

Title: Quantum Foundations Lecture - 230130

Speakers: Lucien Hardy

Collection: Quantum Foundations (2022/2023)

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The many worlds interpretation (Everett 1957)

The axioms of MWI

① The ontology at time t is given by $|\psi(t)\rangle$

② The wavefn, $|\psi(t)\rangle$ evolves according to the Schrödinger eqn

$$i\hbar \frac{\partial |\psi\rangle}{\partial t} = \hat{H}|\psi\rangle$$

and U

Everett (1957)

and that's it!!

The claim is that this is sufficient

Everett (1957)

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The claim is that this is sufficient to

① recover appearances (tables, chairs, etc)

② recover the probabilistic predictions of Ψ .

Talks by D. Wallace

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(part of pirsar/cos001)

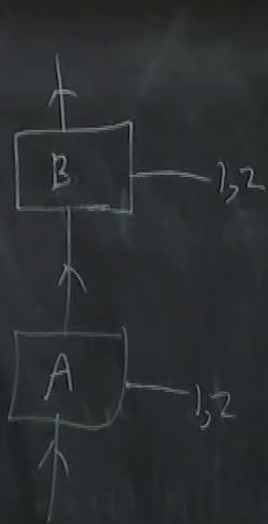
sufficient to
(tables, chairs, etc)
tic predictions of QT.

Two problems Wallace attempts to solve:

① where does the "world" structure come from and in what basis? (influenced by S. Saunders)

② where does the Born rule (prob = |amplitude|²) come from. (Influenced by D. Deutsch)

Wallace argues that worlds are emergent at macroscopic level.



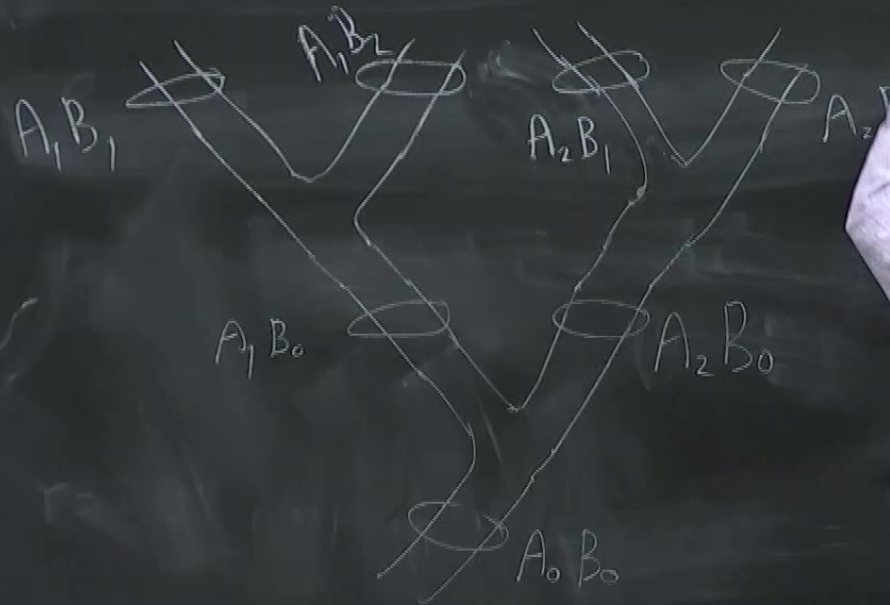
$$|\psi\rangle |A_0\rangle |B_0\rangle$$

$$\rightarrow \alpha |a_1\rangle |A_1\rangle |B_0\rangle + \beta |a_2\rangle |A_2\rangle |B_0\rangle$$

$$\rightarrow \alpha \gamma |b_1\rangle |A_1\rangle |B_1\rangle + \alpha \delta |b_2\rangle |A_1\rangle |B_2\rangle$$

$$+ \beta (-\delta^*) |b_1\rangle |A_2\rangle |B_1\rangle + \beta \gamma^* |b_2\rangle |A_2\rangle |B_2\rangle$$

Branching structure



$$+ \beta \langle 0 | b_1 \rangle |A_2\rangle |B_1\rangle + \beta \langle 0 | b_2 \rangle |A_1\rangle$$

What picks out the $A_{0,1}, B_{0,1}$ bases?

