

Title: Programmable quantum systems based on Rydberg atom arrays

Speakers: Mikhail Lukin

Collection: Cold Atom Molecule Interactions (CATMIN)

Date: July 15, 2022 - 9:00 AM

URL: <https://pirsa.org/22070012>

Abstract: We will discuss the recent advances involving programmable, coherent manipulation of quantum many-body systems using neutral atom arrays excited into Rydberg states, allowing the control over 200 qubits in two dimensions. These systems can be used for realization and probing of exotic quantum phases of matter and exploration of their non-equilibrium dynamics. Recent advances involving the realization and probing of quantum spin liquid states - the exotic topological states of matter have thus far evaded direct experimental detection and the observation of quantum speedup for solving optimization problems will be described. In addition, the realization of novel quantum processing architecture based on dynamically reconfigurable entanglement and the steps towards quantum error correction will be discussed. Finally, we will discuss prospects for using these techniques for realization of large-scale quantum processors.

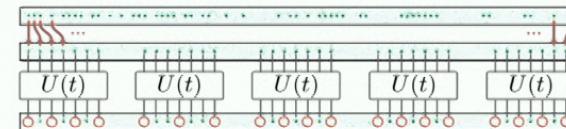
Exploring New Scientific Frontiers using Programmable Rydberg Arrays

Mikhail Lukin
Physics Department, Harvard University

This talk

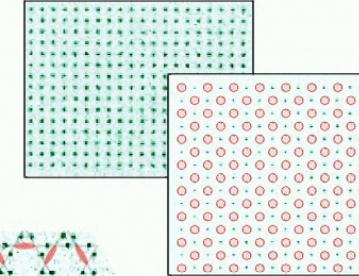
✓ Building scalable quantum systems using Rydberg atom arrays

- Atom-by-atom assembly of strongly interacting quantum matter
- Exploring quantum phase transitions
- Quantum control of large 2D atom arrays



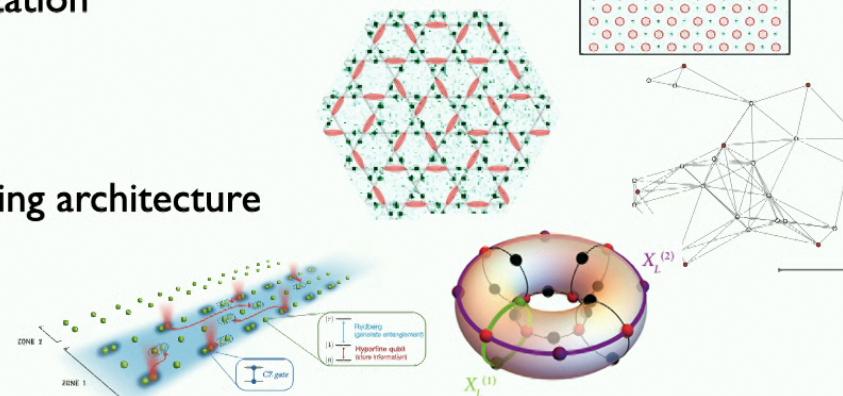
✓ Probing quantum dynamics of many-body systems

- Quantum phases & phase transitions in 2D spin models
- Probing topological spin liquids
- Applications to quantum optimization



✓ Current efforts and outlook

- Reconfigurable quantum processing architecture



Atom-by-atom approach for building scalable quantum systems

Laser cooled neutral atoms: removing entropy by observation

Pioneering work: Regal, Browaeys groups

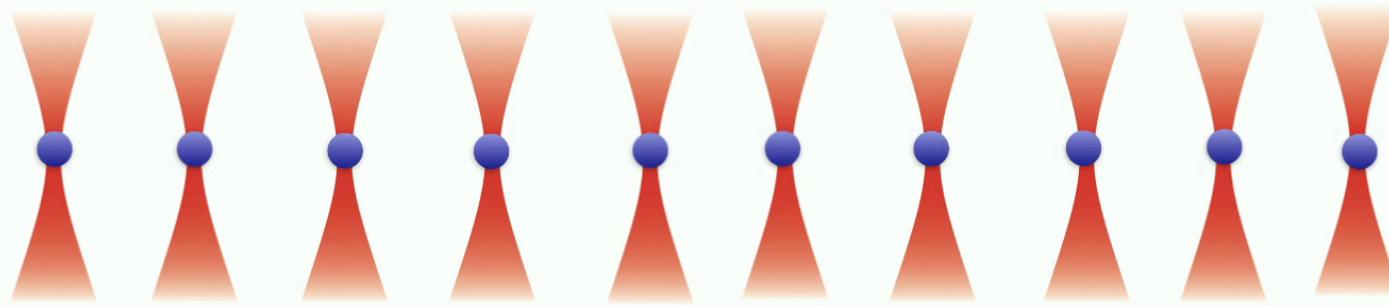
A.M. Kaufman, et al., Science **345**, 306 (2014)
H. Labuhn et al., arXiv:1509.04543 (2015)

Hannes Bernien, Sylvin Schwatz, Alexander Keesling, Harry Levine, Ahmed Omran, Giulia Semeghini
CUA collaboration of Lukin, Greiner & Vuletic groups, Manuel Endres group at Caltech

Atom-by-atom approach for building scalable quantum systems

Laser cooled neutral atoms: removing entropy by observation

1. Tightly focused laser trap loads ultra cold atoms from Magneto-Optical Trap
2. Image and remove empty traps
3. Rearrange remaining traps->regular atom array

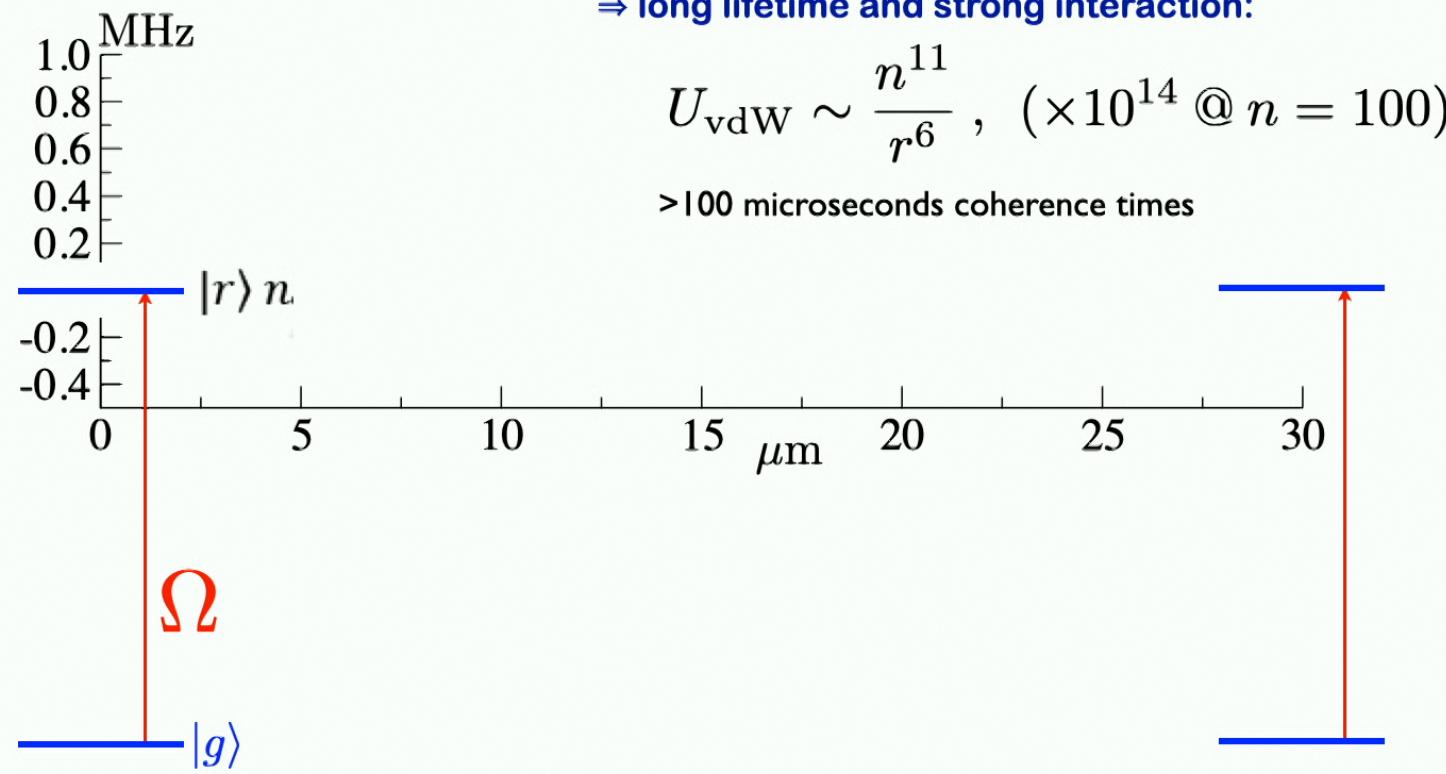


Pioneering work: Regal, Browaeys groups

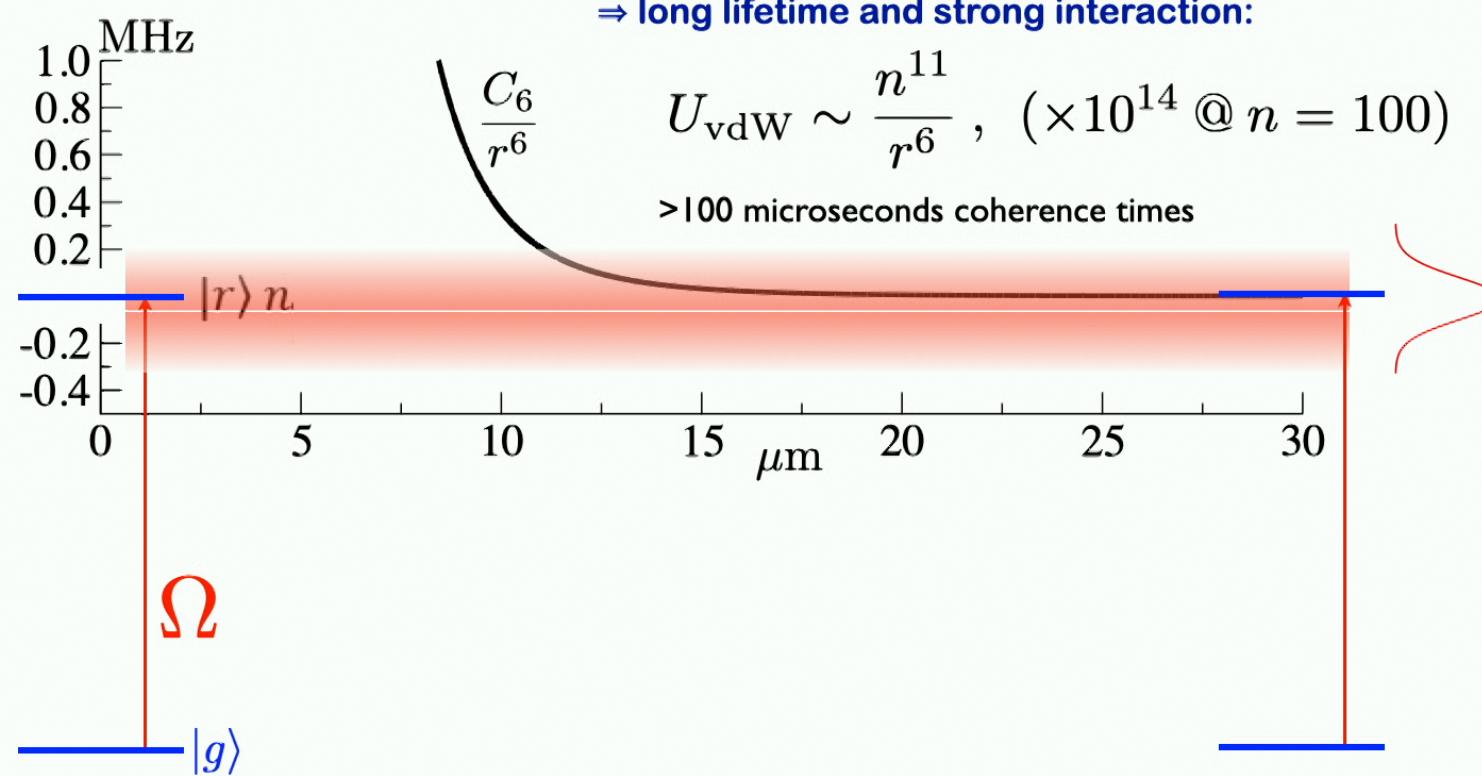
A.M. Kaufman, et al., Science 345, 306 (2014)
H. Labuhn et al., arXiv:1509.04543 (2015)

Hannes Bernien, Sylvin Schwatz, Alexander Keesling, Harry Levine, Ahmed Omran, Giulia Semeghini
CUA collaboration of Lukin, Greiner & Vuletic groups, Manuel Endres group at Caltech

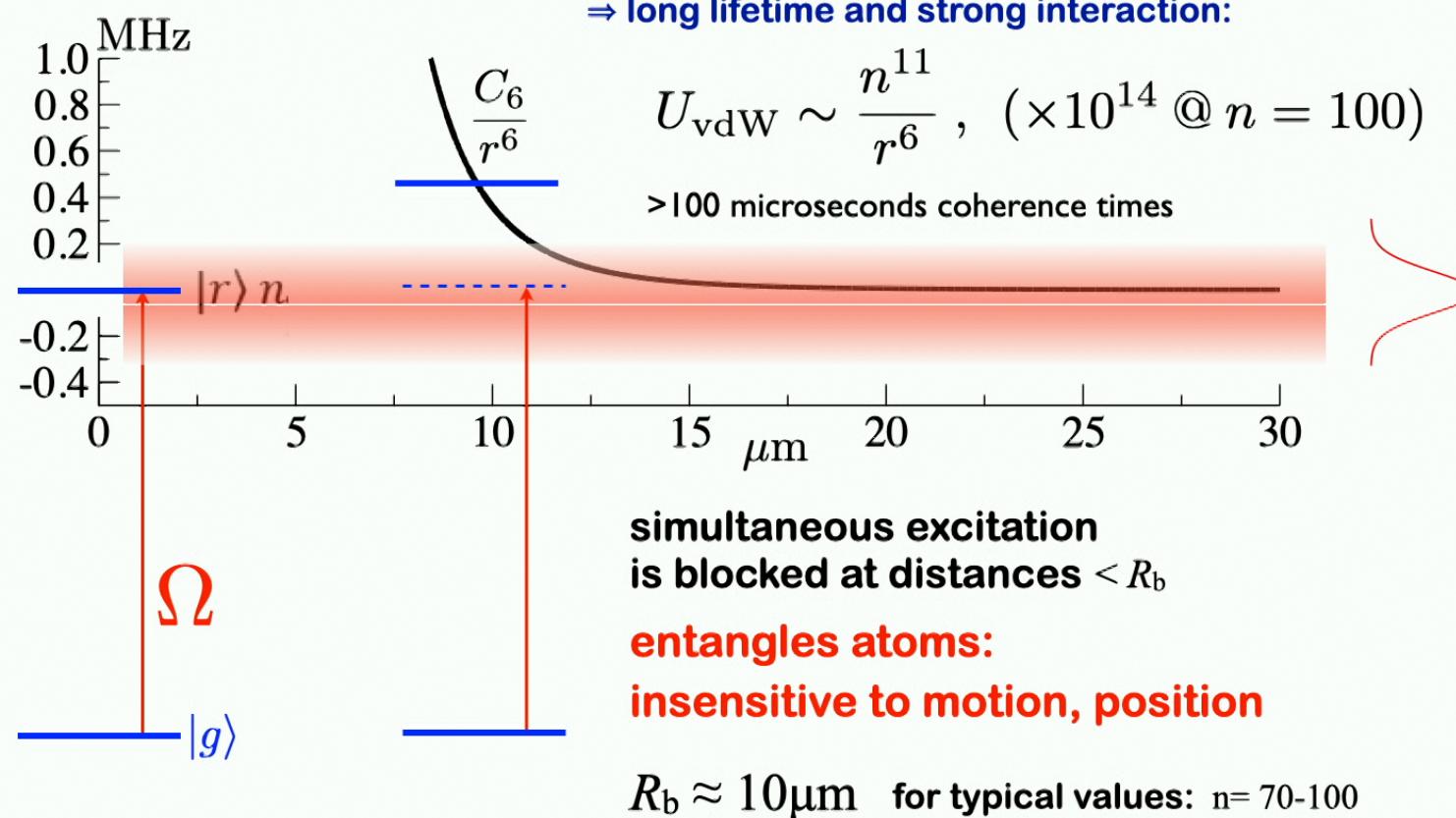
Rydberg blockade for atoms with larger n



Rydberg blockade for atoms with larger n

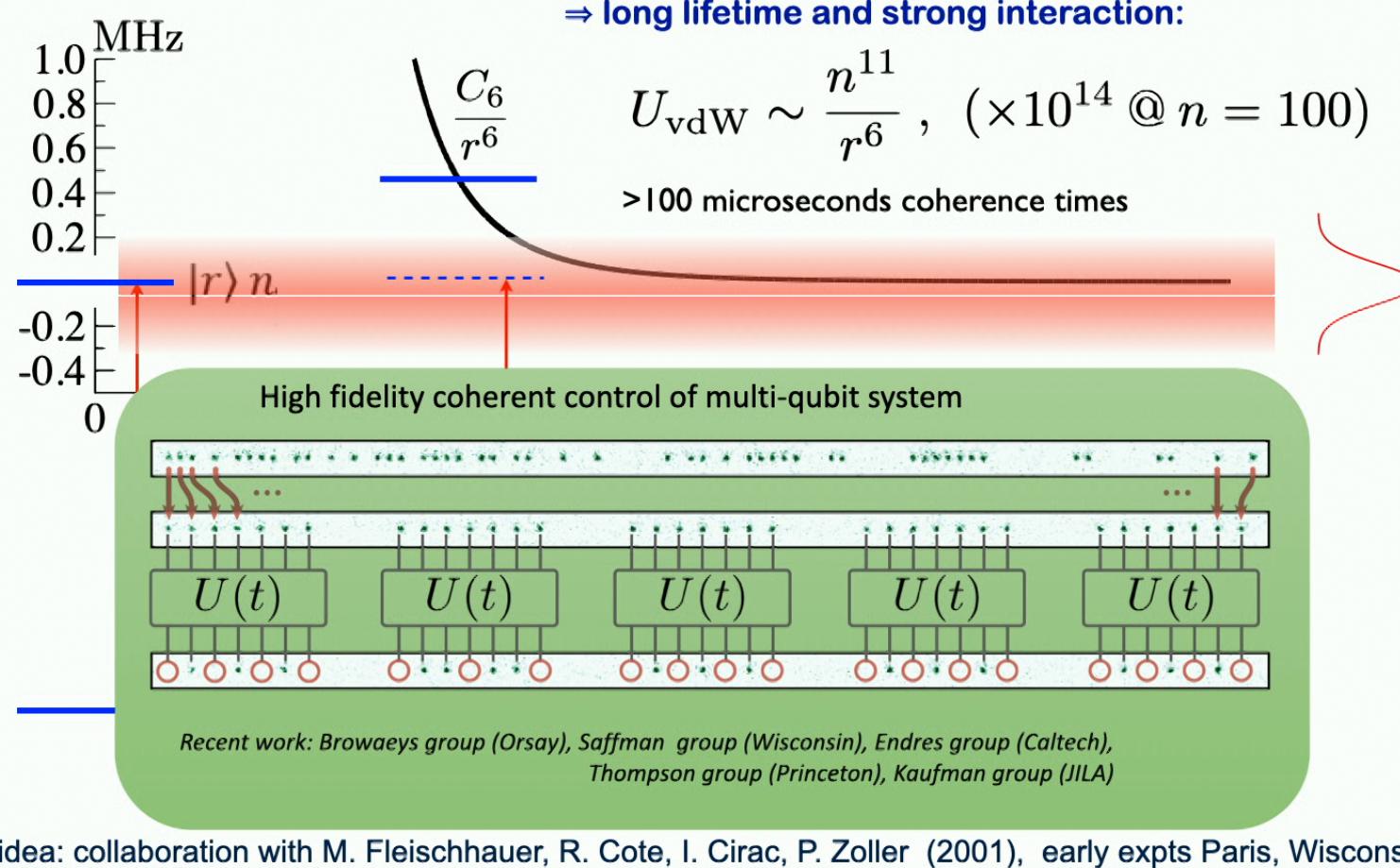


Rydberg blockade for atoms with larger n

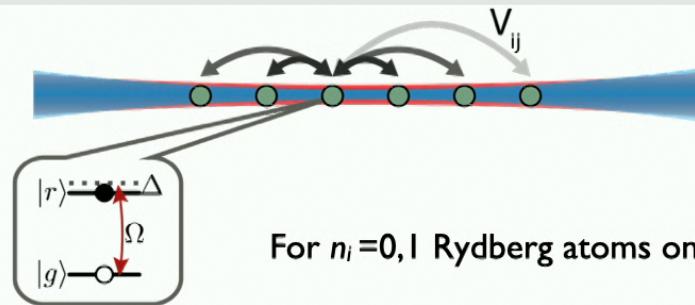


idea: collaboration with M. Fleischhauer, R. Cote, I. Cirac, P. Zoller (2001), early expts Paris, Wisconsin

Rydberg blockade for atoms with larger n



Programmable quantum simulator using atom arrays



For $n_i=0,1$ Rydberg atoms on each site i

$$\mathcal{H} = \sum_i \frac{\hbar\Omega}{2} \sigma_x^i - \sum_i \hbar\Delta n_i + \sum_{i < j} V_{i,j} n_i n_j$$

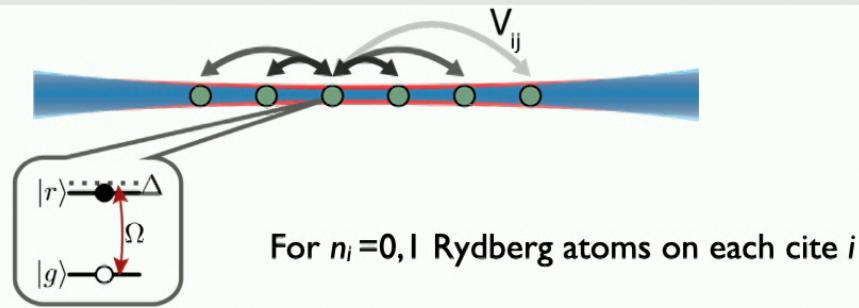
Ising-type model:

Fendley, Sengupta, Sachdev PRB **69**, 075106 (2004)

Original PQS idea: R. Feynman (1981)

Experiment: Hannes Bernien, et al, arXiv 1707.04344, Nature (2017)

Programmable quantum simulator using atom arrays



$$\mathcal{H} = \sum_i \frac{\hbar\Omega}{2} \sigma_x^i - \sum_i \hbar\Delta n_i + \sum_{i < j} V_{i,j} n_i n_j$$

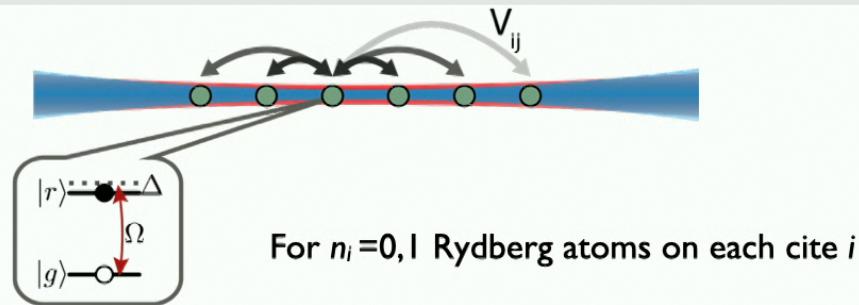
Ising-type model:

Fendley, Sengupta, Sachdev PRB **69**, 075106 (2004)

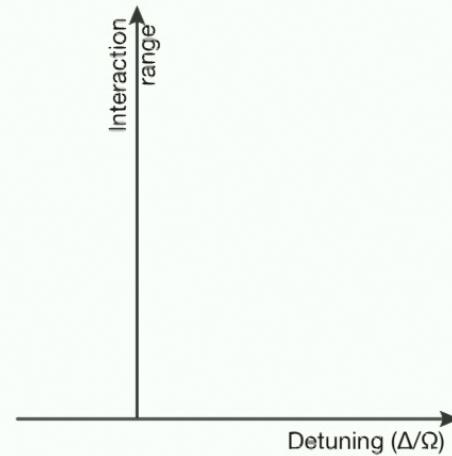
Original PQS idea: R. Feynman (1981)

Experiment: Hannes Bernien, et al, arXiv 1707.04344, Nature (2017)

Programmable quantum simulator using atom arrays



$$\mathcal{H} = \sum_i \frac{\hbar\Omega}{2} \sigma_x^i - \sum_i \hbar\Delta n_i + \sum_{i < j} V_{i,j} n_i n_j$$



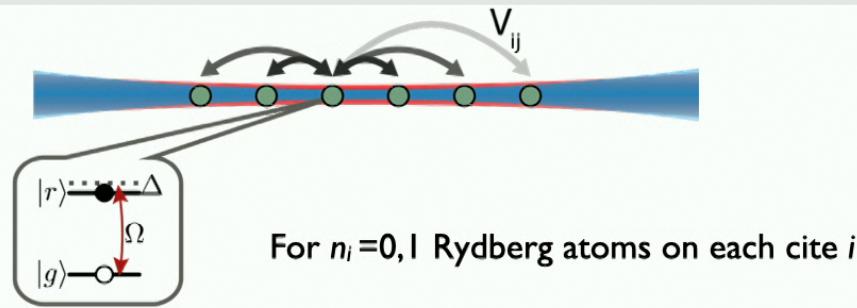
Ising-type model:

Fendley, Sengupta, Sachdev PRB **69**, 075106 (2004)

