

Title: Numerical Methods Lecture - 230112

Speakers: Erik Schnetter

Collection: Numerical Methods (2022/2023)

Date: January 12, 2023 - 9:15 AM

URL: <https://pirsa.org/23010003>

Introduction to Julia part 2 x

Code git Julia 1.8.5

Introduction to Julia, part 2

Erik Schnetter, 2023-01-12

```
[ ]:
```

The image shows a browser window with the URL `symmetry.pi.local`. The JupyterLab interface is visible, with a menu bar containing `File`, `Edit`, `View`, `Run`, `Kernel`, `Git`, `Tabs`, `Settings`, and `Help`. The memory usage is shown as `Mem:1.00 GB`. The active document is titled `Introduction to Julia part 2`. The document content includes the title `Introduction to Julia, part 2`, the author `Erik Schnetter, 2023-01-12`, and a plan for the day:

```
Plan for today:  
- defining types in Julia  
- defining packages in Julia
```

Below the plan, there is a code cell with the prompt `[]:` and an empty input area.



symmetry.pi.local



JupyterLab

File Edit View Run Kernel Git Tabs Settings Help

Mem:1.11 GB

Introduction to Julia part 2

Code git Julia 1.8.5

Introduction to Julia, part 2

Erik Schnetter, 2023-01-12

Plan for today:

- defining types in Julia
- defining packages in Julia

Types

```
[3]: struct IntPoint
      x::Int
      y::Int
      end
```

```
[*]: IntPoint(1, 2)
```

```
[ ]:
```



symmetry.pi.local



JupyterLab



File Edit View Run Kernel Git Tabs Settings Help

Mem:1.07 GB

Introduction to Julia part 2

Code git Julia 1.8.5

```
[6]: typeof(p)
```

```
[6]: IntPoint
```

```
[7]: p.x
```

```
[7]: 1
```

```
[8]: p.y
```

```
[8]: 2
```

```
[9]: struct FloatPoint
      x::Float64
      y::Float64
end
```

```
[10]: q = FloatPoint(1, 2)
```

```
[10]: FloatPoint(1.0, 2.0)
```

```
[ ]:
```

Introduction to Julia part 2

Code git Julia 1.8.5

```
end
```

```
[10]: q = FloatPoint(1, 2)
```

```
[10]: FloatPoint(1.0, 2.0)
```

```
[11]: q.x, q.y
```

```
[11]: (1.0, 2.0)
```

Generic types ¶

```
[12]: struct Point{T}
      x::T
      y::T
      end
```

```
[ ]: Point{Int}
```

Introduction to Julia part 2

Code git Julia 1.8.5

[10]: FloatPoint(1.0, 2.0)

[11]: q.x, q.y

[11]: (1.0, 2.0)

Generic types

```
[12]: struct Point{T}
      x::T
      y::T
      end
```

[13]: Point{Int}(1, 2)

[13]: Point{Int64}(1, 2)

[14]: Point{Float64}(1, 2)

[14]: Point{Float64}(1.0, 2.0)

[]:



symmetry.pi.local



JupyterLab

File Edit View Run Kernel Git Tabs Settings Help

Mem:1.28 GB

Introduction to Julia part 2

Code git Julia 1.8.5

Adding points

```
[16]: function add(p1::Point, p2::Point)
      x = p1.x + p2.x
      y = p1.y + p2.y
      return Point(x, y)
      end
```

```
[16]: add (generic function with 1 method)
```

```
[17]: p1 = Point{Int}(1, 2)
      p2 = Point{Int}(-1, 2)
      add(p1, p2)
```

```
[17]: Point{Int64}(0, 4)
```

```
[ ]:
```

symmetry.pi.local

JupyterLab

File Edit View Run Kernel Git Tabs Settings Help Mem:1.40 GB

Introduction to Julia part 2

Code Julia 1.8.5

Adding points

```
[16]: function add(p1::Point, p2::Point)
      x = p1.x + p2.x
      y = p1.y + p2.y
      return Point(x, y)
      end
```

```
[16]: add (generic function with 1 method)
```

```
[17]: p1 = Point{Int}(1, 2)
      p2 = Point{Int}(-1, 2)
      add(p1, p2)
```

```
[17]: Point{Int64}(0, 4)
```

```
[18]: supertype(Int)
```

```
[18]: Signed
```

```
[ ]:
```



```
[14]: Point{Float64}(1, 2)
```

```
[14]: Point{Float64}(1.0, 2.0)
```

