

Title: Cosmology and Unification

Speakers: Raman Sundrum

Series: Particle Physics

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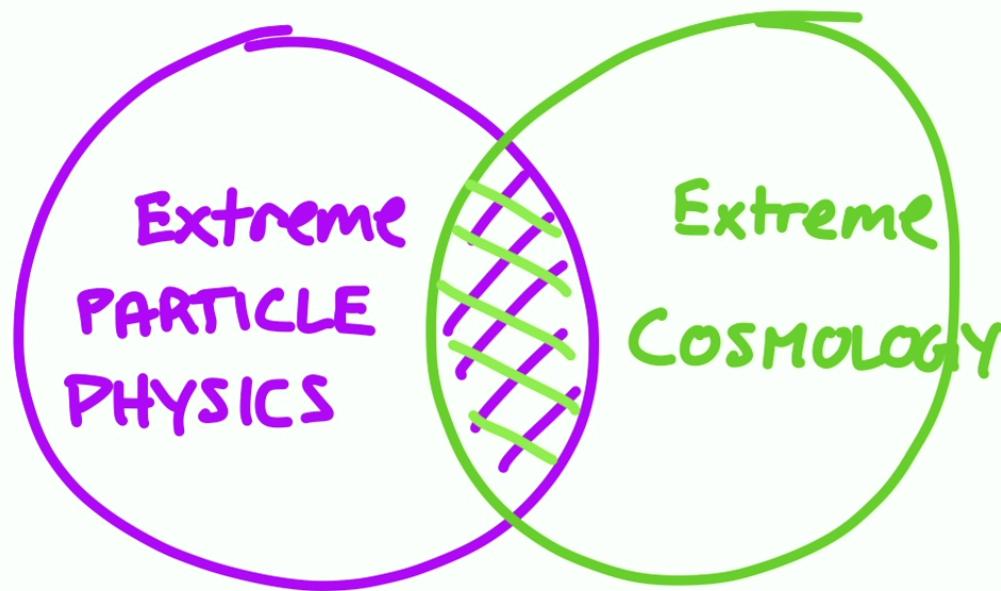
Abstract: Precision measurements of primordial correlators in the CMB, Large Scale Structure, and 21-cm cosmology may contain "on-shell" imprints of extremely heavy particle physics, with masses comparable to the inflationary Hubble scale, via the remarkable inflationary mechanism known as "cosmological collider physics". I will describe my research in (a) finding new robust mechanisms for extending the energy range and strength of such signals, (b) identifying motivated particle physics targets that may be discoverable, (c) showing how cosmological collider physics can probe the mechanism of inflation itself, and (d) demonstrating variants of the mechanism that may be observable in new cosmological "maps", such as stochastic gravitational wave backgrounds with significant anisotropies. While this is an ambitious program of research, there are major challenges to bring it to fruition, on the experimental, phenomenological and theoretical fronts, which I will sketch.

Zoom Link: <https://pitp.zoom.us/j/98923687484?pwd=cjgweEhoejVCeHAvc0RBSDEvVkJdz09>

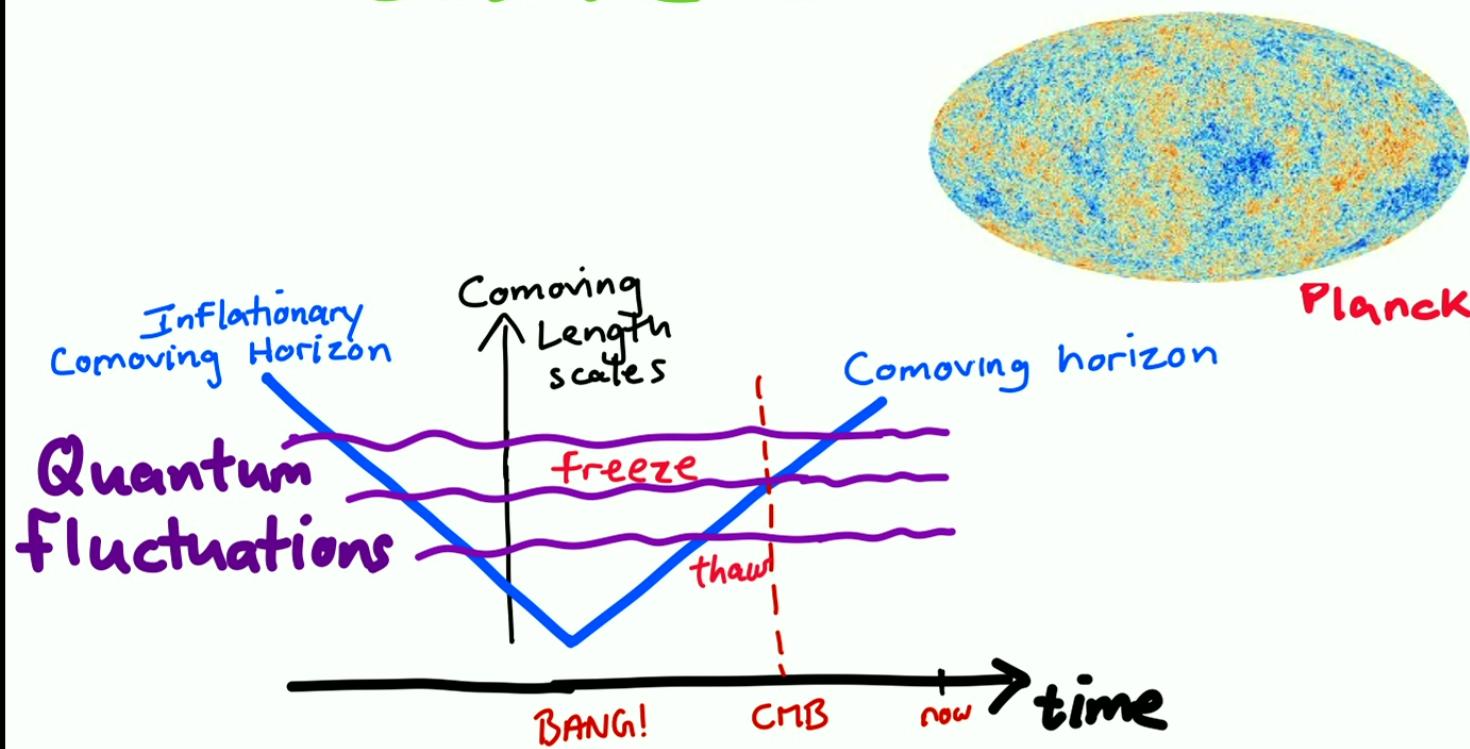
COSMOLOGY & UNIFICATION

Raman Sundrum
University of Maryland

INTRODUCTION

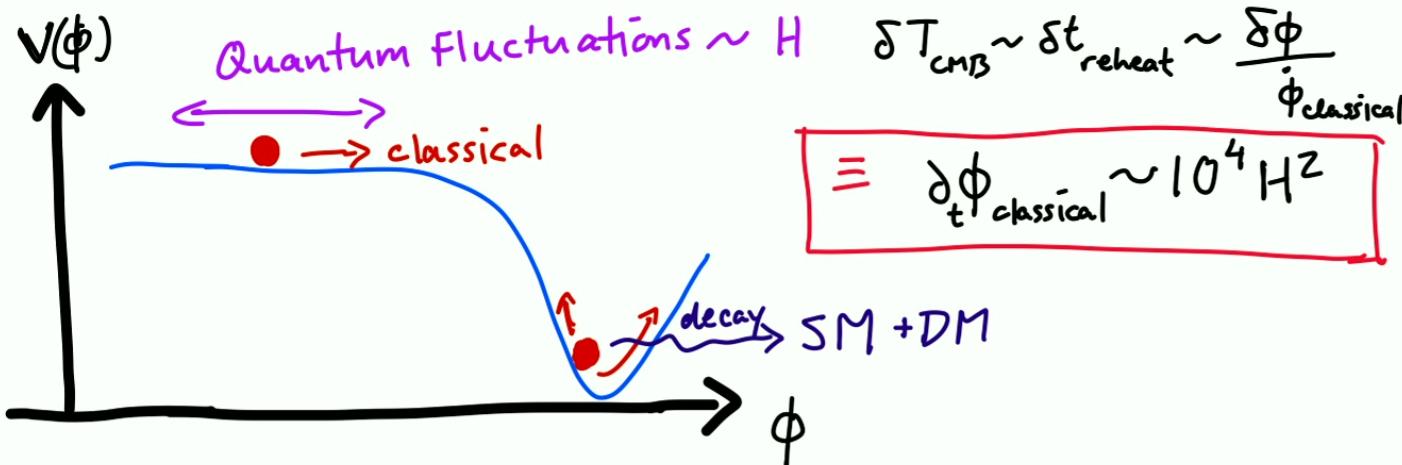


PRIMORDIAL INHOMOGENEITIES SEEDED BY COSMIC INFLATION



3

SLOW-ROLL INFLATION



Approximate de Sitter phase

$$ds^2 \approx dt^2 - e^{2Ht} d\vec{x}^2 = \frac{d\eta^2 - d\vec{x}^2}{\eta^2} \quad \begin{matrix} \text{Time translation inv.} \\ \eta < 0 \end{matrix}$$

