

Title: GWs from high-quality axionic defects

Speakers: Oriol Pujolas

Series: Particle Physics

Date: July 20, 2022 - 1:00 PM

URL: <https://pirsa.org/22070027>

Abstract: The axion solution to the strong CP problem has many virtues but it suffers from the so-called quality problem. This problem is avoided in heavy axion realizations which, however, are harder to probe experimentally. I will show how generic heavy axion models can be tested in current and future gravitational wave (GW) observatories, due to the cosmological GW background produced by the axionic topological defects. Moreover, the resulting GW signal is correlated with a sizable strong CP phase, within reach of upcoming neutron electric dipole moment measurements.

Zoom link: <https://pitp.zoom.us/j/99150077172?pwd=UWhkZVdzV2lCQittWXVtMnludXBkUT09>

# GWs from high-quality axionic defects

Oriol Pujolàs

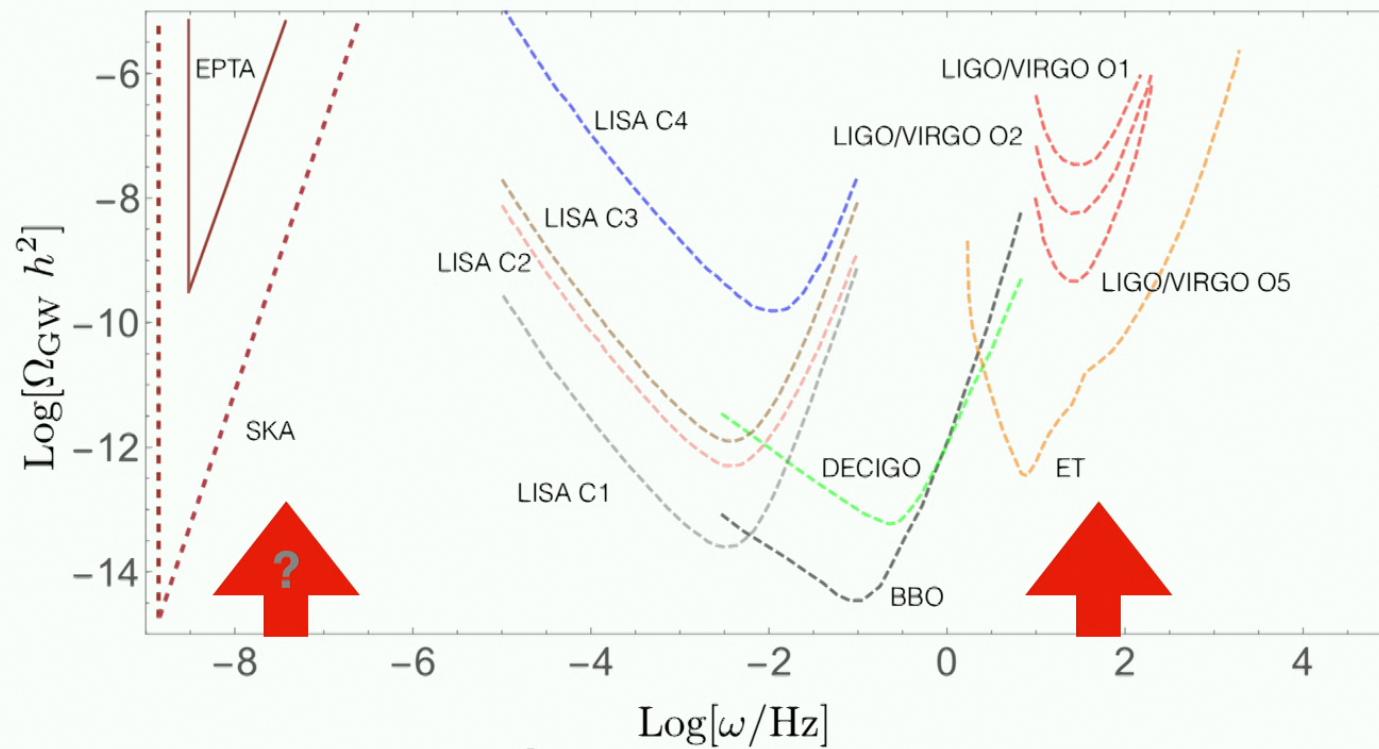
IFAE, UAB, Barcelona



@ Perimeter Institute  
July 20 2022

# GWs

- LIGO/Virgo/Kagra, PTAs (and coming): new window, with impressive views!



# GWs

- LIGO/Virgo/Kagra, PTAs (and coming): new window, with impressive views!
- From HEP perspective: **relic stochastic GWB**
- E.g., LVK sensitive to cosmological phase transitions at  **$T \sim 10^8 \text{ GeV}$** 
  - > close to a *usual suspect*: **Peccei-Quinn scale,  $10^9 - 10^{11} \text{ GeV}$**

# plan

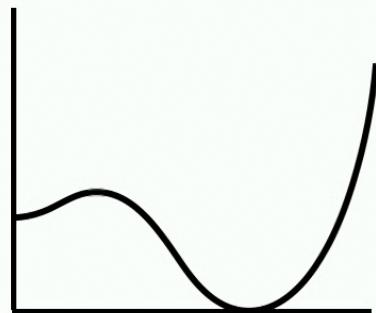
I) GWs from a 1st order Peccei Quinn transition

II) GWs from strings & domain walls in heavy axions

→ post-inflationary PQ – most constrained, but *still* viable

$$10^9 \text{ GeV} < f_a < 10^{11} \text{ GeV}$$

## I) GWs from a 1st order Peccei Quinn transition



# Peccei-Quinn Phase Transition at LIGO

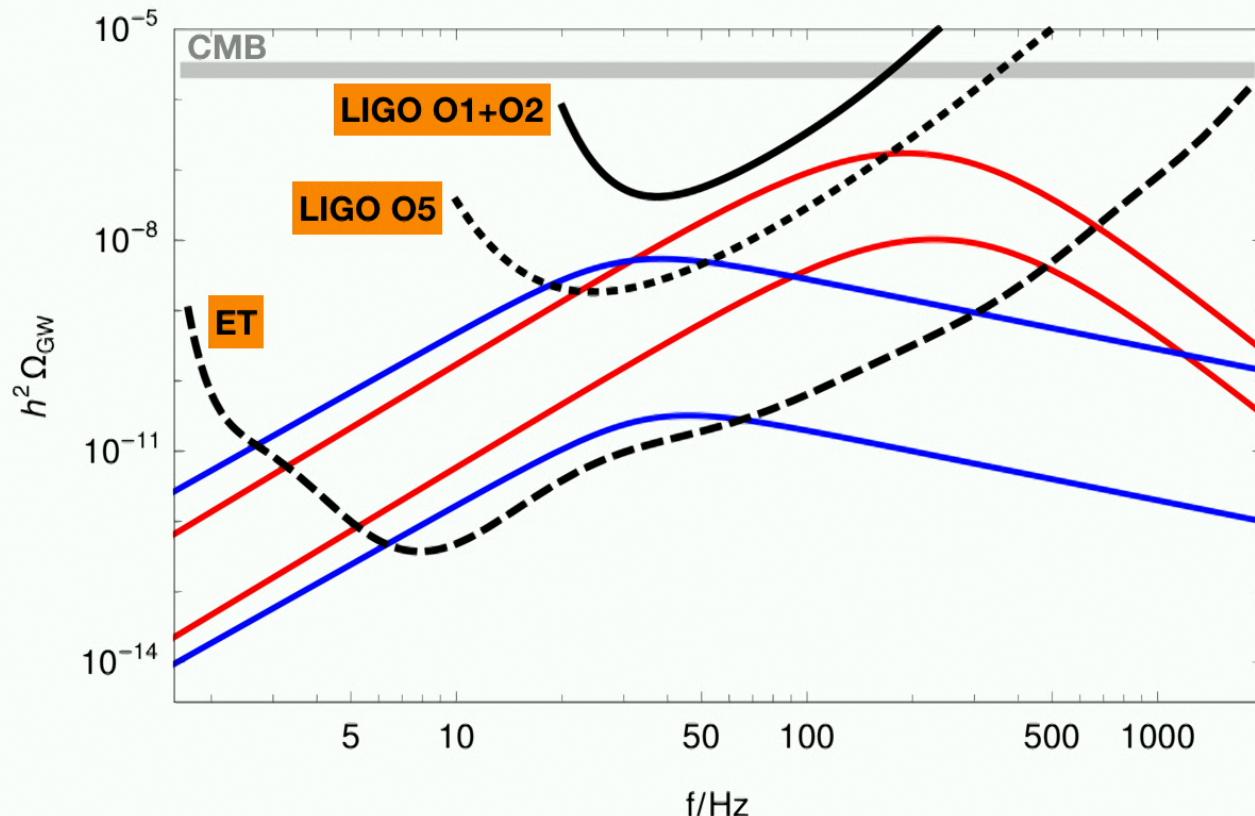
Benedict von Harling<sup>a</sup>, Alex Pomarol<sup>a,b</sup>, Oriol Pujolàs<sup>a</sup>

