolfram Mathematica 11.1

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SB\$RawPlot[]

utility codes

check job output and SDPB output

```
(* Check the job output. Input : job ID *)
ClusterAsyn$JobOutput["407653"]

(* Check the SDPB output. Input : SDP file name *)
ClusterAsyn$SDPBOutput["0.515000000000_1.44999300000_Apr17_20h10m02s.sdp"]
SB$LoadProject[];
ClusterAsyn$SDPBOutput@ObjGet[SB$Proj$calculated$dual, 1, "LastCheckpoint"]
```

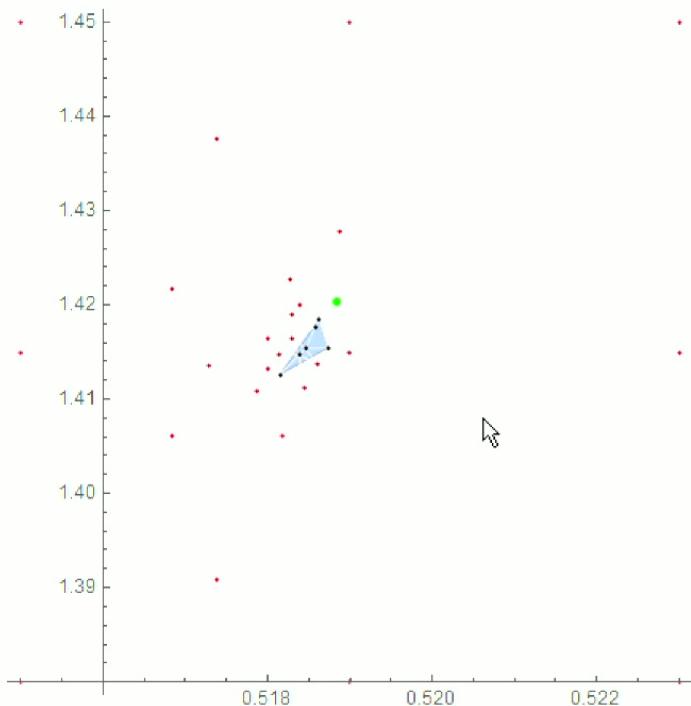
download the project data and monitor the result in real time

```
(* download the project data every 1s and plot the data *)
Monitor[
  While[True,
    Pause[1];
    SSH$DownloadFile@SB$Proj$FileName;
  ]
];
```