H=1
units

"Scale Invariance"

$$t \rightarrow t - \lambda \equiv \eta \rightarrow e^\lambda \eta$$

$$\vec{x} \rightarrow e^\lambda \vec{x}$$

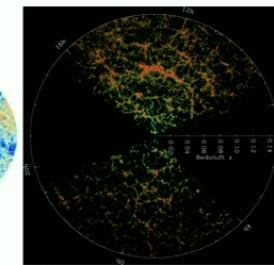
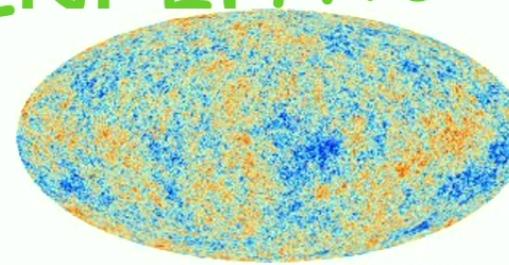
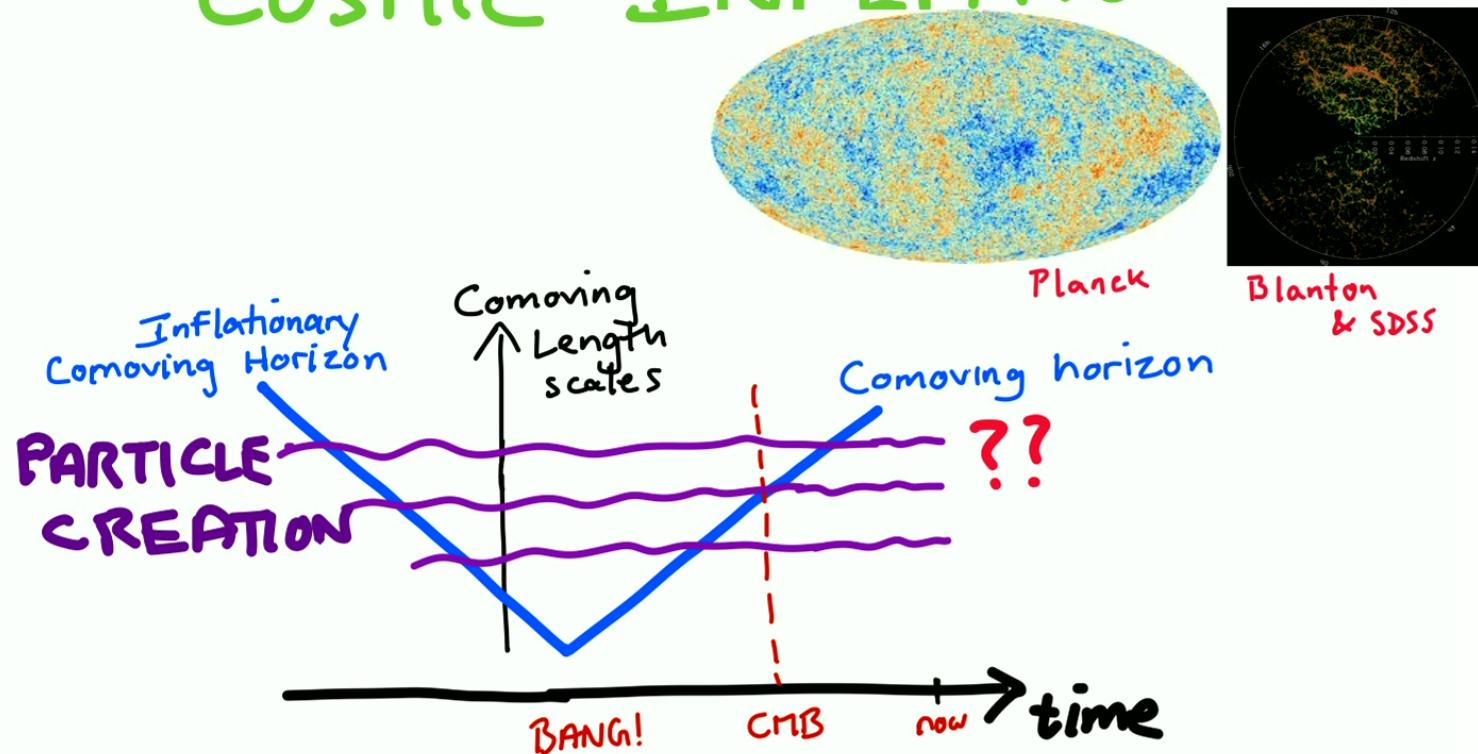
reduces to spatial scale inv.

at reheating $\eta \approx 0$,

$$\vec{x} \rightarrow e^\lambda \vec{x}$$

\Rightarrow Scale-Invariant fluctuations₅

FUNDAMENTAL PHYSICS FROM COSMIC INFLATION



$$E = mc^2 \equiv i\hbar\partial_t \sim \frac{\partial_t a}{a} \equiv H_{\text{inflation}} < 5 \times 10^{13} \text{ GeV}!$$

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MASSIVE FIELDS IN DE SITTER

$$S = \int d^3\vec{x} d\eta \left\{ \sqrt{-g} g^{\mu\nu} \partial_\mu \sigma \partial_\nu \sigma - m^2 \sigma^2 \right\}$$

$$= \int d^3\vec{k} d\eta \left\{ \frac{1}{\eta^2} |\partial_\eta \sigma_{\vec{k}}|^2 - \frac{\vec{k}^2}{\eta^2} |\sigma_{\vec{k}}|^2 - \frac{m^2}{\eta^4} |\sigma_{\vec{k}}|^2 \right\}$$

Equations of motion of Bessel type :

$$\sigma_{\vec{k}}(\eta) = e^{-\pi\sqrt{m^2 - q^2/4}/2} H_{i\sqrt{m^2 - q^2/4}}^{(1)}(-k\eta) \underset{m \gg \text{H}}{\approx} e^{-\pi m/2} H_{im}^{(1)}(-k\eta)$$

$\xrightarrow{|k\eta| \gg m}$ $\frac{1}{\sqrt{2k}} e^{-ik\eta}$

positive energy
(& boosted by blue shift)

BUT ... $\xrightarrow{|k\eta| \ll m}$ $e^{-imt} + \underbrace{e^{imt}}_{\text{negative energy!}} e^{-\pi m}$

PRIMORDIAL NON-GAUSSIANITIES

from “in-in” correlators
with interactions

$$\langle \delta T(\vec{x}_1) \delta T(\vec{x}_2) \delta T(\vec{x}_3) \rangle$$

$$\propto \langle 0 | e^{i \int_{-\infty(1+i\varepsilon)}^{\infty} dt H(t)} \delta\phi(\vec{x}_1) \delta\phi(\vec{x}_2) \delta\phi(\vec{x}_3) e^{-i \int_{-\infty(1-i\varepsilon)}^{\infty} dt H(t)} | 0 \rangle$$

spatially flat gauge

Fourier transform →

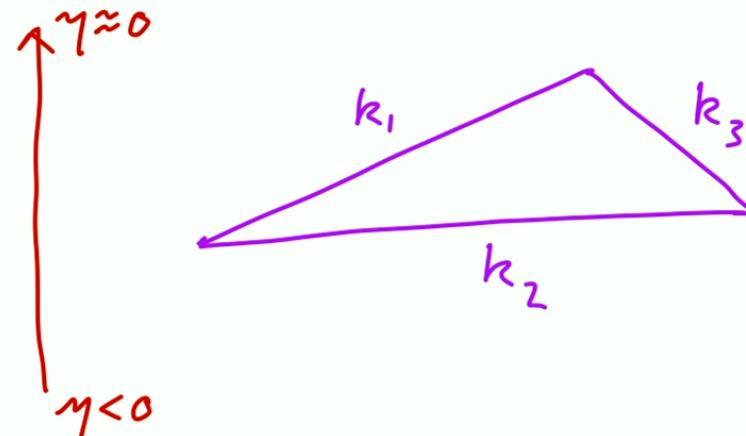
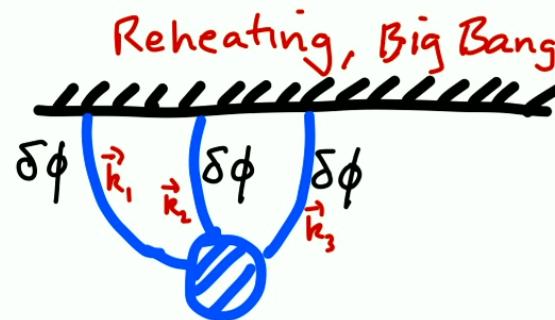
BISPECTRUM

separate out δ-Function

$$\langle \delta\phi_{\vec{k}_1} \delta\phi_{\vec{k}_2} \delta\phi_{\vec{k}_3} \rangle' \delta^3(\vec{k}_1 + \vec{k}_2 + \vec{k}_3)$$

