

Title: Polyatomic ultralong range Rydberg molecules

Speakers: Rosario Gonzalez-Ferez

Collection: Cold Atom Molecule Interactions (CATMIN)

Date: July 14, 2022 - 11:50 AM

URL: <https://pirsa.org/22070008>

Abstract: In cold and ultracold mixtures of atoms and molecules, Rydberg interactions with surrounding atoms or molecules may, under certain conditions, lead to the formation of special long-range Rydberg molecules [1,2,3]. These exotic molecules provide an excellent toolkit for manipulation and control of interatomic and atom-molecule interactions, with applications in ultracold chemistry, quantum information processing and many-body quantum physics.

In this talk, we will discuss ultralong-range polyatomic Rydberg molecules formed when a heteronuclear diatomic molecule is bound to a Rydberg atom [3,4]. The binding mechanism appears due to anisotropic scattering of the Rydberg electron from the permanent electric dipole moment of the polar molecule. We propose an experimentally realizable scheme to produce these triatomic ultralong-range Rydberg molecules in ultracold RbCs traps, which might use the excitation of cesium or rubidium [5]. By exploiting the Rydberg electron-molecule anisotropic dipole interaction, we induce a near resonant coupling of the non-zero quantum defect Rydberg levels with the RbCs molecule in an excited rotational level. This coupling enhances the binding of the triatomic ultralong-range Rydberg molecule and produces favorable Franck-Condon factors.

#### References

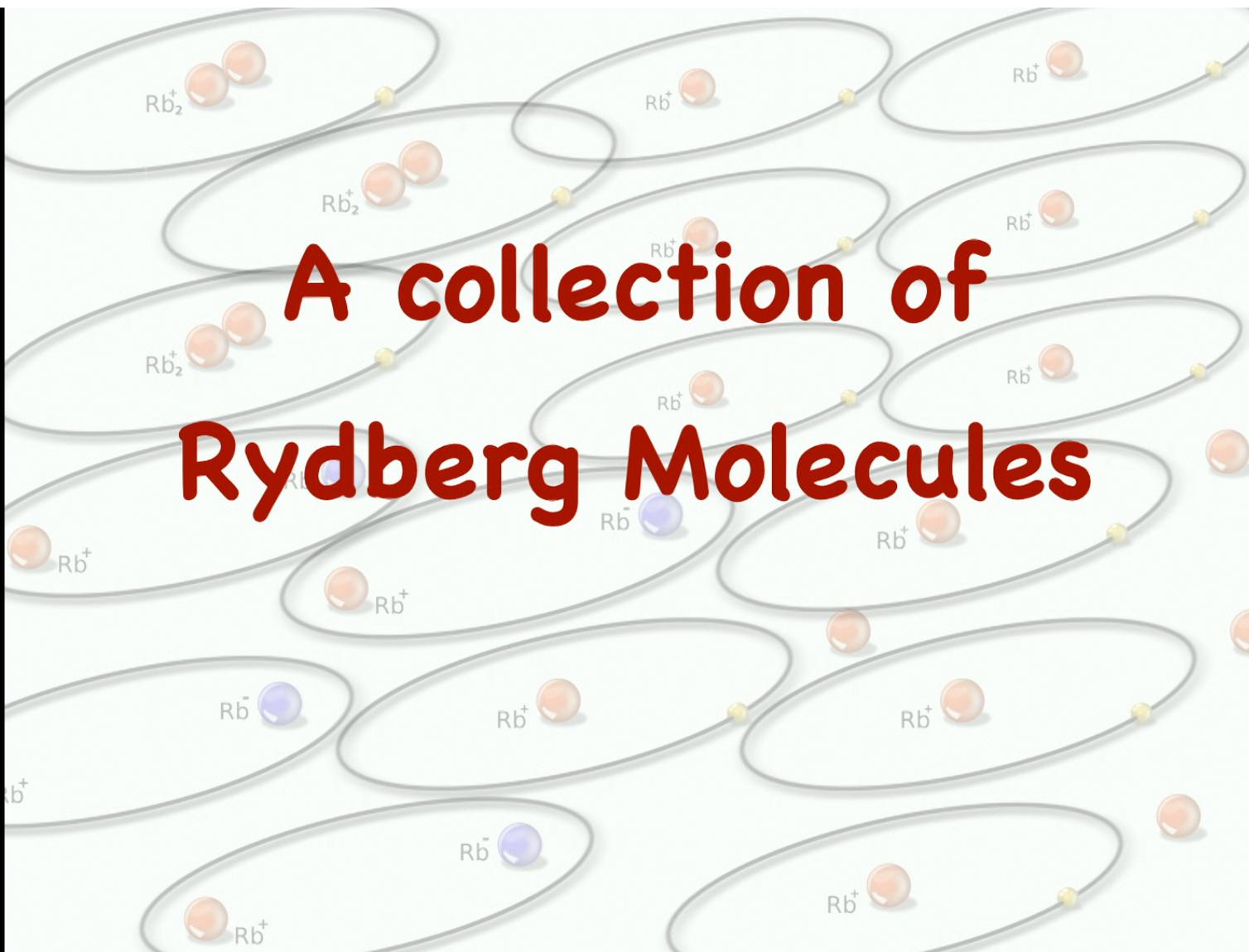
- [1] C. H. Greene, A. S. Dickinson, and H. R. Sadeghpour, Phys. Rev. Lett. 85, 2458 (2000).
- [2] S. T. Rittenhouse and H. R. Sadeghpour, Phys. Rev. Lett. 104, 243002 (2010).
- [3] V. Bendkowsky, B. Butscher, J. Nipper, J. P. Shaffer, R. Löw, and T. Pfau, Nature 458, 1005 (2009).
- [4] R. González-Férez, H. R. Sadeghpour, and P. Schmelcher, New J. Phys. 17, 013021 (2015).
- [5] R. González-Férez, S.T. Rittenhouse, P. Schmelcher and H.R. Sadeghpour, J. Phys. B 53, 074002 (2020)."

# Polyatomic ultralong range Rydberg molecule

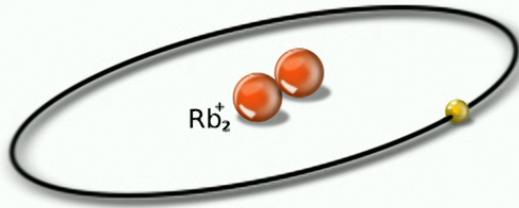
**Rosario González-Férez**  
Universidad de Granada



# A collection of Rydberg Molecules

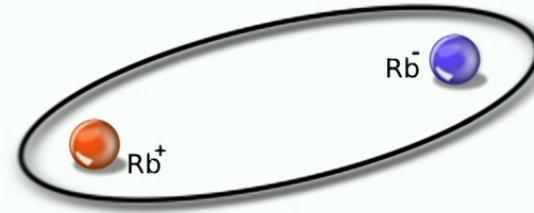


## Rydberg states of molecule



A highly excited electron interacting with the ionic core.

## Heavy Rydberg states of molecules



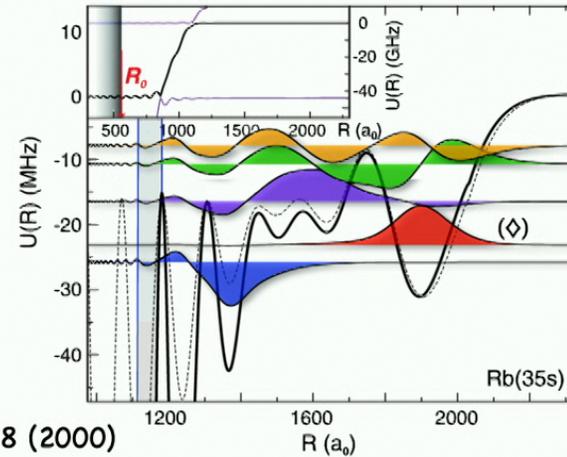
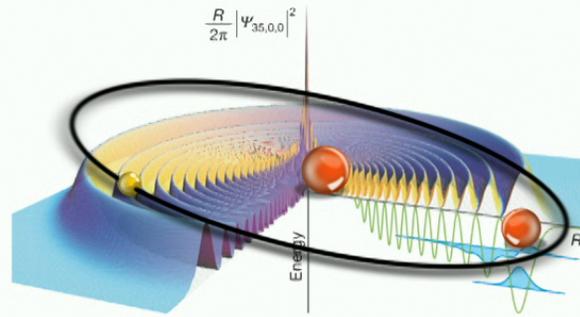
very high vibrational structure approaches a Rydberg series

## Macrodimers



Rydberg atom + Rydberg atom

## Ultralong-range Rydberg molecule Rydberg atom + ground-state atom



V. Bendkowsky et al, Nature **458**, 1005 (2009)

C.H. Greene, A.S. Dickinson & H.R. Sadeghpour, PRL **85**, 2458 (2000)

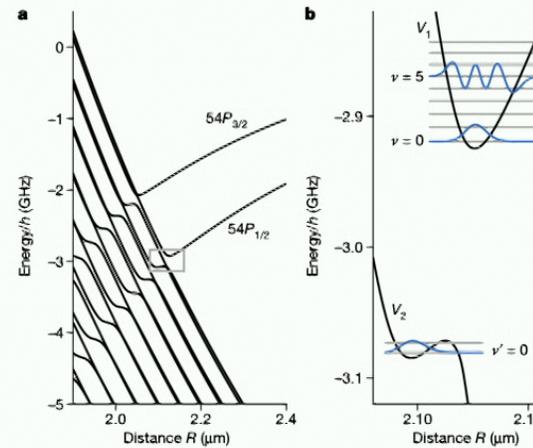
## Long-range ion-Rydberg atom molecule <sup>a</sup>



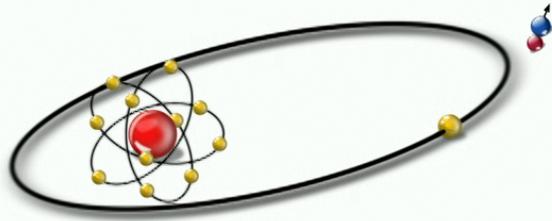
A. Duspayev et al, Phys. Rev. Research **3**, 023114 (2021)

M Deiß, et al, Atoms **9**, 34 (2021)