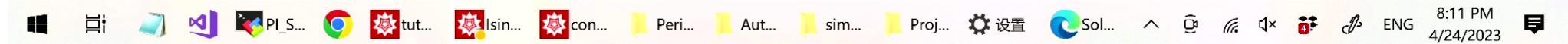
120% 8:09 PM
4/24/2023 ENG

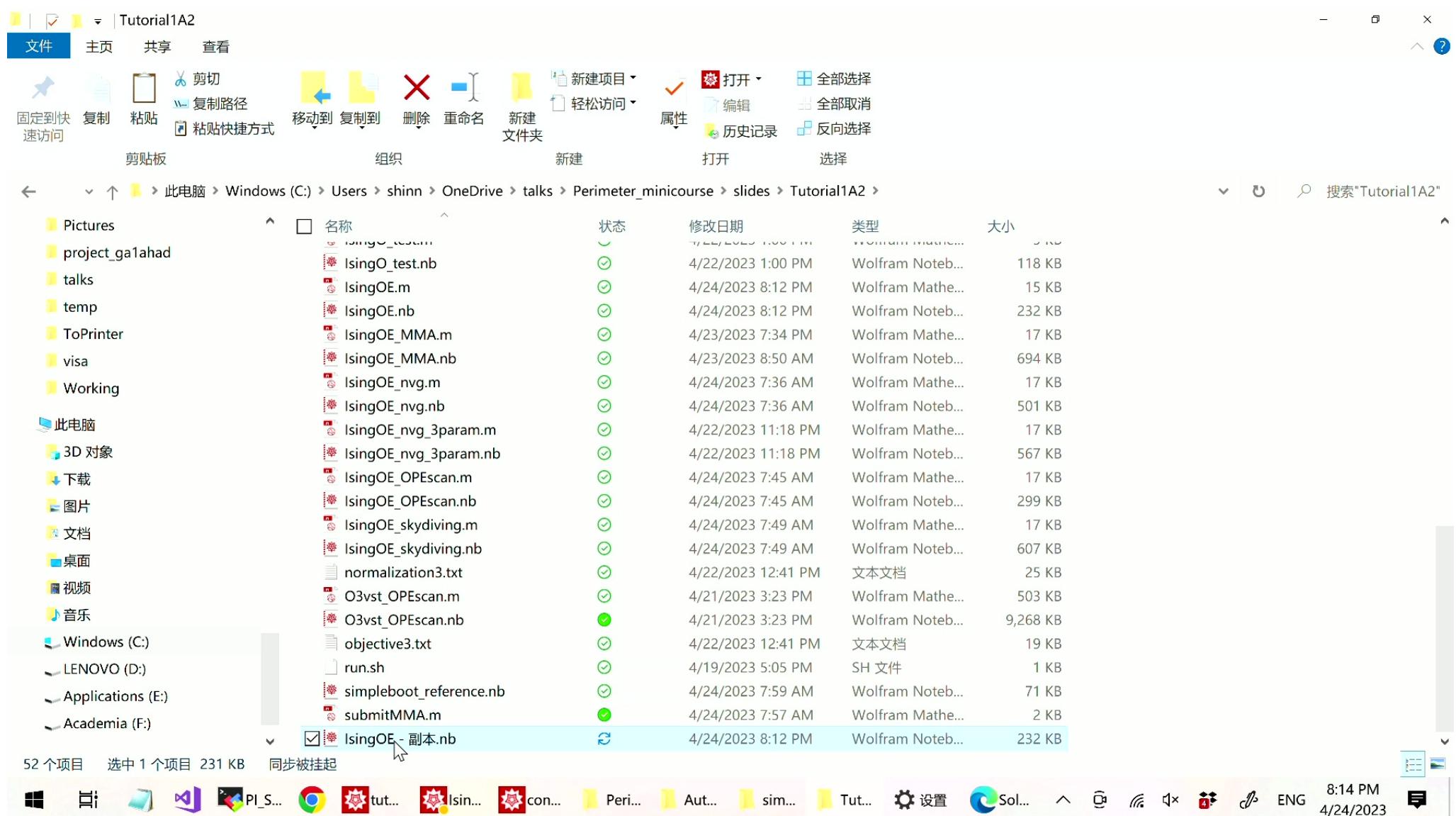
File Edit Insert Format Cell Graphics Evaluation Palettes Window Help
, Refresh[SB\$DelaunayPlot[], UpdateInterval → 1]]



cancel all jobs

```
(* ClusterLoginNode$Evaluate: execute MMA command on the login node of the cluster *)
ClusterLoginNode$Evaluate[
  (* RunShell : execute a shell command *)
```





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Null

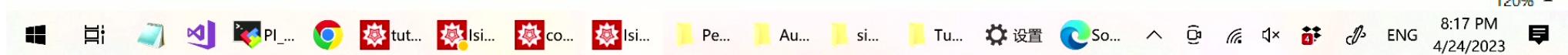
Manually add points for Delaunay scanner to scan

```
(* ClusterLoginNode$Evaluate: execute MMA command on the login node of the cluster *)
ClusterLoginNode$Evaluate[
  (* Cluster$AddPoints : add a list of point for the scanner to compute *)
  Cluster$AddPoints[
    {{0.5177491433922756, 1.4069517019543976`}, {0.517380791833411, 1.4042418752442998`},
     {0.5170706010469988, 1.4008545918566775`}, {0.520560247394137, 1.4294771364820849`},
     {0.5207153427873431, 1.432864419869707}, {0.5216846889948815, 1.4352355182410423`} // SetPrec]
]
```

Add a test region for Delaunay scanner

```
ClusterLoginNode$Evaluate[
  (* Add a test region in the Delaunay scanner. The scanner will only search for new points inside the test region. *)
  SB$LockProject[];
  ObjSet[SB$Proj, "method"] =
    {"sampler" → "Delaunay",
     "Region" → Polygon@{{0.5171516665322581, 1.3974831977419353`}, {0.5189660012096774, 1.4049190132258063`},
      {0.5175772512096775, 1.413332254838709`}, {0.5163900939516128, 1.4025708609677416`}});
  SB$UnlockProject[];
]

ClusterLoginNode$Evaluate[
```