PRIMORDIAL NON-GAUSSIANITIES

from “in-in” correlators
with interactions



Primordial
Non-Gaussianity (NG):

$$F(k_1, k_2, k_3) \equiv -\underbrace{\partial_{+}\phi_{cl}}_{\sim 10^4} \frac{\langle \delta\phi_{\vec{k}_1} \delta\phi_{\vec{k}_2} \delta\phi_{\vec{k}_3} \rangle'}{\langle \delta\phi_{\vec{k}_1} \delta\phi_{-\vec{k}_1} \rangle' \langle \delta\phi_{\vec{k}_3} \delta\phi_{-\vec{k}_3} \rangle'}$$

$$f_{NL} \equiv \frac{5}{18} F(k, k, k) \underset{\text{Planck}}{<\mathcal{O}(10)}$$

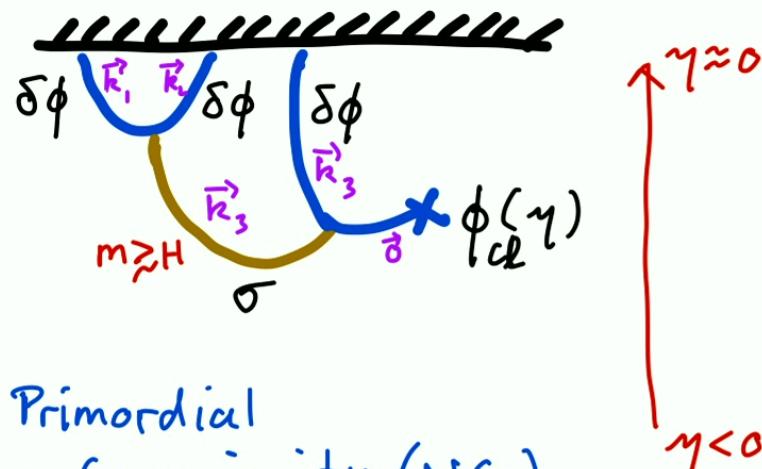
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"COSMOLOGICAL COLLIDER PHYSICS"

$$\mathcal{L}_{\text{int.}} = \sqrt{-g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - \frac{m^2}{2} \phi^2$$

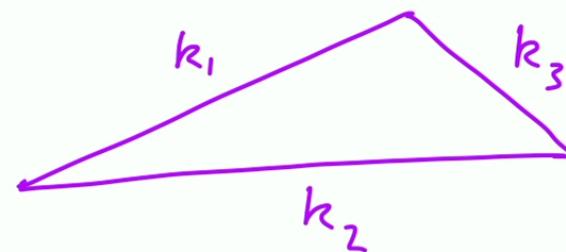
Radiative stability
of V_{inf}

Chen, Wang '09; Baumann, Green '11
 Noumi et. al. '12
 Arkani-Hamed, Maldacena '15
 Lee et. al. '16; Meerburg et. al. '16
 :
 :



Primordial
Non-Gaussianity (NG):

$$\langle \delta\phi_{\vec{k}_1} \delta\phi_{\vec{k}_2} \delta\phi_{\vec{k}_3} \rangle \sim \frac{\partial_t \phi_d}{\Lambda^2} e^{-\pi m} e^{-im(t_{\text{late}} - t_{\text{early}})}$$



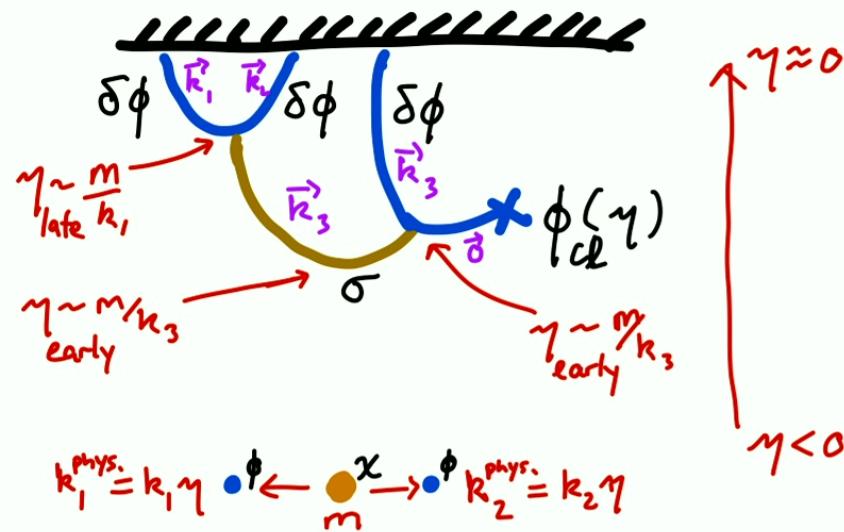
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COSMOLOGICAL COLLIDER PHYSICS

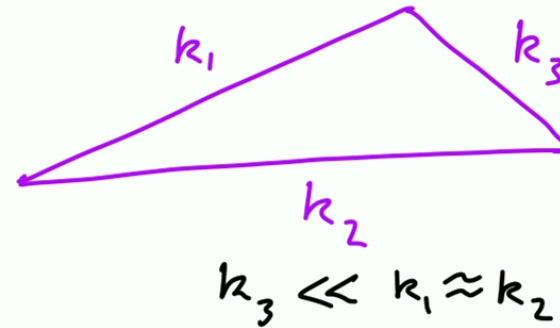
$$\mathcal{L}_{\text{int.}} = \sqrt{-g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - \frac{m}{\sigma} \phi$$

Radiative stability
of V-inflation

Chen, Wang '09; Baumann, Green '11
 Noumi et. al. '12
 Arkani-Hamed, Maldacena '15
 Lee et. al. '16; Meerburg et. al. '16
 ...



SQUEEZED LIMIT:



$$\langle \delta \phi_{\vec{k}_1} \delta \phi_{\vec{k}_2} \delta \phi_{\vec{k}_3} \rangle \sim \frac{\partial_t \phi_d}{\Lambda^2} e^{-\pi m} e^{-im(t_{\text{late}} - t_{\text{early}})} \propto e^{-\pi m} \left(\frac{k_3}{k_1}\right)^{im}$$

non-analytic \equiv on-shell propagation

OUTLINE

Higher-dimensional Grand Unification
& Kaluza-Klein Graviton

Probing Inflaton Partners

"Heavy-Lifting" of Gauge-Higgs Dynamics
& Naturalness

Curvaton Scenario → Stronger Signals

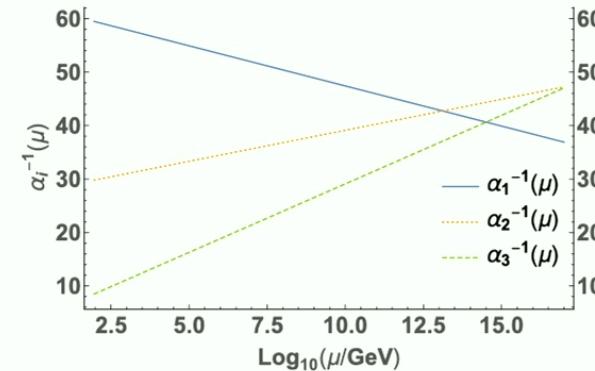
"Chemical Potential" → Larger Window
of Opportunity

New maps from Stochastic Gravitational
Waves & Classical production of Heavy Fields