Adding points

```
[16]: function add(p1::Point, p2::Point)
      x = p1.x + p2.x
      y = p1.y + p2.y
      return Point(x, y)
      end
```

```
[16]: add (generic function with 1 method)
```

```
[17]: p1 = Point{Int}(1, 2)
      p2 = Point{Int}(-1, 2)
      add(p1, p2)
```

```
[17]: Point{Int64}(0, 4)
```

```
[ ]: |
```

Introduction to Julia part 2

Code git Julia 1.8.5

Generic types

```
[12]: struct Point{T}
      x::T
      y::T
      end
```

```
[13]: Point{Int}(1, 2)
```

```
[13]: Point{Int64}(1, 2)
```

```
[14]: Point{Float64}(1, 2)
```

```
[14]: Point{Float64}(1.0, 2.0)
```

Adding points

```
[16]: function add(p1::Point, p2::Point)
      x = p1.x + p2.x
      y = p1.y + p2.y
      return Point(x, y)
      end
```



symmetry.pi.local



JupyterLab

File Edit View Run Kernel Git Tabs Settings Help

Mem:1.27 GB

Introduction to Julia part 2

Code git Julia 1.8.5

```
[16]: function add(p1::Point, p2::Point)
      x = p1.x + p2.x
      y = p1.y + p2.y
      return Point(x, y)
      end
```

```
[16]: add (generic function with 1 method)
```

```
[17]: p1 = Point{Int}(1, 2)
      p2 = Point{Int}(-1, 2)
      add(p1, p2)
```

```
[17]: Point{Int64}(0, 4)
```

Function overloading

```
[20]: 2 + 3
```

```
[20]: 5
```

```
[ ]:
```

symmetry.pi.local

JupyterLab

File Edit View Run Kernel Git Tabs Settings Help | Mem:1.40 GB

Introduction to Julia part 2

Code git Julia 1.8.5

```
add(p1, p2)
```

[17]: Point{Int64}(0, 4)

Function overloading

[20]: 2 + 3

[20]: 5

[21]: +(2, 3)

[21]: 5

```
[ ]: function Base.+(p1::Point, p2::Point)
    x = p1.x + p2.x
    y = p1.y + p2.y
    return Point(x, y)
end
```

Introduction to Julia part 2

Code git Julia 1.8.5

Function overloading

[20]: 2 + 3

[20]: 5

[21]: +(2, 3)

[21]: 5

```
[23]: function Base.:+(p1::Point, p2::Point)
      x = p1.x + p2.x
      y = p1.y + p2.y
      return Point(x, y)
      end
```

[24]: p1 + p2

[24]: Point{Int64}(0, 4)

[]: Base.:+(x::Int, y::Int) = x - y

Introduction to Julia part 2

Code git Julia 1.8.5

```
[ ]: Base.:+(x::Int, y::Int) = x - y
```

SYSTEM: show(lasterr) caused an error

Stacktrace:

- [1] getindex
@ ./array.jl:924 [inlined]
- [2] enq_work(t::Task)
@ Base ./task.jl:736
- [3] schedule(t::Task, arg::Any; error::Bool)
@ Base ./task.jl:800
- [4] schedule
@ ./task.jl:789 [inlined]
- [5] uv_writecb_task(req::Ptr{Nothing}, status::Int32)
@ Base ./stream.jl:1164
- [6] poptask(W::Base.InvasiveLinkedListSynchronized{Task})
@ Base ./task.jl:921
- [7] wait()
@ Base ./task.jl:930
- [8] uv_write(s::Base.PipeEndpoint, p::Ptr{UInt8}, n::UInt64)
- [9] flush(s::Base.PipeEndpoint)
@ Base ./stream.jl:1131
- [10] flush
@ ./io.jl:415 [inlined]

