

Title: Quantum error-correction and quantum gravity

Speakers: Beni Yoshida

Series: Colloquium

Date: April 05, 2023 - 2:00 PM

URL: <https://pirsa.org/23040082>

Abstract: In this colloquium, I will review how the notion of quantum error-correction has transformed our understanding of quantum gravity in the past decade.

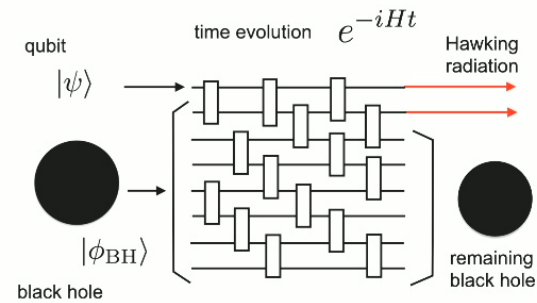
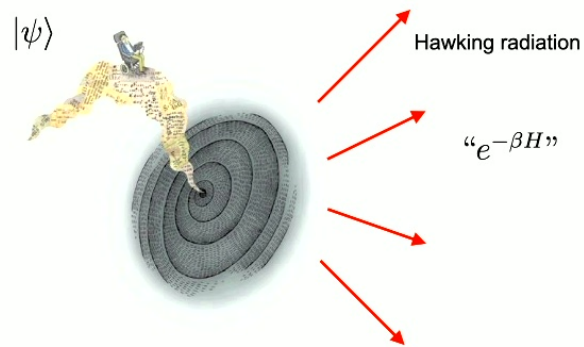
Zoom link: <https://pitp.zoom.us/j/94349082665?pwd=OFdJdkpHU1NEcm1NeW5pWlg4WmNBZz09>

# Quantum error-correction in quantum gravity

[Beni Yoshida](#) (Perimeter Institute)

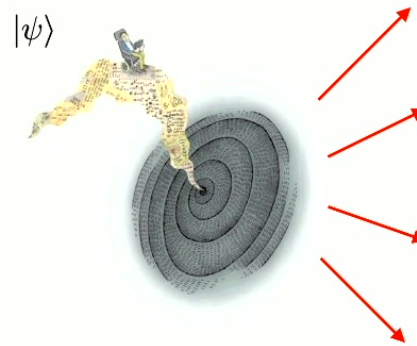
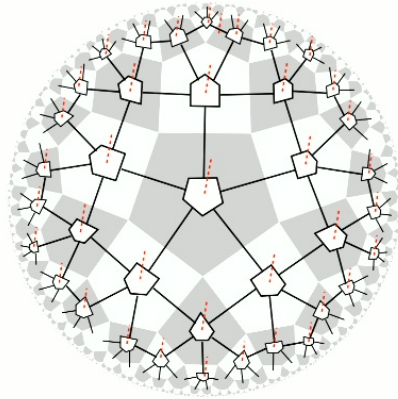
# Quantum Information in Gravity

- ❖ Quantum mechanics and general relativity are in **serious conflicts**, e.g. information loss puzzle, firewall puzzle, etc...
- ❖ These are questions of **quantum information theory**.



## Quantum Error-Correction in Gravity ?

- ❖ Stores quantum information **non-locally** into many-body degrees of freedom. Local measurements/errors cannot destroy/reveal the hidden information.
- ❖ **Quantum gravity seems to hide quantum information**, like a quantum error-correcting code.

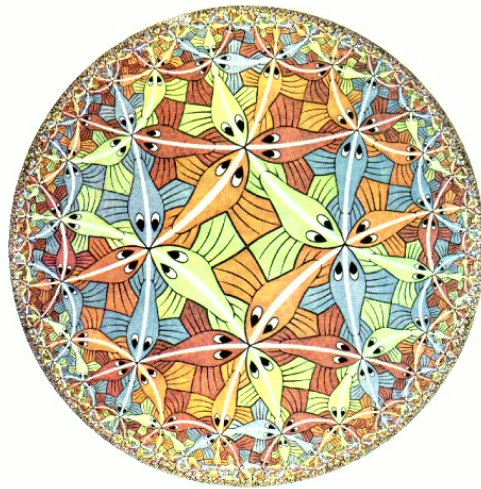


# Overview

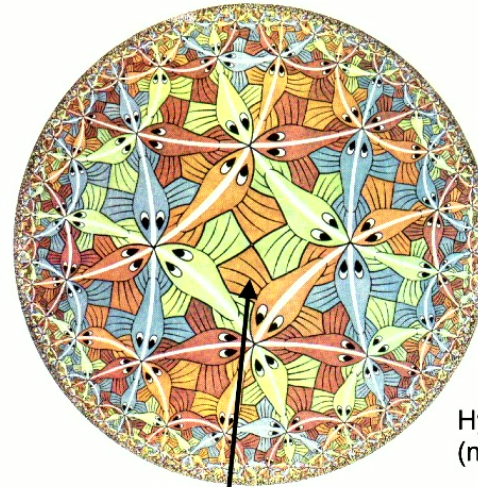
- ❖ **Bulk-boundary mapping** in the AdS/CFT correspondence, and beyond
  - Holographic quantum error-correcting code (Harlow-Pastawski-Preskill-BY 2015)
  - Holographic scattering (May-Sorce-BY 2022)
- ❖ **Quantum information scrambling** and black holes
  - Information recovery from black hole (Hosur-Qi-Roberts-BY 2015, BY-Kitaev 2017)
  - Firewall puzzle and black hole interior (BY 2019)

# AdS/CFT correspondence

❖ Quantum gravity in bulk = CFT on boundary ?



Boundary D-dimensional conformal field theory (without gravity)



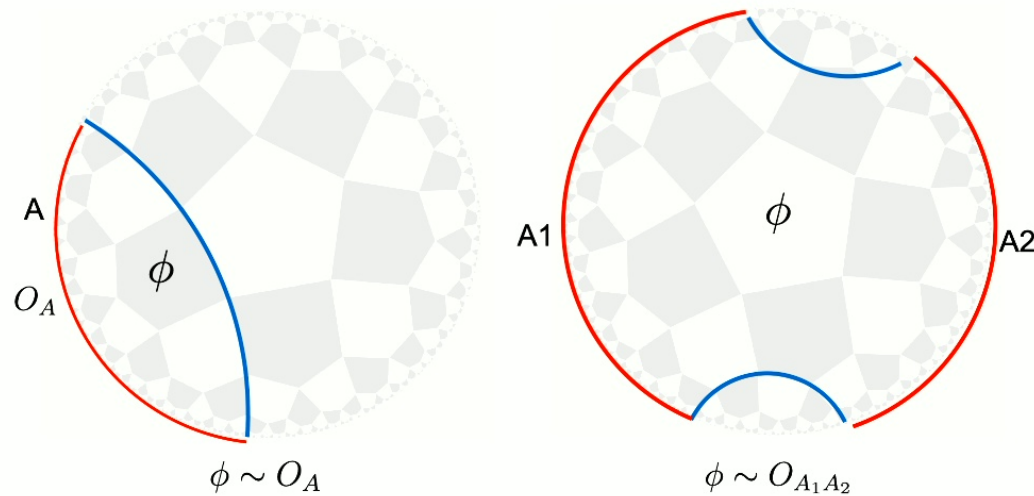
Bulk (D+1)-dimensional theory with gravity on AdS space

Hyperbolic space (negatively curved)

# Bulk operator vs boundary operator

## ❖ Entanglement wedge reconstruction

A bulk operator  $\phi$  can be represented by some integral of local boundary operators supported on A if  $\phi$  is contained inside the **entanglement wedge** of A.

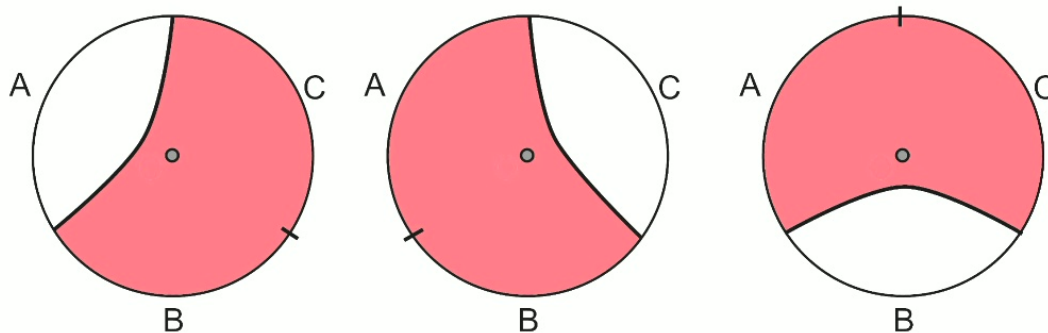


- “Proven” by using a generalized RT formula (Jefferis et al)
- **No explicit recipe is known** for more than one intervals

## Bulk locality puzzle

♣ The reconstruction recipe leads to a paradox

- All the bulk operators must correspond to **identity operators** on the boundary ?



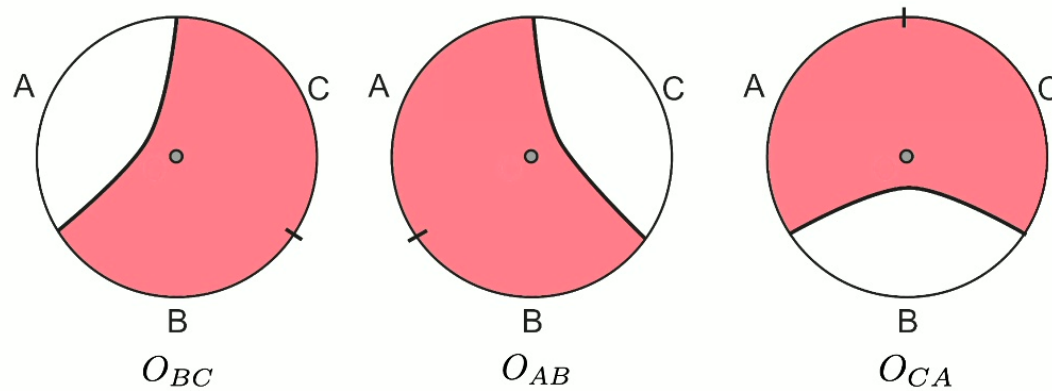
If so, the AdS/CFT seems very boring ...

(Almheiri-Dong-Harlow)



## Quantum error-correction in AdS/CFT ?

❖ The AdS/CFT correspondence can be viewed as a [quantum error-correcting code](#).



They are different operators, but [act in the same manner](#) in a low energy subspace.

