

Title: Extended Path Intensity Correlation: Differential Astrometry with Microarcsecond Precision

Speakers: Marios Galanis

Series: Cosmology & Gravitation

Date: April 10, 2023 - 12:00 PM

URL: <https://pirsa.org/23040128>

Abstract: The angular resolution of a stellar interferometer, as for a single telescope, becomes better at smaller wavelengths and larger baselines. The goal for ground detectors would then be optical interferometers with baselines as long as the Earth's diameter. The latter goal has been achieved in radio, but it becomes prohibitive in the optical, as the electromagnetic field oscillates too rapidly to record and analyze directly over km-long baselines. Intensity interferometry relying on second-order correlations can make this possible: rather than the amplitude and phase of incoming light, we need only count photons. This technique has a long history and to date the best measurements of nearby stellar radii, dating back to the 1950s. Its main limitations are the need for very bright sources and its narrow field of view, restricting kilometer-long baselines to sources only a few λ s away. In this talk, I will propose an optical-path modification of astronomical intensity interferometers, which introduces an effective time delay in the two-photon interference amplitude, splitting the main intensity correlation fringe into others at finite opening angles, allowing for differential astrometry of multiple compact sources such as stars or quasar images. Together with the exponential progress in the field of single photon detection, such a modification will immensely increase the scope of intensity interferometry beyond measurements of the optical emission region morphology. I will lay out the theory and technical requirements of time-delay intensity interferometry and, time permitting, I will talk about some promising applications, which include astrometric microlensing of stars and quasar images, binary-orbit characterization, exoplanet detection, Galactic acceleration measurements and calibration of the cosmic distance ladder, all at unprecedented relative astrometric precision.

Zoom Link: TBD

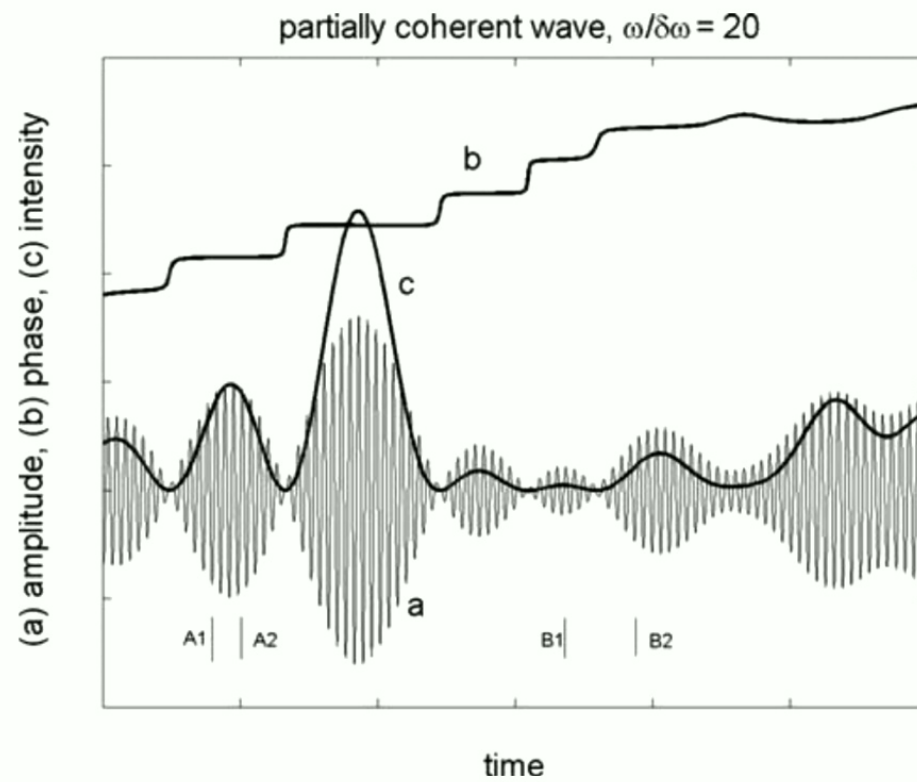
Extended Path Intensity Correlation: Differential Astrometry with Microarcsecond Precision

Marios Galanis
Perimeter Institute

In collaboration with: **Ken Van Tilburg** (NYU & CCA), **Masha Baryakhtar** (UW), **Neal Weiner** (NYU)