N. Zuber et al, Nature **605**, 453 (2022)



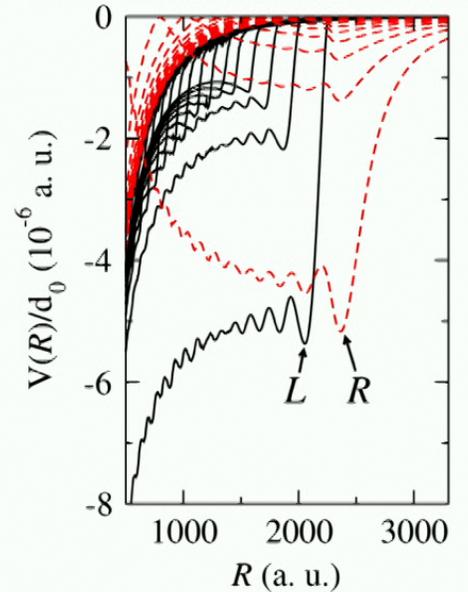
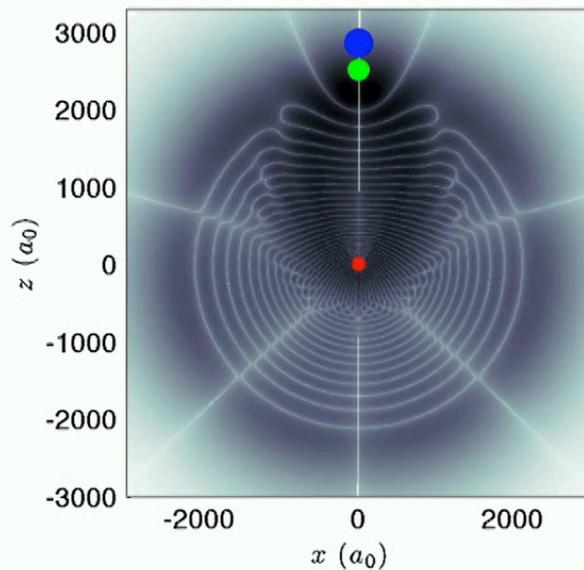
## Rydberg molecules: Rydberg atom + polar molecule



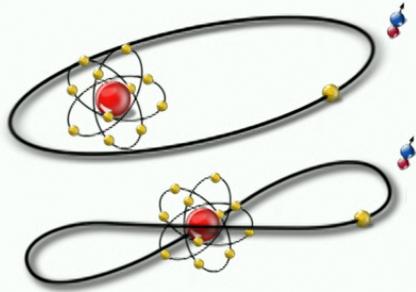
Binding mechanism: anisotropic scattering of the Rydberg electron with the dipole moment of the dimer

S.T. Rittenhouse & H.R. Sadeghpour, PRL (2010)

## Electronic structure Rb- $\Lambda$ -Doublet dimer



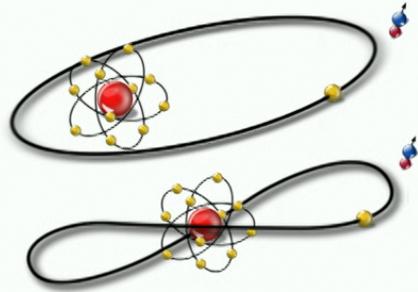
# Rydberg atom + heteronuclear molecule



Core & Rydberg electron electric fields:

$$\mathbf{F}_{ryd}(\mathbf{R}, \mathbf{r}) = e \frac{\mathbf{R}}{R^3} + \frac{\mathbf{r} - \mathbf{R}}{|\mathbf{r} - \mathbf{R}|^3}$$

# Rydberg atom + heteronuclear molecule

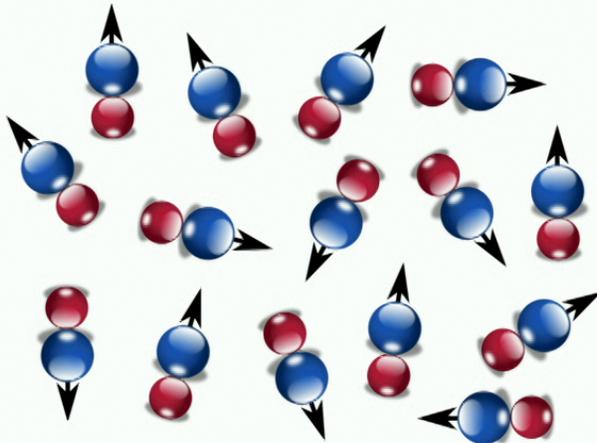


Core & Rydberg electron electric fields:

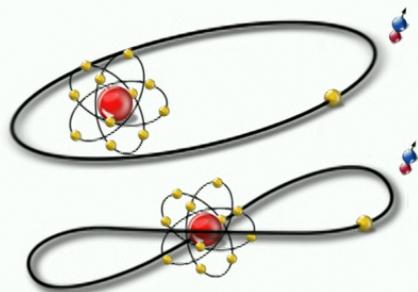
$$\mathbf{F}_{ryd}(\mathbf{R}, \mathbf{r}) = e \frac{\mathbf{R}}{R^3} + \frac{\mathbf{r} - \mathbf{R}}{|\mathbf{r} - \mathbf{R}|^3}$$

Field-free

$$H = BN^2$$



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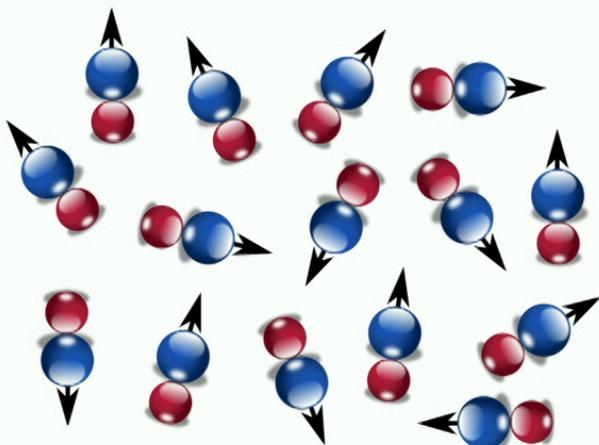
Field-free



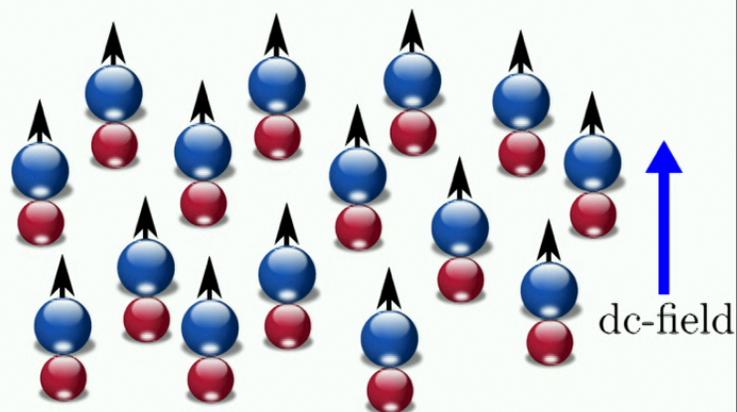
dc electric field

Orientation: the molecule-fixed axes are confined and the dipole moment has a well-defined direction

$$H = BN^2$$



$$H = BN^2 - \mathbf{d} \cdot \mathbf{F}$$



## Our Rydberg molecule

The total Hamiltonian  $H = H_A + H_{mol} + V_{n,e}$

The Rydberg electron Hamiltonian

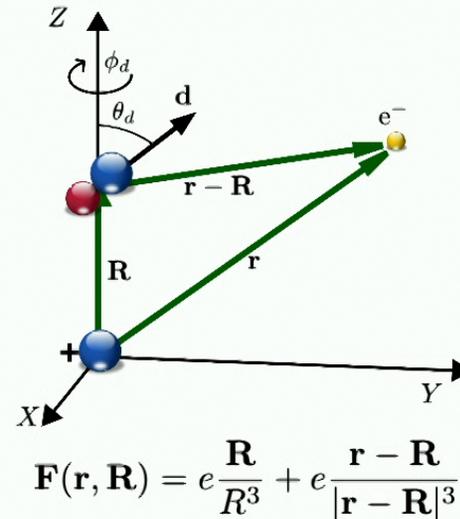
$$H_A = -\frac{\hbar^2}{2m_e} \nabla_r^2 + V_l(r)$$

The Hamiltonian of the molecule

$$H_{mol} = BN^2 - \mathbf{d} \cdot \mathbf{F}(\mathbf{r}, \mathbf{R})$$

Fermi-Teller critical dipole:  $d < 1.63D$ .

The electron-RbCS scattering  $V_{n,e}(\mathbf{r}, \mathbf{R}) = 2\pi A_s(k)\delta(\mathbf{r} - \mathbf{R})$



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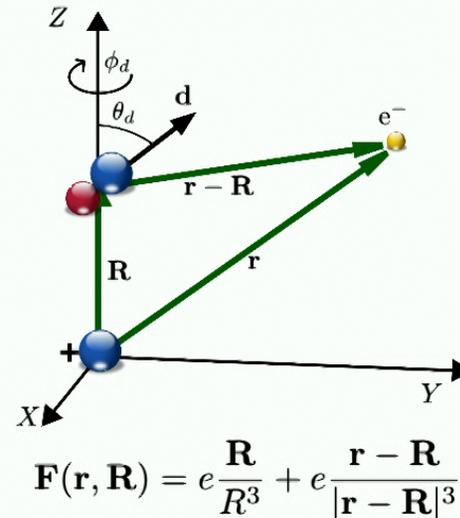
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By a basis set expansion in terms of the coupled basis

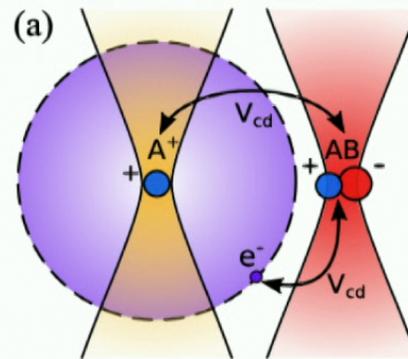
$$\psi_{n l N J M_J}(\mathbf{r}, \Omega_d) = \sum_{m_l=-l}^{m_l=l} \sum_{M_N=-N}^{M_N=N} \psi_{n l m}(\mathbf{r}) Y_{N M_N}(\Omega_d) \langle l m_l N M_N | J M_J \rangle$$

- $Y_{N M_N}(\Omega_d)$  the field-free rotational wave function of KRb
- $\psi_{n l m}(\mathbf{r})$  the Rydberg electron wave function



## Experimental setup

Ultracold molecules:  
KRb (K.K Ni, Harvard)  
RbCs (S. Cornish, Durham)



## Experimental setup

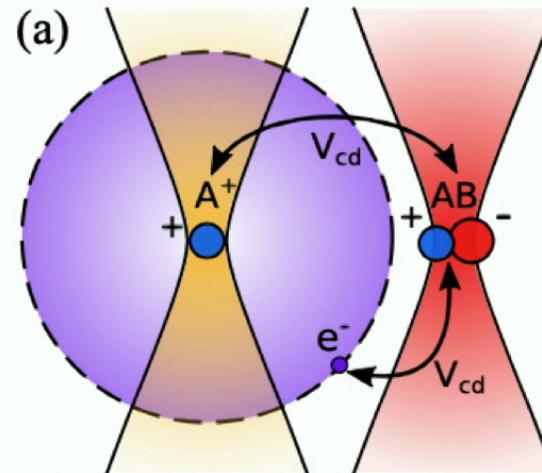
### RbCs rotational states

$B=0.5$  GHz

$d=1.25D$

### Cesium Rydberg states

State	$E_{n,l} - E_{70,l \geq 4}$ [GHz]
$\text{Cs}(n = 70, l \geq 4)$	0.000
$\text{Cs}(70f)$	-0.642
$\text{Cs}(74s)$	-0.948
$\text{Cs}(72d)$	-9.124
$\text{Cs}(73p)$	-11.175

