Title: Quantum steampunk: Quantum information meets thermodynamics

Speakers: Nicole Yunger Halpern

Series: Colloquium

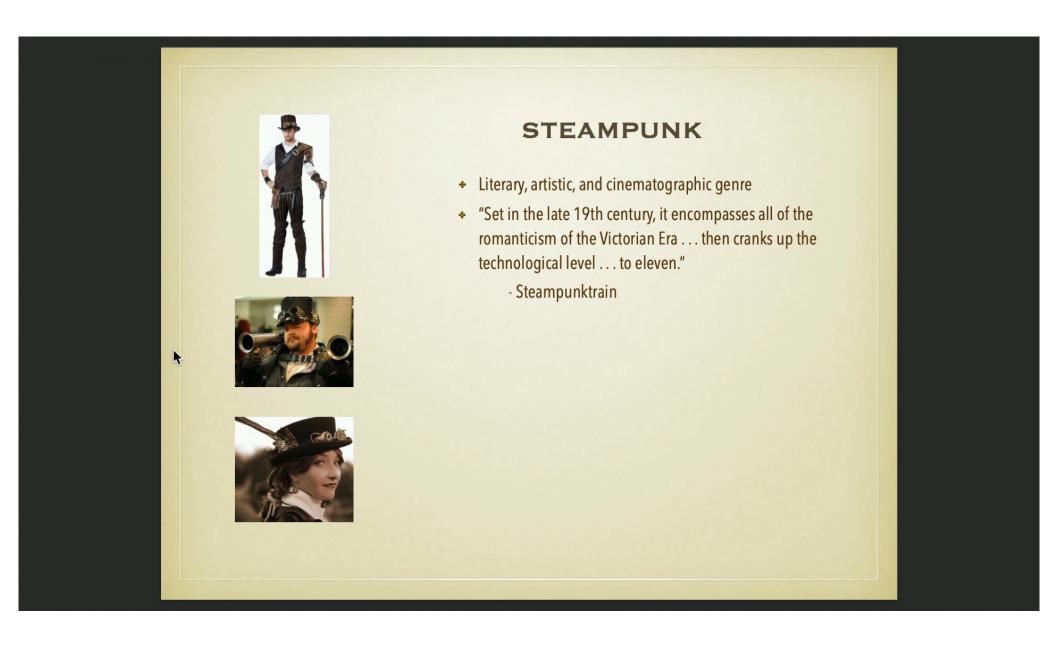
Date: May 18, 2022 - 2:00 PM

URL: https://pirsa.org/22050002

Abstract: Thermodynamics has shed light on engines, efficiency, and time's arrow since the Industrial Revolution. But the steam engines that powered the Industrial Revolution were large and classical. Much of today's technology and experiments are small-scale, quantum, far from equilibrium, and processing information. Nineteenth-century thermodynamics needs re-envisioning for the 21st century. Guidance has come from the mathematical toolkit of quantum information theory. Applying quantum information theory to thermodynamics sheds light on fundamental questions (e.g., how does entanglement spread during quantum thermalization? How can we distinguish quantum heat from quantum work?) and practicalities (e.g., quantum engines and the thermodynamic value of coherences). I will overview how quantum information theory is being used to revolutionize thermodynamics in quantum steampunk, named for the steampunk genre of literature, art, and cinema that juxtaposes futuristic technologies with 19th-century settings.

Zoom Link: https://pitp.zoom.us/j/92454766615?pwd=QzZXMnYwN3ZZOTE5RzZEcHp6TkhMdz09

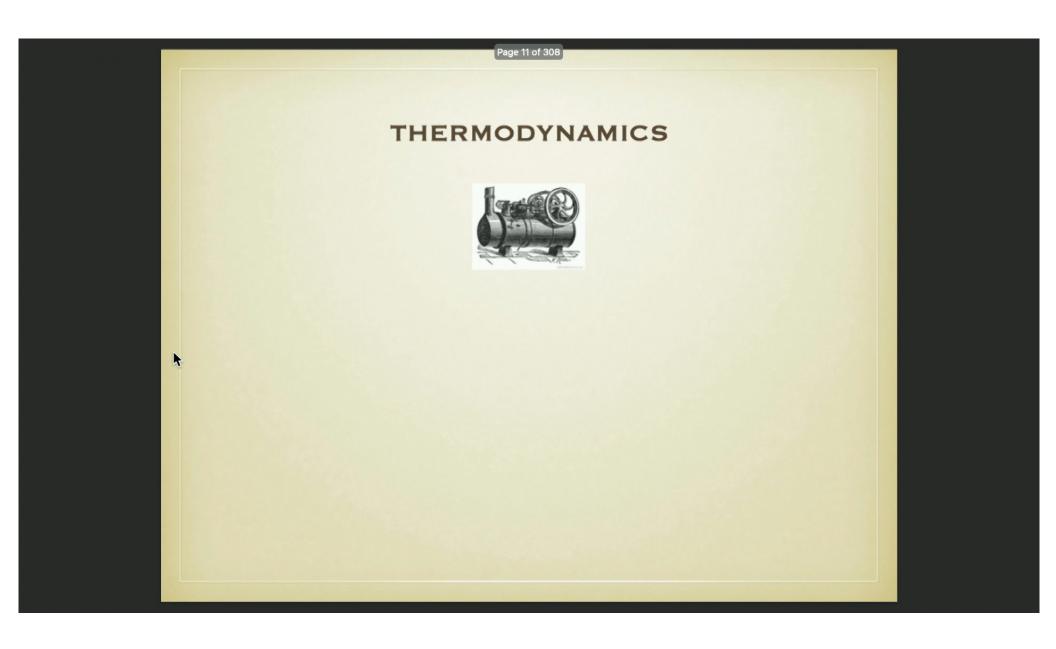
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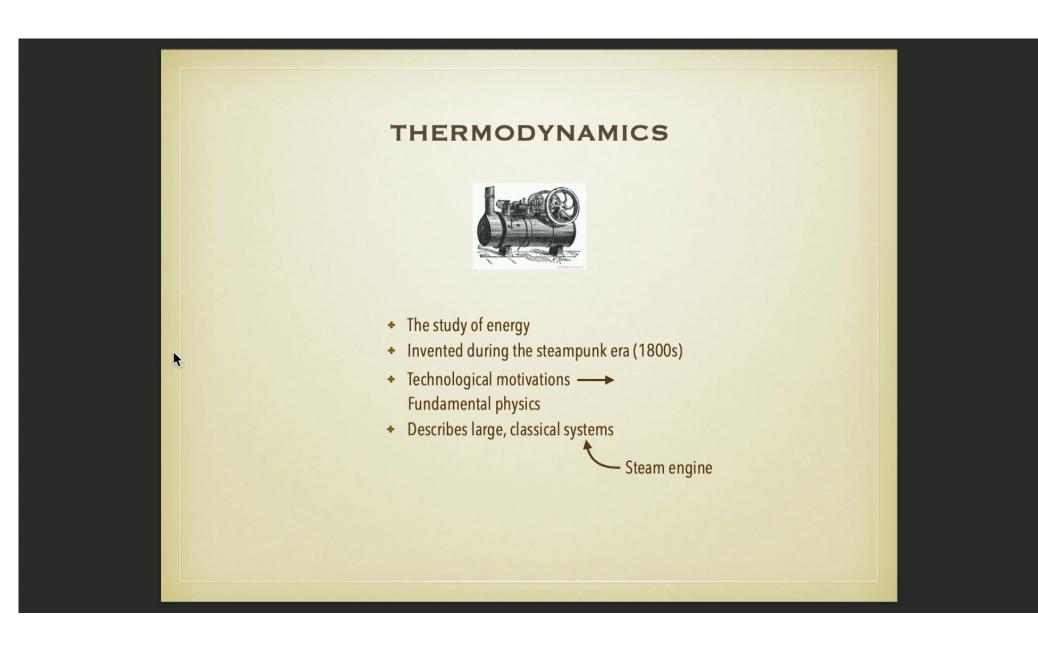
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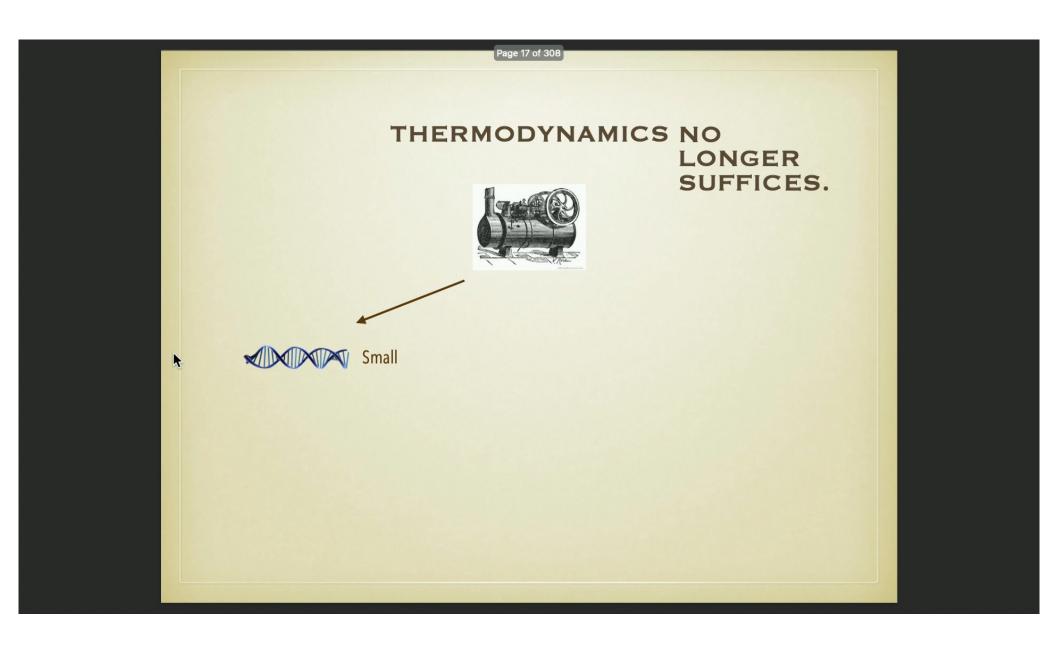
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THERMODYNAMICS • The study of energy • Invented during the steampunk era (1800s)