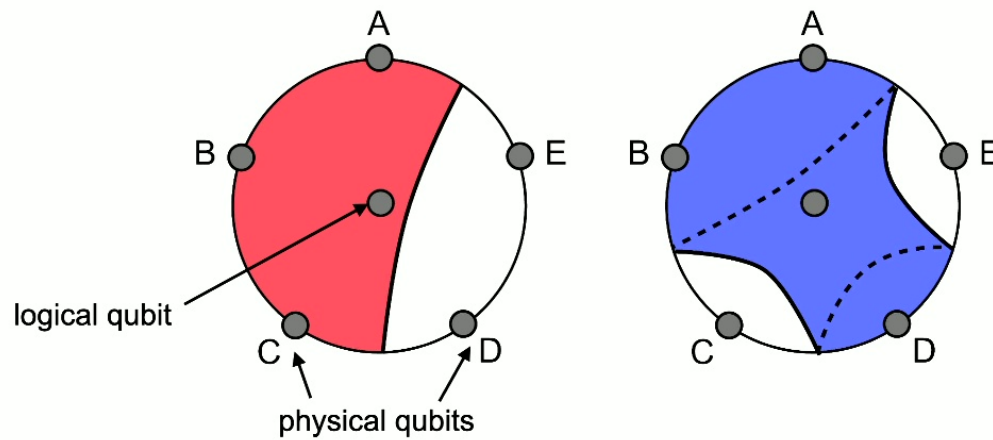
cf. [Quantum secret-sharing code](#)

## A simple toy model ?

1 bulk qubit  
5 boundary qubits

in total, just 6 qubits

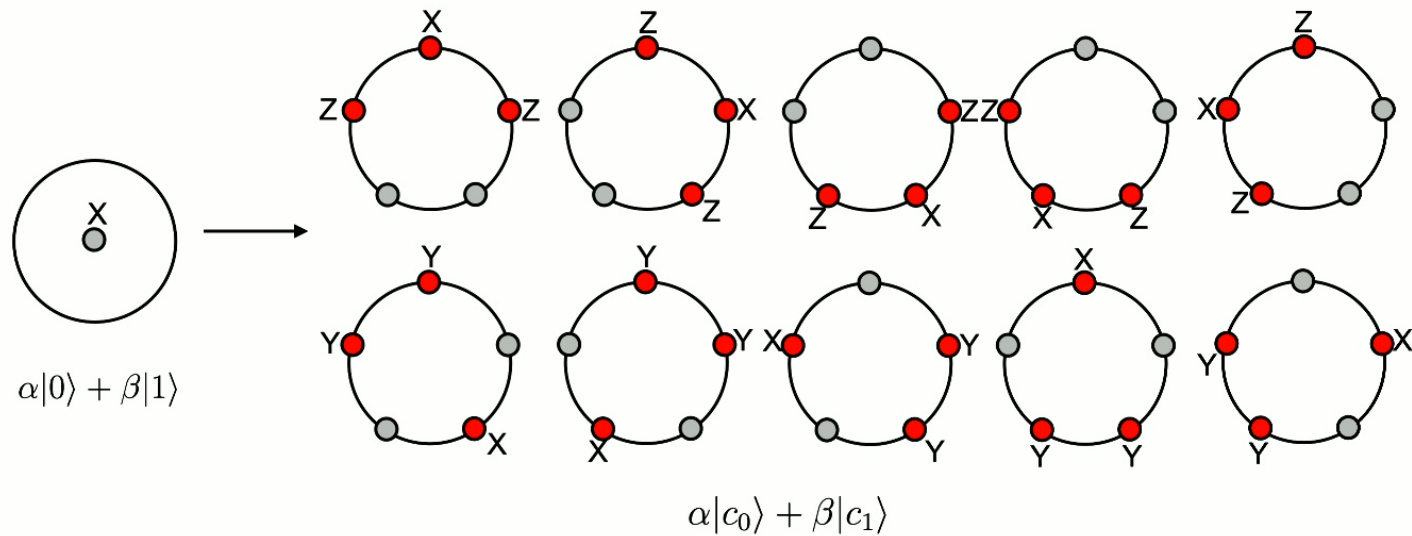
A bulk operator must have representations on any region with three qubits.



Entanglement wedge reconstruction !

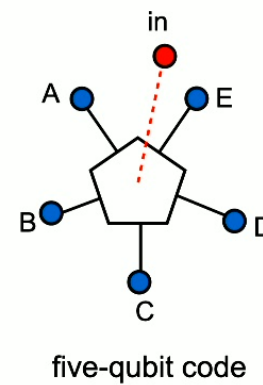
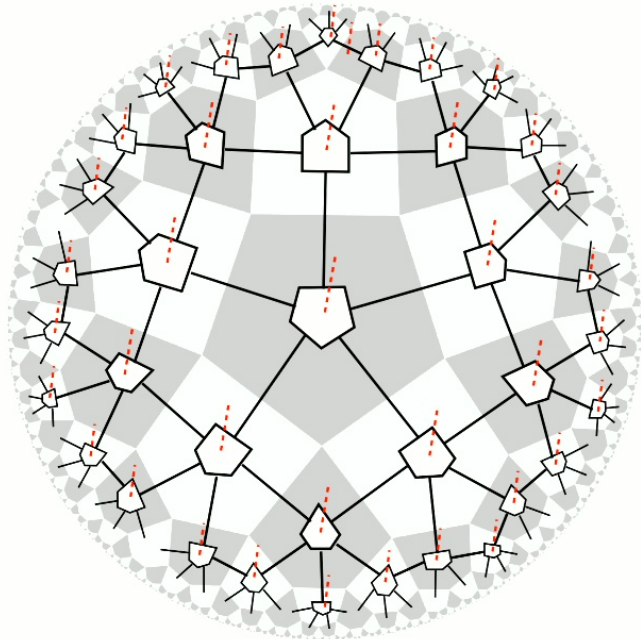
# Five-qubit code

♣ Pauli X operator in the input (bulk) corresponds to following 3-body operators.



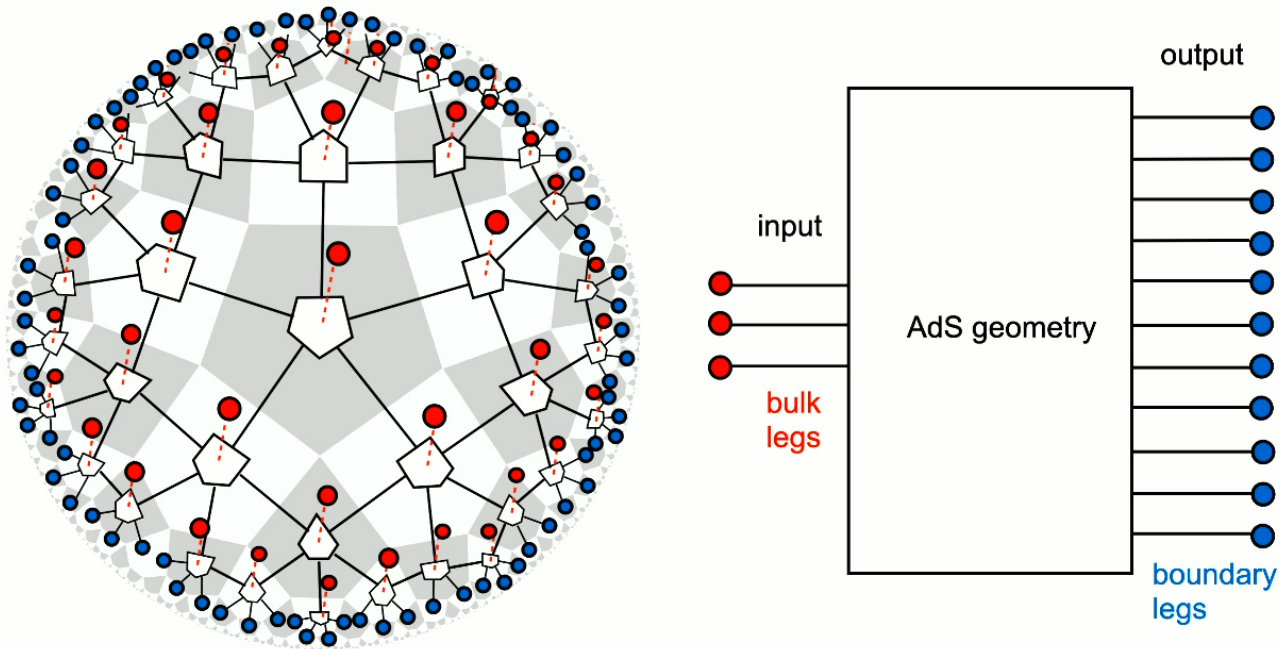
# Holographic quantum error-correcting code

- ♣ A tiling of the five qubit code via tensor network technique



# Holographic quantum error-correcting code

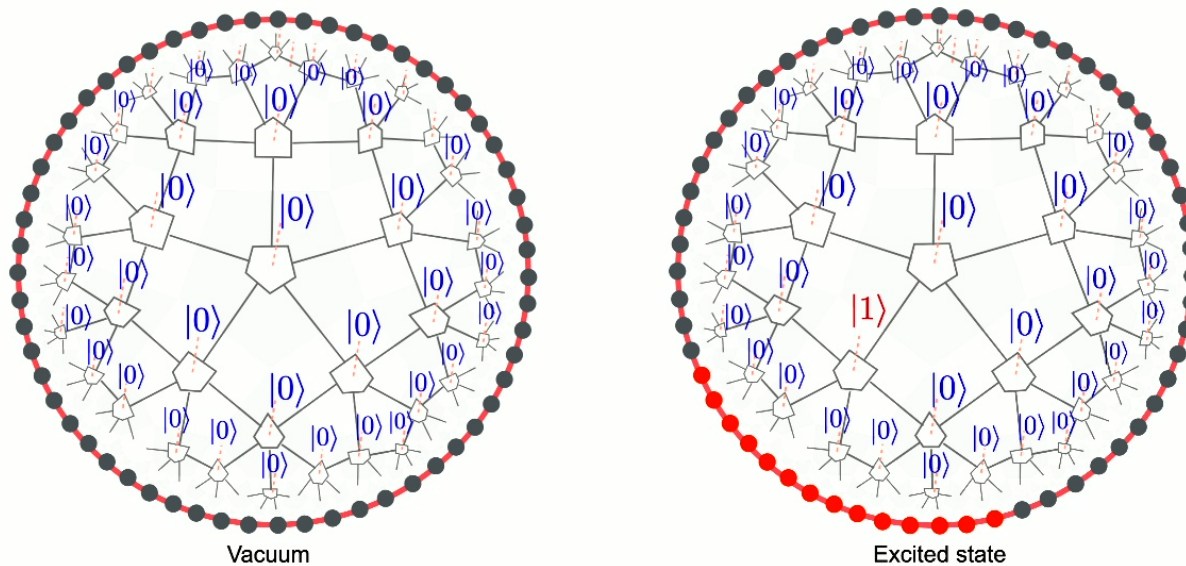
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\* Tensor network and AdS/CFT : Vidal07, Swingle12, Qi13, Czech et al15 ...

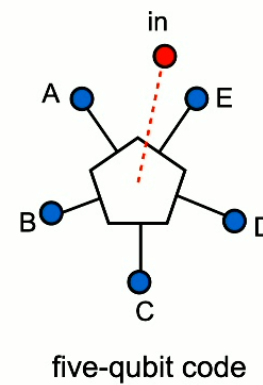
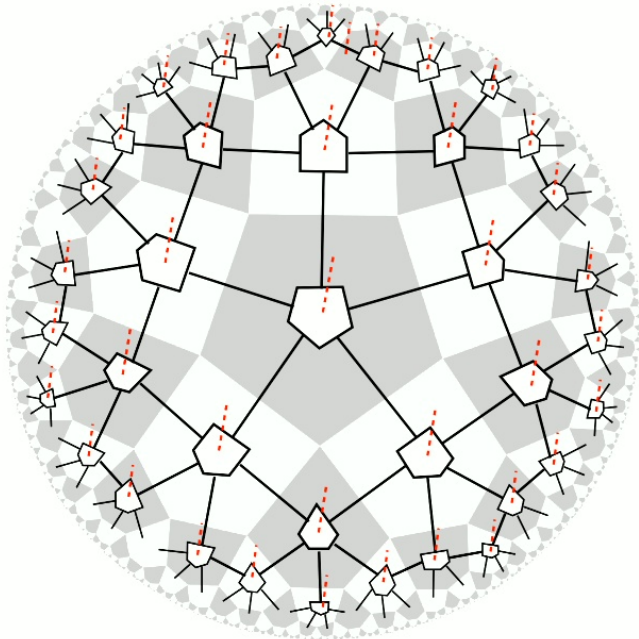
# Physical interpretation

- ❖ Qubits on the bulk represent **matter fields**, coupled to **the geometry** (via tensors).
- ❖ Perturbations around a fixed geometry.