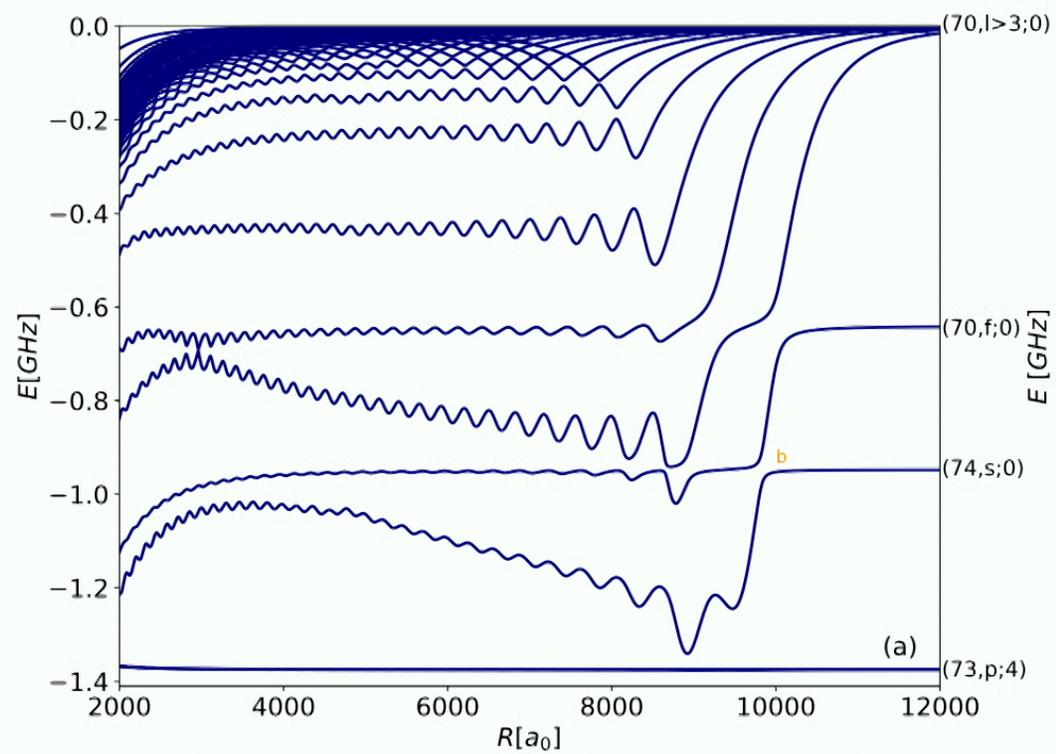


Rydberg molecule: Cs-RbCs

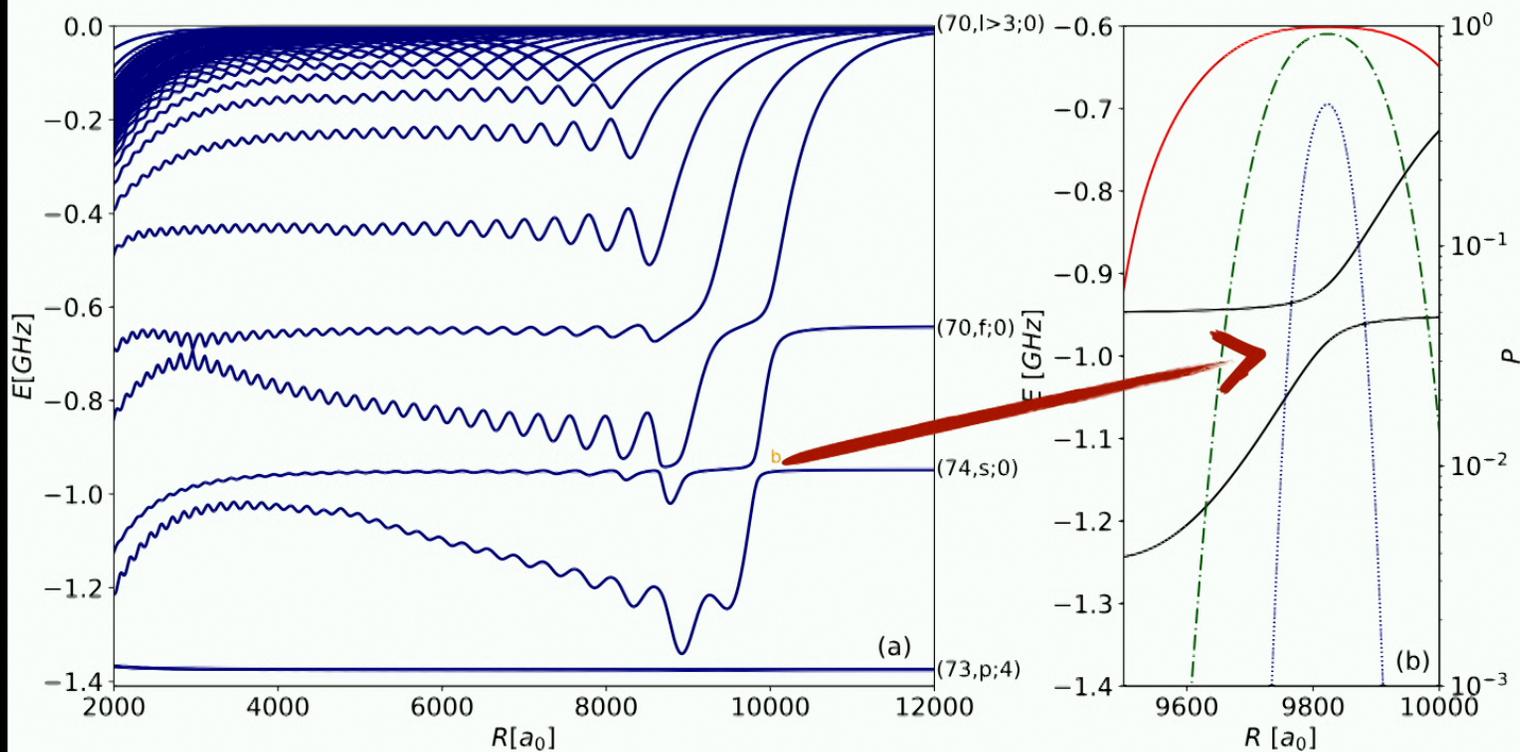
Energy limit for  $R \gg 1$

$$E_{nl} + BN(N + 1)$$

## Electronic structure of Cs(n=70)-RbCS



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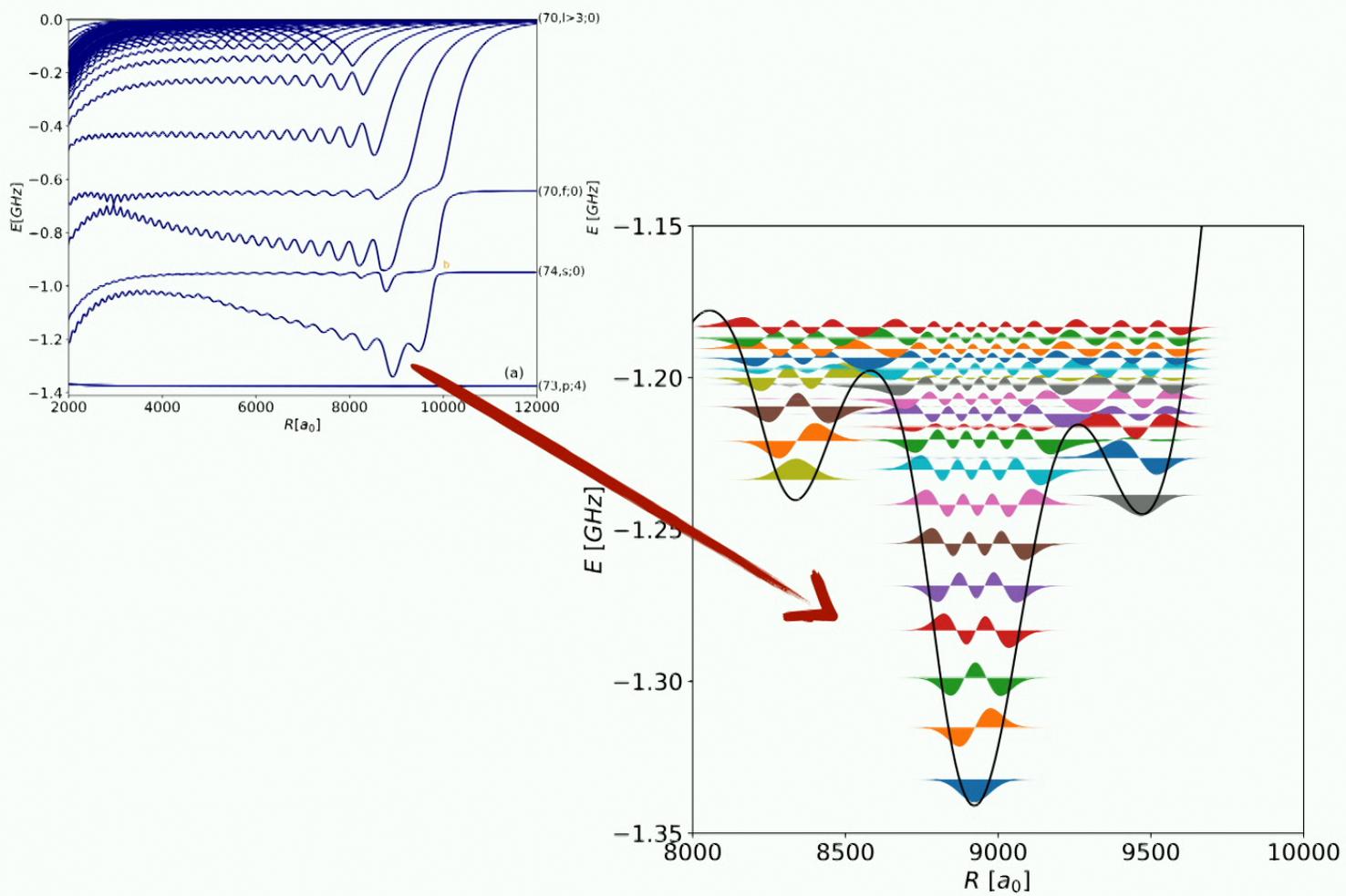