Introduction to Julia part 2

Code git Julia 1.8.5

[5]: p.y

[5]: 2

```
[6]: struct FloatPoint
      x::Float64
      y::Float64
end
```

[7]: q = FloatPoint(1, 2)

[7]: FloatPoint(1.0, 2.0)

[8]: q.x, q.y

[8]: (1.0, 2.0)

Generic types

```
[9]: struct Point{T}
      x::T
      y::T
end
```



symmetry.pi.local



JupyterLab

File Edit View Run Kernel Git Tabs Settings Help

Mem:1.56 GB

Introduction to Julia part 2

Code git

Julia 1.8.5

Function overloading

```
[14]: 2 + 3
```

```
[14]: 5
```

```
...
```

```
[15]: 5
```

```
[16]: function Base.:+(p1::Point, p2::Point)
      x = p1.x + p2.x
      y = p1.y + p2.y
      return Point(x, y)
      end
```

```
[17]: p1 + p2
```

```
[17]: Point{Int64}(0, 4)
```

```
[ ]:
```



symmetry.pi.local



JupyterLab



File Edit View Run Kernel Git Tabs Settings Help

Mem:1.56 GB

Introduction to Julia part 2

+ ✂ 📄 📁 ▶ ■ ↻ ⏩ Code ⌵ ⌚ git

Julia 1.8.5

```
end
```

```
[17]: p1 + p2
```

```
[17]: Point{Int64}(0, 4)
```

Mutable structs

```
[18]: mutable struct MPoint{T}
        x::T
        y::T
      end
```

```
[ ]: |
```

Introduction to Julia part 2

```
[22]: p.x = 14
```

[22]: 14

```
[23]: p
```

[23]: MPoint{Int64}(14, 3)

Dual Numbers

Complex:



Introduction to Julia part 2

```
[22]: p.x = 14
```

```
[22]: 14
```

```
[23]: p
```

```
[23]: MPoint{Int64}(14, 3)
```

Dual Numbers

```
Complex: a + i b ("algebraic definition")  
- two-vector of real numbers a, b  
- can add complex numbers, multiply by a real numbers  
Define: i^2 := -1  
(a+ib)*(c+id) = ac + ibc + iad + i^2bd  
              = ac - bd + i(bc + ad)  
- can multiply complex numbers  
- can divide (inverse of multiplication)
```

Introduction to Julia part 2

Markdown git

Julia 1.8.5

[22]: 14

[23]: p

[23]: MPoint{Int64}(14, 3)

Dual Numbers

Complex: $a + i b$ ("algebraic definition")

- two-vector of real numbers a, b
- can add complex numbers, multiply by a real numbers

Define: $i^2 := -1$

$$(a+ib)*(c+id) = ac + ibc + iad + i^2bd$$

$$= ac - bd + i(bc + ad)$$

- can multiply complex numbers
- can divide (inverse of multiplication)

Dual numbers: $a + \epsilon b$

- two-vector of real numbers a, b
- can add dual numbers, multiply by a real numbers

Define: $\epsilon^2 := 0$

$$(a + \epsilon b) * (c + \epsilon d) = ac + \epsilon (bc + ad)$$

Introduction to Julia part 2

Dual Numbers

Complex: $a + i b$ ("algebraic definition")

- two-vector of real numbers a, b
- can add complex numbers, multiply by a real numbers
- Define: $i^2 := -1$
- $(a+ib)*(c+id) = ac + ibc + iad + i^2bd$
 $= ac - bd + i(bc + ad)$
- can multiply complex numbers
- can divide (inverse of multiplication)

Dual numbers: $a + \epsilon b$

- two-vector of real numbers a, b
- can add dual numbers, multiply by a real numbers
- Define: $\epsilon^2 := 0$
- $(a + \epsilon b) * (c + \epsilon d) = ac + \epsilon (bc + ad)$
- can multiply dual numbers

Introduction to Julia part 2

Complex: $a + i b$ ("algebraic definition")

- two-vector of real numbers a, b
- can add complex numbers, multiply by a real numbers
- Define: $i^2 := -1$
- $(a+ib)(c+id) = ac + ibc + iad + i^2bd$
 $= ac - bd + i(bc + ad)$
- can multiply complex numbers
- can divide (inverse of multiplication)