arXiv: 2304.xxxxx

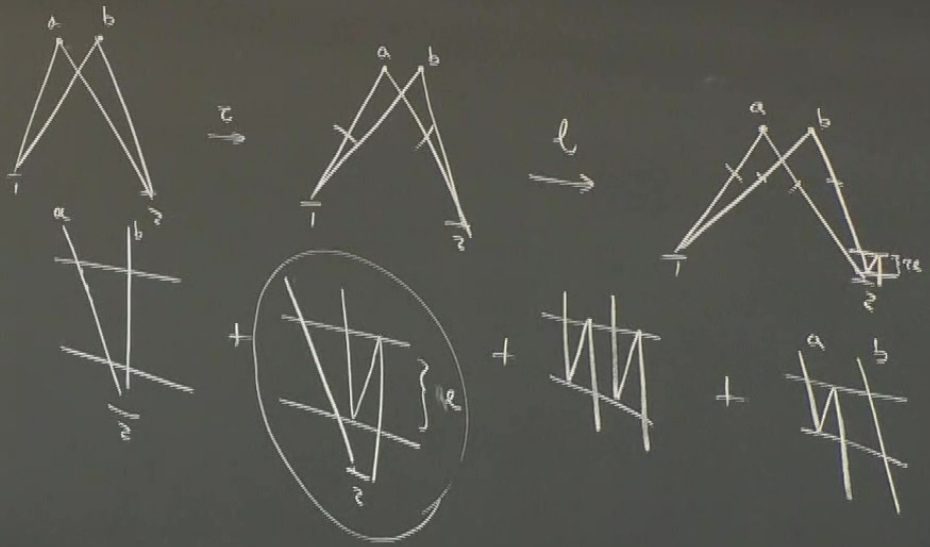
Photon Counts





Interferometry

EPIC



Intensity Interferometry

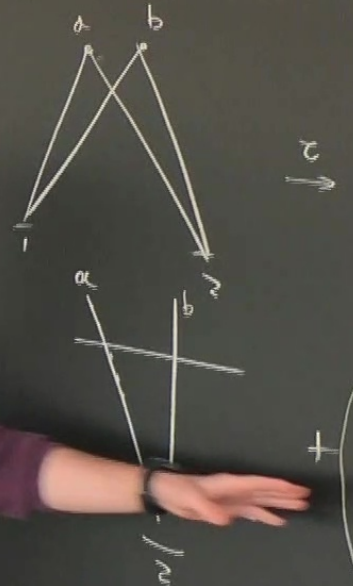
HBT

$$\bar{k} + (\Delta k)$$

$$\theta \approx \frac{1}{\Delta k d} \sim \text{few mas}$$

$$C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} - 1 \sim \frac{2}{i} \cos(\bar{k} [\vec{d} \cdot \vec{\theta} + L]) e^{-(\Delta k (\vec{d} \cdot \vec{\theta} + L))^2 / 4}$$

EPIC



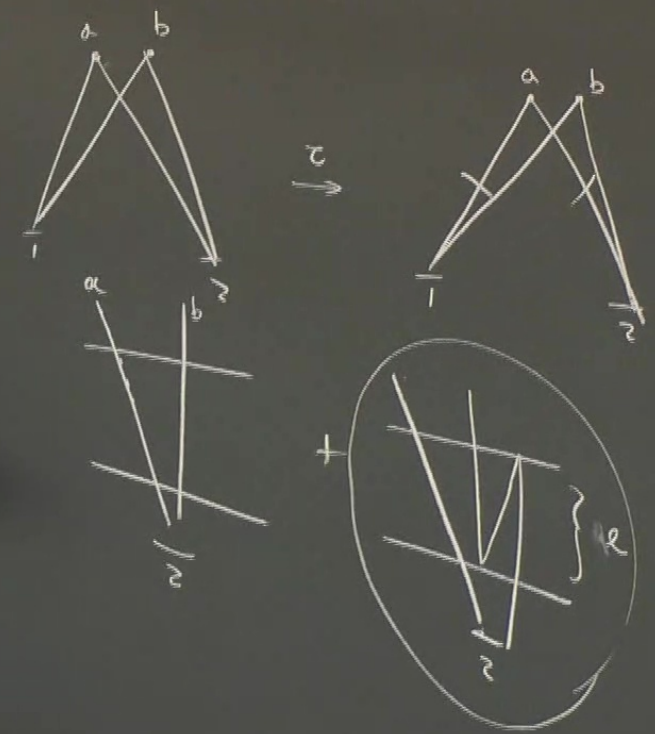
Intensity Interferometry

HBT

$$C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} - 1 \sim \sum_l \cos(\vec{k} \cdot \vec{d} + L_l) e^{-\frac{(\Delta k \cdot \vec{d} + L_l)^2}{4}}$$

$\vec{k} + \Delta \vec{k}$ $\theta \approx \frac{1}{\Delta k d} \sim \text{few mas}$
 $L_l \approx -\vec{d} \cdot \vec{\theta}$ $\times \epsilon_T^\# \epsilon_R^\#$

EPIC



Intensity Interferometry

HBT

$$\bar{k} + (\Delta k)$$

$$\theta \approx \frac{1}{\Delta k d} \sim \text{few mas}$$

$$C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} - 1 \sim \sum_i \Delta \cos(\bar{k}[\vec{d} \cdot \vec{\theta} + L_i]) e^{-\frac{(\Delta k(\vec{d} \cdot \vec{\theta} + L_i))^2}{4}} \times \# \epsilon_T \# \epsilon_R$$

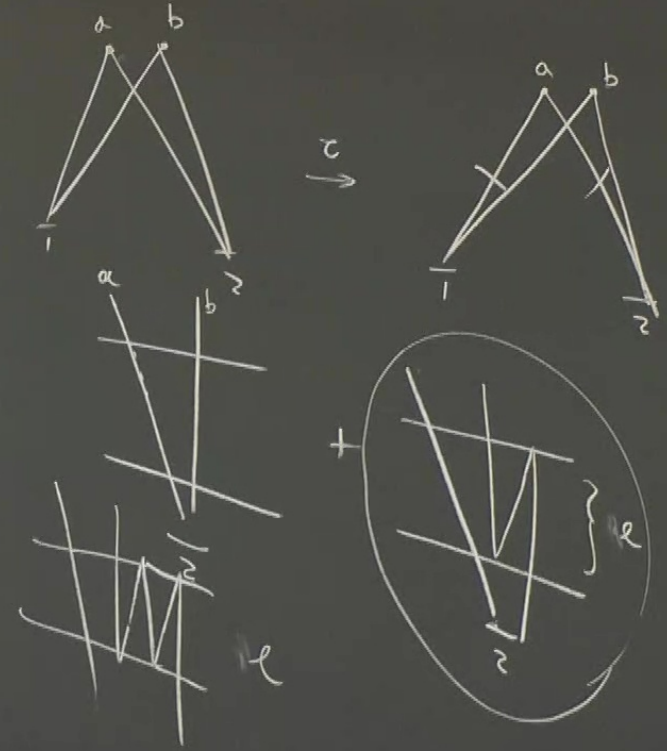
$$2L \approx -\vec{d} \cdot \vec{\theta}$$