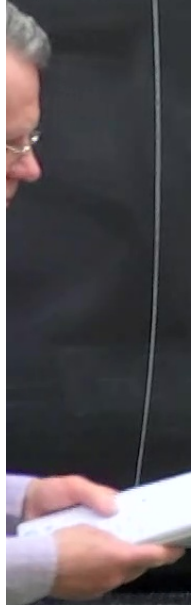
could have had $(A_0 \pm A_1), (B_0 \pm B_1)$

Interaction with environment

$$|A_i\rangle |E_0\rangle \rightarrow |A_i\rangle |E_i\rangle$$

$$\langle E_1 | E_2 \rangle \approx \delta_{12}$$

$A_2 B_2$



$$(|A_1\rangle + |A_2\rangle)|E_0\rangle \rightarrow (|A_1\rangle|E_1\rangle + |A_2\rangle|E_2\rangle)$$

$$|A_{3/4}\rangle|E_0\rangle \rightarrow$$



R (large)

Take $2M$ at large R

$$ds_{(2M)}^2 = \left(1 - \frac{2GM}{R}\right) dt^2 + R^2 d\Omega^2$$

$$n = -\sqrt{1 - \frac{2GM}{R}} \frac{\partial}{\partial R} \quad (\text{inward})$$

$$\begin{aligned} K &= \nabla_a n^a = \frac{1}{\sqrt{g}} \partial_a (\sqrt{g} n^a) \\ &= \frac{1}{r^2} \partial_r (r^2 \sqrt{1 - \frac{2GM}{r}}) \\ &= -\frac{2}{r} \sqrt{1 - \frac{2GM}{r}} - \frac{GM}{r^2 \sqrt{1 - \frac{2GM}{r}}} \\ &= -\frac{1}{r^2 \sqrt{1 - \frac{2GM}{r}}} \left[2\left(1 - \frac{2GM}{r}\right) + GM \right] \end{aligned}$$

$$\begin{aligned} K|_R &= -\frac{1}{R^2 \sqrt{1 - \frac{2GM}{R}}} [2R - 3GM] \\ \sqrt{h} d^3x &= R^2 \sin\theta \sqrt{1 - \frac{2GM}{R}} \frac{dr d\theta d\phi}{r^2} \frac{4\pi}{4\pi} \\ \Rightarrow \int K \sqrt{h} d^3x &= -4\pi \beta [2R - 3GM] \end{aligned}$$

DIVERGENT AS $R \rightarrow \infty$

But FLAT SPACE

$$ds^2 = dt_0^2 + R^2 d\Omega^2$$

$$K_0 = -\frac{2}{R}$$

$$\int K_0 \sqrt{h} d^3x = -4\pi \beta_0 \times 2R$$

also divergent.

Probability in MWI

The problem: Everything that has non-zero amplitude certainly happens.

$$|\psi\rangle|A_0\rangle \rightarrow \alpha|a_1\rangle|A_1\rangle + \beta|a_2\rangle|A_2\rangle$$

what if $\beta = 10^{-1000}$?