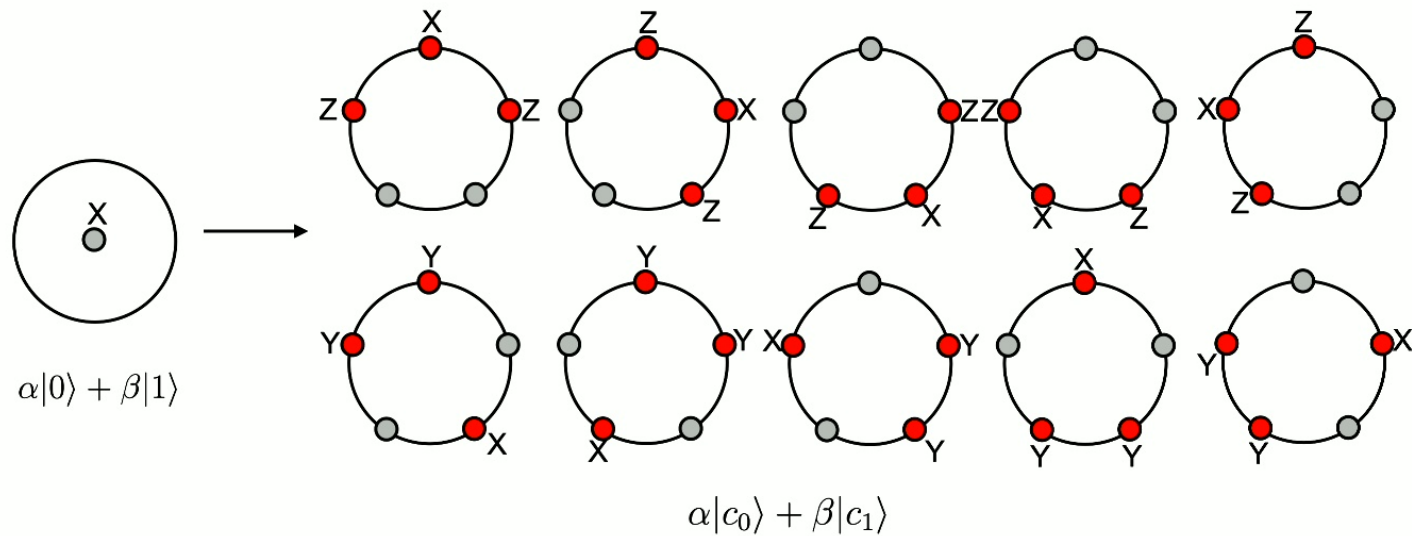
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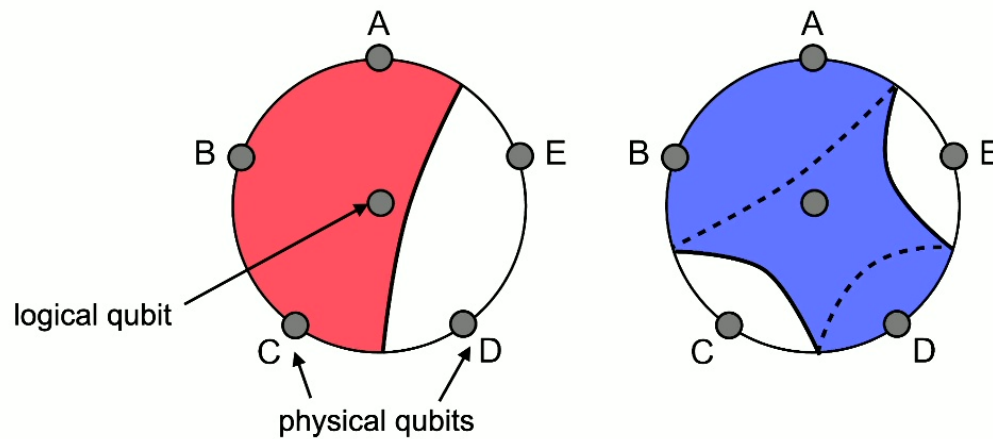


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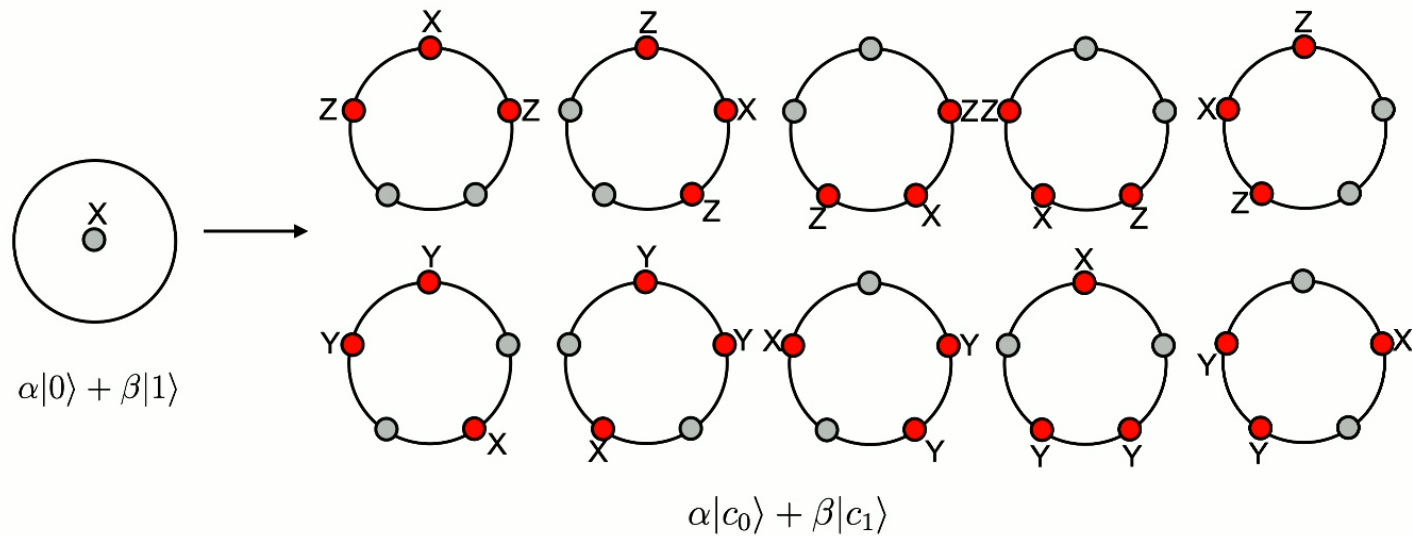
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Entanglement wedge reconstruction !

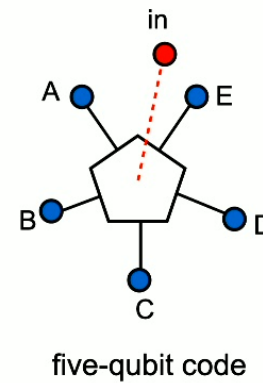
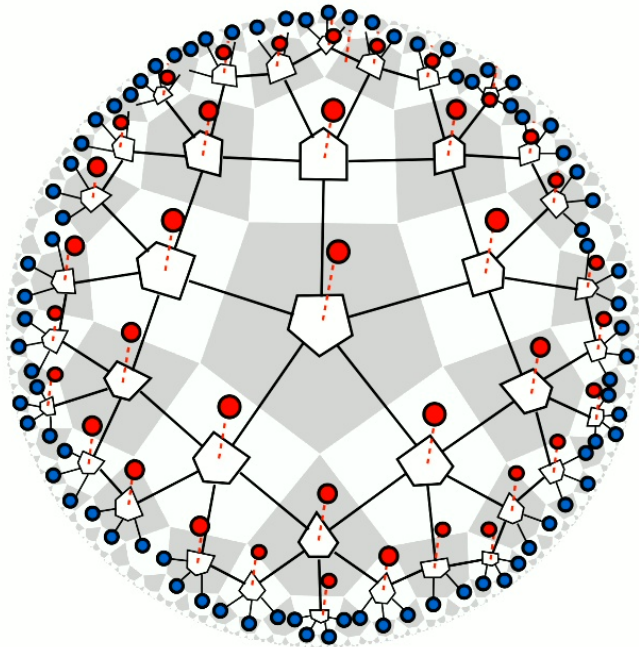
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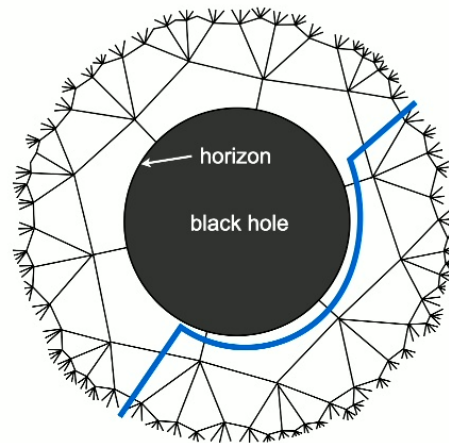


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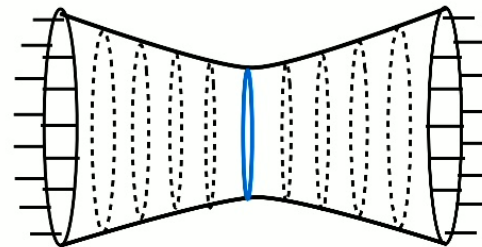
# Aspects of holographic tensor networks

- ❖ Toy model becomes more “realistic” by using **Haar random tensors**.
  - Entanglement growth and operator growth in many-body physics.
- ❖ Toy models of **black holes**.
  - Complexity = Volume = Action? (**number of tensors = complexity?**)
  - “Page curve” derivation

One-sided black hole



Two-sided black hole

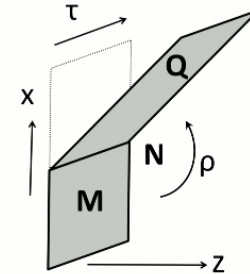


Einstein-Rosen bridge

## Some of ongoing works

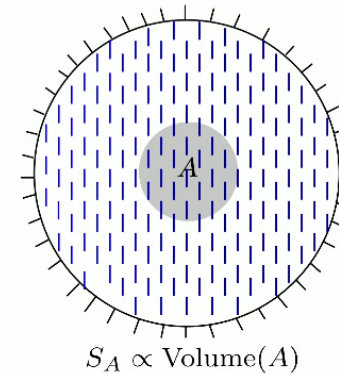
### ♣ Spacetime with End-of-World branes

- Projective measurements ? (Takayanagi et al)
- Causality violation ? (Omiya-Wei)



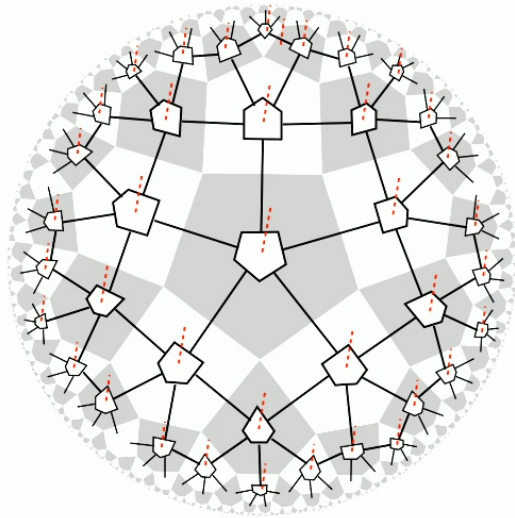
### ♣ de Sitter space

- Emergence of “dark force” (Verlinde)
- Puzzles about de Sitter horizon

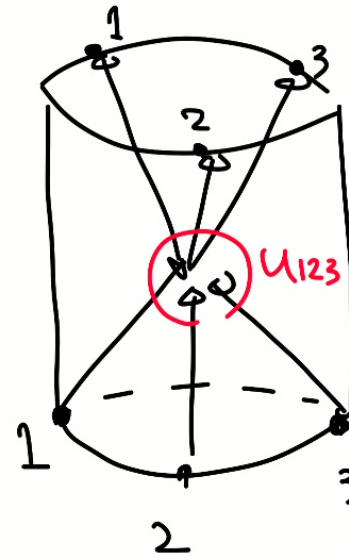


# Emergence of interaction

♣ Spacetime from entanglement



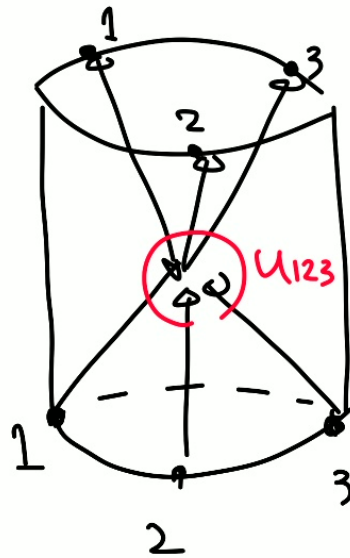
♣ Interaction from entanglement ?