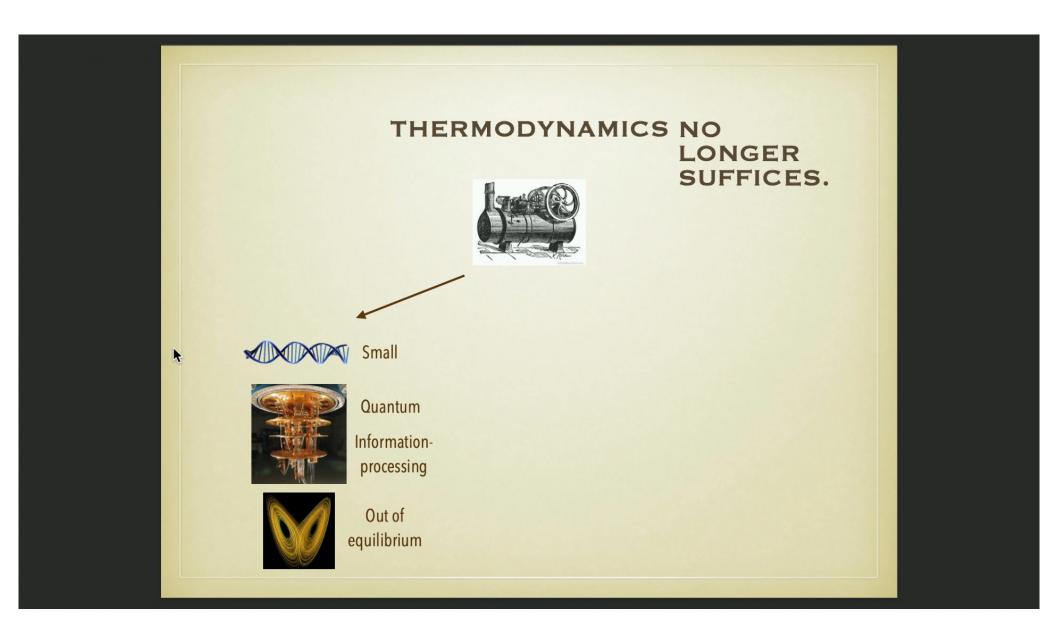
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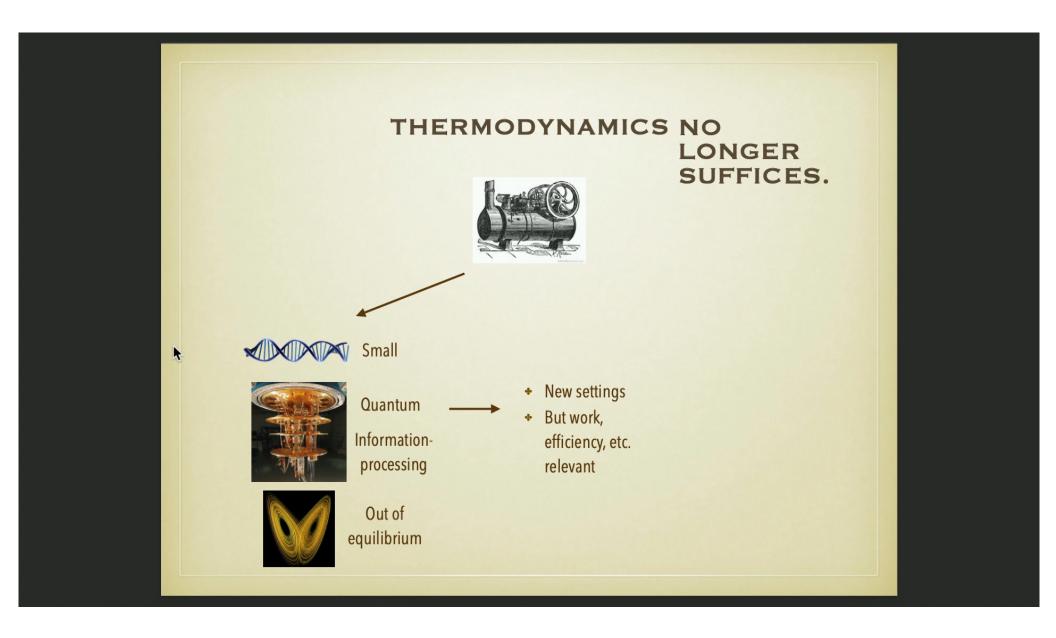
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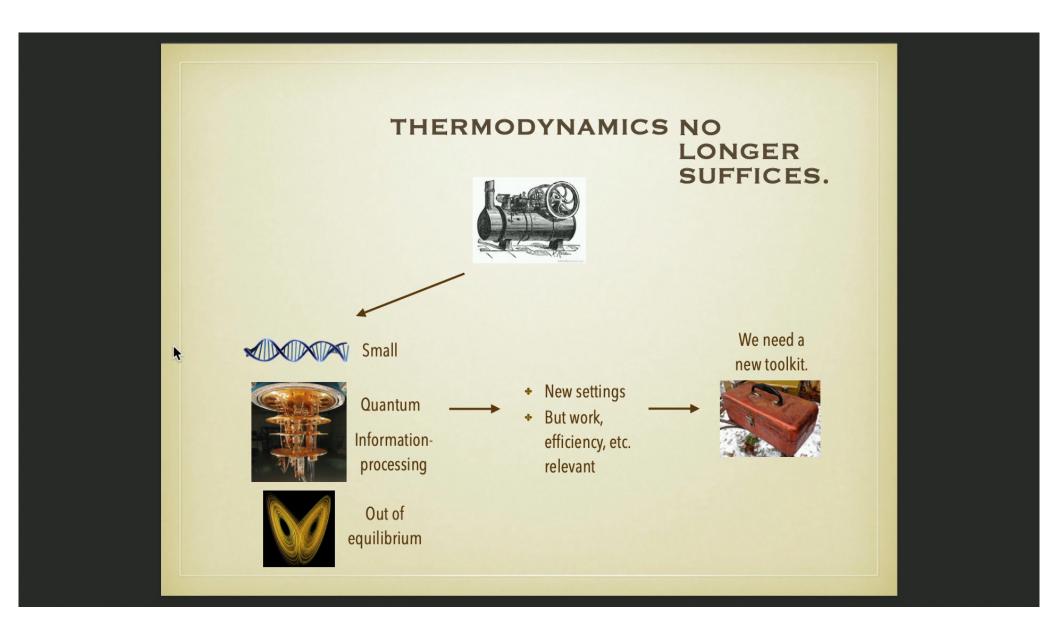
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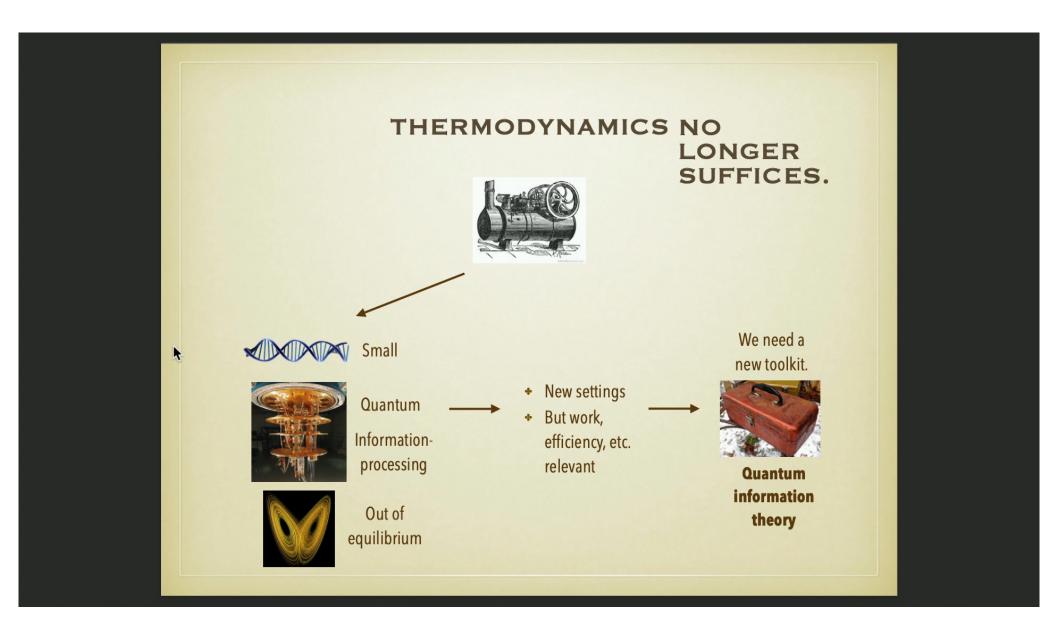
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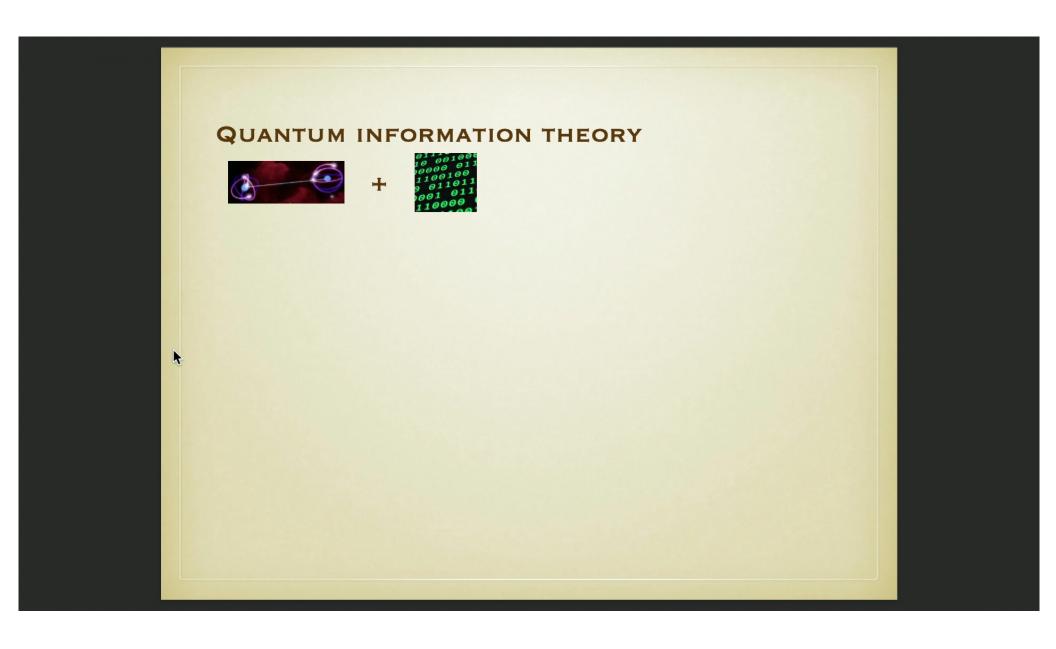
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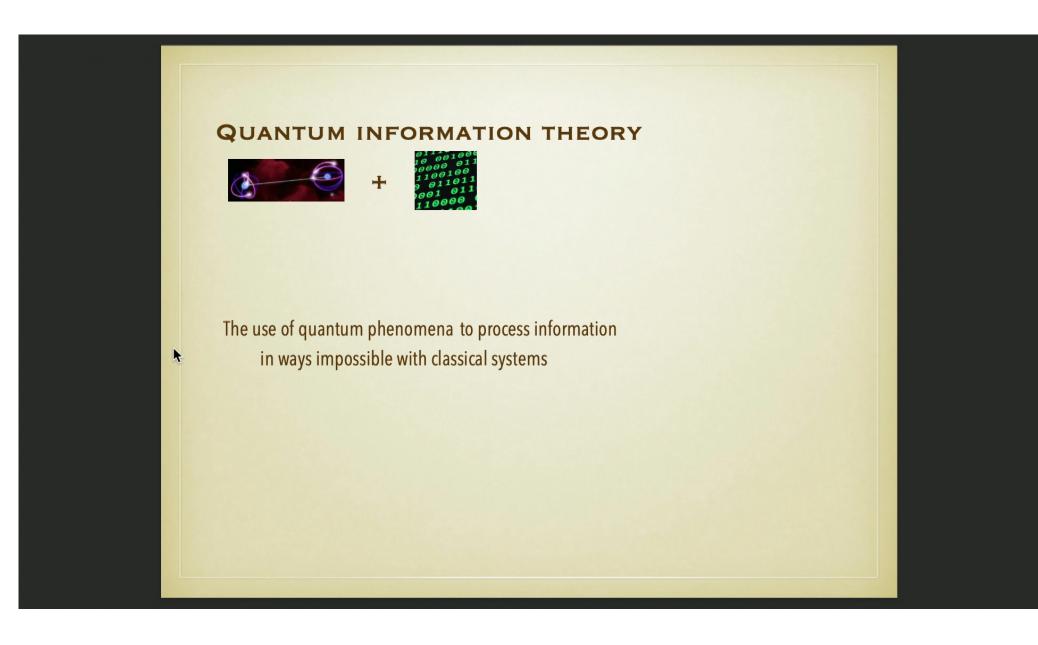
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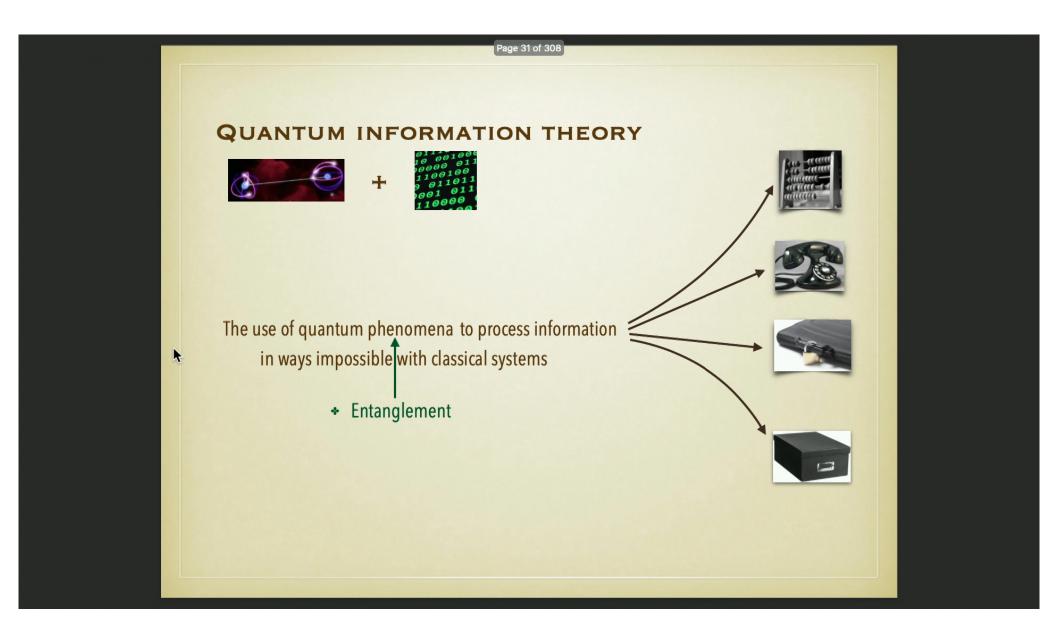
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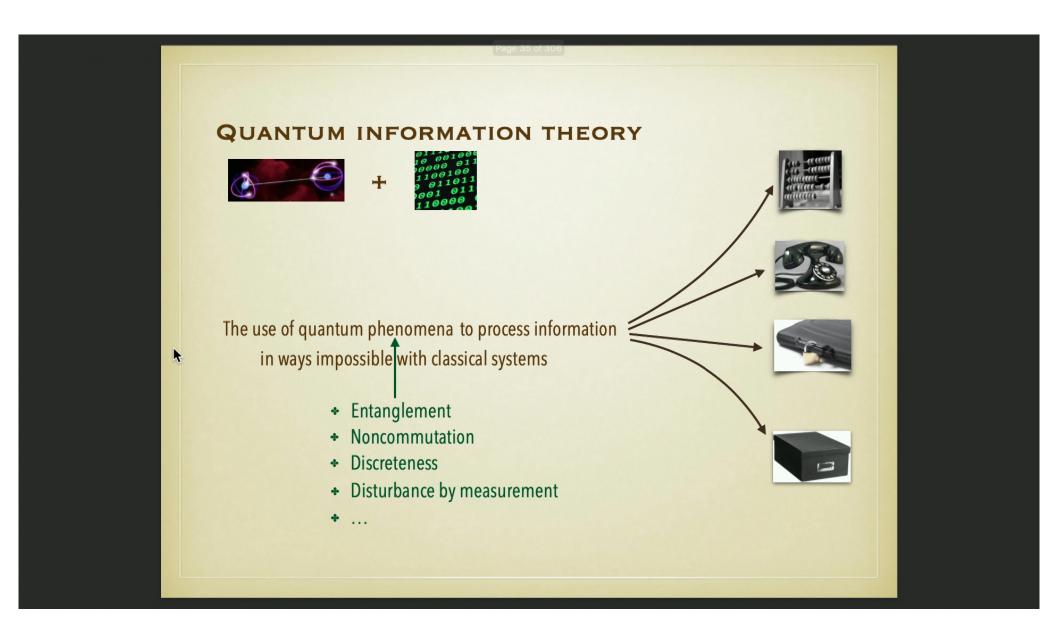
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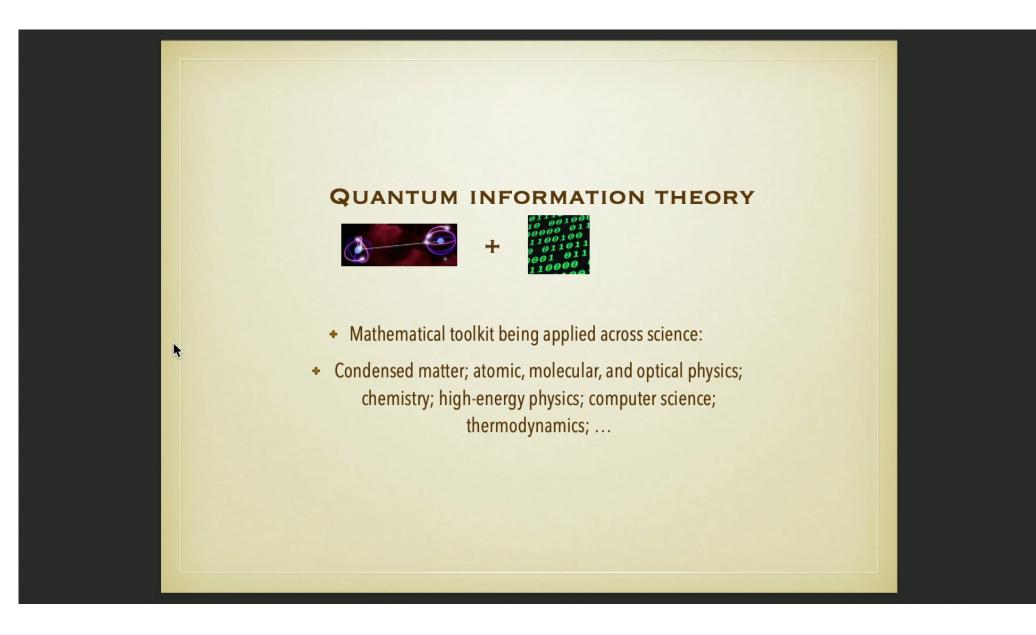
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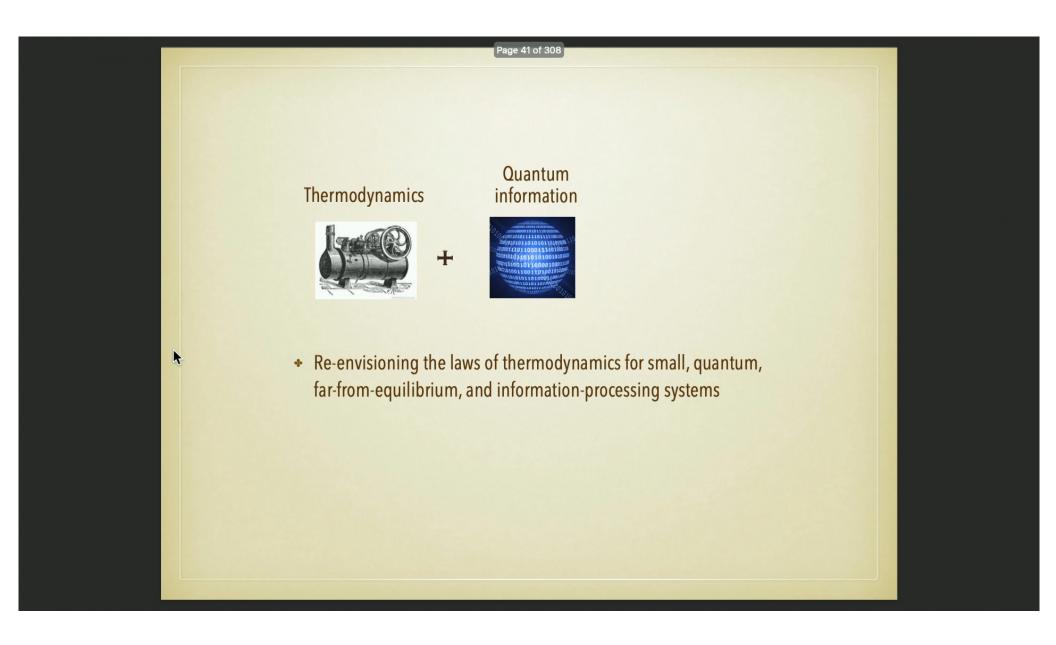
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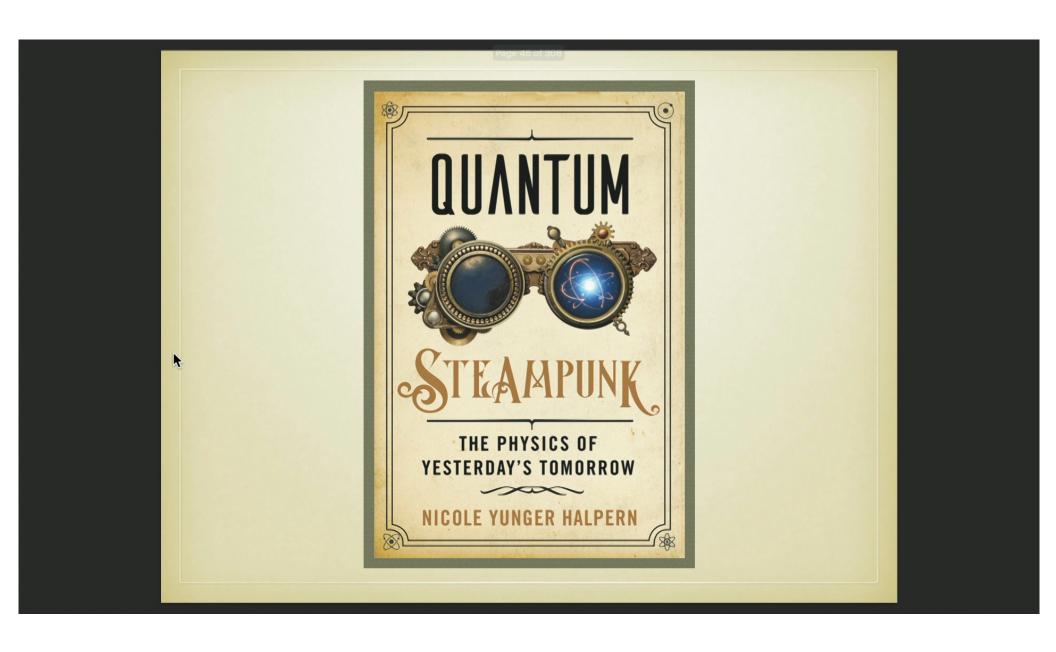
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Quantum Thermodynamics information Re-envisioning the laws of thermodynamics for small, quantum, far-from-equilibrium, and information-processing systems How can nonclassical resources enhance thermodynamic tasks? Which features of thermodynamics are truly nonclassical?