and Fabrizio Rompineve<sup>c</sup>

**arXiv:1912.07587**  
**JHEP 04 (2020) 195**

also:  
arXiv:1912.06139  
JHEP 04 (2020) 025  
Delle Rose, Panico, Redi, Tesi

## Are there axion models with strong enough 1st order transition to lead to detectable GWs at LVK?

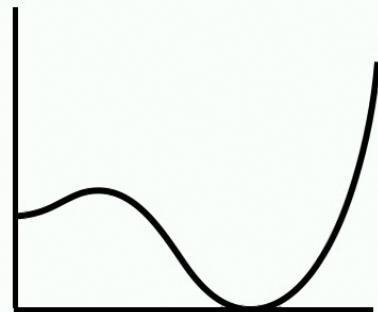


$$F_a = 10^8 \text{ GeV} \text{ with } \alpha \approx 3.5$$

$$F_a = 10^9 \text{ GeV} \text{ with } \alpha \sim 10^6$$

## “ABC” of (1st order) cosmological phase transitions

$\alpha = \frac{\Delta V}{\rho_\gamma(T_n)}$	latent heat (~strength)
$\beta = \frac{\dot{\Gamma}}{\Gamma} \Big _{T_n}$	inverse duration
$\Gamma = \mathcal{A} e^{-S_B}$	nucleation rate
$T_n$	nucleation temperature
$T_*$	transition completed



## Axion models with strong PT:



- **KSVZ** (Kim, Shifman, Vainshtein, Zakharov)  
*=> extra heavy quarks with PQ-charge*



- **DFSZ** (Dine, Fischler, Srednicki, Zhitnitsky)  
*=> extra Higgs doublet with PQ-charge*

$$V = \lambda_\phi(|\Phi|^2 - f^2/2)^2 + |H_1|^2(\kappa_1|\Phi|^2 - \mu_1^2) + |H_2|^2(\kappa_2|\Phi|^2 + \mu_2^2) - (\kappa_3\Phi^n H_1 H_2 + h.c.) \\ + \lambda_1|H_1|^4 + \lambda_2|H_2|^4 + \lambda_3|H_1 H_2|^2 + \lambda_4|H_1|^2|H_2|^2,$$

**DFSZ type models give strong PT**

**when close to scale invariant**

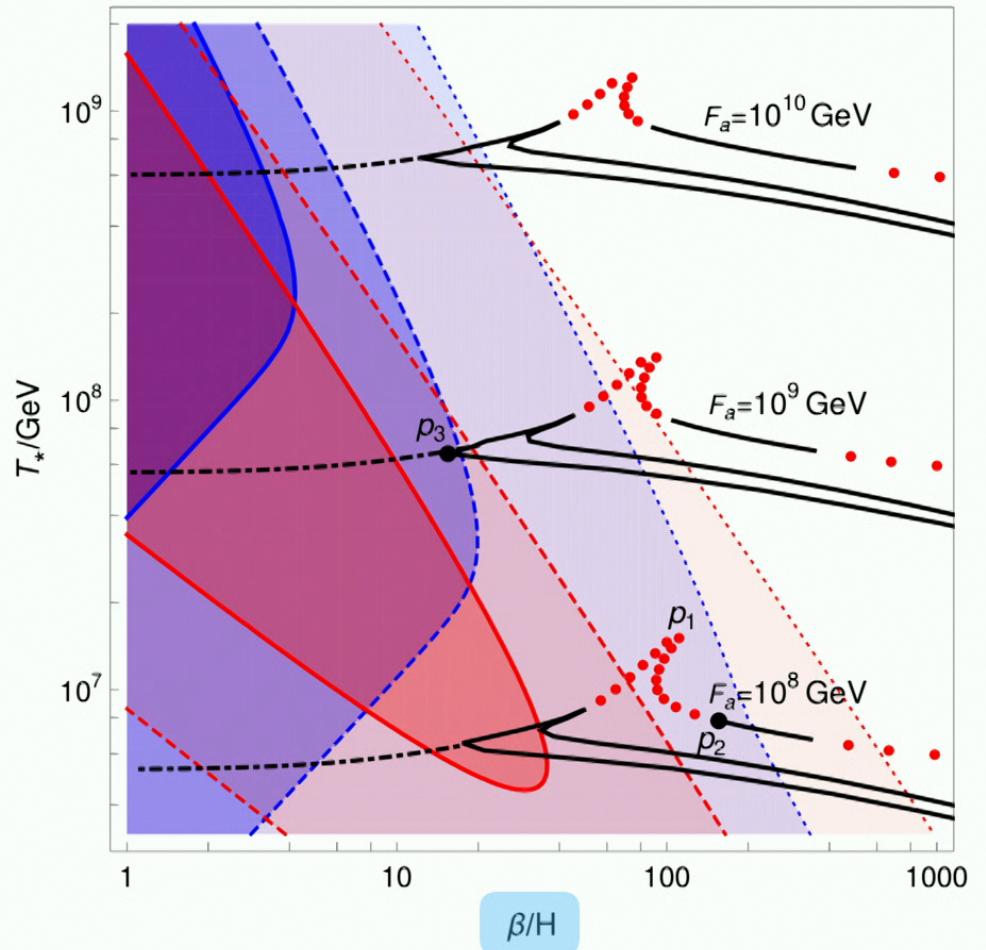
$$\mu_2^2, \lambda_\phi f^2 \ll f^2$$

$$V = \frac{1}{4} \lambda_\phi(\phi) \phi^4$$

$$T_* \simeq 0.1 \sqrt{\kappa_2} F_a$$

**$T_*$  is ~ 1 order of magnitude below  $F_a$**

(solid black line:  $\alpha > 3$ )

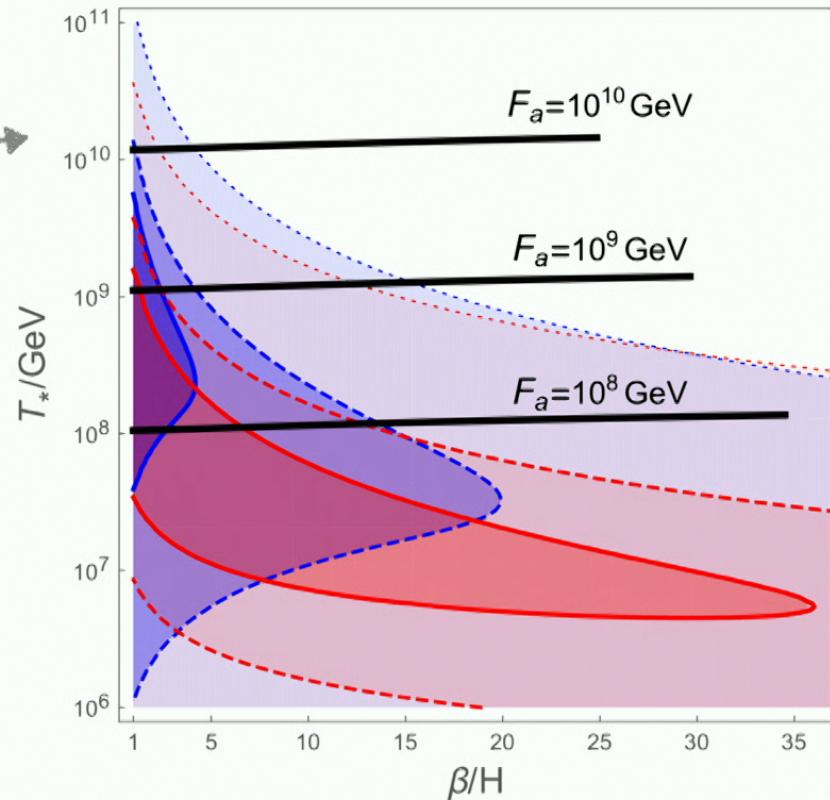


## KSVZ/DFSZ can be embedded in larger new physics sectors

- SUSY version of KSVZ
- Strong dynamics

both of them also lead to strong PTs

already  
ruling-out  
some  
parameter  
space!