$$\frac{F_a F_b}{(F_a + F_b)^2} \sim \frac{F_b}{F_a}$$

$$\gamma = \langle E_a E_b^* \rangle \sim \text{Fovner}(I(l, m))$$

$$C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} = 1 + |\gamma|^2$$

EPIC



Intensity Interferometry

HBT

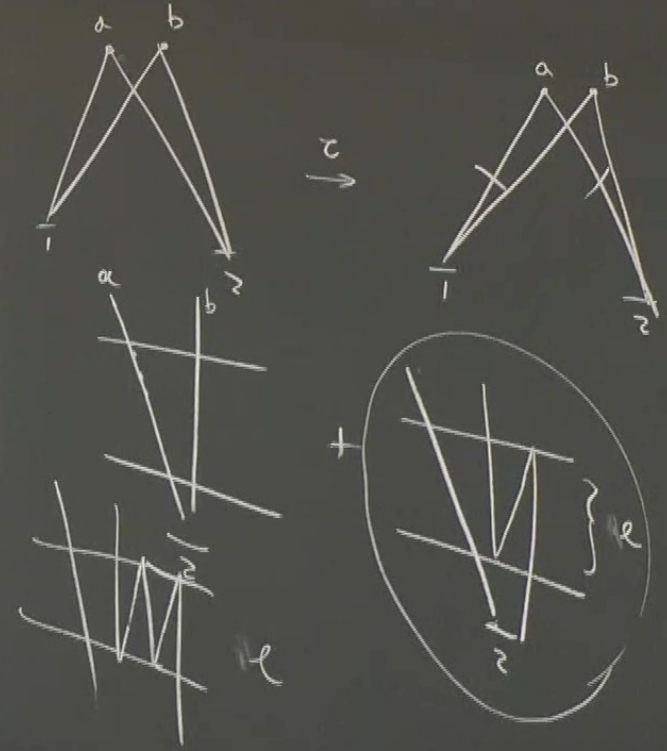
$\bar{k} + (\Delta k)$ $\theta \gtrsim \frac{1}{\Delta k d} \sim \text{few mas}$

$$C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} - 1 \sim \sum_i \Delta \cos(\bar{k} [d \cdot \vec{\theta} + L_i]) e^{-\frac{(\Delta k (d \cdot \vec{\theta} + L_i))^2}{4}} \times \begin{matrix} \# \\ E_T \end{matrix} \begin{matrix} \# \\ E_R \end{matrix}$$

$\frac{F_a + F_b}{(F_a + F_b)^2} \sim \frac{F_b}{F_a}$ $2L \approx -d \cdot \vec{\theta}$ $\tau_c \sim \text{fs}$ $\sigma_{\tau} \sim \text{10ps}$ $t_{\text{res}} \sim \text{tenths ns}$

$\gamma = \langle E_a E_b^* \rangle \sim \text{Fourier}(I(l, m))$
 $C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} = 1 + |\gamma|^2$

EPIC





$$\theta \approx \frac{1}{\Delta k d} \sim \text{few mas}$$

$$[\vec{d} \cdot \vec{\theta} + L_i] e^{-i(\Delta k (\vec{d} \cdot \vec{\theta} + L_i)) / 4}$$

$$2L \approx -\vec{d} \cdot \vec{\theta}$$

$$\frac{F_b}{F_a} \gamma = \langle E_a E_b^* \rangle \sim \text{Fourier}(I(l, m))$$

$$C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} = 1 + |\gamma|^2$$

EPIC

$$\sigma_{\text{bright}} \sim 10 \mu\text{as}$$

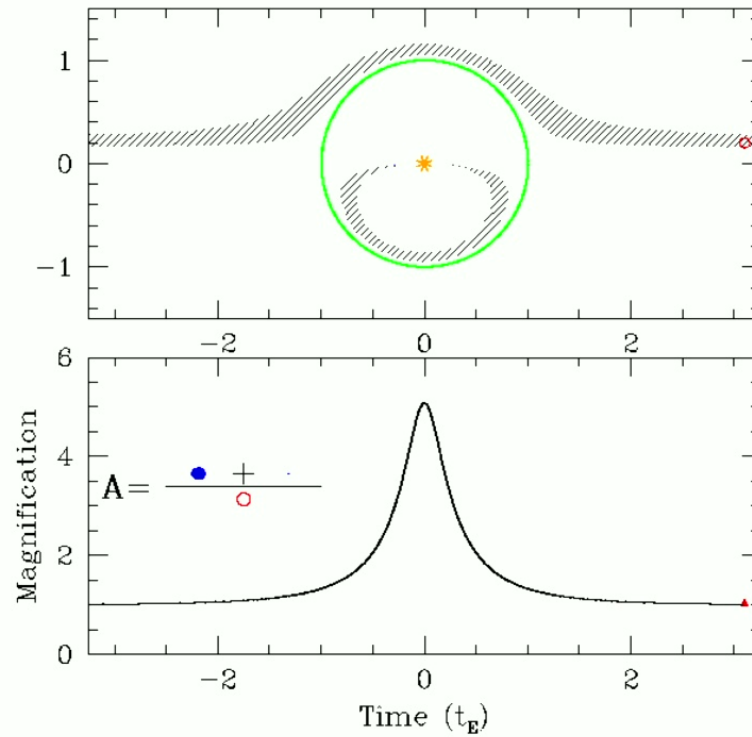
$$\frac{1}{k \sigma_{\theta}} \approx d$$

$$\sigma_{\text{Durs}} \sim \text{mas}$$

$$\frac{1}{k(\text{mas})} \sim 100 \text{m}$$

$$\sigma_{\theta} \sim \frac{1}{k d} \frac{1}{\text{SNR}}$$

Stellar Microlensing



$$\theta_E = \sqrt{\frac{4GM_L}{D_L} \frac{D_{LS}}{D_S}} \sim 3 \text{ mas} \sqrt{\frac{M_L \text{ kpc}}{M_\odot D_L}}$$