(Non-supersymmetric) GRAND UNIFICATION

$SO(10) \supset SU(5) \xrightarrow[\text{Higgs mechanism}]{\uparrow} SU(3) \times SU(2) \times U(1)$

Spinor representation
weak isospin 2 + color 3
entire SM matter generation



1-loop SM RGE

(Non-supersymmetric) GRAND UNIFICATION

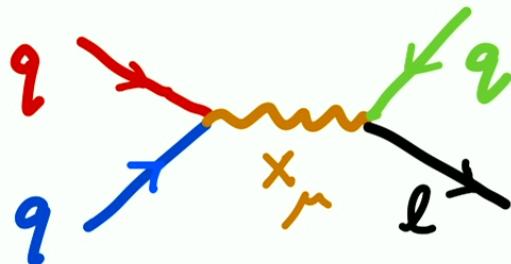
$SO(10) \supset SU(5)$ $\xrightarrow[\text{Higgs mechanism}]{} SU(3) \times SU(2) \times U(1)$

Spinor representation \supset entire SM matter generation

weak isospin 2 + color 3

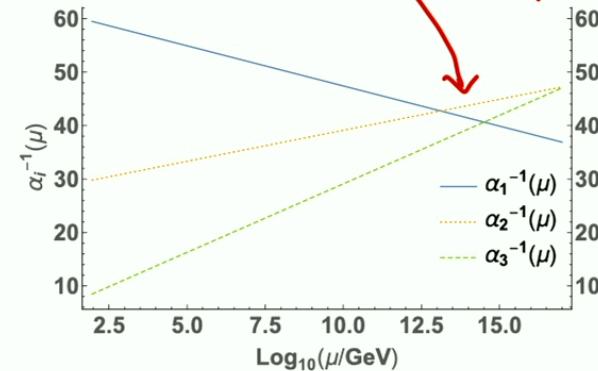
striking, but why imperfect?

PROTON DECAY?



$$m_X > 5 \times 10^{15} \text{ GeV}$$

Super-K '16



15

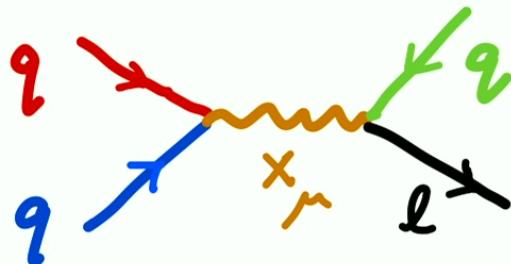
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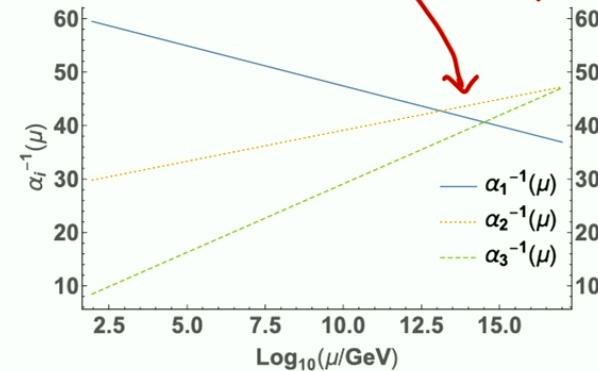
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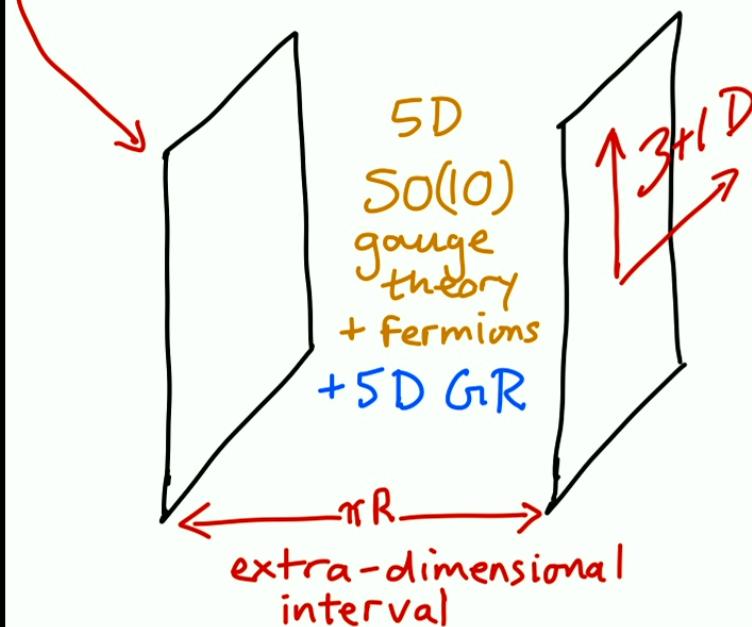
ORBIFOLD GUTS

Kawamura '99, '00
Hall, Nomura '01, '03

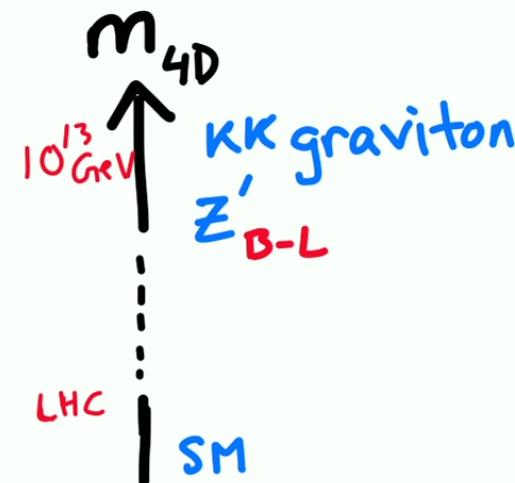
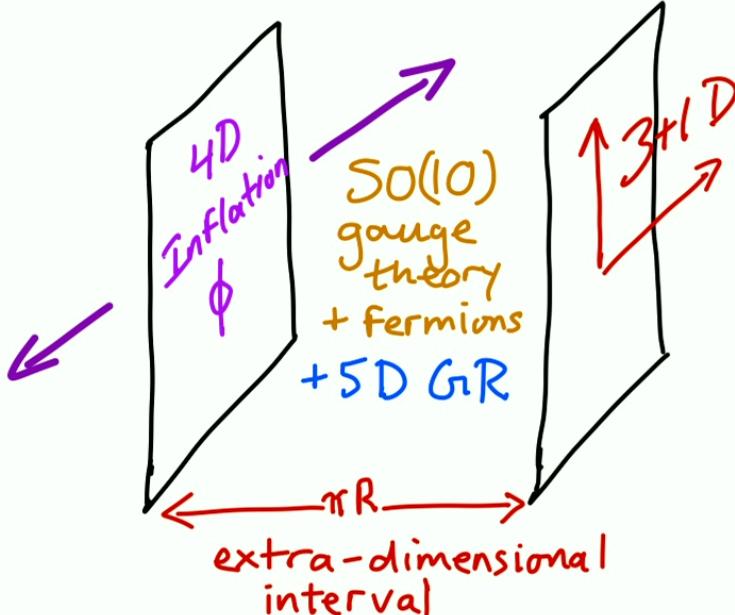
Higher-dimensional $SO(10)$

gauge theory,

with extra-dimensional
boundary conditions (eg. Neumann, Dirichlet)
respecting only $SU(3) \times SU(2) \times U(1)$, & global $U(1)_{\text{baryon}}$



ADD BOUNDARY-LOCALIZED 4D INFLATION . . .



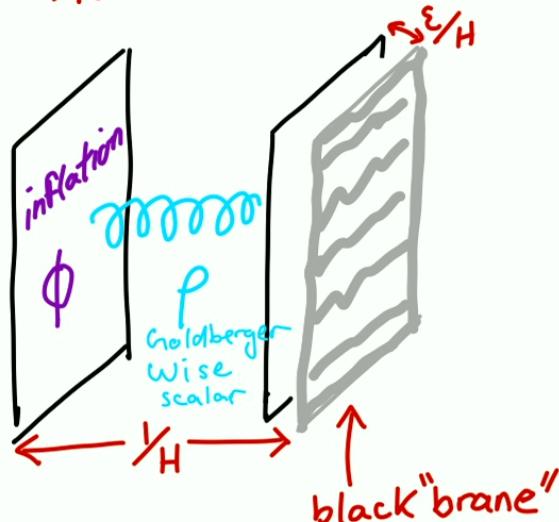
Kumar, Sundrum '18

OPPORTUNITY ON THE HORIZON...