## LIGO/Virgo search on SGWB from 1st order phase transitions:

Phys.Rev.Lett. 126 (2021) 15, 151301  
arXiv:2102.01714

Phenomenological model (bubble collisions)				
		$\Omega_{\text{coll}}^{95\%}$ (25 Hz)		
$\beta/H_{\text{pt}}$	$T_{\text{pt}}$	$10^7$ GeV	$10^8$ GeV	$10^9$ GeV
1		$1.0 \times 10^{-8}$	$8.4 \times 10^{-9}$	$5.0 \times 10^{-9}$
10		$4.0 \times 10^{-9}$	$6.3 \times 10^{-9}$	—

TABLE III: The 95% CL upper limits on  $\Omega_{\text{coll}}^{95\%}$  (25 Hz) for fixed values of  $\beta/H_{\text{pt}}$  and  $T_{\text{pt}}$ , and  $v_w = \kappa_\phi = 1$ . The dashed lines denote no sensitivity for exclusion.

=> some models start to getting ruled out already

# Conclusions

- LIGO/Virgo are sensitive to cosmological phase transitions in the early universe at around  $10^8 \text{ GeV}$  — HEP!
- Relevant for axion physics: we can tell whether PQ phase transition was strong!
- LVK are sensitive to PQ models close to scale invariant (Coleman-Weinberg): DFSZ, strong dynamics, SUSY-KSVZ...
- Prospects for the CE & ET are promising
- Complementary to other gravitational axion tests, superradiance

## **II) GWs from strings & domain walls in heavy axions**

## **II) GWs from strings & domain walls in heavy axions**

**High Quality QCD Axion at Gravitational Wave Observatories**

Ricardo Z. Ferreira,<sup>1,\*</sup> Alessio Notari,<sup>2,†</sup> Oriol Pujolàs,<sup>1,‡</sup> and Fabrizio Rompineve<sup>3,§</sup>

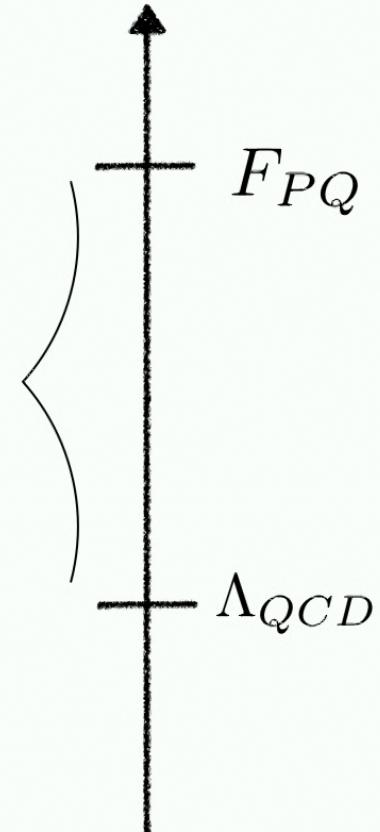
**arXiv:2107.07542**

**Phys.Rev.Lett. 128 (2022) 14, 141101**

# Axion *quality* problem

Axion solution to the strong CP problem (aka, Peccei-Quinn mechanism): **only QCD contributes to  $V(a)$**

Solution can be **spoiled** by any other "misaligned" sector



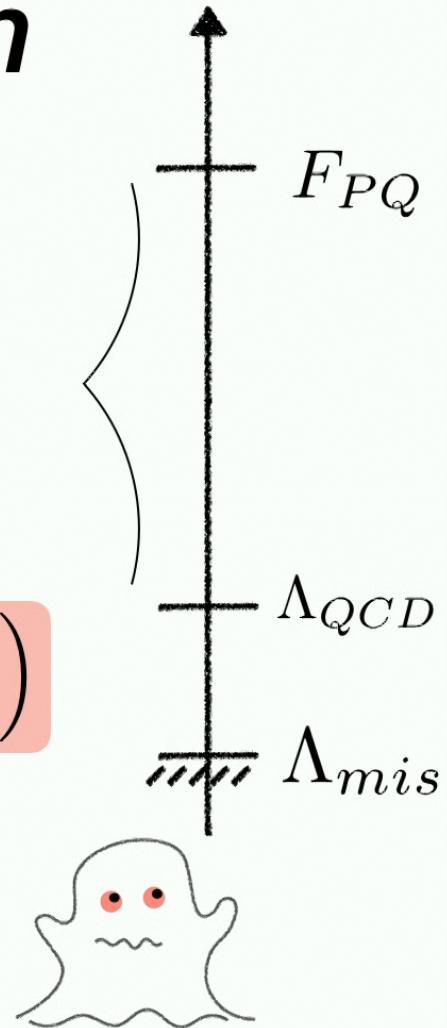
# Axion *quality* problem

Axion solution to the strong CP problem (aka, Peccei-Quinn mechanism): **only QCD contributes to  $V(a)$**

Solution can be **spoiled** by any other "misaligned" sector

$$V(a) = \Lambda_{QCD}^4 \left(1 - \cos(a)\right) + \Lambda_{mis}^4 \left(1 - \cos(a + \delta)\right)$$

**strong CP solved  $\Leftrightarrow$**   $\Delta\theta = \sin \delta \frac{\Lambda_{mis}^4}{\Lambda_{QCD}^4} \lesssim 10^{-10}$



**From the 'PQ-EFT' perspective, misaligned terms**

$$c_N \frac{\Phi^{4+N}}{M^N} \rightarrow \Lambda_{mis} = c_N^{1/4} \left( \frac{f}{M} \right)^{N/4} \lesssim 10^{-2.5} \Lambda_{QCD}$$

**Either first nonzero  $c_N$  has large N**

**Or PQ is nonperturbative ( $c_N$ 's exponentially suppressed)**

**In any case, robustness against this PQ is desirable**

push " $\Lambda_{QCD}$ " up  
*Heavy axion*

# Heavy axions

SM extended with (or embedded into) new sector with  $\Lambda \gg \Lambda_{QCD}$

$$V(a) = [\Lambda_{QCD}^4 + \Lambda^4] (1 - \cos(a))$$

- ***Mirror SM with softly broken  $Z_2$***
- ***Small instantons***
- ***Color - Dark Color unification***

# Heavy axions

**In practice:**

$$V(a) = \Lambda^4 \left( 1 - \cos(N_{DW} a) \right) + \Lambda_{mis}^4 \left( 1 - \cos(N'_{DW} a + \delta) \right)$$

$$f_a m_a = \Lambda^2 \gg \Lambda_{QCD}^2$$

$$m_a \simeq 10^8 \text{ GeV} \left( \frac{10^{12} \text{ GeV}}{f} \right) \left( \frac{\Lambda_H}{10^{10} \text{ GeV}} \right)^2$$

# Heavy axions

Heavy => decays quickly

Axions  $\neq$  DM

Heavy and weakly coupled => difficult to probe directly!

presence of the  
misaligned  
sector =>  $\theta \neq 0$

improving precision in neutron EDM  $d_n$

nEDM@SNS (1908.09937)  $\rightarrow$   $\Delta\theta \gtrsim 10^{-12}$

pEDM (2007.10332)  $\rightarrow$   $\Delta\theta \gtrsim 10^{-13}$

# Heavy axionic defects

$$\sigma_{DW} \sim m_a f_a^2 \quad \Rightarrow \text{ DWs are also } \textit{heavy}$$