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Quantum Quantum steampunk Thermodynamics information Re-envisioning the laws of thermodynamics for small, quantum, far-from-equilibrium, and information-processing systems How can nonclassical resources enhance thermodynamic tasks? Which features of thermodynamics are truly nonclassical?

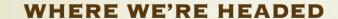
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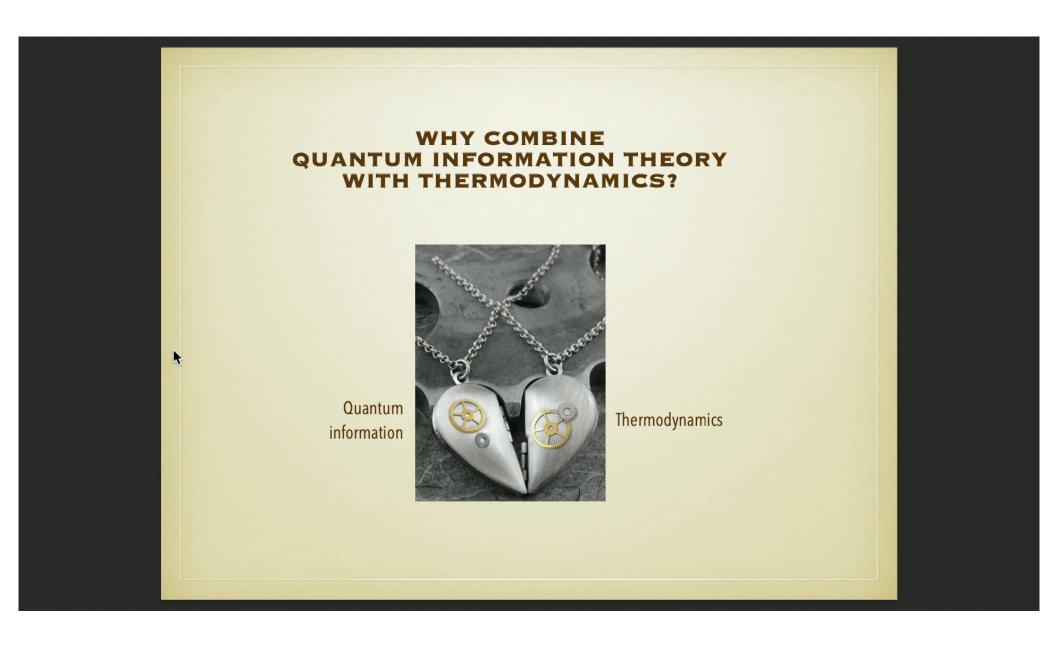
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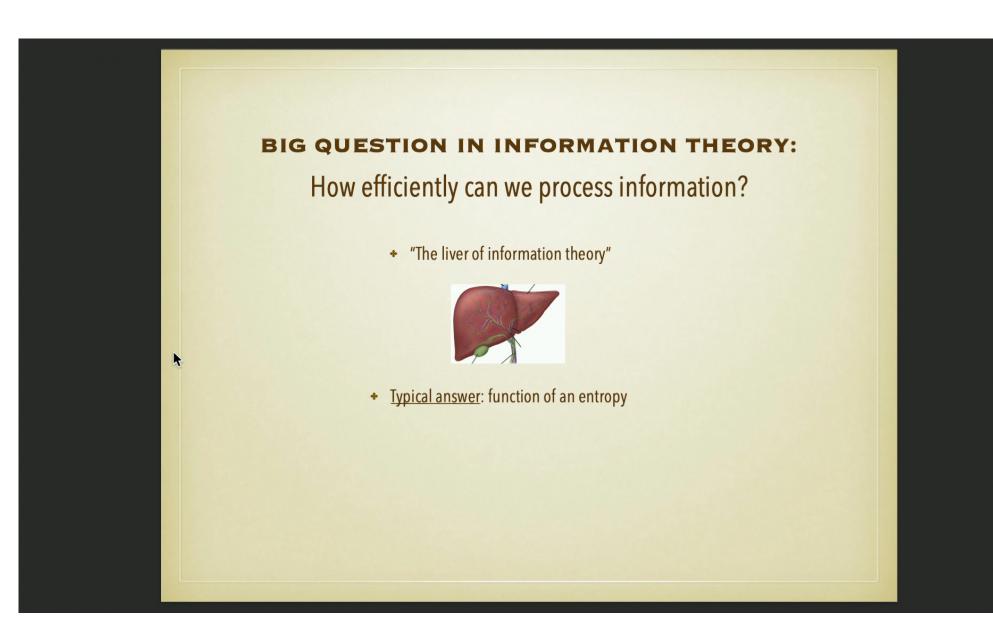


- Why quantum information theory + thermodynamics?
- Work and information as resources in thermodynamics and computation
- Quantum many-body engine —>
 - NYH, White, Gopalakrishnan, and Refael, Phys. Rev. B 99, 024203 (2019).

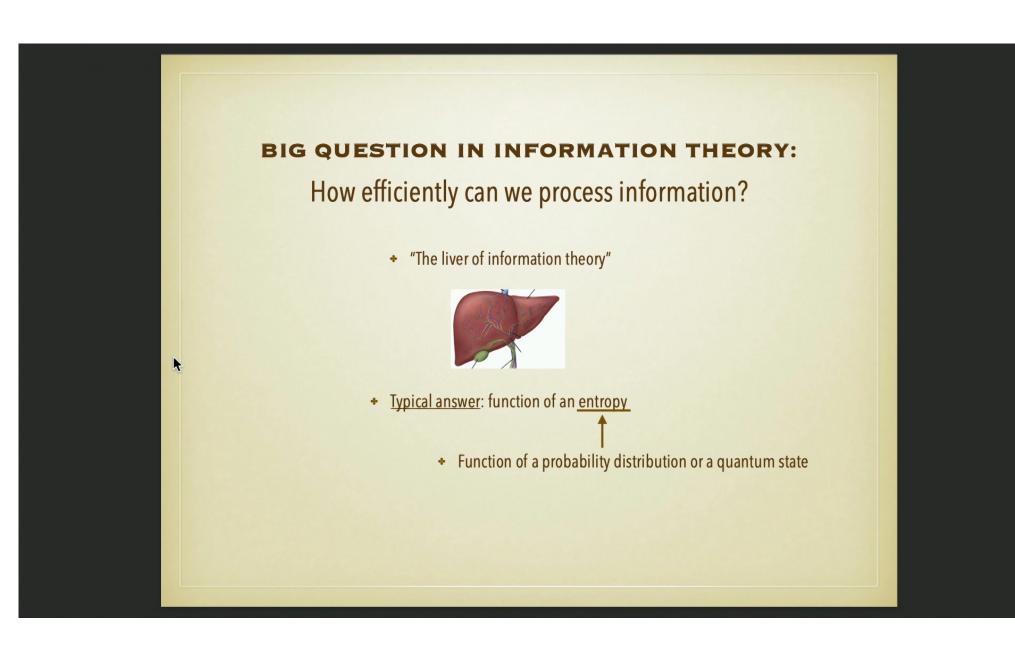
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How efficiently can we process information?

"The liver of information theory"



* Typical answer: function of an entropy



- Function of a probability distribution or a quantum state
- Quantifies the uncertainty in the outcome of a measurement

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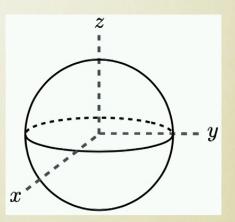
QUICK REVIEW: QUBITS * Basic units of quantum information Quantum analogues of bits: 0 Quantum 2-level systems • Example: spin degree of freedom with s = 1/2

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QUICK REVIEW: QUBIT STATES

- + 1
- Density operator (matrix)
- Trace-1 positive-semidefinite linear operator
- **Pure** state: $\rho = |\psi\rangle\langle\psi|$
 - Vector in Hilbert space
 - Arrow meets the Bloch sphere

Bloch sphere



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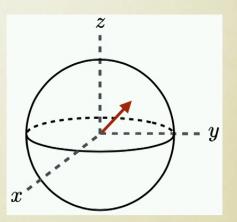
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- Mixed state
 - Can't be expressed as a ket $|\psi\rangle$
 - Is the state of an entangled quantum system
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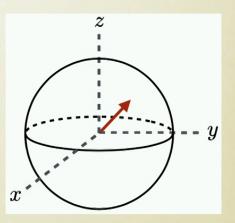
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 - * Example: quantum thermal state, $\exp(-\beta H)/Z$

Bloch sphere





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- * $|a\rangle, |b\rangle, ...$
- Probabilities: p_a, p_b, \dots
- * Quantum state: $\rho = \sum_{j} p_{j} |j\rangle\langle j|$ * \longrightarrow n copies of $\rho \longrightarrow \rho^{\otimes n}$
- ◆ Into how few qubits can I squeeze the total message? → data compression

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- * Schumacher's theorem:

In the limit as $n \to \infty$, the number of qubits required per copy of ρ equals

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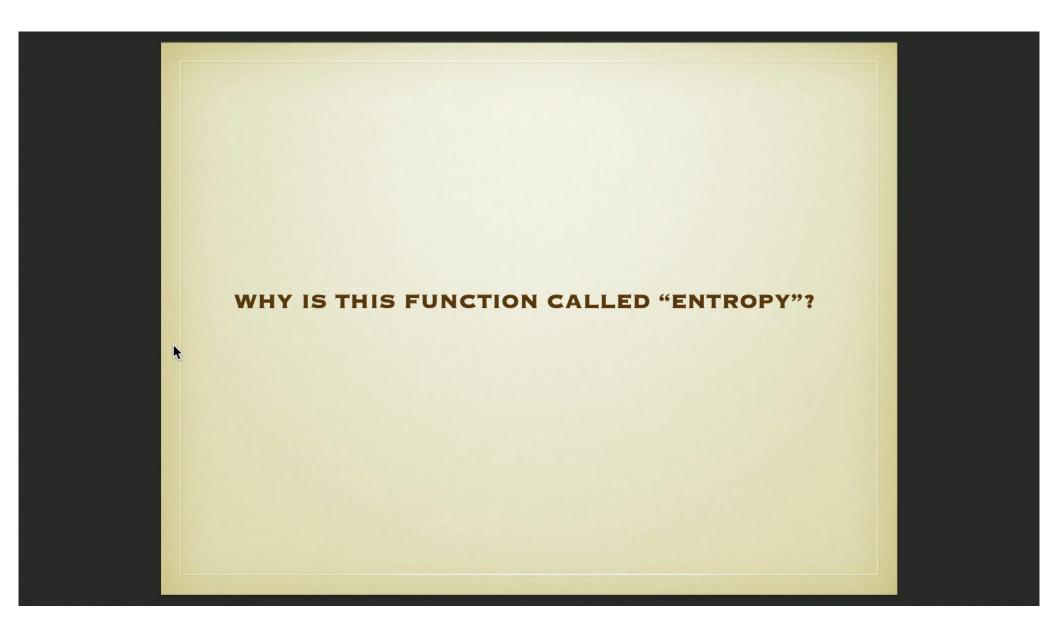
von Neumann entropy

