

Title: Higher-order Correlation Function of Large-Scale Structures and Parity-Violation Search

Speakers: Jiamin Hou

Series: Cosmology & Gravitation

Date: July 18, 2022 - 12:00 PM

URL: <https://pirsa.org/22070026>

Abstract: In the standard cosmological paradigm, the initial condition follows Gaussian statistics. At later times, gravitational evolution induces nonlinearities in the large-scale structure, information that was fully captured by the two-point statistics at the early times gets spread into higher-order statistics. Whilst current standard cosmological analyses have focused on two-point statistics, higher-order statistics help further to tighten constraints by breaking parameter degeneracies as well as to probe the primordial Universe. In this talk, I will present our recent progress on the N-point Correlation Function (NPCF), including an analytical Gaussian covariance formalism, a first detection of the 4-point correlation function from nonlinear structure formation. Finally, I will focus on our recent analysis of parity-odd mode using the data from Baryon Oscillation Spectroscopic Survey (BOSS) and discuss the implication of parity-search at cosmological scales with large scale structure.

Zoom Link: <https://pitp.zoom.us/j/92321535422?pwd=VlF4cHpvUit4bmR0eXYyczI5Qmw4dz09>



Max-Planck-Institut für
extraterrestrische Physik



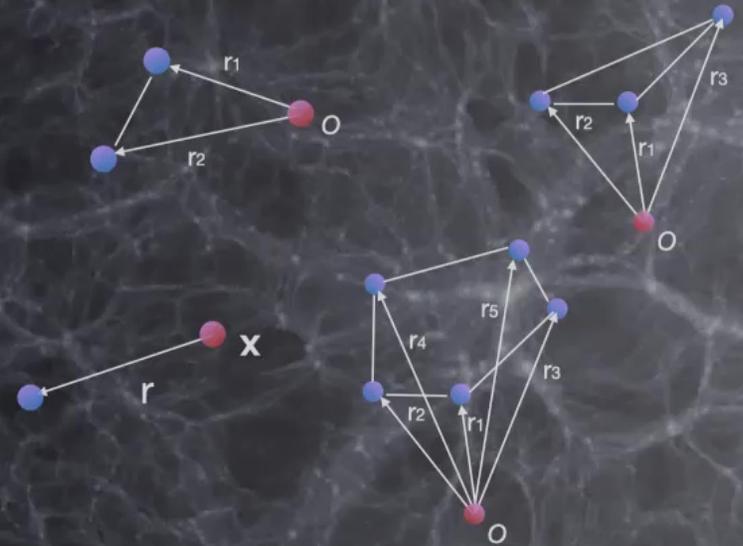
N-Point Statistics of Large-Scale Structure and Parity-Violation Search

Perimeter Institute

July 18 2022

Jiamin Hou

Marie Curie Fellow @UF (with MPE support)



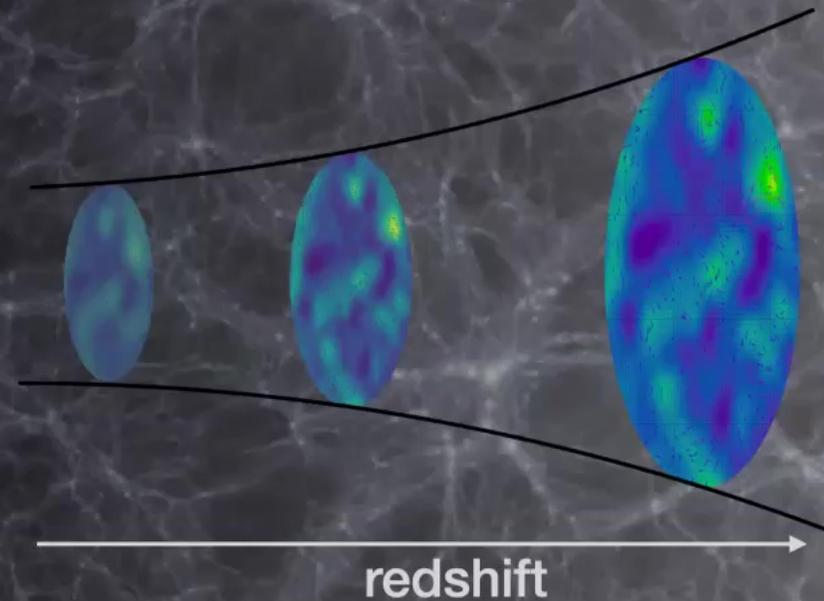
Background Image credit: O.Hahn

Information in Galaxies' 3D distribution

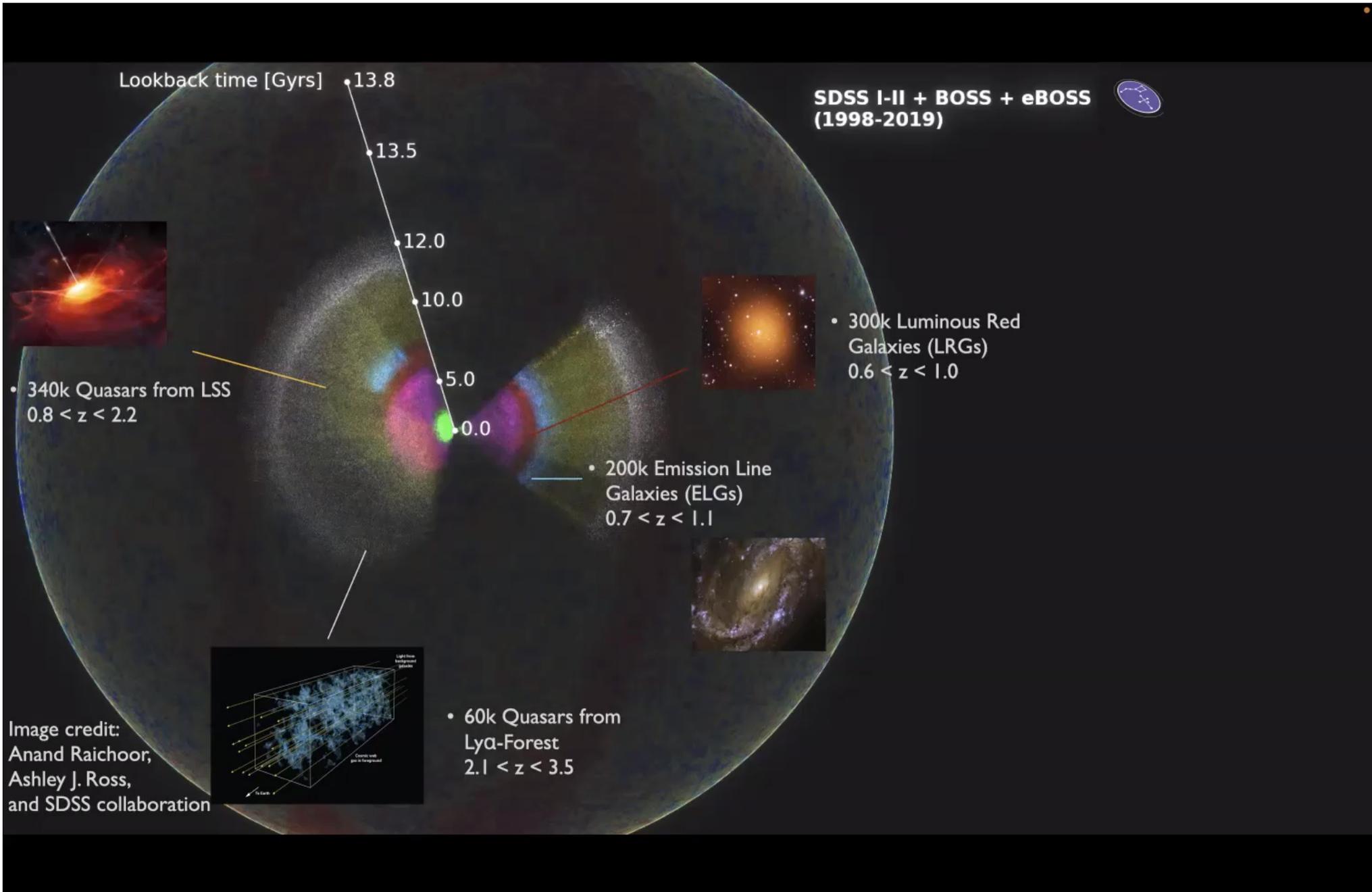
- Map the expansion history
- Probe growth of cosmic structure
- Origin of the Universe