[May 2019]

# Holographic scattering

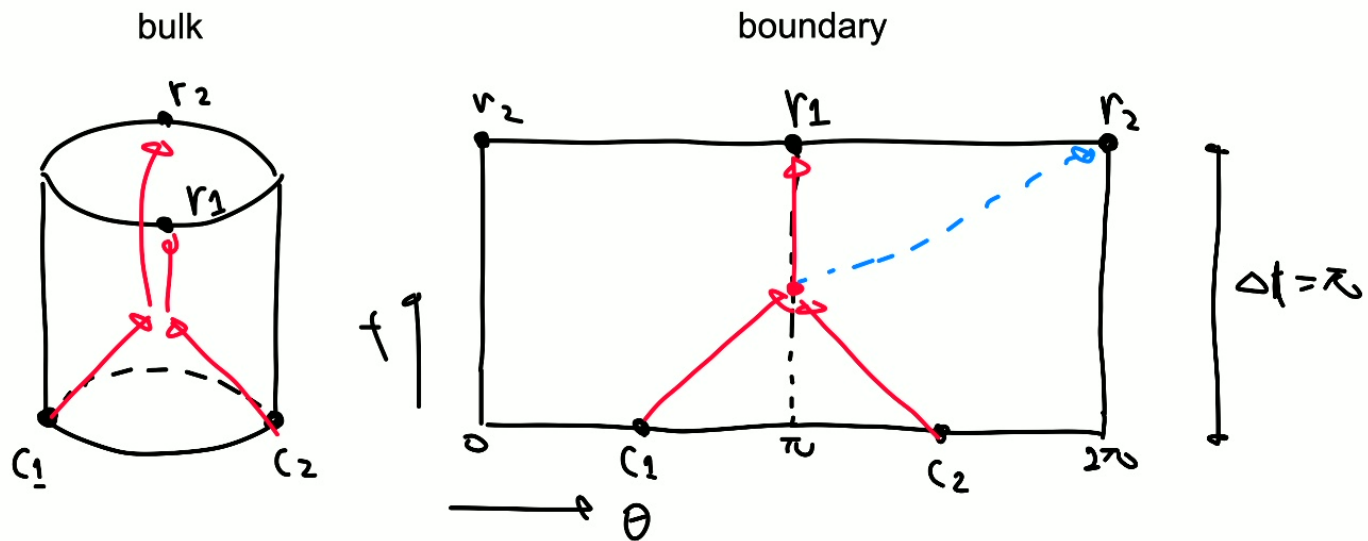
- ❖ How are **interactions** induced on the boundary quantum systems?



In principle, arbitrary unitary should be realizable.

# Boundary causality puzzle

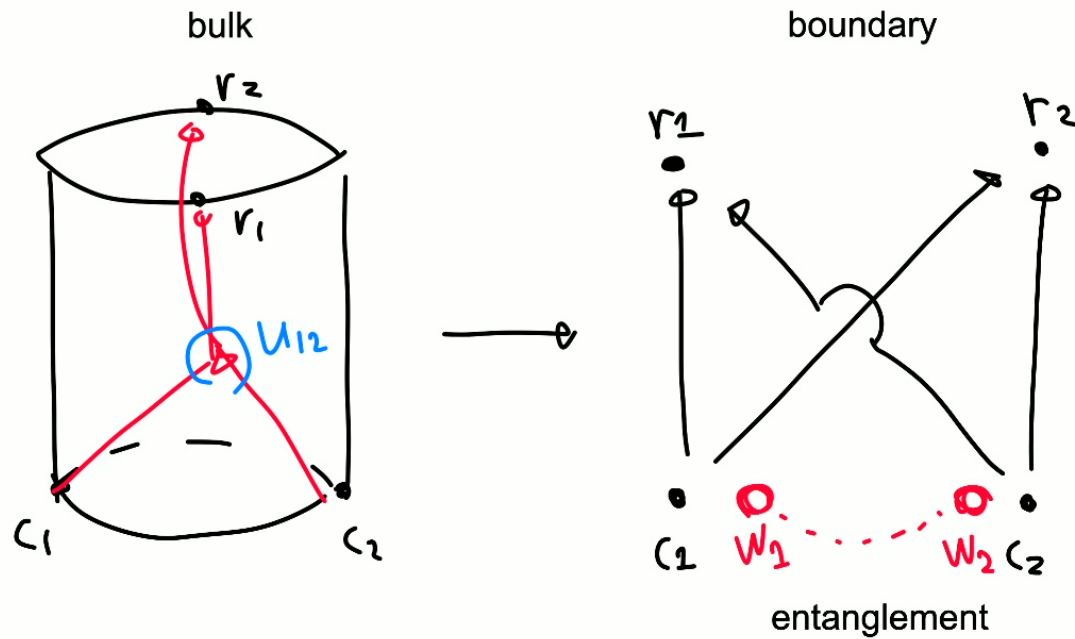
- ❖ On the boundary, there is **not enough time** for particles to interact.
  - Particles in the AdS/CFT correspondence must be **non-interacting... !?**





# Non-local quantum computation

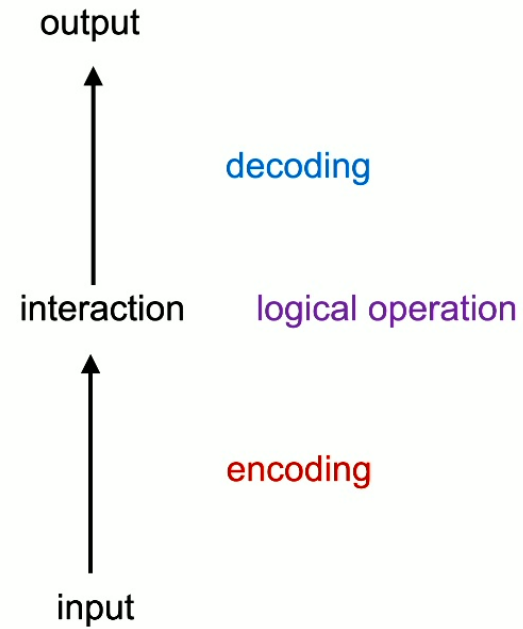
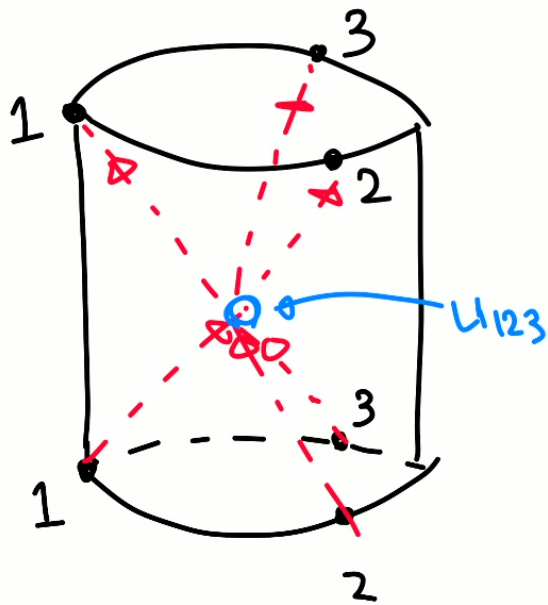
- ❖ By using the **pre-shared entanglement**, (in principle) one can induce arbitrary unitary interactions.



[May 2019]

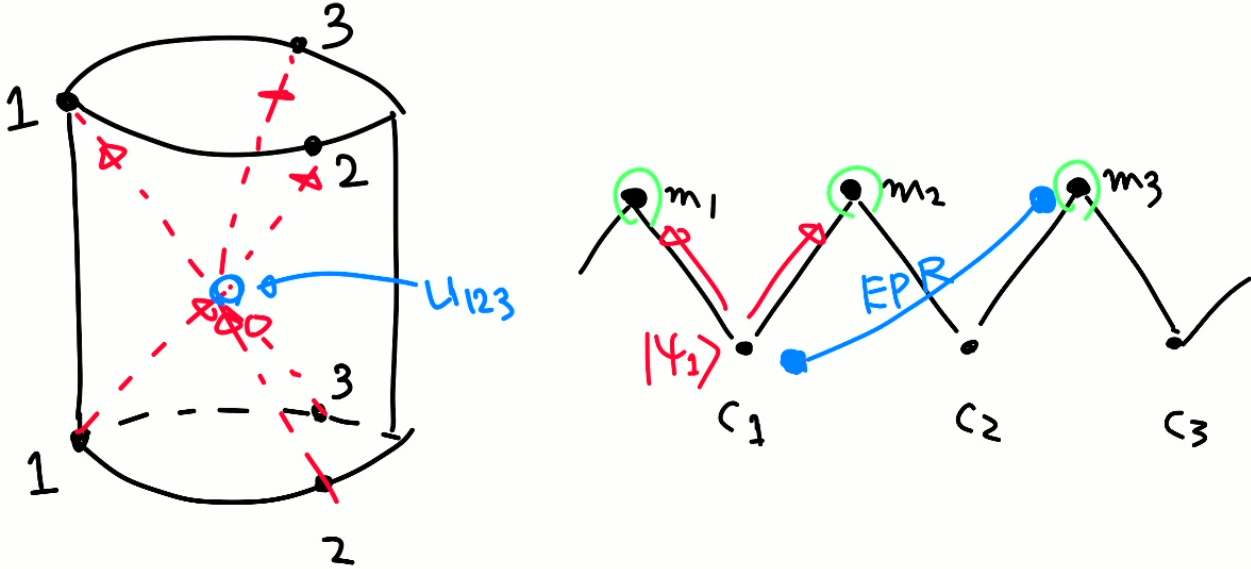
# Scattering and quantum error-correction

- ❖ Interactions must occur in a quantum error-correcting code.