IsingOE2.nb * - Wolfram Mathematica 11.1

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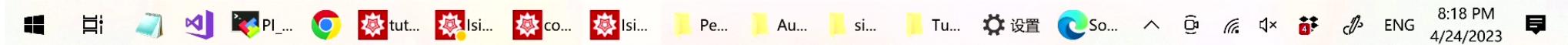
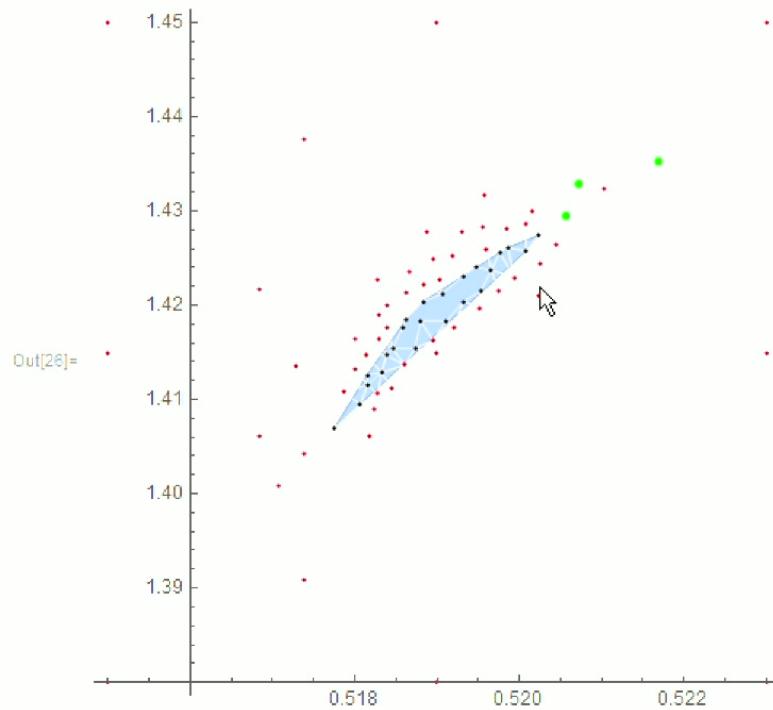
(* Check the SDPB output. Input : SDP file name *)

ClusterAsyn\$SDPBOutput["0.518148900000_1.41262500000_Apr24_14h03m21s.sdp"]

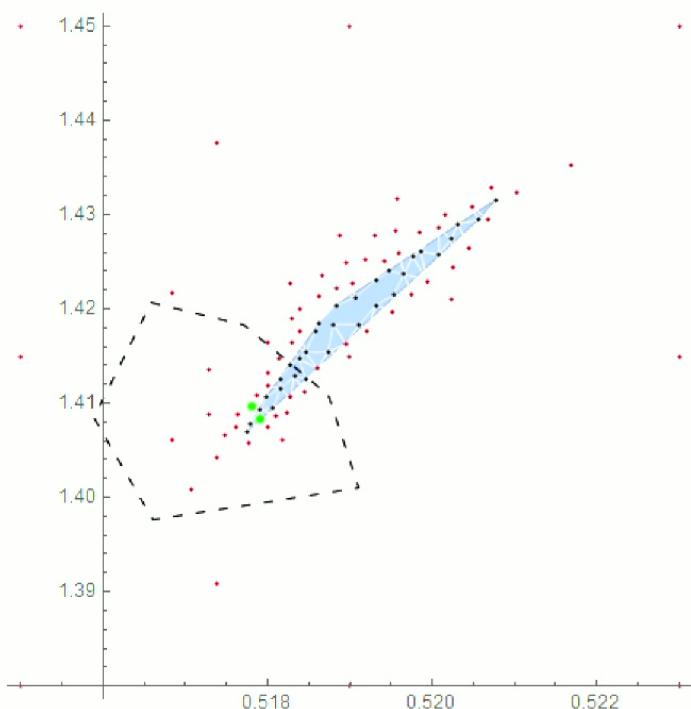
In[24]:= SSH\$DownloadFile@SB\$Proj\$FileName; (* download current project data from the cluster *)

SB\$LoadProject[]; (* load current project data *)

In[26]:= SB\$DelaunayPlot[] (* plot the scan result *)