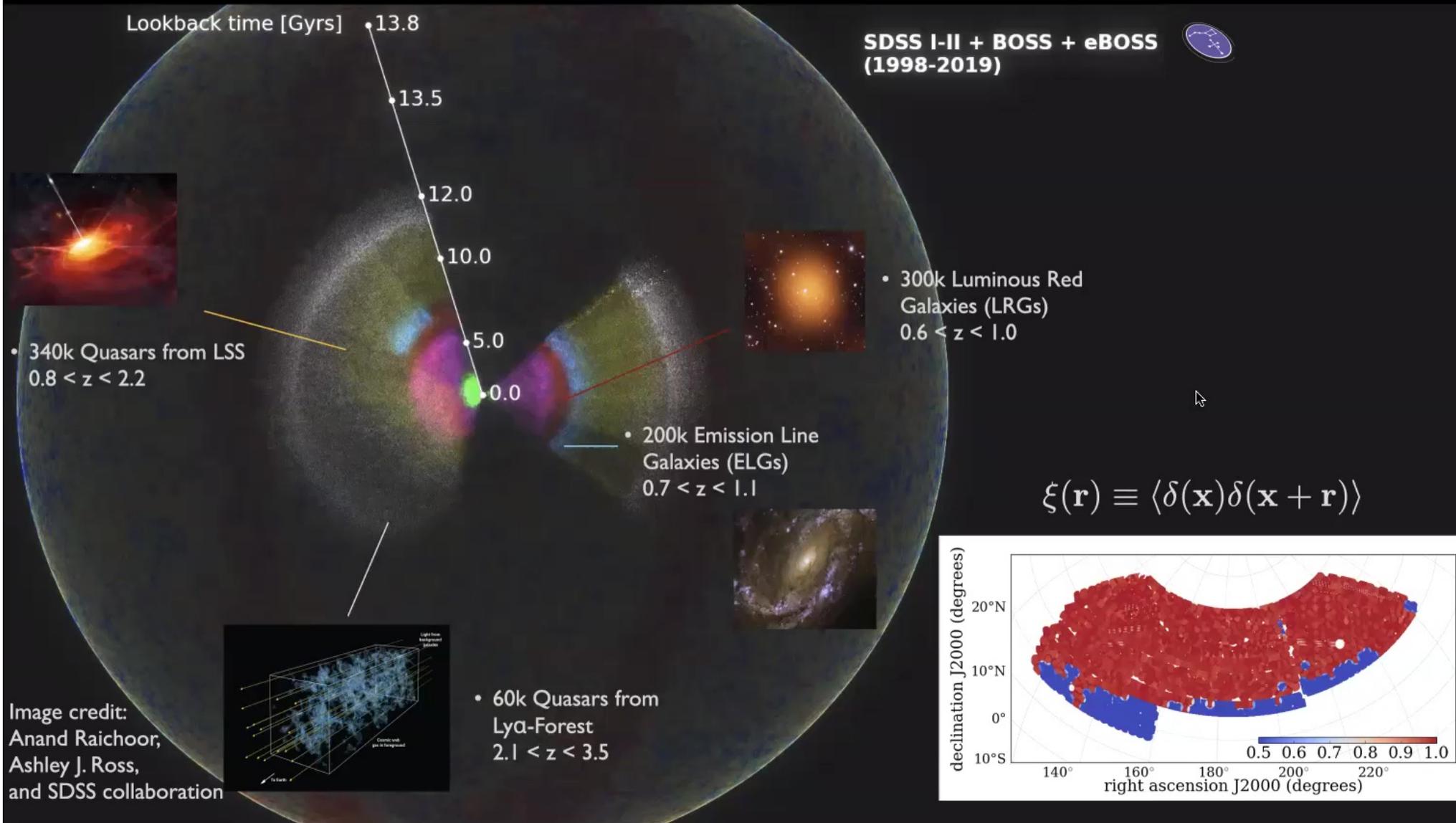
→ Standard cosmological paradigm

- Cosmic inflation
- $w = -1$
- CDM



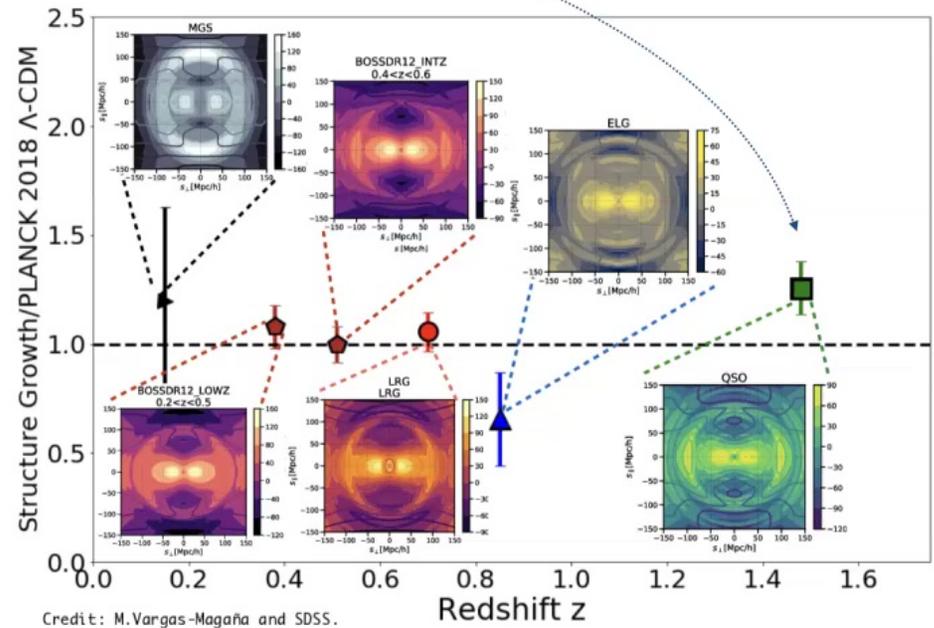
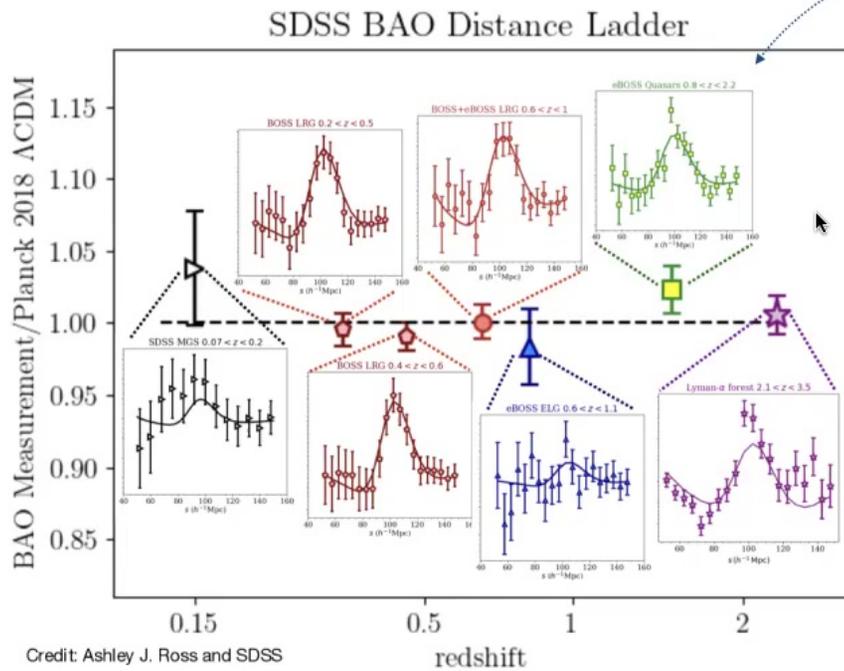
Background Image credit: O.Hahn



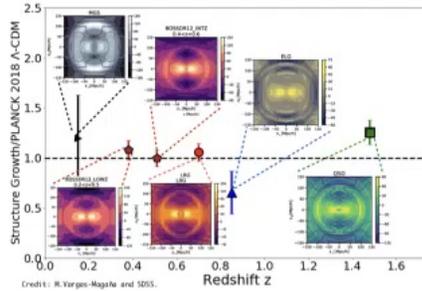
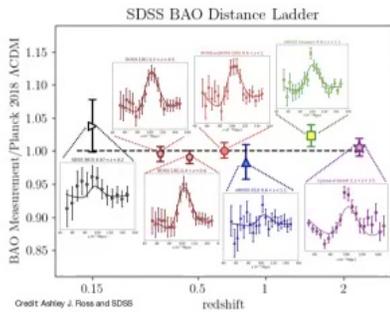


2-point statistics and Developments in the Last Decade

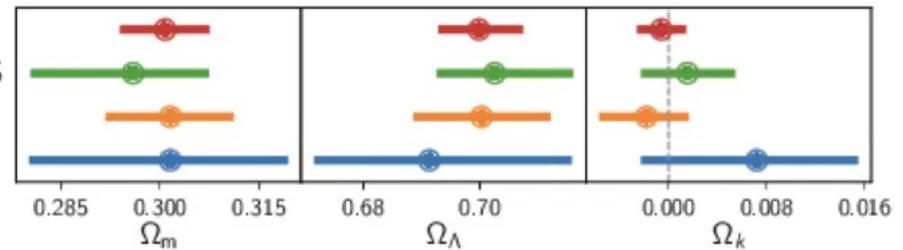
JH ++ 2020,
Neveux ++ 2020



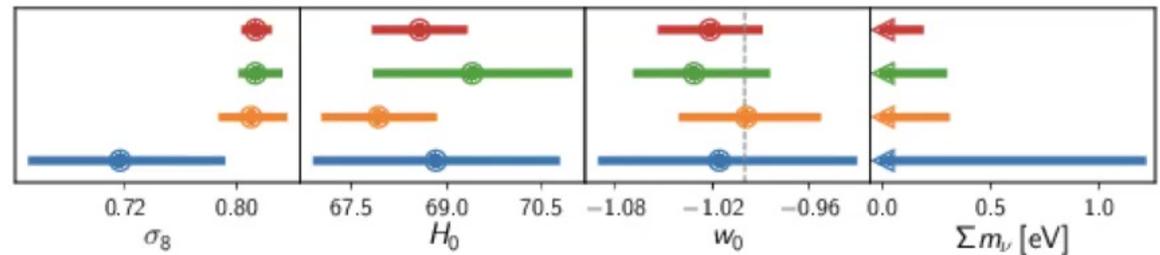
2-point statistics and Developments in the Last Decade



- Stage III
- Stage III w/o SDSS
- Stage II + SDSS
- Stage II

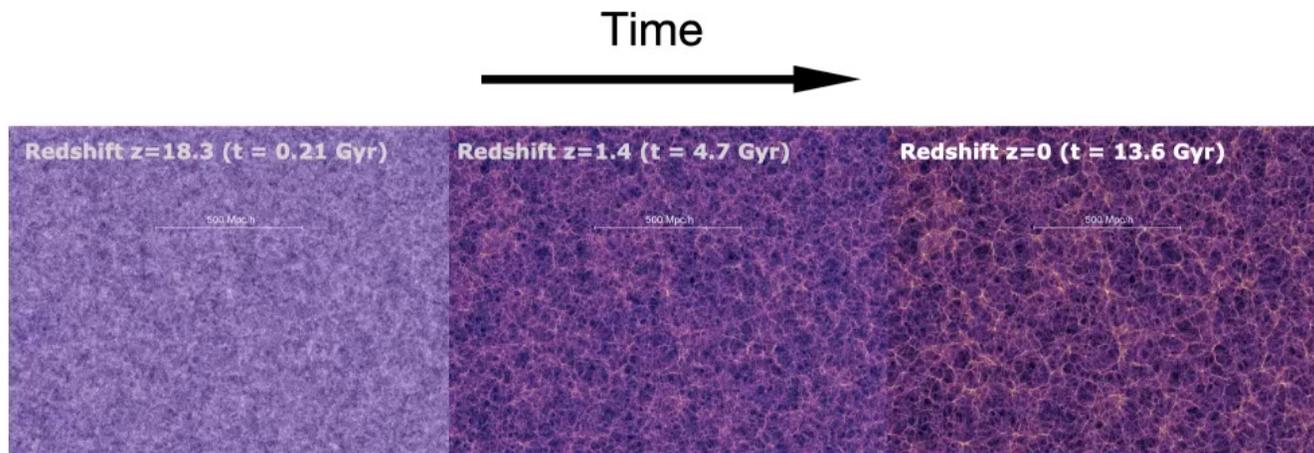


Stage II: WMAP, JLA SN, SDSS DR7 (2010)
 Stage III: Planck, Pantheon SNe Ia, DES (2020)



Credit: eBOSS collaboration (2020)

Information in higher-order statistics?