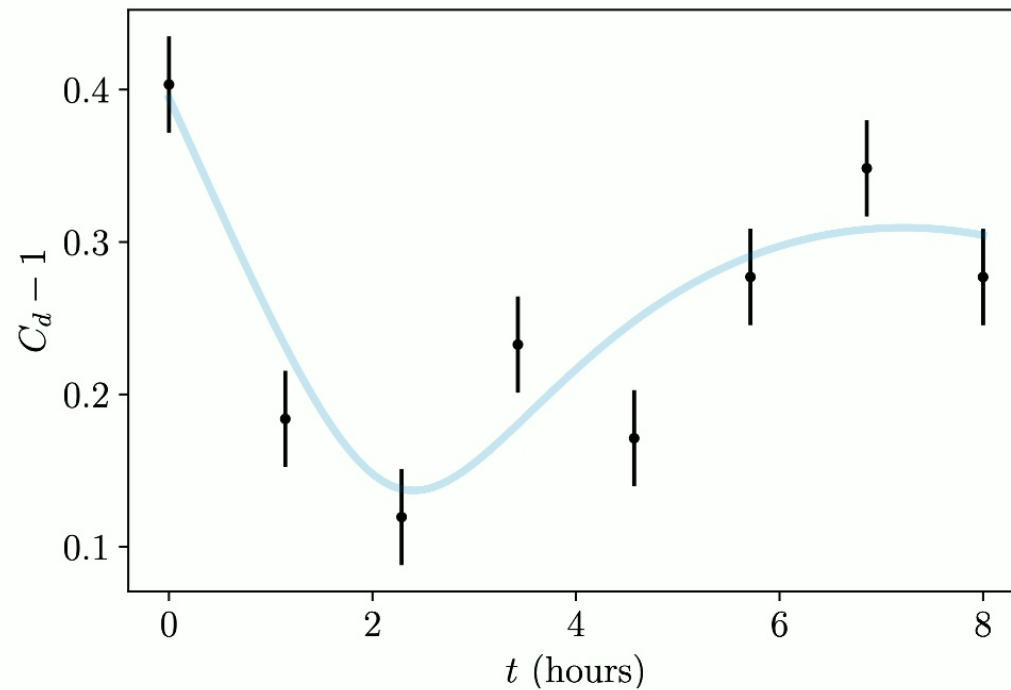
Stellar Microlensing

$$\theta_{\text{SL}} = \begin{pmatrix} \Delta\alpha^{\text{unl}} \\ \Delta\delta^{\text{unl}} \end{pmatrix} \left[\sqrt{0.5 + \frac{4\pi GM_{\text{L}} |\Delta\varpi|/c^2}{(\Delta\alpha^{\text{unl}} \cos \delta)^2 + (\Delta\delta^{\text{unl}})^2}} \right]$$

Quantity	Catalogue [84]	$d = 100$ m	$d = 800$ m
$\Delta\alpha_0$	46.7 mas	-	-
$\Delta\delta_0$	-46.5 mas	-	-
$\Delta\mu_{\alpha^*,\text{L}}$	108.04 mas/yr	-	-
$\Delta\mu_{\delta,\text{L}}$	-118.78 mas/yr	-	-
$\Delta\varpi$	11.4 mas	-	-
M_{L}	$1.3 M_{\odot}$	-	-
$\sigma_{\Delta\alpha}$	0.7 mas	0.08 mas	0.013 mas
$\sigma_{\Delta\delta}$	0.57 mas	0.03 mas	0.009 mas
$\sigma_{\Delta\mu}$	$\lesssim 10$ mas/yr	-	-
$\sigma_{\Delta\varpi}$	$\lesssim 1.6$ mas	-	-
$\sigma_{\theta_{\text{res}}}$	620 μas	54 μas	11 μas

Stellar Microlensing

$$\theta_{\text{SL}} = \left(\frac{\Delta\alpha^{\text{unl}}}{\Delta\delta^{\text{unl}}} \right) \left[\sqrt{0.5 + \frac{4\pi GM_L |\Delta\varpi|/c^2}{(\Delta\alpha^{\text{unl}} \cos \delta)^2 + (\Delta\delta^{\text{unl}})^2}} \right]$$



Intensity Interferometry

HBT

$$C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} - 1 \sim \sum_{\vec{k}} \cos(\vec{k} \cdot [\vec{d} \cdot \vec{\theta} + L]) e^{-\frac{(\Delta k \cdot (\vec{d} \cdot \vec{\theta} + L))^2}{4}} \times \epsilon_T^{\#} \epsilon_R^{\#}$$

$\vec{k} + (\Delta k)$ $\theta \approx \frac{1}{\Delta k d} \sim \text{few mas}$ $\Delta k \cdot d \cdot \sigma$
 $2L \approx -\vec{d} \cdot \vec{\theta}$ $\tau_c \sim fs$ $\tau_{res} \sim \text{tenths ns}$
 $\frac{F_a; F_b}{(F_a + F_b)^2} \sim \frac{F_b}{F_a}$ $\sigma_t \sim 10ps$
 $\gamma = \langle E_a E_b^* \rangle \sim \text{Fisher}(I(l, m))$
 $C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} = 1 + |\gamma|^2$ within $\frac{1}{\Delta k}$
 $\vec{d} \cdot \vec{\theta} - 2L = f(\epsilon)$

EPIC

$\sigma_{\text{bright}} \sim 10 \mu\text{as}$
 $\frac{1}{k \sigma_{\theta}} \approx d$
 $\sigma_{\text{dark}} \sim \text{mas}$
 $\frac{1}{k(\text{mas})} \sim 100 \text{m}$

$d \sim$
 $x \in T \in R$
 $t_{\text{res}} \sim \text{tenths ns}$
 $\sim \text{Fourier}(I(l, m))$
 δl^2

EPIC

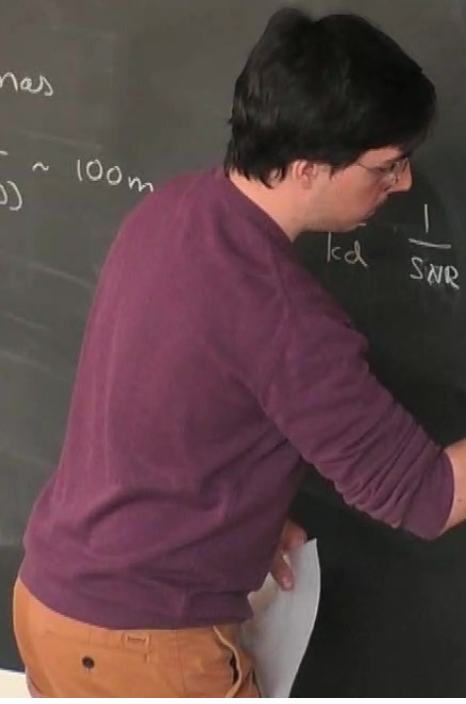
$\sigma_{\theta_{\text{res}}}^{\text{bright}} \sim 10 \mu\text{as}$