# Entanglement-assisted quantum error-correction

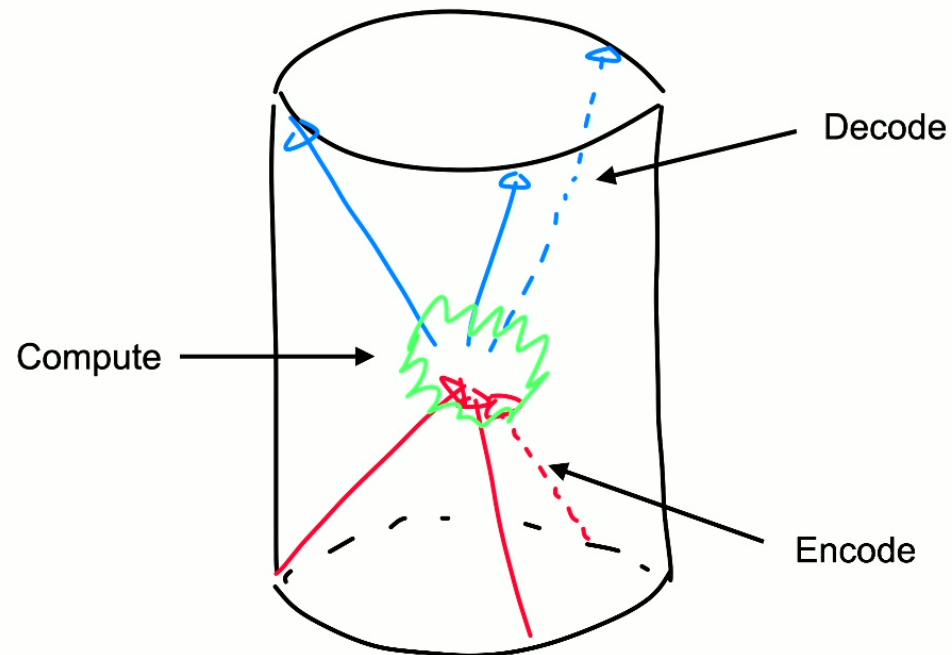
- ❖ Pre-existing entanglement delocalizes the input to the whole system
  - **Non-local encoding** is possible. Interactions are induced by **transversal logical operators**.



## like a quantum computer...

❖ This is how a **fault-tolerant quantum computer** works.

- Creating a **black hole** is an error that spoils the quantum computation ?



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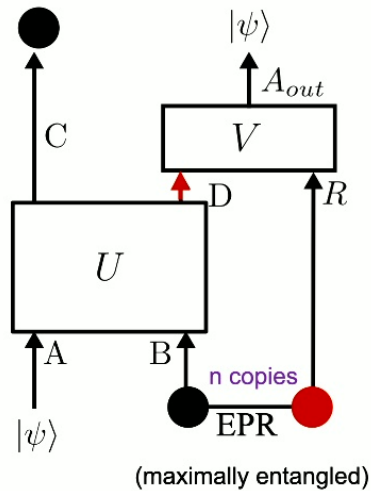
# Hayden-Preskill thought experiment

♣ Alice throws an unknown quantum state into an **old black hole**. Bob collects the Hawking radiation and **reconstructs the original state**.

Bob has an access to **both** early and late radiations !

- Bob needs to collect **just a few qubits from D**.

(Hayden-Preskill 2007)



C : Remaining BH  
D : Late radiation  
R : Early radiation

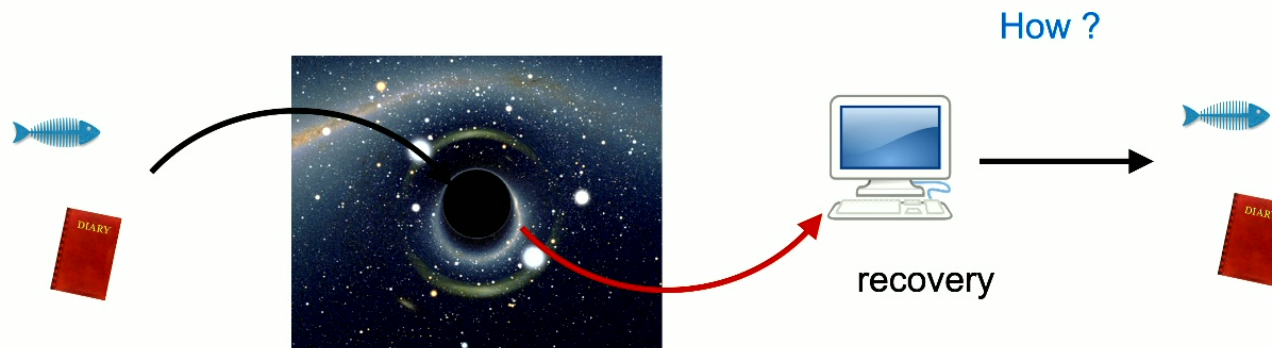
# Can we really recover information?

## ✿ Haar random unitary

$$e^{iHt} \approx \text{Haar random unitary}$$

Does it really work for **actual black holes**?

## ✿ How do we **actually recover** information?



# Scrambling is *operator* growth

## ✦ Operator growth

Size of operators becomes bigger under chaotic time-evolution.

$$e^{-iHt} \quad \bullet \quad \bullet \quad \bullet \quad \bullet \quad \bullet \quad \bullet \quad \bullet \quad W(t)$$



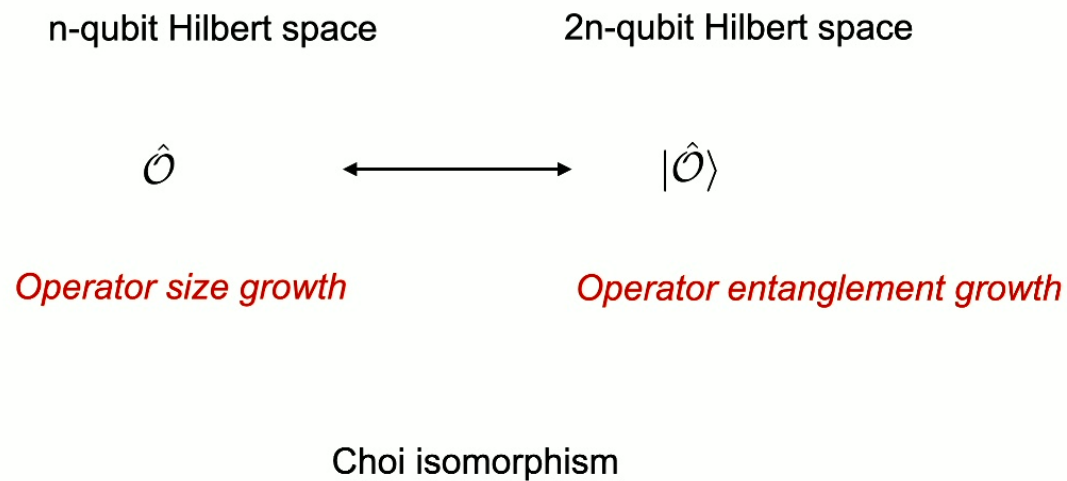
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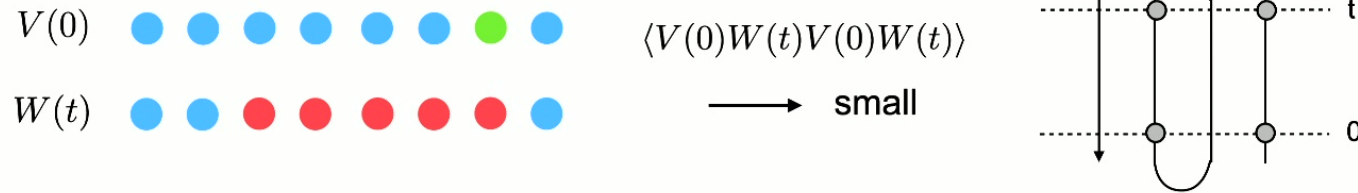
$$e^{-iHt} \quad \bullet \quad \bullet \quad \bullet \quad \bullet \quad \bullet \quad \bullet \quad \bullet \quad W(t)$$

- Operator-to-state mapping (Hosur-Qi-Roberts-BY15)



# Out-of-time order correlation function

## ❖ Out-of-time order correlator (Kitaev)



## ❖ Black hole scrambles quantum information

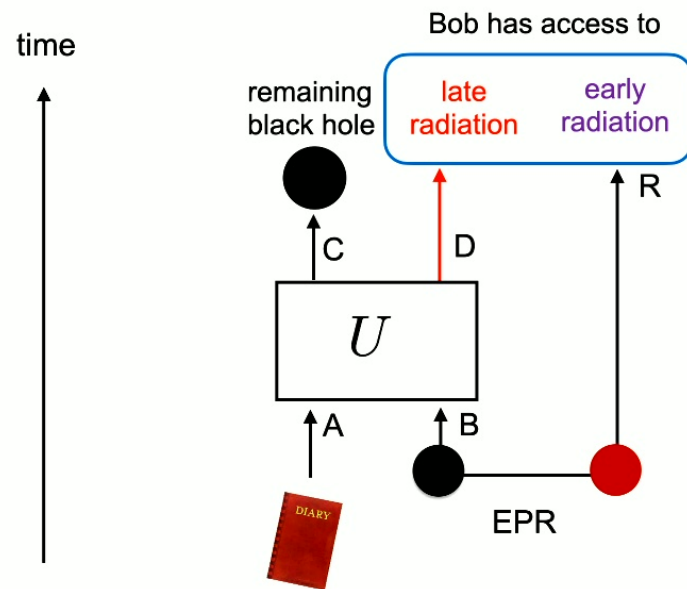
- **Gravitational shockwave** calculations

't Hooft (1980s) and Kiem-Verlinde-Verlinde (1990s)

Shenker-Stanford and Kitaev (2014) for AdS black hole

- This goes **beyond** Hawking's semi-classical calculation

# Decoupling theorem from scrambling

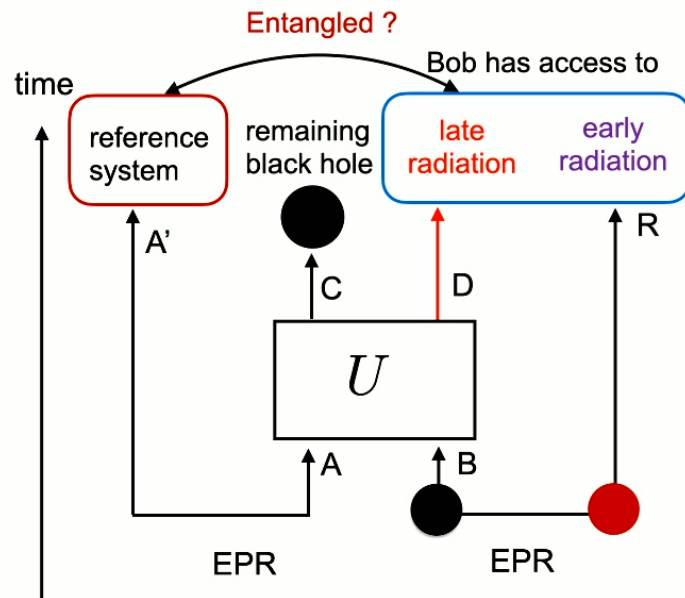


# Decoupling theorem from scrambling

**Theorem 1.** Suppose that the black hole's dynamics is scrambling and  $d_D \gtrsim d_A$ . Then, the subsystems  $A'$  and  $C$  are decoupled:

$$\rho_{A'C} \approx \rho_{A'} \otimes \rho_C. \quad \text{OTOCs } \langle O_A(0)O_D(t)O_A(0)O_D(t) \rangle \quad (1)$$

(BY-Kitaev17)



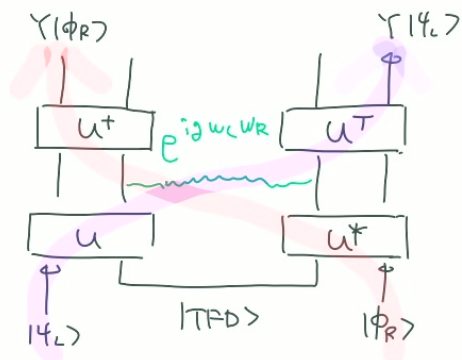
The reference  $A'$  will be (nearly maximally) entangled with DR.