Credit: Millenium Simulation Project

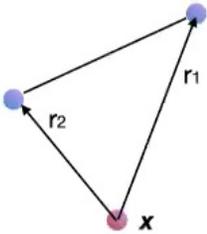
- Gaussian initial conditions
- Nonlinearities are not fully captured by 2-point statistics
- Unique window to different inflationary models
- Break parameter degeneracies

Go beyond 2-point statistics?

N = 2

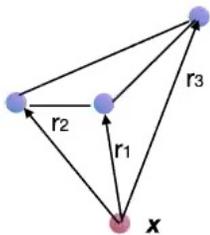


N = 3

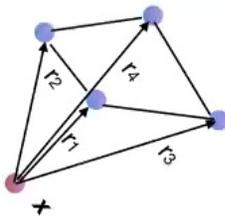


- Tighten constraints on Λ CDM
- Break parameter degeneracies
- Constrain primordial non-Gaussianity

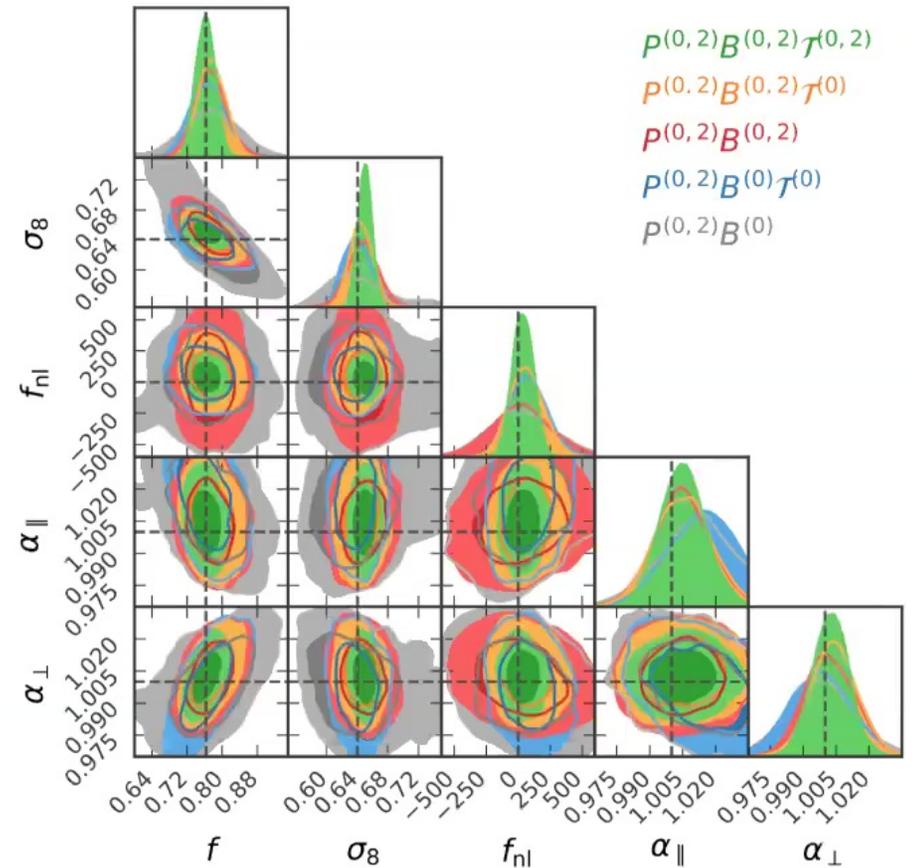
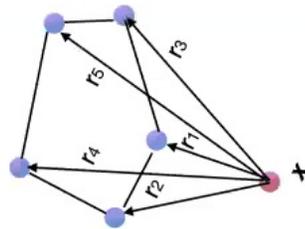
N = 4



N = 5



N = 6



Gualdi++ 2021

NPCFs in the Isotropic Basis

$$\left\langle \prod_i \delta(\mathbf{r}_i) \right\rangle = \sum_{\Lambda} Z_{\Lambda}(R) \mathcal{P}_{\Lambda}(\hat{R})$$

$$\bullet \mathcal{P}_{\Lambda}(\hat{R}) = \sum_M C_M^{\Lambda} \prod_i Y_{\ell_i m_i}$$

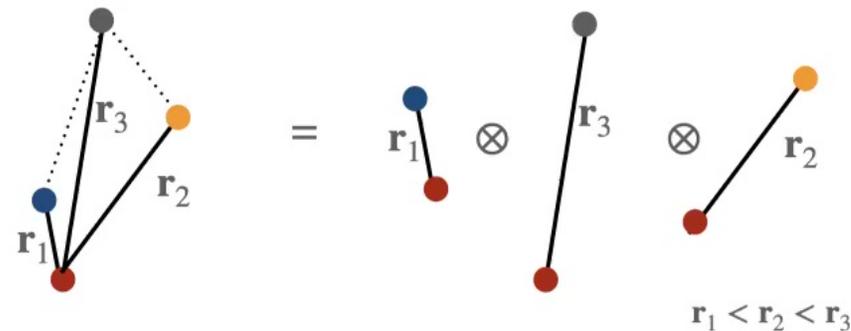
$$\bullet C_M^{\Lambda} = \mathcal{E}(\Lambda) \sqrt{2\ell_{12} + 1} \times \cdots \times \sqrt{2\ell_{12} \dots N - 3 + 1} \\ \times \sum_{m_{12} \dots} (-1)^{\kappa} \begin{pmatrix} \ell_1 & \ell_2 & \ell_{12} \\ m_1 & m_2 & -m_{12} \end{pmatrix} \cdots \begin{pmatrix} \ell_{12 \dots N-3} & \ell_{N-2} & \ell_{N-1} \\ m_{12 \dots N-3} & m_{N-2} & m_{N-1} \end{pmatrix}$$

- Complete orthonormal basis
- Given isotropy:
 - An efficient approach to sort information
- Separable angular basis:
 - offers a speed boost to measure it

Cahn and Slepian, arXiv: 2010.14418

Efficient N-point Correlator Estimation (ENCORE)

<https://github.com/oliverphilcox/encore>

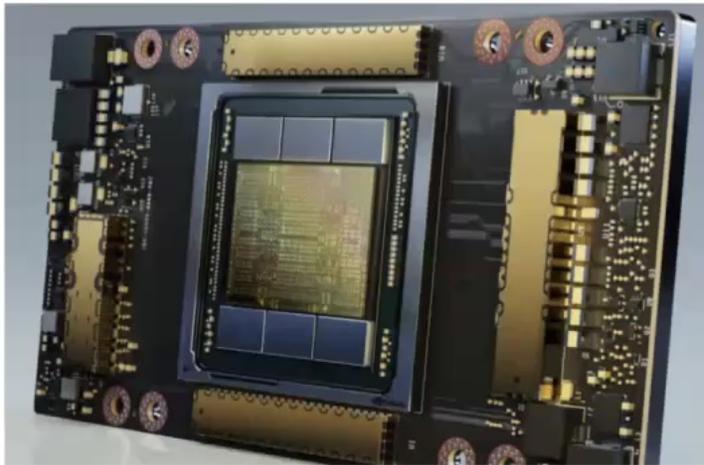


- Algorithm based on Slepian & Eisenstein 2015
- Survey geometry induces angular momentum coupling
 - Edge correction is included
- “Connected-only” estimator

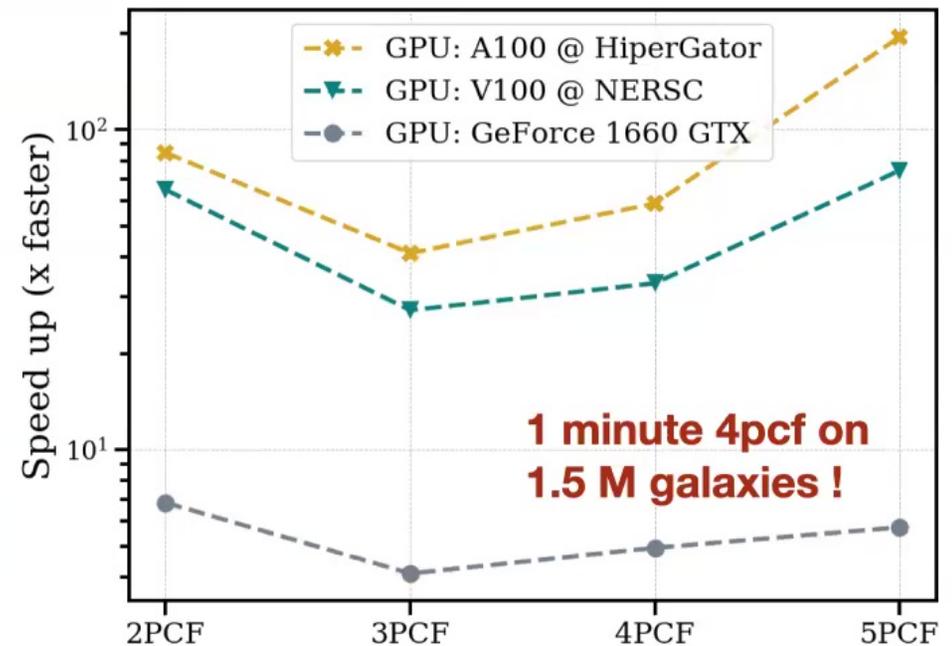
$$\zeta(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3) = \xi(\mathbf{r}_1) \xi(\mathbf{r}_2 - \mathbf{r}_3) + \text{cyc.} + \zeta^{(c)}(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3)$$