$\frac{1}{k \sigma_{\theta}} \approx d$

$\sigma_{\theta_{\text{res}}} \sim \text{mas}$

$\frac{1}{k(\text{mas})} \sim 100 \text{m}$

$100 \text{m} \downarrow \vec{\theta}_{\text{rel}}(t) = \theta$
 $C = \cos(k[|d| |\theta(t)| \cos \psi(t) - r \ell(t)])$
 $f(t) = d \theta \cos \psi = r \ell$
 $\cos(k f(t))$
 $\frac{\delta f}{\delta \theta} = \frac{\partial C}{\partial \theta}$



α
 $\# \in T \quad \# \in R$
 $\text{res} \sim \text{tenths ns}$
 Fourier ($I(l, m)$)

EPIC

$$\sigma_{\text{Obs}}^{\text{bright}} \sim 10 \mu\text{as}$$

$$\frac{1}{k \sigma_{\theta}} \approx d$$

σ_{θ}

100m

100m

$$\vec{\theta}_{\text{rel}}(t) = \theta$$

$$C = \cos(k [d | \theta(t) | \cos \psi(t) - r \ell(t)])$$

$$f(t) = d \theta \cos \psi = r \ell$$

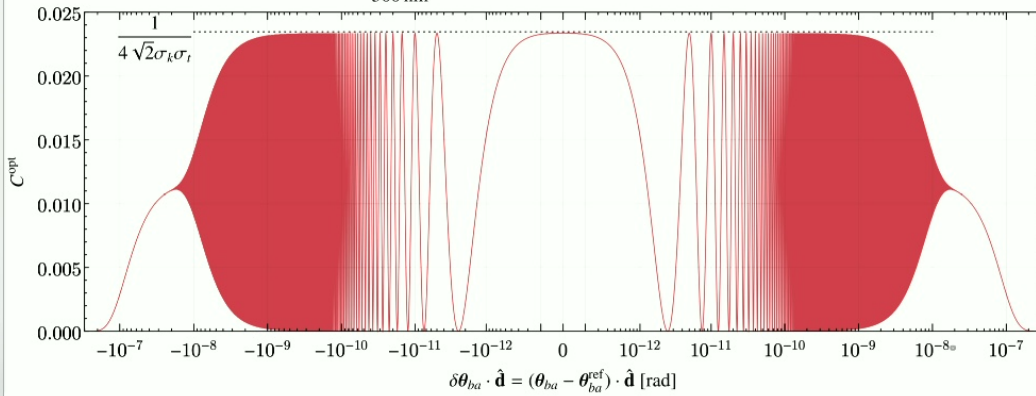
$$\cos(k f(t))$$

$$\sigma_{\theta} \sim \frac{1}{k d} \frac{1}{\text{SNR}}$$

$$\sigma_{\theta}^2 = \sum_i \left(\frac{\partial C}{\partial x_i} \delta x_i \right)^2$$

Correlation - Extended FOV

$$d = 100 \text{ km}, \bar{k} = \frac{2\pi}{500 \text{ nm}}, \sigma_k = \bar{k}/5000, \sigma_t = 10 \text{ ps}$$



Yale University, High Energy Particle Theory Seminar, Feb 7, 2023

100m
 \downarrow
 $\vec{\theta}_{\text{rel}}(t) = \theta$

$C = \cos(k[|d| |\theta(t)| \cos \psi(t) - z \ell(t)])$

$f(t) = d\theta \cos \psi \rightarrow z \ell$

$\cos(k f(t))$

$\frac{1}{\text{SNR}}$

$\sigma_{\theta}^2 = \sum_i \left(\frac{\partial C}{\partial x_i} \delta x_i \right)^2$

$\delta \ell = \frac{1}{k}$

$\delta \ell = \vec{d} \cdot \vec{\delta \theta}$

$\delta \ell = \vec{d} \cdot \delta \vec{\theta}$ within $\frac{1}{k}$

Correlation -

$d = 100 \text{ km}, k = \frac{2\pi}{500 \text{ nm}}, \sigma_k = k/5$

$4\sqrt{2}\sigma$

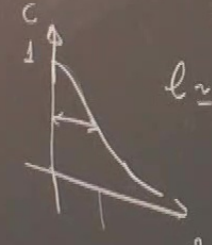
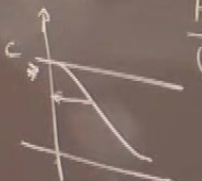
Yale University, High Energy

Intensity Interferometry

HBT

$$C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} - 1 \sim \frac{\sum_i A_i \cos(\vec{k} [\vec{d} \cdot \vec{\theta} + L_i]) e^{-\frac{(\Delta k (\vec{d} \cdot \vec{\theta} + L_i))^2}{4}}}{\langle I_1 \rangle \langle I_2 \rangle} \times \epsilon_T^\# \epsilon_R^\#$$

$\bar{k} + (\Delta k)$ $\theta \gtrsim \frac{1}{\Delta k d}$ ~ few mas $\Delta k \sim d^{-1}$
 $\tau_c \sim fs$ $\sigma_t \sim 10ps$ $t_{res} \sim \text{femtoseconds}$
 $2L \approx -\vec{d} \cdot \vec{\theta}$ $\gamma = \langle E_a E_b^* \rangle$ ~ Fourier $(I(\ell, m))$
 $\frac{F_a F_b}{(F_a + F_b)^2} \sim \frac{F_b}{F_a}$ $C = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} = 1 + |\gamma|^2$
 $\ell \approx -\vec{d} \cdot \vec{\theta}$ within $\frac{1}{\Delta k}$
 $\vec{d} \cdot \vec{\theta} - 2L = f(\epsilon)$