$$v = 2.2 \times 10^2, 2.2 \times 10^3, 2.2 \times 10^4 \text{ cm s}^{-1}$$

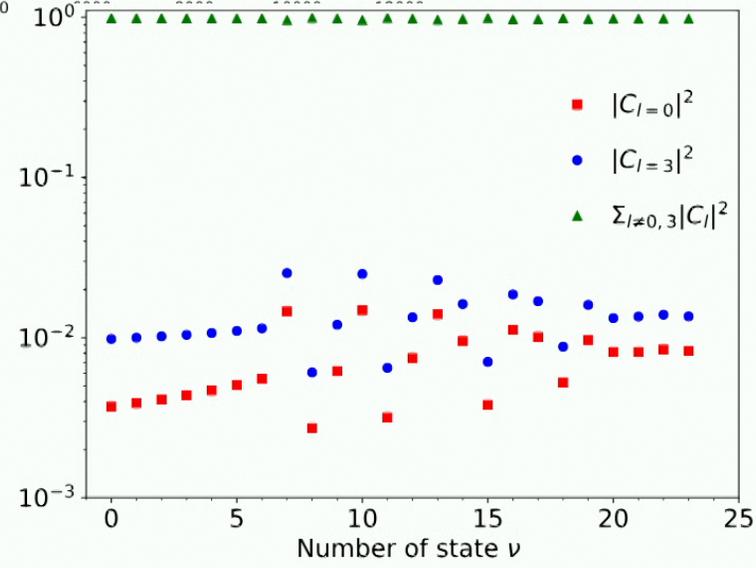
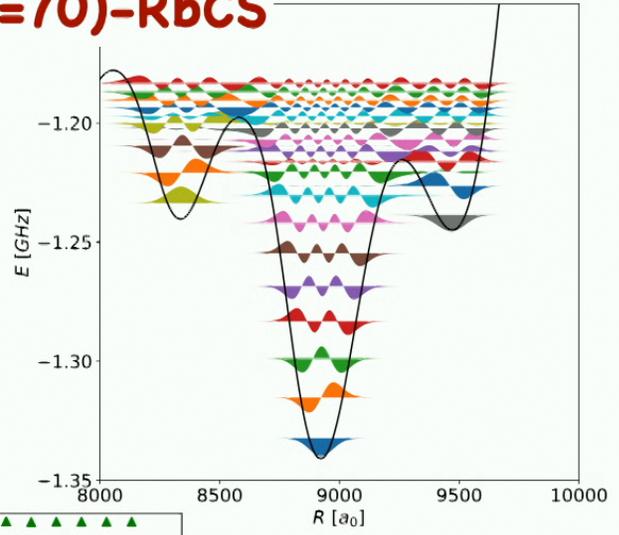
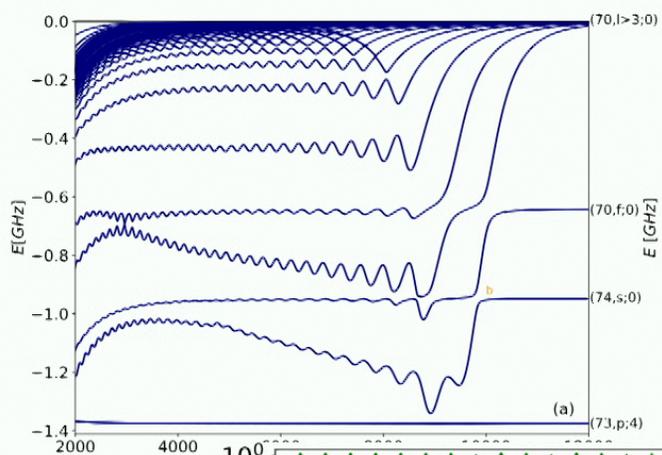
$$P = e^{-\frac{\pi \Delta E}{4 \hbar g v}}$$

$$g = \left| \langle \Phi_i | \frac{d}{dR} | \Phi_j \rangle \right|$$

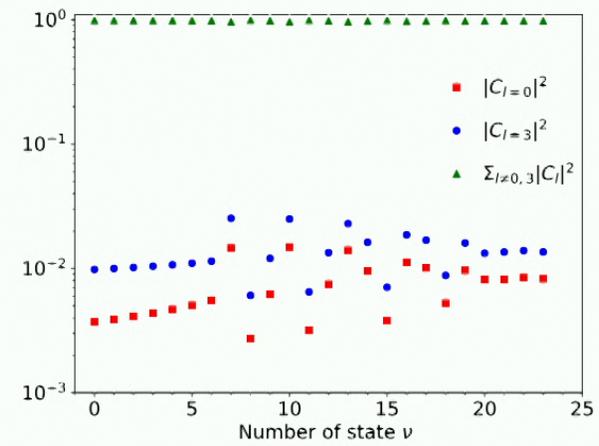
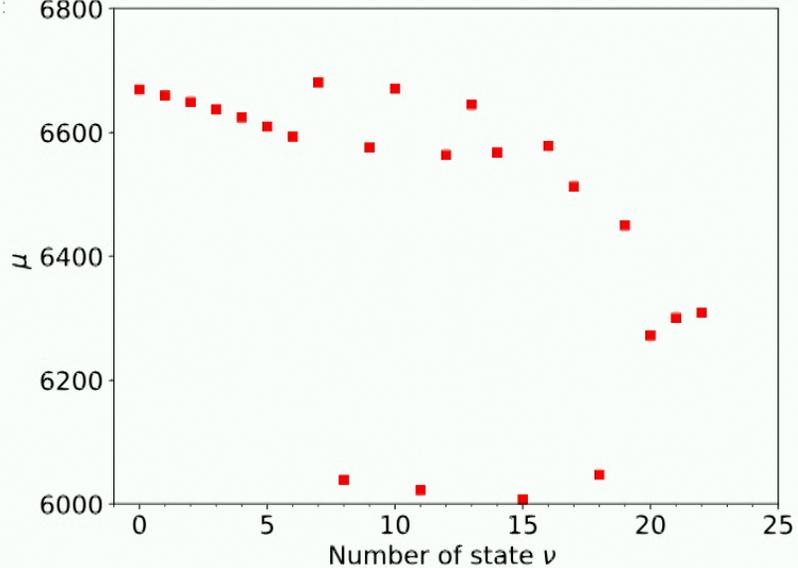
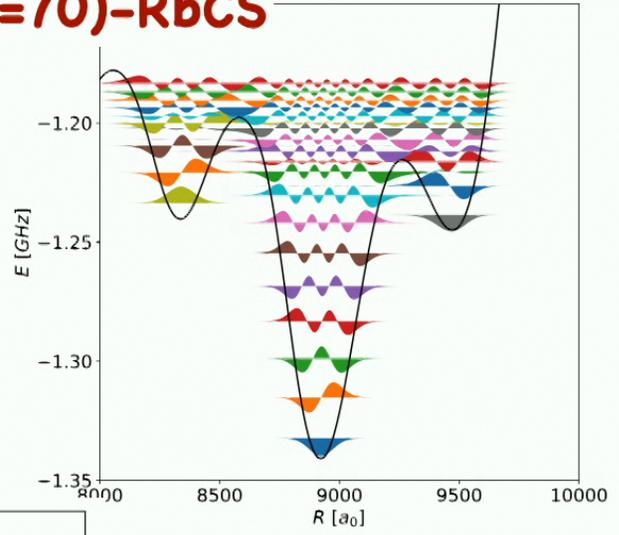
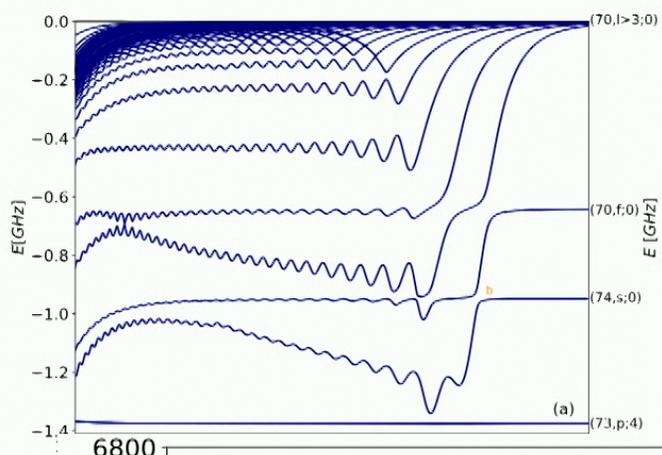
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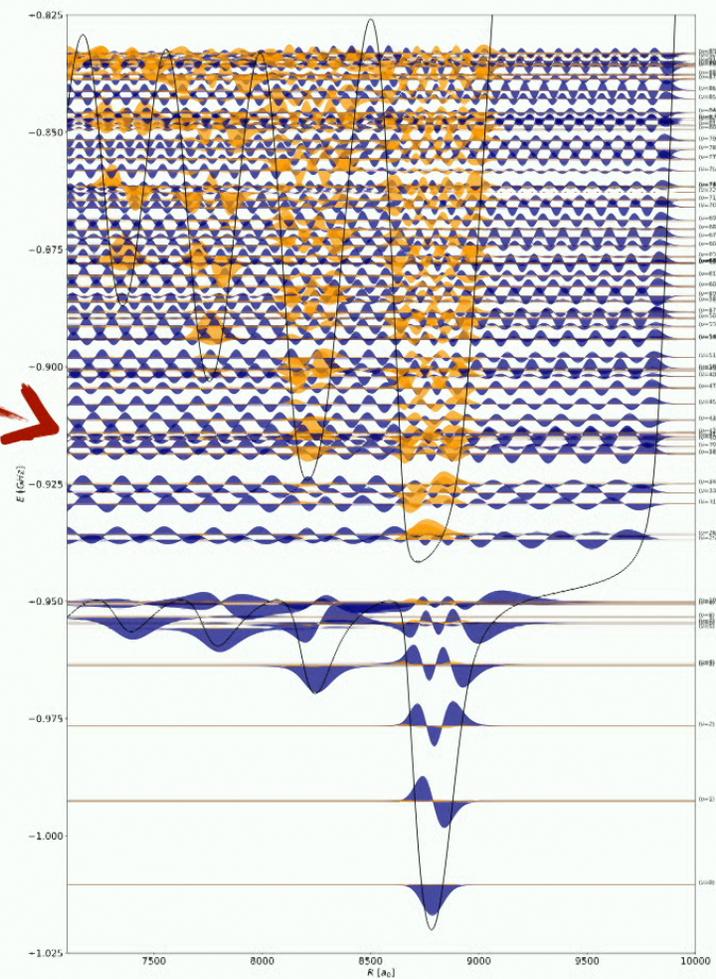
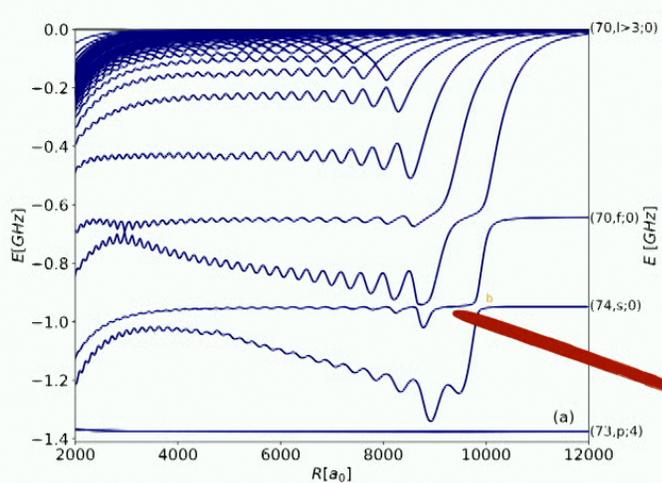
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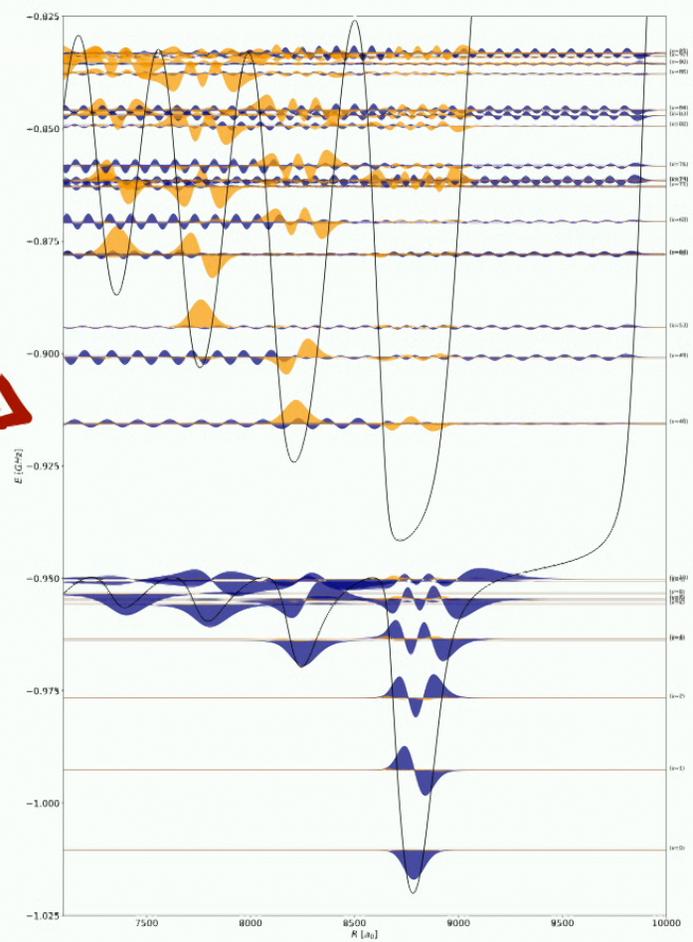
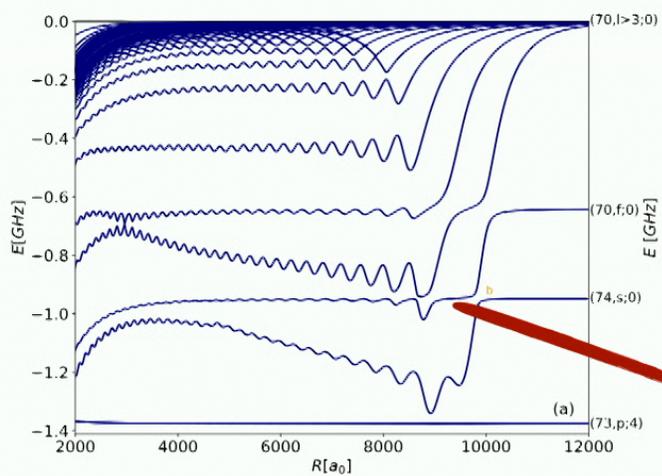
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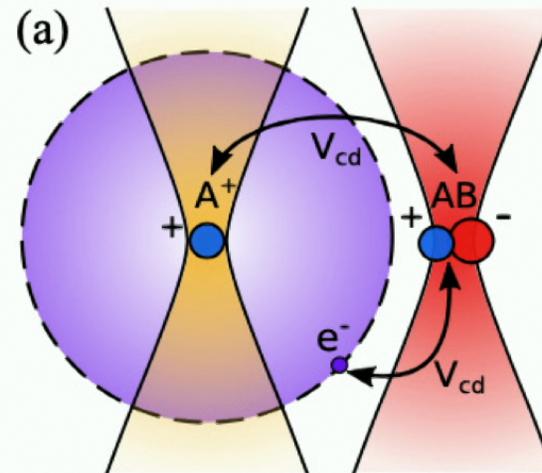
# Electronic structure of Cs(n=70)-RbCS