Philcox, Slepian, JH, Cahn, Warner, Eisenstein arXiv: 2105.08722

GPU for N-point Correlator Estimation (Cadenza)



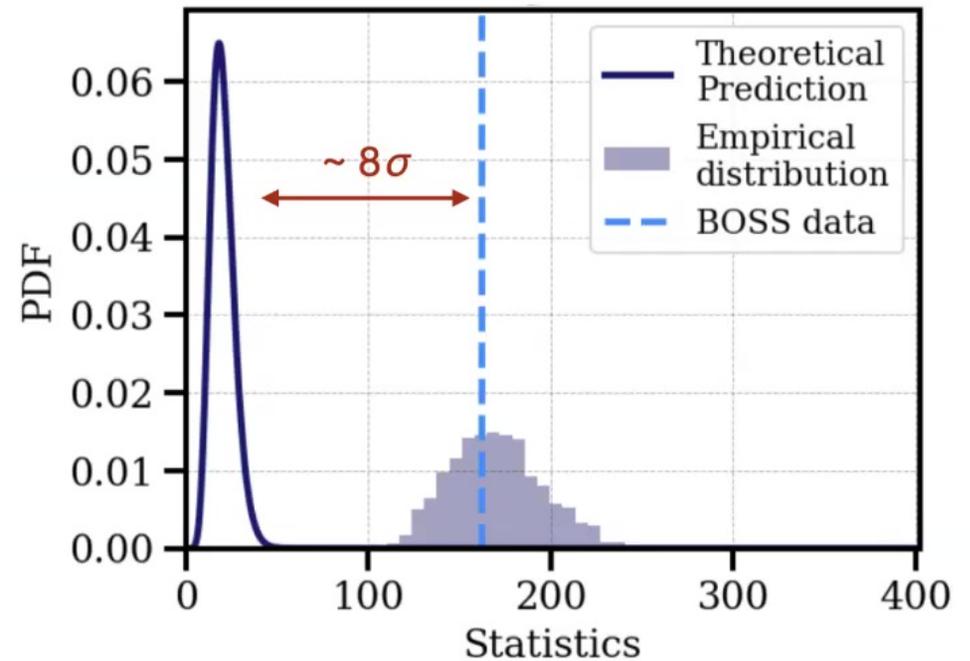
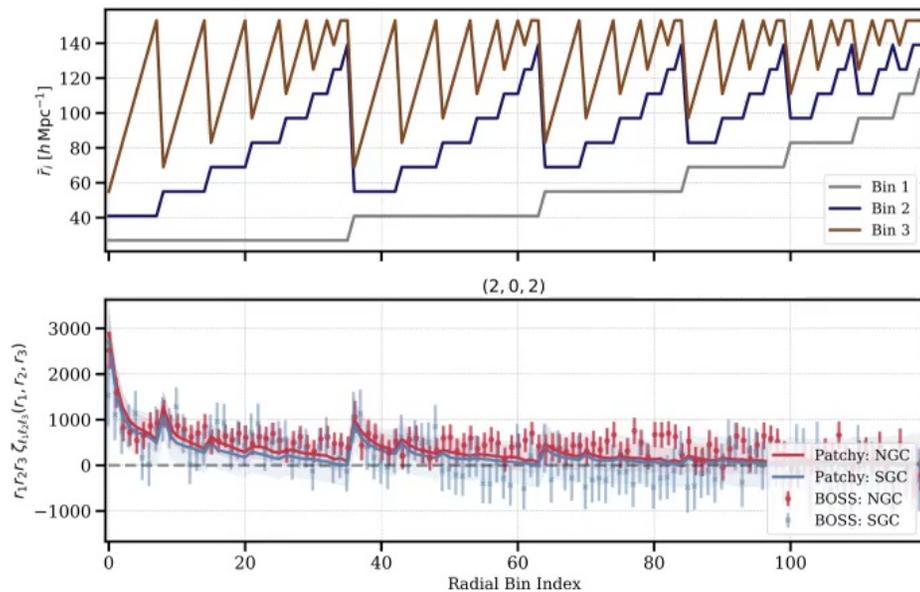
GPU vs single thread CPU



CADENZA: Slepian, Warner, Hou, Cahn in prep.

First Detection of Gravitationally-induced non-Gaussianity with BOSS CMASS

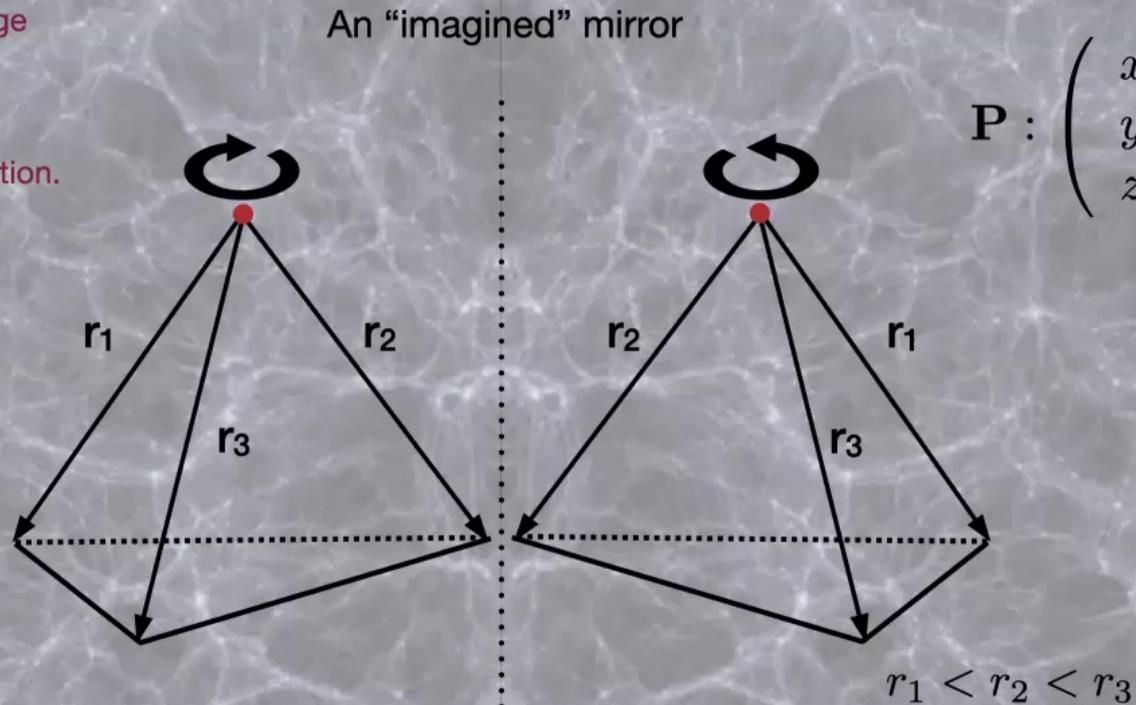
4PCF from BOSS CMASS



O. Philcox, JH, Z. Slepian, arXiv: 2108.01670

Parity Violation with the 4PCF of LSS

- A tetrahedron and its mirror image cannot be superimposed in 3D.
- The 4PCF is the lowest order statistics sensitive to parity violation.



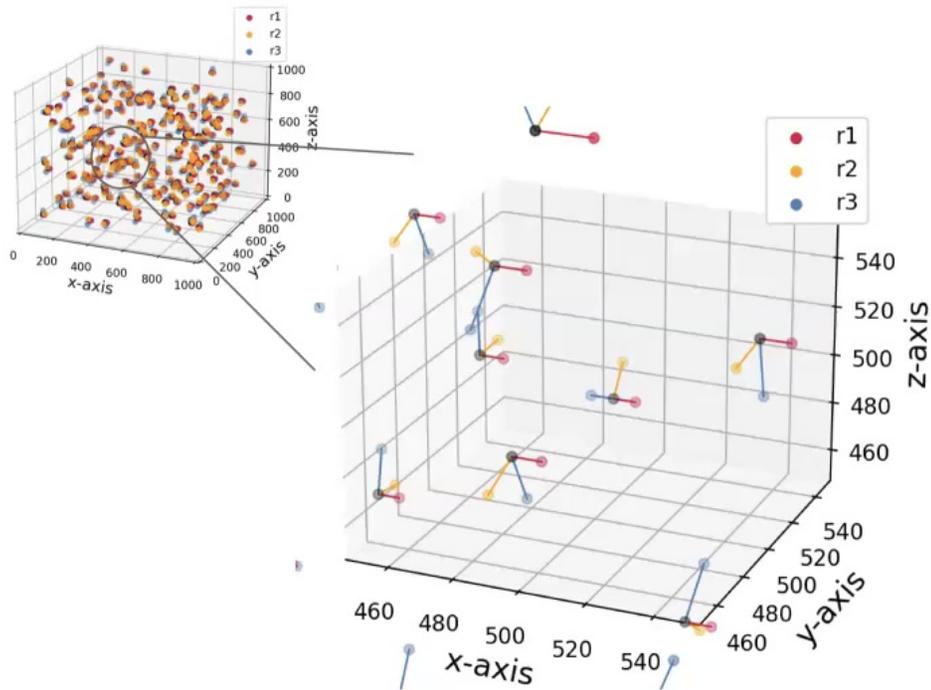
$$P : \begin{pmatrix} x \\ y \\ z \end{pmatrix} \mapsto \begin{pmatrix} -x \\ -y \\ -z \end{pmatrix}$$

$$\mathcal{P}_{\ell_1 \ell_2 \ell_3}(-\hat{\mathbf{r}}_1, -\hat{\mathbf{r}}_2, -\hat{\mathbf{r}}_3) = (-1)^{\ell_1 + \ell_2 + \ell_3} \mathcal{P}_{\ell_1 \ell_2 \ell_3}(\hat{\mathbf{r}}_1, \hat{\mathbf{r}}_2, \hat{\mathbf{r}}_3)$$

Parity Violation at Cosmological Scale

- Standard single-field inflation preserves parity
- Gravity is parity-conserving
- **Sources for parity violation?**
 - Chern-Simons like interaction
 - e.g. axion coupled to gauge field (Kim+2005, Namba+2015)
 - Primordial vorticity (Vilenkin 1978)
 - Broken symmetry during phase transition (G.'t Hooft 1974, Quashnock+1989; Baym+1996)
 - String-sourced perturbations (Pogosian&Wyman 2008)
 - ...