EPIC

$\sigma_{\theta_{broad}} \sim 10 \mu\text{as}$
 $\frac{1}{k \sigma_\theta} \approx d$
 $\sigma_{\theta_{mas}} \sim \text{mas}$
 $\frac{1}{k(\text{mas})} \sim 100m$
 $C = \cos(\dots)$
 $\delta l = \lambda$
 $\delta l = -\vec{d} \cdot \vec{\theta} = \lambda$
 $\sigma_\theta \sim \frac{1}{kd} \sim \frac{1}{SNR}$

EPIC

$$\sigma_{\Theta_{\text{bright}}} \sim 10 \mu\text{as}$$

$$\frac{1}{k \sigma_{\Theta}} \approx d$$

$$\sigma_{\Theta_{\text{mas}}} \sim \text{mas}$$

$$\frac{1}{k(\text{mas})} \sim 100 \text{m}$$

$$\delta l = \lambda$$

$$\delta l = -\vec{d} \cdot \delta \vec{\Theta} = \lambda$$

$$\sigma_{\Theta} \sim \frac{1}{k d} \frac{1}{\text{SNR}}$$

$$\begin{matrix} 100 \text{m} \\ \downarrow \\ \vec{\Theta}_{\text{rel}}(t) = \Theta \end{matrix}$$

$$C = \cos(k[|d| |\Theta(t)| \cos \psi(t) - z \ell(t)])$$

$$\cos \psi = z \ell$$

$$f(t)$$

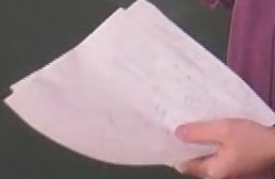
$$100 \text{m} \cdot 500 \mu\text{mas} \sim 100 \cdot 5 \cdot 10^{-7}$$

$$\delta l = \frac{1}{k}$$

$$\delta l = \vec{d} \cdot \delta \vec{\Theta}$$

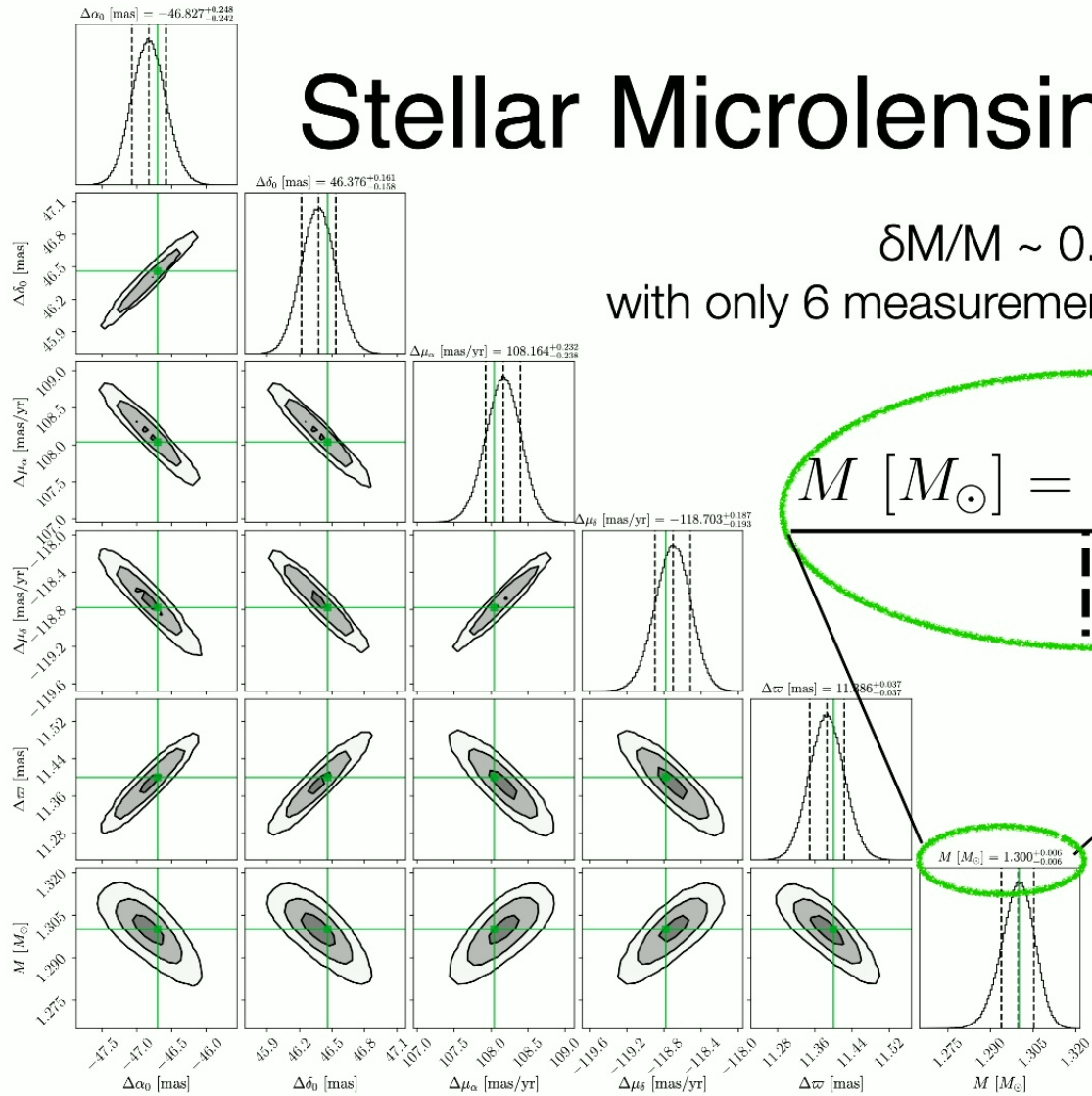
$$\delta l = \vec{d} \cdot \delta \vec{\Theta}$$

within $\frac{1}{k}$



Stellar Microlensing

$\delta M/M \sim 0.4\%$
with only 6 measurements at $\delta\theta \sim 10\mu\text{as}$!