$m_{KK} = 1/R \sim H_{inflation} \Rightarrow$ significant backreaction
to 5D geometry
from boundary inflation

$$ds^2 = \underset{m_{KK} \gg H}{dt^2 - e^{2Ht} d\vec{x}^2 - dx_5^2}$$

$$\xrightarrow{1/R \sim H} (1 - Hx_5)^2 [dt^2 - e^{2Ht} d\vec{x}^2] - dx_5^2$$



Near-horizon analysis
of Goldberger-Wise '99
extra-dimensional stabilization
by 5D scalar P is possible
for small ϵ

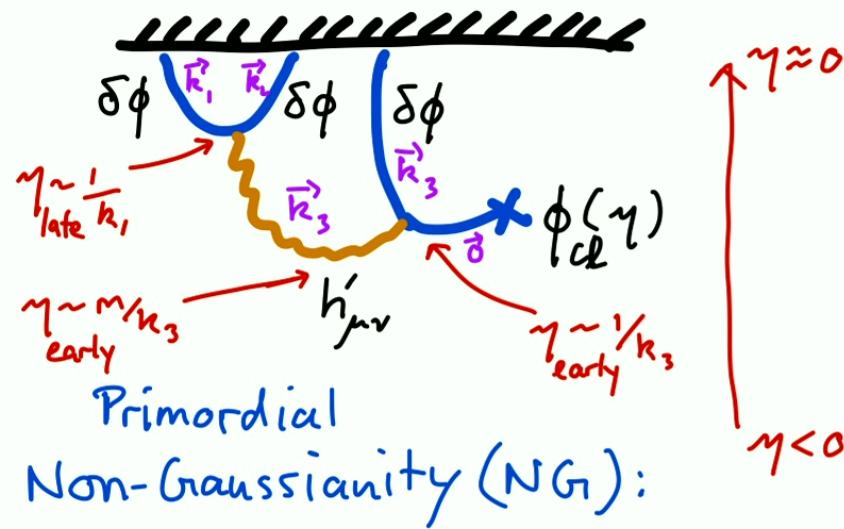
$$\epsilon \equiv 1 - H\pi R$$

$$\Delta m_{KK} \sim \epsilon H$$

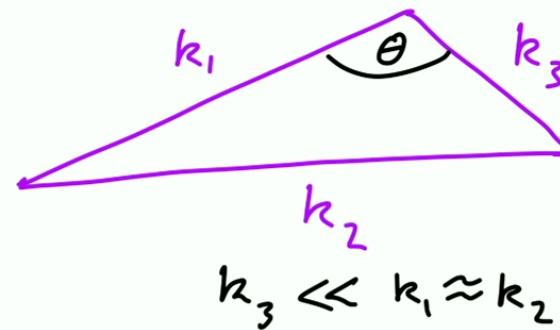
Further backreacted
 ds^2 treated in
 ϵ -perturbation theory

KALUZA-KLEIN GRAVITON

$$\mathcal{L}_{\text{int.}} = \sqrt{-g} \partial_\mu \phi \partial_\nu \phi \frac{h'^{\mu\nu}}{M_{\text{Pl}}}$$



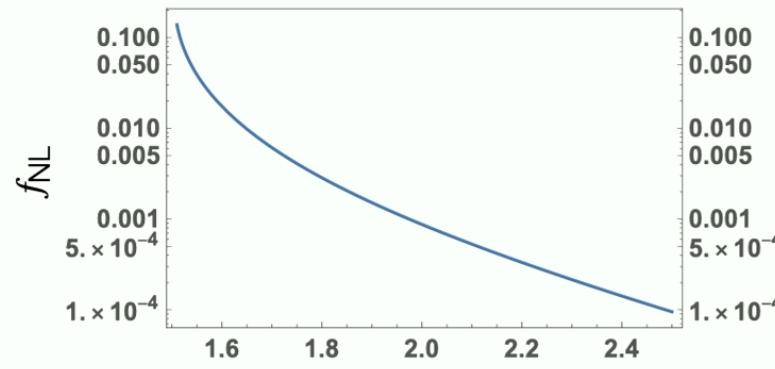
SQUEEZED LIMIT:



$$F(\vec{k}_1, \vec{k}_2, \vec{k}_3) \sim \frac{(\partial_t \phi_{\text{cl}})^2}{M_{\text{Pl}}^2} e^{-\pi m_{kk}} \left(\frac{k_3}{k_1}\right)^{im_{kk}} (\cos^2 \theta - \gamma_3) < 10^{-2}$$

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Subtle backreaction to 5D geometry More carefully: KK graviton mediated NG



$r = 0.1$;
Maximal H_{inf} .
allowed

$$\mu = \sqrt{\frac{m^2}{H^2} - \frac{9}{4}}$$

$$F = \frac{r}{8} \times \left(\cos^2 \theta - \frac{1}{3} \right) \frac{\frac{m}{H} \sqrt{\pi}}{8(1 + 4\mu^2)^2 \cosh(\pi\mu)} \\ \times \left(A(\mu)(1 + i \sinh \pi\mu) \left(\frac{k_3}{k_1} \right)^{3/2+i\mu} + (\mu \rightarrow -\mu) \right)$$

$$A(\mu) = (-27 + 120i\mu + 152\mu^2 - 32i\mu^3 + 16\mu^4)\Gamma(5/2 + i\mu)\Gamma(-i\mu)2^{-2i\mu}$$

Soubhik Kumar, Maryland

Seeing Orbifold GUTs in Primordial Non-Gaussianities

21

PROBING INFLATION

Inflation & reheating present naturalness (fine-tuning) puzzles, resolvable with new symmetries.

Symmetry partners of inflaton can appear in Cosmo Collider, such as the Sinflaton of SUSY

Deshpande, Sundrum '21

or the

Twinflaton of hybrid inflation with "twin" discrete symmetry Deshpande, Kumar, Sundrum '21

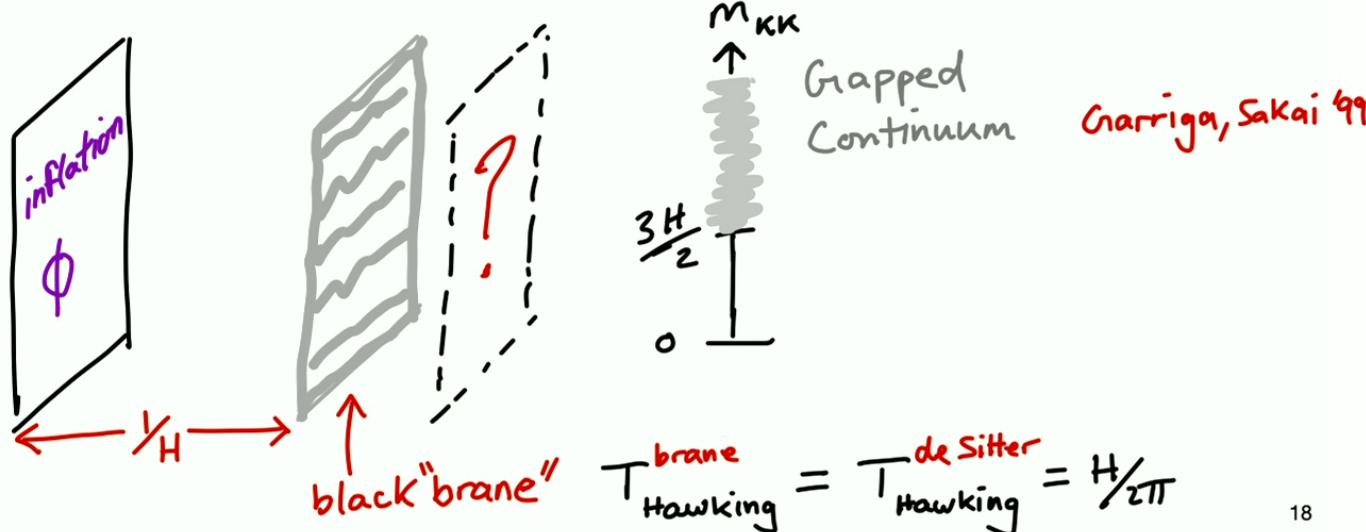
TROUBLE ON THE HORIZON...