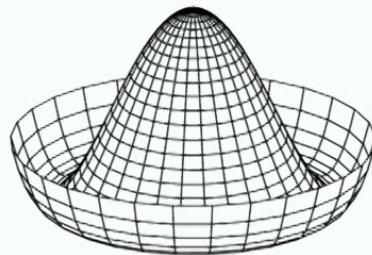
**DW motion induces *strong* GWs**

$$\rho_{GW} \sim \frac{\sigma_{DW}^2}{M_P^2}$$

# Axionic defects

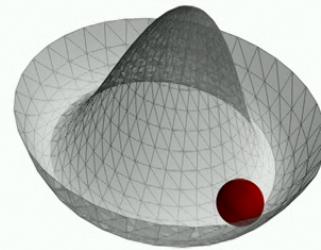
Peccei-Quinn mech: introduce a  $U(1)_{PQ}$  symmetry with 2 properties:

1) SB, i.e.:



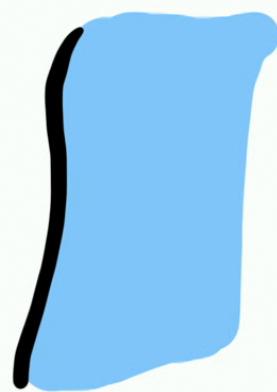
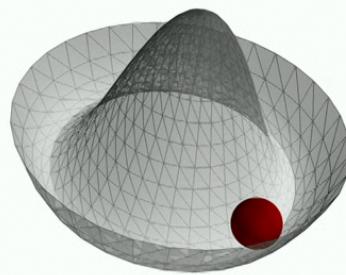
spont.  ~~$U(1)_{PQ}$~~  @  $f_a$

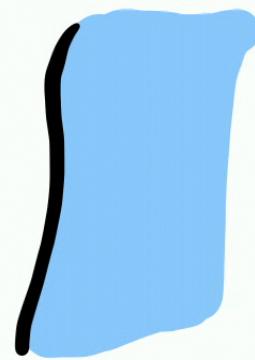
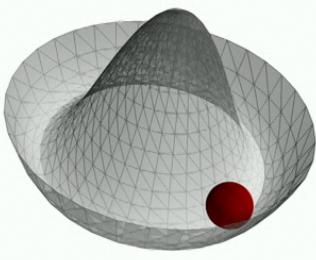
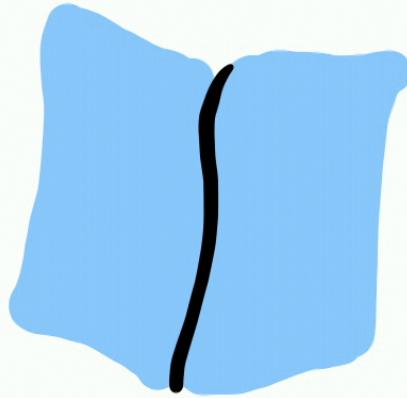
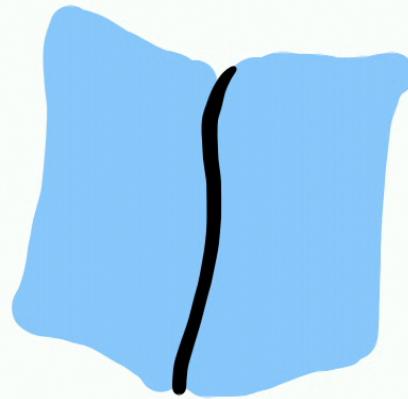
2)  $U(1)_{PQ} \text{SU}(3)_c \text{SU}(3)_c$  anomaly



expl.  ~~$U(1)_{PQ}$~~  @  $\Lambda_{QCD}$

$$N_{DW} = 1$$

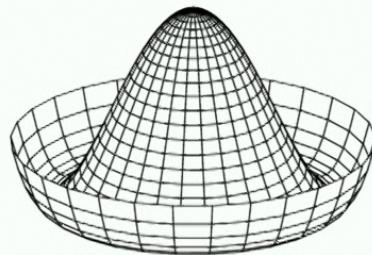


$N_{DW} = 1$  $N_{DW} = 2$ 

# Axionic defects

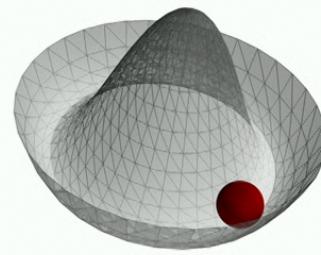
Peccei-Quinn mech: introduce a  $U(1)_{PQ}$  symmetry with 2 properties:

1) SB, i.e.:



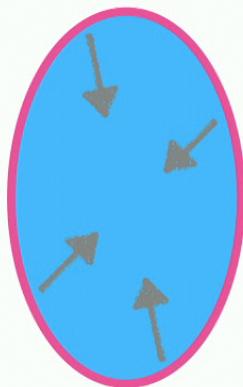
spont.  ~~$U(1)_{PQ}$~~  @  $f_a$

2)  $U(1)_{PQ} \text{SU}(3)_c \text{SU}(3)_c$  anomaly



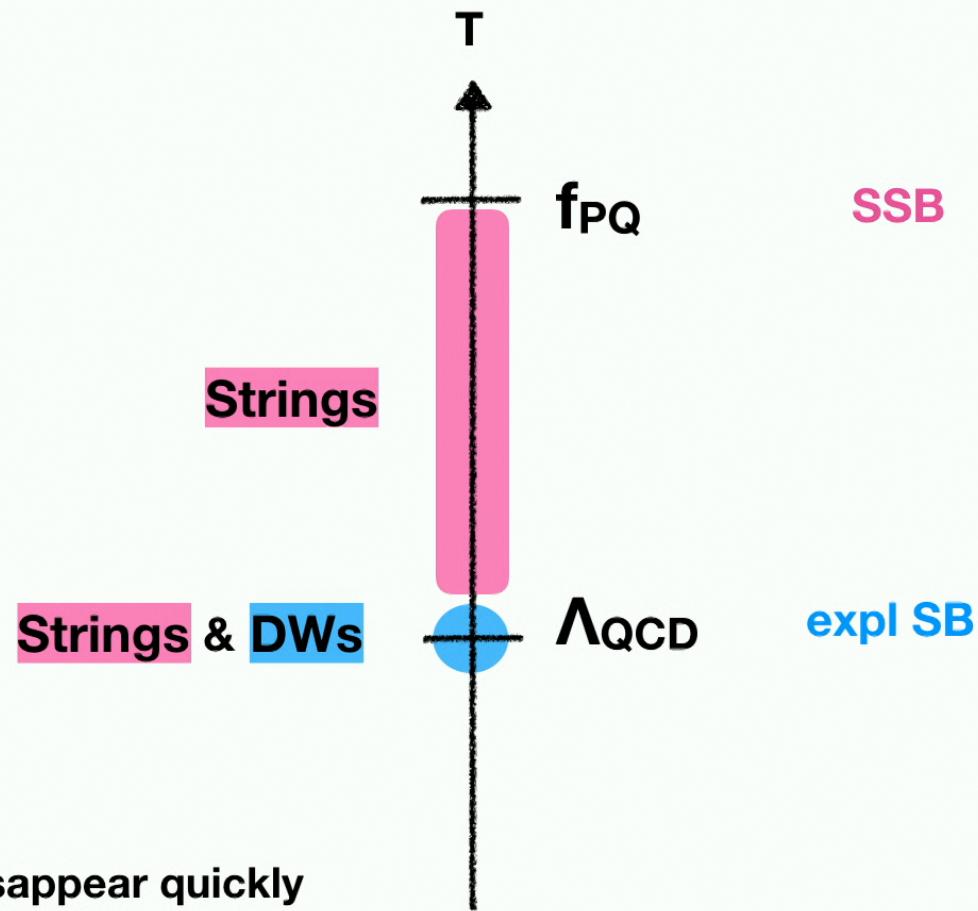
expl.  ~~$U(1)_{PQ}$~~  @  $\Lambda_{QCD}$