## Experimental setup

### RbCs rotational states

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 $d=1.25D$

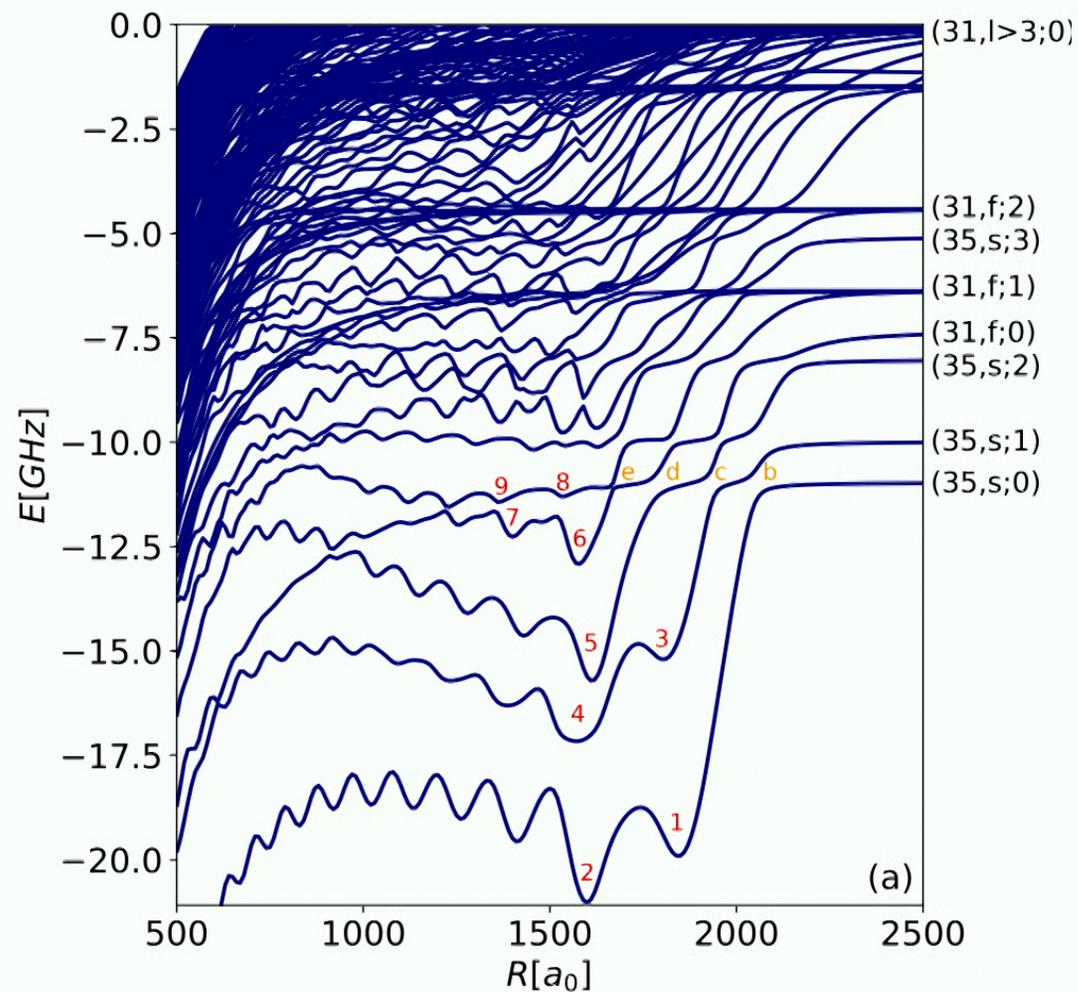


### Cesium Rydberg states

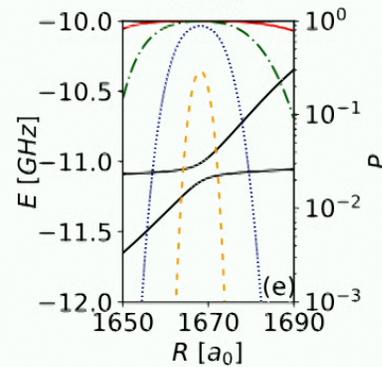
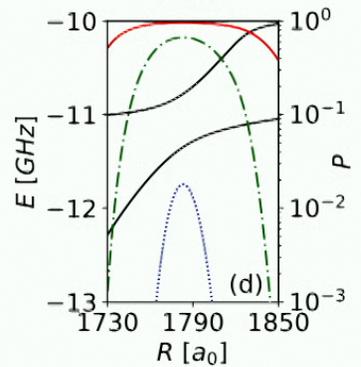
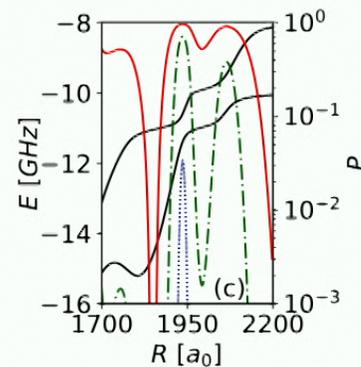
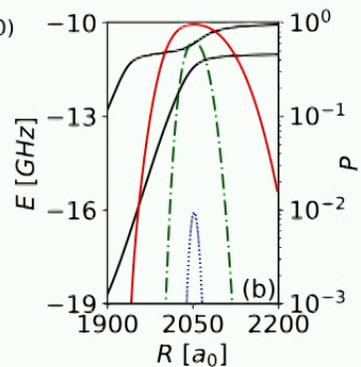
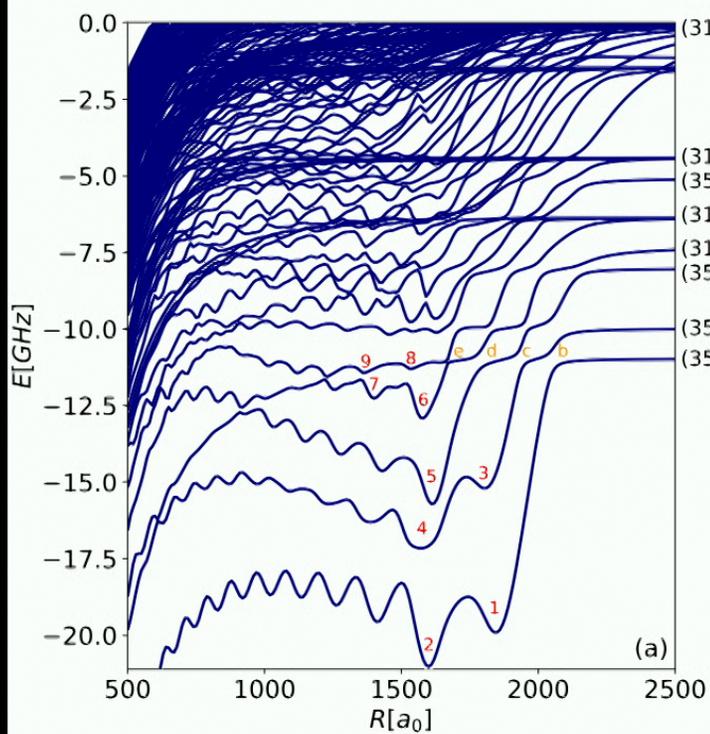
State	$E_{n,l} - E_{70,l \geq 4}$ [GHz]
Cs( $n = 70, l \geq 4$ )	0.000
Cs(70 <i>f</i> )	-0.642
Cs(74 <i>s</i> )	-0.948
Cs(72 <i>d</i> )	-9.124
Cs(73 <i>p</i> )	-11.175