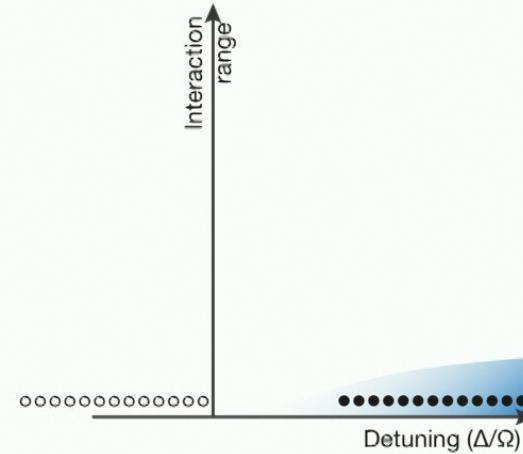
Original PQS idea: R. Feynman (1981)

Experiment: Hannes Bernien, et al, arXiv 1707.04344, Nature (2017)

Programmable quantum simulator using atom arrays



$$\mathcal{H} = \sum_i \frac{\hbar\Omega}{2} \sigma_x^i - \sum_i \hbar\Delta n_i + \sum_{i < j} V_{i,j} n_i n_j$$



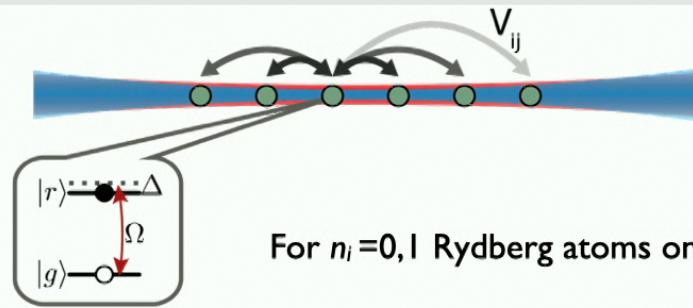
Ising-type model:

Fendley, Sengupta, Sachdev PRB **69**, 075106 (2004)

Original PQS idea: R. Feynman (1981)

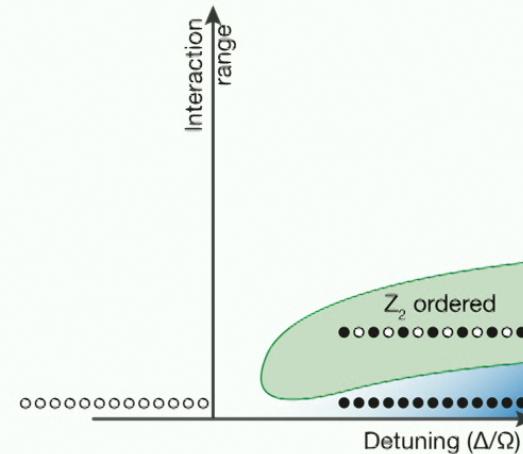
Experiment: Hannes Bernien, et al, arXiv 1707.04344, Nature (2017)

Programmable quantum simulator using atom arrays



For $n_i=0,1$ Rydberg atoms on each site i

$$\mathcal{H} = \sum_i \frac{\hbar\Omega}{2} \sigma_x^i - \sum_i \hbar\Delta n_i + \sum_{i < j} V_{i,j} n_i n_j$$



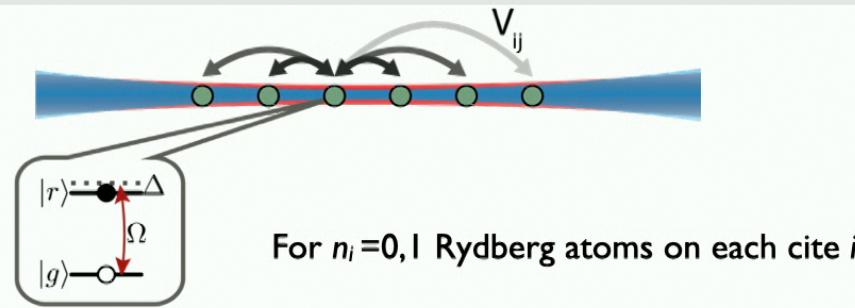
Ising-type model:

Fendley, Sengupta, Sachdev PRB **69**, 075106 (2004)

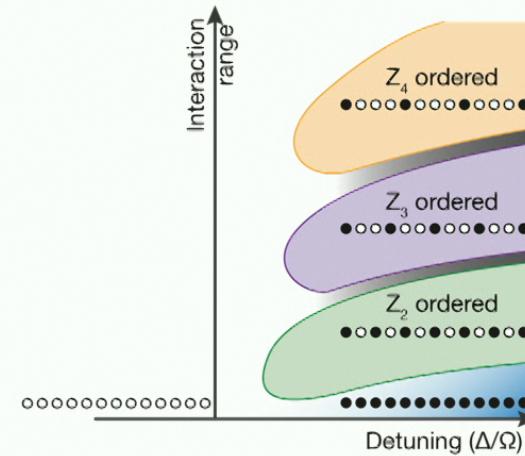
Original PQS idea: R. Feynman (1981)

Experiment: Hannes Bernien, et al, arXiv 1707.04344, Nature (2017)

Programmable quantum simulator using atom arrays



$$\mathcal{H} = \sum_i \frac{\hbar\Omega}{2} \sigma_x^i - \sum_i \hbar\Delta n_i + \sum_{i < j} V_{i,j} n_i n_j$$



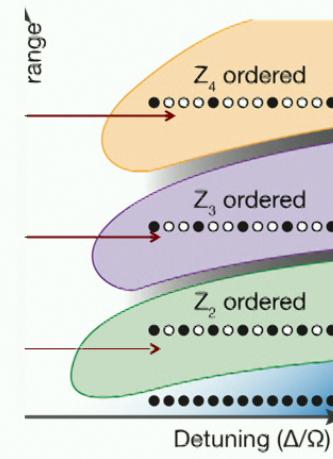
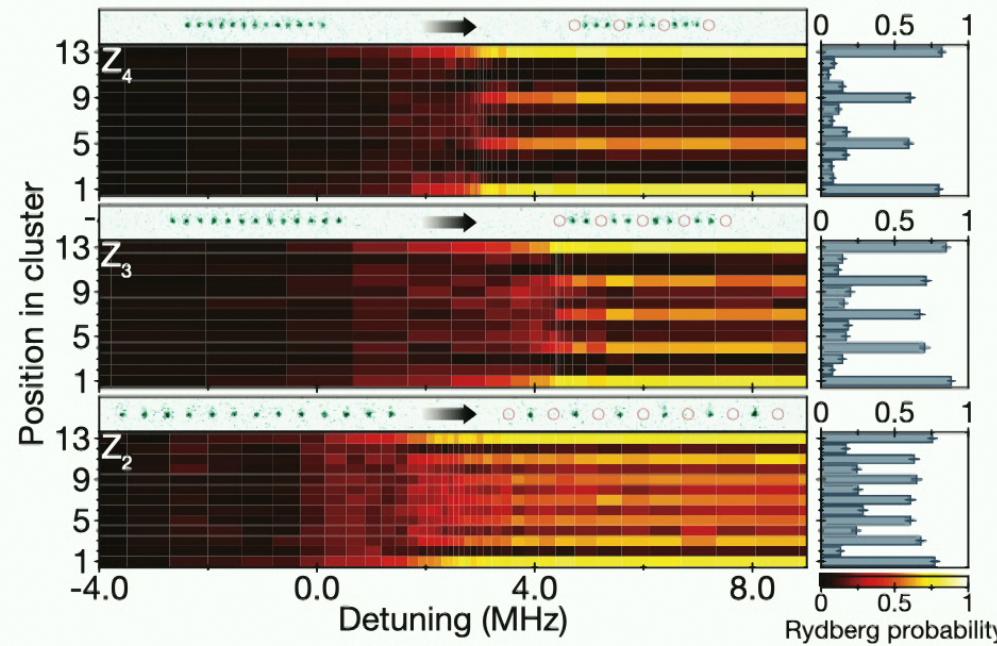
Ising-type model:

Fendley, Sengupta, Sachdev PRB **69**, 075106 (2004)

Original PQS idea: R. Feynman (1981)

Experiment: Hannes Bernien, et al, arXiv 1707.04344, Nature (2017)

Programmable quantum simulator using atom arrays

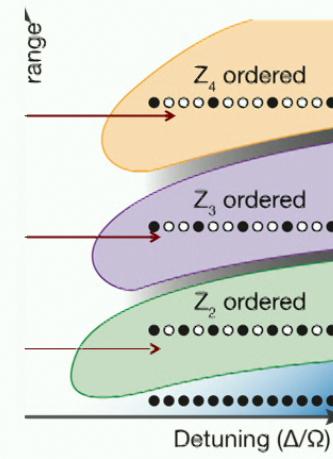
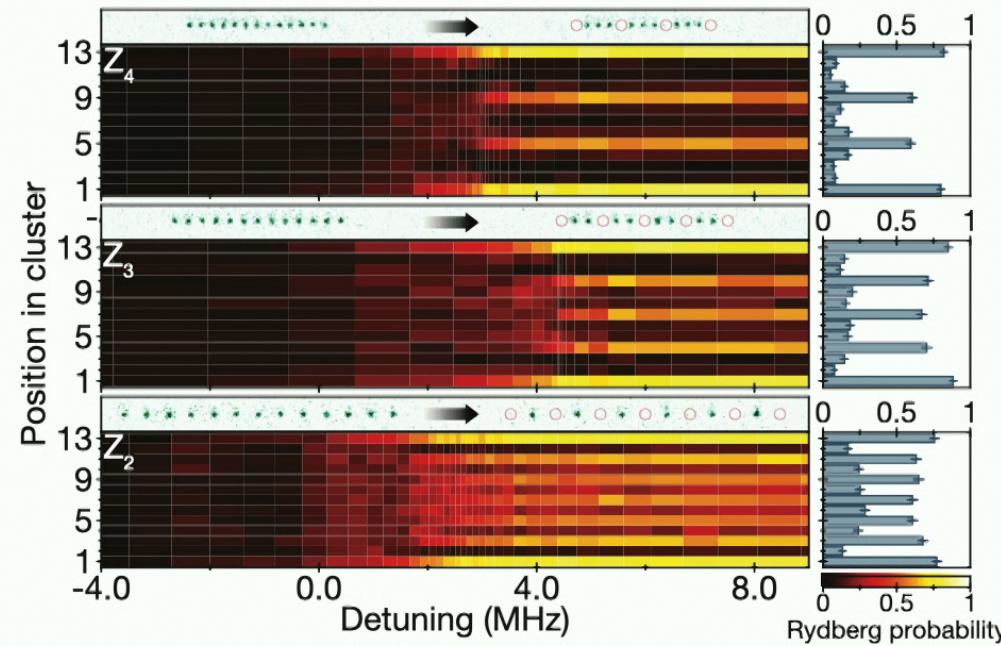


Approach: adiabatic following across phase transition

Original PQS idea: R. Feynman (1981)

Experiment: Hannes Bernien, et al, arXiv 1707.04344, Nature (2017)

Programmable quantum simulator using atom arrays



Approach: adiabatic following across phase transition

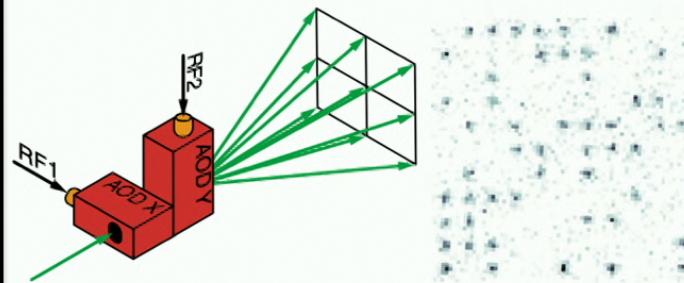
Programmable interactions result in desired symmetry breaking!

Original PQS idea: R. Feynman (1981)

Experiment: Hannes Bernien, et al, arXiv 1707.04344, Nature (2017)

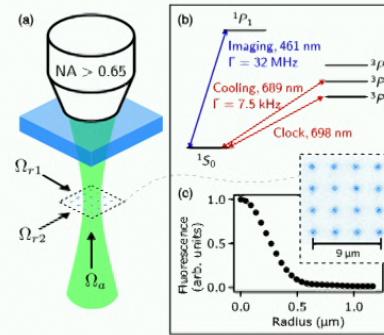
Tweezer arrays for different atoms and molecules

Strontium array, EndresLab@Caltech



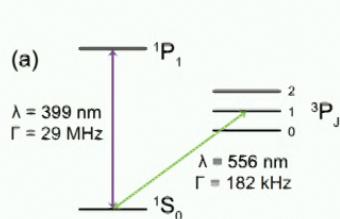
A. Cooper et al. PRX 8, 041055 (2018)

Strontium array, KaufmanLab@JILA



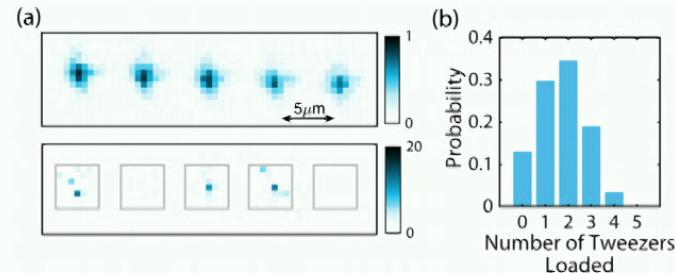
M. A. Norcia et al. PRX 8, 041054 (2018)

Ytterbium array, ThompsonLab@Princeton



S. Saskin et al. arXiv:1810.10517 (2018)

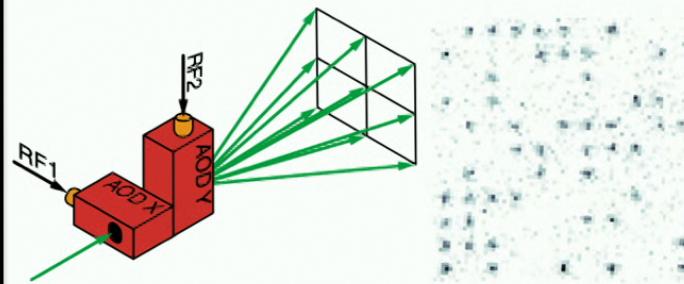
CaF molecules array, DoyleLab@Harvard



L. Anderegg et al. arXiv:1902.00497 (2019)

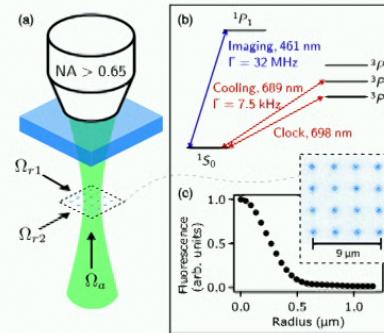
Tweezer arrays for different atoms and molecules

Strontium array, EndresLab@Caltech



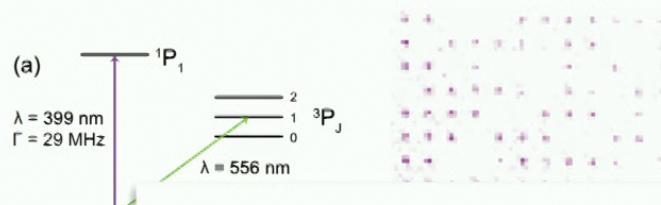
A. Cooper et al. PRX 8, 041055 (2018)

Strontium array, KaufmanLab@JILA

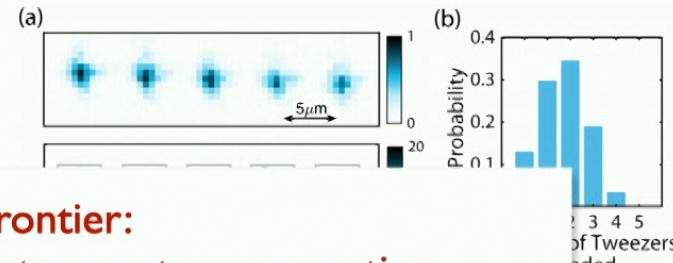


M. A. Norcia et al. PRX 8, 041054 (2018)

Ytterbium array, ThompsonLab@Princeton



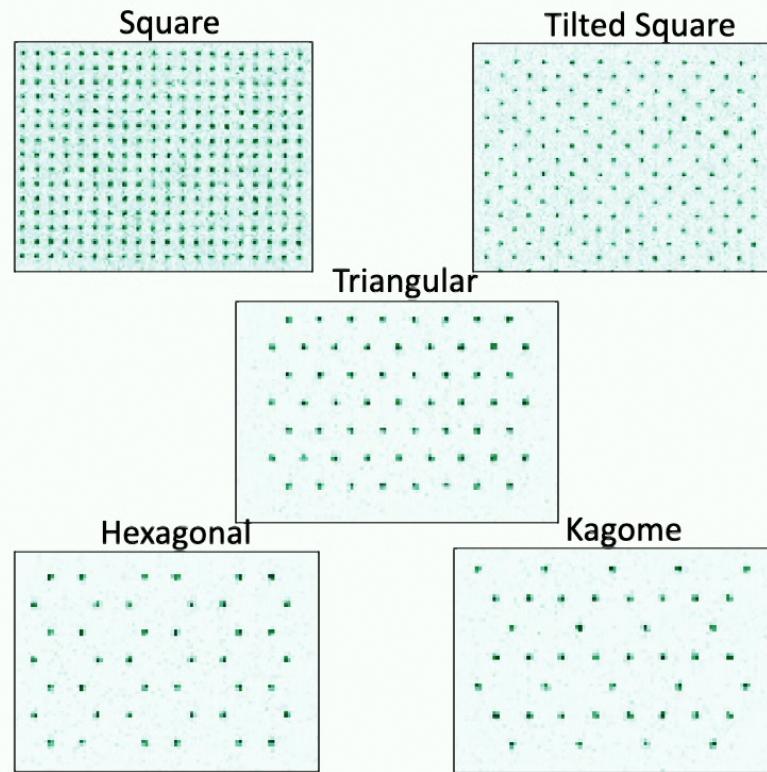
CaF molecules array, DoyleLab@Harvard



(2019)

Exciting frontier:
from many-body dynamics to quantum computing
and quantum metrology, complimentary to optical lattices

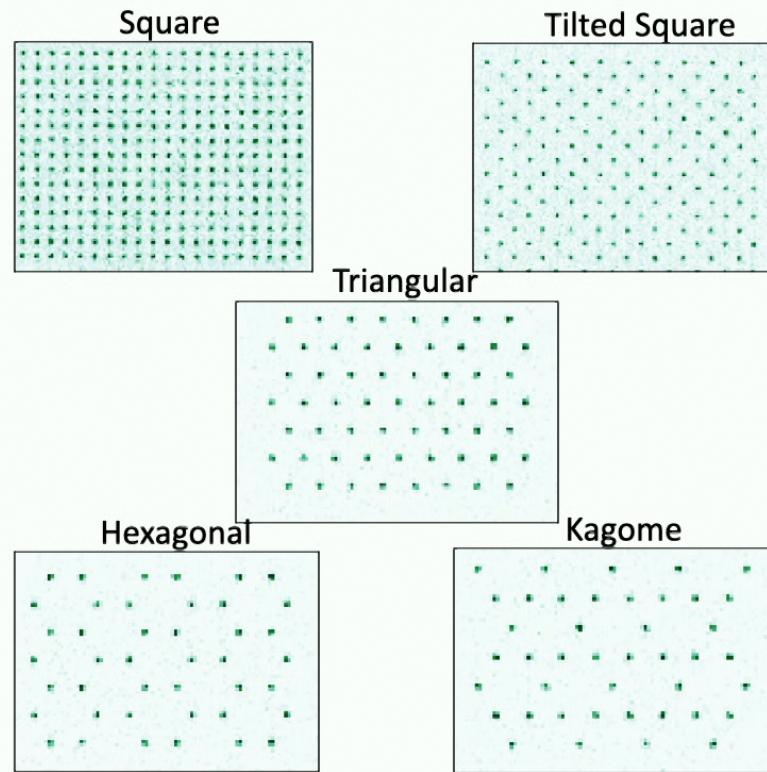
Atom Array Generation 2: large scale 2D atom arrays



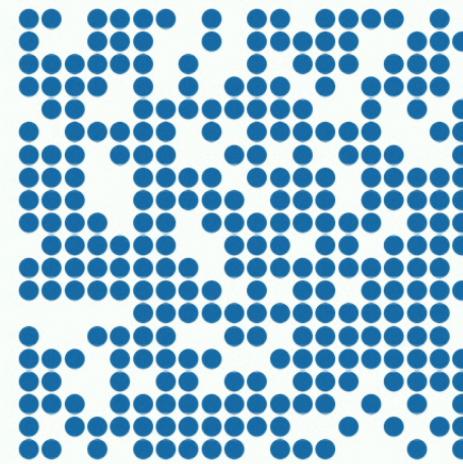
S. Ebadi et al arxiv 2012.12281, Nature (2021)

see also work on 2d and 3d atom arrays at Orsay, Penn State

Atom Array Generation 2: large scale 2D atom arrays



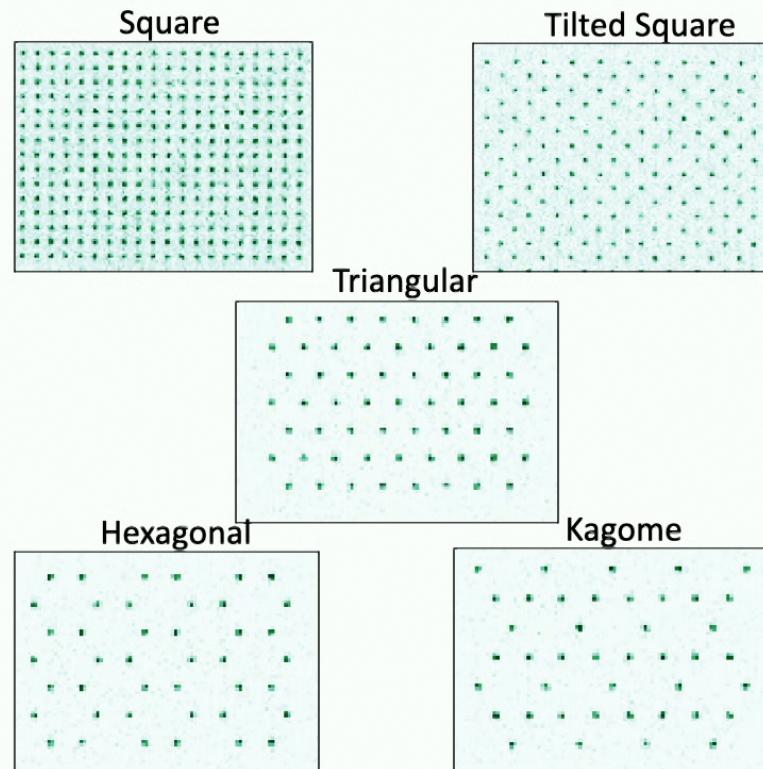
Arbitrary patterns:
randomly generated 75%
filling in 20x20



S. Ebadi et al arxiv 2012.12281, Nature (2021)

see also work on 2d and 3d atom arrays at Orsay, Penn State

Atom Array Generation 2: large scale 2D atom arrays

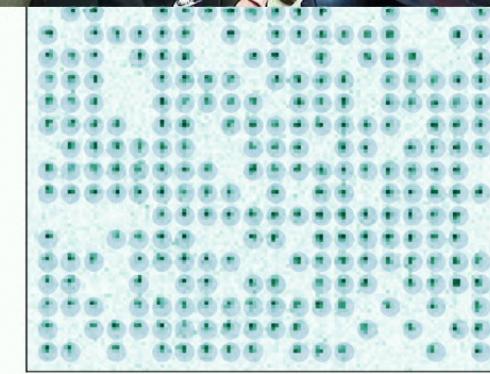
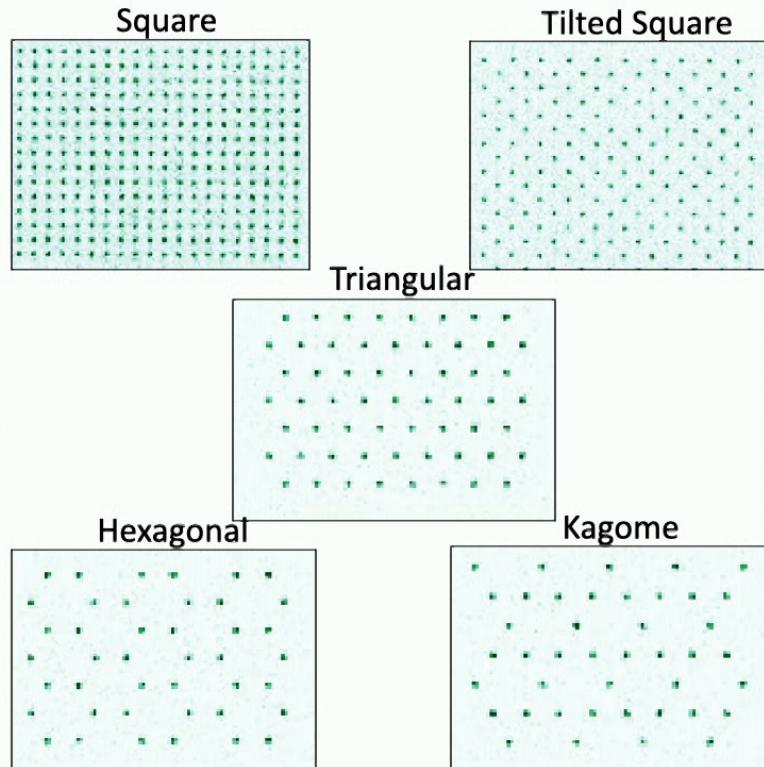


55-60% filling fraction for 600 traps => 300 sorted atoms, each filled trap >99% probability

S. Ebadi et al arxiv 2012.12281, Nature (2021)

see also work on 2d and 3d atom arrays at Orsay, Penn State

Atom Array Generation 2: large scale 2D atom arrays



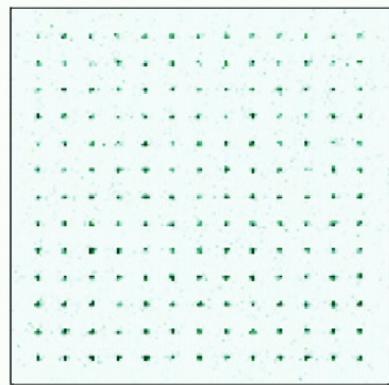
55-60% filling fraction for 600 traps => 300 sorted atoms, each filled trap >99% probability