$$N_{DW} = 1$$

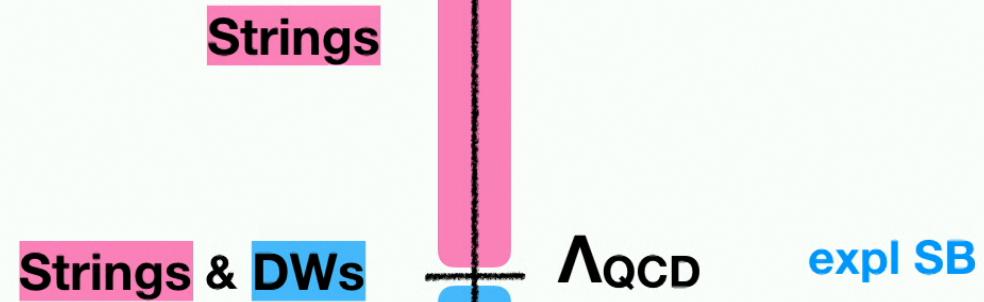
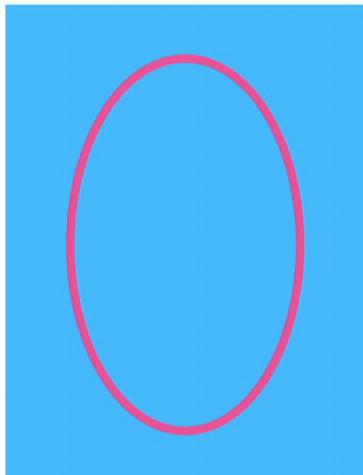


1 DW per string

DWs make the whole network disappear quickly

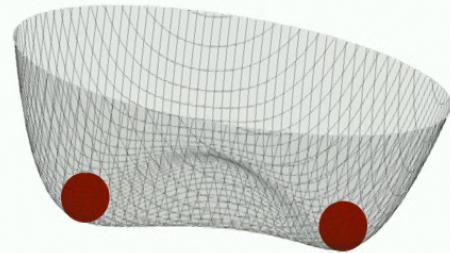
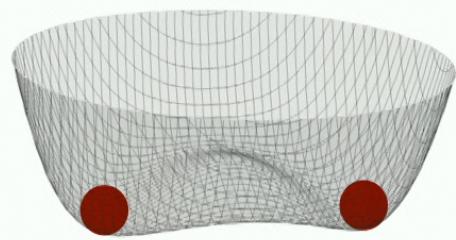


**$N_{DW} > 1$**

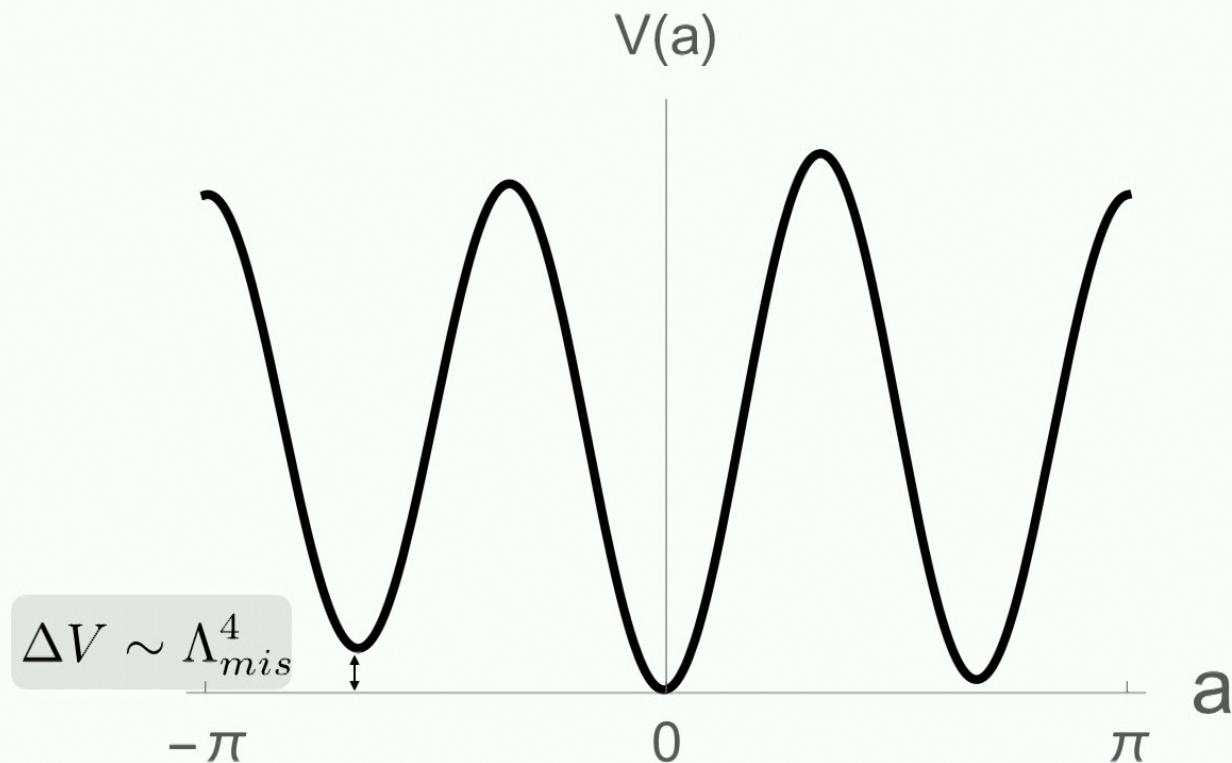


Network is stable  
=> DW problem!

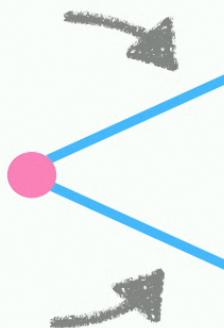
**the misaligned contributions  
(which motivate heavy axions)  
come to rescue the  $N_{DW} > 1$  case**



$$V(a) = \Lambda^4 \left( 1 - \cos(N_{DW} a) \right) + \Lambda_{mis}^4 \left( 1 - \cos(N'_{DW} a + \delta) \right)$$



**$N_{DW} > 1$**



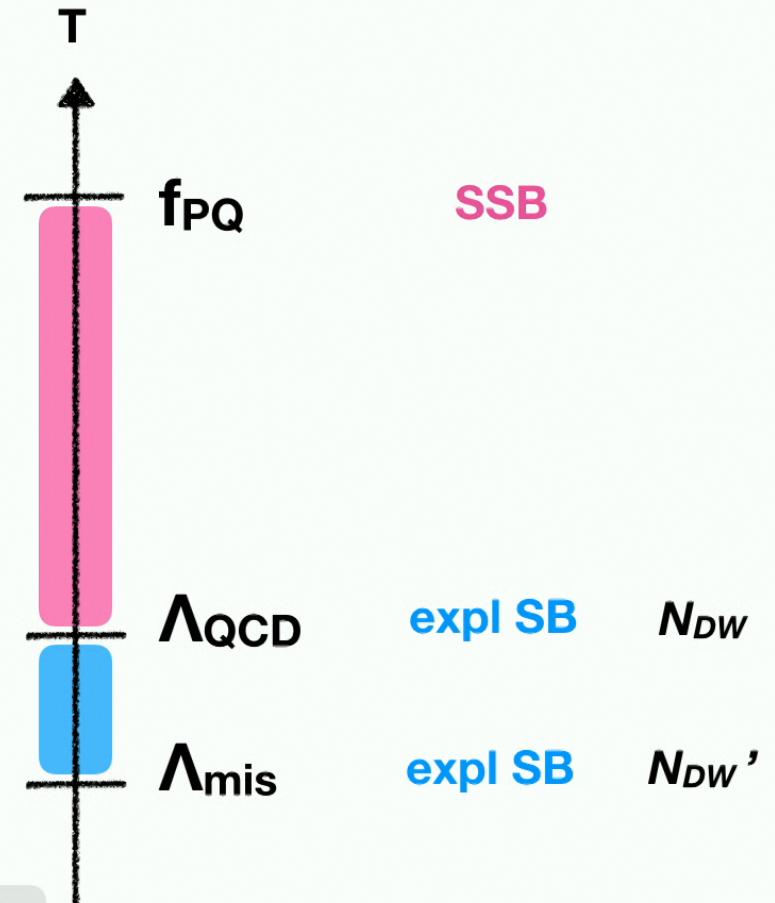
Delayed  
network  
annihilation

long DW  
epoch

Strings

Strings & DWs

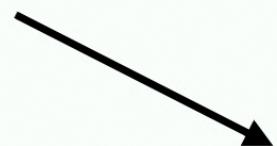
Strings & DWs &  
pressure difference on the DWs