Corollary

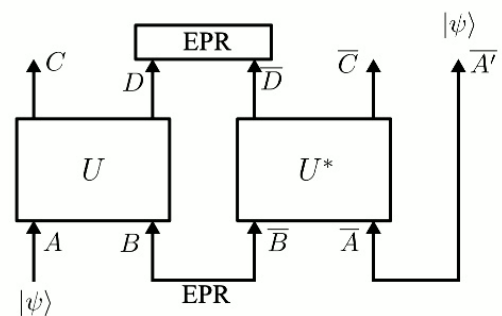
Information can be recovered from a black hole !

# Recovery protocols

Traversable wormhole (Gao-Jafferis-Wall)



Decoding via Petz map (Kitaev-BY)

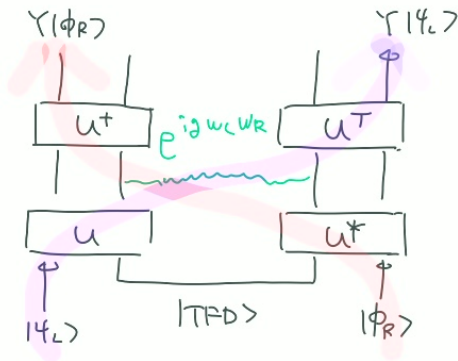


Google group (Brown-Gharibyan-Leichenauer-Lin-Nezami-Salton-Susskind-Swingle-Walter)

Our followup (Schuster-Kobrin-Gao-Cong-Khabiboulline-Linke-Lukin-Monroe-BY-Yao)

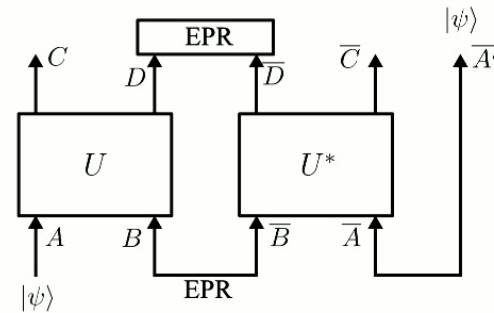
# Recovery protocols

Traversable wormhole (Gao-Jafferis-Wall)



before scrambling time

Decoding via Petz map (Kitaev-BY)



after scrambling time

time scale

“computational complexity”  
phase transition

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# Experiment !

## LETTER

<https://doi.org/10.1038/s41586-019-0952-6>

### Verified quantum information scrambling

K. A. Landsman<sup>1\*</sup>, C. Figgatt<sup>1,6</sup>, T. Schuster<sup>2</sup>, N. M. Linke<sup>1</sup>, B. Yoshida<sup>3</sup>, N. Y. Yao<sup>2,4</sup> & C. Monroe<sup>1,5</sup>

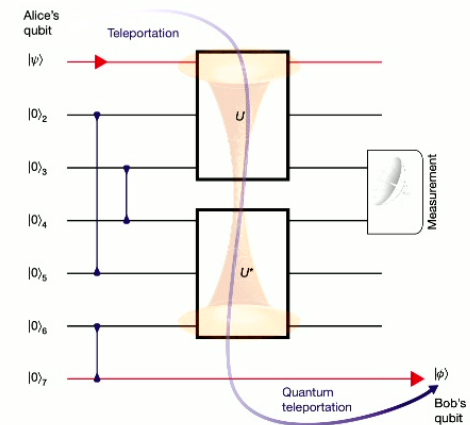
Quantum scrambling is the dispersal of local information into many-body quantum entanglements and correlations distributed throughout an entire system. This concept accompanies the dynamics of thermalization in closed quantum systems, and has recently emerged as a powerful tool for characterizing chaos in black holes<sup>1–4</sup>. However, the direct experimental measurement of quantum scrambling is difficult, owing to the exponential complexity of ergodic many-body entangled states. One way to characterize quantum scrambling is to measure an out-of-time-ordered correlation function (OTOC); however, because scrambling leads to their decay, OTOCs do not generally discriminate between quantum scrambling and ordinary decoherence. Here we implement a quantum circuit that provides a positive test for the scrambling features of a given unitary process<sup>5,6</sup>. This approach conditionally teleports a quantum state through the circuit, providing an unambiguous test for whether scrambling has occurred, while simultaneously measuring an OTOC. We engineer quantum scrambling processes through a tunable three-qubit unitary operation as part of a seven-qubit circuit on an ion trap quantum computer. Measured teleportation fidelities are typically about 80 per cent, and enable us to experimentally bound the scrambling-induced decay of the corresponding OTOC measurement.

For example, non-unitary time-evolution arising from depolarization or classical noise processes naturally lead the OTOC to decay, even in the absence of quantum scrambling. A similar decay can also originate from even slight mismatches between the purported forward and backwards time-evolution of  $\hat{W}(t)$  (refs 6,16 and 24). Although full quantum tomography can in principle distinguish scrambling from decoherence and experimental noise, this requires a number of measurements that scales exponentially with system size and is thus impractical.

In this work, we overcome this challenge and implement a quantum teleportation protocol that robustly distinguishes information scrambling from both decoherence and experimental noise<sup>5,6</sup>. Using this protocol, we demonstrate verifiable information scrambling in a family of unitary circuits and provide a quantitative bound on the amount of scrambling observed in the experiments.

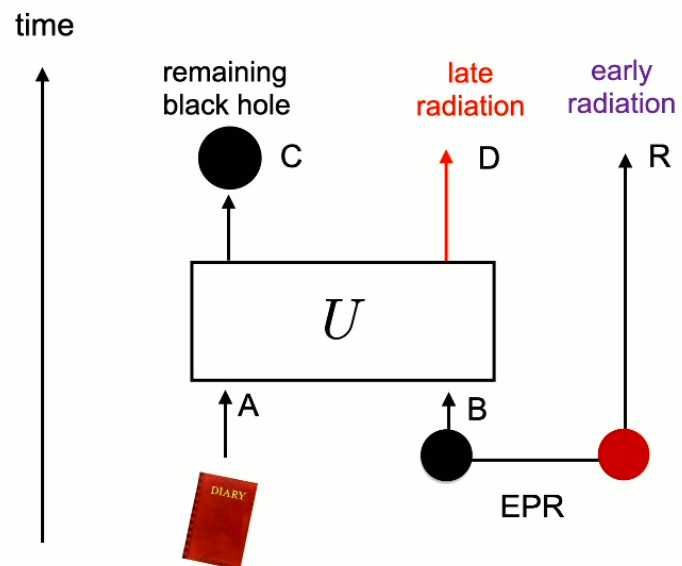
The intuition behind our approach lies in a re-interpretation of the black-hole information paradox<sup>9,10</sup>, under the assumption that the dynamics of the black hole can be modelled as a random unitary operation  $\hat{U}$  (Fig. 1). Schematically, an observer (Alice) throws a secret quantum state into a black hole, while an outside observer (Bob) attempts to reconstruct this state by collecting the Hawking radiation emitted at a later time<sup>1,10</sup>.

An explicit decoding protocol has been recently proposed<sup>5,6</sup>, which



## Entanglement-assisted QECCs

- ❖ Information is delocalized over CDR due to the **preexisting entanglement**.
- ❖ Recoverable from CD, DR, CR. (losing one subsystem is fine).





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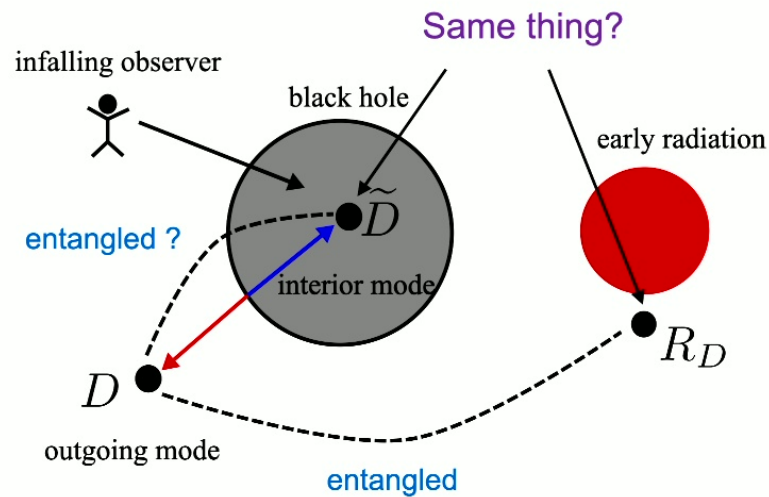
# Firewall puzzle

♣ The outgoing mode  $D$  is **entangled** with the interior mode  $\tilde{D}$  **as well as** with the early radiation  $R_D$  ?

▸ Monogamy of entanglement suggests a **firewall** ?

♣ ER=EPR proposal : interior mode is embedded on the **early radiation** ?

▸ Suffers from the **non-locality problem** ! (Also violation of **extended quantum Church-Turing thesis**)



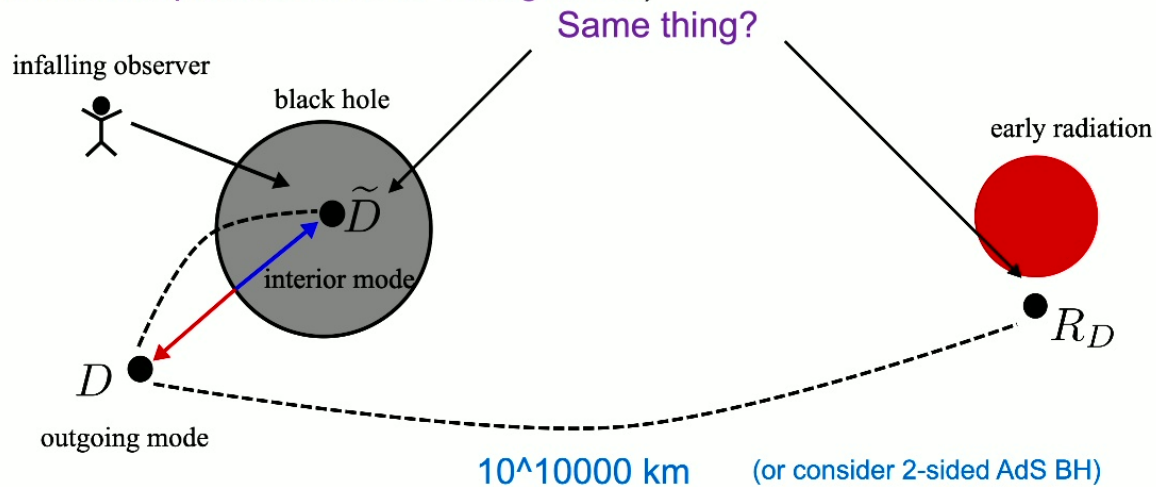
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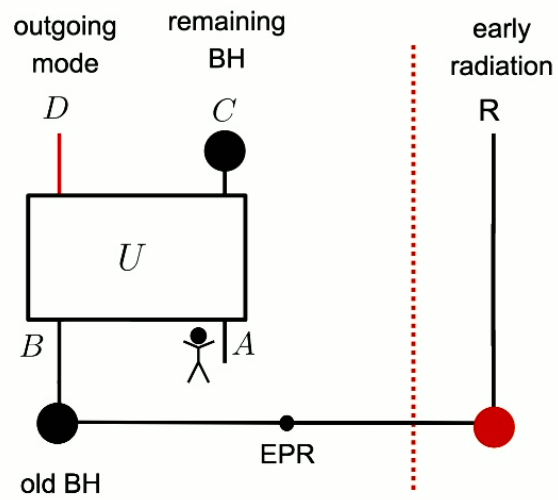
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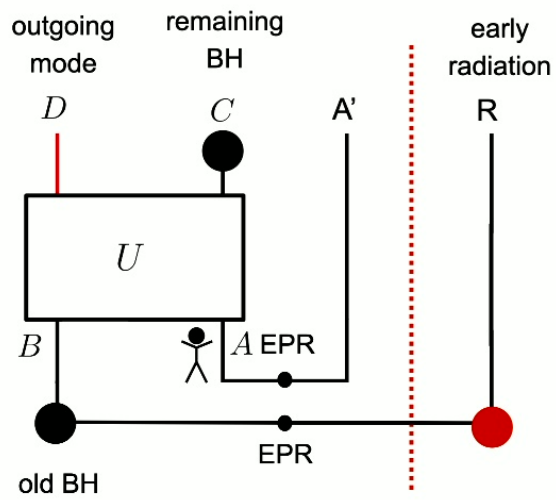
## Black hole with infalling observer

- ✿ An **observer** (finite energy) jumps into a black hole at  $t=0$ .