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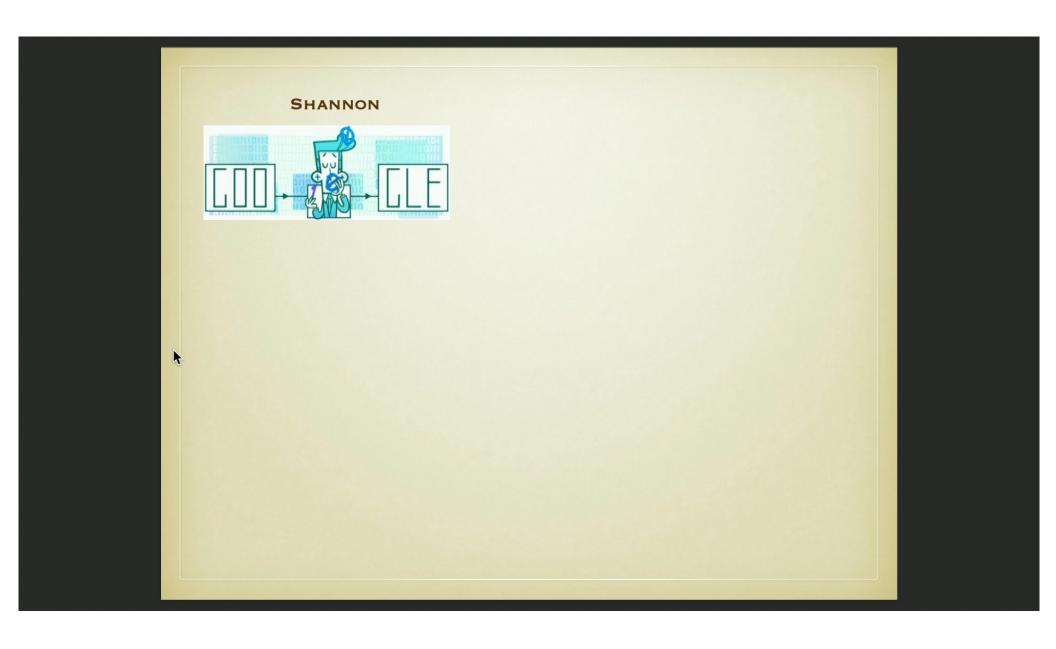
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von Neumann entropy



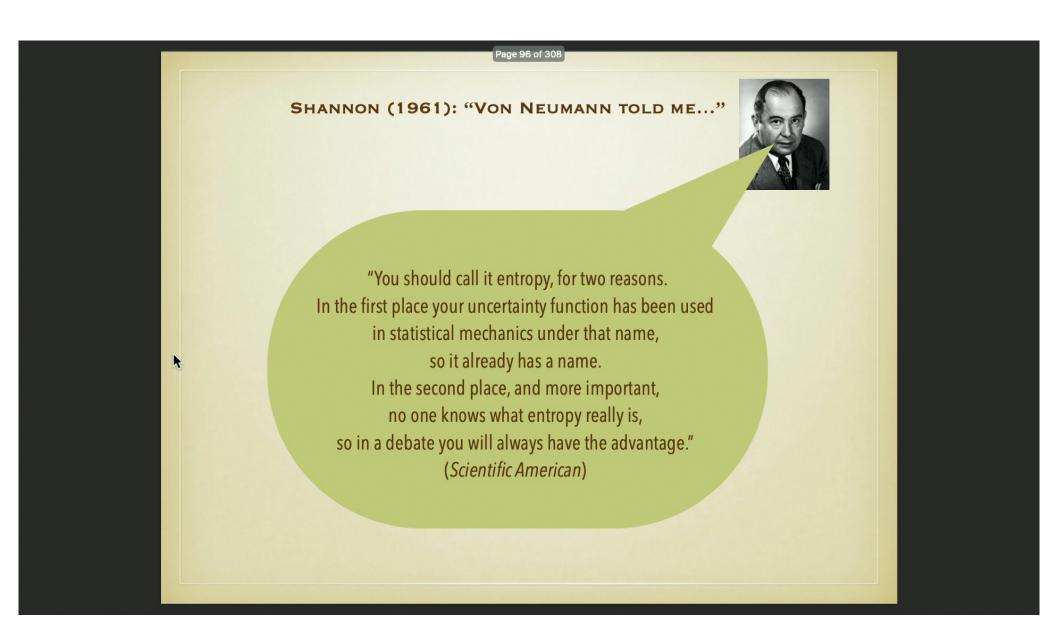
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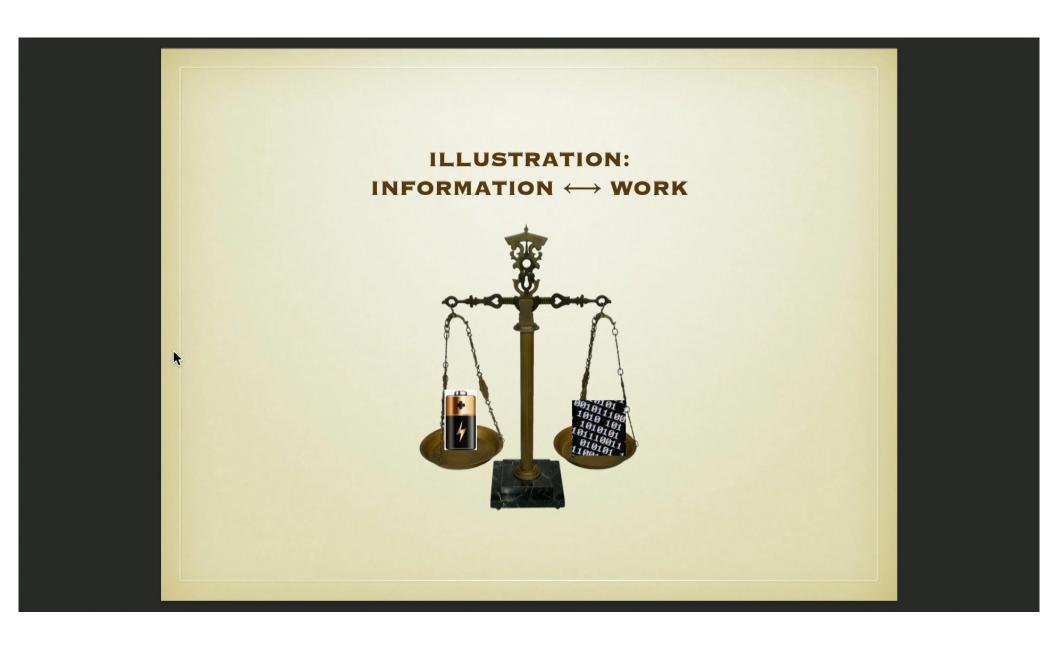
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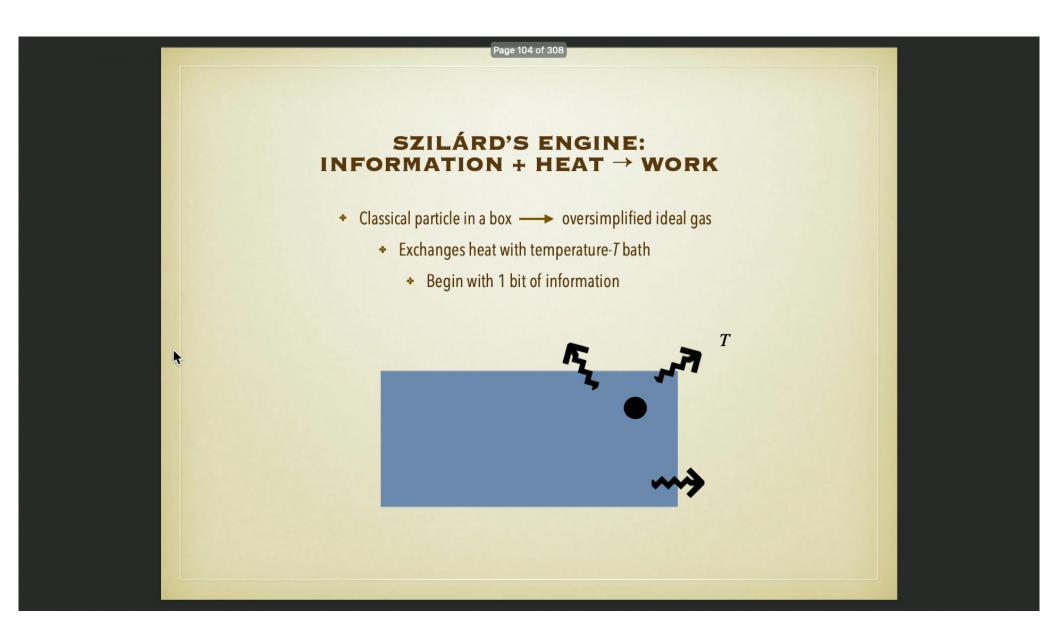
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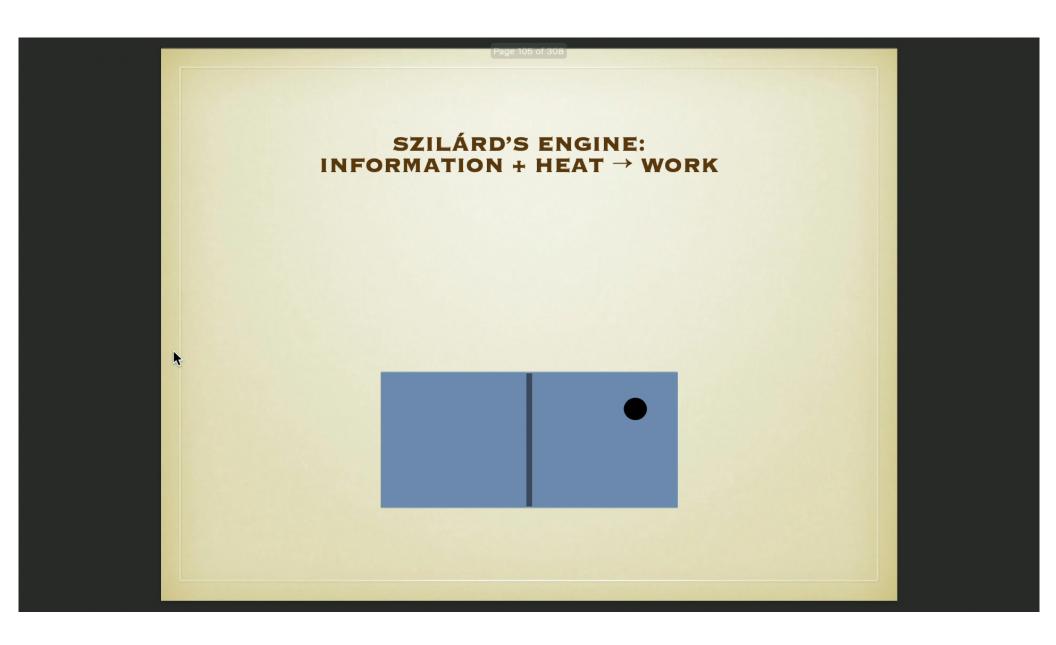




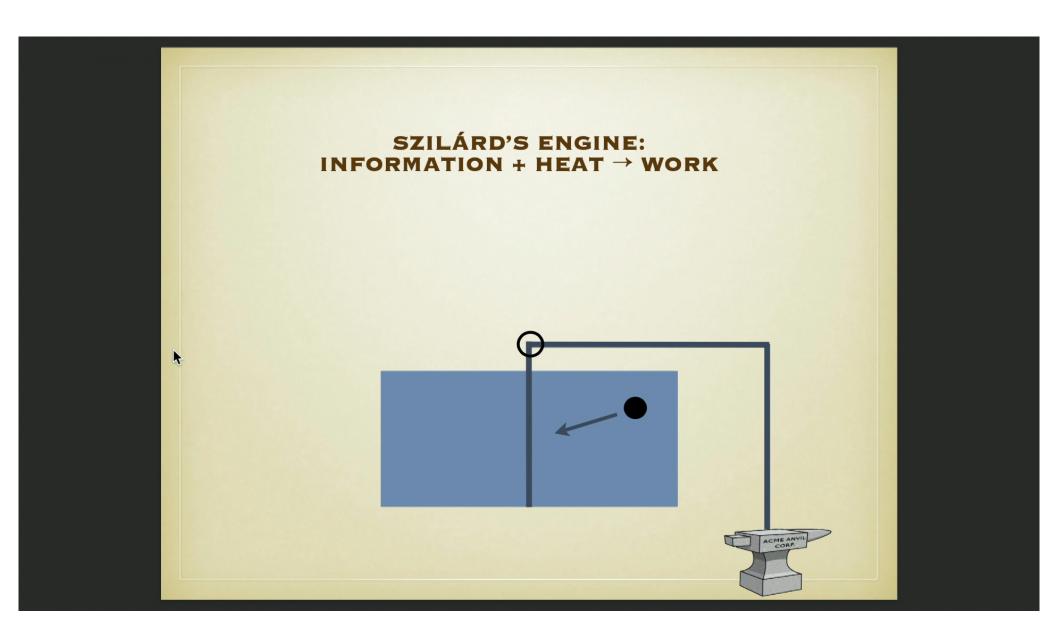
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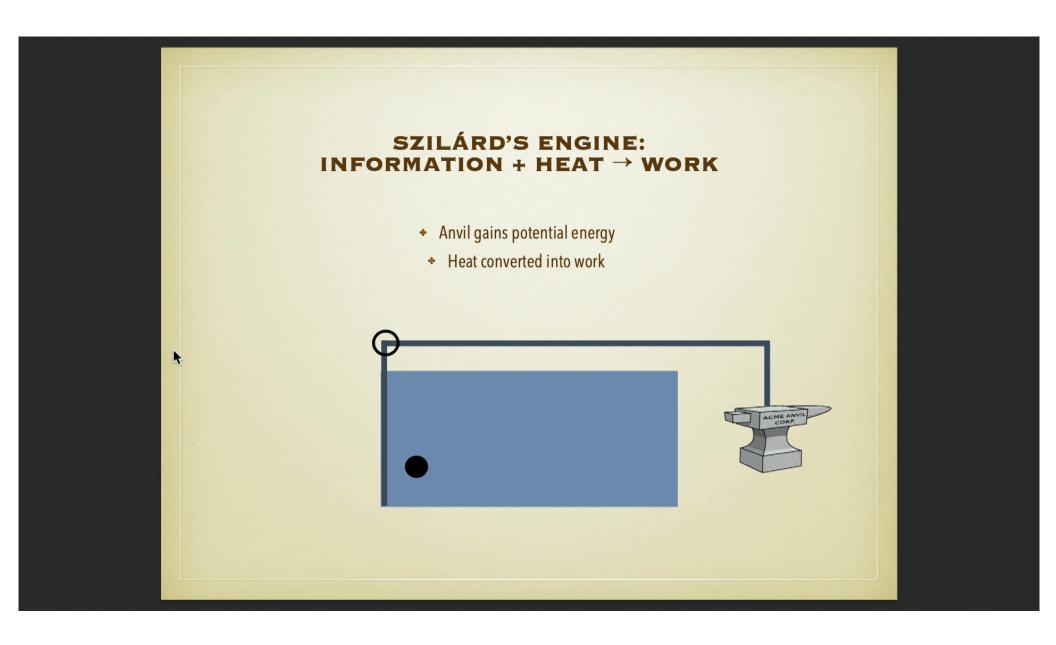
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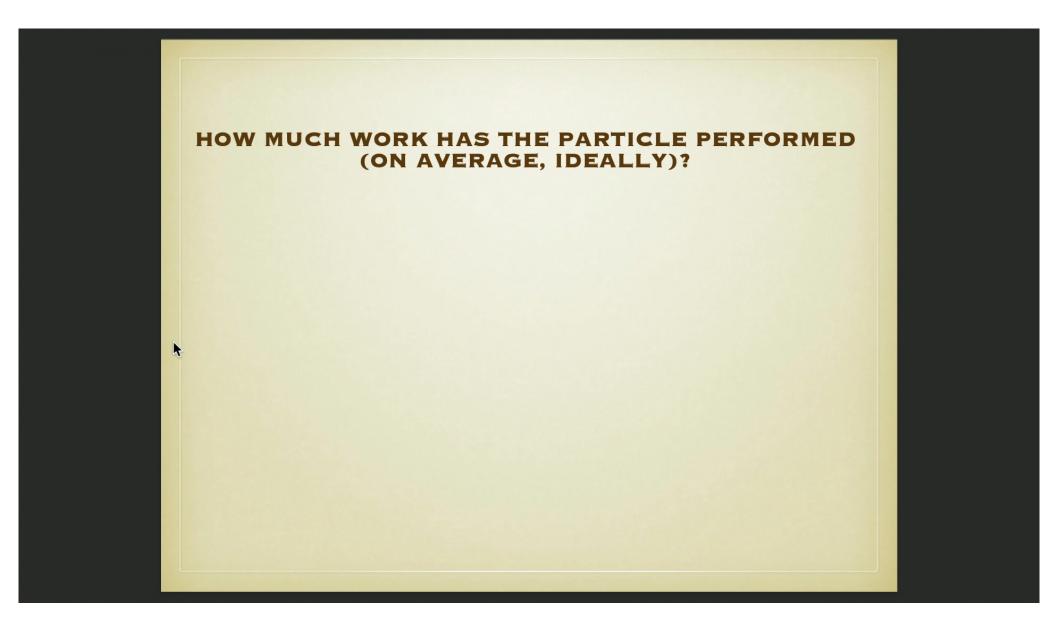
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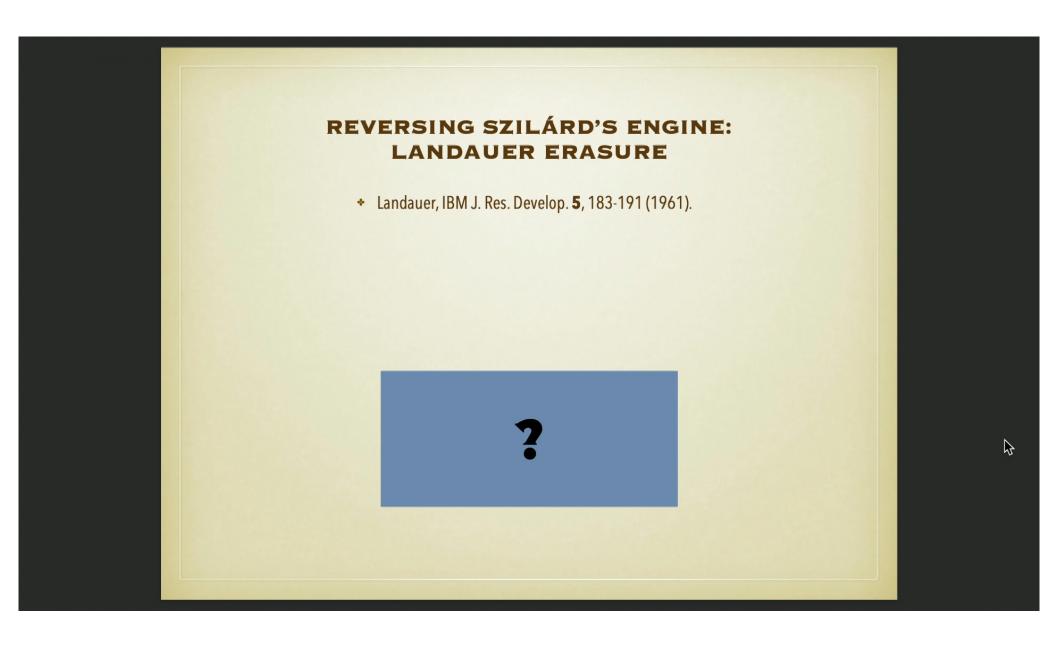
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HOW MUCH WORK HAS THE PARTICLE PERFORMED (ON AVERAGE, IDEALLY)?