Dual numbers: $a + \epsilon b$

- two-vector of real numbers a, b
- can add dual numbers, multiply by a real numbers
- Define: $\epsilon^2 := 0$
- $(a + \epsilon b) * (c + \epsilon d) = ac + \epsilon (bc + ad)$
- can multiply dual numbers
- can divide (inverse of multiplication)

symmetry.pi.local

JupyterLab

File Edit View Run Kernel Git Tabs Settings Help | Mem:2.13 GB

Introduction to Julia part 2

Code git Julia 1.8.5

- $(a+ib)(c+id) = ac + ibc + iad + i^2bd$
 $= ac - bd + i(bc + ad)$
- can multiply complex numbers
- can divide (inverse of multiplication)

Dual numbers: $a + \epsilon b$

- two-vector of real numbers a, b
- can add dual numbers, multiply by a real numbers
- Define: $\epsilon^2 := 0$
- $(a + \epsilon b) * (c + \epsilon d) = ac + \epsilon (bc + ad)$
- can multiply dual numbers
- can divide (inverse of multiplication)

$(x + \epsilon)^n = x^n + \epsilon n x^{(n-1)}$

[]:

Introduction to Julia part 2

Terminal 2

```
Desktop
dist
Documents
DualNumbers
etc
'FFT and Ylm.ipynb'
'FFT Example.ipynb'
FFTW-Playground.ipynb
FiniteDifferences.ipynb
gnuplot.ipynb
'Introduction to Julia 2023.ipynb'
'Introduction to Julia.ipynb'
'Introduction to Julia part 2 2023.ipynb'
Julia
Julia-Demo-20200729.ipynb
julia-mpi-symmetry.sh
jupyterhub_slurm_354479.log
jupyterhub_slurm_354657.log
lib
'Linear Algebra.ipynb'
eschnetter@cn002:~ (10:00:30)
$ cd DualNumbers
eschnetter@cn002:~/DualNumbers (10:00:38)
$ ls
Project.toml src
eschnetter@cn002:~/DualNumbers (10:00:40)
$ cat Project.toml
name = "DualNumbers"
uuid = "2008ef51-30f0-46f1-933e-d54484ac2fea"
authors = ["Erik Schnetter <schnetter@gmail.com>"]
version = "0.1.0"
slurmstats
Smoothing.ipynb
spaces-project
src
_ssh
test-symmetry.sh
tmp
Tutorial
tutorial2
Tutorial.ipynb
TWL-MPI.zip
Untitled1.ipynb
Untitled2.ipynb
Untitled3.ipynb
Untitled4.ipynb
Untitled.ipynb
varad
WGLMakie.ipynb
'Wolfram Mathematica'
work
```

Introduction to Julia part 2 × Terminal 2 ×

GNU nano 2.9.3 DualNumbers.jl

```
module DualNumbers  
  
greet() = print("Hello World!")  
  
end # module DualNumbers
```

Introduction to Julia part 2 × Terminal 2 ×

```
GNU nano 2.9.3 DualNumbers.jl
module DualNumbers
export Dual
"""
    Dual: A dual number
"""
struct Dual{T}
    real::T
    dual::T
end
end # module DualNumbers
```

[Wrote 13 lines]

```
module DualNumbers DualNumbers.jl
export Dual
"""
Dual: A dual number
"""
struct Dual{T}
    real::T
    dual::T
end
end # module DualNumbers
```

```
Introduction to Julia part 2
[24]: ]generate DualNumbers
Generating project DualNumbers
:
DualNumbers/Project.toml
DualNumbers/src/DualNumbers.jl
[*]: ]add Revise
[ ]:
```

```
module DualNumbers
export Dual
"""
    Dual: A dual number
"""
struct Dual{T}
    real::T
    dual::T
end
end # module DualNumbers
```

```
Introduction to Julia part 2
Code
```

```
Generating project DualNumbers
:
DualNumbers/Project.toml
DualNumbers/src/DualNumbers.jl
```

```
[25]: ]add Revise
```

```
Updating registry at `~/.julia/registries/General`
Updating git-repo `https://github.com/JuliaRegistries/General.git`
Resolving package versions...
No Changes to `~/.julia/environments/v1.8/Project.toml`
No Changes to `~/.julia/environments/v1.8/Manifest.toml`
```

```
[26]: using Revise
```

```
[ ]:
```

```
module DualNumbers
export Dual
...
Dual: A dual number
...
struct Dual{T}
  real::T
  dual::T
end
end # module DualNumbers
```

```
Updating registry at `~/.julia/registries/General`
Updating git-repo `https://github.com/JuliaRegistries/General.git`
Resolving package versions...
No Changes to `~/.julia/environments/v1.8/Project.toml`
No Changes to `~/.julia/environments/v1.8/Manifest.toml`
```