# Black hole with infalling observer

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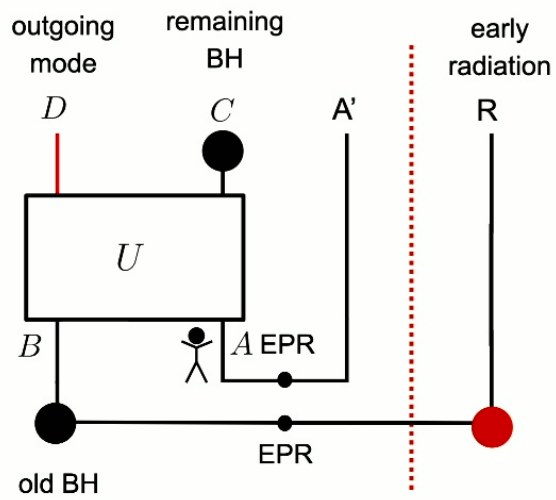


## Black hole with infalling observer

✿ An **observer** (finite energy) jumps into a black hole at  $t=0$ .

Without infalling observer  $\longrightarrow$  Interior mode would be in R

With infalling observer  $\longrightarrow$  **Where is the interior mode ?**

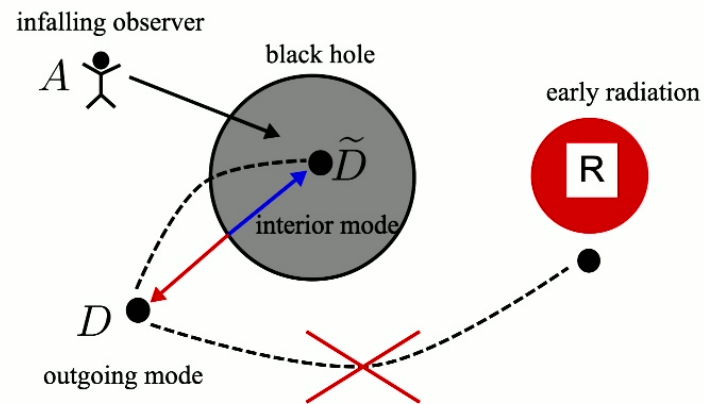


# Black Hole decoupling theorem

**Theorem 1.** Suppose that the black hole's dynamics is scrambling and  $d_A \gtrsim d_D$ . Then, the subsystems  $D$  and  $R$  are decoupled:

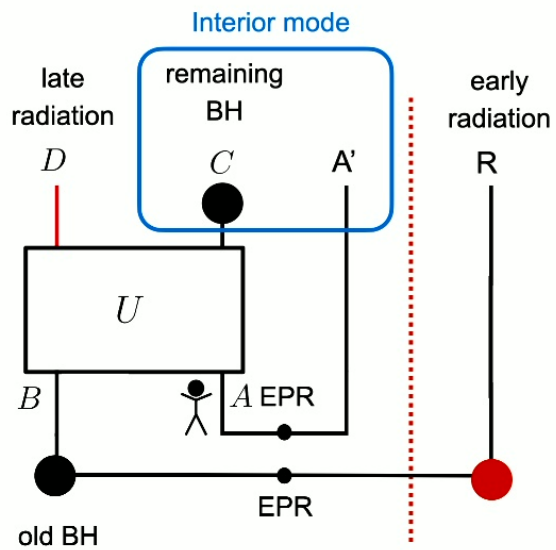
$$\rho_{DR} \approx \rho_D \otimes \rho_R. \quad \text{OTOCs } \langle O_A(0)O_D(t)O_A(0)O_D(t) \rangle \quad (8)$$

(BY-Kitaev17)



# State-independent and Observer-dependent

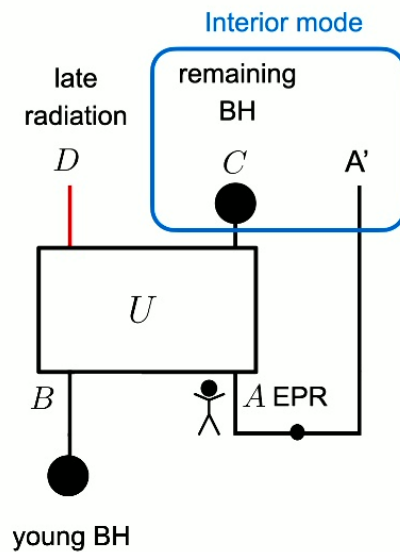
- ❖ Interior partner mode can be found on  $CA'$ . Non-locality is avoided.





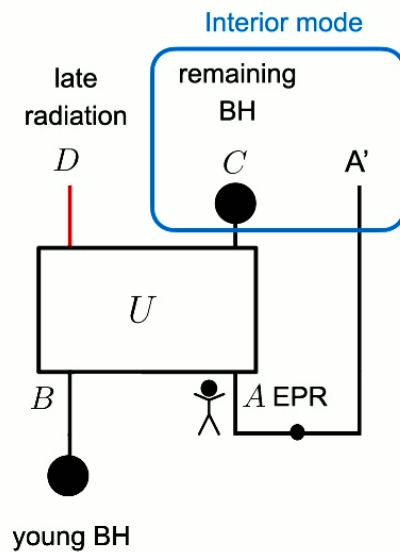
## State-independent and Observer-dependent

- ❖ Interior partner mode can be found on  $CA'$ . Non-locality is avoided.
  - Construction is **state-independent**
- ❖ The same interior partner mode works well for **young black hole as well**



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  - This resolves the “**typical state**” puzzle due to Marolf-Polchinski.



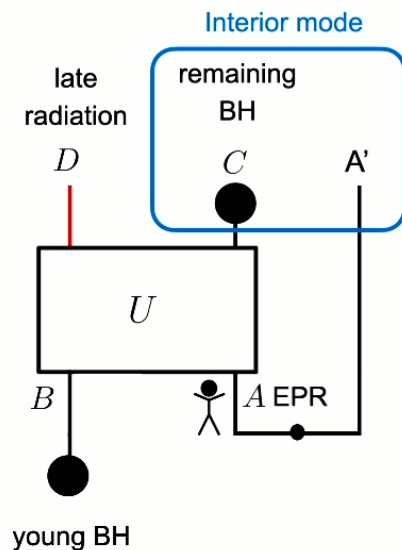
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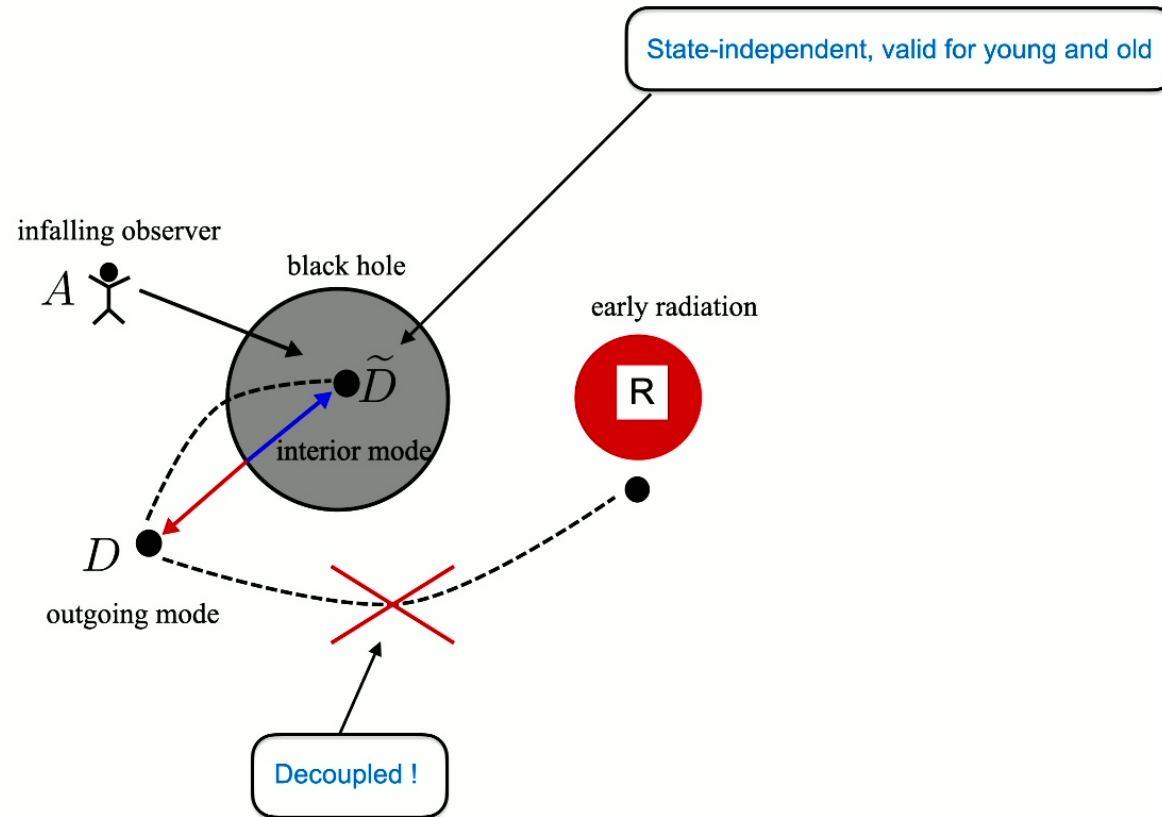
→ This resolves the “**typical state**” puzzle due to Marolf-Polchinski.



• The construction is **observer-dependent**.