State	$E_{n,l} - E_{31,l \geq 4}$ [GHz]
Cs( $n = 31, l \geq 4$ )	0.000
Cs(31 <i>f</i> )	-7.359
Cs(35 <i>s</i> )	-10.977
Cs(33 <i>d</i> )	-106.468
Cs(34 <i>p</i> )	-130.787

## Electronic structure of Cs( $n=31, l>3$ )-RbCS



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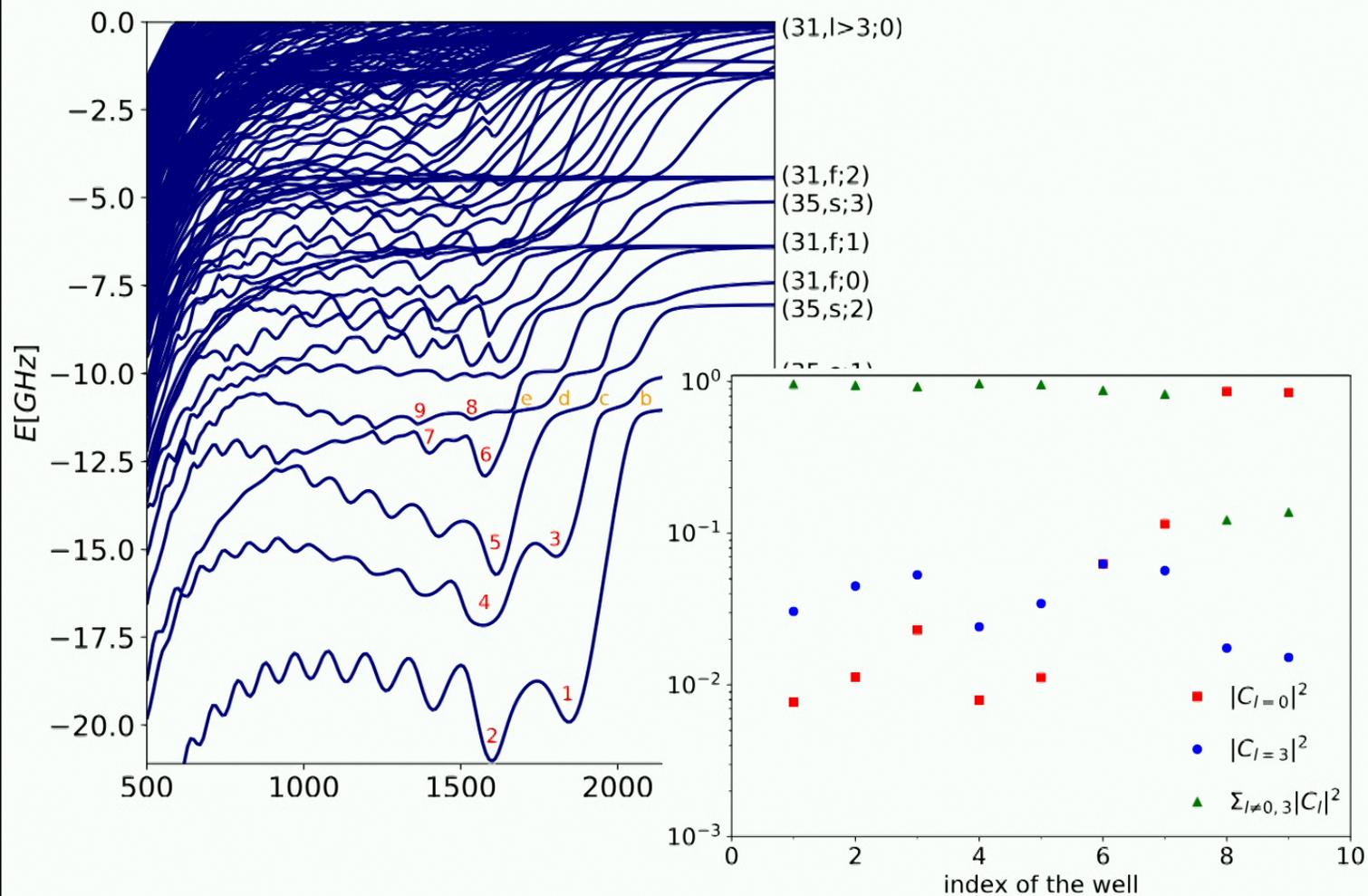


$$v = 2.2 \times 10^2, 2.2 \times 10^3, 2.2 \times 10^4 \text{ cms}^{-1}$$

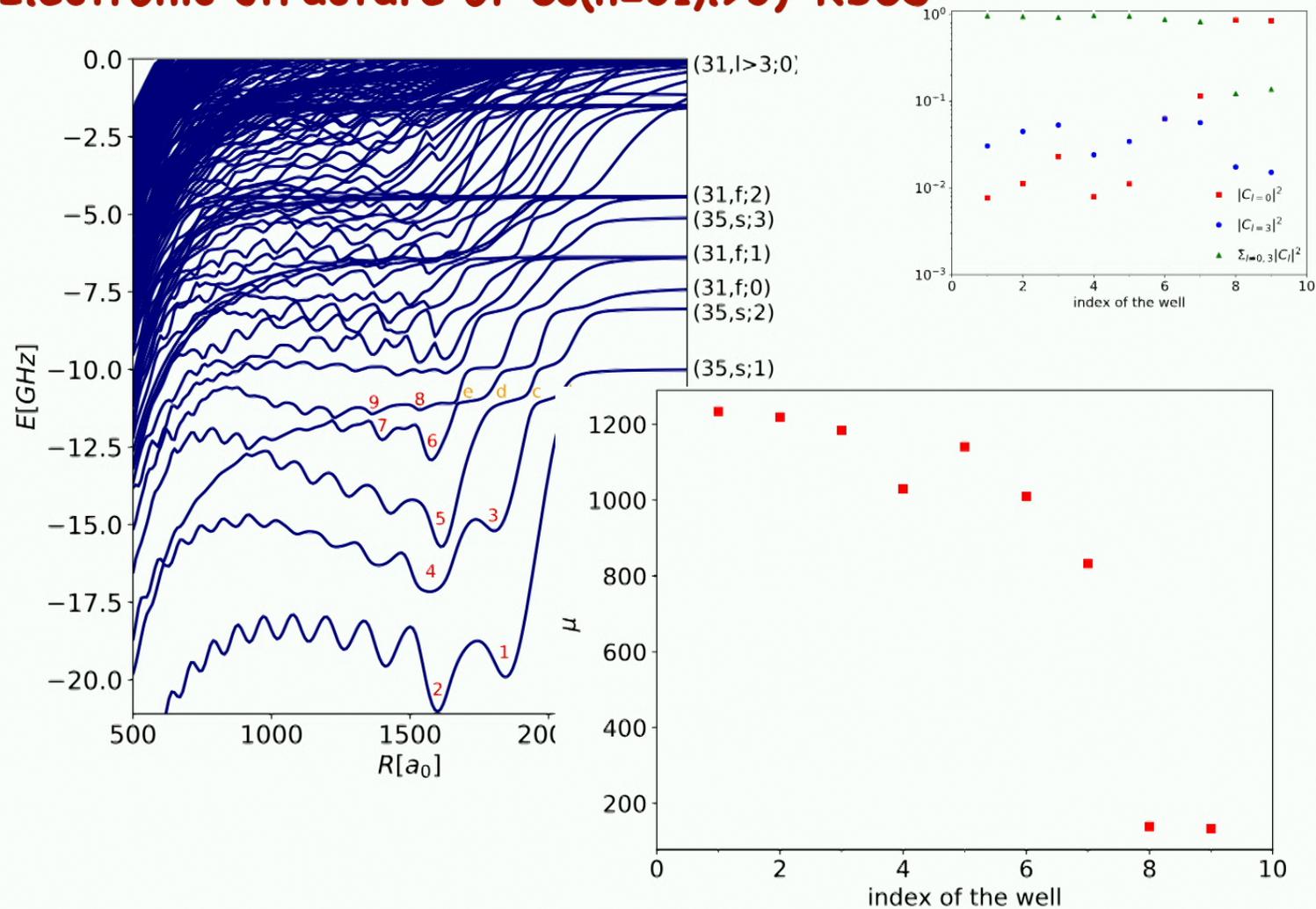
$$P = e^{-\frac{\pi \Delta E}{4 \hbar g v}}$$