A Toy Simulation for the Parity-Odd 4PCF

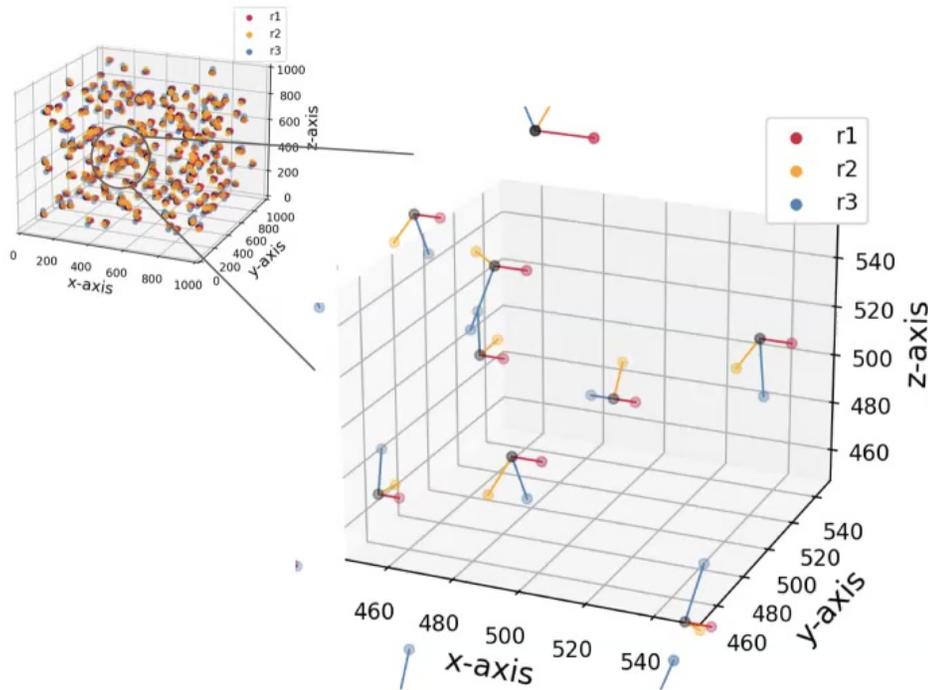


$$\mathcal{P}_{111}(\hat{\mathbf{r}}_1, \hat{\mathbf{r}}_2, \hat{\mathbf{r}}_3) = -i \frac{3}{\sqrt{2}} (4\pi)^{-3/2} \hat{\mathbf{r}}_1 \cdot (\hat{\mathbf{r}}_2 \times \hat{\mathbf{r}}_3),$$

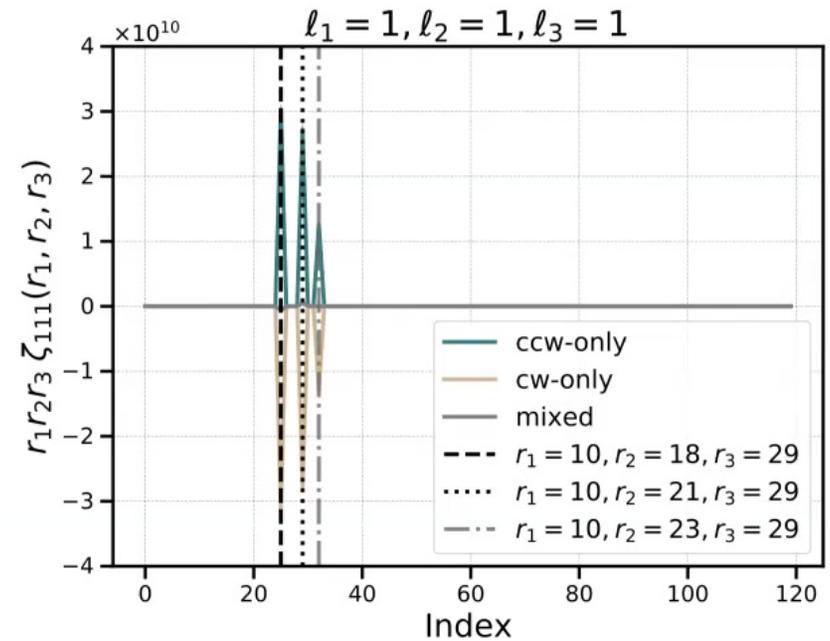
$$\mathcal{P}_{122}(\hat{\mathbf{r}}_1, \hat{\mathbf{r}}_2, \hat{\mathbf{r}}_3) = i \sqrt{\frac{45}{2}} (4\pi)^{-3/2} \hat{\mathbf{r}}_1 \cdot (\hat{\mathbf{r}}_2 \times \hat{\mathbf{r}}_3) (\hat{\mathbf{r}}_2 \cdot \hat{\mathbf{r}}_3),$$

$$\mathcal{P}_{133}(\hat{\mathbf{r}}_1, \hat{\mathbf{r}}_2, \hat{\mathbf{r}}_3) = -i \frac{15}{4} \sqrt{7} (4\pi)^{-3/2} \hat{\mathbf{r}}_1 \cdot (\hat{\mathbf{r}}_2 \times \hat{\mathbf{r}}_3) \left[(\hat{\mathbf{r}}_2 \cdot \hat{\mathbf{r}}_3)^2 - \frac{1}{5} \right]$$

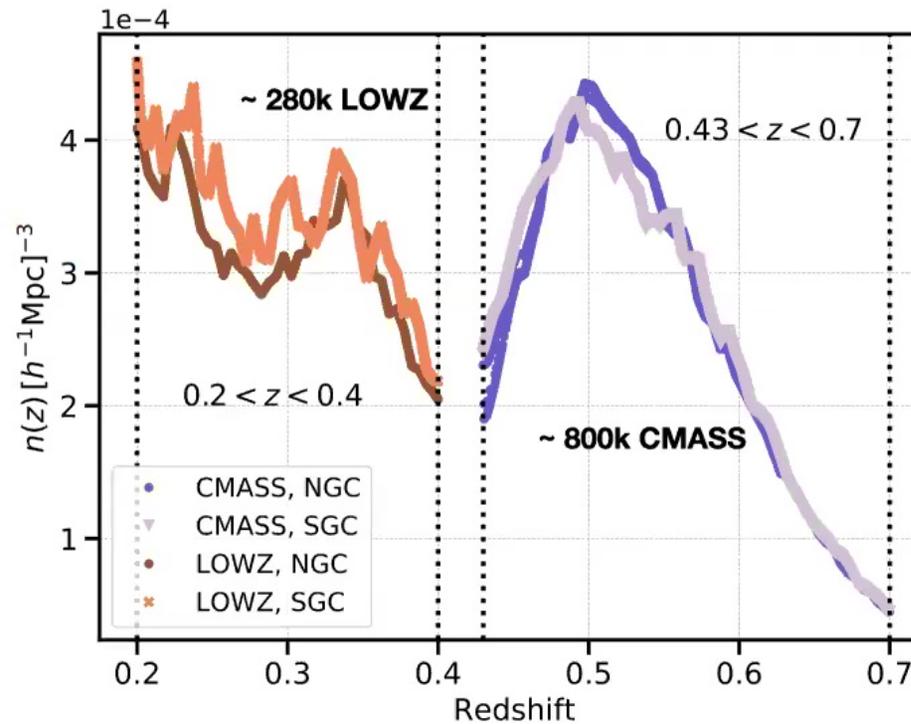
A Toy Simulation for the Parity-Odd 4PCF



$$P_{111}(\hat{r}_1, \hat{r}_2, \hat{r}_3) \propto -i\hat{r}_1 \cdot (\hat{r}_2 \times \hat{r}_3)$$



Measurement of Parity-Odd Modes in the 4PCF of SDSS BOSS DR12 CMASS and LOWZ



JH, Slepian, Cahn (arXiv: 2206.03625)

Statistical Background Estimation

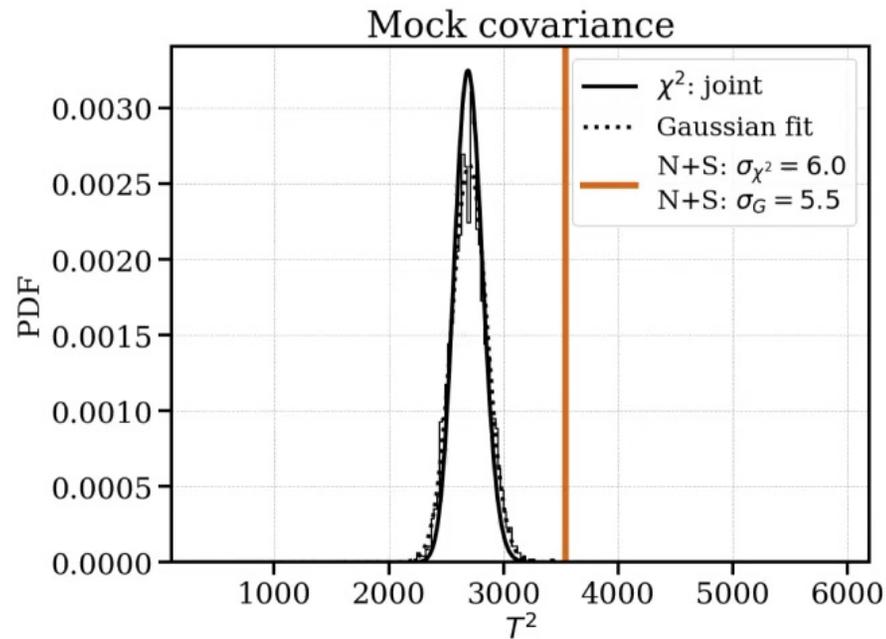
Model-independent search, null hypothesis

- Challenge: high dimensionality for 4PCF
 - NO sampling covariance from mocks
- Gaussian analytic covariance
- Compressed data vector¹
- Direct: restrict angular momentum and/or radial bin to reach reduced d.o.f.