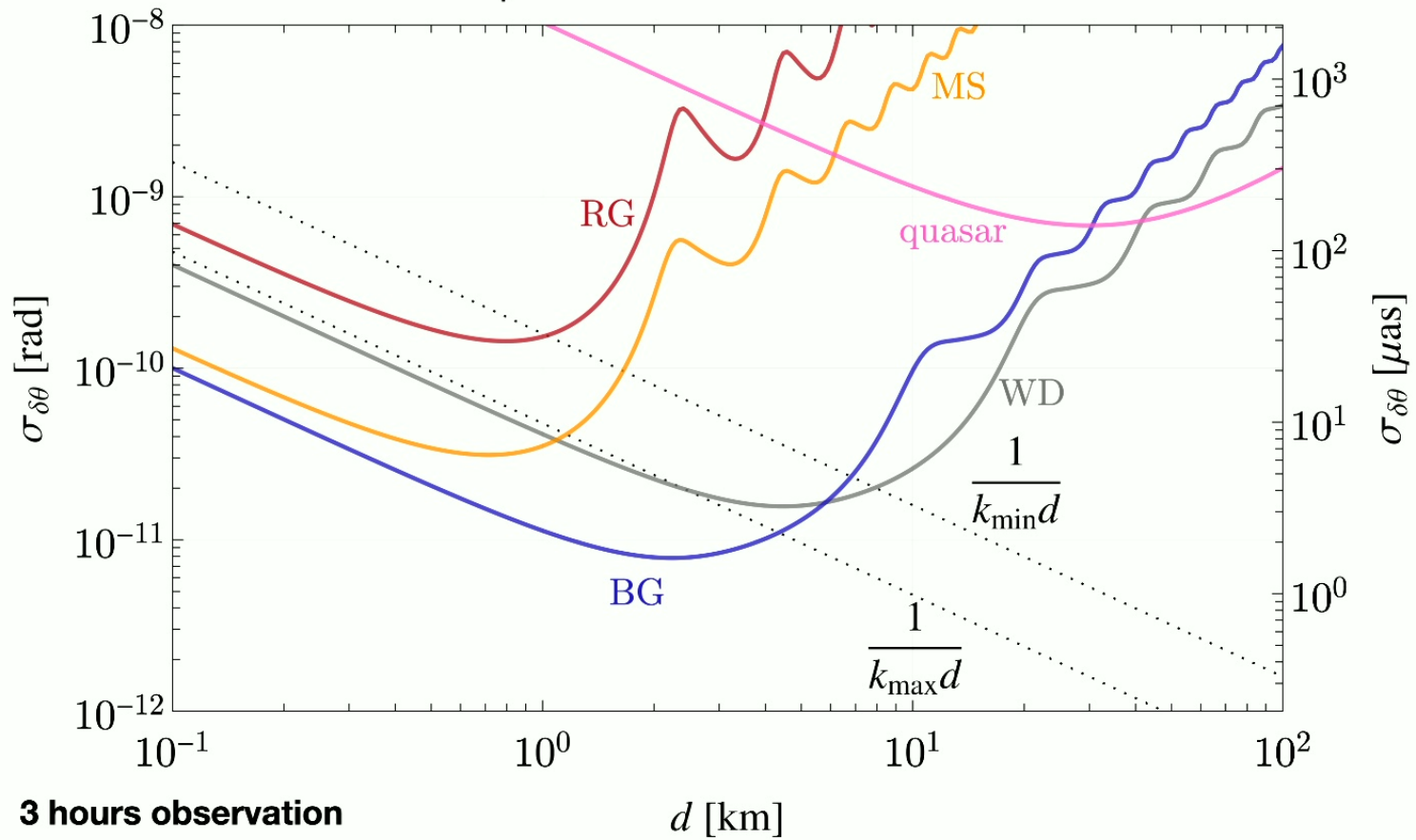


$$M [M_\odot] = 1.300^{+0.006}_{-0.006}$$

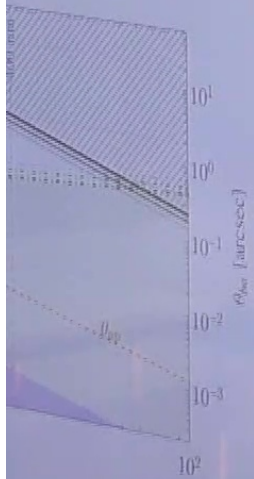
$$M [M_\odot] = 1.300^{+0.006}_{-0.006}$$

Light-Centroiding Precision

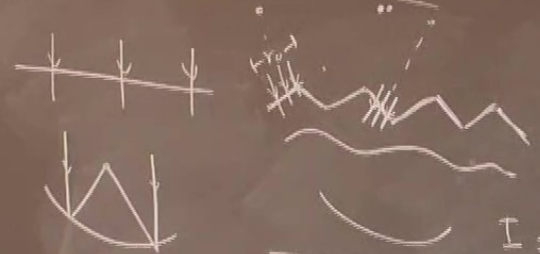
$$A = \frac{\pi}{4}(4 \text{ m})^2, \bar{k}/\sigma_k = 5000, \sigma_t = 10 \text{ ps}$$