$$g = \left| \langle \Phi_i | \frac{d}{dR} | \Phi_j \rangle \right|$$

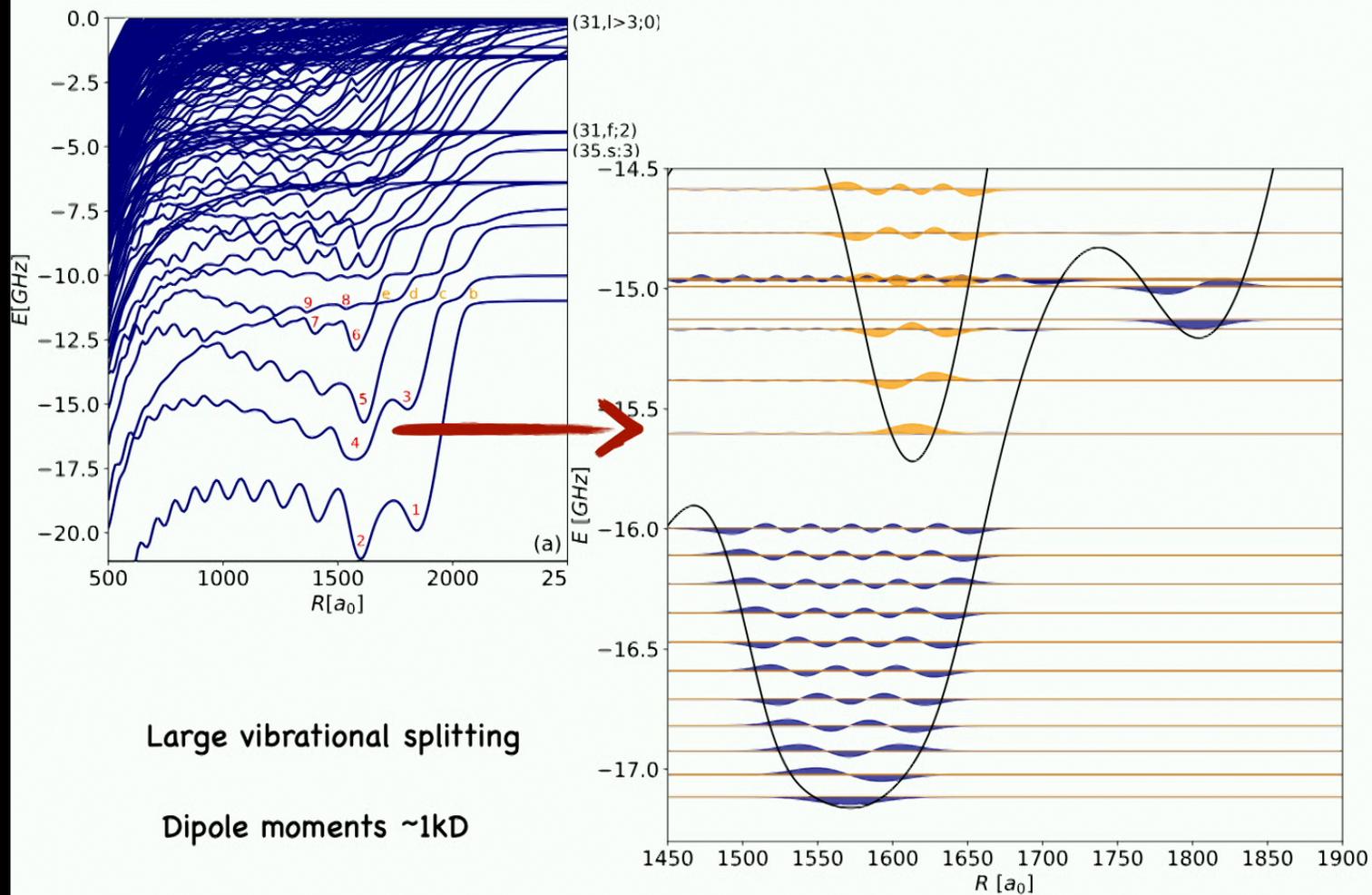
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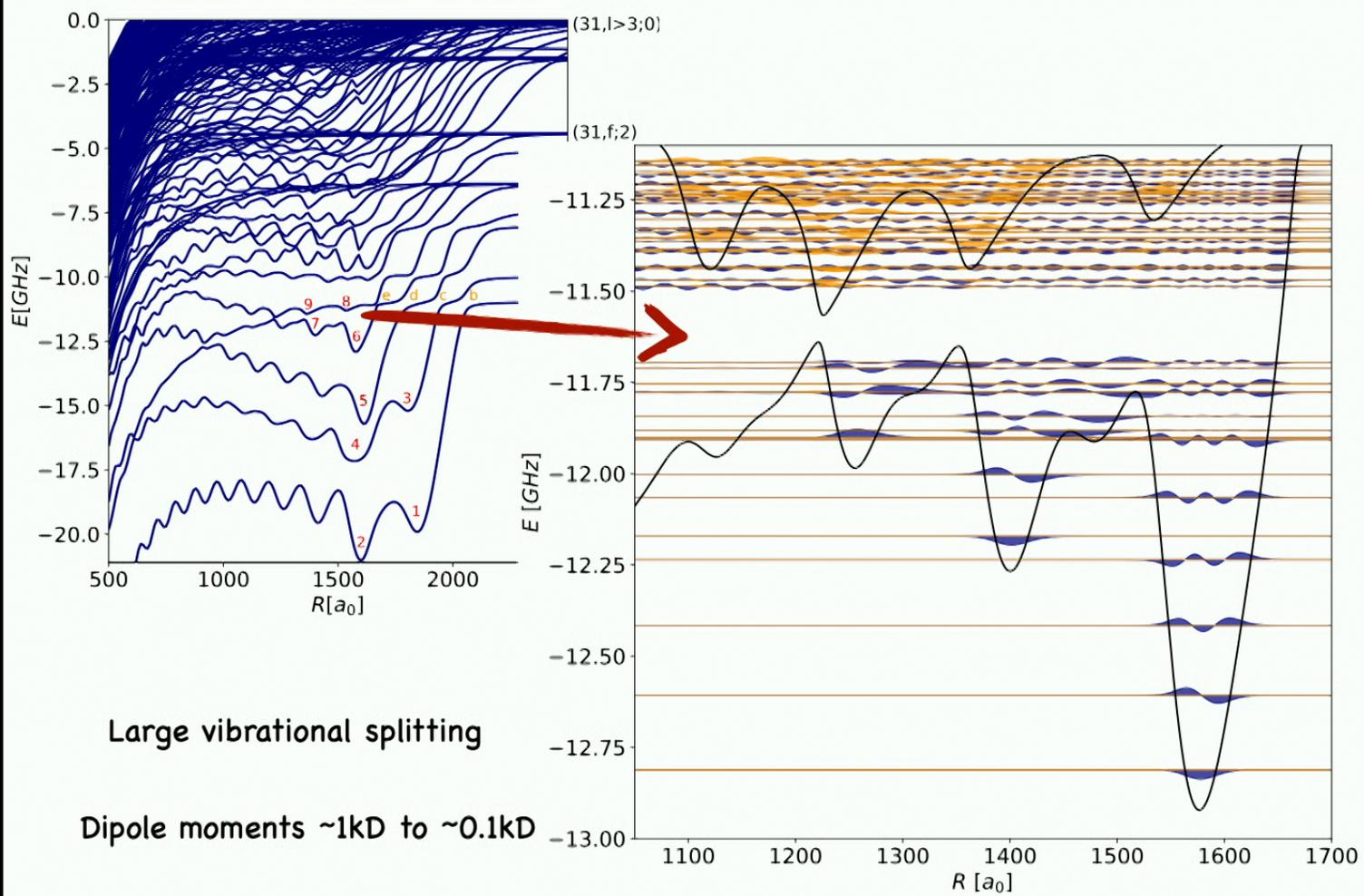
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## $\text{NO}(^2\Pi)$ - $\text{NO}(nI)$ bi-molecule

In March 2020 (!), we tried to find out if such molecules could exist

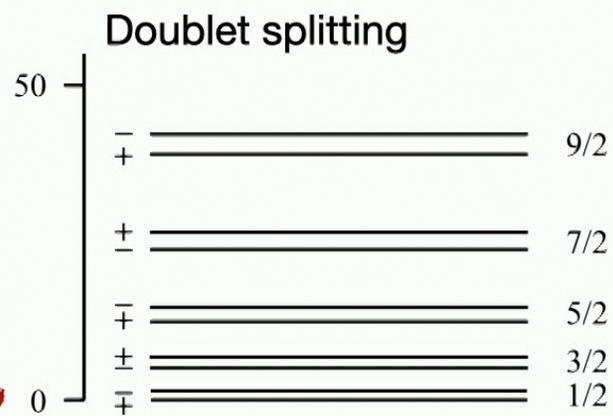
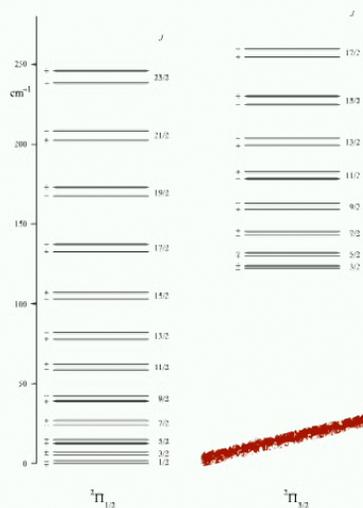
Hossein R. Sadeghpour



Janine Shertzer

# NO( $^2\Pi$ )

A simple (two-level)  $\Lambda$ -doublet molecule!

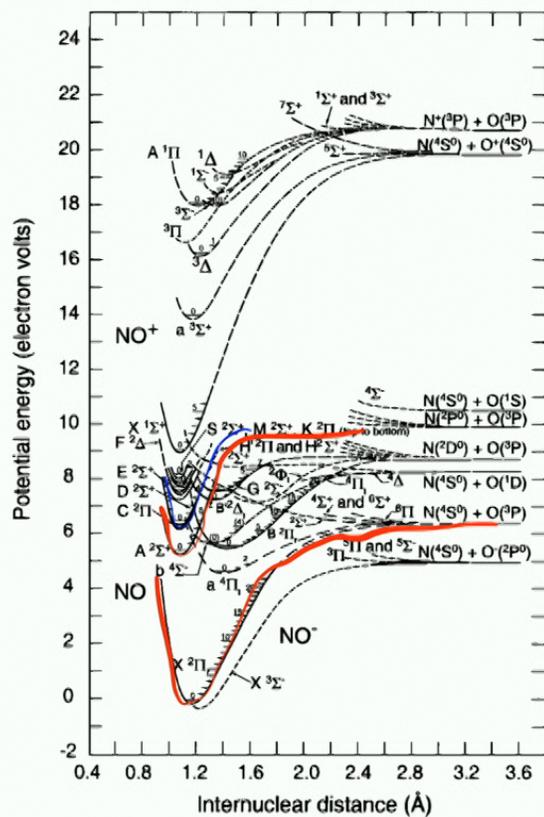


$$B = 50.848 \text{ GHz}$$

$$E_{\Lambda} = 205.95 \text{ MHz}$$

$$d = 0.15 D$$

$$H_{\text{NO}} = E_{+}|+\rangle\langle+| + E_{-}|-\rangle\langle-|$$



**NO\***

$A^2\Sigma^+$  ( $l=0$  94%,  $l=1$  1%,  $l=2$  5%)

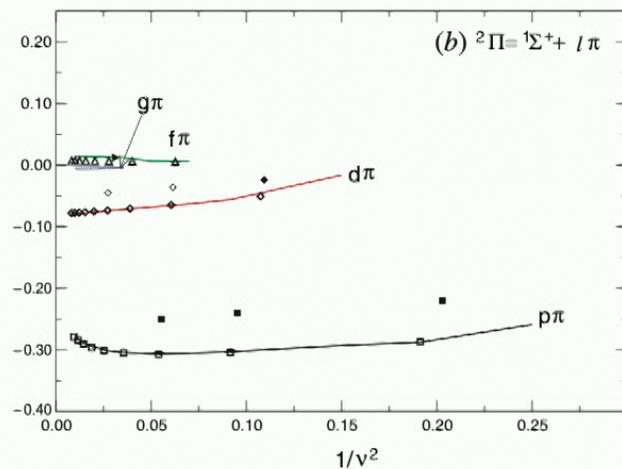
$np, nf$  ( $\Delta N = 0, 2$ ) excitations

$ng$  near  $NO^+(X^1\Sigma)$

$NO(ng)$  states are longest lived;  
fraction of  $\mu s$  (R. Field 2022)