[1] Scoccimarro 1999

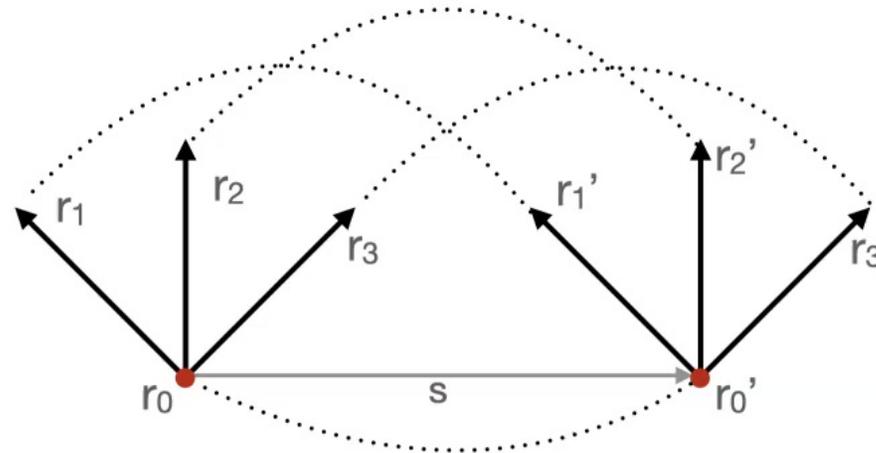
Detection Significance and Statistical Convergence test

Reduced data vector in radial binning



Analytic NPCF covariance in the Gaussian limit

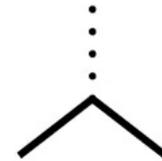
Couple density fields from two tetrahedra, one for each



$$\langle \delta(\mathbf{x} + \mathbf{r}_i) \delta(\mathbf{x} + \mathbf{s} + \mathbf{r}'_j) \rangle \equiv \xi(|\mathbf{r}'_j + \mathbf{s} - \mathbf{r}_i|)$$



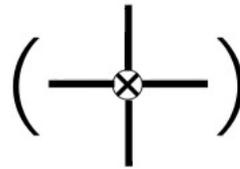
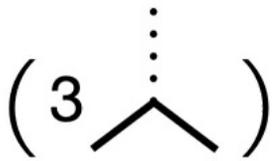
$$(4\pi)^{3/2} \sum_{\ell_i \ell'_j L} i^{\ell_i - \ell'_j - L} f_{\ell_i \ell'_j L}(r, r', s) \mathcal{D}_{\ell_i \ell'_j L}^P \mathcal{C}_{000}^{\ell_i \ell'_j L}$$



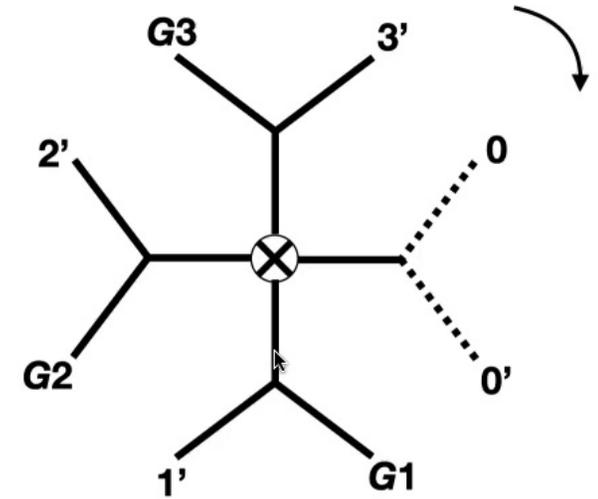
- “Real space” covariance — Ignore higher multipole coupling

Analytic 4PCF covariance in the isotropic basis

Case I

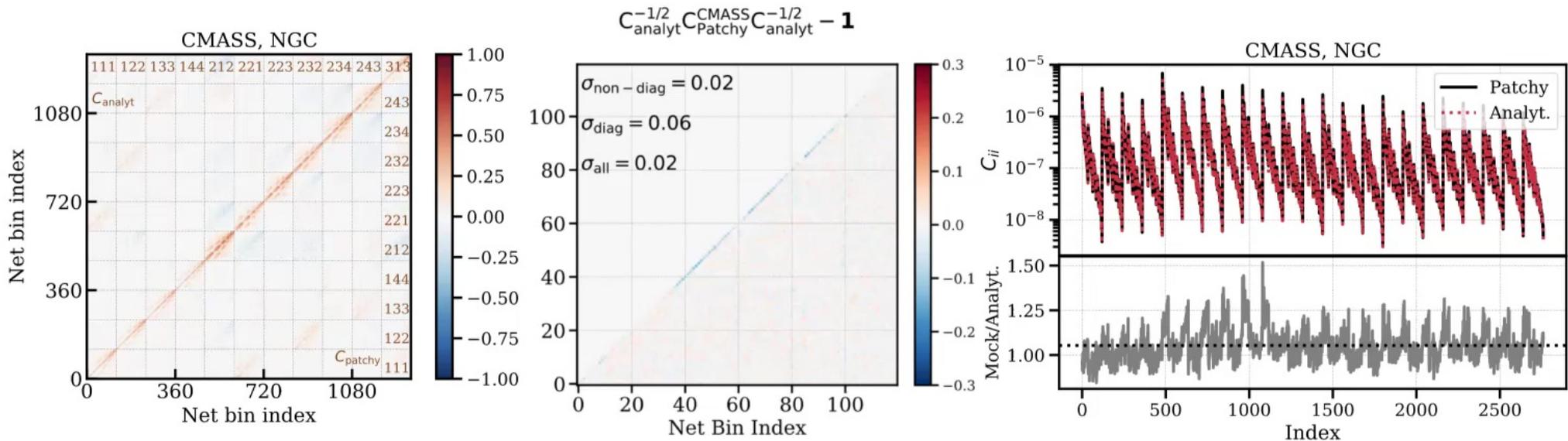


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Comparison to simulations

- Gaussianity
- “Isotropy”
- Uniform window

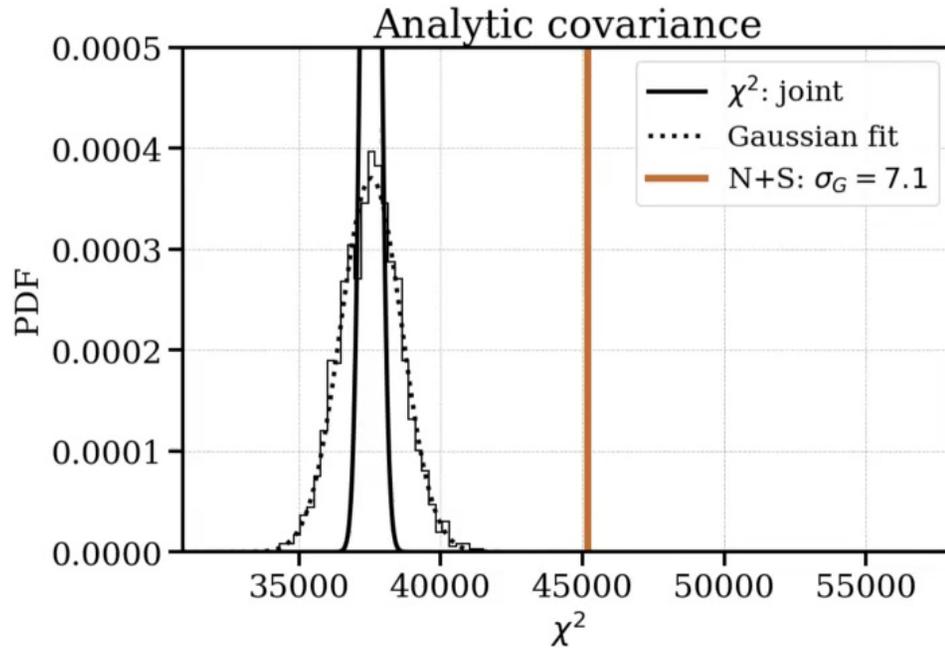


- Include higher order statistics, i.e. $\langle 332 \rangle$, $\langle 44 \rangle$ types;
- Include window function
- “Anisotropy”
- Extended formalism for $N > 4$

JH, R.Cahn, O. Philcox, Z.Slepian 2022 PRD

Detection Significance and Statistical Convergence test

Full data vector



- Vary radial bin interval:
 - $dr = \{8, 14, 24\}$ [Mpc/h]
 - Detection significance drops as interval increases
 - Conjecture:
 - internal cancellation

Impact of Systematics on Parity-odd Modes

- Survey-related effects
- Observer-induced effects
- Algorithm-related effects

Impact of Systematics on Parity-odd Modes

- Survey-related effects
 - redshift failure ...