[26]: using Revise

[28]:

```
ArgumentError: Package DualNumbers not found in current path.
- Run `import Pkg; Pkg.add("DualNumbers")` to install the DualNumbers package.
```

```
Stacktrace:
 [1] macro expansion
   @ ./loading.jl:1163 [inlined]
 [2] macro expansion
   @ ./lock.jl:223 [inlined]
```

```

module DualNumbers
export Dual
"""
    Dual: A dual number
"""
struct Dual{T}
    real::T
    dual::T
end
end # module DualNumbers

```

Introduction to Julia part 2

Code

```

No Changes to `~/julia/environments/v1.8/Project.toml`
No Changes to `~/julia/environments/v1.8/Manifest.toml`

[26]: using Revise

[29]: ]activate DualNumbers

Activating project at `~/DualNumbers`

[30]: using DualNumbers

[ Info: Precompiling DualNumbers
[2008ef51-30f0-46f1-933e-d54484ac2fea]

[31]: ?Dual

search: Dual DualNumbers MethodSummary

[31]: Dual: A dual number

[ ]: x|

```

```
module DualNumbers
export Dual
"""
    Dual: A dual number
"""
struct Dual{T}
    real::T
    dual::T
end
end # module DualNumbers
```

- can divide (inverse of multiplication)

$$(x + \epsilon)^n = x^n + \epsilon n x^{(n-1)}$$

A package for dual numbers

```
[24]: ]generate DualNumbers
```

```
Generating project DualNumbers
:
DualNumbers/Project.toml
DualNumbers/src/DualNumbers.jl
```

```
[25]: ]add Revise
```

```
Updating registry at `~/julia/registries/General`
Updating git-repo `https://github.com/JuliaRegistries/General.git`
```

```
module DualNumbers
export Dual
"""
    Dual: A dual number
"""
struct Dual{T}
    real::T
    dual::T
end
end # module DualNumbers
```

```
thub.com/JuliaRegistries/General.
git`
Resolving package versions...
No Changes to `~/.julia/environ
ments/v1.8/Project.toml`
No Changes to `~/.julia/environ
ments/v1.8/Manifest.toml`

[26]: using Revise

[29]: ]activate DualNumbers

Activating project at `~/DualNu
mbers`

[30]: using DualNumbers

[ Info: Precompiling DualNumbers
[2008ef51-30f0-46f1-933e-d54484ac
2fea]

[31]: ?Dual

search: Dual DualNumbers MethodSu
mary

[31]: Dual: A dual number
```

Terminal 2

```
module DualNumbers Modified
export Dual
...
    Dual: A dual number
...
struct Dual{T}
    real::T
    dual::T
end

Base.:+(x::Dual, y::Dual) = Dual(x.r
end # module DualNumbers
```

Introduction to Julia part 2

Code

```
zTea]
[31]: ?Dual
search: Dual DualNumbers MethodSummary
[31]: Dual: A dual number
[32]: x = Dual(1, 2)
[32]: Dual{Int64}(1, 2)
[33]: y = Dual(2, 3)
[33]: Dual{Int64}(2, 3)
[34]: z = x + y
MethodError: no method matching +
(::Dual{Int64}, ::Dual{Int64})
Closest candidates are:
  +(::Any, ::Any, ::Any, ::Any...)
  at operators.jl:591
Stacktrace:
```

Terminal 2

GNU nano 2.9.3 DualNumbers.jl Modified

```
...
struct Dual{T}
  real::T
  dual::T
end

Base.:+(x::Dual, y::Dual) =

end # module DualNumbers
```

