

Title: Quantum Matter Lecture (230414)

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Collection: Quantum Matter (2022/2023)

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URL: <https://pirsa.org/23040011>

CARTOON 3.

[Faint, mostly illegible handwritten notes and scribbles on the chalkboard]

CARTOON
4
Cartoons

$$|BCS\rangle = \prod_k (|u_k| + |v_k| e^{i\theta} c_{k\uparrow}^{\dagger} c_{-k\downarrow}^{\dagger})$$

$$H = -\sum_{\sigma} t_{ij} c_{i\sigma}^{\dagger} c_{j\sigma} + h.c.$$

$$c \rightarrow e^{-i\theta} c$$

$$c_{i\sigma}^{\dagger} \rightarrow e^{i\theta} c_{i\sigma}^{\dagger}$$

$$[H, \sum_{\sigma} c_{i\sigma}^{\dagger} c_{i\sigma}] = 0$$

U(1)

H

$$\psi(r_1, r_2) = \psi(r_2, r_1)$$

A

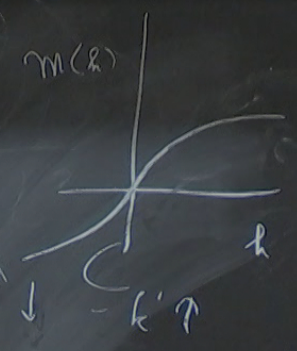
$3N$

$$J \vec{s}_1 \cdot \vec{s}_2$$

$$c_{\uparrow\downarrow} + h.c.$$

$$|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$

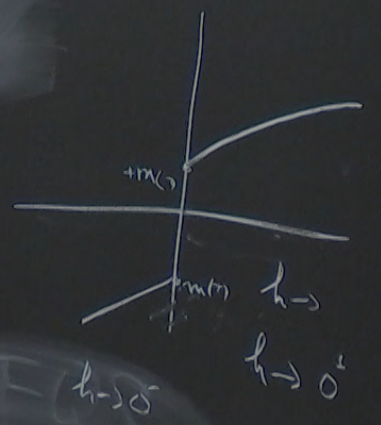
$$-V \sum_{\langle ij \rangle} (c_{i\uparrow}^\dagger c_{j\uparrow}^\dagger + c_{i\downarrow}^\dagger c_{j\downarrow}^\dagger + h.c.)$$



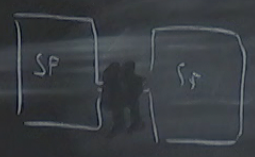
$$\sum_{\sigma} c_{\sigma}^\dagger c_{\sigma} = 0$$

Lieb-Schultz-Thomson

$$V \Delta_{\sigma} \sum_{\langle ij \rangle} (c_{i\sigma}^\dagger c_{j\sigma}^\dagger + h.c.)$$



(ZN)

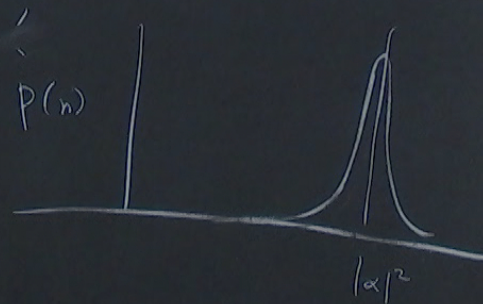


a^\dagger, a

$$[a, a^\dagger] = 1$$

$$|\alpha\rangle = e^{-\alpha a^\dagger} |0\rangle$$

$$|\alpha|^2 \sim N$$



Gaussian Integral

$$\frac{1}{\sigma\sqrt{\pi}} \int_{-\infty}^{\infty} e^{-\frac{x^2}{2\sigma^2}} dx = 1$$

$$\int_{-\infty}^{\infty} e^{-\pi x^2} dx = 1$$

$$e^{-a^2} = \int_{-\infty}^{\infty} e^{-\pi x^2 - 2\sqrt{\pi} a x} dx$$

$$\int_{-\infty}^{\infty} e^{-\pi(x-a)^2} dx = 1$$

Hubbard PRL (1999)

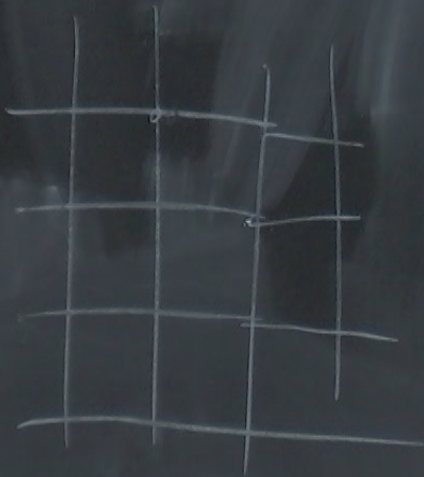
Hubbard-Stratonovic Identity

Hubbard PRL (1959)

Hubbard-Stratonovic Identity

Polyakov

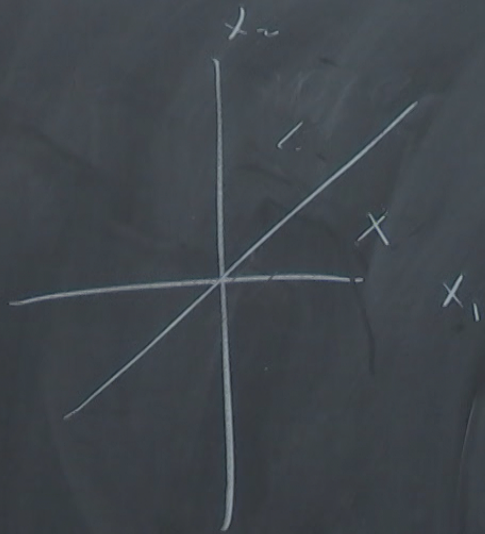
Weiss



$$S_i^z = \pm 1$$

$$H = -J \sum_{\langle i,j \rangle} S_i^z S_j^z - h \sum_i S_i^z$$

$$Z(\beta) = \sum_{\{S_i = \pm 1\}} e^{-\beta \sum_{\langle i,j \rangle} J S_i^z S_j^z - \beta \sum_i h S_i^z}$$



T_{re}

$$\sum k_{ij} s_i s_j$$

$= T_r$

$$\int \pi d\varphi \quad e$$

$$\rightarrow \int (\pi d\varphi) e$$

$$- \sum \varphi$$

$$- \sum \varphi k$$

$$m = \tanh\left(\frac{j^m}{kT}\right)$$

$$|\alpha\rangle = e^{-\alpha a^\dagger} |0\rangle$$

$$-\sum \varphi_i k_{ij} \varphi_j + \sum s_i k_{ij} \varphi_j$$

$$\int \pi d\varphi_i e^{-\dots}$$

$$|\alpha| \sim N$$

$$-\sum \varphi_i k_{ij} \varphi_j + \ln \cosh(\sum J_{ij} \varphi_j)$$

$$\cosh(\sum k_{ij} \varphi_j)$$

$$\int (\pi d\varphi_i) e^{-\dots}$$