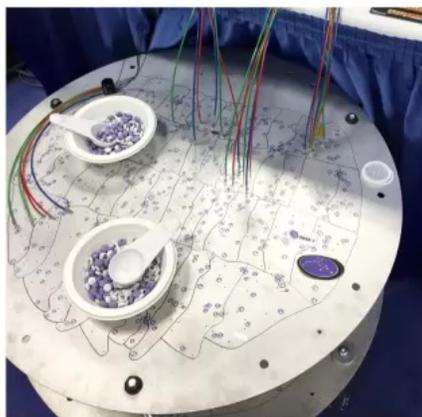


Photo taken at AAS 2020, Honolulu

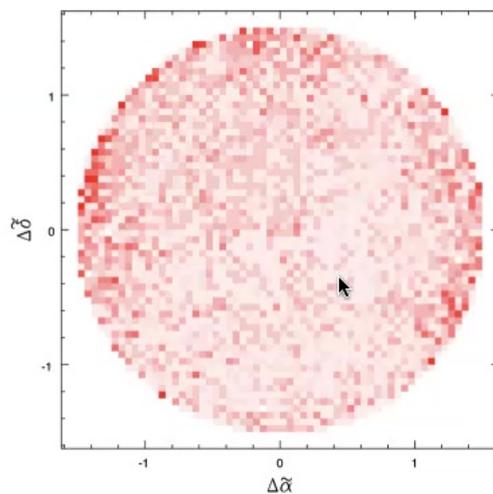
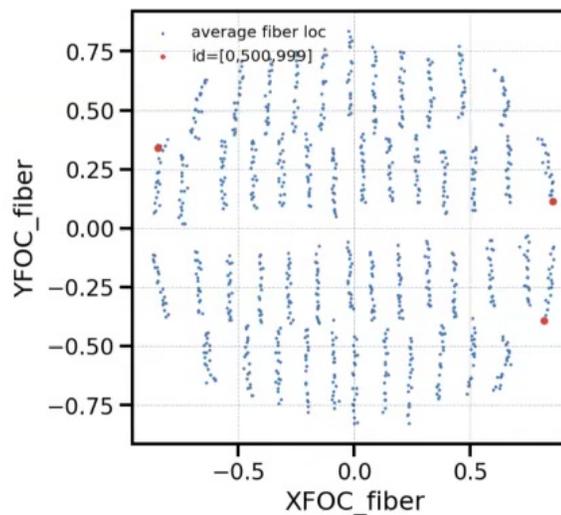


Image credit: Ross+ 2012



Impact of Systematics on Parity-odd Modes

- Observer-induced effects
 - Tidal alignment

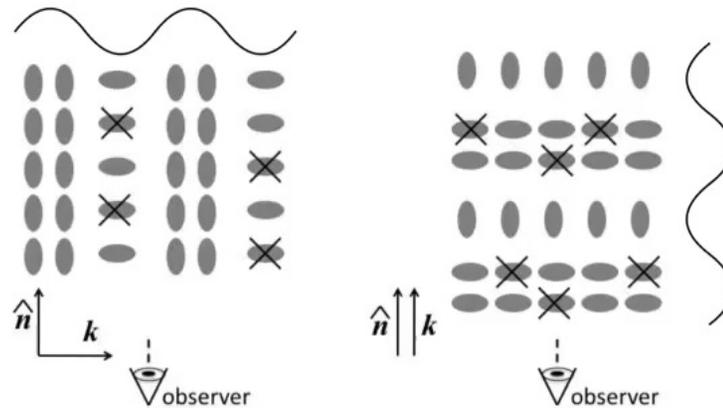


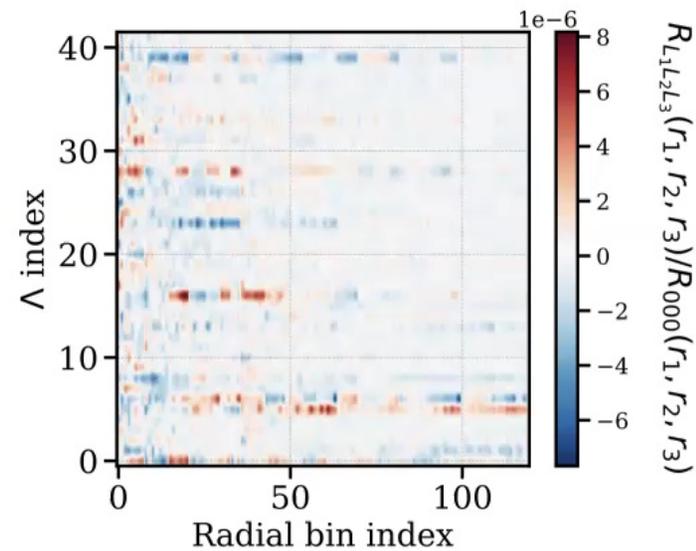
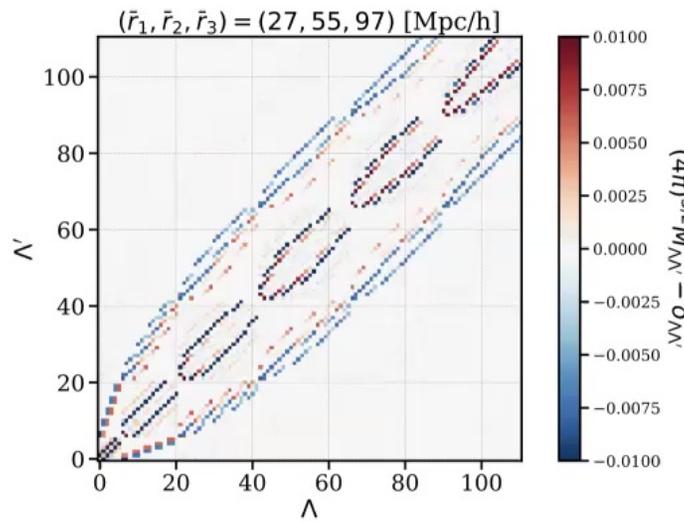
Image credit: Hirata 2009

$$\delta_g^{\text{obs}} + 1 = (\delta_g^{\text{true}} + 1) (1 + \epsilon(\hat{\mathbf{n}} | \mathbf{x}))$$

$$\epsilon(\hat{\mathbf{n}} | \mathbf{k}) = A \left[(\hat{\mathbf{n}} \cdot \hat{\mathbf{k}})^2 - \frac{1}{3} \right] \delta_m(\mathbf{k}) \quad \text{Parity-even}$$

Impact of Systematics on Parity-odd Modes

- Algorithm-related effects
 - edge-correction

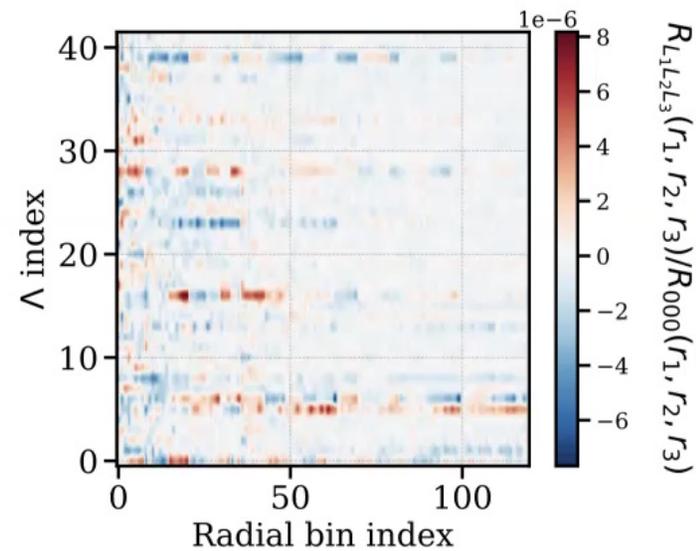
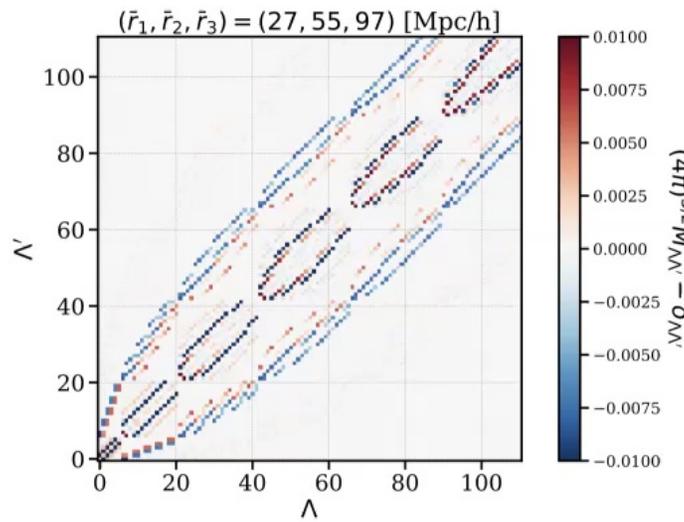


$$\hat{\zeta}_\Lambda \sim \sum_{\Lambda'} \mathbf{M}_{\Lambda\Lambda'}^{-1} (D - R)_{\Lambda'}^4.$$

$$\mathbf{M}_{\Lambda\Lambda'} \sim (-1)^{\ell'_1 + \ell'_2 + \ell'_3} \sum_{L_1 L_2 L_3} \frac{\mathcal{R}_{L_1 L_2 L_3}}{\mathcal{R}_{000}} \prod_{i=1}^3 D_{\ell_i L_i \ell'_i}^P C_{000}^{\ell_i L_i \ell'_i} \left\{ \begin{matrix} \ell_1 & L_1 & \ell'_1 \\ \ell_2 & L_2 & \ell'_2 \\ \ell_3 & L_3 & \ell'_3 \end{matrix} \right\}$$

Impact of Systematics on Parity-odd Modes

- Algorithm-related effects
 - edge-correction

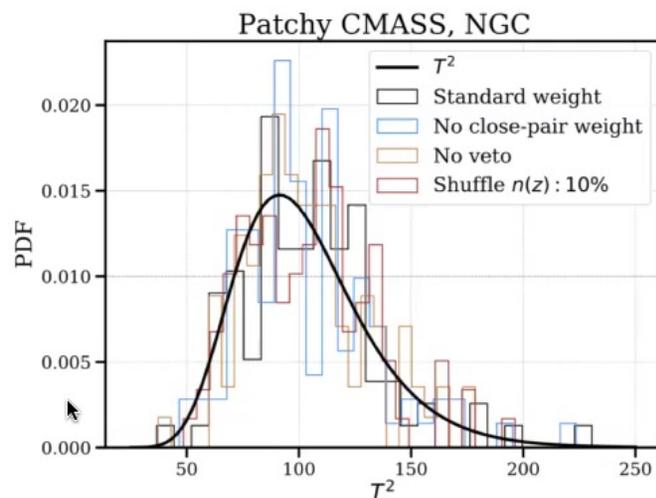


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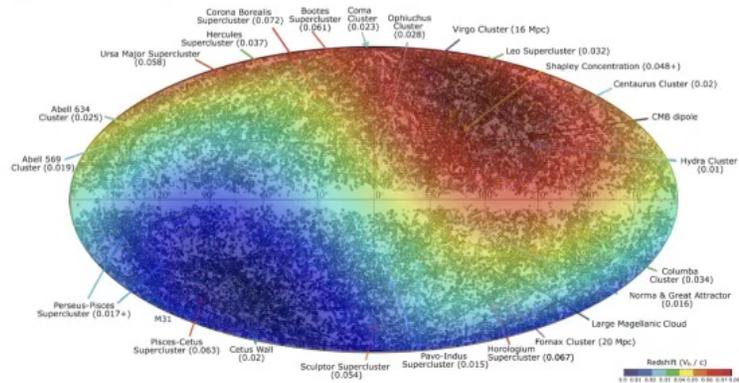
Impact of Systematics on Parity-odd Modes