NO\*

## NO quantum defects



M.Hiyama & M. S. Child JPB **35**, 1337 (2002)



J. Phys. B: At. Mol. Opt. Phys. **29** (1996) 3747–3761. Printed in the UK

### *R*-matrix calculation of the bound and continuum states of the $e^-$ -NO $^+$ system

I Rabadán and J Tennyson†  
Department of Physics and Astronomy, University College London, Gower Street, London WC1E 6BT, UK

$$E_{nl} = \frac{Ry}{(n - \mu_l)^2}$$

INSTITUTE OF PHYSICS PUBLISHING JOURNAL OF PHYSICS B: ATOMIC, MOLECULAR AND OPTICAL PHYSICS  
J. Phys. B: At. Mol. Opt. Phys. **36** (2003) 4547–4559 PII: S0951-4075(03)66009-8

### *Ab initio R*-matrix/multi-channel quantum defect theory study of nitric oxide: II. Analysis of valence/Rydberg interactions

Miyabi Hiyama and Mark S Child  
Physical and Theoretical Chemistry Laboratory, South Parks Road, Oxford OX1 3QZ, UK

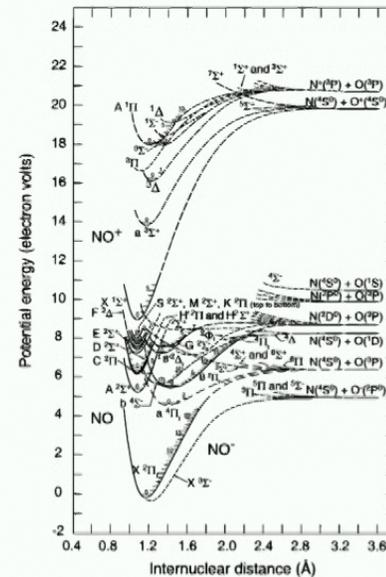
We're interested in high- $l$  (longer lifetimes),  
and not the core penetrating  $l$  states

$$H = H_{\text{Ryd}} + H_{\text{NO}} + H_{e\text{-NO}}$$

$$H_{\text{NO}} = E_+ |+\rangle\langle +| + E_- |-\rangle\langle -|$$

NO Rydberg molecular potent

$$U_{n\Lambda}(R_{\text{NO}}) = U^+(R_{\text{NO}}) - \frac{1}{2(n - \mu_\Lambda)^2}$$



NO( $X^2\Pi$ ) has electron affinity (EA)

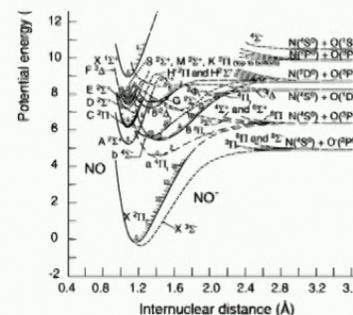
$$EA = NO^-(^3\Sigma, \nu = 0, J = 0) - NO(^2\Pi, \nu = 0, J = 0) = 33 \text{ meV}$$

$$a_S(0) = -\tan(\delta_S(k))/k \quad \text{Scattering length}$$

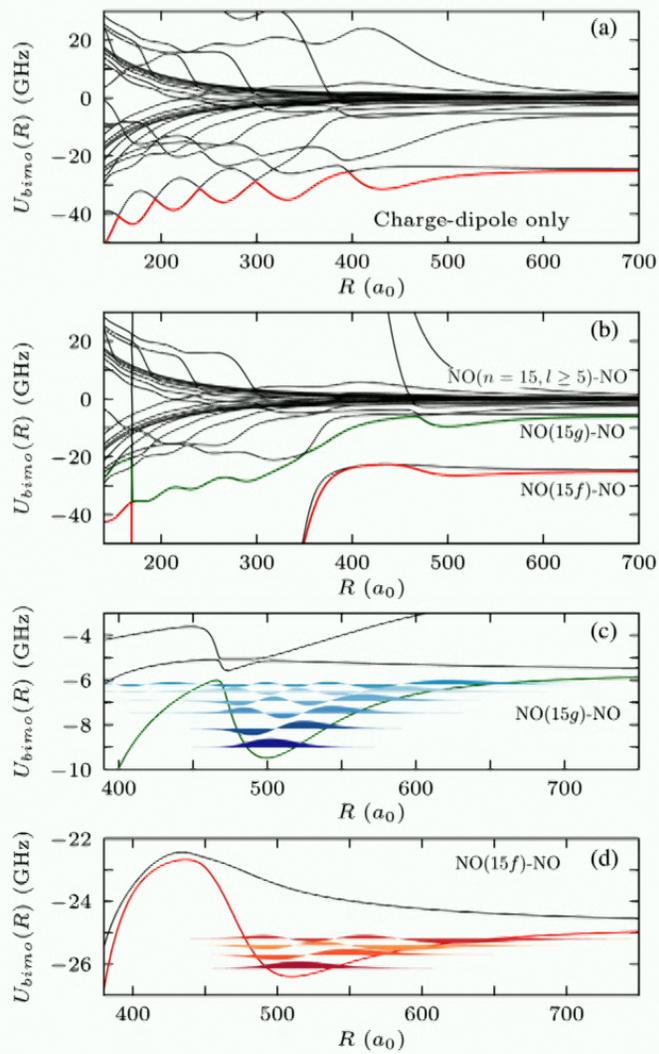
resonance in elastic channel



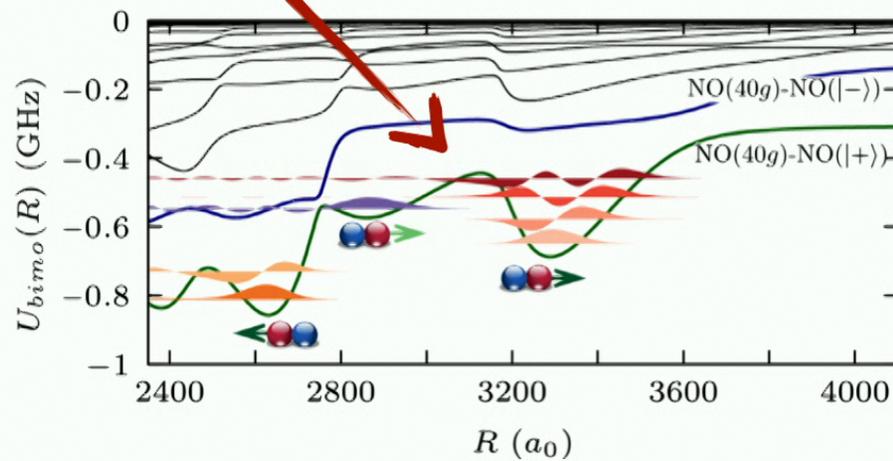
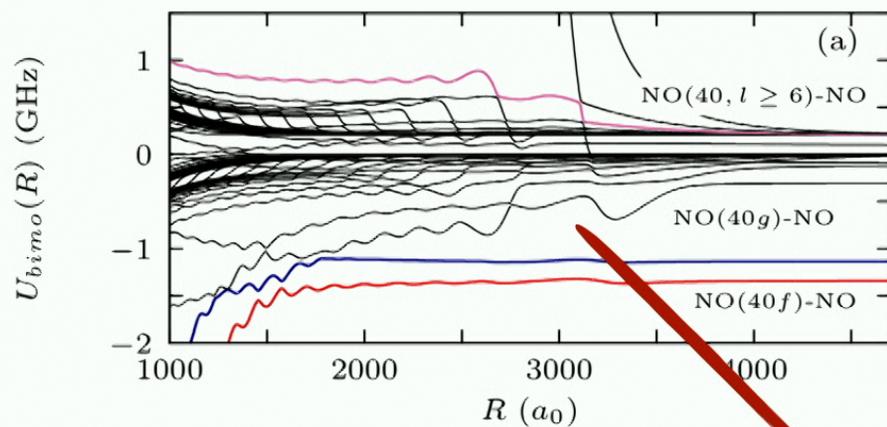
$$a_P^3(0) = -\tan(\delta_P(k))/k^3 \quad \text{Scattering volume}$$



$NO(nf, ng) - NO(X^2\Pi_{1/2})$



# $NO(nf, ng) - NO(X^2\Pi_{1/2})$



$$B_{NONO^*} = 0.1 - 1 \text{ MHz}$$

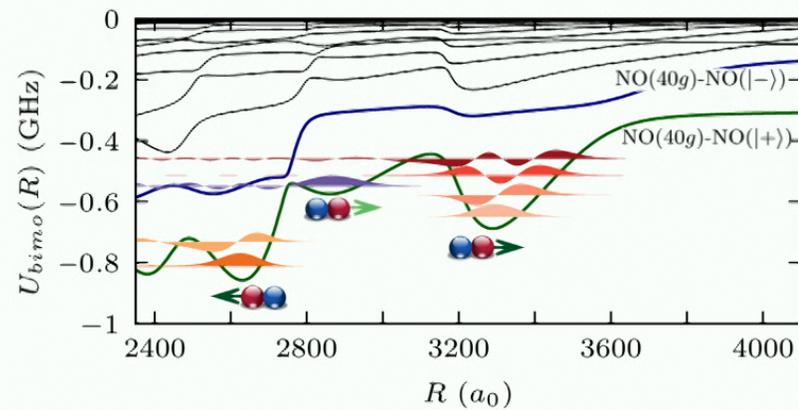
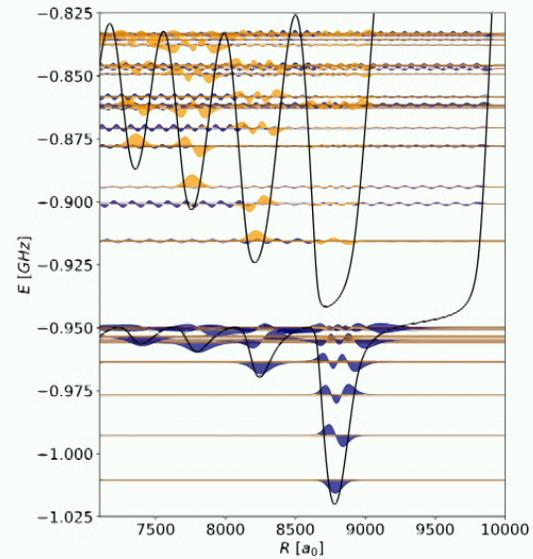
## Conclusions

Rydberg molecules:  
Rb-KRb (K.K Ni, Harvard)  
Cs-RbCs (S. Cornish, Durham)

RGF, et al JPB **53**, 074002 (2020),  
PRA **96**, 052509 (2017),  
New J. Phys. **17**, 013021 (2015)

Rydberg bimolecules: NO-NO  
T. Pfau & H. Kübler, Stuttgart

RGF, J. Shertzer, H.R. Sadeghpour, PRL **126**, 043401 (2021)



# **EGAS 54**

**54th European Group on Atoms System Conference**

**19-23 June, 2023**

**Strasbourg, France**

**Organized by Guido Pupillo and his team**

# Gracias