$$N_{DW} > 1$$

DWs form when

$$3H(T_1) = m_a(T_1)$$



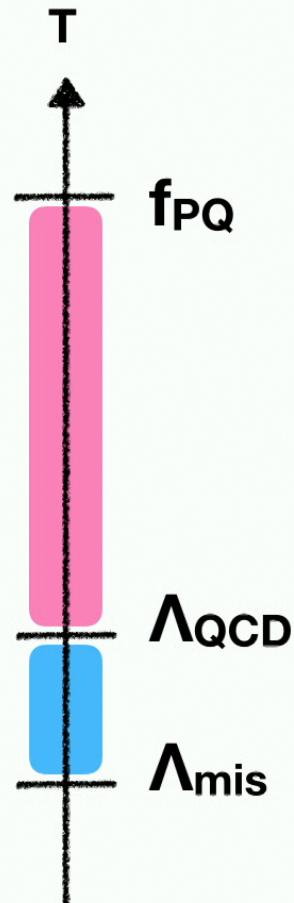
$$T_1$$

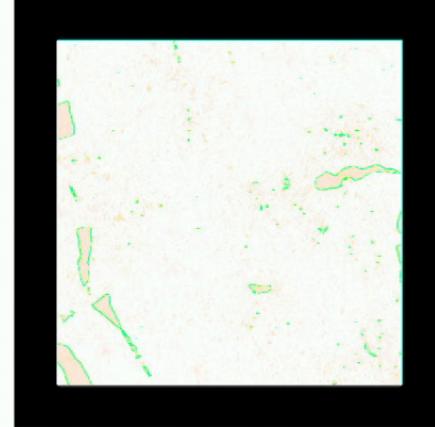
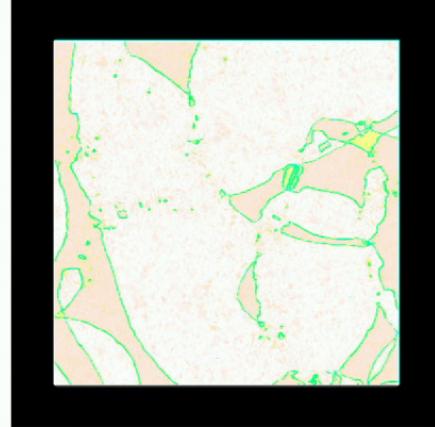
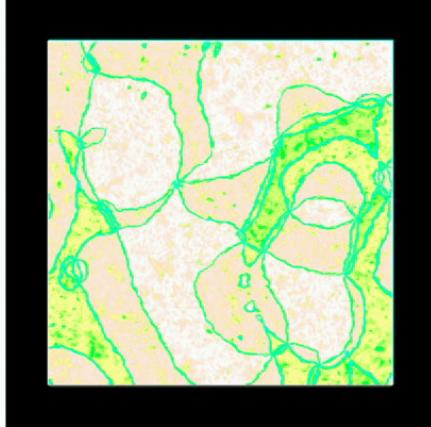
DW+string network ends when

$$a_{DW} = \frac{\Delta V}{\sigma} \sim H(T_2)$$



$$T_2$$





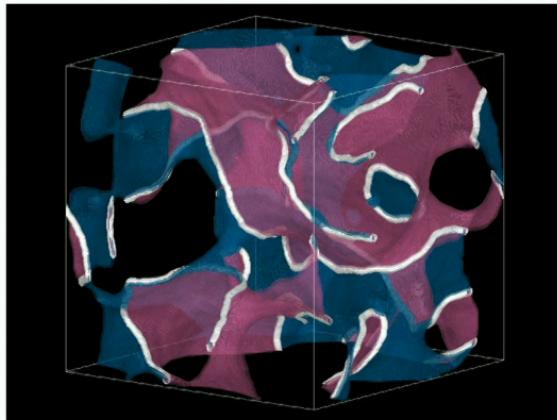
$(N_{DW} > 1)$

**without  $\Lambda_{mis}$  :  
the network  
persists**

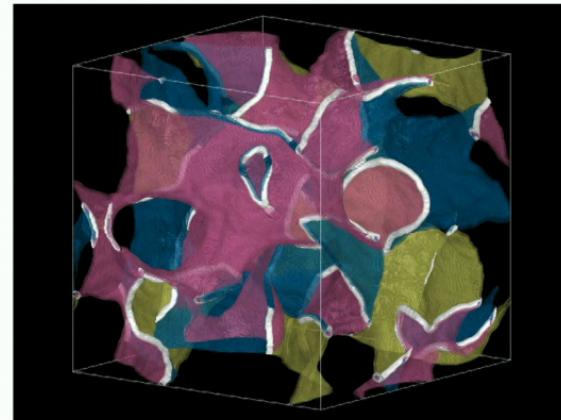
**with  $\Lambda_{mis}$   
the network  
annihilates**

from [Kawasaki et al. '14]

$$\Delta V \approx 10^{-3} V_{QCD}$$



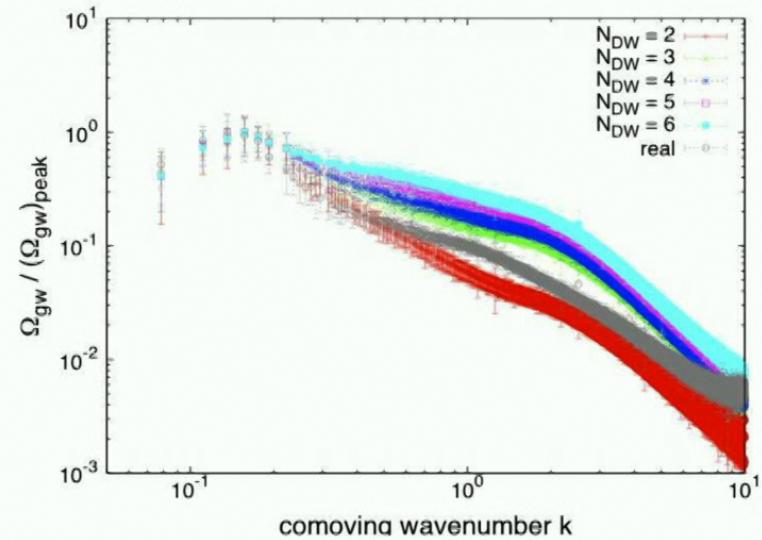
(a)  $N_{\text{DW}} = 2$



(b)  $N_{\text{DW}} = 3$

**Hiramatsu et al arXiv:**  
**1207.3166**

$$\Omega_{\text{gw}}(\omega) = \Omega_{\text{gw}}(\omega_{\text{peak}}) \frac{4}{\left(\frac{\omega}{\omega_{\text{peak}}}\right)^{-3} + 3 \left(\frac{\omega}{\omega_{\text{peak}}}\right)}$$



**The peak in the GW spectrum ~ from network annihilation time, i.e.,**

$$T_2 \simeq \frac{10^7 \text{GeV}}{\sqrt{\kappa_H}} \sqrt{\frac{10^{12} \text{GeV}}{f}} \left( \frac{\Lambda_H}{10^{10} \text{GeV}} \right) \left( \frac{r}{0.005} \right)^2$$