Comparisons



Intensity Interferometry



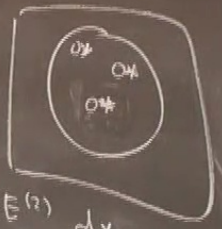
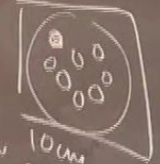
$$C \sim \dots e^{-\left(\frac{\theta_{ab}}{\theta_{iso}}\right)^{1/3}}$$

$$l = d \theta_{ab}$$

$$I = \int |E^{(1)}|^2 dx_{p_1} \int |E^{(2)}|^2 dx_{p_2}$$

$$\otimes E_a^{(1)} E_a^{(2)} E_b^{(1)*} E_b^{(2)}$$

$$\theta_{iso} \sim \lambda / r \sim \theta_{iso}^2 \frac{r_0}{h} \sim \frac{10 \text{ cm}}{10 \text{ km}} \sim 2.5 \text{ as}$$



$$e^{i(\phi_a^{(1)} - \phi_a^{(2)} - \phi_b^{(1)} + \phi_b^{(2)})}$$

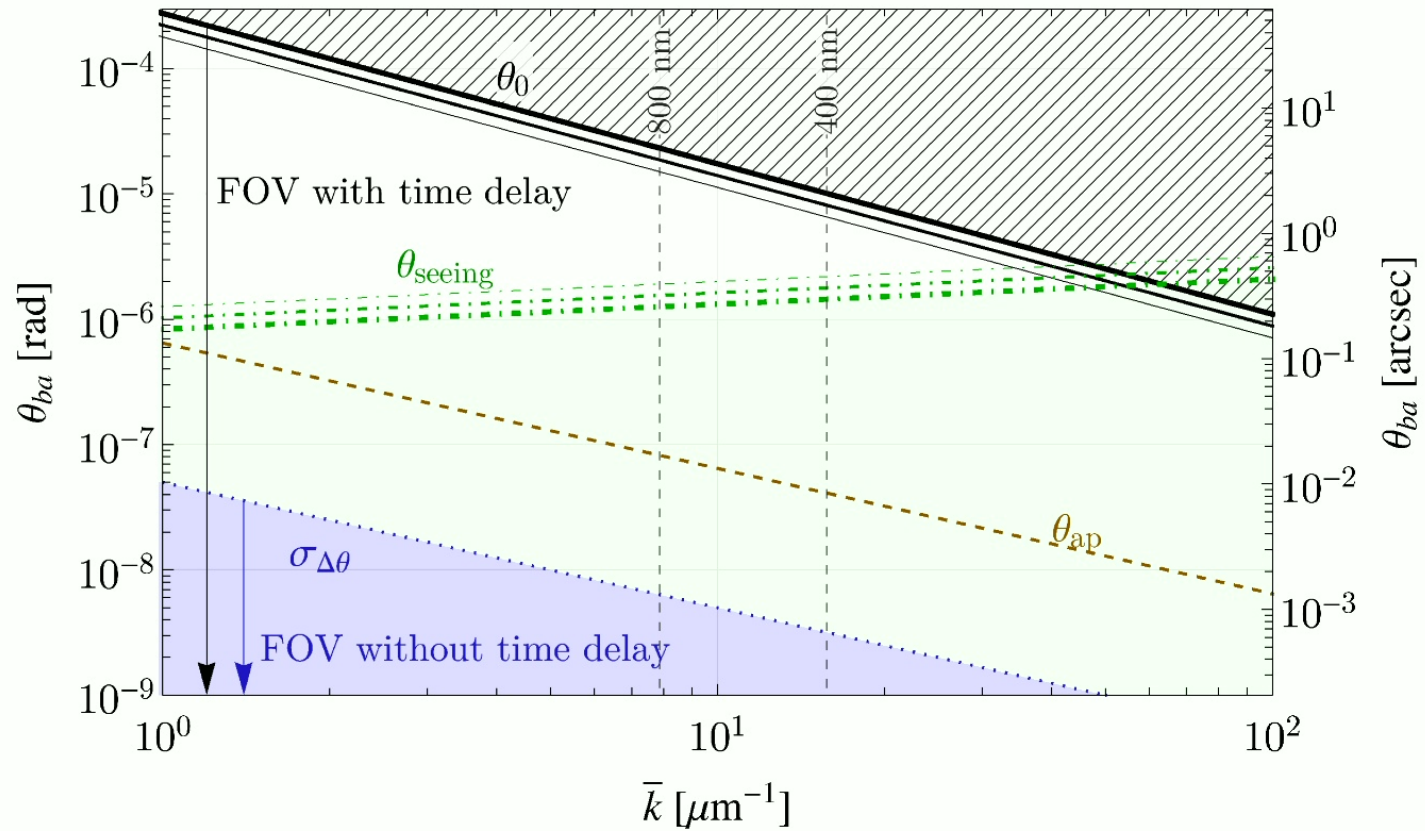
EPIC

$$\sigma_{\theta_{min}}^{\text{bright}} \sim \frac{1}{L \sigma_{\theta}} \approx d$$

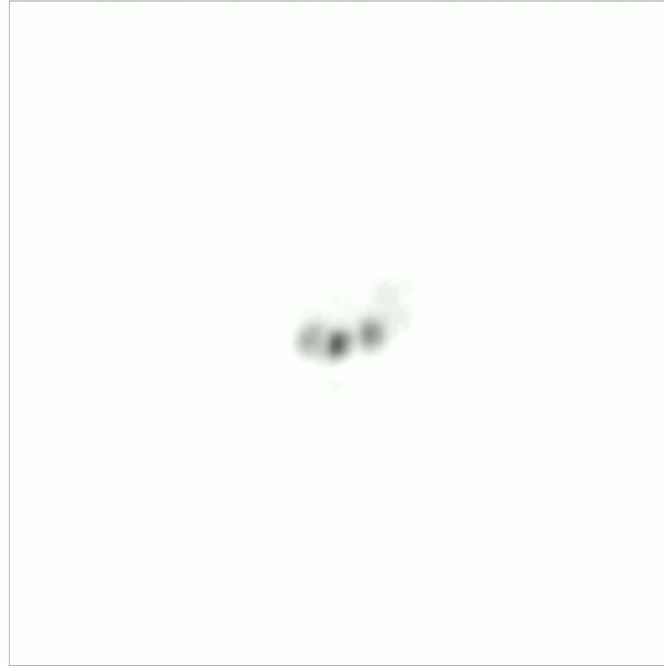
$$\sigma_{\theta_{min}} \sim \text{mas}$$

$$\frac{1}{L(\text{mas})} \sim$$

Limiting separations



Astronomical Seeing



$$r_0 \lesssim 30 \text{ cm} \Rightarrow \sigma_{\theta_{\text{res}}} \gtrsim 0.4 \text{ arcsec}$$

Seeing Blurring

