

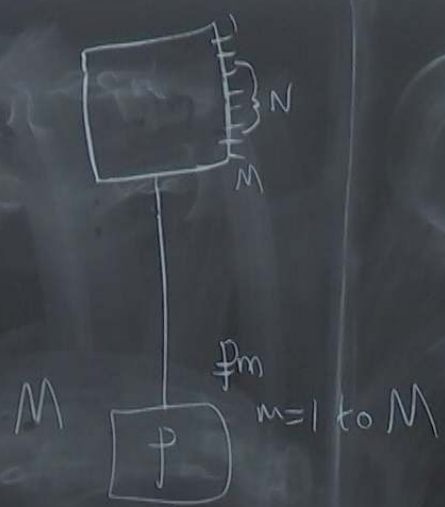
Title: Quantum Foundations Lecture - 230206

Speakers: Lucien Hardy

Collection: Quantum Foundations (2022/2023)

Date: February 06, 2023 - 10:15 AM

URL: <https://pirsa.org/23020017>



$f \in R, \dots \in R, z \in \Gamma$

## Postulates for QT

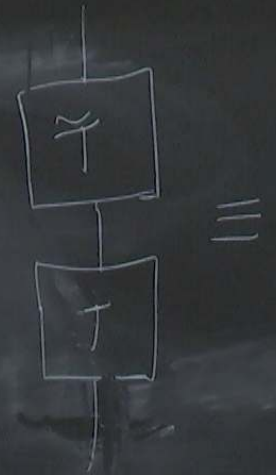
① Information Systems having, or constrained to have, a information carrying capacity have the same prop

② Information locality  $N_{ab} = N_a N_b$

③ Tomographic locality  $K_{ab} = K_a K_b$

④ Continuity. There exists a continuous reversible transformation between any pair of pure states for any given system.

ormation  
on system

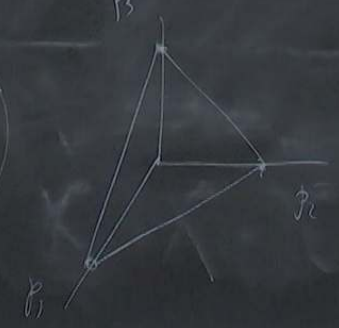
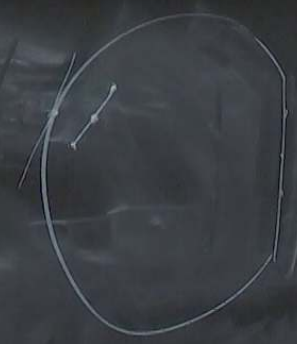


pure states are not mixed

Mixed state:  

$$P = \lambda P_A + (1-\lambda) P_B$$

$0 < \lambda < 1$      $P_A \neq P_B$



reversible take pure  $\rightarrow$  pure



④ Continuity There exists a continuous reversible transformation between any pair of pure states for any given system.

⑤ Simplicity Systems are described by the smallest number of probabilities consistent with the other postulates.  
(For each  $N$ ,  $K$  should be as small as possible.)

$$K = N^1 \quad K = N \times N \quad K = N^2$$

# The shape of Quantum State space

$$K = N^2$$

Normalized states

$$K-1 = N^2 - 1$$

Boundary of the  
normalised statespace

$$K-2 = N^2 - 2$$

Dim of pure states

=

# The shape of Quantum State space

$$K = N^2$$

Normalized states

$$K-1 = N^2 - 1$$

Boundary of the  
normalised statespace

$$K-2 = N^2 - 2$$

Dim of pure states

$$= 2N - 2$$

$$|\psi\rangle = \sum_{n=1}^N a_n |n\rangle$$

$$N=2$$

$$K=4$$

$$N=3$$

$$K-1=3$$

$$K-2=2$$

$$\text{puresub} = 2$$

Pringle space



pure

$$P = (1 - \lambda) \sum_{n=2}^{\infty} a_n |n\rangle \langle n| + \lambda |1\rangle \langle 1|$$



$$P = (1 - \lambda) \sum_{n=2}^{\infty} a_n |n\rangle \langle n| + \lambda |1\rangle \langle 1|$$

$$\lambda \geq 0$$

$$\rho = \rho^2 \quad \text{cond for purity}$$



$p_k = \text{quadratic fn of } p$

$$= q_k(p)$$

$N^2$  quadratic eqns.

Jones Linden 2004

Fuchs

0906.2187

0910.2750

$\rho$  is Hermitian

$$\text{tr}(\rho^2) = \text{tr}(\rho^3) = 1$$

$\Rightarrow \rho$  is pure

$\rho$  has eigenvalues  $\lambda_i$

$$\textcircled{1} \quad \sum_i \lambda_i^2 = 1$$

$$\textcircled{2} \quad \sum_i \lambda_i^3 = 1$$

$$|\lambda_i| \leq 1 \Rightarrow 1 - \lambda_i \geq 0 \quad \forall i$$

$$\textcircled{1} - \textcircled{2} \quad \sum_i \underbrace{\lambda_i^2(1 - \lambda_i)}_{\neq 0} = 0 \quad \lambda_i = 1 \text{ for at least one } i$$

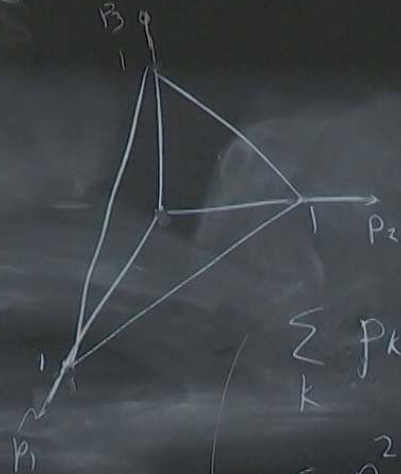
$\lambda_i = 1$  for one  $i$   
 $\lambda_j = 0$  for other cases.

quadratic( $p$ ) = 1

cubic( $p$ ) = 1

at least one  $i$

Classical case



$$\sum_k p_k = 1$$

$$\sum_k p_k^2 = 1$$

① Contextuality.

② Pusey, Barrett, Rudolph

③ Wigner's friend.

④ Spekkens' toy model

⑤ Weak measurements

Brukner

Renner

Lidia del Rio