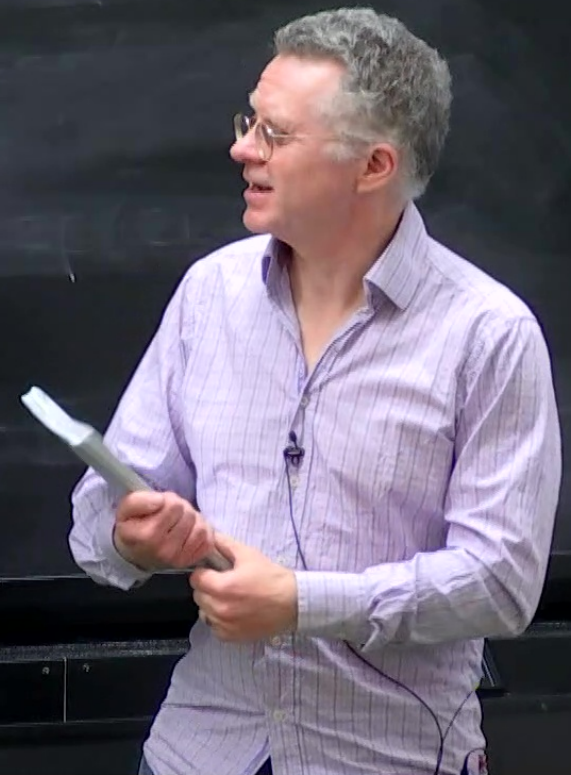
then probs = 10^{-2000} in regular QM

In MWI why not

Decision Theory

L. Savage found. of Stat.

states, S



Decision theory

L. Savage found. of Stat.

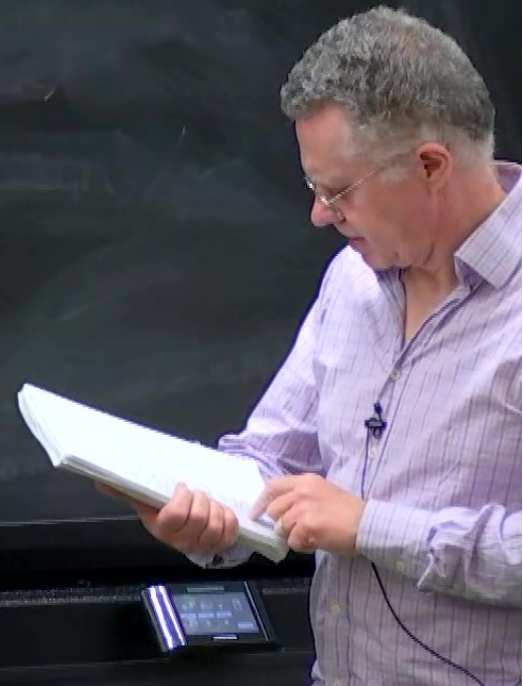
states, S

→ rewards, R .

→ bets, B

Impose axioms

$$b_1 > b_2$$



Decision theory

L. Savage found. of Stat.

states, S

→ rewards, R

→ bets, B

Impose axioms

$$b_1 > b_2, b_2 > b_3$$

$$b_1 > b_3$$

Get a representation theorem

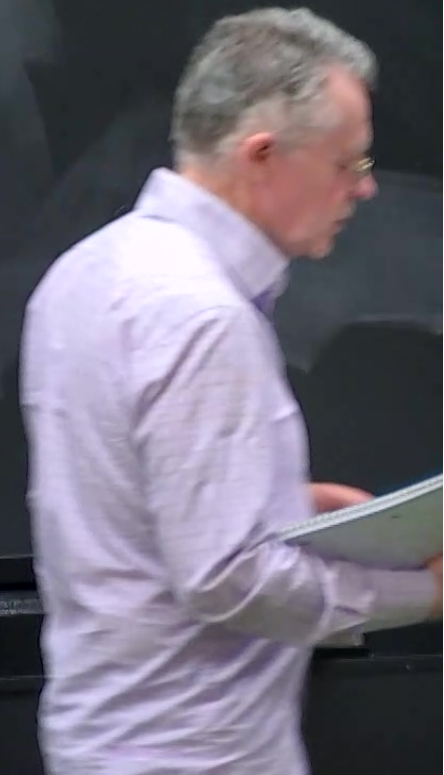
$$\exists \text{ a unique } p(s) \text{ s.t. } \sum_s p(s) = 1$$
$$p(s) \geq 0$$

Now need to show that

$$p = |\alpha|^2$$

The Principle Principle

A rational agent who knows that the objective probability is p is required to choose this as his subjective probability



How Wallace's proof works

- ① If two events have same weight $|\alpha|^2$ then agents are rationally required to give them the same prob (equivalence rule)
- ② Equivalence rule \Rightarrow Born rule.

$|b_1\rangle, |b_2\rangle, |B_1\rangle, |B_2\rangle$

bases?

$|B_1\rangle$

$|E_i\rangle$

Criticisms of MWI

- ① Probabilities. Jury is still out.
- ② Distasteful.
- ③ Progress in physics may undermine MWI

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w
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