S. Ebadi et al arxiv 2012.12281, Nature (2021)

see also work on 2d and 3d atom arrays at Orsay, Penn State

Quantum phase transitions in 2D arrays

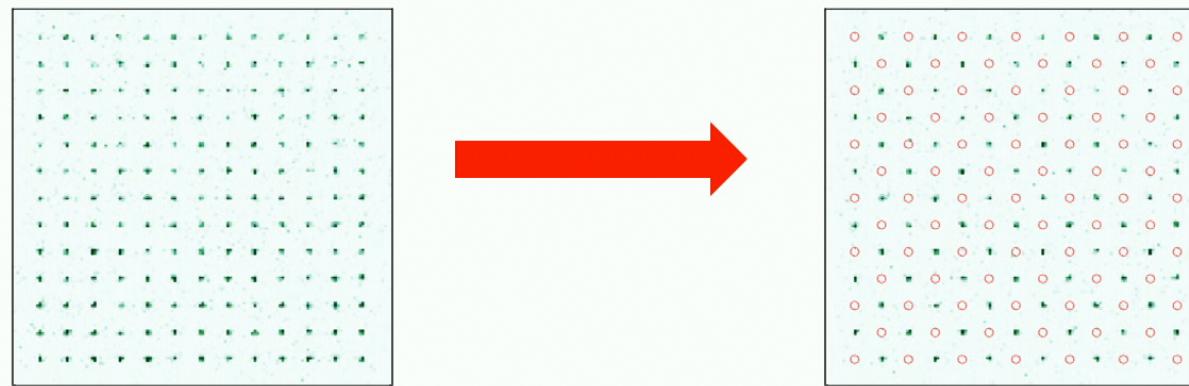
- adjust Rydberg blockade to control interaction range
- adiabatic detuning sweep to reach the state



S. Ebadi et al arxiv 2012.12281, Nature (2021)

Quantum phase transitions in 2D arrays

- adjust Rydberg blockade to control interaction range
- adiabatic detuning sweep to reach the state

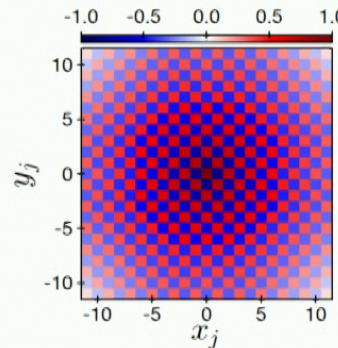


S. Ebadi et al arxiv 2012.12281, Nature (2021)

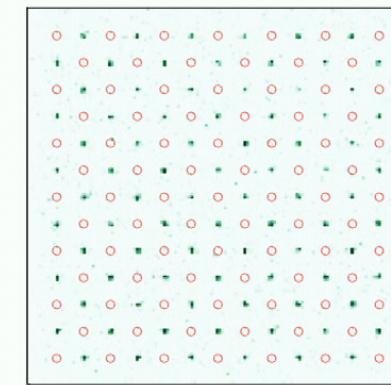
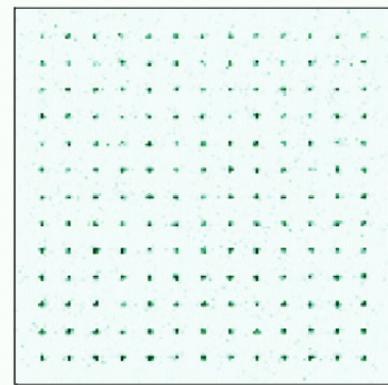
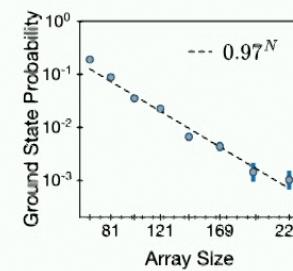
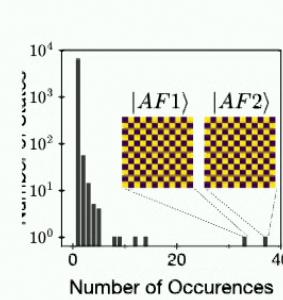
Quantum phase transitions in 2D arrays

Correlations

$$g^2(i,j) = \langle n_i n_j \rangle - \langle n_i \rangle \langle n_j \rangle$$

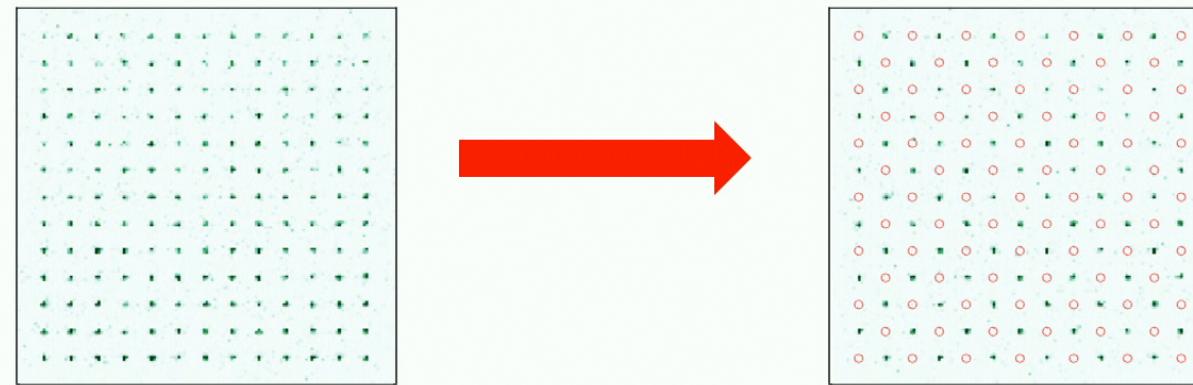
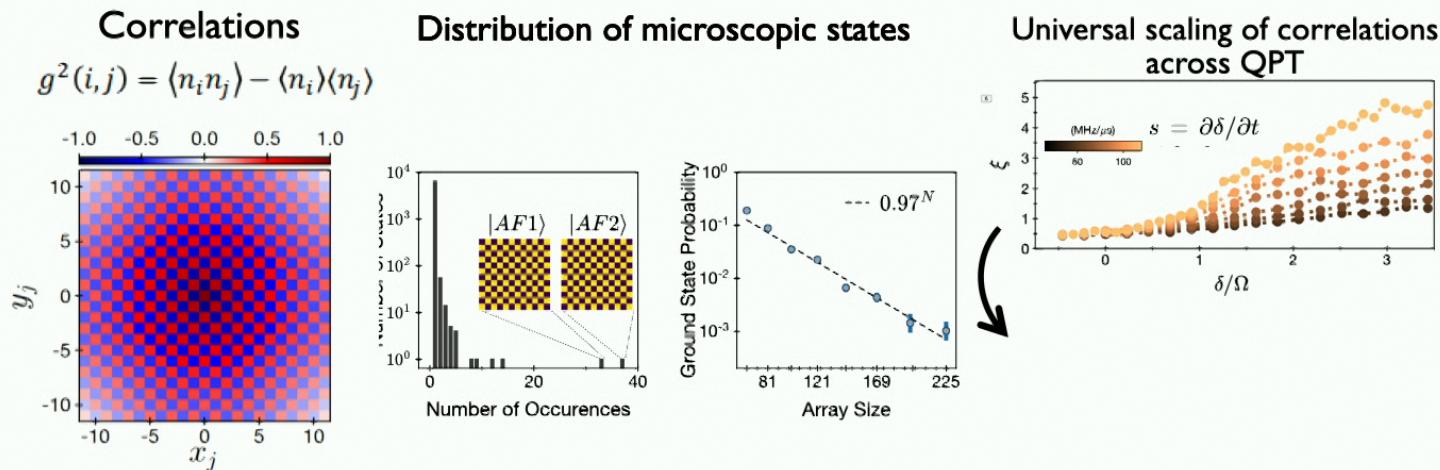


Distribution of microscopic states



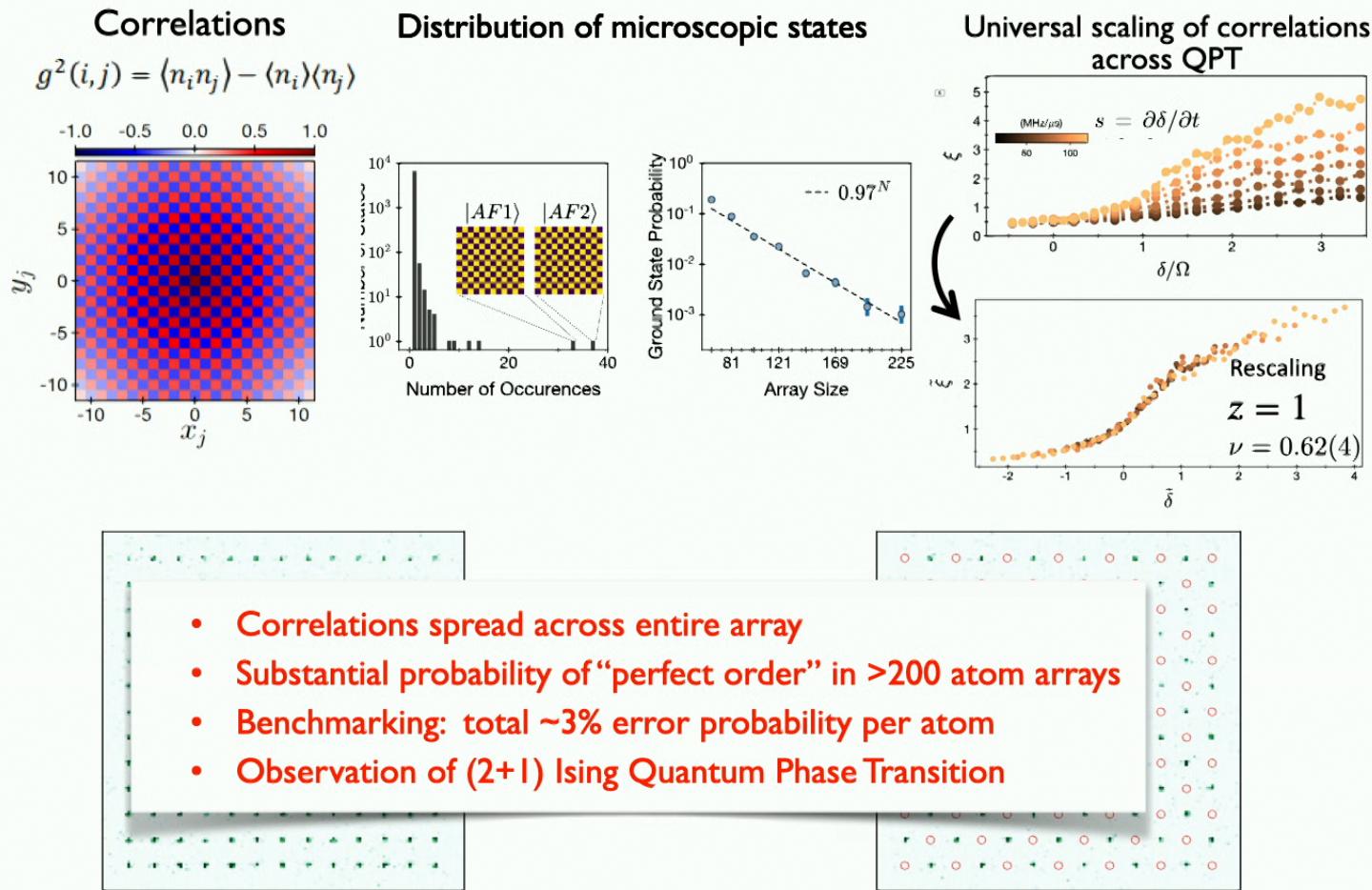
S. Ebadi et al arxiv 2012.12281, Nature (2021)

Quantum phase transitions in 2D arrays



S. Ebadi et al arxiv 2012.12281, Nature (2021)

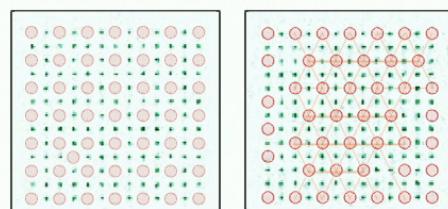
Quantum phase transitions in 2D arrays



S. Ebadi et al arxiv 2012.12281, Nature (2021)

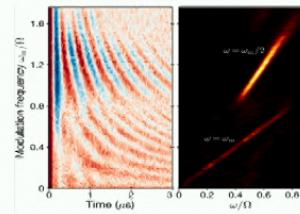
Programmable quantum simulators based on Rydberg arrays: recent progress

Exploring 2D phase diagrams



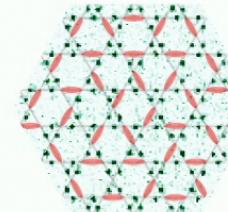
S. Ebadi et al arxiv 2012.12281, Nature (2021)

Non-equilibrium dynamics: many-body scars



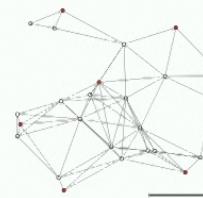
D. Bluvstein, et al arxiv 2012.12276, Science (2021)

Probing topological spin liquids



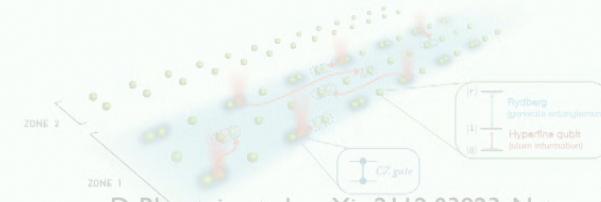
G. Semeghini et al, arXiv:2104.04119, Science (2021)

Accelerating combinatorial optimization



S. Ebadi et al, arXiv 2202.09372
Science (2022)

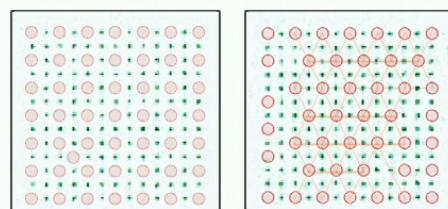
Entanglement transport & universal programmability



D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

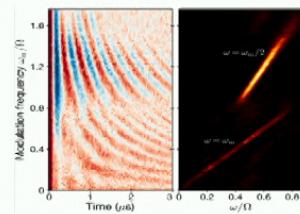
Programmable quantum simulators based on Rydberg arrays: recent progress

Exploring 2D phase diagrams



S. Ebadi et al arxiv 2012.12281, Nature (2021)

Non-equilibrium dynamics: many-body scars



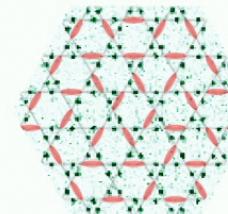
D. Bluvstein, et al, arxiv 2012.12276, Science (2021)

IQuEra™

Available on AWS cloud
this year!

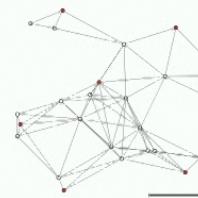


Probing topological spin liquids



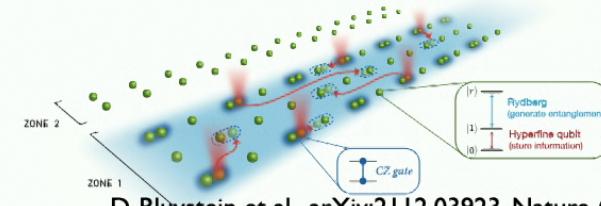
G. Semeghini et al, arXiv:2104.04119, Science (2021)

Accelerating combinatorial optimization



S. Ebadi et al, arXiv 2202.09372
Science (2022)

Entanglement transport & universal programmability



D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Tackling a Long-Elusive Goal: Topological Spin Liquids

Special form of matter in “frustrated” systems, postulated by P.W.Anderson
Materials Research Bulletin 8 (1973), Science 235 (1987)



Tackling a Long-Elusive Goal: Topological Spin Liquids

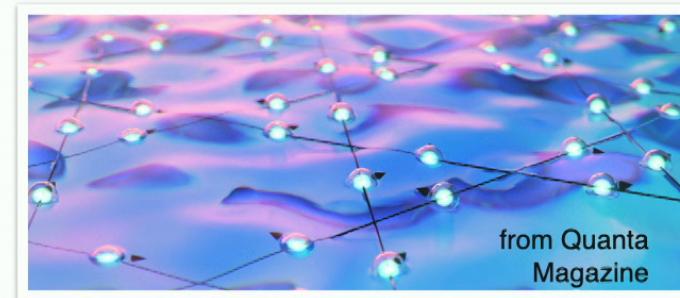
Special form of matter in “frustrated” systems, postulated by P.W.Anderson
Materials Research Bulletin 8 (1973), Science 235 (1987)



Phase of matter with exotic properties:

topological order robust against perturbations, long-range quantum entanglement, emergent lattice gauge theories, anyonic excitations...

→ major effort in condensed matter physics for the past several decades



Early work: Sachdev, Read, Wen, Kivelson, Moessner, Sondi ...

Tackling a Long-Elusive Goal: Topological Spin Liquids

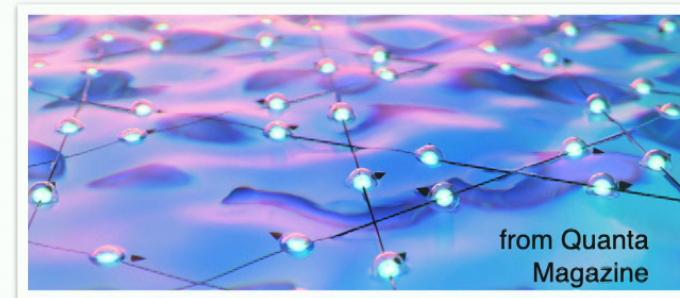
Special form of matter in “frustrated” systems, postulated by P.W.Anderson
Materials Research Bulletin 8 (1973), Science 235 (1987)



Phase of matter with exotic properties:

topological order robust against perturbations, long-range quantum entanglement, emergent lattice gauge theories, anyonic excitations...

→ major effort in condensed matter physics for the past several decades

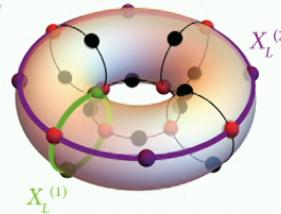


Fault-tolerant quantum computation by anyons

A.Yu. Kitaev*

L.D. Landau Institute for Theoretical Physics, 117940, Kosygina St. 2, Germany

Received 20 May 2002



Application to quantum information processing:

topological qubits robust against external noise

Early work: Sachdev, Read, Wen, Kivelson, Moessner, Sondi ...

Tackling a Long-Elusive Goal: Topological Spin Liquids

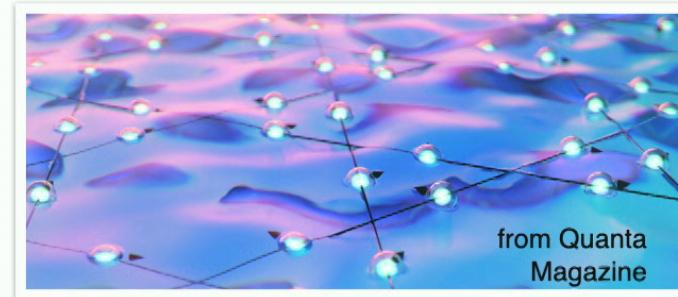
Special form of matter in “frustrated” systems, postulated by P.W.Anderson
Materials Research Bulletin 8 (1973), Science 235 (1987)



Phase of matter with exotic properties:

topological order robust against perturbations, long-range quantum entanglement, emergent lattice gauge theories, anyonic excitations...

→ major effort in condensed matter physics for the past several decades

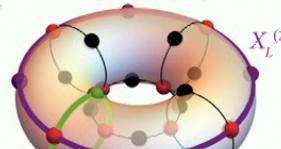


Fault-tolerant quantum computation by anyons

A.Yu. Kitaev*

L.D. Landau Institute for Theoretical Physics, 117940, Kosygina St. 2, Germany

Received 20 May 2002



Application to quantum information processing:

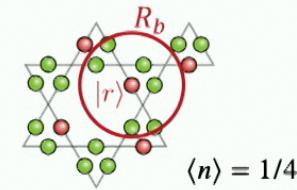
topological qubits robust against external noise

No conclusive experimental evidence in any system

Wen, Levin, Wilczek, Levinson, Moessner, Sondi ...

Dimer model with Rydberg atoms on links of kagome lattice

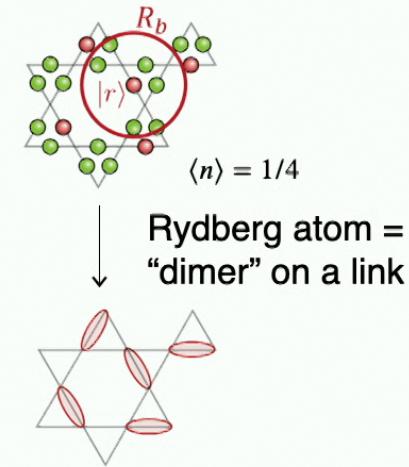
Key idea: Rydberg blockade on frustrated lattice results in highly degenerate states



Theory: R. Samajdar, et al S. Sachdev's group arXiv:2011.12295, PNAS (2020)
R. Verresen, et al A. Vishwanath's group arXiv:2011.12310, PRX (2021)

Dimer model with Rydberg atoms on links of kagome lattice

Key idea: Rydberg blockade on frustrated lattice results in highly degenerate states

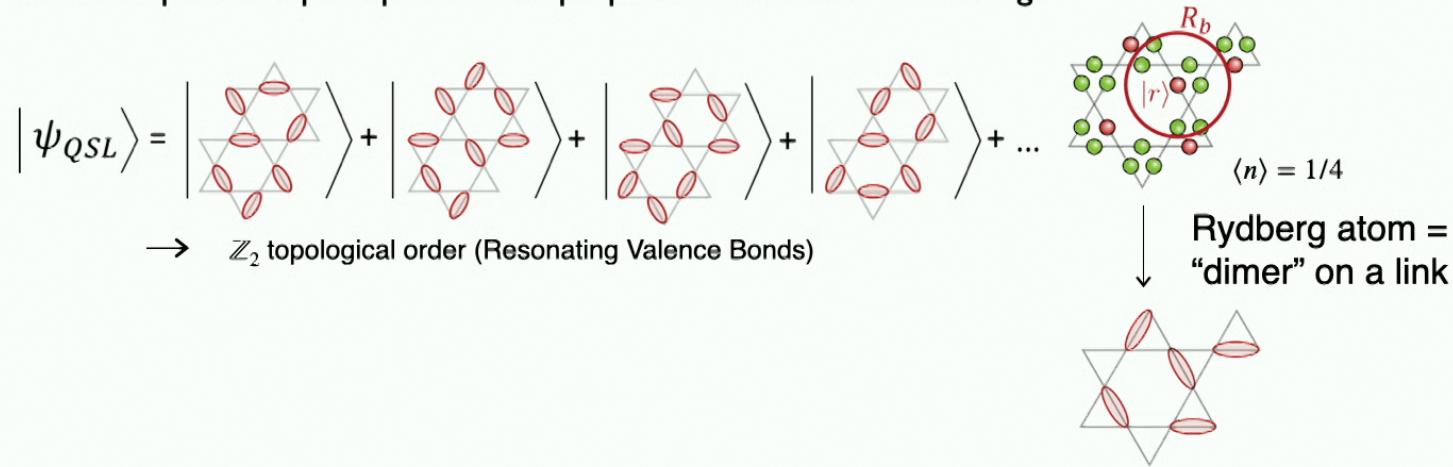


Theory: R. Samajdar, et al S. Sachdev's group arXiv:2011.12295, PNAS (2020)
R. Verresen, et al A. Vishwanath's group arXiv:2011.12310, PRX (2021)

Dimer model with Rydberg atoms on links of kagome lattice

Key idea: Rydberg blockade on frustrated lattice results in highly degenerate states

Predicted quantum spin liquid state: superposition of all dimer coverings



Theory: R. Samajdar, et al S. Sachdev's group arXiv:2011.12295, PNAS (2020)
R. Verresen, et al A. Vishwanath's group arXiv:2011.12310, PRX (2021)

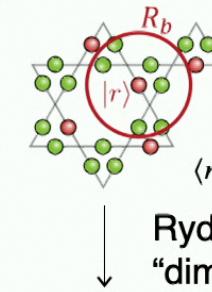
Dimer model with Rydberg atoms on links of kagome lattice

Key idea: Rydberg blockade on frustrated lattice results in highly degenerate states

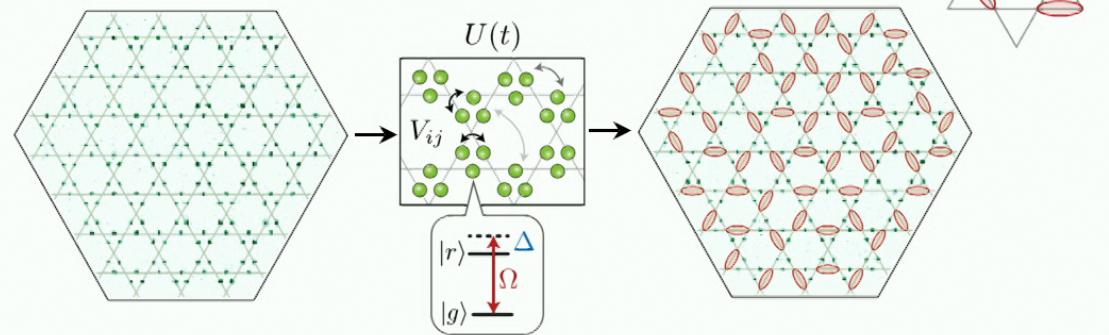
Predicted quantum spin liquid state: superposition of all dimer coverings

$$|\psi_{QSL}\rangle = \left| \text{dimer covering 1} \right\rangle + \left| \text{dimer covering 2} \right\rangle + \left| \text{dimer covering 3} \right\rangle + \left| \text{dimer covering 4} \right\rangle + \dots$$

$\rightarrow \mathbb{Z}_2$ topological order (Resonating Valence Bonds)