$m_{KK} = 1/R \sim H_{inflation} \Rightarrow$ significant backreaction
to 5D geometry
from boundary inflation

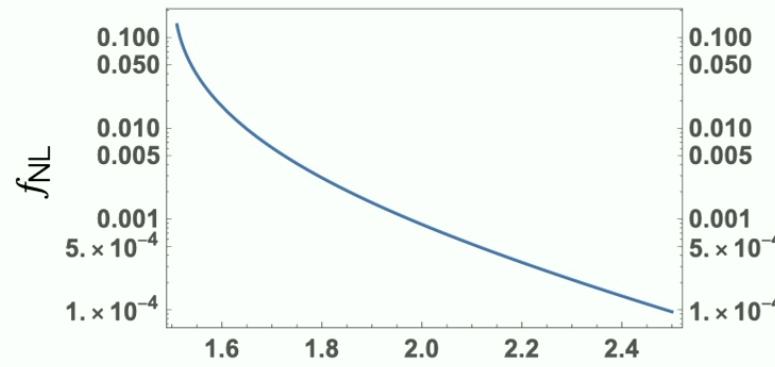
$$ds^2 = \frac{1}{R \gg H} dt^2 - e^{2Ht} d\vec{x}^2 - dx_5^2$$

$$\xrightarrow{\frac{1}{R \sim H}} (1 - Hx_5)^2 [dt^2 - e^{2Ht} d\vec{x}^2] - dx_5^2$$

Vilenkin '83
Ipser, Sikivie '84
Kaloper, Linde '98
Kaloper '99



Subtle backreaction to 5D geometry More carefully: KK graviton mediated NG



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Maximal H_{inf} .
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$$A(\mu) = (-27 + 120i\mu + 152\mu^2 - 32i\mu^3 + 16\mu^4)\Gamma(5/2 + i\mu)\Gamma(-i\mu)2^{-2i\mu}$$

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Deshpande, Sundrum '21

or the

Twinflaton of hybrid inflation with "twin" discrete symmetry Deshpande, Kumar, Sundrum '21

EXTREME PRECISION

Only one sky to measure quantum expectations.

But translation & rotation (& \approx scale) symmetry allows us to make many measurements of same correlator :

$$\delta f_{NL} \sim \frac{10^4}{\sqrt{N_{\text{modes}}}}$$

$z = 0$

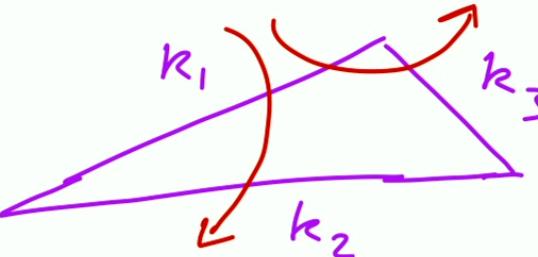
$z \sim 2-3$

$z \sim 30$

$z \sim 100$

$z \sim 1100$

$$\rightarrow z \equiv \frac{1}{a} - 1$$



Alvarez et. al. '14

Loeb, Zaldarriaga '03

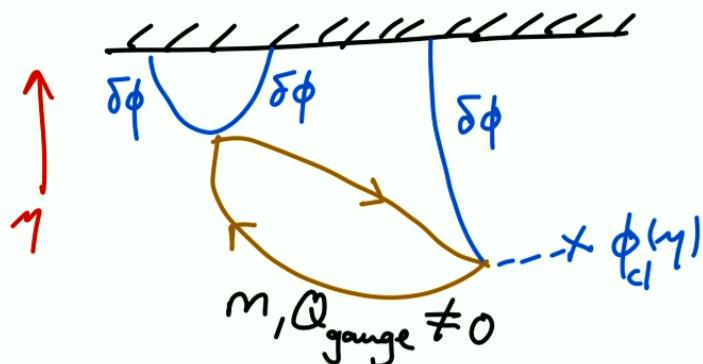
Planck: $N_{\text{modes}} \sim 10^7 \Rightarrow \delta f_{NL} \sim 10$ Current bound

LSS: $N_{\text{modes}} \sim 10^9 \Rightarrow \delta f_{NL} \sim 1$ (EUCLID, DESI, SPHEREx ...) 2022

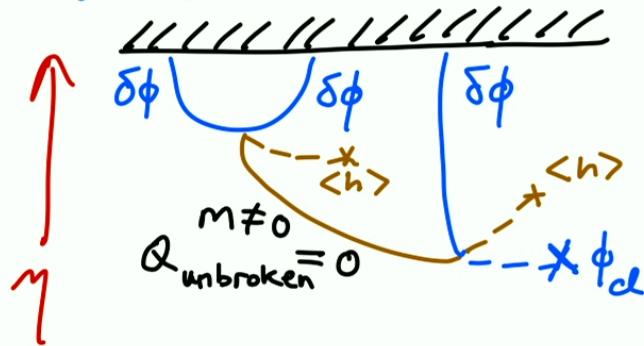
21-cm Cosmology: $N_{\text{modes}} \sim 10^{16} \Rightarrow \delta f_{NL} \sim 10^{-4} - 10^{-3}$ 20??

GAUGE-HIGGS THEORY

Gauge-charged particles can only appear in (suppressed) loops, as inflaton is singlet



unless rendered neutral after Higgsing:



Eg. Z^0

Kumar, Sundrum '17

"HEAVY-LIFTING" BY INFLATION

Kumar, Sundrum
'17

Natural to have Higgs fields couple to curvature:

$$\mathcal{L}_{\text{Higgs}} = \sqrt{-g} \left\{ g^{\mu\nu} D_\mu h^\dagger D_\nu h + m^2 h^\dagger h - \lambda (h^\dagger h)^2 \pm \mathcal{O}(1) R h^\dagger h \right\}$$

$\uparrow_{\text{tachyonic } \ll H_{\text{inf}}^2}$

$\sim \overbrace{H_{\text{inf}}^2 h^\dagger h}^{\text{during inflation}}$

\Rightarrow Higgs mechanisms at lower scales today, negligible today could have been at $\sim H_{\text{inflation}}$ during inflation!

This extreme volatility of Higgs mechanism is an aspect of the Hierarchy Problem.

But here, particles getting Higgs-generated masses, are "lifted" into the sights of the "Cosmological Collider":

$$V_{\text{effective}}(h) = -\mathcal{O}(H_{\text{inf}}^2) h^\dagger h + \lambda (h^\dagger h)^2$$

$$m_Z \sim H_{\text{inf}}. \quad \text{Not a "problem"!}$$

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HIGGSED GAUGE THEORY

$$L_{\text{int.}} \supset \sqrt{-g} g^{\mu\nu} \left\{ \frac{\partial_\mu \phi \partial_\nu \phi \rho}{\Lambda} + \frac{\partial_\mu \phi h^\dagger D_\nu h \rho}{\Lambda^2} \right\}$$

mediator $\Lambda > \dot{\phi}_{\text{cl}}$
Cremmelli '03

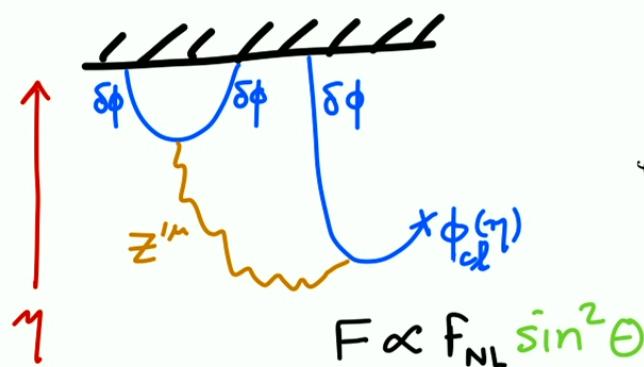
integrate out ρ , $m_\rho > H$
 $\langle h \rangle \approx v$

$$\sqrt{-g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \partial_\alpha \phi Z'^\alpha / \frac{v^2}{\Lambda^3 m_\chi^2}$$

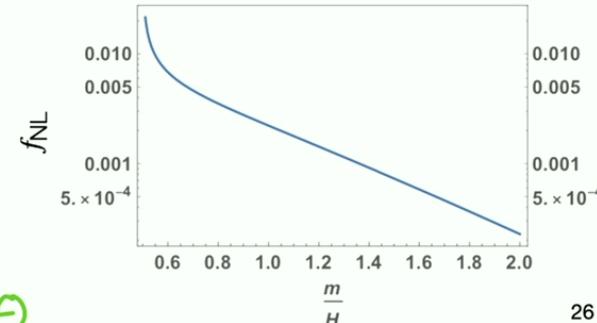
must be small enough
to keep EFT control of $(\partial\phi)^n$ expansion

ORBIFOLD GUTs

$$L_{\text{int}} \supset \sqrt{-g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \partial_\alpha \phi \partial_{x_5} Z'^\alpha_{B-L} / \Lambda^2 m_\chi^2$$