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos
^X Exit ^R Re^R Read File ^\ ReplaceText ^U Uncut Text ^T To Spell ^ Go To Line

Introduction to Julia part 2

Code git Julia 1.8.5

[]:

Terminal 2

GNU nano 2.9.3 DualNumbers.jl

```
module DualNumbers
export Dual
...
Dual: A dual number
...
struct Dual{T}
  real::T
  dual::T
end
```

[Wrote 15 lines]

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos
^X Exit ^R Re^R Read File ^\ ReplaceText ^U Uncut Text ^T To Spell ^ Go To Line

Introduction to Julia part 2

Code git

Julia 1.8.5

[34]: z = x + y

```
MethodError: no method matching +(::Dual{Int64}, ::Dual{Int64})
Closest candidates are:
  +(::Any, ::Any, ::Any, ::Any...) at operators.jl:591
```

```
Stacktrace:
 [1] top-level scope
      @ In[34]:1
```

Terminal 2

GNU nano 2.9.3 DualNumbers.jl

```
***
struct Dual{T}
  real::T
  dual::T
end
Base.:+(x::Dual, y::Dual) = Dual(x.real + y.real, x.dual + y.dual)
end # module DualNumbers
```

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos
^X Exit ^R Re^R Read File ^\ ReplaceText ^U Uncut Text ^T To Spell ^ Go To Line

Introduction to Julia part 2

Code git

Julia 1.8.5

[Info: Precompiling DualNumbers [2008ef51-30f0-46f1-933e-d54484ac2fea]

[31]: ?Dual

search: Dual DualNumbers MethodSummary

[31]: Dual: A dual number



symmetry.pi.local



JupyterLab

File Edit View Run Kernel Git Tabs Settings Help

Mem:1.50 GB

Terminal 2



GNU nano 2.9.3

DualNumbers.jl

```

"""
struct Dual{T}
    real::T
    dual::T
end
Base.:+(x::Dual, y::Dual) = Dual(x.real + y.real, x.dual + y.dual)
end # module DualNumbers

```

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos
^X Exit ^R Re^R Read File [\] ReplaceText ^U Uncut Text ^T To Spell [^] Go To Line

Introduction to Julia part 2

Code git

Julia 1.8.5

```

[33]: y = Dual(2, 3)
[33]: Dual{Int64}(2, 3)
[35]: z = x + y
[35]: Dual{Int64}(3, 5)

```

Terminal 2

GNU nano 2.9.3

DualNumbers.jl

```
"""  
struct Dual{T}  
    real::T  
    dual::T  
end  
  
Base.:+(x::Dual, y::Dual) = Dual(x.real + y.real, x.dual + y.dual)  
Base.:-(x::Dual, y::Dual) = Dual(x.real - y.real, x.dual - y.dual)  
  
end # module DualNumbers
```

[Wrote 16 lines]

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos
^X Exit ^R Re^R Read File ^\ ReplaceText ^U Uncut Text ^T To Spell ^ Go To Line

Introduction to Julia part 2

Code Julia 1.8.5

[33]: Dual{Int64}(2, 3)

[35]: z = x + y

[35]: Dual{Int64}(3, 5)

[36]: x - y

[36]: Dual{Int64}(-1, -1)

```
Terminal 2
eschnetter@cn002:~/DualNumbers/src (10:01:39)
$ nano DualNumbers.jl
eschnetter@cn002:~/DualNumbers/src (10:30:25)
$ ls
DualNumbers.jl
eschnetter@cn002:~/DualNumbers/src (10:30:30)
$ cd ..
eschnetter@cn002:~/DualNumbers (10:30:34)
$ ls
Project.toml src
eschnetter@cn002:~/DualNumbers (10:30:35)
$ mkdir test
eschnetter@cn002:~/DualNumbers (10:30:48)
$ cd test
eschnetter@cn002:~/DualNumbers/test (10:30:52)
$
```

```
Introduction to Julia part 2 x
Code git Julia 1.8.5
[33]: Dual{Int64}(2, 3)
[35]: z = x + y
[35]: Dual{Int64}(3, 5)
[36]: x - y
[36]: Dual{Int64}(-1, -1)
```