**Signal:**

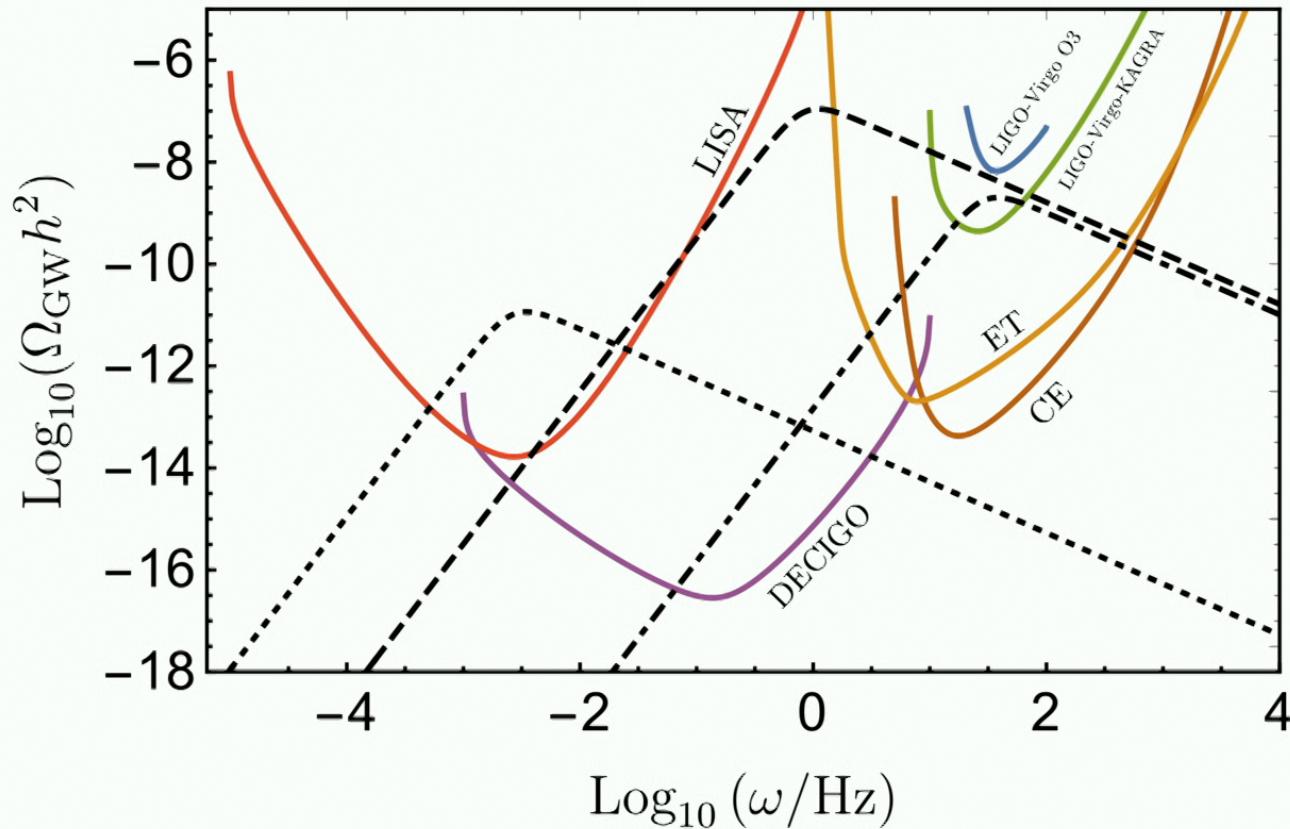
$$\omega_{\text{peak}} \simeq \frac{5 \text{ Hz}}{\sqrt{\kappa_H}} \left( \frac{r}{0.005} \right)^2 \left( \frac{\Lambda_H}{10^{10} \text{GeV}} \right) \sqrt{\frac{10^{11} \text{GeV}}{f}}.$$

$$\Omega_{GW} \sim 10^{-7} \left( \frac{\rho_{DW}}{\rho_{rad}} \right)_{T=T_2}^2$$