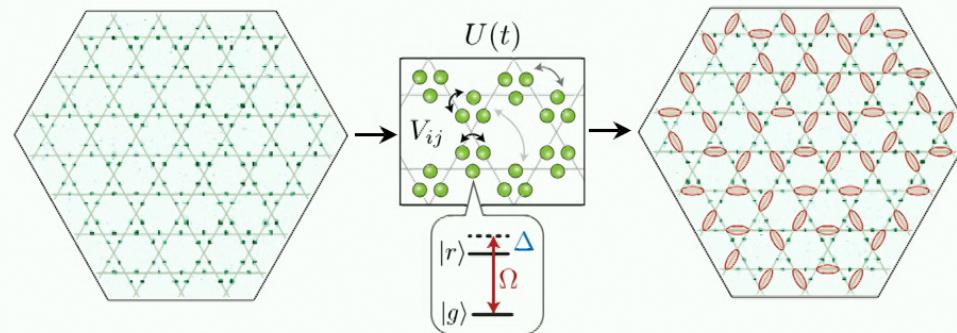
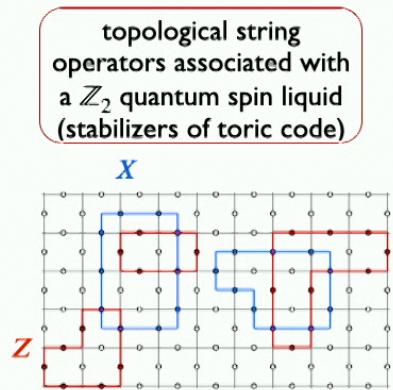


Experiment: 219 atoms



Theory: R. Samajdar, et al S. Sachdev's group arXiv:2011.12295, PNAS (2020)
R. Verresen, et al A. Vishwanath's group arXiv:2011.12310, PRX (2021)

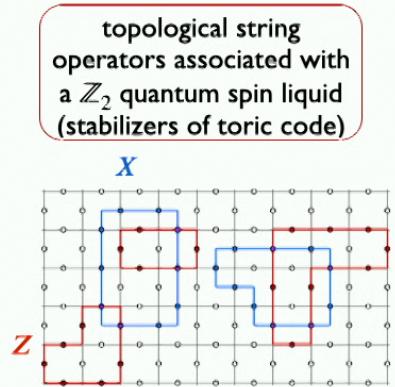
Topological string operators



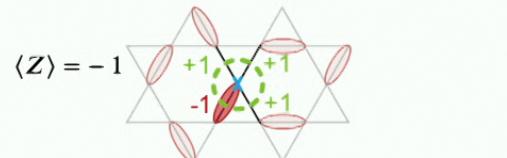
Theory R.Verresen, et al arXiv:2011.12310 (2020)

G. Semeghini et al, arXiv:2104.04119
Science (2021)

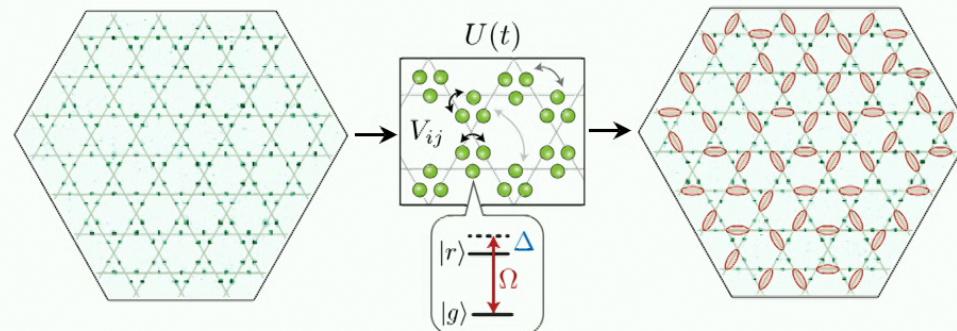
Topological string operators



diagonal string operator Z :



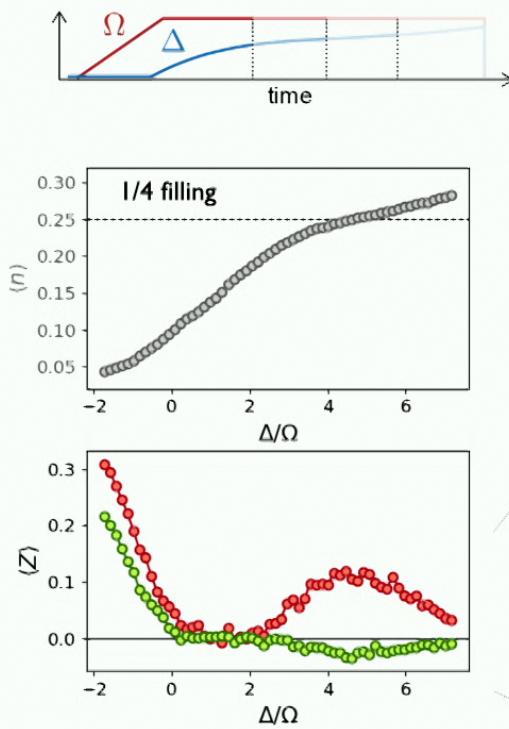
parity of dimers along a string
("Gauss law")



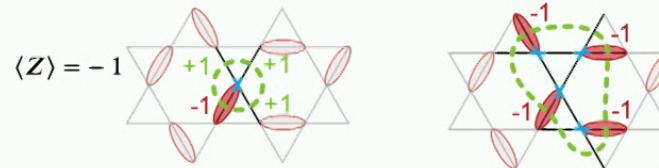
Theory R.Verresen, et al arXiv:2011.12310 (2020)

G. Semeghini et al, arXiv:2104.04119
Science (2021)

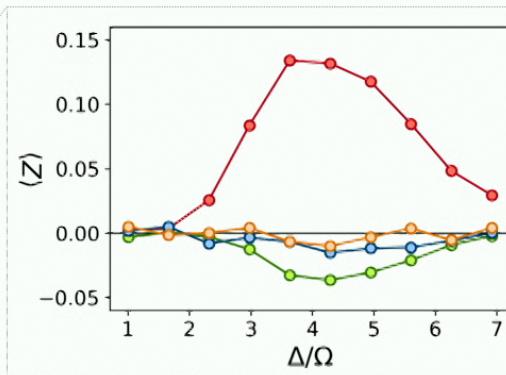
Topological string operators



diagonal string operator Z : $\langle Z \rangle = (-1)^{\# \text{enclosed vertices}}$



parity of dimers along a string
("Gauss law")



Theory R.Verresen, et al arXiv:2011.12310 (2020)

G. Semeghini et al, arXiv:2104.04119
Science (2021)

Probing coherence: off-diagonal string operator

off-diagonal string operator X :

$$\text{Diagram : } \left\{ \begin{array}{l} \text{triangle} \leftrightarrow (-1) \text{ red triangle} \\ \text{wavy line} \leftrightarrow \text{red wavy line} \end{array} \right.$$

Probing coherence: off-diagonal string operator

off-diagonal string operator X :

$$\text{Diagram : } \left\{ \begin{array}{l} \text{triangle with wavy line} \leftrightarrow (-1) \text{ triangle with red loop} \\ \text{triangle with red loop} \leftrightarrow \text{triangle with red loop} \end{array} \right. \quad \text{Diagram} = \left| \text{star with red loops} \right\rangle \langle \text{star with red loops} \right| + \left| \text{star with red loops} \right\rangle \langle \text{star with red loops} \right| + \left| \text{star with red loops} \right\rangle \langle \text{star with red loops} \right| + \dots$$

Probing coherence: off-diagonal string operator

off-diagonal string operator X :

$$\text{Diagram : } \left\{ \begin{array}{l} \text{triangle with wavy line} \leftrightarrow (-1) \text{ triangle with red loop} \\ \text{triangle with red loop} \leftrightarrow \text{triangle with red loop} \end{array} \right. \quad \text{Diagram} = \left| \text{star with red loops} \right\rangle \langle \text{star with red loops} | + \left| \text{star with red loops} \right\rangle \langle \text{star with red loops} | + \left| \text{star with red loops} \right\rangle \langle \text{star with red loops} | + \dots$$

Qubit analogy: measure $\sigma_x = |0\rangle\langle 1| + |1\rangle\langle 0|$

$$\langle \psi | \sigma_x | \psi \rangle = \langle \psi | 0 \rangle \langle 1 | \psi \rangle + h.c \quad \text{measures coherence between } |0\rangle \text{ and } |1\rangle$$

Probing coherence: off-diagonal string operator

off-diagonal string operator X :

$$\text{Diagram of } X : \left\{ \begin{array}{l} \text{triangle} \leftrightarrow (-1) \text{ triangle} \\ \text{triangle} \leftrightarrow \text{triangle} \end{array} \right. \quad \text{Diagram of } X = \left| \text{star} \right\rangle \langle \text{star} | + \left| \text{star} \right\rangle \langle \text{star} | + \left| \text{star} \right\rangle \langle \text{star} | + \dots$$

rotation to measure X : operation on 3-atom states transforms X string into “dual” Z string

$$X = U_q^\dagger(\tau) \text{ (3 atoms)} \xrightarrow{\text{Z}} U_q(\tau) \text{ (3 atoms)}$$

Theory R.Verresen, et al arXiv:2011.12310 (2020)
Experiment G. Semeghini et al, arXiv:2104.04119, Science (2021)

Probing coherence: off-diagonal string operator

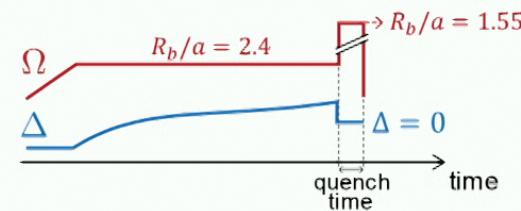
off-diagonal string operator X :

$$\text{Diagram : } \left\{ \begin{array}{l} \triangle \leftrightarrow (-1) \triangle \\ \triangle \leftrightarrow \triangle \end{array} \right. \quad \text{Diagram} = \left| \text{Diagram} \right\rangle \langle \text{Diagram} | + \left| \text{Diagram} \right\rangle \langle \text{Diagram} | + \left| \text{Diagram} \right\rangle \langle \text{Diagram} | + \dots$$

rotation to measure X : operation on 3-atom states transforms X string into “dual” Z string

$$X = U_q^\dagger(\tau) Z U_q(\tau)$$

The diagram shows three boxes. The first box contains a triangle with a wavy line and is labeled X . The second box contains a triangle with a dashed line and is labeled Z . The third box contains a triangle with a wavy line and is labeled $U_q^\dagger(\tau)$ above and $U_q(\tau)$ below. Arrows point from the first box to the second, and from the second to the third.



Theory R.Verresen, et al arXiv:2011.12310 (2020)
Experiment G. Semeghini et al, arXiv:2104.04119, Science (2021)

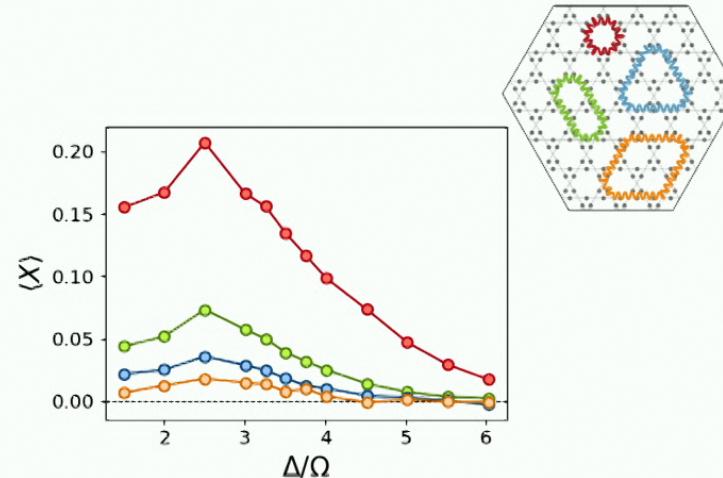
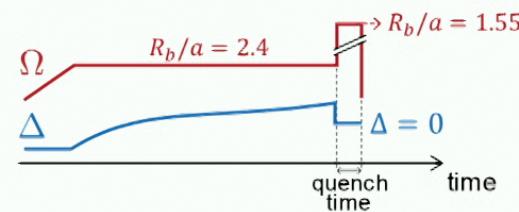
Probing coherence: off-diagonal string operator

off-diagonal string operator X :

$$\text{Diagram of } X \text{ operator} : \left\{ \begin{array}{l} \text{triangle with wavy line} \leftrightarrow (-1) \text{ triangle with wavy line} \\ \text{triangle with dashed line} \leftrightarrow \text{triangle with dashed line} \end{array} \right. \quad \text{Diagram of } X \text{ operator} = \left| \text{hexagon with red loops} \right\rangle \langle \left| \text{hexagon with red loops} \right\rangle + \left| \text{hexagon with red loops} \right\rangle \langle \left| \text{hexagon with red loops} \right\rangle + \left| \text{hexagon with red loops} \right\rangle \langle \left| \text{hexagon with red loops} \right\rangle + \dots$$

rotation to measure X : operation on 3-atom states transforms X string into “dual” Z string

$$X = U_q^\dagger(\tau) Z U_q(\tau)$$



Theory R.Verresen, et al arXiv:2011.12310 (2020)
Experiment G. Semeghini et al, arXiv:2104.04119, Science (2021)

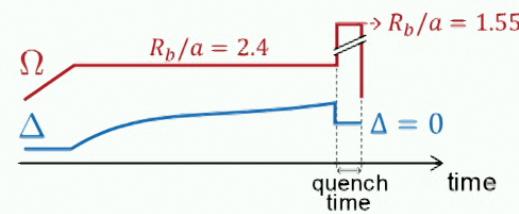
Probing coherence: off-diagonal string operator

off-diagonal string operator X :

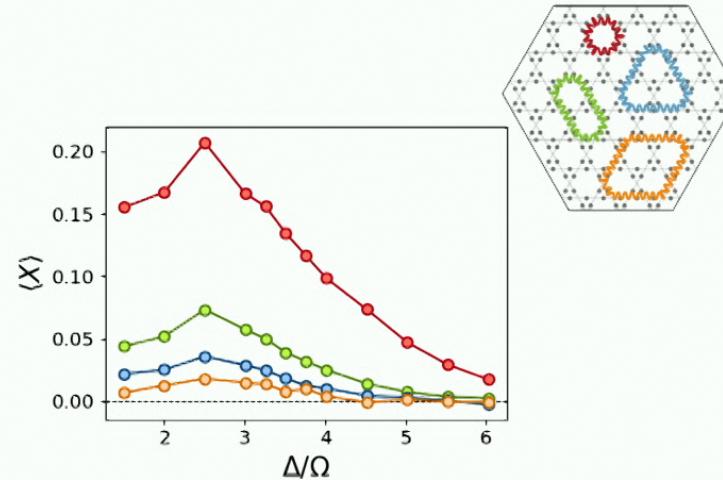
$$\text{Diagram : } \left\{ \begin{array}{l} \triangle \leftrightarrow (-1) \bar{\triangle} \\ \bar{\triangle} \leftrightarrow \triangle \end{array} \right. \quad \text{Diagram} = \left| \text{Star} \right\rangle \langle \text{Star} | + \left| \text{Star} \right\rangle \langle \text{Star} | + \left| \text{Star} \right\rangle \langle \text{Star} | + \dots$$

rotation to measure X : operation on 3-atom states transforms X string into “dual” Z string

$$X = U_q^\dagger(\tau) Z U_q(\tau)$$



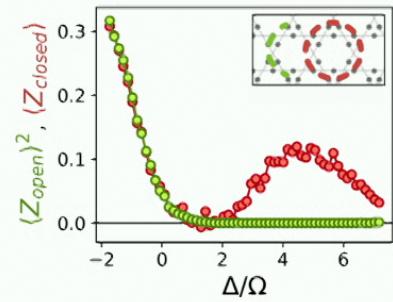
Theory R.Verresen, et al arXiv:2011.12310 (2020)
Experiment G. Semeghini et al, arXiv:2104.04119, Science (2021)



Signature of **coherence** between dimer coverings!

Topological properties of QSL phase

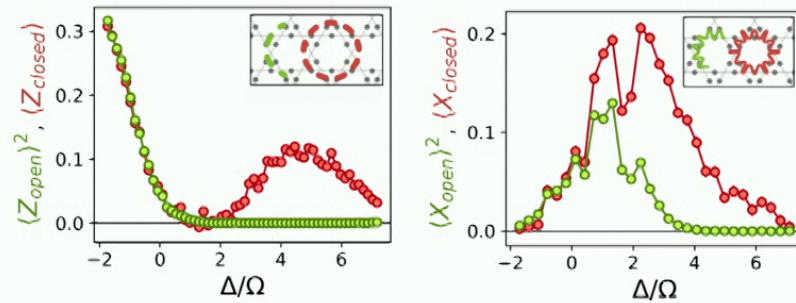
closed loops vs open strings



G. Semeghini et al, arXiv:2104.04119, Science (2021)

Topological properties of QSL phase

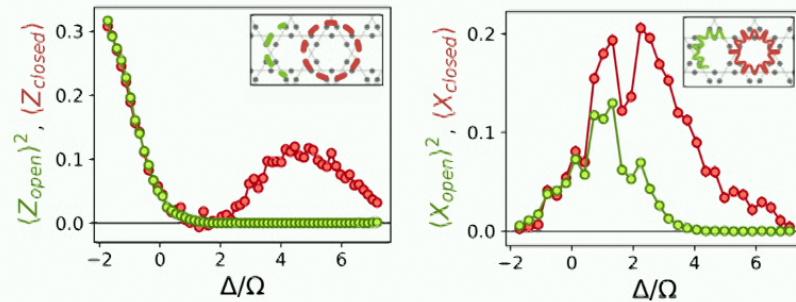
closed loops vs open strings



G. Semeghini et al, arXiv:2104.04119, Science (2021)

Topological properties of QSL phase

closed loops vs open strings



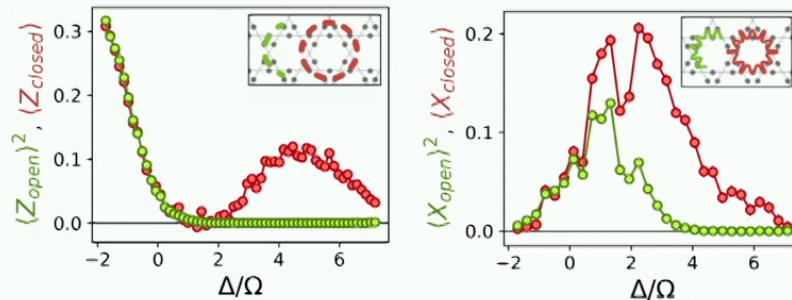
closed loops: detect non-trivial topological correlations

open strings: distinguish QSL from nearby phases

G. Semeghini et al, arXiv:2104.04119, Science (2021)

Topological properties of QSL phase

closed loops vs open strings



closed loops: detect non-trivial topological correlations

open strings: distinguish QSL from nearby phases

BFFM string order parameters:

$$\langle Z \rangle_{BFFM} = \left\langle \frac{\langle Z_{\text{closed}} \rangle}{\sqrt{\langle Z_{\text{closed}} \rangle}} \right\rangle$$

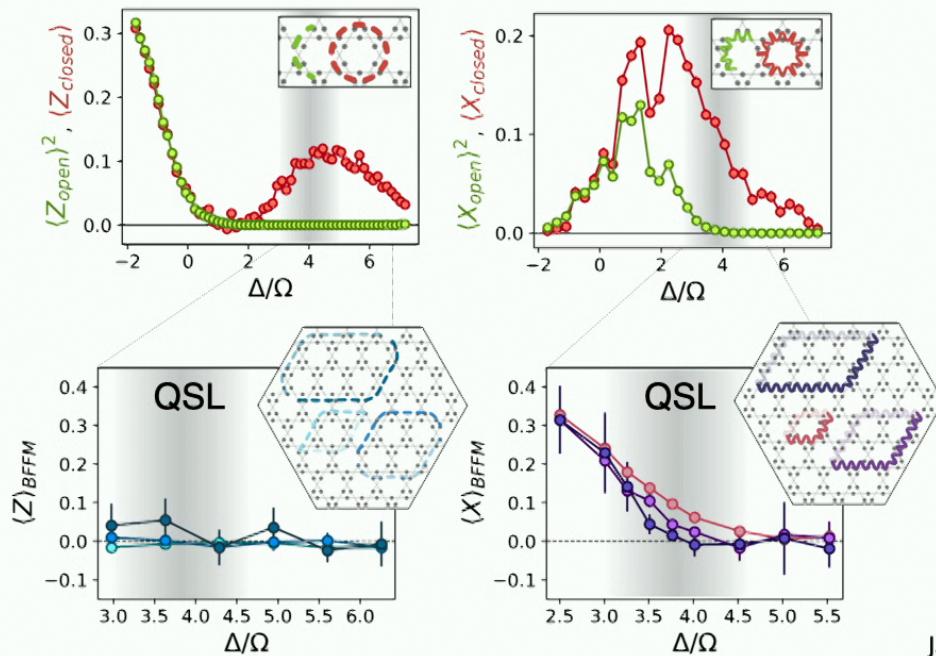
$$\langle X \rangle_{BFFM} = \left\langle \frac{\langle X_{\text{open}} \rangle}{\sqrt{\langle X_{\text{open}} \rangle}} \right\rangle$$

J. Bricmont and J. Frölich, Physics Letters B 122 (1983)
K. Fredenhagen and M. Marcu, Comm. Math. Phys. 92 (1983)

G. Semeghini et al, arXiv:2104.04119, Science (2021)

Topological properties of QSL phase

closed loops vs open strings



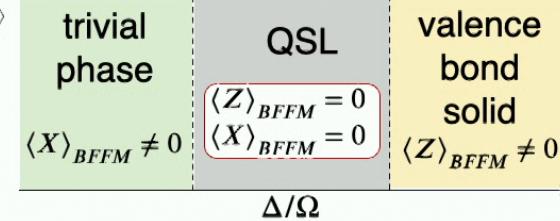
closed loops: detect non-trivial topological correlations

open strings: distinguish QSL from nearby phases

BFFM string order parameters:

$$\langle Z \rangle_{BFFM} = \left\langle \text{Diagram A} \right\rangle / \sqrt{\left\langle \text{Diagram B} \right\rangle}$$

$$\langle X \rangle_{BFFM} = \left\langle \text{Diagram C} \right\rangle / \sqrt{\left\langle \text{Diagram D} \right\rangle}$$



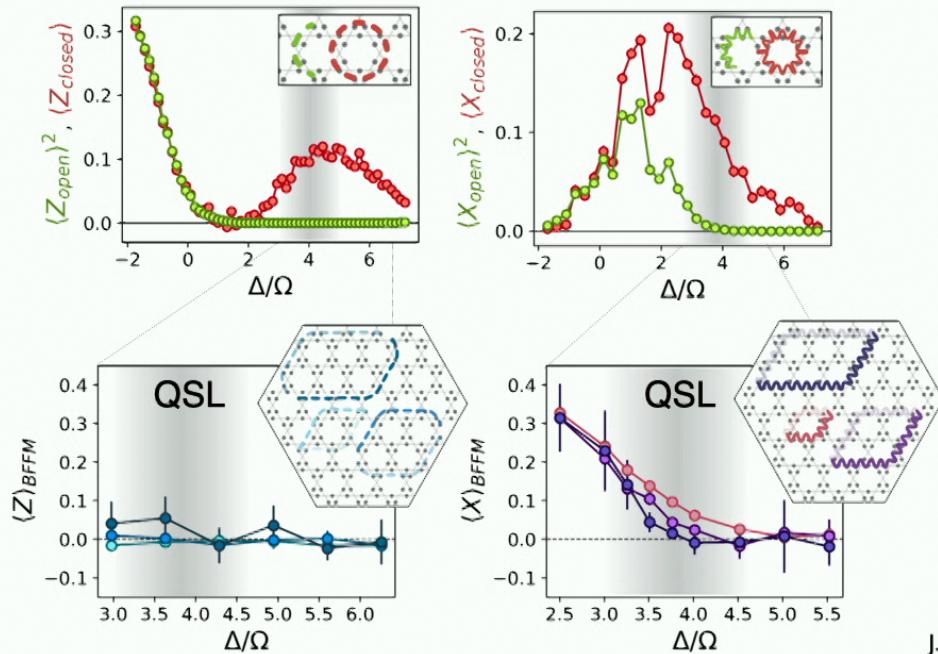
J. Bricmont and J. Frölich, Physics Letters B 122 (1983)

K. Fredenhagen and M. Marcu, Comm. Math. Phys. 92 (1983)

G. Semeghini et al, arXiv:2104.04119, Science (2021)

Topological properties of QSL phase

closed loops vs open strings



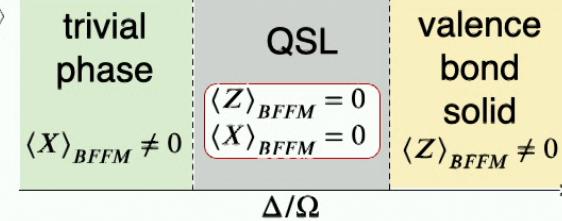
closed loops: detect non-trivial topological correlations

open strings: distinguish QSL from nearby phases

BFFM string order parameters:

$$\langle Z \rangle_{BFFM} = \left\langle \frac{\text{red circles}}{\text{green circles}} \right\rangle / \sqrt{\left\langle \frac{\text{red circles}}{\text{green circles}} \right\rangle}$$

$$\langle X \rangle_{BFFM} = \left\langle \frac{\text{purple wavy lines}}{\text{blue dashed lines}} \right\rangle / \sqrt{\left\langle \frac{\text{purple wavy lines}}{\text{blue dashed lines}} \right\rangle}$$



J. Bricmont and J. Frölich, Physics Letters B 122 (1983)

K. Fredenhagen and M. Marcu, Comm. Math. Phys. 92 (1983)

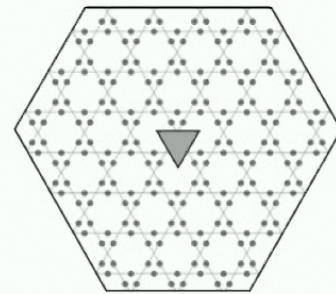
Onset of a quantum spin liquid phase!