- fiber collision
- veto mask
- selection function

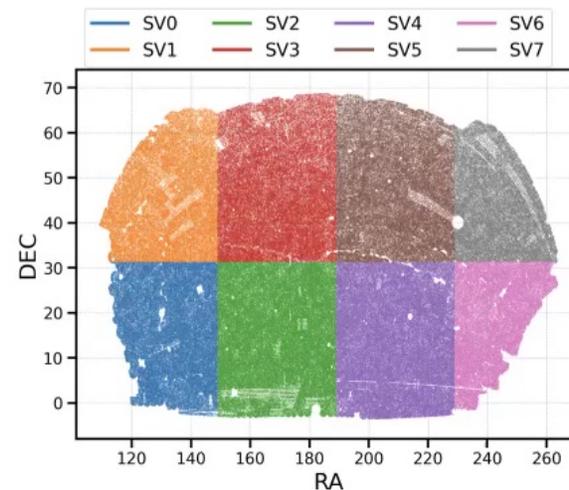


- Split sky test

Image credit: reproduced from Huchra et al. 2012

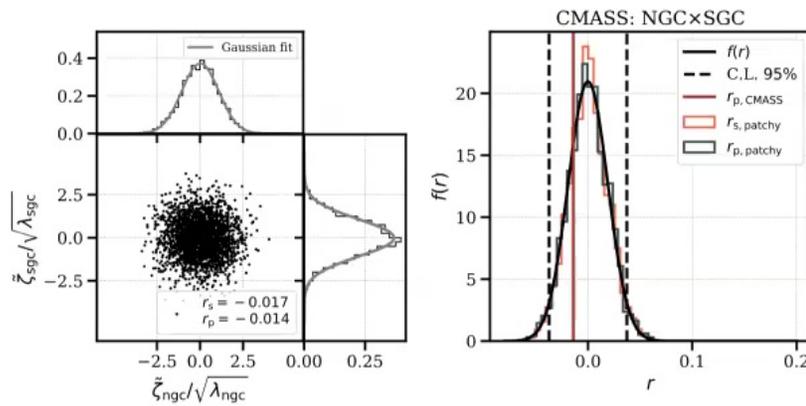


- Kaiser-rocket effect



A non-exhaustive list for Potential Questions

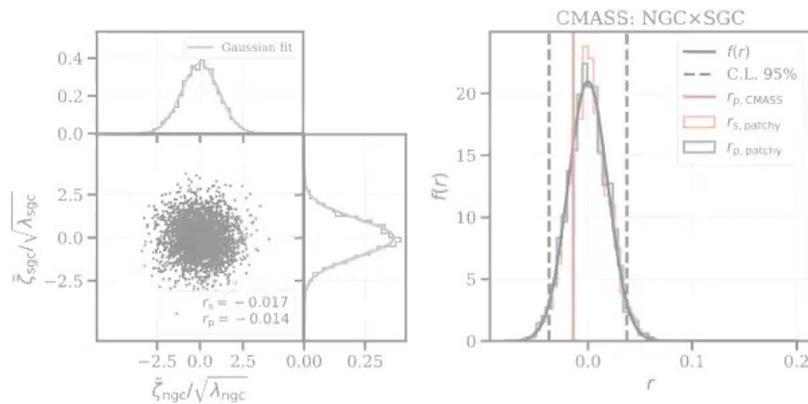
Correlation across the Sky?



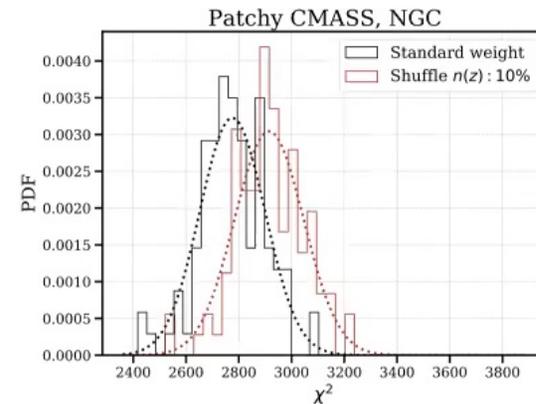
- Low signal-to-noise ratio
- Toy model: possible to have statistically significant detection but low correlation.

A non-exhaustive list for Potential Questions

Correlation across the Sky?



Systematics-induced variance?

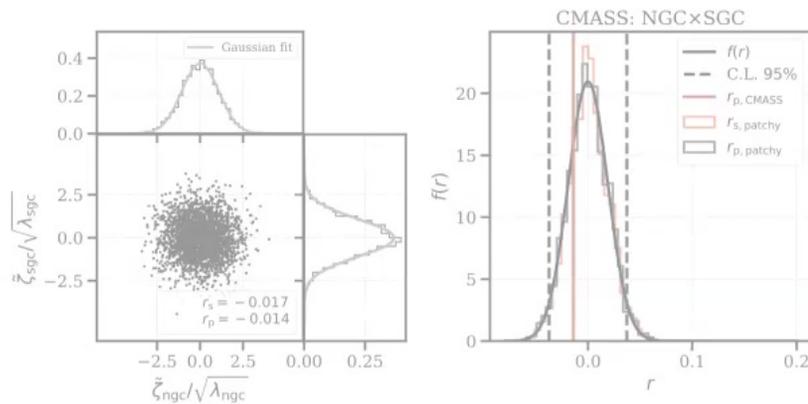


Consistency in Even-Parity Sector	CMASS 18 bins	Rescaling Factor	Rescaled Odd Detection Significance
1 standard deviation	Analytic Covariance	0.88	2.0σ
	$N_{\text{eig}} = 800$	0.98	4.0σ
3 standard deviation	Analytic Covariance	0.94	4.6σ
	$N_{\text{eig}} = 800$	-	4.4σ

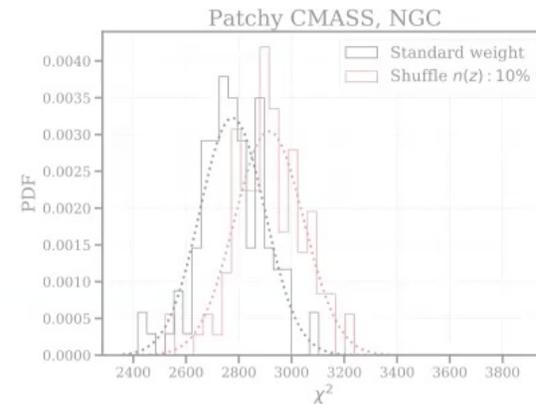
- Under-estimate covariance
- Self calibration with parity-even mode

A non-exhaustive list for Potential Questions

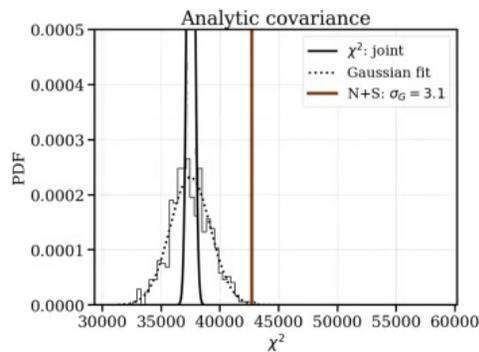
Correlation across the Sky?



Systematics-induced variance?



Consistency with LOWZ?



- Smaller volume?
- Different galaxy properties than CMASS (population, $n(z)$...)?

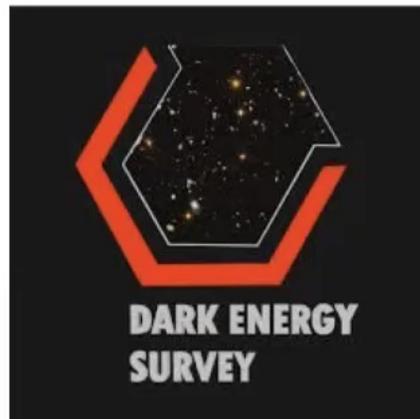
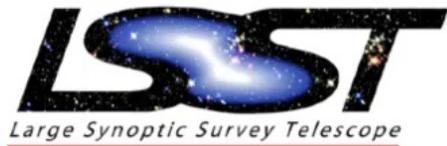
Summary

- NPCF algorithm
- First detection of connected 4PCF
- Analytical covariance matrix in the Gaussian limit
- 4PCF of LSS as a test for parity violation
 - ➔ **Statistically significant detection**
 - ➔ **If true: likely non-Gaussian initial condition**
 - ➔ **To be validated on future datasets**
 - ➔ **Open an avenue to study parity violation with LSS**

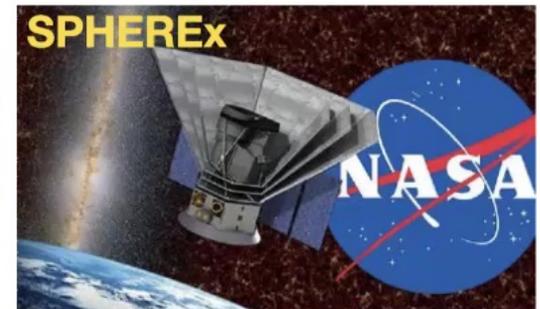
Next-stage Galaxy Surveys



Vera Rubin
Observatory



Prime
Focus
Spectrograph



Next steps

- Dark Energy Spectroscopic Instrument (DESI)
 - Started 5-year survey on May 17, 2021
 - Collected ~18 M galaxies' spectra (2.7 M LRGs)
- Models for parity-odd signal
- Simulations with parity-violating mechanism
- Residual systematics