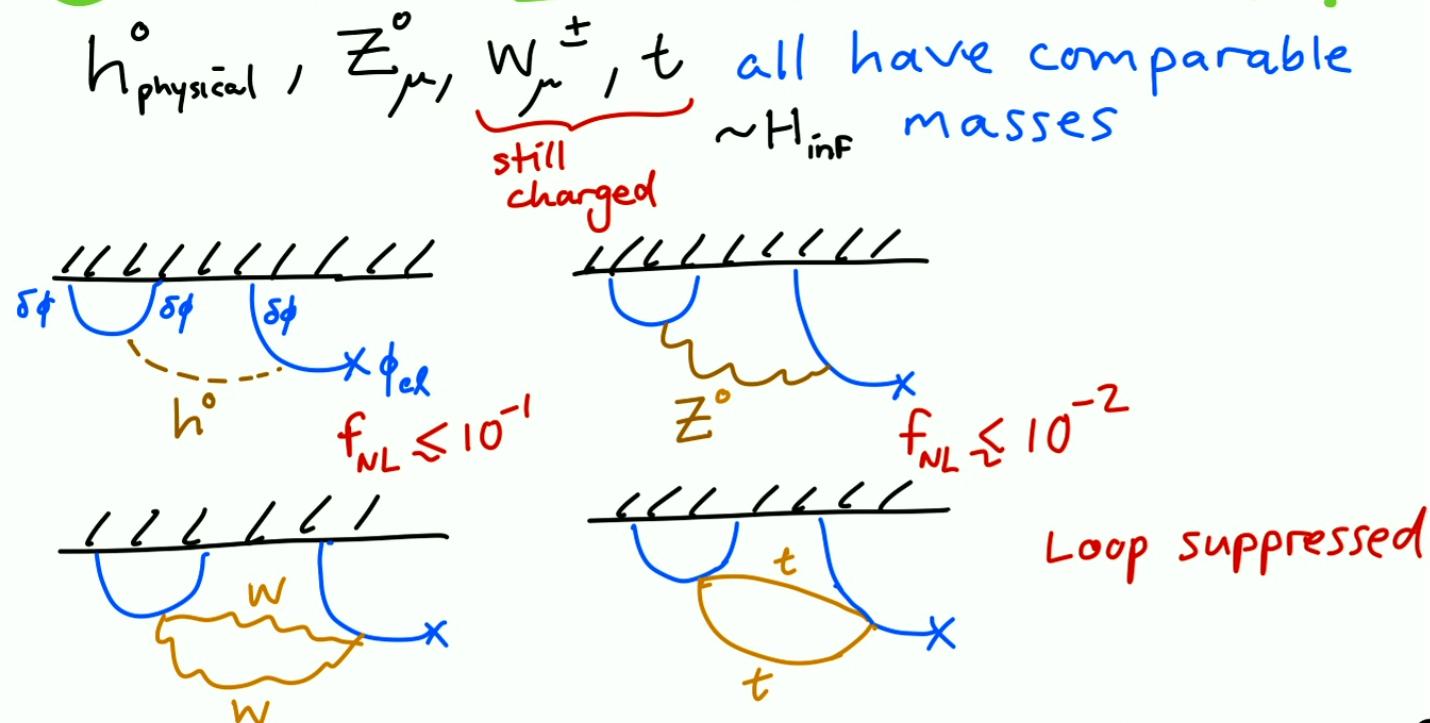


$$F \propto f_{NL} \sin^2 \Theta$$



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COULD WE SEE THE SM?



IF signals observable, the mass ratios eg. $\frac{m_W}{m_t} = \frac{g}{2\gamma_t}$
 would be unmodified, except for
calculable RG effects!

HIGGSED GAUGE THEORY

$$L_{\text{int.}} \supset \sqrt{-g} g^{\mu\nu} \left\{ \frac{\partial_\mu \phi \partial_\nu \phi \rho}{\Lambda} + \frac{\partial_\mu \phi h^\dagger D_\nu h \rho}{\Lambda^2} \right\}$$

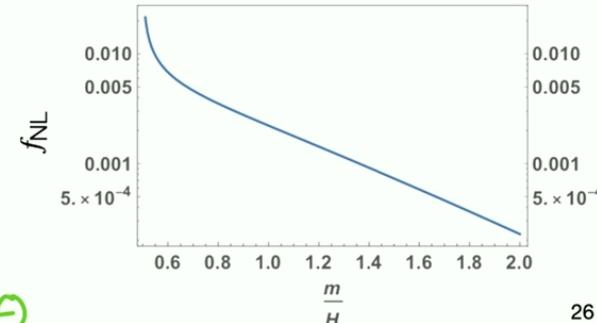
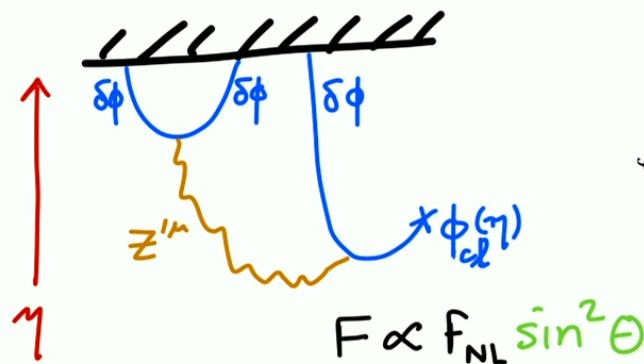
mediator $\Lambda > \dot{\phi}_{\text{cl}}$

$\xrightarrow{\text{integrate out } \rho, m_\rho > H}$ $\sqrt{-g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \partial_\alpha \phi Z'^\alpha / \frac{v^2}{\Lambda^3 m_\chi^2}$

$\langle h \rangle \lesssim v$ must be small enough to keep EFT control of $(\partial\phi)^n$ expansion

ORBIFOLD GUTs

$$L_{\text{int.}} \supset \sqrt{-g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \partial_\alpha \phi \partial_{x_5} Z'^\alpha_{B-L} / \Lambda^2 m_\chi^2$$



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COSMOLOGICAL COLLIDER PHYSICS & THE CURVATON

Kumar, Sundrum'19

(or how to have bigger signals WITH theoretical control)

Single-Field (ϕ) Slow-Roll Inflation $\Rightarrow \partial_t \phi \sim (60H)^2$

\Rightarrow Non-renormalizable suppression $\Lambda > 60H$ Creminelli'03
for EFT control.

Curvaton (X) Scenario : Enqvist, Sloth'01; Lyth, Wands'01;
Moroi, Takahashi'01

Job of driving inflation, $\phi_{cl}(\gamma)$, $V_{inf}(\phi_{cl})$

separated from job of seeding primordial

fluctuations : $\delta X_{\text{quantum}} > \delta \phi_{\text{quantum}}$
 $\xrightarrow{\text{decay}}$ SM

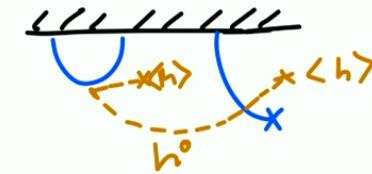
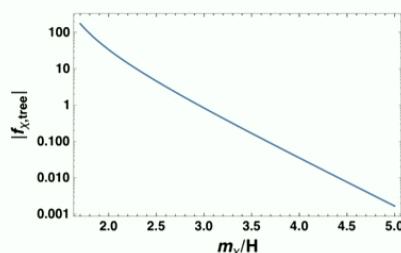
$\partial_t X_{cl} \sim H^2$, $V_{\text{curvaton}}(X_{cl}) \ll V_{\text{inflation}}(\phi_{cl}) \Rightarrow$