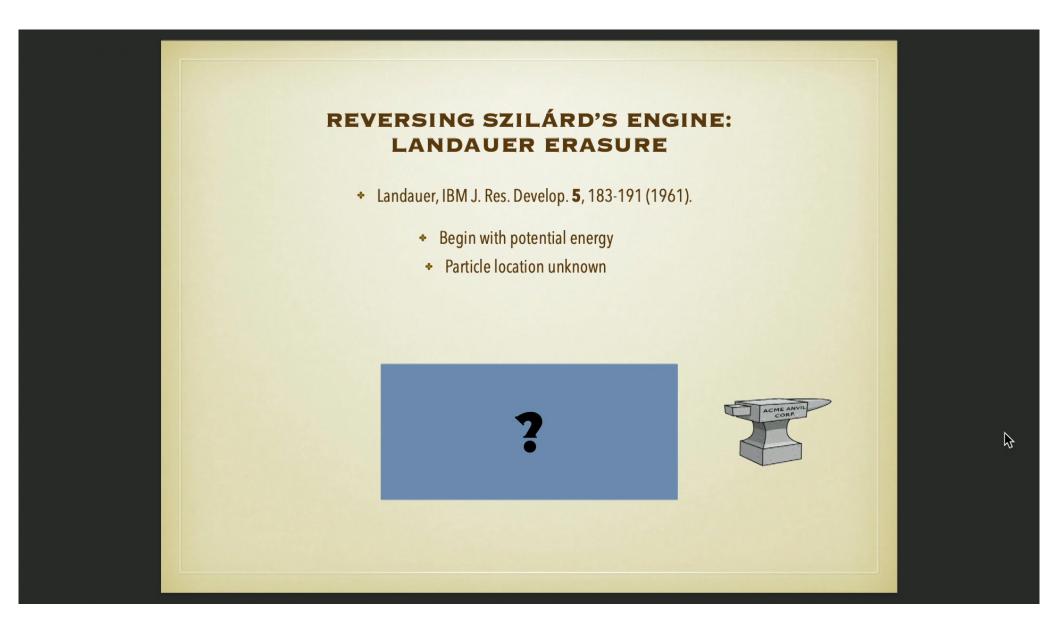
- Pressure-volume work: $W = \int_{V_i}^{V_f} p \ dV$
- Ideal gas law: $pV = nk_{\rm B}T$ \Rightarrow $p = \frac{k_{\rm B}T}{V}$
- Substitute in: $W = k_{\rm B}T \int_{V/2}^{V} \frac{{\rm d}V'}{V'}$

$$= k_{\rm B} T \ln |V'| \Big|_{V/2}^{V}$$

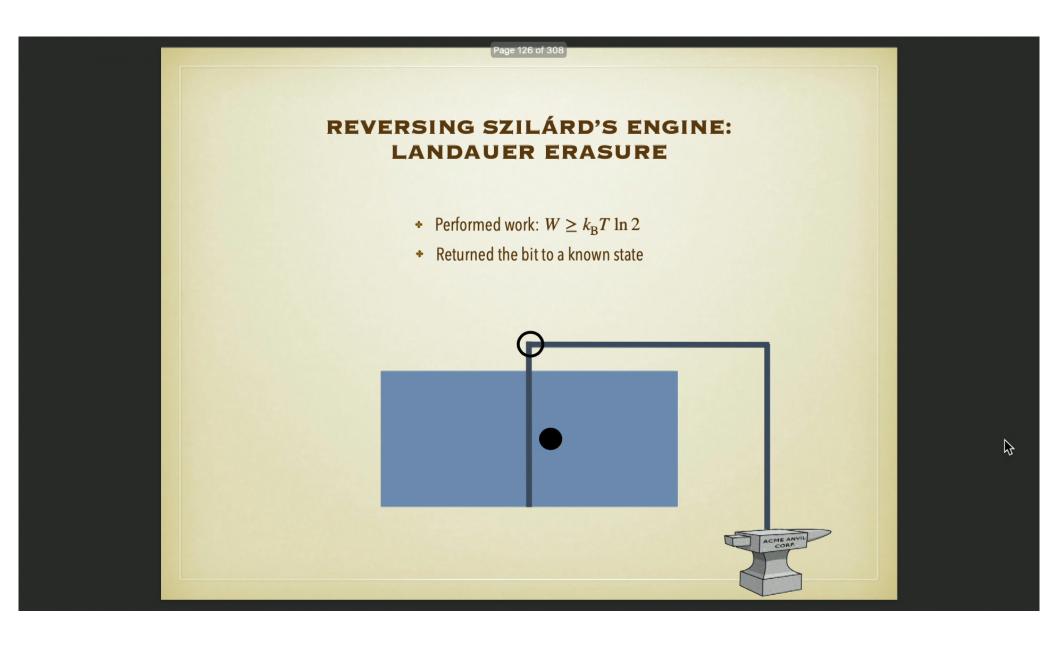
$$= k_{\rm B} T \ln 2$$



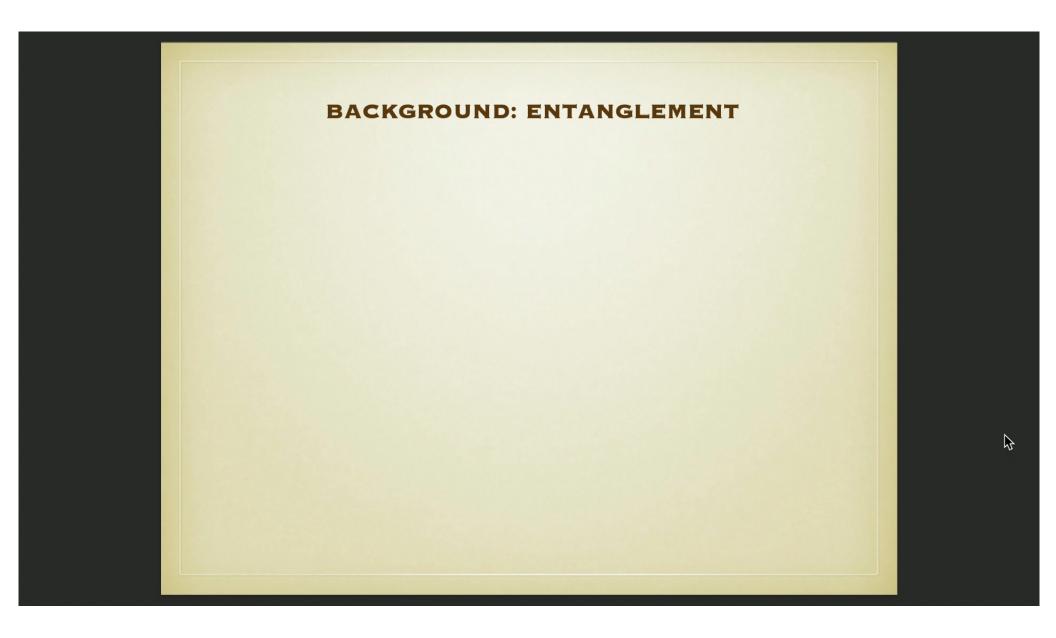
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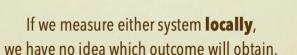
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- Manifests in correlations between measurement outcomes
- * Stronger than any correlations achievable with classical systems
- Example: singlet state of 2 qubits: $|\psi\rangle = (|0\rangle \otimes |1\rangle |1\rangle \otimes |0\rangle)/\sqrt{2}$





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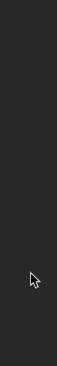
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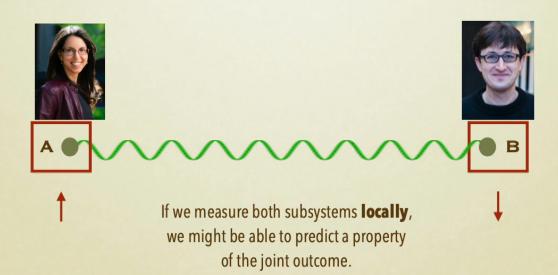
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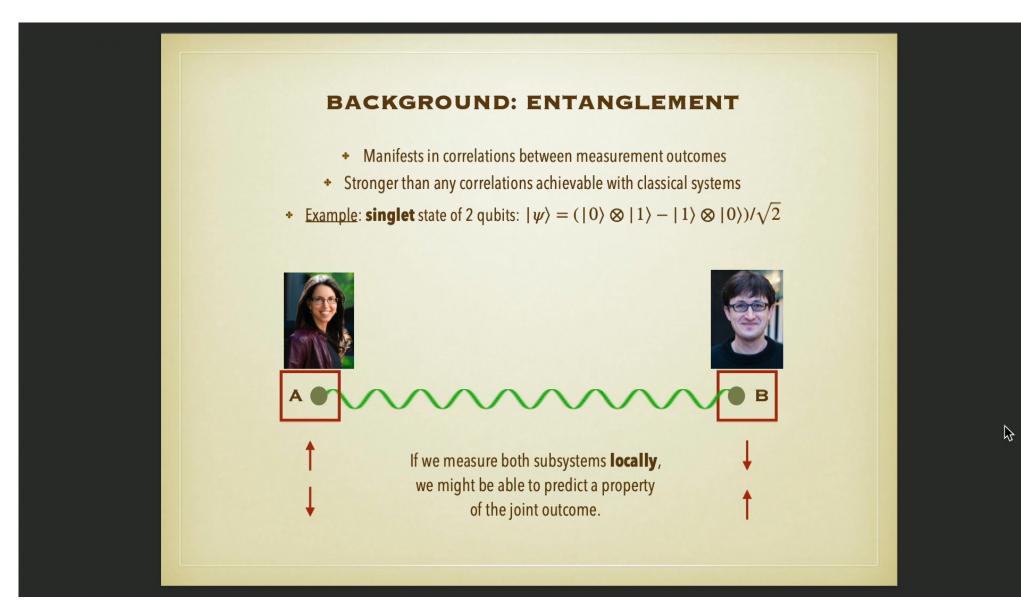
If we measure both subsystems **locally**, we might be able to predict a property of the joint outcome.



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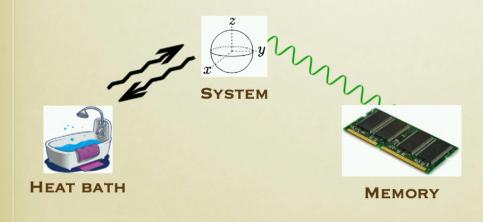
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There exists a certain **whole-system** measurement whose outcome we can predict exactly.

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ENTANGLEMENT & ERASURE IN THERMODYNAMICS

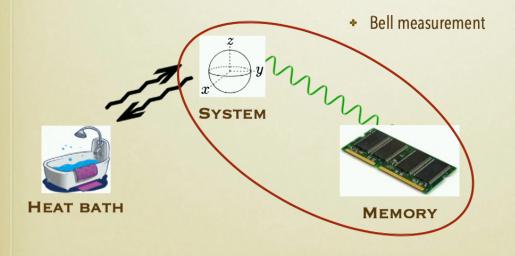
- Del Rio et al., Nature 474, 61 (2011).
- * Goal: reset to $|0\rangle$ a qubit entangled with a memory in a heat bath's presence
- While erasing the system and keeping the memory's state fixed, you can extract work.