G. Semeghini et al, arXiv:2104.04119, Science (2021)

Towards a topological qubit

non-trivial topology:

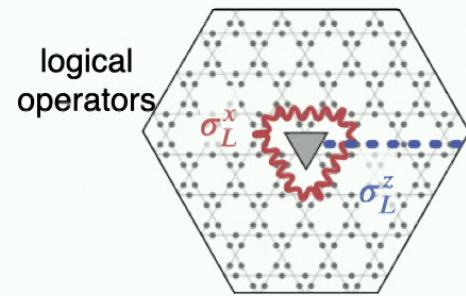
array with a hole



Towards a topological qubit

non-trivial topology:

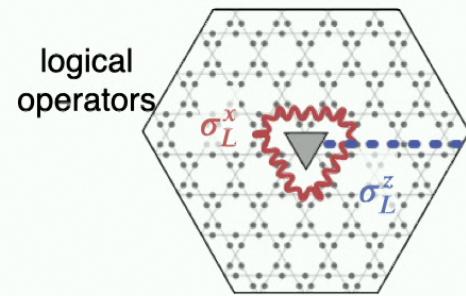
array with a hole



Towards a topological qubit

non-trivial topology:

array with a hole



Two-fold degenerate ground state:

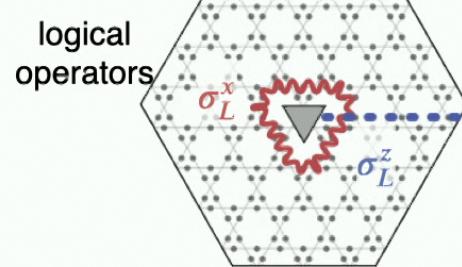
$$|\psi_+\rangle \sim |0_L\rangle + |1_L\rangle$$

$$|\psi_-\rangle \sim |0_L\rangle - |1_L\rangle$$

Towards a topological qubit

non-trivial topology:

array with a hole



Two-fold degenerate ground state:

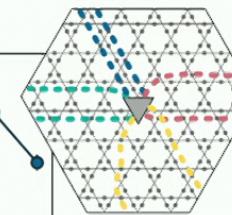
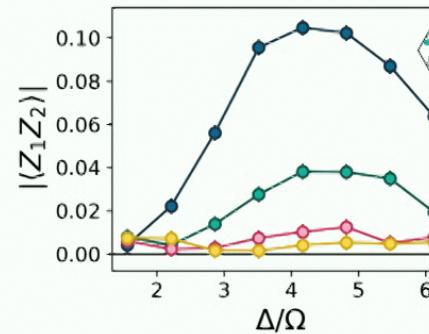
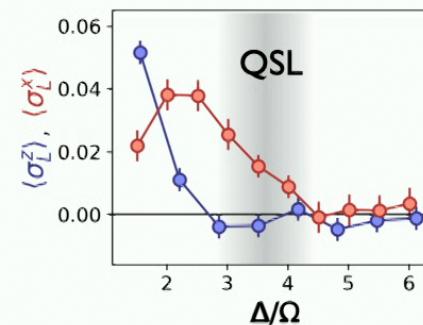
$$|\psi_+\rangle \sim |0_L\rangle + |1_L\rangle \quad \langle\sigma_L^x\rangle = +1$$

$$|\psi_-\rangle \sim |0_L\rangle - |1_L\rangle \quad \langle\sigma_L^x\rangle = -1$$

$$\langle\sigma_L^z\rangle = 0 \quad \langle\sigma_L^z \sigma_L^z\rangle = 1$$

Expected in adiabatic state preparation

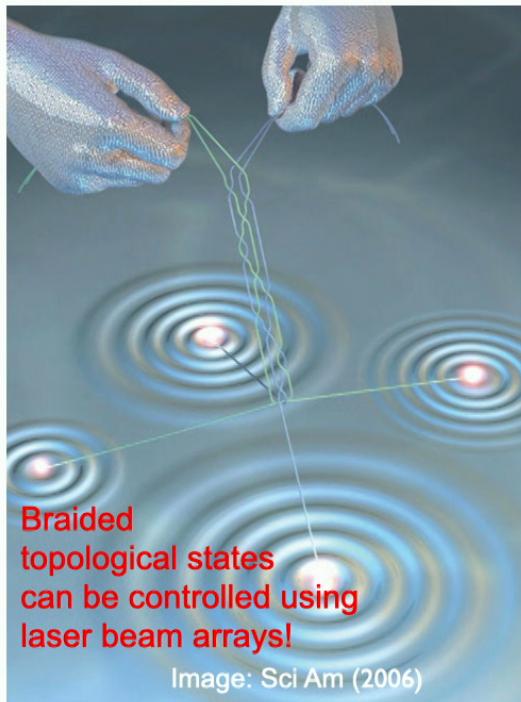
Experimental results



First steps towards topological qubits!

G. Semeghini et al, arXiv:2104.04119, Science (2021), related work by Google Quantum AI: K. J. Satzinger et al., arXiv:2104.01180 (2021)

Probing topological matter: new opportunities

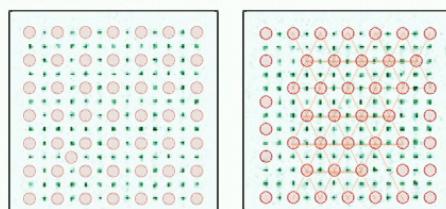


- Unprecedented insights into topological matter
- New tools complementary to analytical theories & numerical simulations
- New methods to analyze, inspired by QEC
- Simulating Lattice Gauge Theories
- Insights for engineering topological 2D materials
- Platforms for exploring fault tolerant quantum information processing

Giulia Semeghini et al, arXiv:2104.04119, Science (2021)
see also work by Google group arXiv:2104.01180

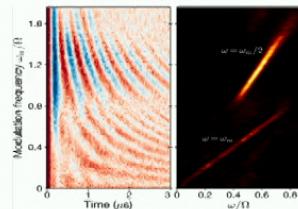
Programmable quantum simulators based on Rydberg arrays: recent progress

Exploring 2D phase diagrams



S. Ebadi et al arxiv 2012.12281, Nature (2021)

Non-equilibrium dynamics

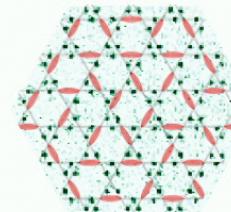


D. Bluvstein, et al, arxiv 2012.12276, Science (2021)

IQuEra™



Probing topological spin liquids



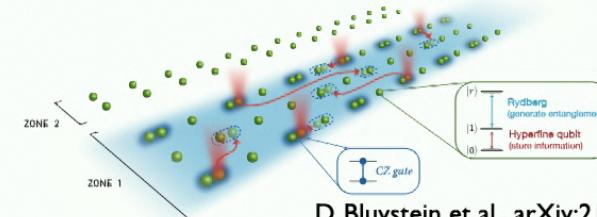
G. Semeghini et al, arXiv:2104.04119, Science (2021)

Accelerating combinatorial optimization



S. Ebadi et al, arXiv 2202.09372
Science (2022)

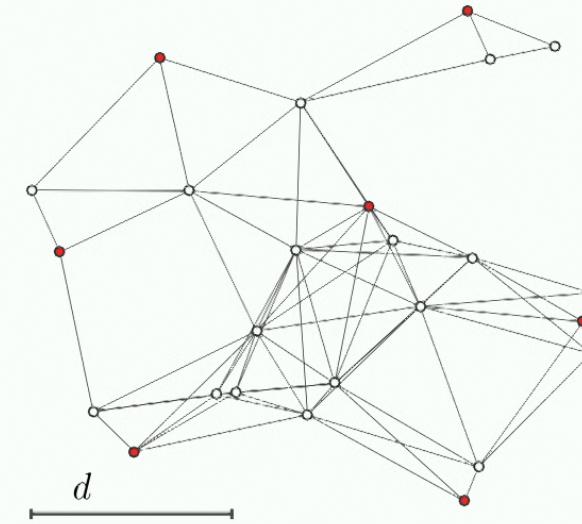
Entanglement transport & universal programmability



D. Bluvstein et al, arXiv:2112.03923

Quantum Optimization of Maximum Independent Set

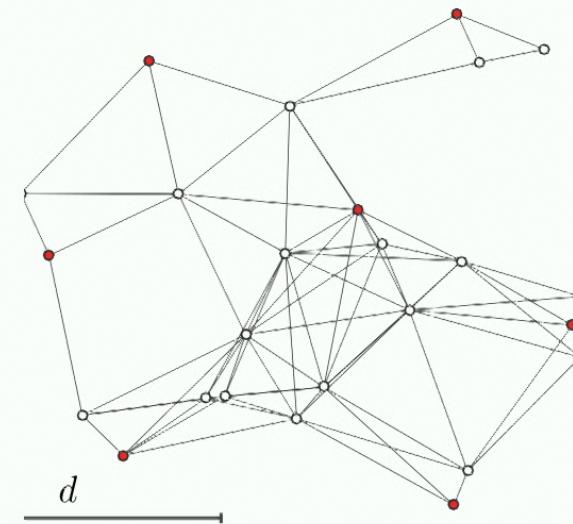
- We are given a undirected graph $G=(V,E)$ with vertices V and edges E
- Independent set S is a subset of V such that no elements of S are neighboring on G
- The MIS problem consists in finding the largest independent set
- **Example:** MIS on unit disk graph - vertices connected if they are within a given distance



24

Quantum Optimization of Maximum Independent Set

- We are given a undirected graph $G=(V,E)$ with vertices V and edges E
- Independent set S is a subset of V such that no elements of S are neighboring on G
- The MIS problem consists in finding the largest independent set
- **Example:** MIS on unit disk graph - vertices connected if they are within a given distance
 - Many real world applications, e.g. design of networks, machine learning
 - Example of NP-complete problem
 - Cost function => Rydberg blockade Hamiltonian



H. Pichler, S. Wang, L. Zhou et al, arXiv:1808.10816, PRX (2020); D. Wild et al arXiv:2005.14059

25

Quantum Optimization of Maximum Independent Set

- We are given a undirected graph $G=(V,E)$ with vertices V and edges E
- Independent set S is a subset of V such that no elements of S are neighboring on G
- The MIS problem consists in finding the largest independent set
- **Example:** MIS on unit disk graph - vertices connected if they are within a given distance
 - Many real world applications, e.g. design of networks, machine learning
 - Example of NP-complete problem
 - Cost function => D'yubkova blockade Hamiltonian

$$H = \sum_{v \in V} -\Delta n$$

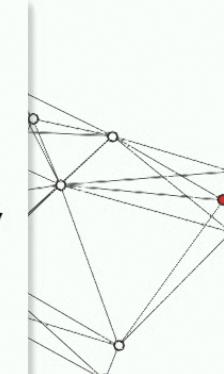
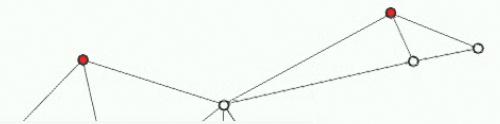
$$U_{u,w} > \Delta >$$

Prior work/ideas:
Adiabatic evolution, annealing (D-Wave)
Approximate Quantum Optimization

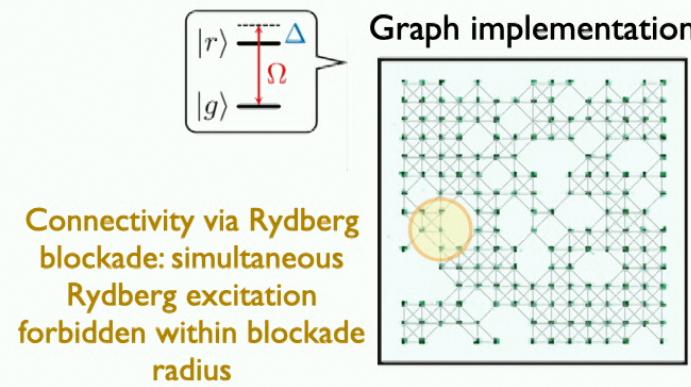
E. Farhi, A. Harrow et al, C. Laumann et al, recent work by M. Hastings, S. Bravyi focused on "shallow circuits", several experiments

Our approach: beyond shallow circuits,
efficient implementation via co-design

H. Pichler, S. Wang, L. Zhou et al, arXiv:1808.10816, PRX (2020); D. Wild et al arXiv:2005.14059

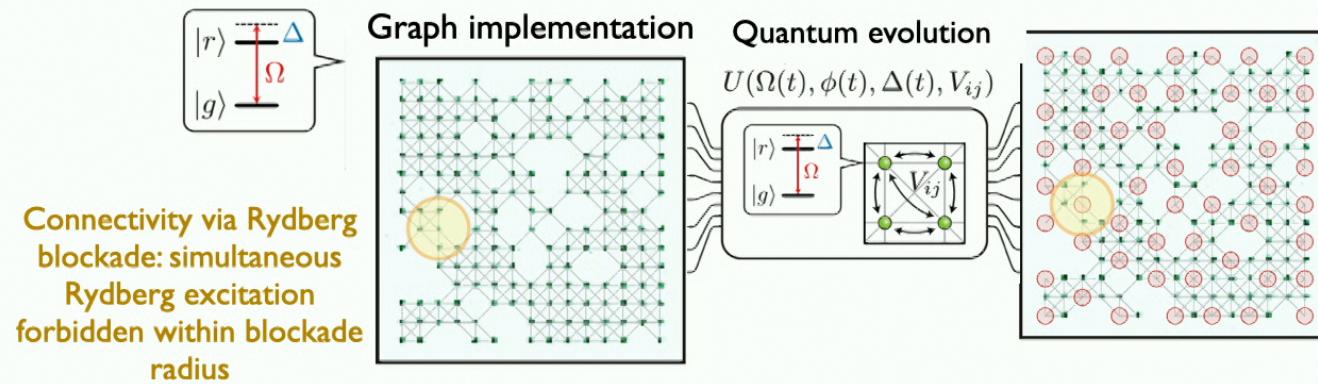


Hardware-efficient encoding MIS on unit disk graphs via Rydberg blockade



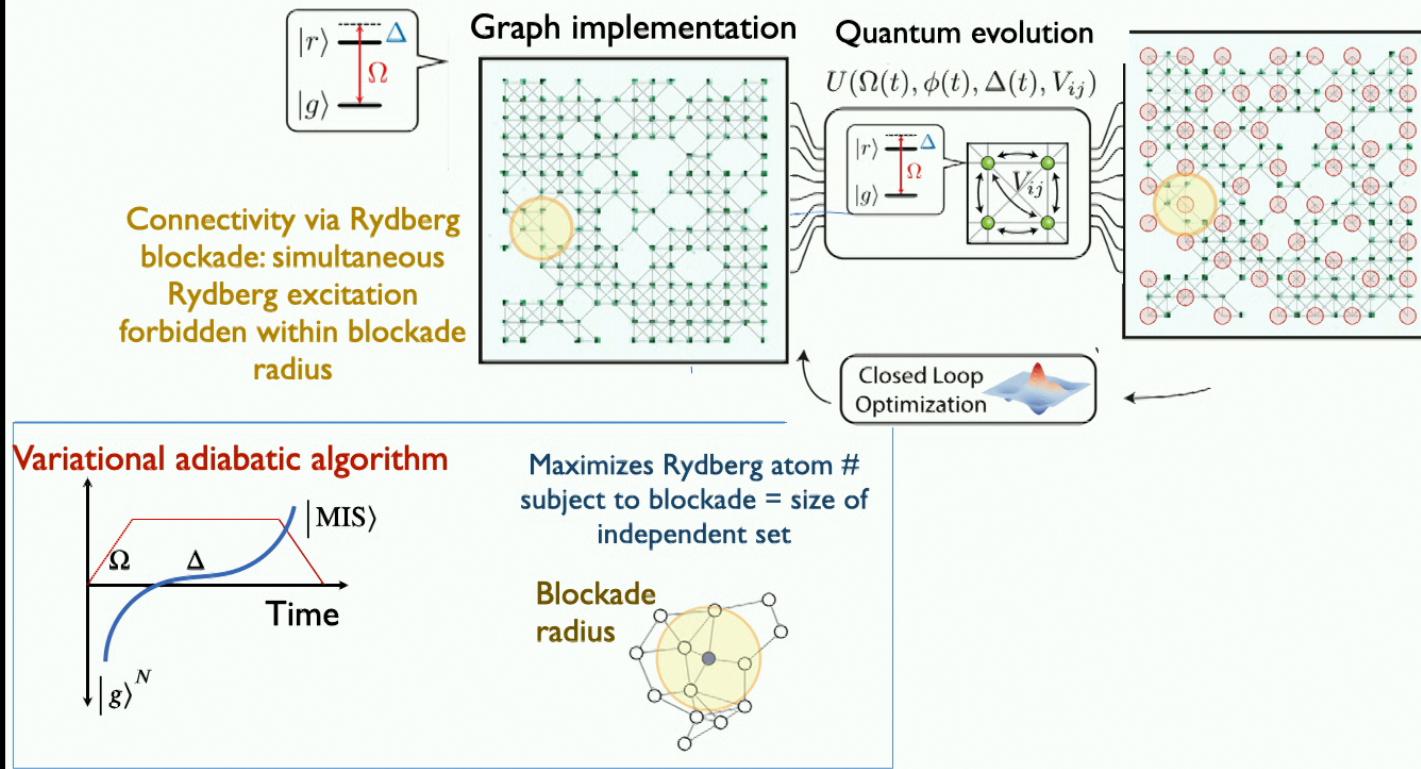
Idea H. Pichler, S. Wang, L. Zhou et al, arXiv:1808.10816, PRX (2020)

Hardware-efficient encoding MIS on unit disk graphs via Rydberg blockade



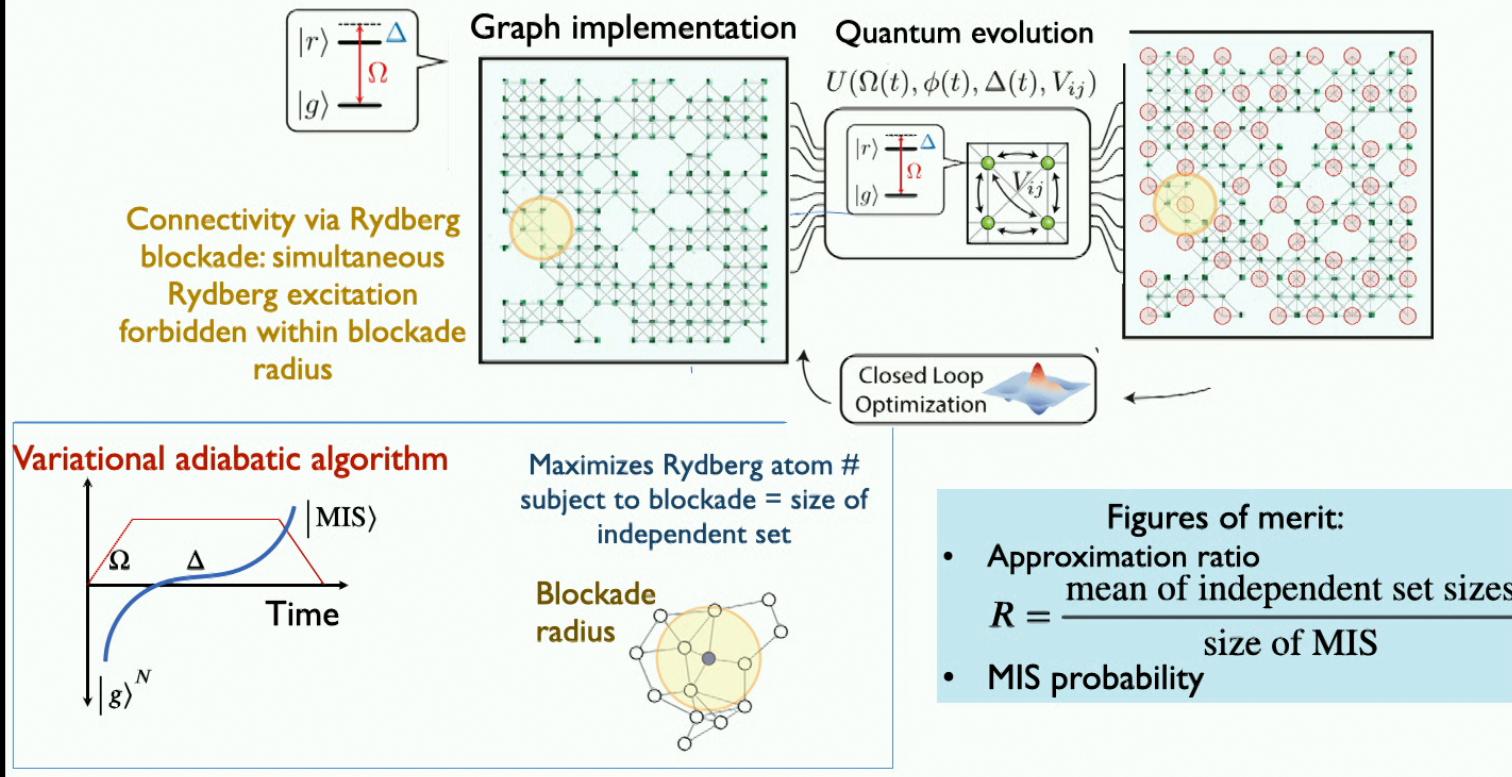
Idea H. Pichler, S. Wang, L. Zhou et al, arXiv:1808.10816, PRX (2020)

Hardware-efficient encoding MIS on unit disk graphs via Rydberg blockade



Idea H. Pichler, S. Wang, L. Zhou et al, arXiv:1808.10816, PRX (2020)

Hardware-efficient encoding MIS on unit disk graphs via Rydberg blockade

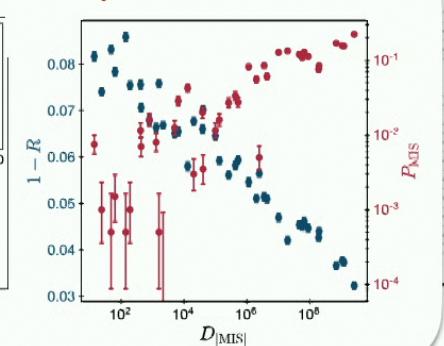
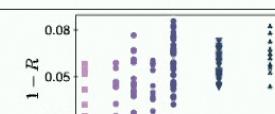
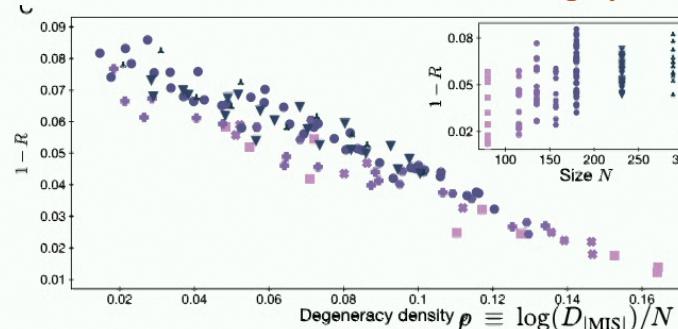


Hardware-efficient encoding MIS on unit disk graphs via Rydberg blockade

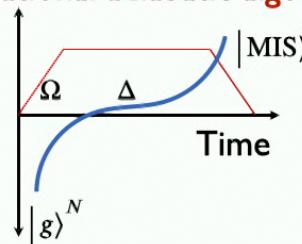


Results across hundreds of graphs 69-289 qubits

Con
block
R
forbid



Variational adiabatic algorithm



Maximizes Rydberg atom #
subject to blockade = size of
independent set



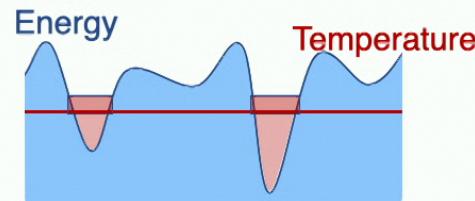
Figures of merit:

- Approximation ratio
 $R = \frac{\text{mean of independent set sizes}}{\text{size of MIS}}$
- MIS probability

Idea H. Pichler, S. Wang, L. Zhou et al, arXiv:1808.10816, PRX (2020)

Benchmarking against simulated annealing

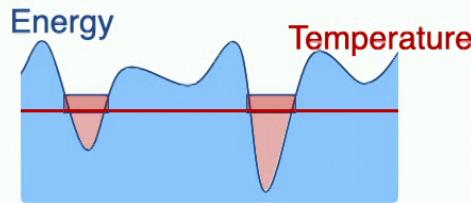
Simulated annealing (SA): classically cool
to Hamiltonian ground state by
stochastically flipping spins



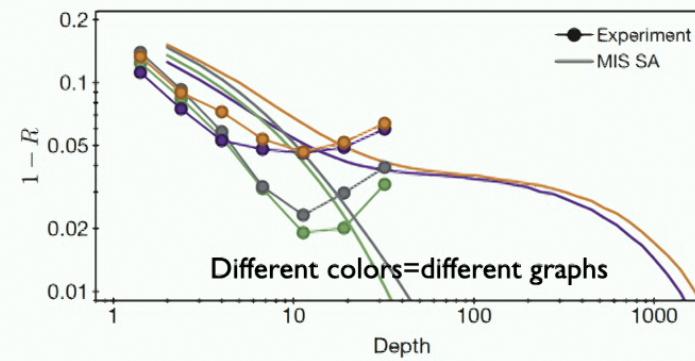
S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Benchmarking against simulated annealing

Simulated annealing (SA): classically cool to Hamiltonian ground state by stochastically flipping spins



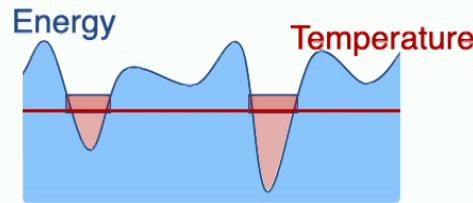
This work: optimized SA with collective updates



S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Benchmarking against simulated annealing

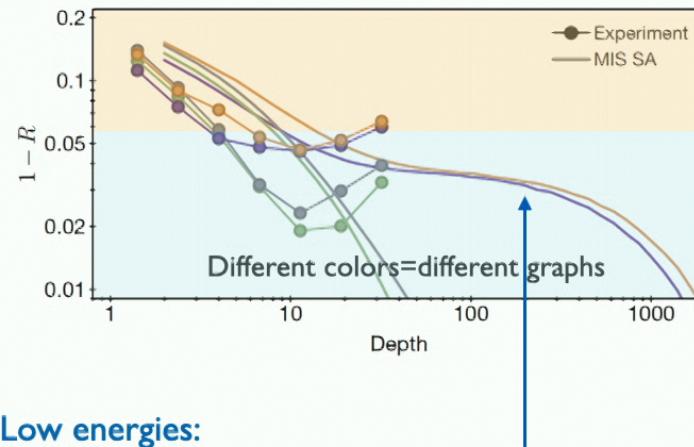
Simulated annealing (SA): classically cool to Hamiltonian ground state by stochastically flipping spins