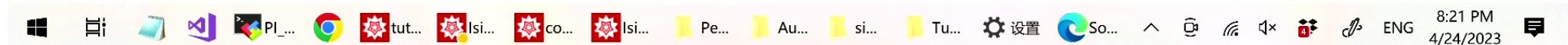


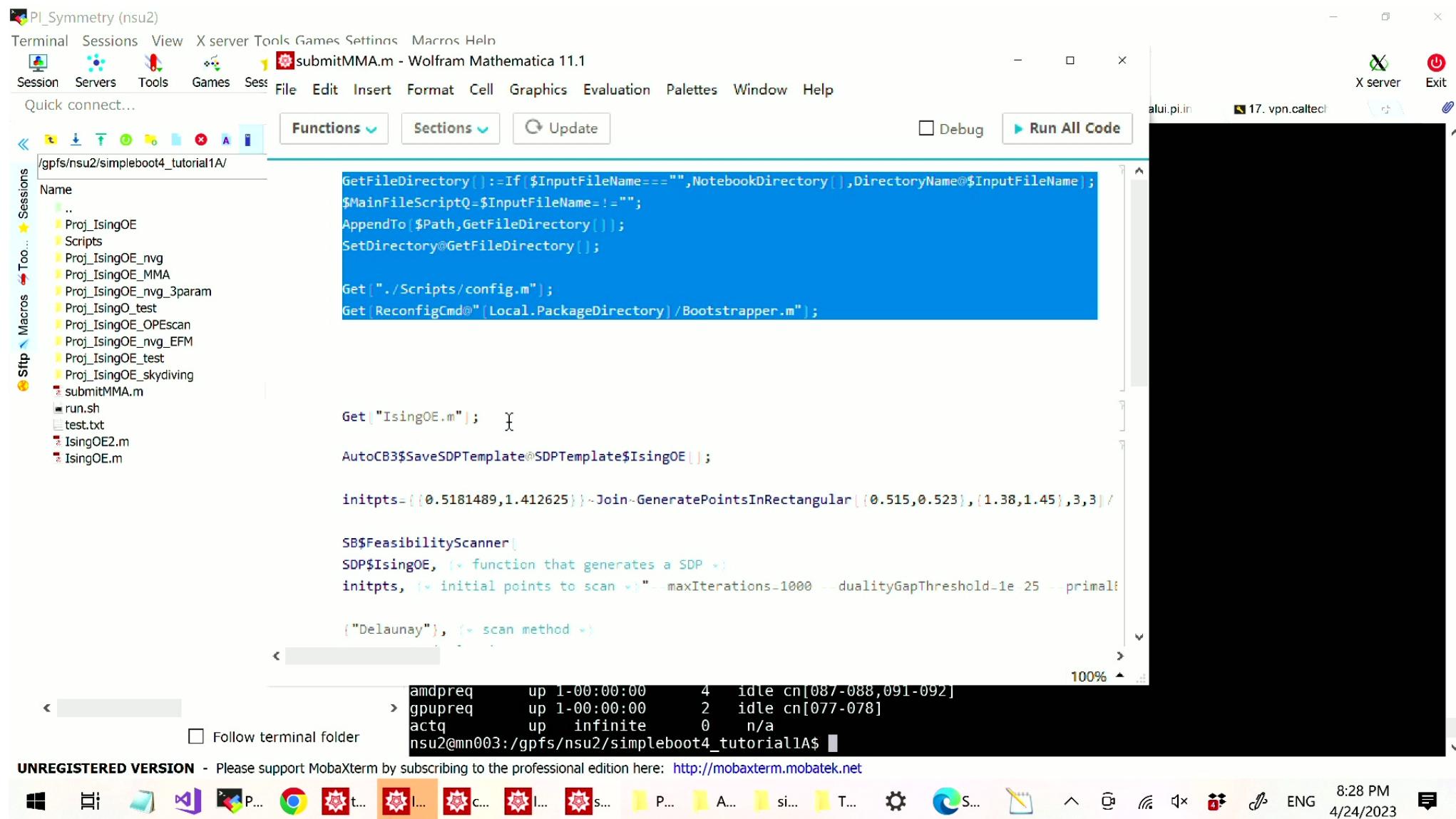
File Edit Insert Format Cell Graphics Evaluation Palettes Window Help
, Refresh[SB\$DelaunayPlot[], UpdateInterval → 1]]



cancel all jobs

```
(* ClusterLoginNode$Evaluate: execute MMA command on the login node of the cluster *)
ClusterLoginNode$Evaluate[
  (* RunShell : execute a shell command *)
```





Exercise_Tutorial1A.nb - Wolfram Mathematica 11.1

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This is a long exercise set. But the computation is pretty quick for $\Lambda = 11$ (around 10mins to ~1 hour).

For perimeter user:

We are sharing limited computational resources among many participants. Please don't do heavy computations. For debugging, you can use debugq. Once the code runs correctly for 10mins, you can stop it and re-run it on defq. Once the feasible region have rough sharp (usually around 100 to 200 points), you can stop the computation.

Try to do Exercise 1-3 today. Try to finish Exercise 4 by Thursday (it's related to what I want to discuss on Thursday).

Exercise 1

Go through IsingOE.nb to understand how the bootstrap conditions are set up.

Execute IsingOE.nb to scan a 3D Ising island.

Exercise 2

Go through IsingO.nb to understand how to use user-defined variables.

Execute IsingO.nb to scan single correlator for 3D Ising.

Exercise 3

Modify IsingO.nb to scan single correlator bound for 3D O(N). You can use the crossing vector from ArXiv:1307.6856 (2.5).

In simpleboot, the default definition of conformal block is in ArXiv:1805.04405 TABLE I row 1, while the convention of ArXiv:1307.6856 is in row 5. Therefore there is a $(-1)^f$ difference for V_{A,Δ_f} . When you type in crossing vector, you should take minus of V_{A,Δ_f} in ArXiv:1307.6856 (2.5).

Exercise 4