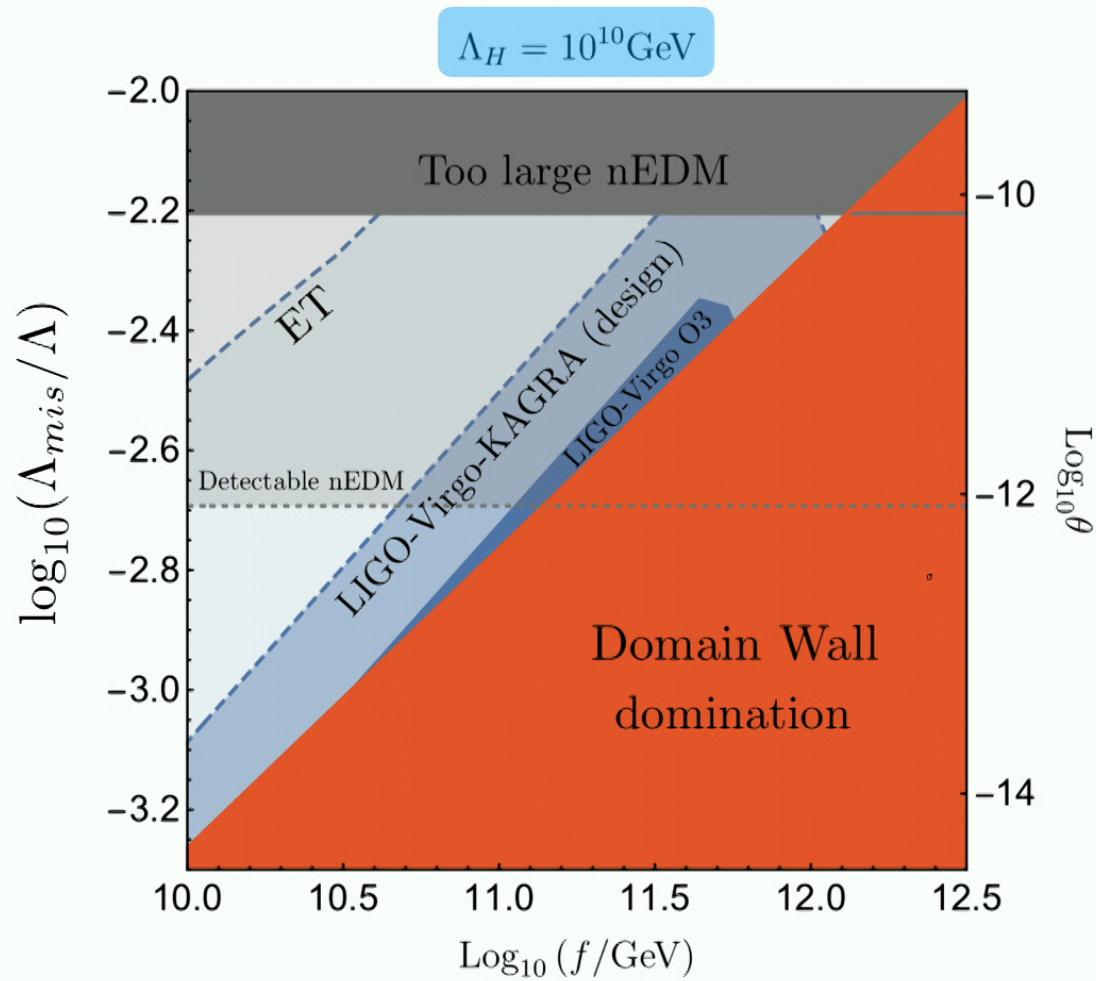
$$r = \Lambda_{mis}/\Lambda_H$$

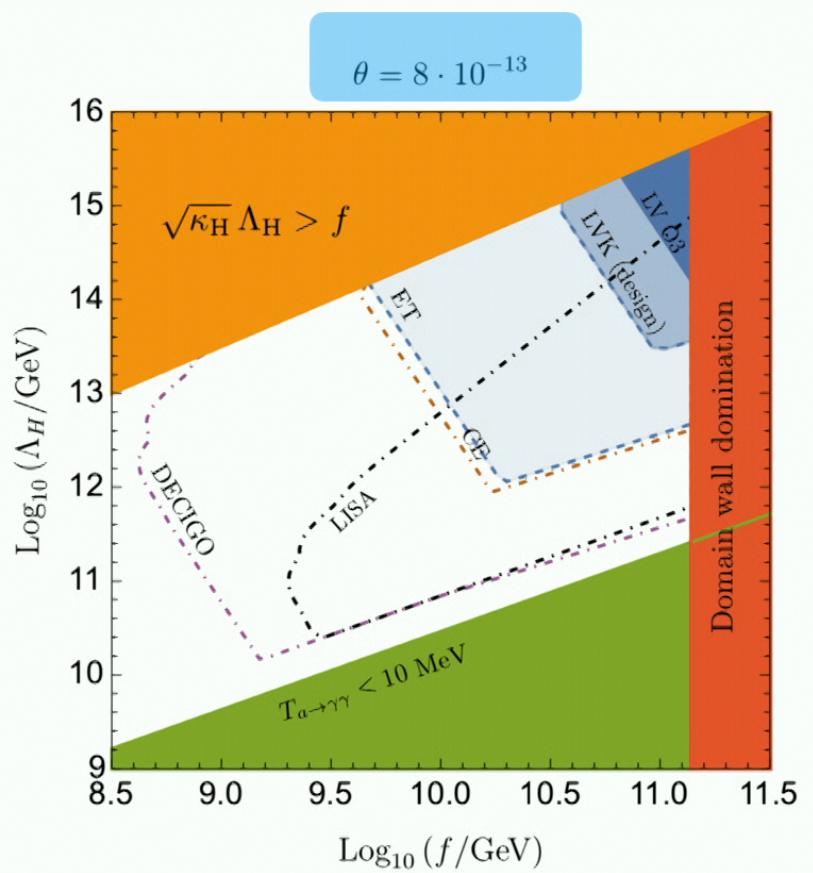
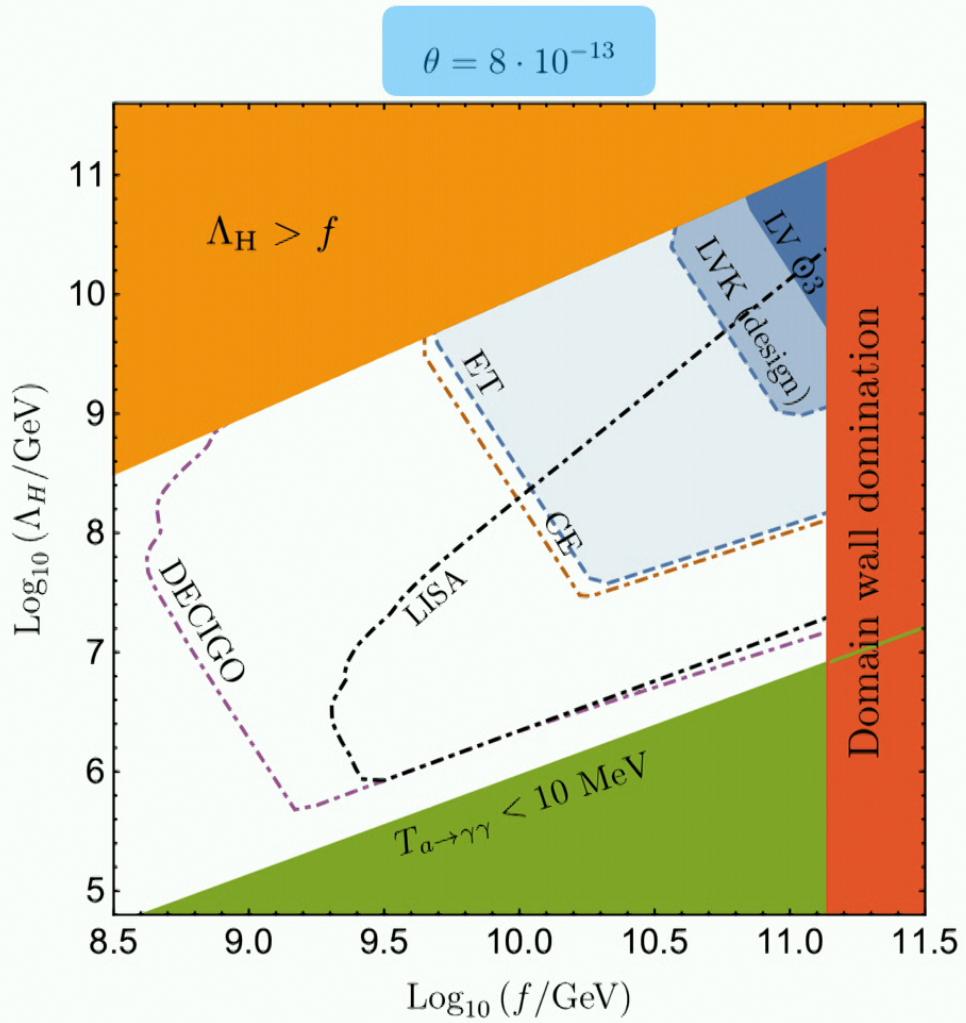
$$\sim \theta^{1/4}$$

$$(\Lambda^4 \equiv \kappa_H^2 \Lambda_H^4)$$



$\Lambda_H =$	$10^7 \text{ GeV}$	$10^{10} \text{ GeV}$	$10^{11} \text{ GeV}$
$f =$	$10^{10} \text{ GeV}$	$3 \cdot 10^{11} \text{ GeV}$	$1.6 \cdot 10^{11} \text{ GeV}$
$\theta =$	$2 \cdot 10^{-12}$	$9 \cdot 10^{-11}$	$1.2 \cdot 10^{-11}$





with  $\kappa_H = 10^{-9}$ .

$$\Lambda^4 \equiv \kappa_H^2 \Lambda_H^4$$

Broken power law model			
	$f_* = 1 \text{ Hz}$	$f_* = 25 \text{ Hz}$	$f_* = 200 \text{ Hz}$
$n_2 = -1$	$3.3 \times 10^{-7}$	$3.5 \times 10^{-8}$	$2.8 \times 10^{-7}$
$n_2 = -2$	$8.2 \times 10^{-6}$	$6.0 \times 10^{-8}$	$3.7 \times 10^{-7}$
$n_2 = -4$	$5.2 \times 10^{-5}$	$1.8 \times 10^{-7}$	$3.7 \times 10^{-7}$

TABLE II: Upper limits for the energy density amplitude,  $\Omega_*^{95\%}$ , in the broken power law model for fixed values of the peak frequency,  $f_*$ , and negative power law index,  $n_2$ .

$$\Omega_{\text{bpl}}(f) = \Omega_* \left( \frac{f}{f_*} \right)^{n_1} \left[ 1 + \left( \frac{f}{f_*} \right)^\Delta \right]^{(n_2 - n_1)/\Delta}$$

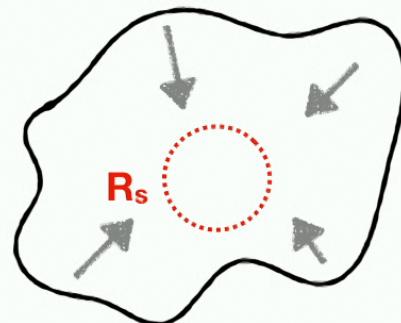
=> some models are already constrained...

$$n_1 = 3 \quad n_2 = -1$$

# Primordial Black Holes

The same network collapse can lead to PBHs

Ferrer Masso Panico OP Rompineve  
Phys.Rev.Lett. 122 (2019) 10, 101301  
1807.01707



Tension & pressure helps collapse

Collapse condition

$$R_S = \frac{\sigma}{H^2 M_P^2} \gtrsim \frac{1}{H}$$

coincides with DW domination

near DW domination region, PBHs are expected

# Conclusions

**Heavy axion models naturally contain long DW epoch — very different from bubbles**

**DW network collapse generates strong GW signal (and PBHs)**

**Combined signature both in GWs and in nEDM**

**LIGO/Virgo/KAGRA are already testing interesting axion models!**

**LVK = extremely high-energy machines**

**Better simulations of bubble collisions and string/wall networks are needed to chart the excluded parameter space**