This work: optimized SA with collective updates

Two regimes emerge

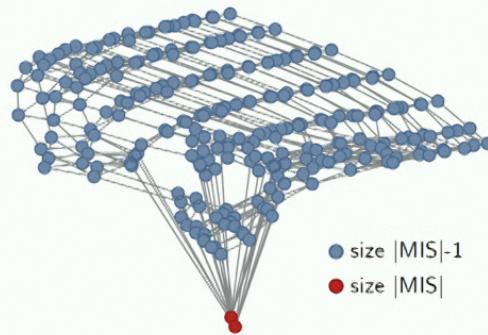
High energies:
comparable depth to fixed approximation ratio



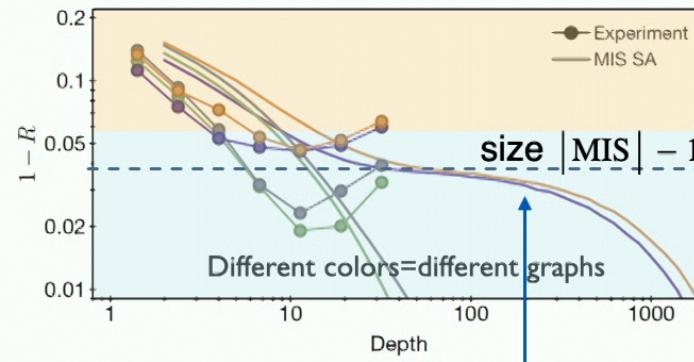
S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Simulated annealing trapped in local minima

SA randomly walks (**edges**) between solution configurations (**nodes**) until it finds an MIS



High energies:
comparable depth to fixed approximation ratio

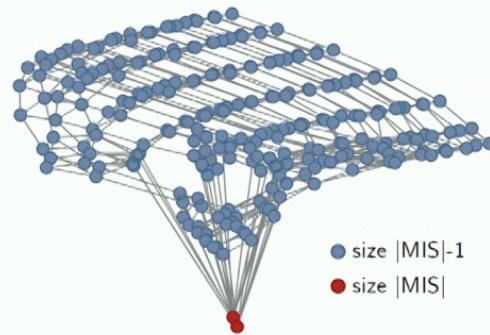


Low energies:
SA trapped in local minima on some instances

S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Simulated annealing trapped in local minima

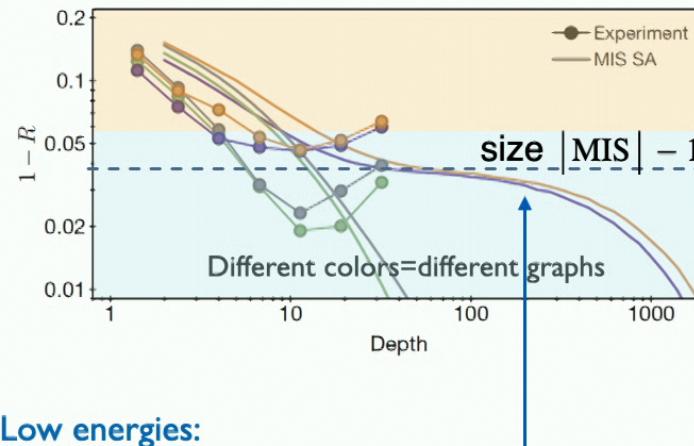
SA randomly walks (**edges**) between solution configurations (**nodes**) until it finds an MIS



Fundamental limit to SA (provable)

$$\text{Hardness parameter } \mathcal{H}^P = \frac{\text{Number of } |\text{MIS}|-1}{\text{Number of edges leading into MIS}}$$

High energies:
comparable depth to fixed approximation ratio

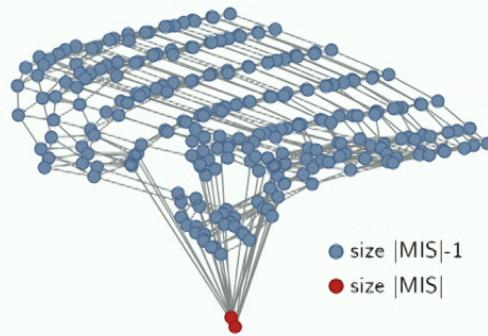


Low energies:
SA trapped in local minima on some instances

S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Simulated annealing trapped in local minima

SA randomly walks (**edges**) between solution configurations (**nodes**) until it finds an MIS

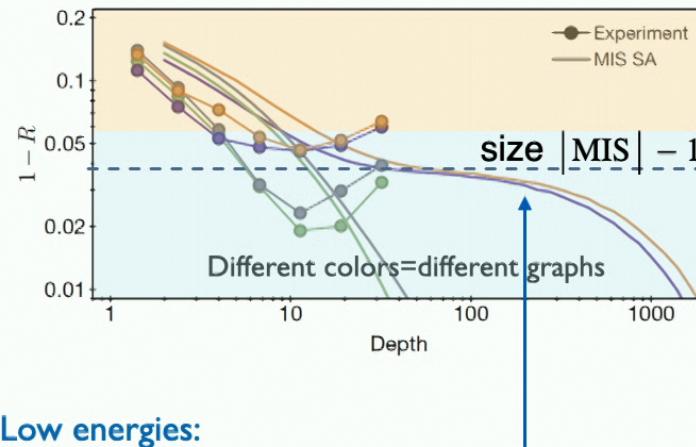


Fundamental limit to SA (provable)

$$\text{Hardness parameter } \mathcal{H}^P = \frac{\text{Number of } |\text{MIS}|-1}{\text{Number of edges leading into MIS}}$$

Exponential runtime in $(\text{system size})^{1/2}$
(numerical evidence, worst case)

High energies:
comparable depth to fixed approximation ratio



Low energies:
SA trapped in local minima on some instances

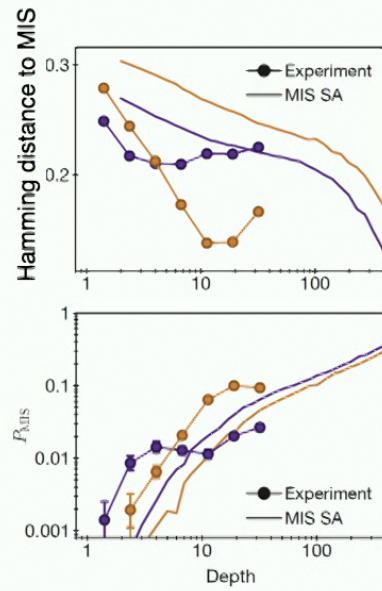
S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Performance comparison on hardest instances

How does performance scale with \mathcal{H}^D ?

Example: top 2% hardest graphs

Instances with similar classical hardness



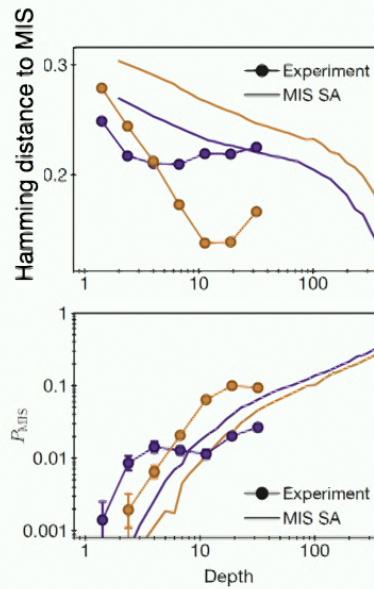
S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Performance comparison on hardest instances

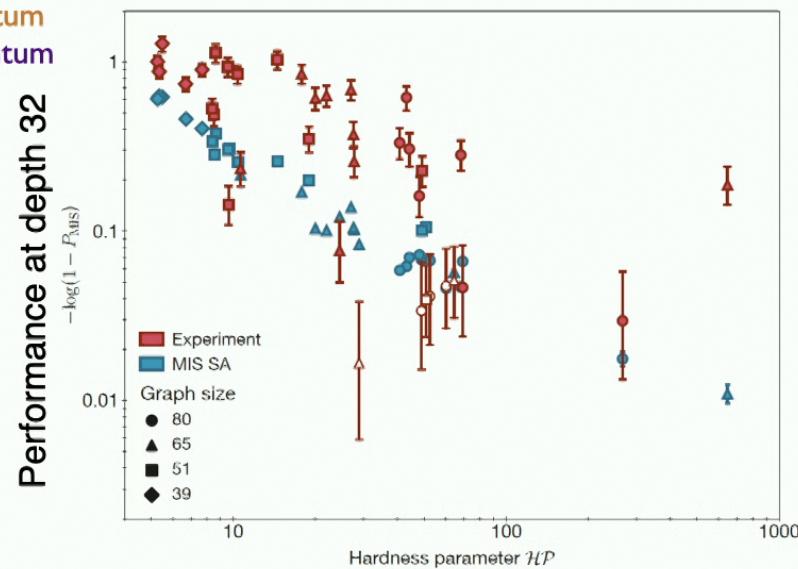
How does performance scale with $\mathcal{H}\mathcal{P}$?

Example: top 2% hardest graphs

Instances with similar classical hardness



Easy graph for quantum
Hard graph for quantum



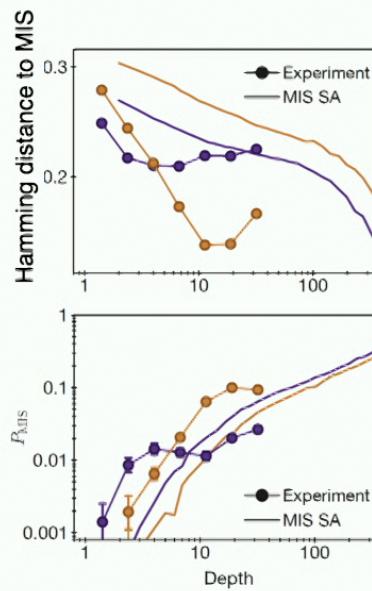
S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Performance comparison on hardest instances

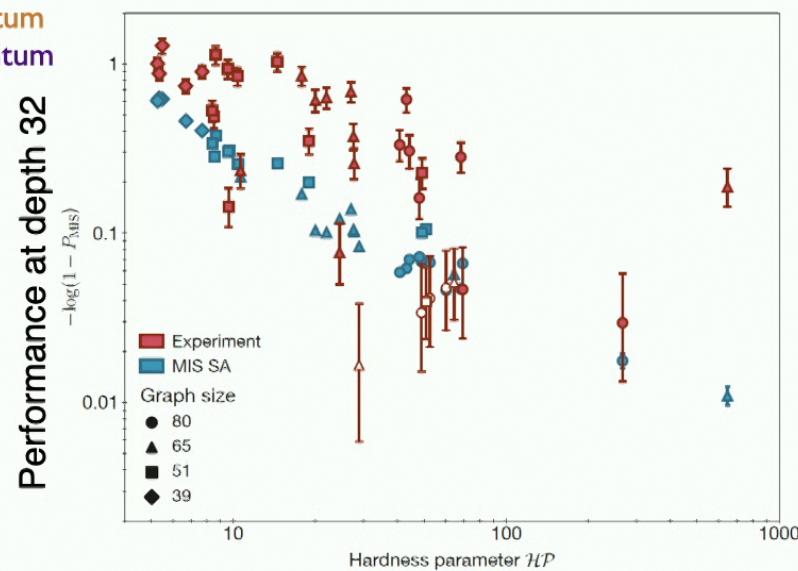
How does performance scale with $\mathcal{H}P$?

Example: top 2% hardest graphs

Instances with similar classical hardness



Easy graph for quantum
Hard graph for quantum



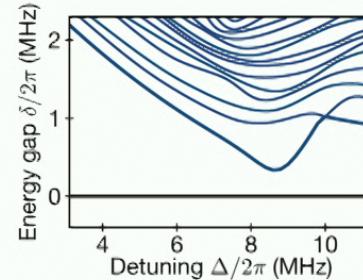
Quantum algorithm is faster on many (but not all) instances:
what controls quantum hardness?

S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022), collaboration with B. Barak, E. Farhi

Quantum hardness controlled by minimum energy gap

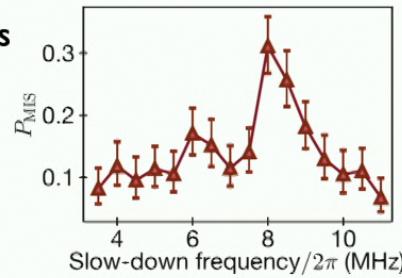
Adiabaticity is limited by the minimum energy gap

Example : 65 node graph



Experiment is sensitive to many-body gap

MIS probability increases
when detuning sweep
slowed at gap minimum

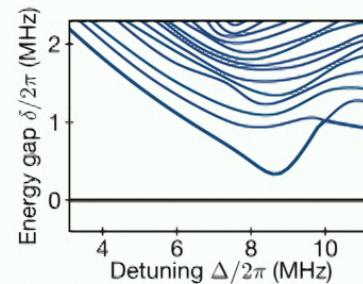


S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022)

Quantum hardness controlled by minimum energy gap

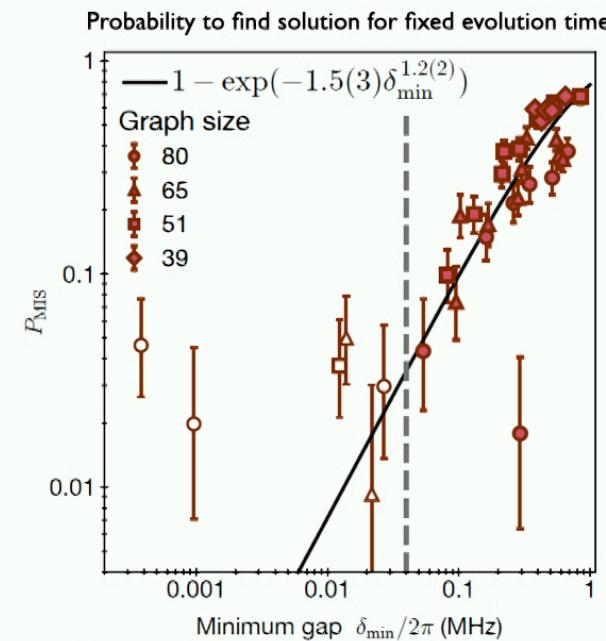
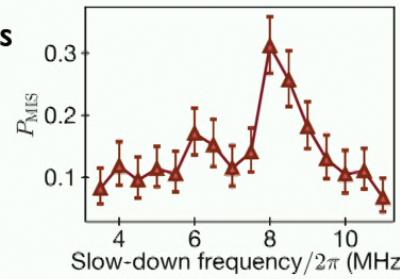
Adiabaticity is limited by the minimum energy gap

Example : 65 node graph



Experiment is sensitive to many-body gap

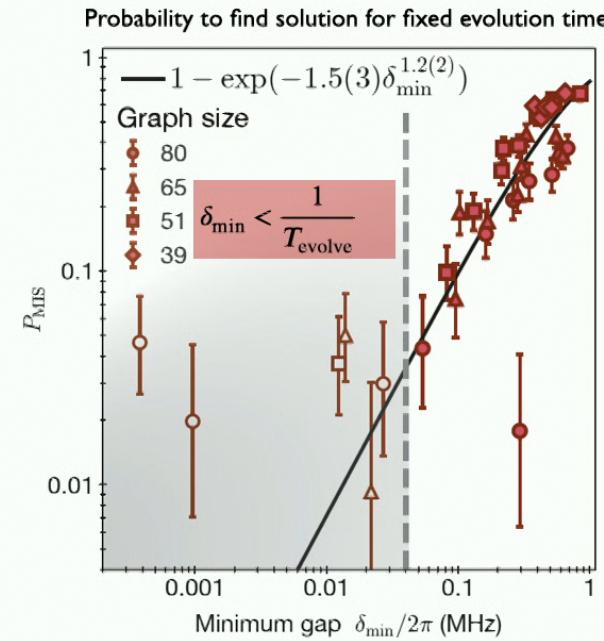
MIS probability increases when detuning sweep slowed at gap minimum



S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022)

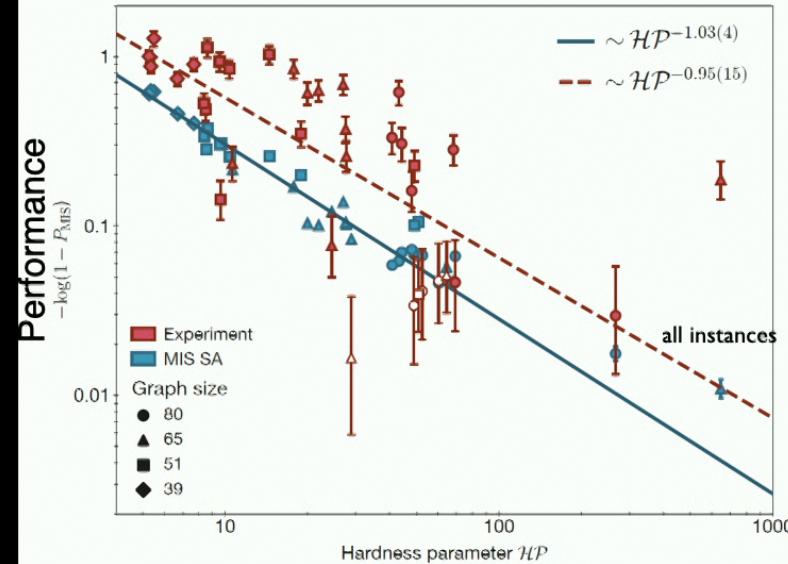
Quantum speedup in deep circuit regime

Hardness controlled by adiabatic gap:
Landau-Zener scaling

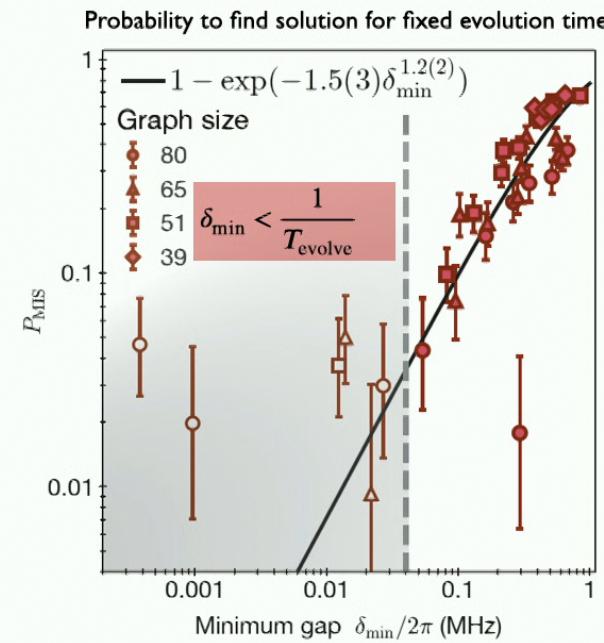


S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022)

Quantum speedup in deep circuit regime

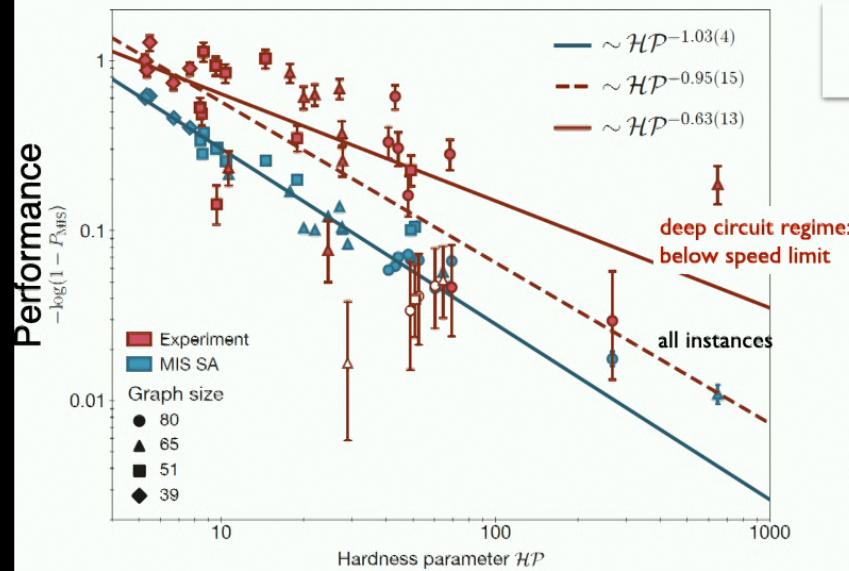


Hardness controlled by adiabatic gap:
Landau-Zener scaling



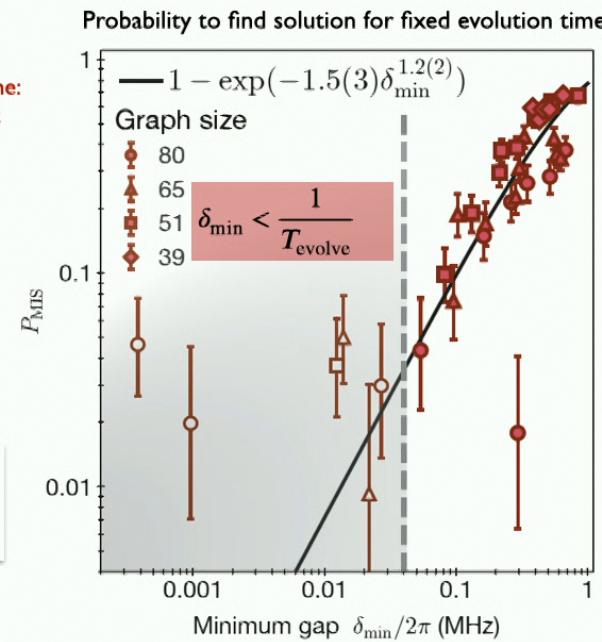
S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022)

Quantum speedup in deep circuit regime



Superlinear (nearly quadratic)
speedup in deep circuit regime!

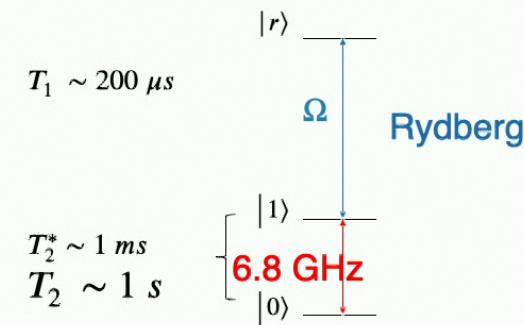
Hardness controlled by adiabatic gap:
Landau-Zener scaling



S. Ebadi, A. Keesling, M. Cain et al, arXiv 2202.09372
Science (2022)

Outlook: reconfigurable quantum architecture

Idea: Rydberg interactions to **entangle** atoms,
then store in **long-lived states**

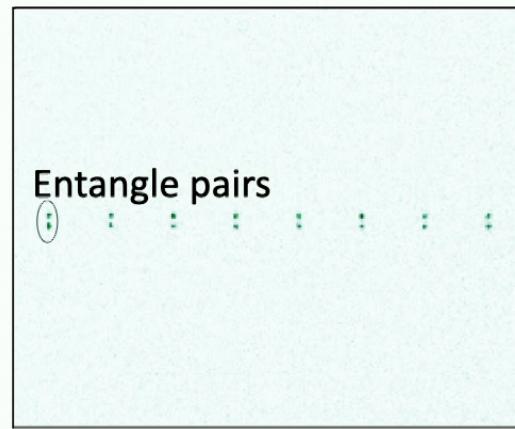


Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

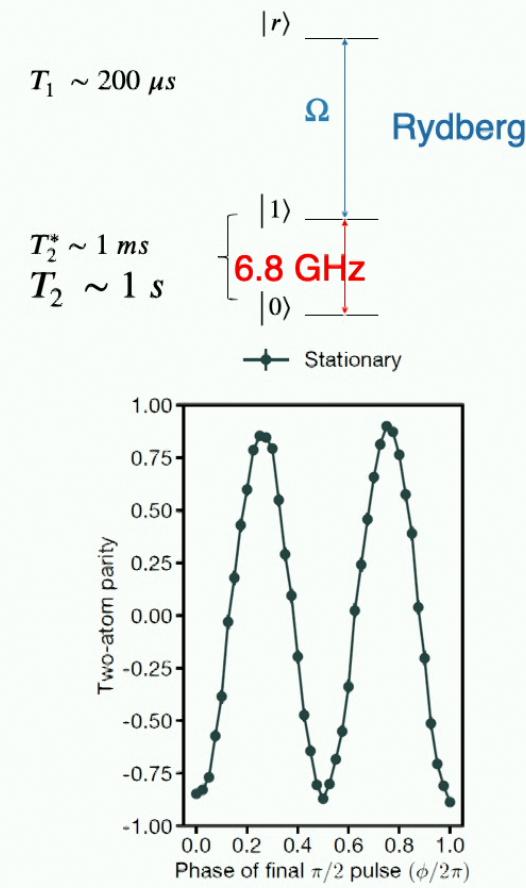
D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Outlook: reconfigurable quantum architecture

Idea: Rydberg interactions to **entangle** atoms, then store in **long-lived states**



Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

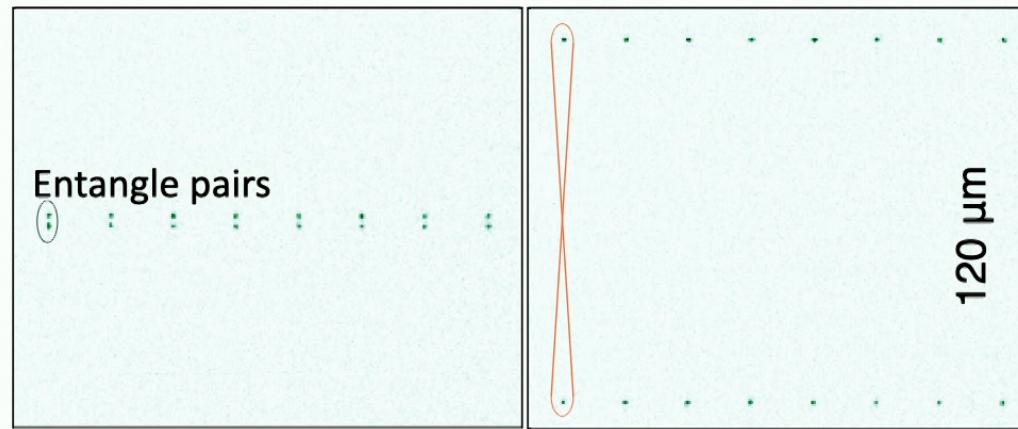


D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

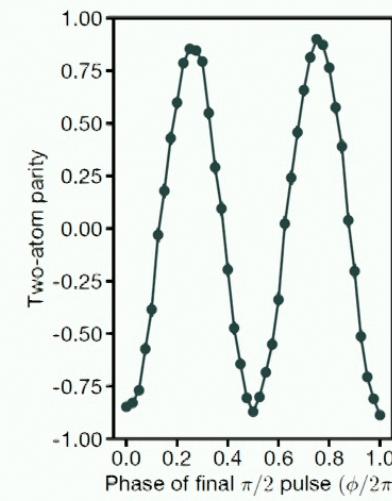
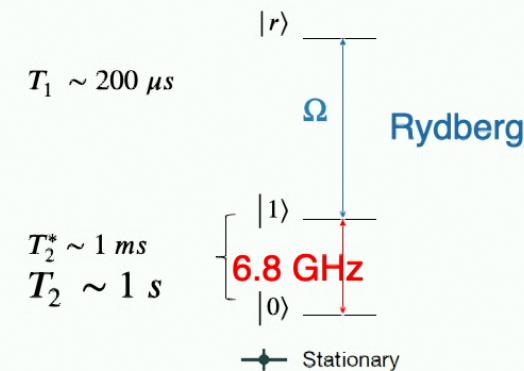
Outlook: reconfigurable quantum architecture

Idea: Rydberg interactions to **entangle** atoms,
then store in **long-lived states**
... and transport ...

in ~500 microseconds ...



Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

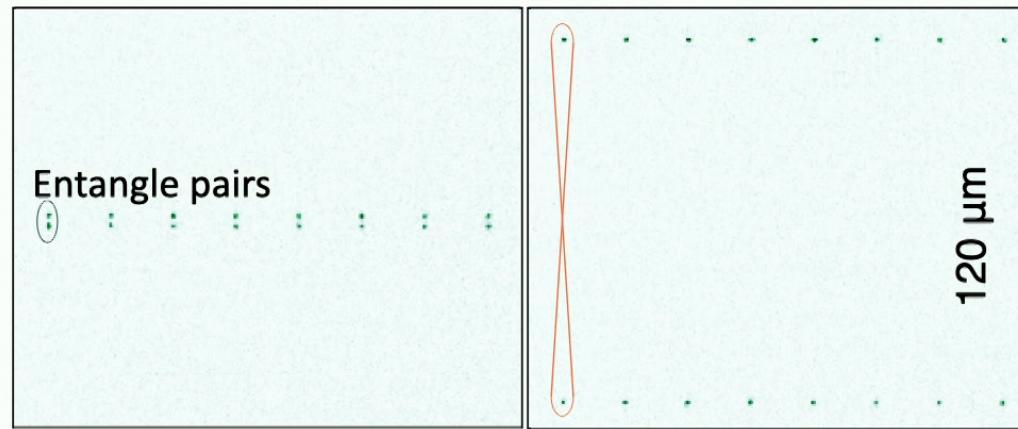


D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Outlook: reconfigurable quantum architecture

Idea: Rydberg interactions to **entangle** atoms,
then store in **long-lived states**
... and transport ...

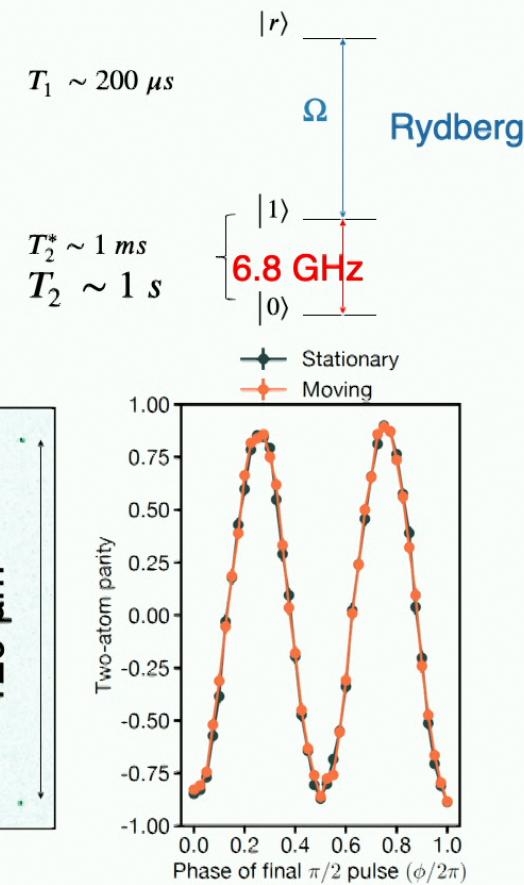
in ~500 microseconds ...



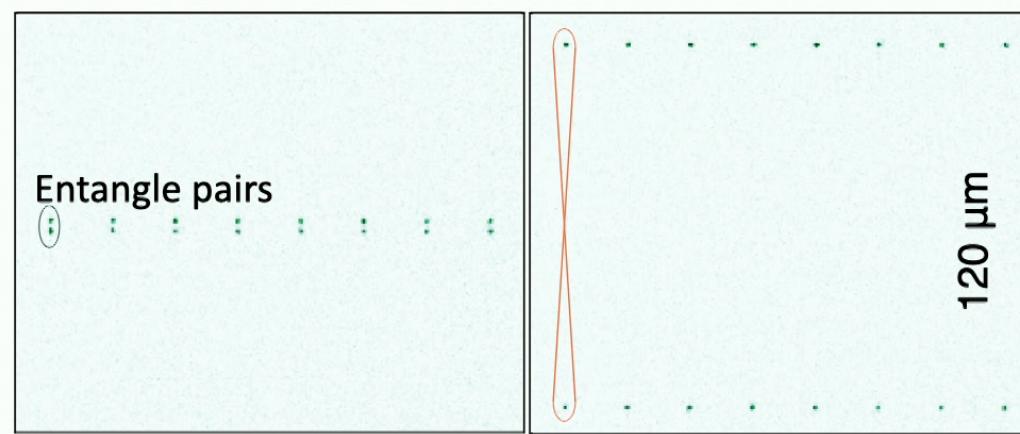
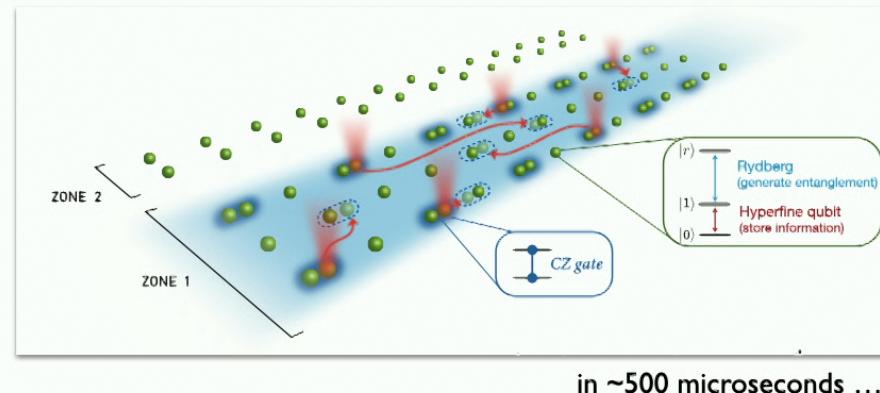
Entanglement and coherence preserved while moving!

Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)



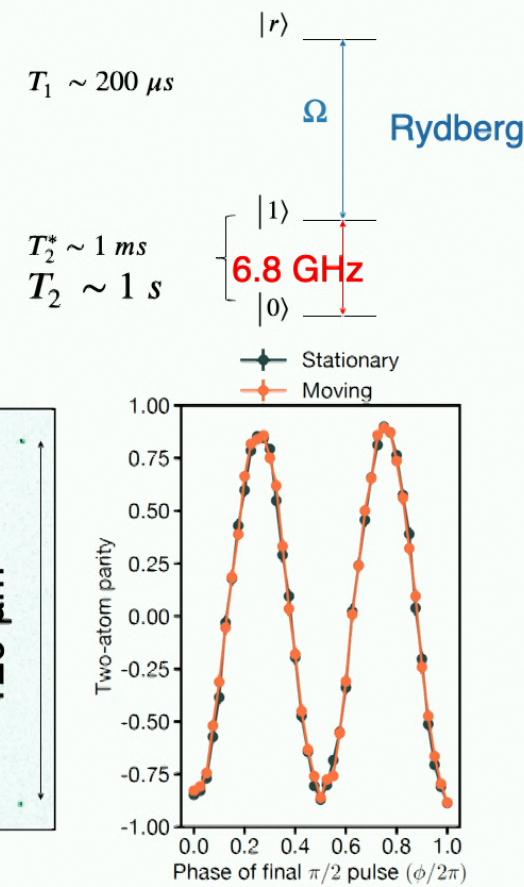
Outlook: reconfigurable quantum architecture



Entanglement and coherence **preserved** while moving!

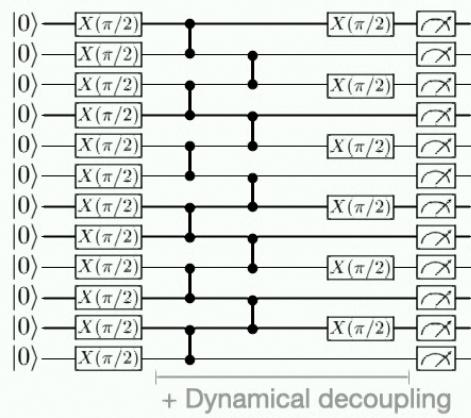
Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)



Gate-based quantum evolution: graph states

Example: two copies of cluster states - parallel preparation



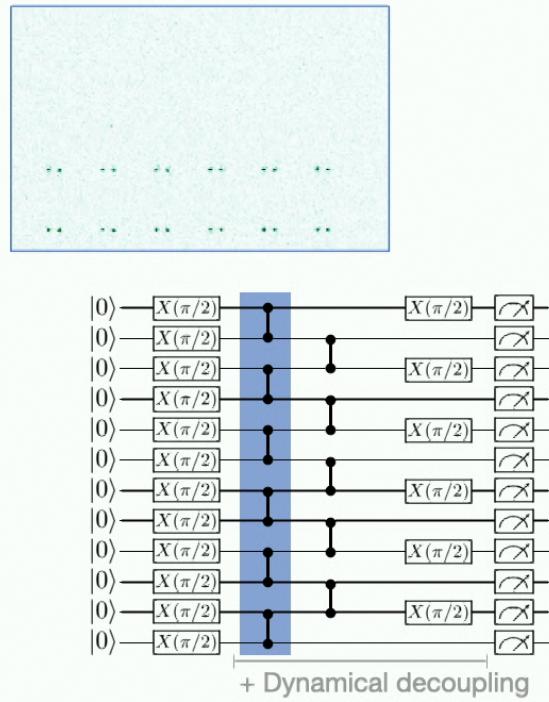
Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Gate-based quantum evolution: graph states

Example: two copies of cluster states - parallel preparation

1st CZ gate



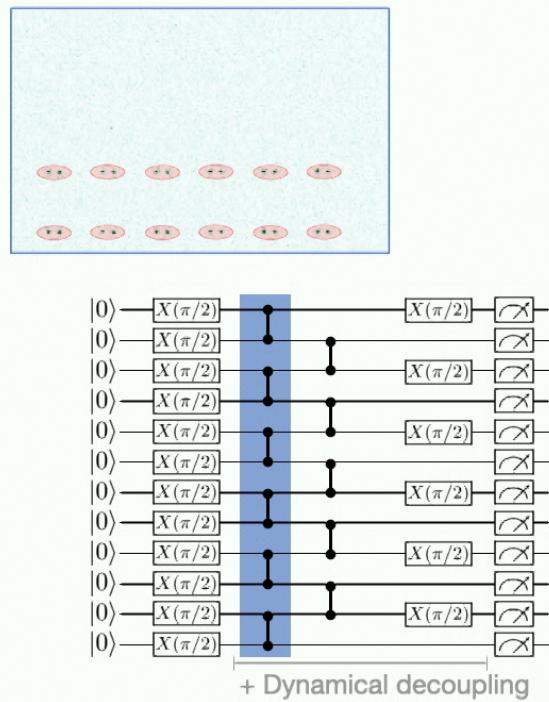
Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Gate-based quantum evolution: graph states

Example: two copies of cluster states - parallel preparation

1st CZ gate

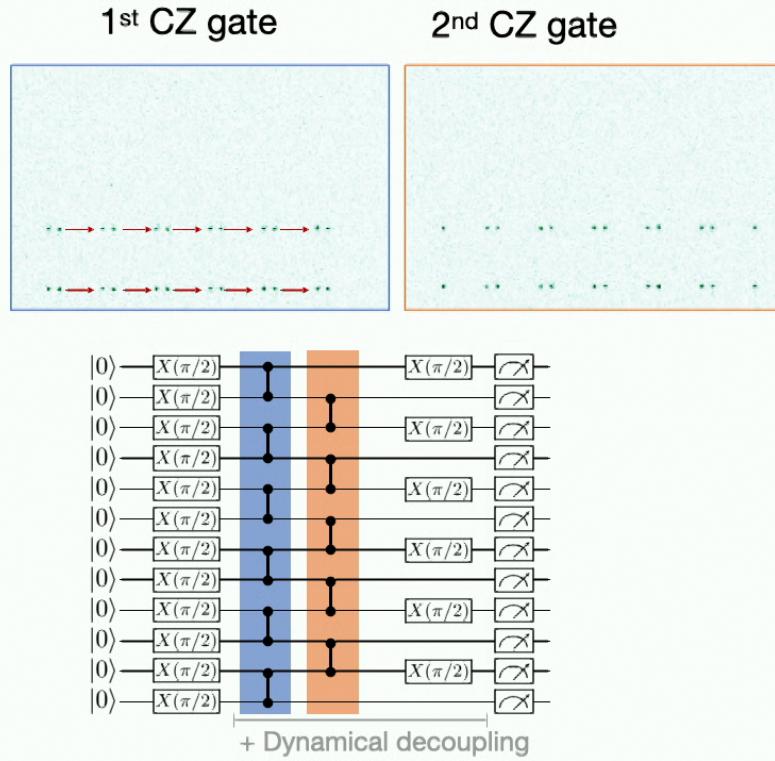


Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Gate-based quantum evolution: graph states

Example: two copies of cluster states - parallel preparation

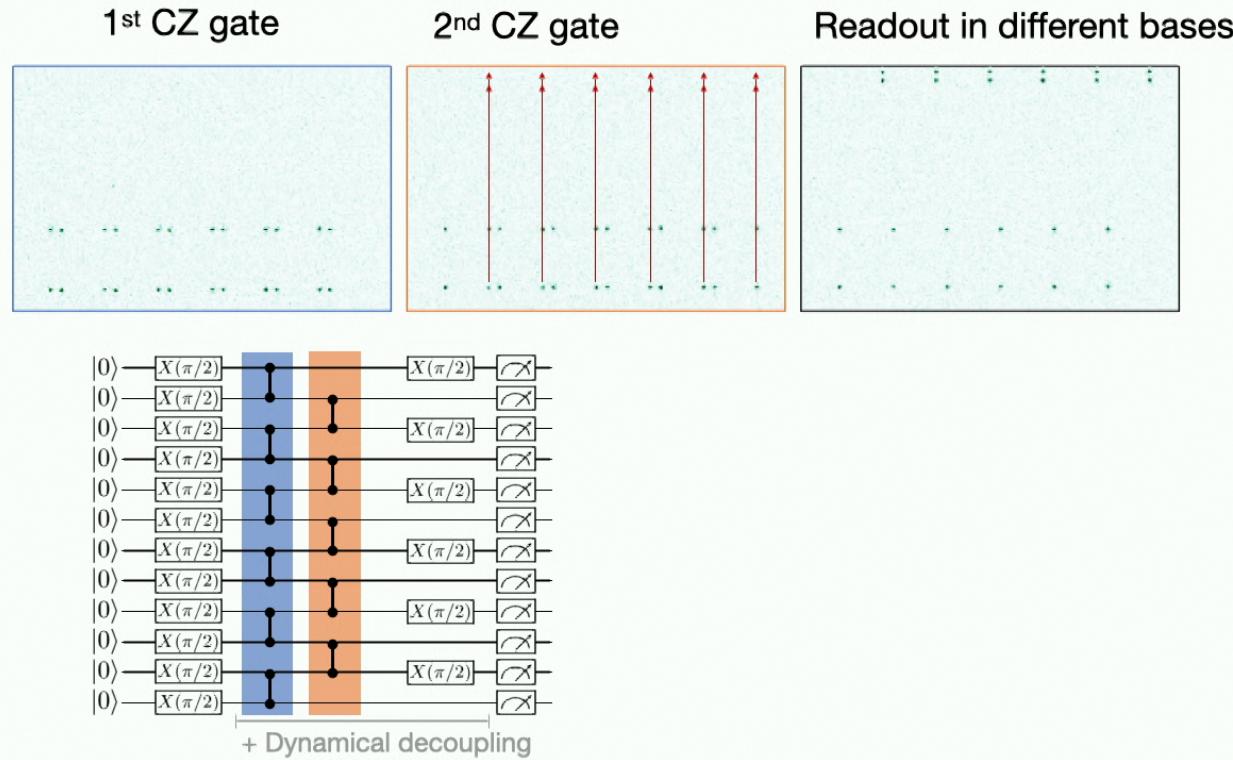


Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Gate-based quantum evolution: graph states

Example: two copies of cluster states - parallel preparation

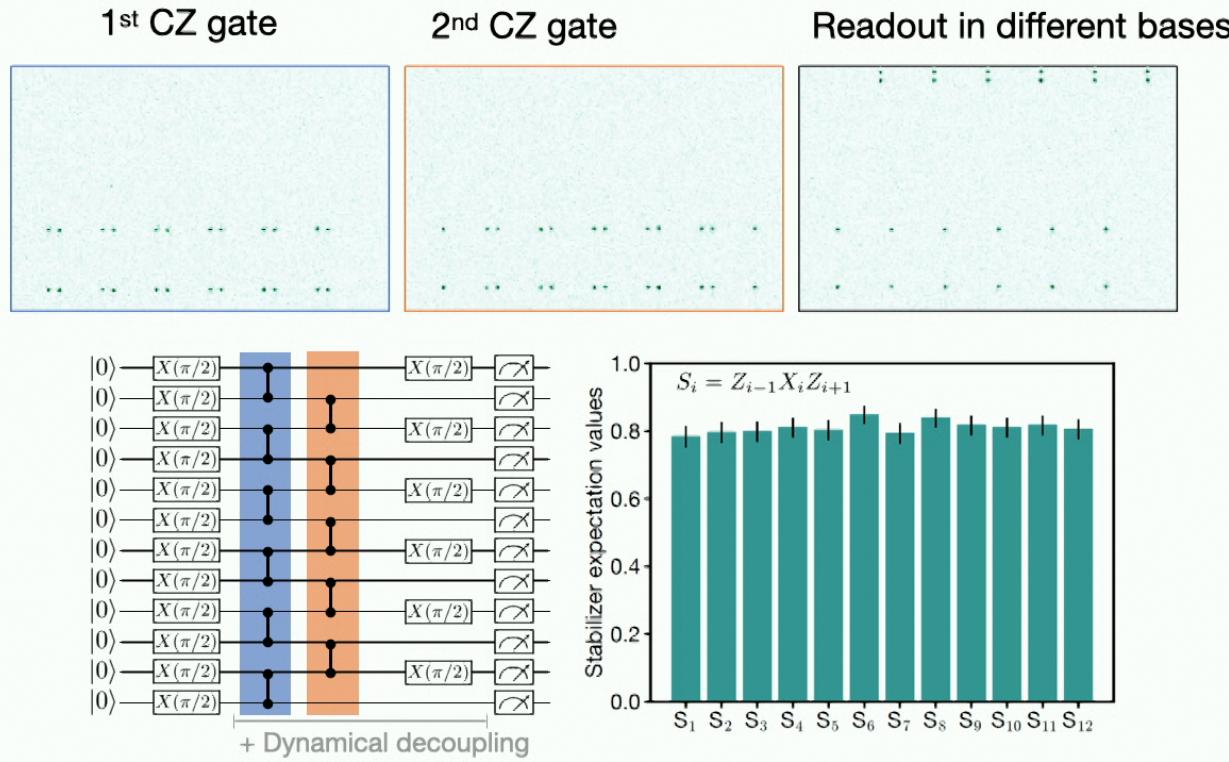


Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Gate-based quantum evolution: graph states

Example: two copies of cluster states - parallel preparation

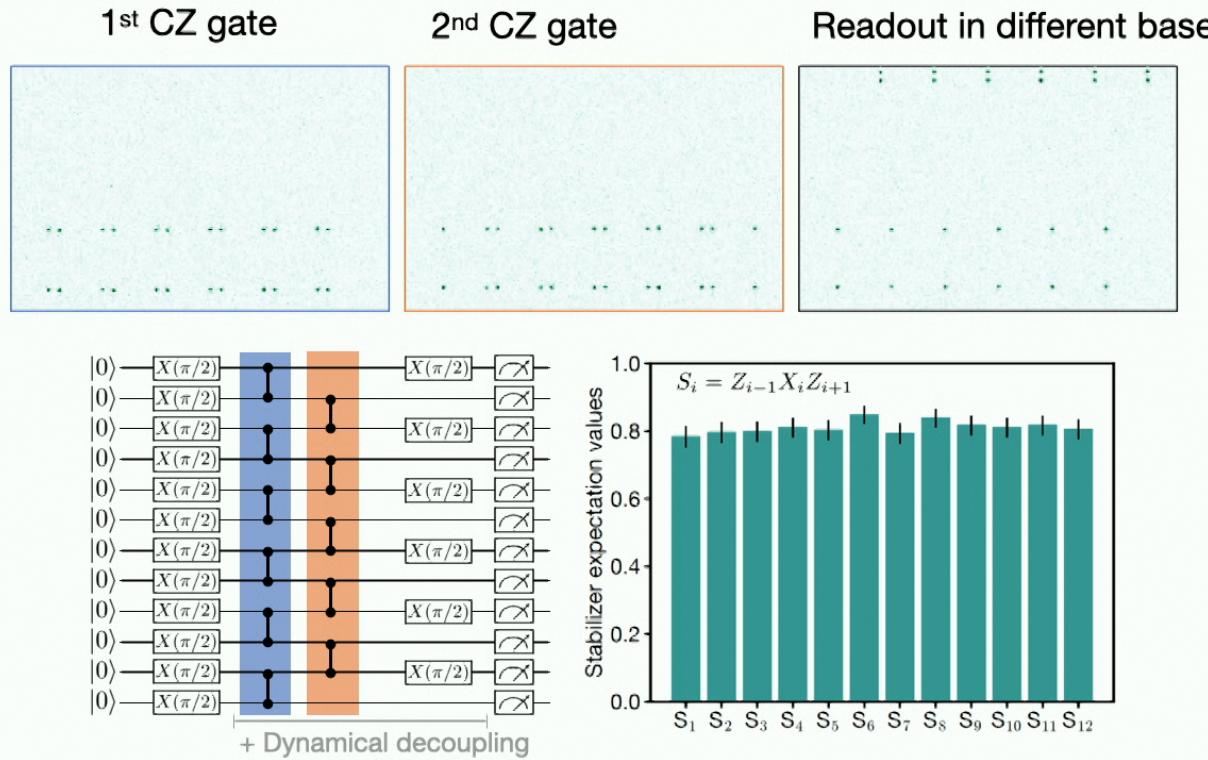


Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Gate-based quantum evolution: graph states

Example: two copies of cluster states - parallel preparation

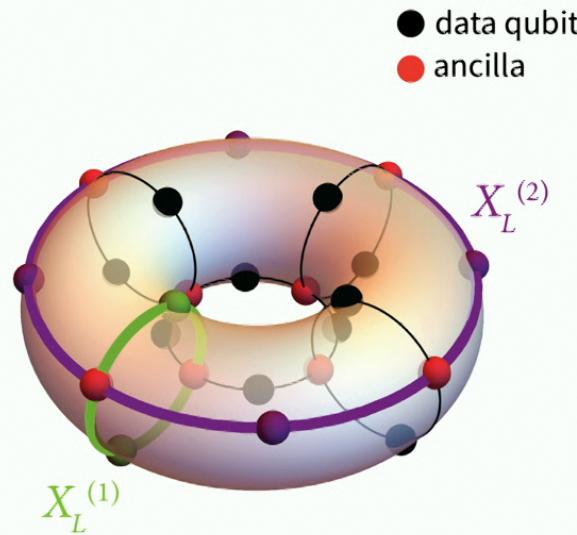


Can one prepare more complex states?

Entanglement via CZ gate: Levine, Pichler et al, PRL 2019

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Towards quantum error correction: toric code ... on the torus??



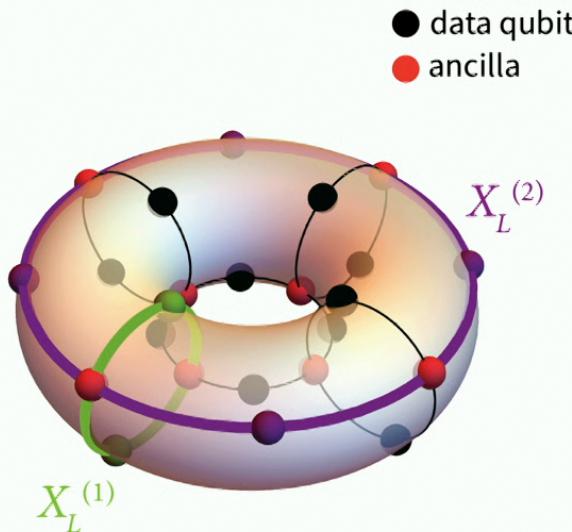
Quantum Error Correction primer

Toric code:

- Grid of physical qubits encodes logical qubit(s)
- Logical qubit: building block of fault-tolerant QC
- Stabilizer measurements detect local errors

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Towards quantum error correction: toric code ... on the torus??