$\Lambda_{\text{non-renormalizable}} \gtrsim \text{few } H$

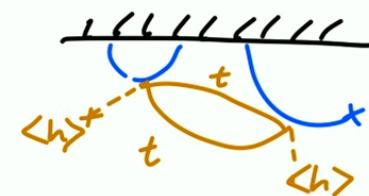
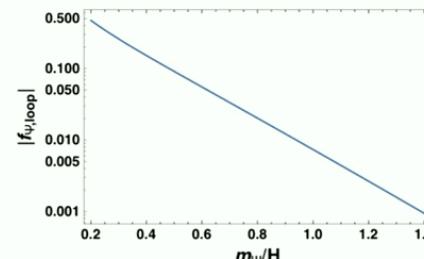
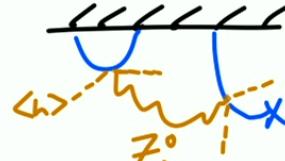
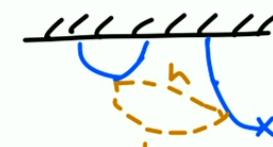
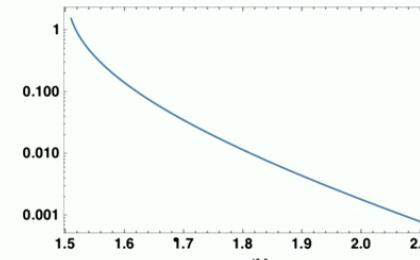
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$$\mathcal{L}_{\text{interactions}} \sim \sqrt{-g} P \left\{ g^{\mu\nu} \partial_\mu X \partial_\nu X + h^\dagger h + \bar{t}_R^i h(t_b^i) + g^{\mu\nu} \partial_\mu X h^\dagger D_\nu h + \dots \right\}$$

massive mediator



$$f_{NL}^{Z^\circ} \sim O(1)$$



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"Chemical Potential"

Radiative stability of $V_{\text{inf}}(\phi)$:

\Rightarrow Derivative couplings $(\partial\phi)^n \Theta_{\text{heavy particles}}$

Special case $n=1$: $\cancel{\frac{\partial_\mu \phi}{\Lambda} J^\mu_{\text{heavy}}} \rightarrow \frac{\dot{\phi}_{\text{cl}}}{\Lambda} J^0_{\text{heavy}}$

Inflationary heavy particle production \sim Boltzmann-ish $\sim e^{-m/T_{\text{Hawking}}}$
 $\uparrow H/2\pi$

EFT control $\Rightarrow \lambda \equiv \frac{\dot{\phi}_{\text{cl}}}{\Lambda} < \Lambda \quad \lambda < \sqrt{\dot{\phi}_{\text{cl}}} \sim 60H$

Applied to non-zero spin heavy particles:

Chen, Wang, Xianyu '18; Adshead, Pearce, Peloso, Roberts, Sorbo '18;

Wang, Xianyu '19; Hook, Huang, Racco '19

(Complex) Scalar Chemical Potential

Bodas, Kumar, Sundrum
'20

$$J_\mu = \sigma^* D_\mu \sigma, \quad \sigma = \sigma_1 + i \sigma_2$$

2 real heavy scalar

Eliminate by "gauge transformation":

$$\sigma \rightarrow e^{i\phi/\lambda} \sigma$$

∴ only physical in non-symmetric terms:

$$L \supset \cancel{\Theta(\sigma, \sigma^*)}_{\text{sym}} \rightarrow e^{iq\phi/\lambda} \cancel{\Theta(\sigma, \sigma^*)}_{\text{sym}}$$

$$\approx e^{\frac{iq\langle\phi\rangle_c t}{\lambda}} + iq\delta\phi/\lambda \Theta_{\cancel{\text{sym}}}(\sigma, \sigma^*)$$

$$= e^{iq\lambda t} e^{iq\delta\phi/\lambda} \Theta_{\cancel{\text{sym}}}(\sigma, \sigma^*)$$

v. high background frequency!

"Chemical Potential"

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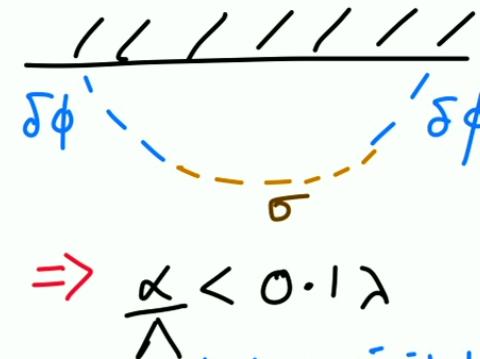
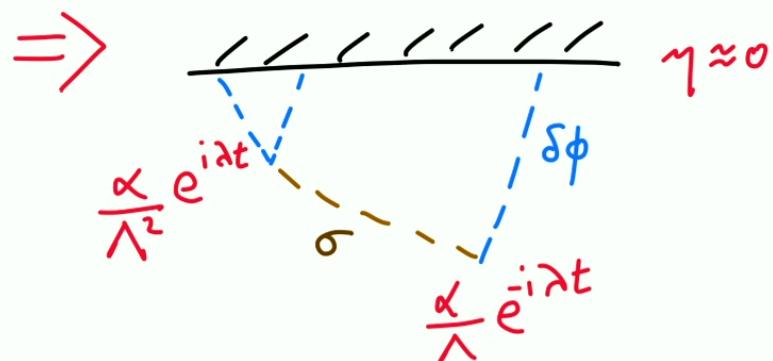
Wang, Xianyu '19; Hook, Huang, Racco '19

NEW PRIMORDIAL MAPS?

- CMB, LSS, (21-cm) consistent with single primordial source of fluctuations, via inflaton reheating
- New "map" of BSM origin may give complementary insights into inflation & extreme particle physics.
- Improved cosmic variance limitations?

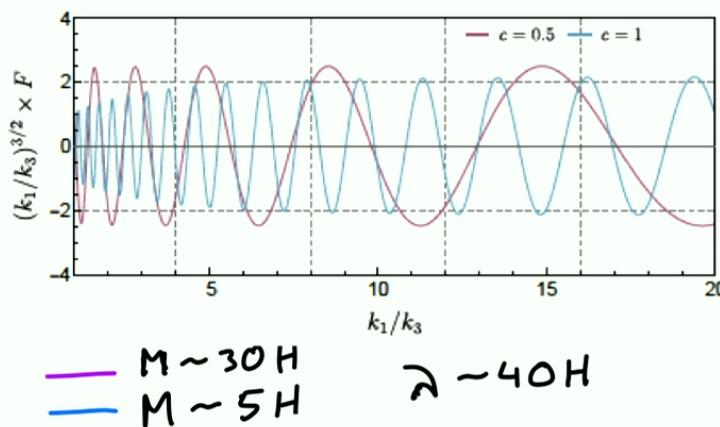
Most simply:

$$L \supset \alpha(\sigma + \sigma^*) \rightarrow \alpha e^{i\omega t} e^{i\delta\phi/\lambda} \sigma + \text{conjugate}$$



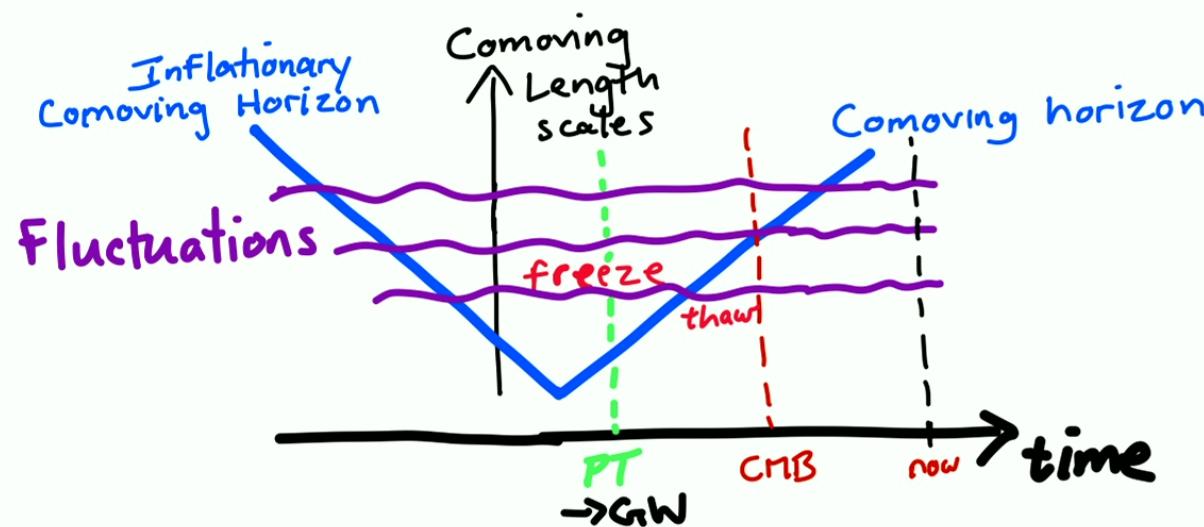
$$\Rightarrow \frac{\alpha}{\lambda} < 0.1 \lambda$$

to not be visible in CMB.



"PRISTINE" COSMOLOGICAL STOCHASTIC GW MAPS

Essentially no cosmic variance
limit in principle: spherical harmonics
 $l < 10^{14}$ outside horizon at time of
PT & GW production!



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