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ENTANGLEMENT & ERASURE IN THERMODYNAMICS

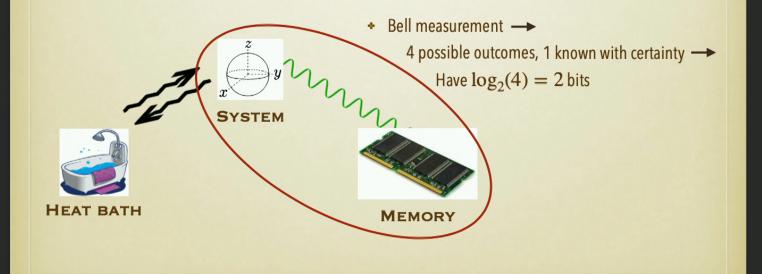
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- * <u>Trick</u>: "Burn" the correlations between system and memory.



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ENTANGLEMENT & ERASURE IN THERMODYNAMICS

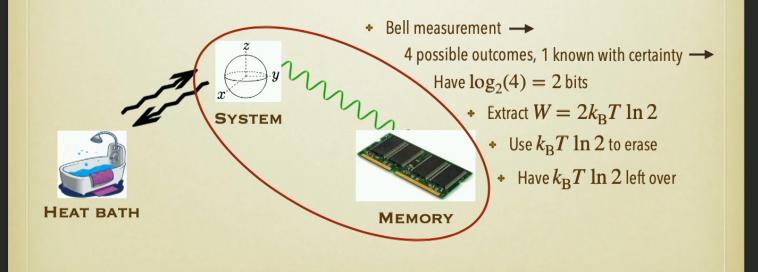
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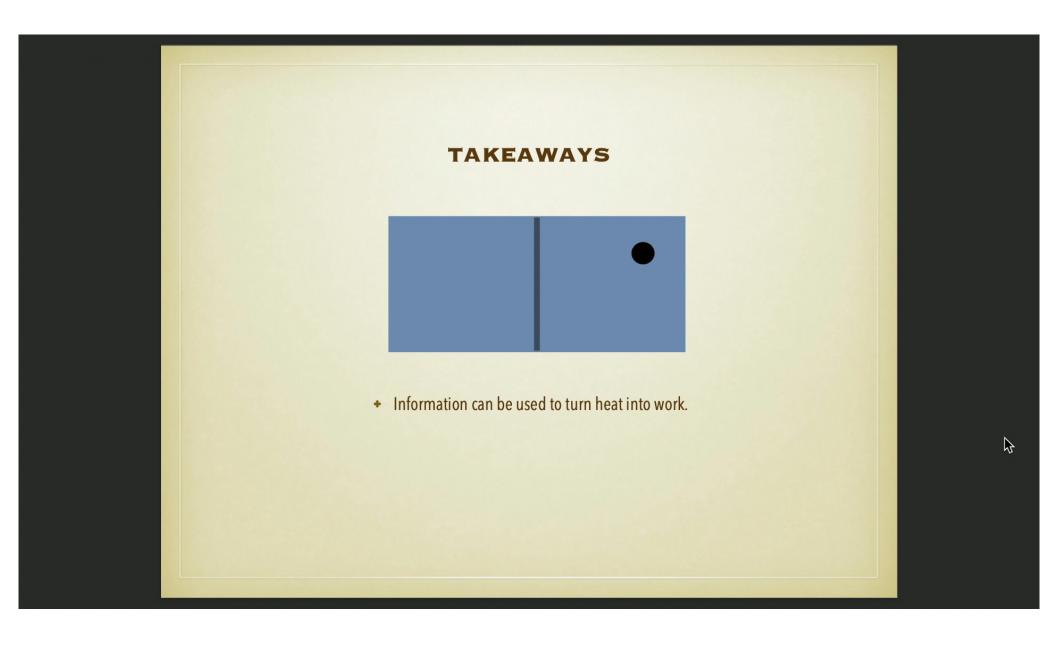


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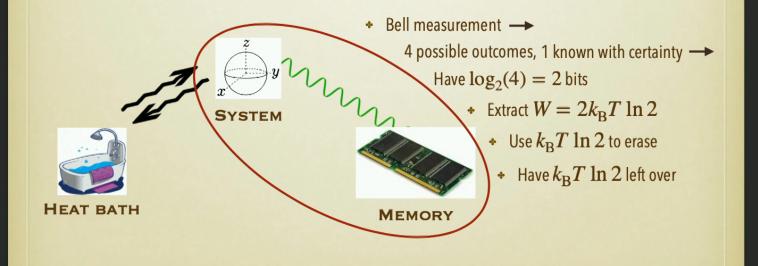
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- Goal: reset to $|0\rangle$ a qubit entangled with a memory in a heat bath's presence
- * While erasing the system and keeping the memory's state fixed, you can extract work.
- * Trick: "Burn" the correlations between system and memory.
 - → Quantum information/entanglement as a thermodynamic "fuel"



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QUANTUM MANY-BODY ENGINE



PHYSICAL REVIEW B 99, 024203 (2019)

Editors' Suggestion

Featured in Physics

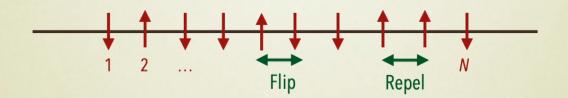
Quantum engine based on many-body localization

Nicole Yunger Halpern, 1,2,* Christopher David White, 1,2,† Sarang Gopalakrishnan, 1,2,3,4,‡ and Gil Refael 1,2,3,§

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MANY-BODY LOCALIZATION (MBL)

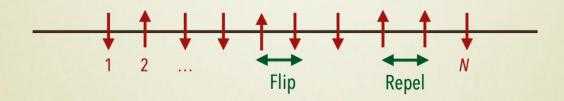


$$H = \sum_{j=1}^{N-1} \overrightarrow{\sigma}_j \cdot \overrightarrow{\sigma}_{j+1}$$

- Phase of quantum many-body systems
- * Review: Abanin et al., Rev. Mod. Phys. 91, 021001 (2019).

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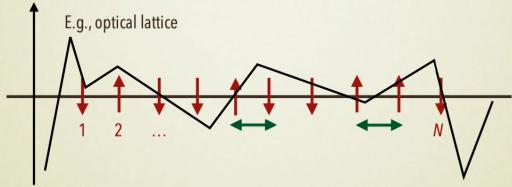
$$H = J \sum_{j=1}^{N-1} \overrightarrow{\sigma}_j \cdot \overrightarrow{\sigma}_{j+1}$$

- Phase of quantum many-body systems
- * Review: Abanin et al., Rev. Mod. Phys. 91, 021001 (2019).

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MANY-BODY LOCALIZATION (MBL)

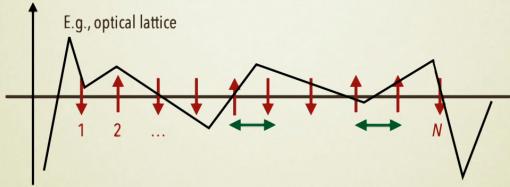


$$H = J \sum_{j=1}^{N-1} \overrightarrow{\sigma}_j \cdot \overrightarrow{\sigma}_{j+1} + h \sum_{j=1}^{N} h_j \sigma_j^z$$

- Phase of quantum many-body systems
- * Review: Abanin et al., Rev. Mod. Phys. 91, 021001 (2019).

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MANY-BODY LOCALIZATION (MBL)

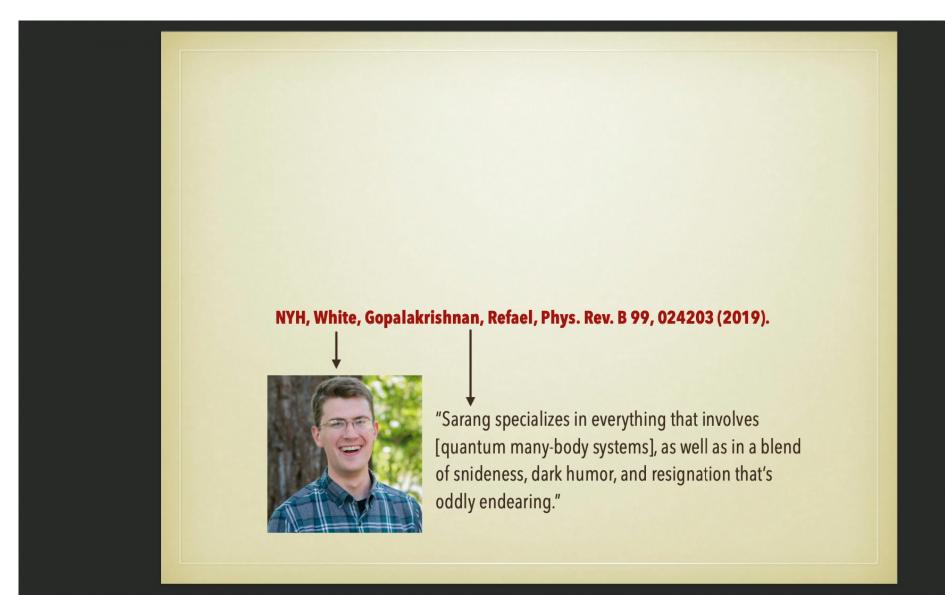


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- Phase of quantum many-body systems
- * Review: Abanin et al., Rev. Mod. Phys. 91, 021001 (2019).
- If $h \gg J$ and you measure the particles' positions, the particles will stay ~ static for a long time afterward.

D



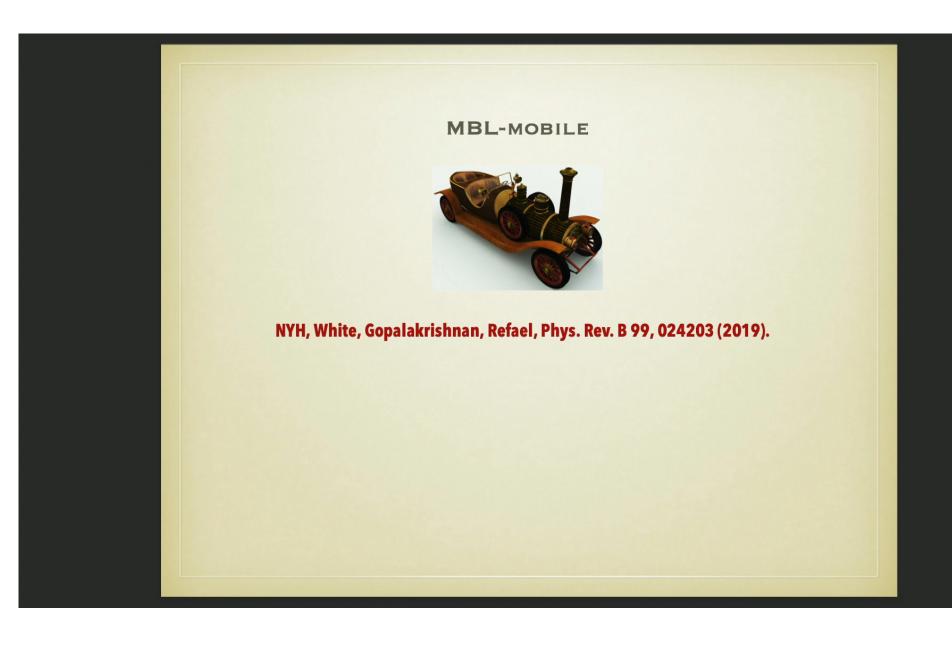


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MBL-MOBILE



NYH, White, Gopalakrishnan, Refael, Phys. Rev. B 99, 024203 (2019).

- Quantum many-body engine
- Run on an Otto cycle

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MBL-MOBILE



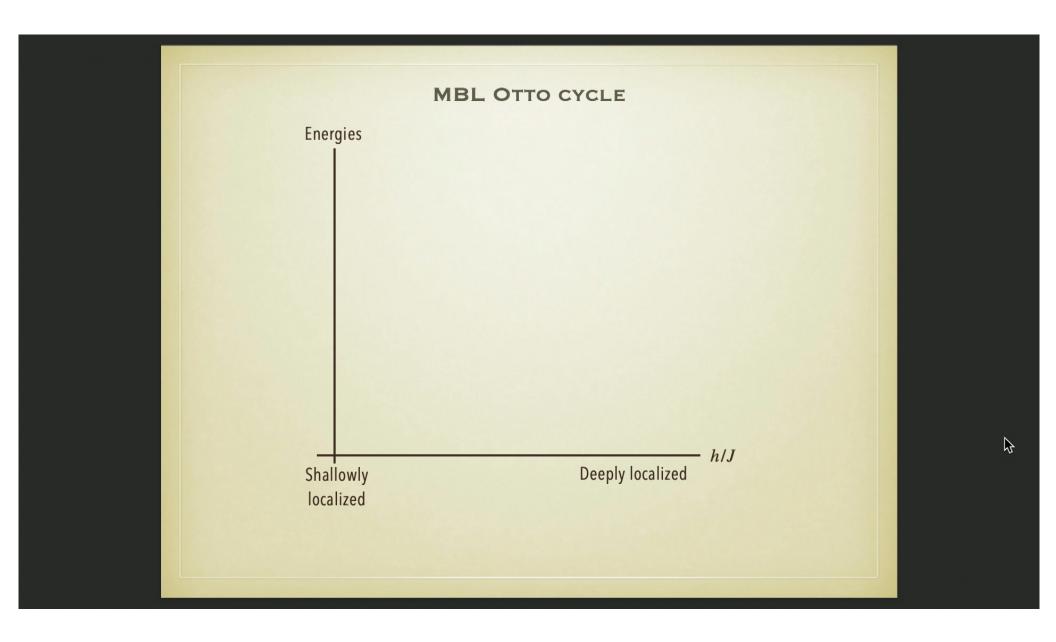
NYH, White, Gopalakrishnan, Refael, Phys. Rev. B 99, 024203 (2019).