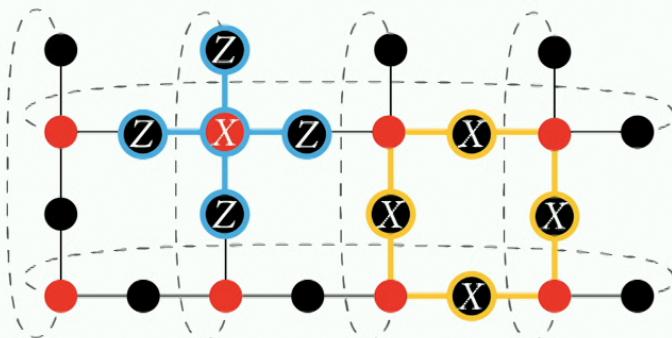
● data qubit
● ancilla

Quantum Error Correction primer

Toric code:

- Grid of physical qubits encodes logical qubit(s)
- Logical qubit: building block of fault-tolerant QC
- Stabilizer measurements detect local errors

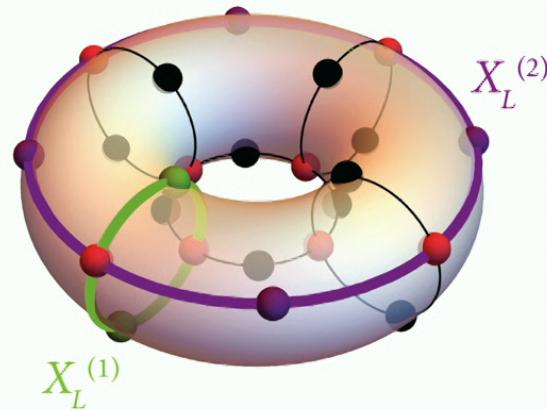
Equivalent to graph state with non-local connectivity



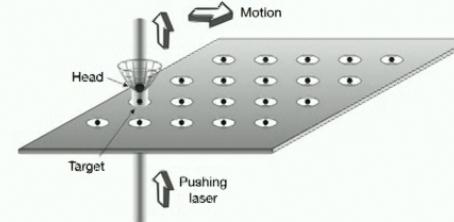
D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Towards quantum error correction: toric code ... on the torus??

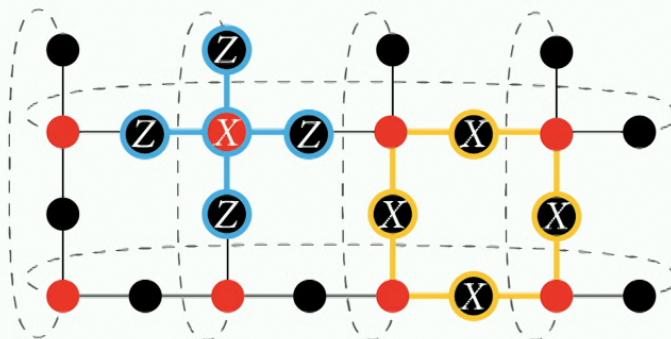
● data qubit
● ancilla



Realization via parallel ancilla transport
(idea Cirac, Zoller, Nature 2001)



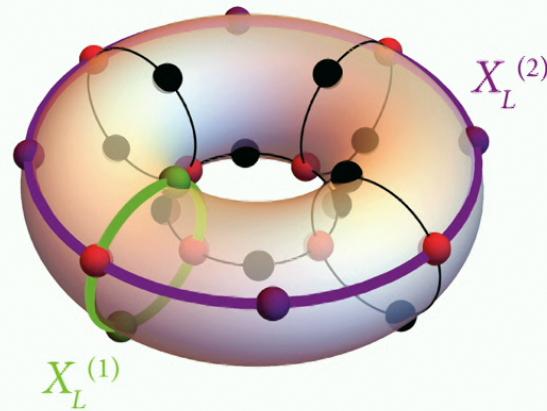
Equivalent to graph state with non-local connectivity



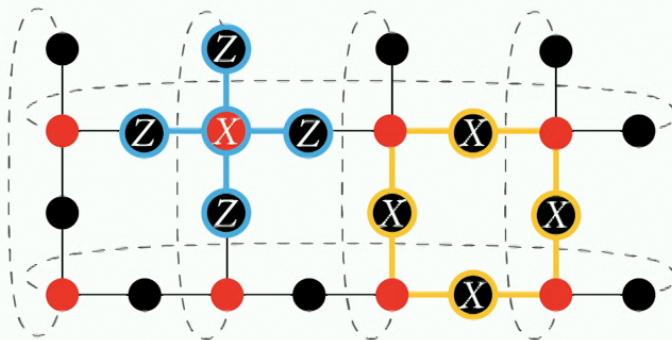
D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Towards quantum error correction: toric code ... on the torus??

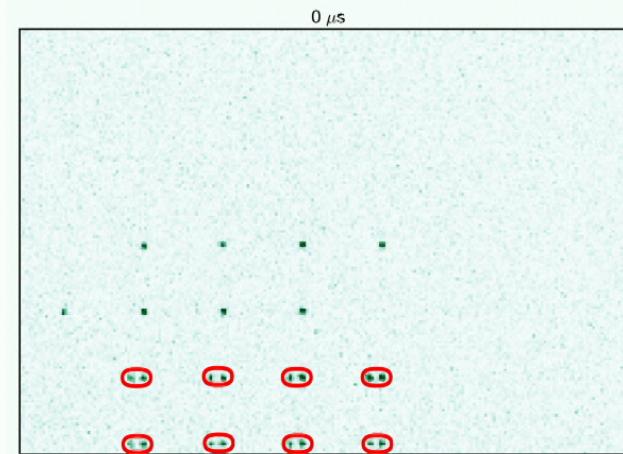
● data qubit
● ancilla



Equivalent to graph state with non-local connectivity



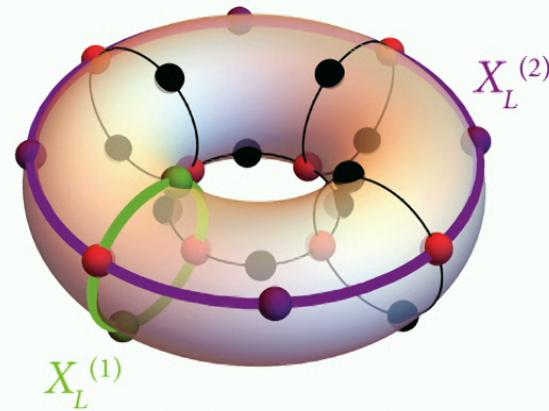
Realization via parallel ancilla transport
(idea Cirac, Zoller, Nature 2001)



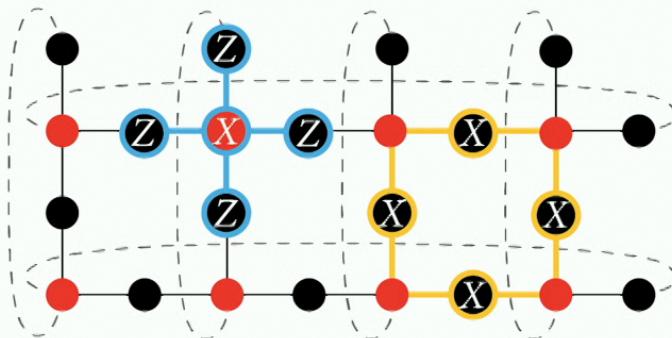
D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Towards quantum error correction: toric code ... on the torus??

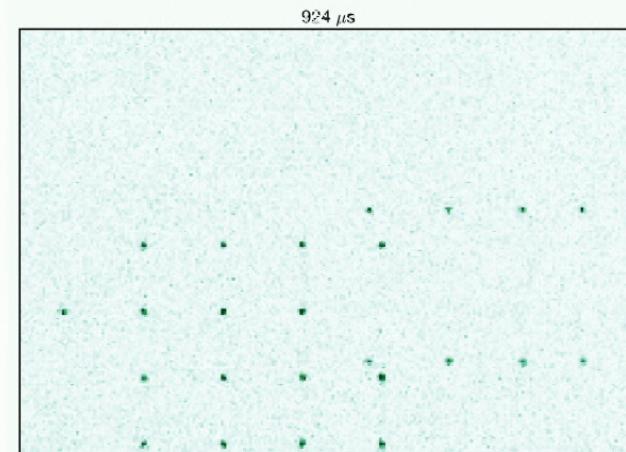
● data qubit
● ancilla



Equivalent to graph state with non-local connectivity



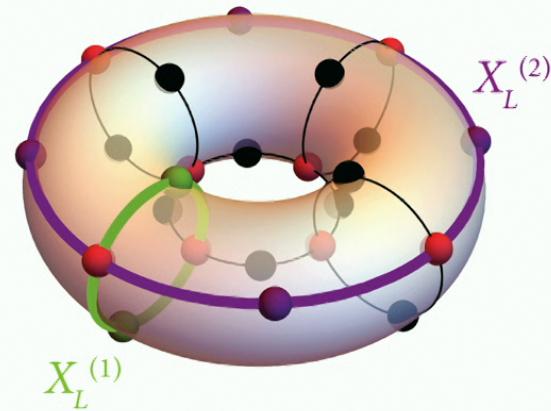
Realization via parallel ancilla transport
(idea Cirac, Zoller, Nature 2001)



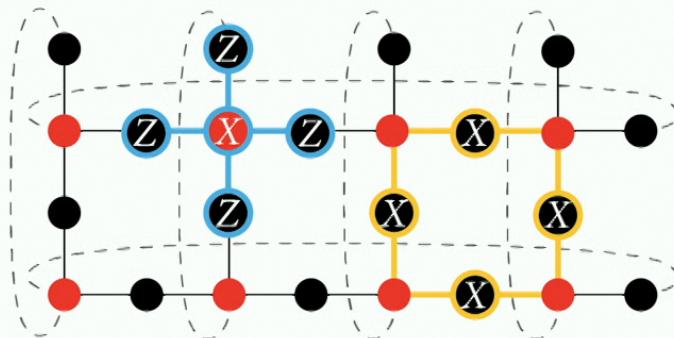
D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Towards quantum error correction: toric code ... on the torus??

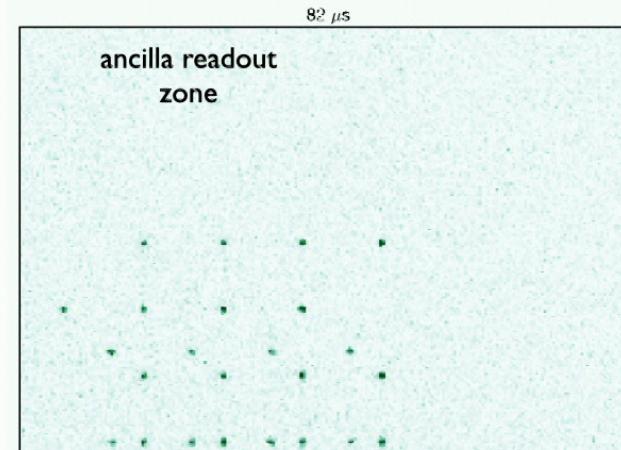
● data qubit
● ancilla



Equivalent to graph state with non-local connectivity



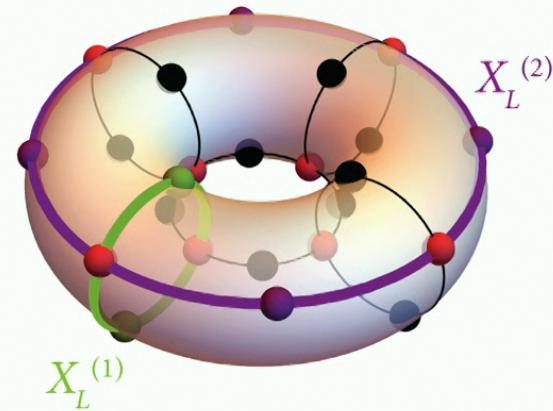
Realization via parallel ancilla transport
(idea Cirac, Zoller, Nature 2001)



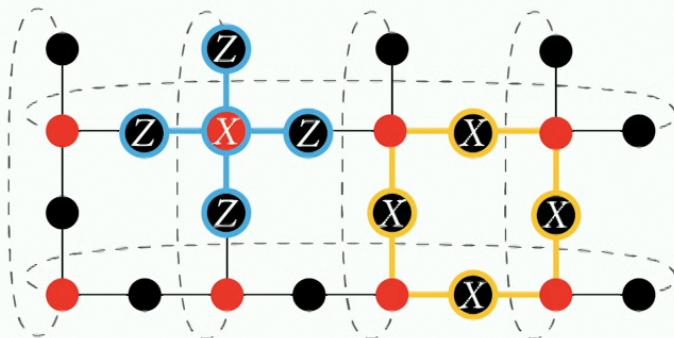
D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Towards quantum error correction: toric code ... on the torus??

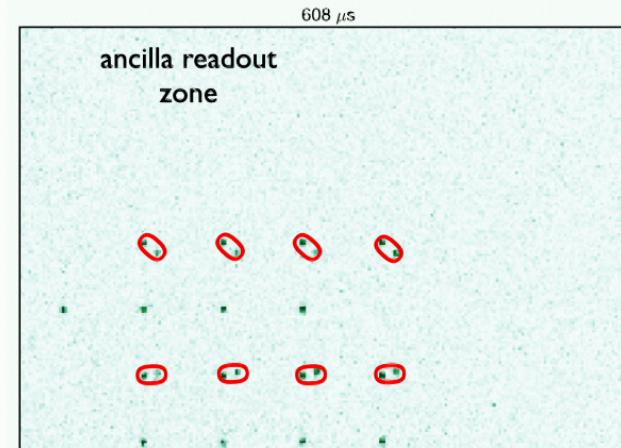
● data qubit
● ancilla



Equivalent to graph state with non-local connectivity



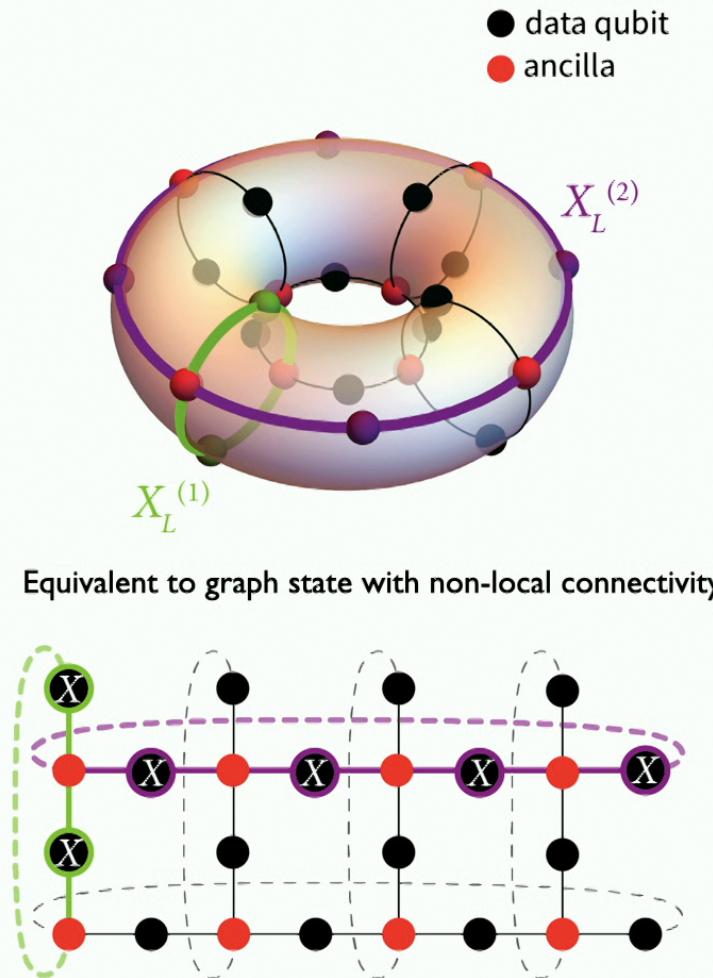
Realization via parallel ancilla transport
(idea Cirac, Zoller, Nature 2001)



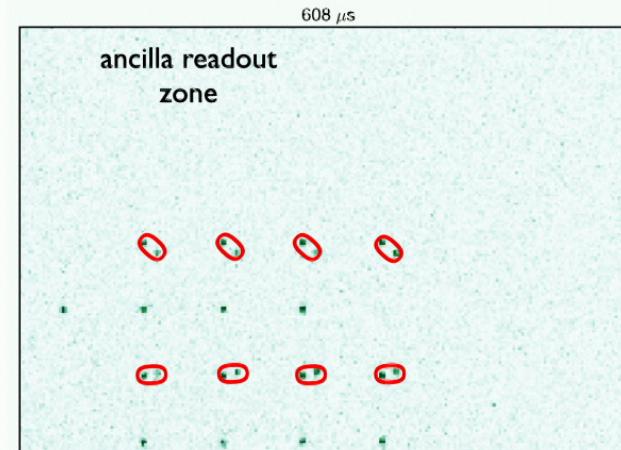
Encodes two (!) logical qubits

D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

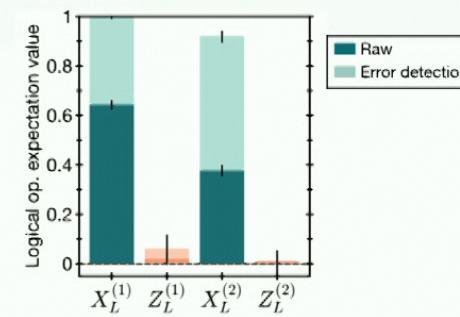
Towards quantum error correction: toric code ... on the torus??



Realization via parallel ancilla transport
(idea Cirac, Zoller, Nature 2001)



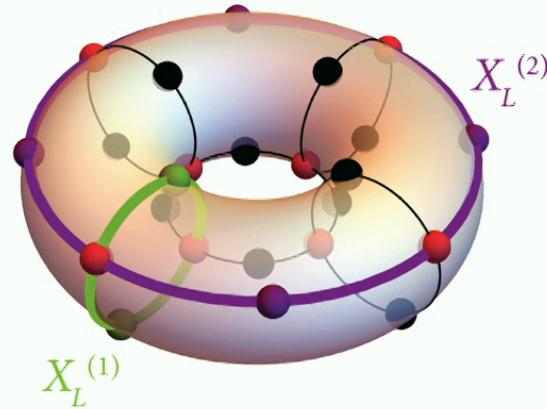
Encodes two (!) logical qubits



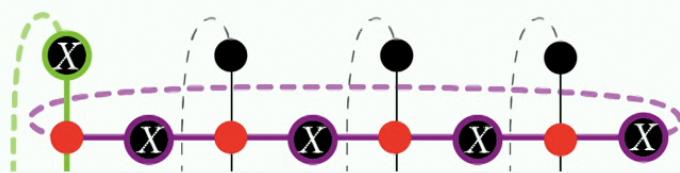
D. Bluvstein et al, arXiv:2112.03923, Nature (2022)

Towards quantum error correction: toric code ... on the torus??

● data qubit
● ancilla

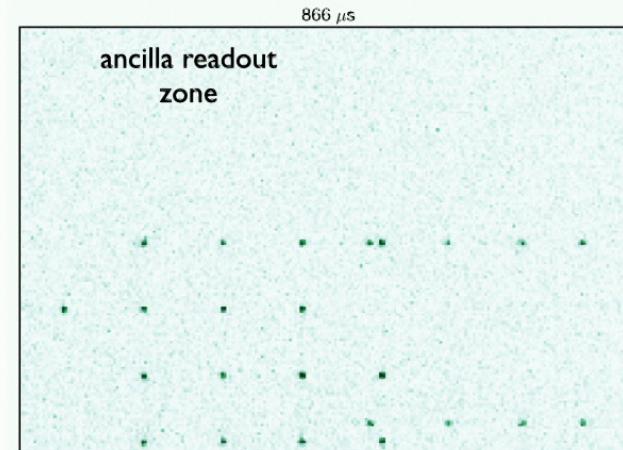


Equivalent to graph state with non-local connectivity

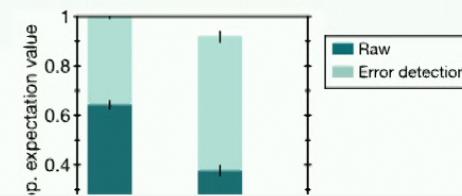


New opportunities for fault-tolerant quantum processing (e.g hypergraph, LDPC codes)
Hardware-efficient methods for quantum error correction I. Cong et al, PRX (2022)
Hybrid approaches combining analog and digital quantum dynamics

Realization via parallel ancilla transport
(idea Cirac, Zoller, Nature 2001)

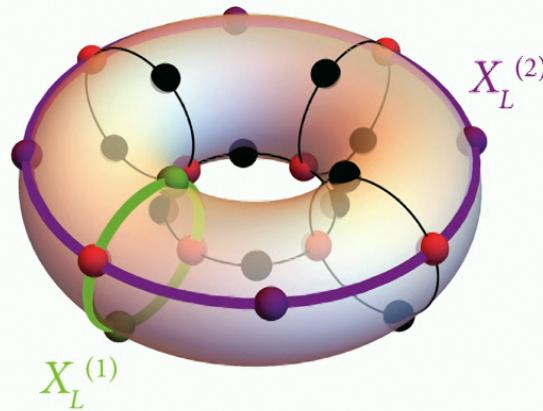


Encodes two (!) logical qubits

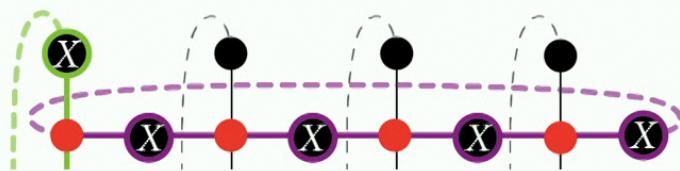


Towards quantum error correction: toric code ... on the torus??

● data qubit
● ancilla

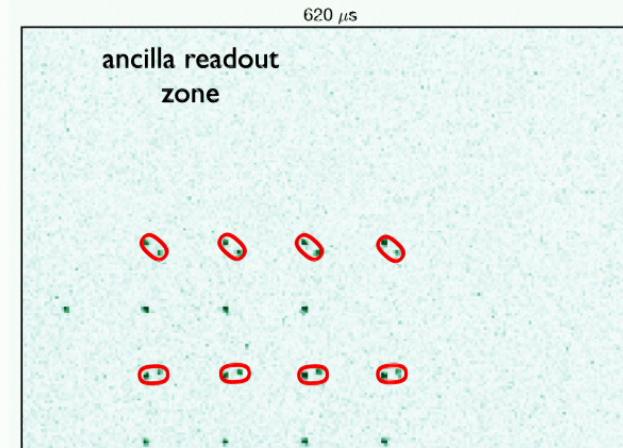


Equivalent to graph state with non-local connectivity

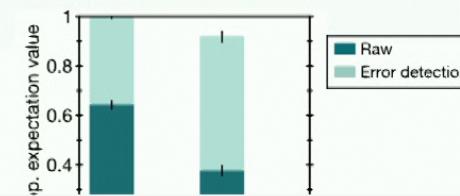


New opportunities for fault-tolerant quantum processing (e.g hypergraph, LDPC codes)
Hardware-efficient methods for quantum error correction I. Cong et al, PRX (2022)
Hybrid approaches combining analog and digital quantum dynamics

Realization via parallel ancilla transport
(idea Cirac, Zoller, Nature 2001)

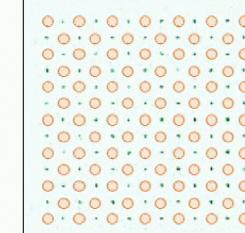
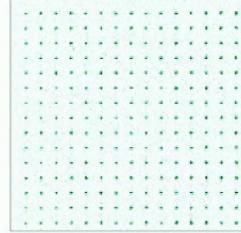


Encodes two (!) logical qubits

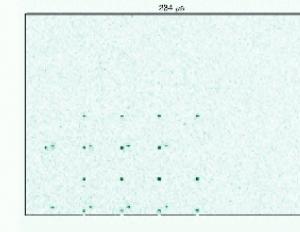
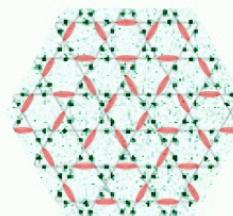
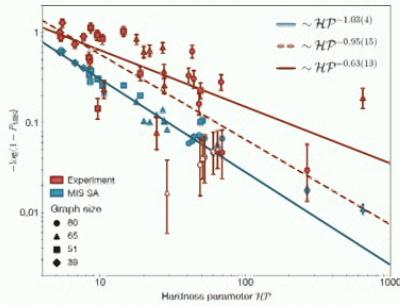


Summary

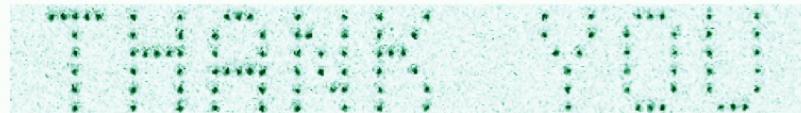
- ✓ Atom by atom approach to building quantum matter
New platform for exploring synthetic quantum matter
Experiments with strongly interacting atom arrays
New generation >200 atom systems in 2D



- ✓ Many-body dynamics on programmable simulator
Engineering & exploring phase transitions
Realization and probing quantum spin liquid states
Exploring quantum optimization algorithm
New architecture based on entanglement transport: towards QEC



✓ Outlook: exciting scientific frontier
era of “quantum discovery”
from quantum many-body physics to new applications



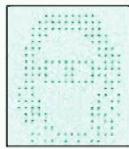
Acknowledgements



Harry Levine



Tout Wang



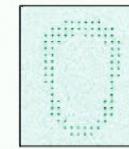
Sepehr Ebadi



Giulia Semeghini



Alex Keesling



Dolev Bluvstein



Ahmed Omran



All data was taken remotely!

CUA collaboration of
Lukin, Vuletic, Greiner, Englund groups
QuEra Computing, Inc.



Funding: NSF, CUA, Vannevar Bush,
AFOSR MURI, DARPA, DOE, NDSEG

H. Pichler S. Choi N. Maskara L. Zhou R. Samajdar M.Cain R.Verresen



Collaborations with Sachdev group, Vishwanath group,
Maksym Serbyn group, Hannes Pichler group