Terminal 2

GNU nano 2.9.3 runtests.jl Modified

```
using DualNumbers
using Test

x = Dual(1, 2)
y = Dual(2, 3)

z = x + y
@test z == Dual
```

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos
^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Spell ^ Go To Line

Introduction to Julia part 2

Code git Julia 1.8.5

[33]: Dual{Int64}(2, 3)

[35]: z = x + y

[35]: Dual{Int64}(3, 5)

[36]: x - y

[36]: Dual{Int64}(-1, -1)

Terminal 2

GNU nano 2.9.3 runtests.jl

```
using DualNumbers
using Test

x = Dual(1, 2)
y = Dual(2, 3)

z = x + y
@test z == Dual(3, 5)
```

[Wrote 9 lines]

Get Help Write Out Where Is Cut Text Justify Cur Pos
Exit Read File Replace Uncut Text To Spell Go To Line

Introduction to Julia part 2

Code git Julia 1.8.5

```
[56ddb016] Logging `@stdlib/Logging`
[d6f4376e] Markdown `@stdlib/Markdown`
[9a3f8284] Random `@stdlib/Random`
[ea8e919c] SHA v0.7.0 `@stdlib/SHA`
[9e88b42a] Serialization `@stdlib/Serialization`
[8dfed614] Test `@stdlib/Test`
Testing Running tests...
Testing DualNumbers tests passed
```

Terminal 2

GNU nano 2.9.3 runtests.jl

```
using DualNumbers
using Test

x = Dual(1, 2)
y = Dual(2, 3)

z = x + y
@test z == Dual(3, 5)
```

[Wrote 9 lines]

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos
^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Spell ^_ Go To Line

Introduction to Julia part 2

Code git Julia 1.8.5

```
[9a3f8284] + Random
[ea8e919c] + SHA v0.7.0
[9e88b42a] + Serialization
[8dfed614] + Test
Precompiling project...
  ✓ DualNumbers
  1 dependency successfully precompiled in 0 seconds
  1 dependency precompiled but a different version is currently loaded. Restart julia to access the new version
```

Terminal 2

GNU nano 2.9.3 DualNumbers.jl Modified

```
Base.:- (x::Dual) = Dual(-x.real, -x.dual)

Base.:+ (x::Dual, y::Dual) = Dual(x.real + y.real, x.dual + y.dual)
# Base.:- (x::Dual, y::Dual) = Dual(x.real - y.real, x.dual - y.dual)
Base.:- (x::Dual, y::Dual) = x +

end # module DualNumbers
```

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos
^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Spell ^_ Go To Line

Introduction to Julia part 2

Code git Julia 1.8.5

```
[ea8e919c] + SHA v0.7.0
[9e88b42a] + Serialization
[8dfed614] + Test
Precompiling project...
  ✓ DualNumbers
  1 dependency successfully precompiled in 0 seconds
  1 dependency precompiled but a different version is currently loaded. Restart julia to access the new version
```

Terminal 2

GNU nano 2.9.3 DualNumbers.jl

```

"""
struct Dual{T}
    real::T
    dual::T
end

Base.:- (x::Dual) = Dual(-x.real, -x.dual)

Base.:+ (x::Dual, y::Dual) = Dual(x.real + y.real, x.dual + y.dual)
# Base.:- (x::Dual, y::Dual) = Dual(x.real - y.real, x.dual - y.dual)
Base.:- (x::Dual, y::Dual) = x + -y

```

[Wrote 19 lines]

^G Get Help	^O Write Out	^W Where Is	^K Cut Text	^J Justify	^C Cur Pos
^X Exit	^R Read File	^_ Replace	^U Uncut Text	^T To Spell	^_ Go To Line

Introduction to Julia part 2

Code git

Julia 1.8.5

```

[ea8e919c] + SHA v0.7.0
[9e88b42a] + Serialization
[8dfed614] + Test
Precompiling project...
  ✓ DualNumbers
  1 dependency successfully precompiled in 0 seconds
  1 dependency precompiled but a different version is currently loaded. Restart julia to access the new version

```