- Quantum many-body engine
- Run on an Otto cycle →
- 4 strokes: 2 isentropic, 2 isochoric

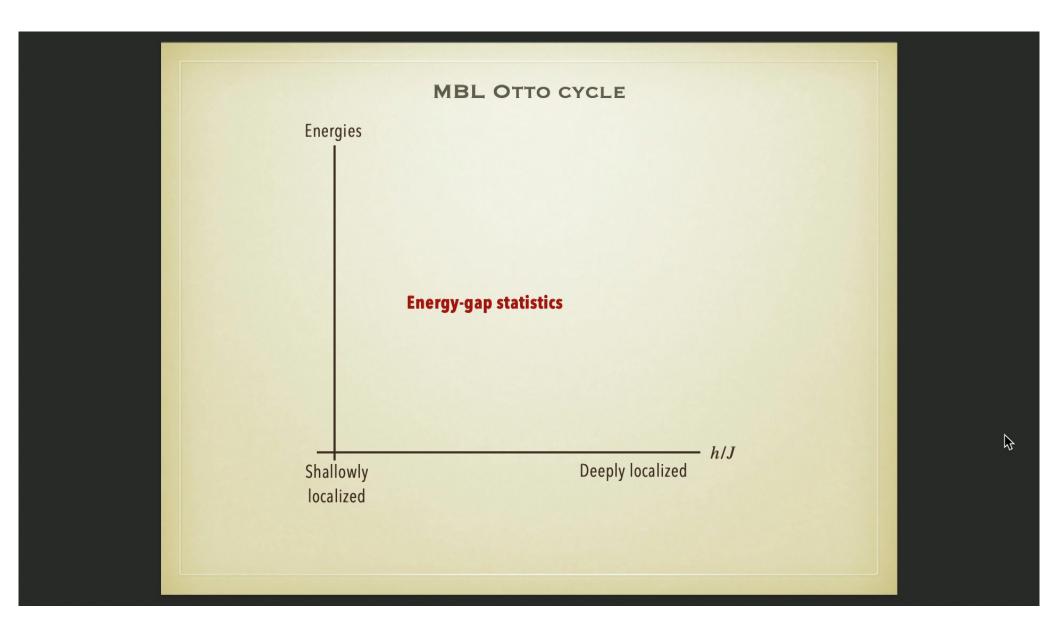
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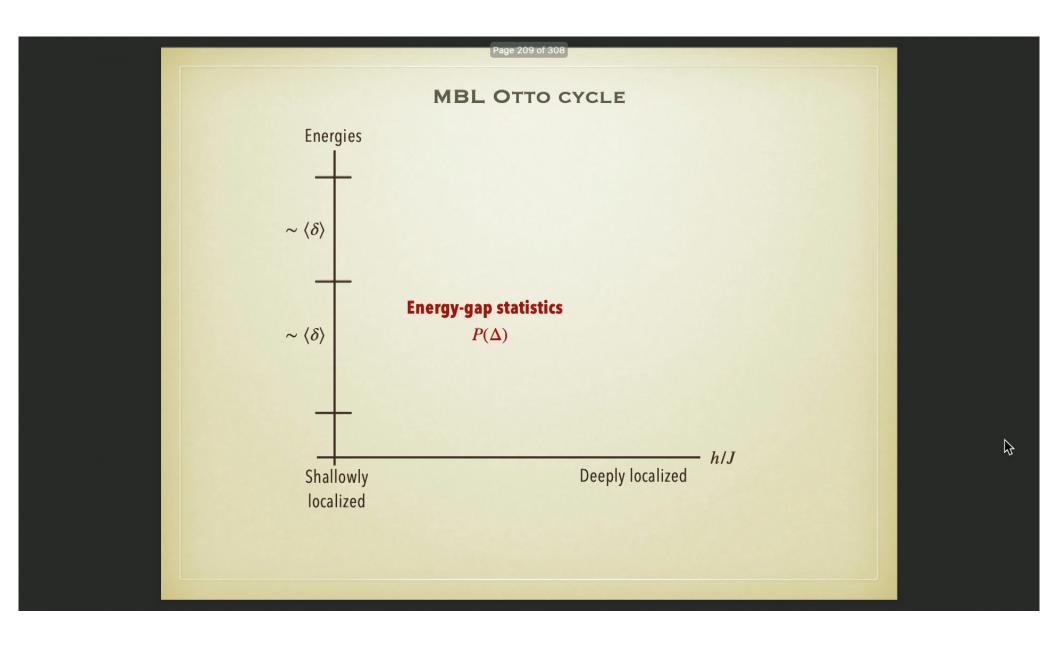
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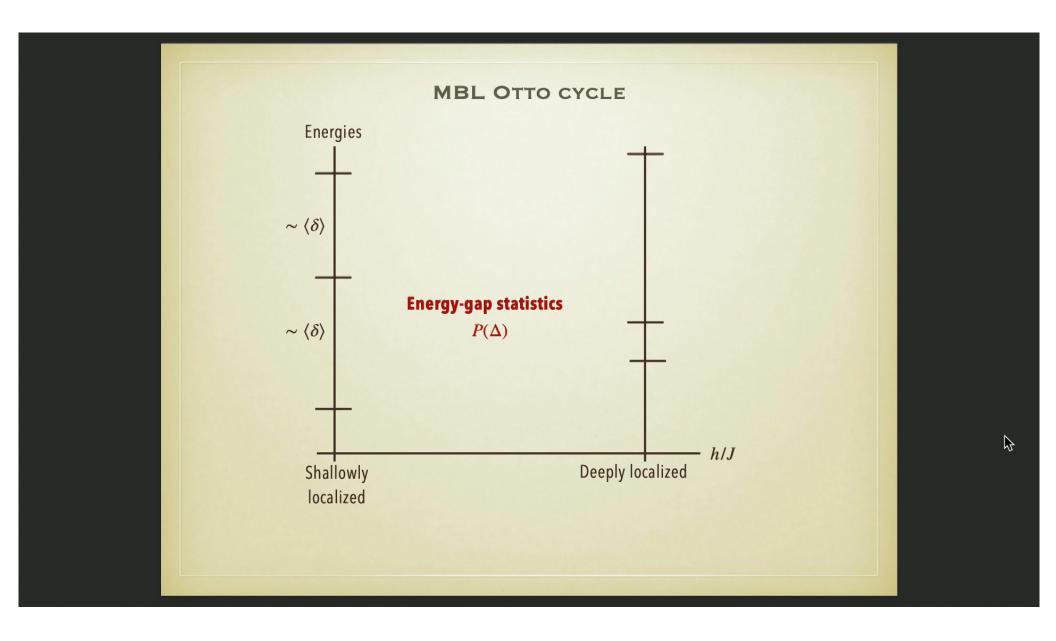
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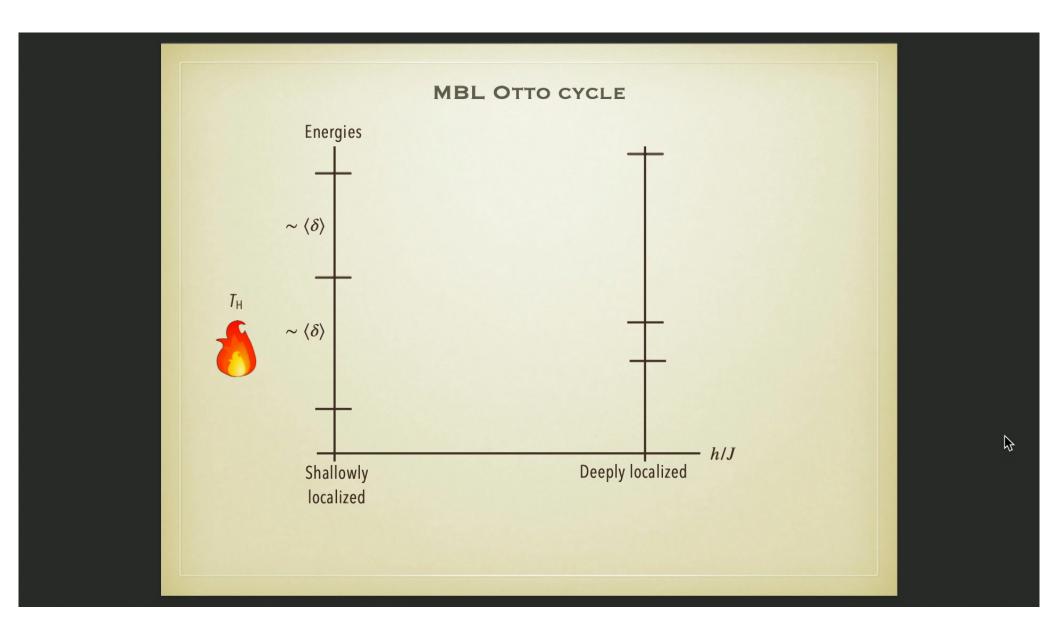
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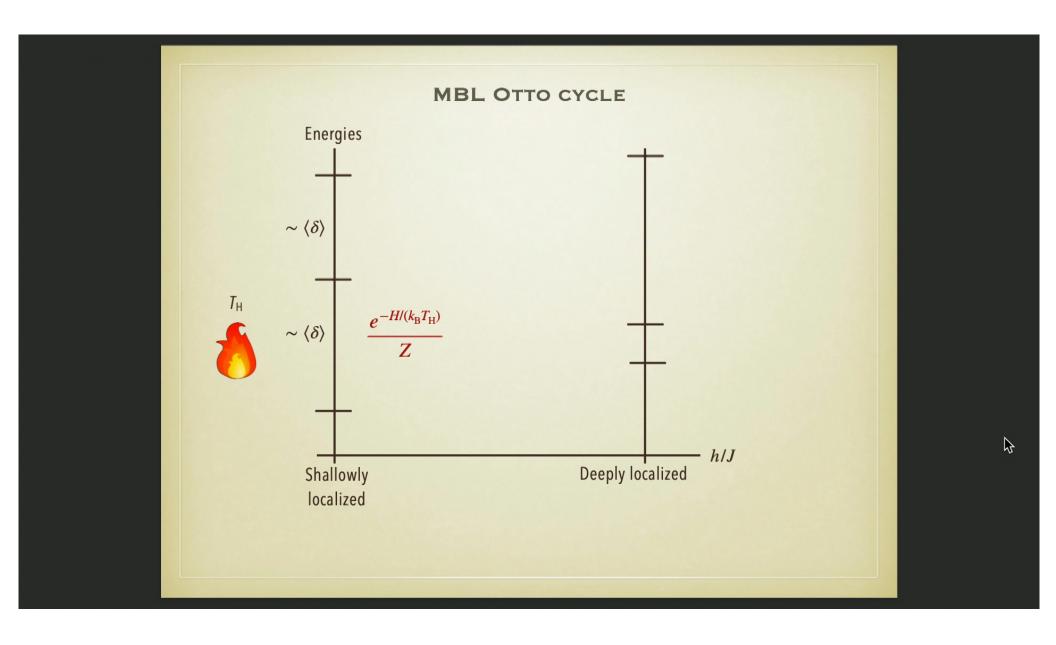
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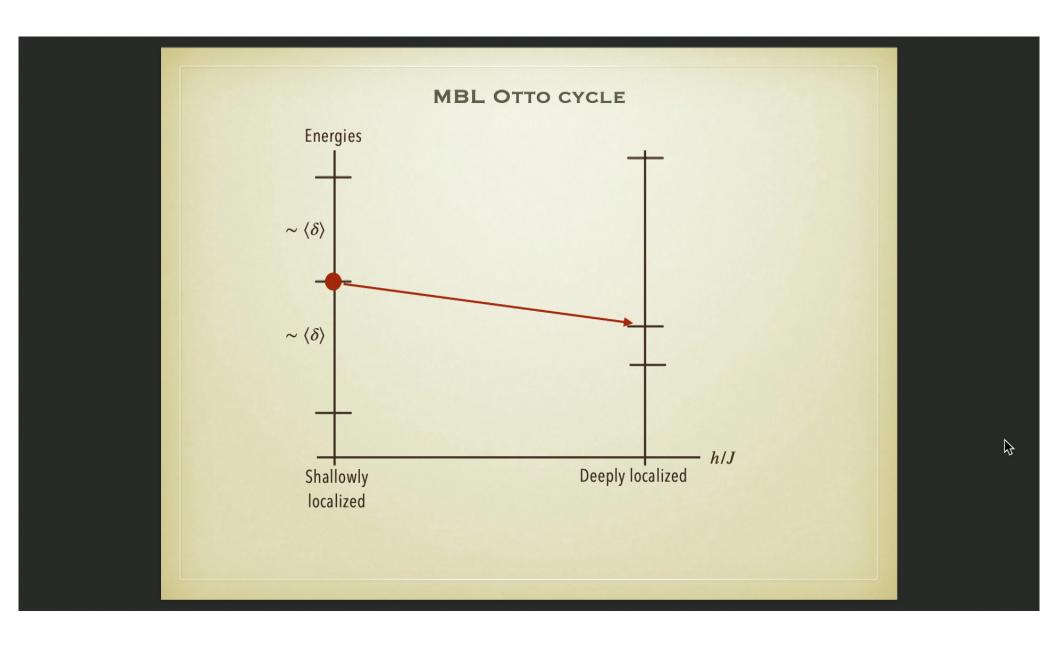
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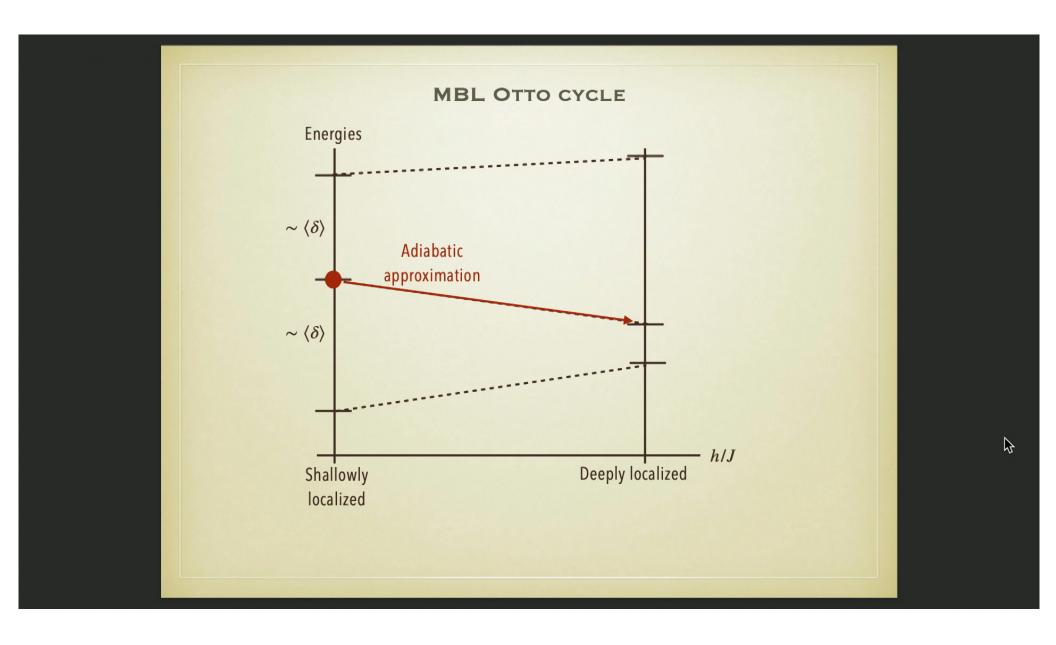
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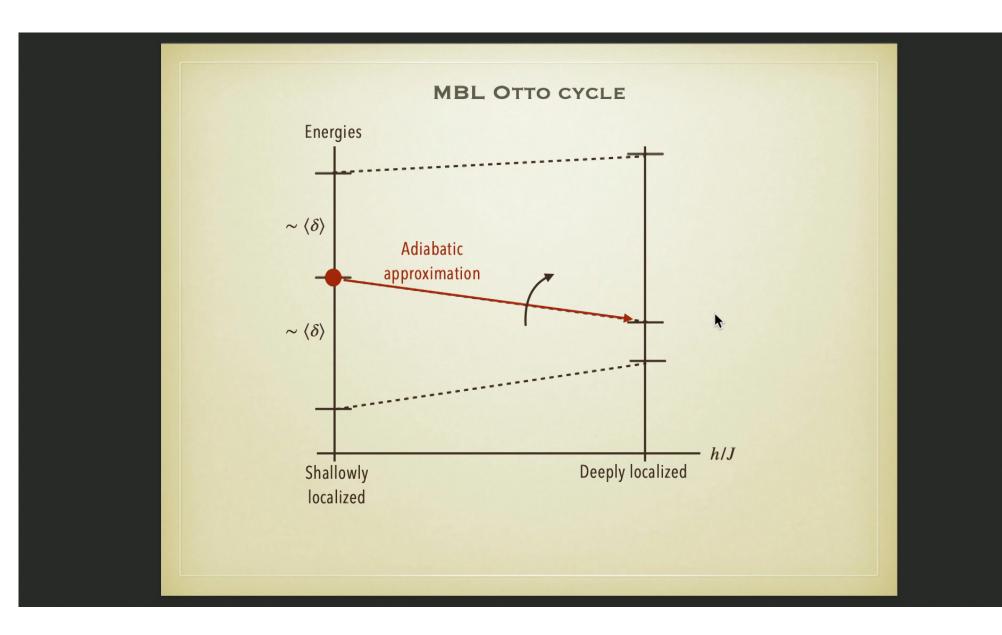
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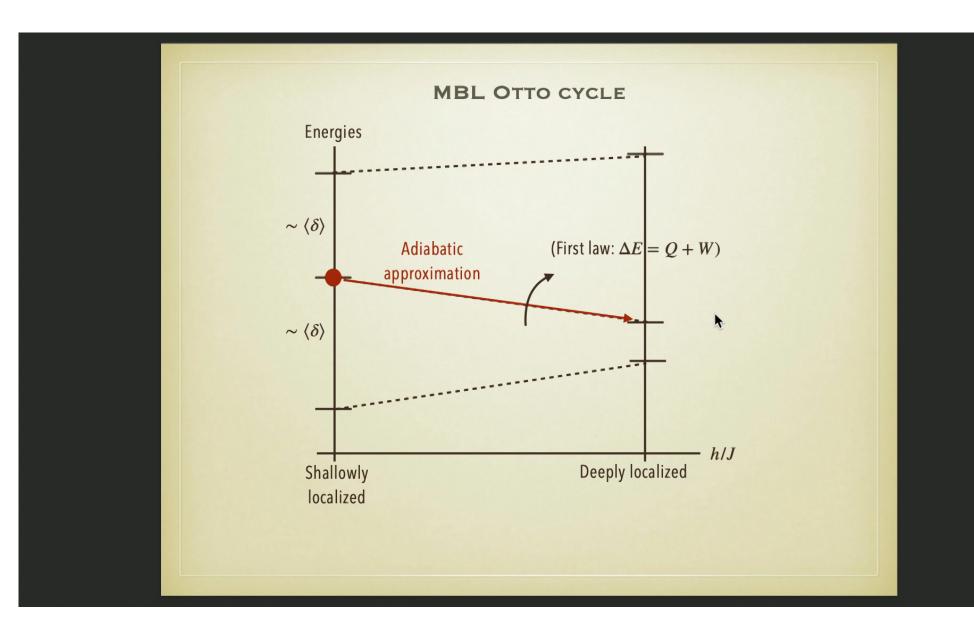
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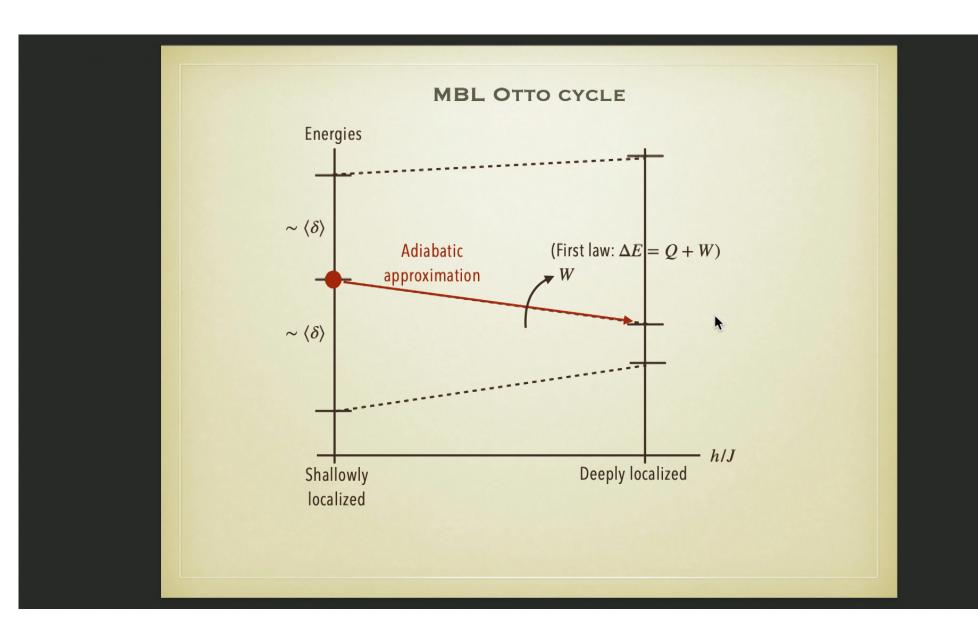
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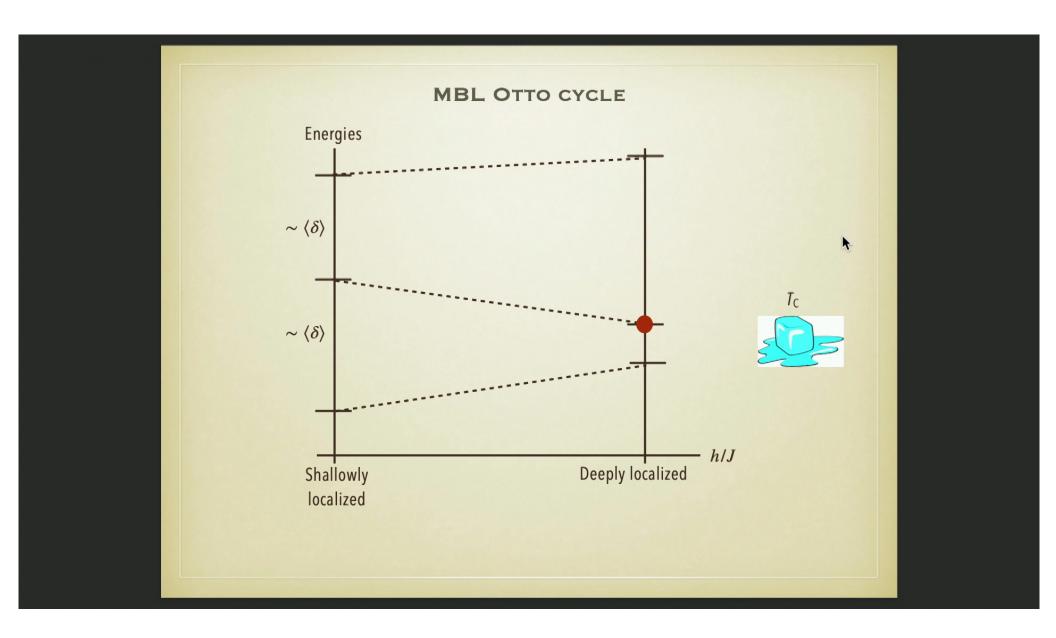
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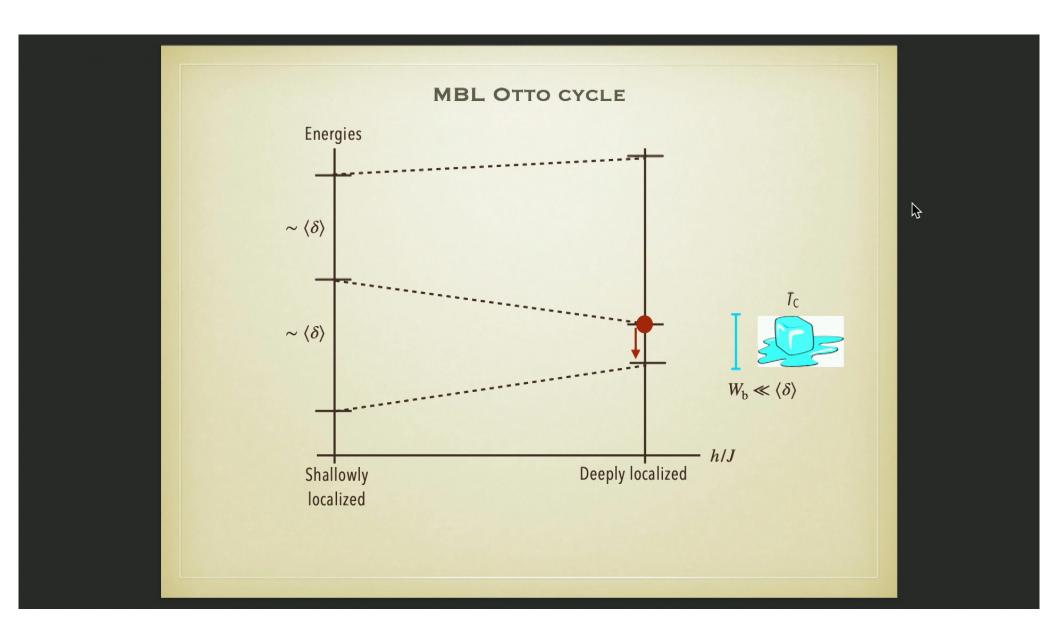
Pirsa: 22050002 Page 84/117