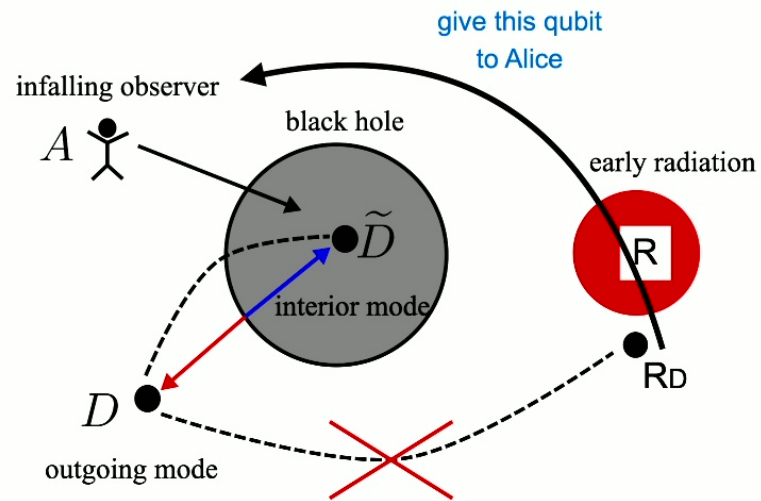
→ Interior operators change **dynamically**, depending on the observer's initial state

# Summary



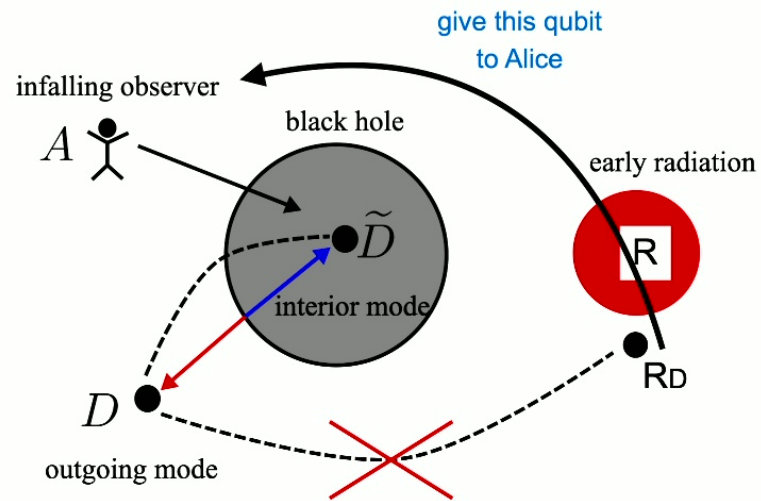
# AMPS thought experiment

- Alice jumps into a black hole with  $R_D$ . Will she cross the horizon safely?

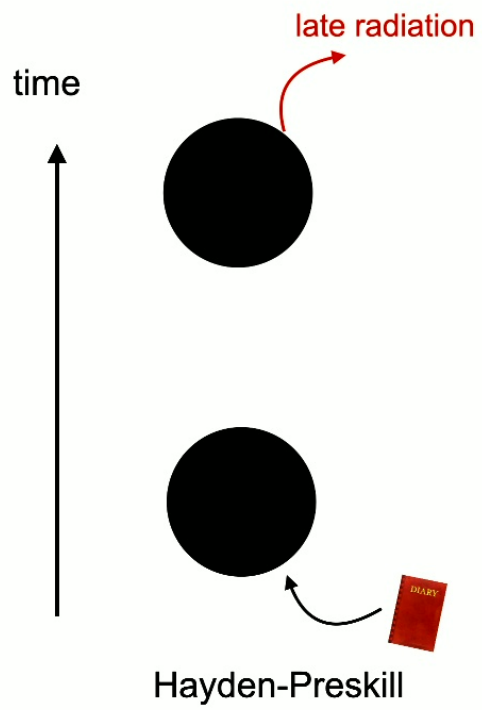


# AMPS thought experiment

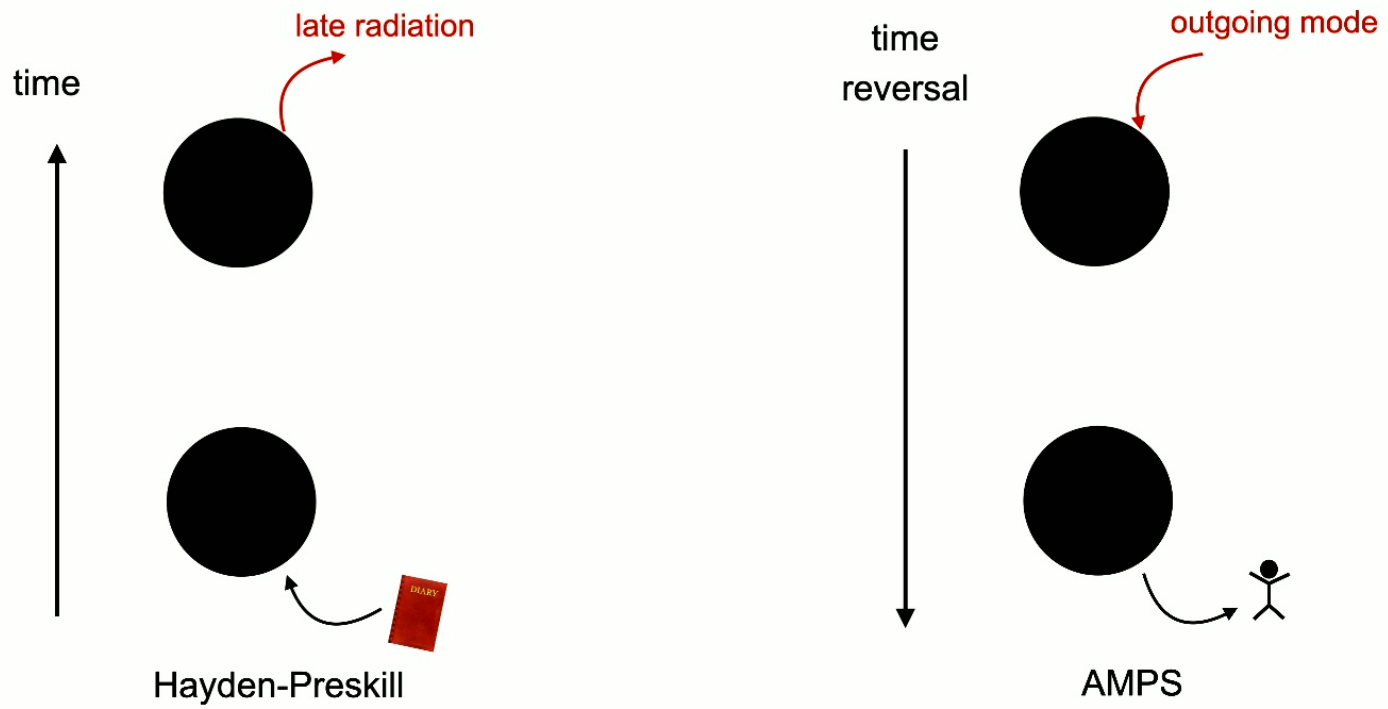
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# Hayden-Preskill and AMPS

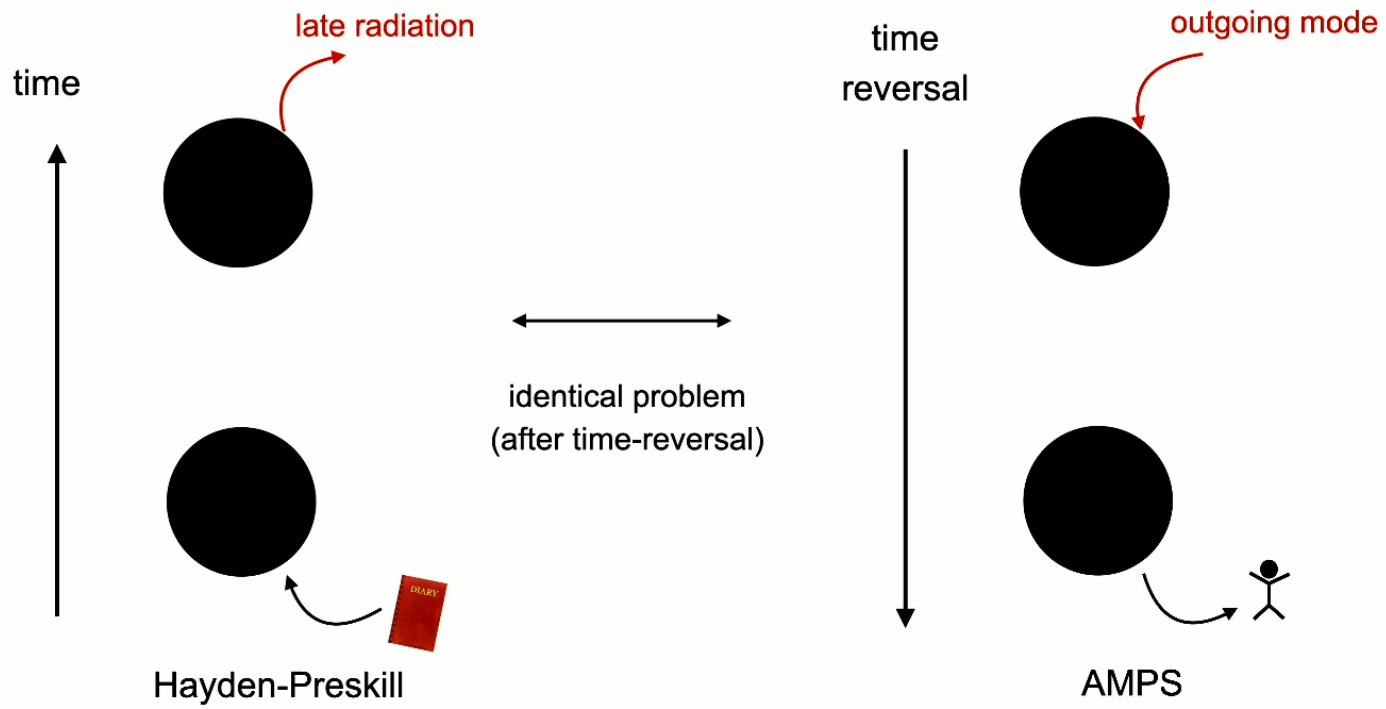


# Hayden-Preskill and AMPS





# Hayden-Preskill and AMPS



# Overview

- ❖ **Bulk-boundary mapping** in the AdS/CFT correspondence, and beyond
  - Holographic quantum error-correcting code (Harlow-Pastawski-Preskill-BY 2015)
  - Holographic scattering (May-Sorce-BY 2022)
- ❖ **Quantum information scrambling** and black holes
  - Information recovery from black hole (Hosur-Qi-Roberts-BY 2015, BY-Kitaev 2017)
  - Firewall puzzle and black hole interior (BY 2019)

# Future directions

## ♣ Going **beyond AdS**

- de Sitter horizon puzzles
- entanglement in de Sitter

## ♣ Emergence of **interaction from entanglement**

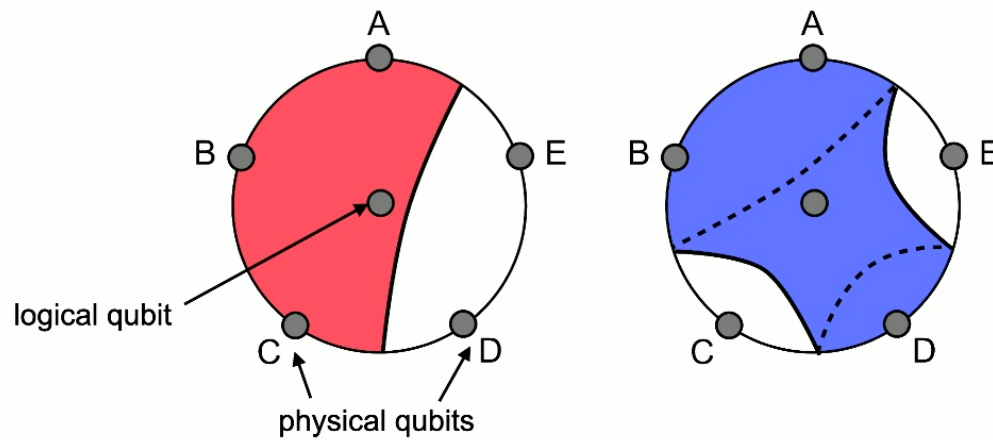
- calculate it in “holographic” CFT

## A simple toy model ?

1 bulk qubit  
5 boundary qubits

in total, just 6 qubits

A bulk operator must have representations on any region with three qubits.



Entanglement wedge reconstruction !