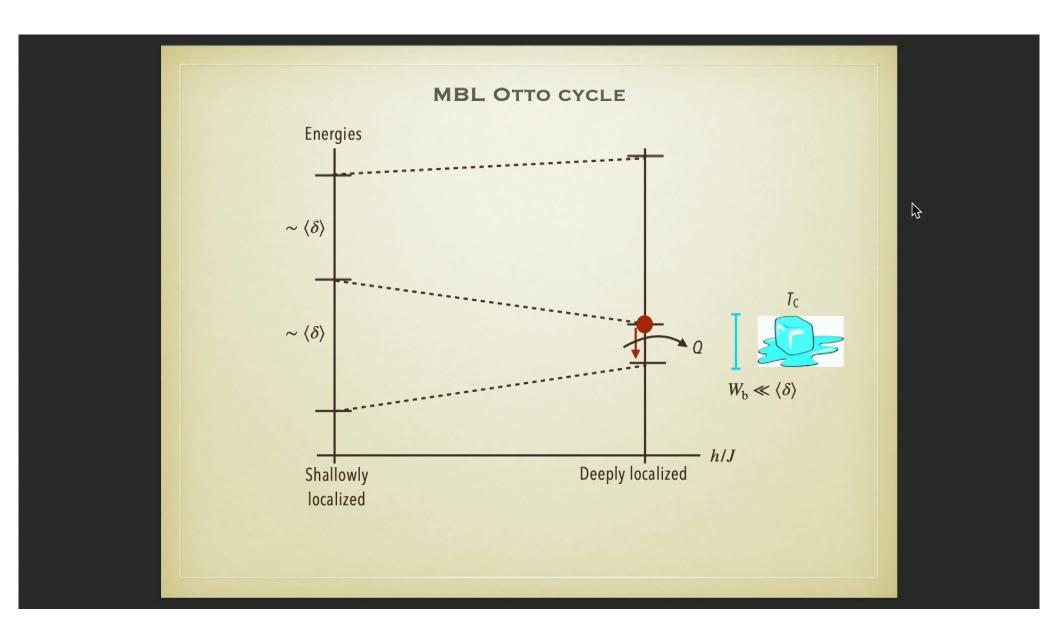
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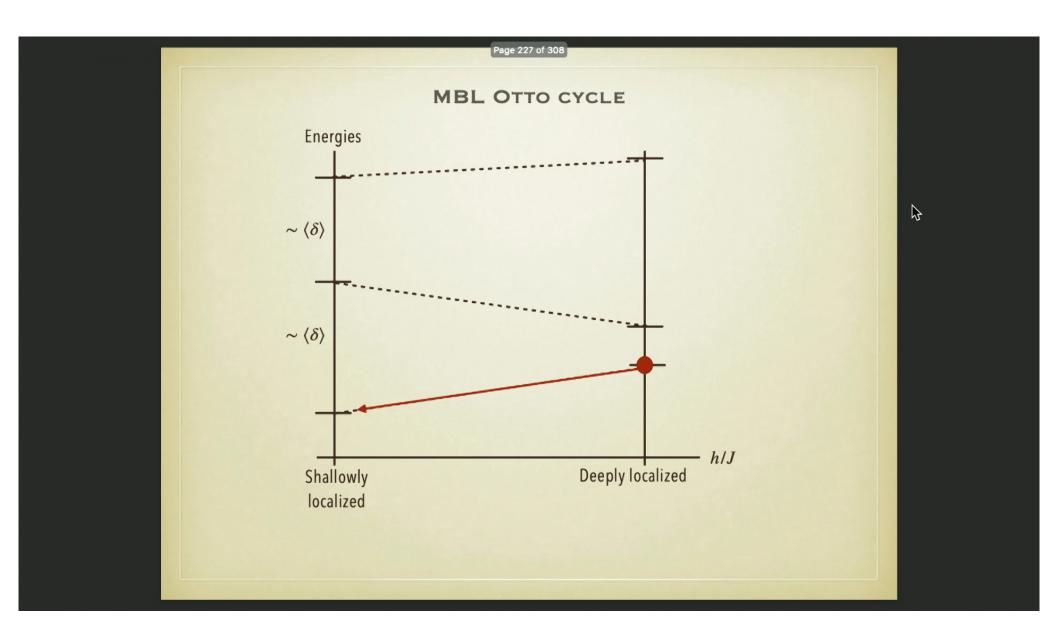
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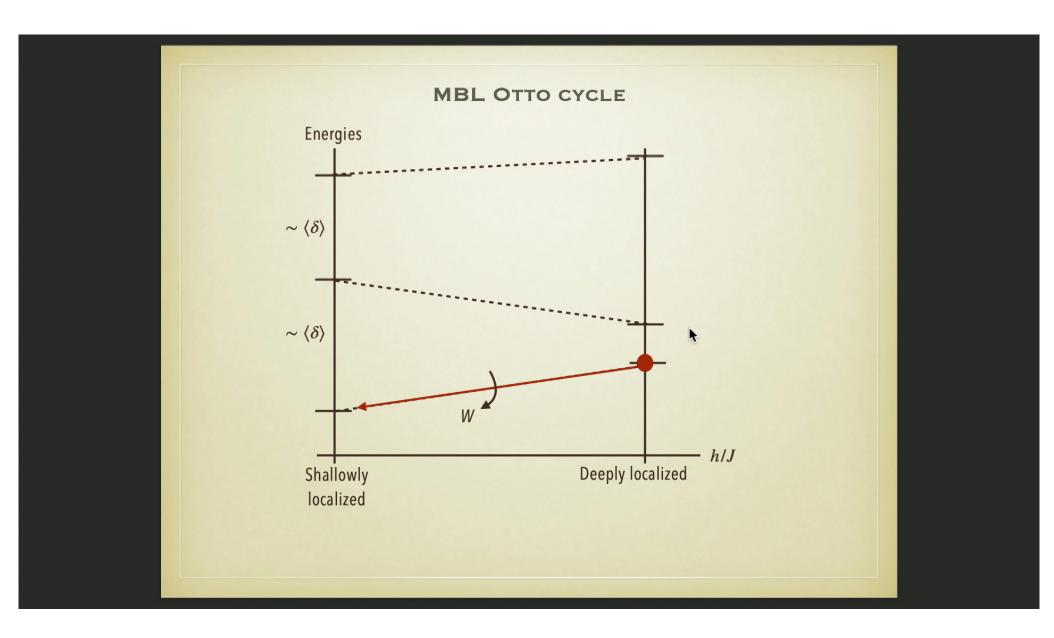
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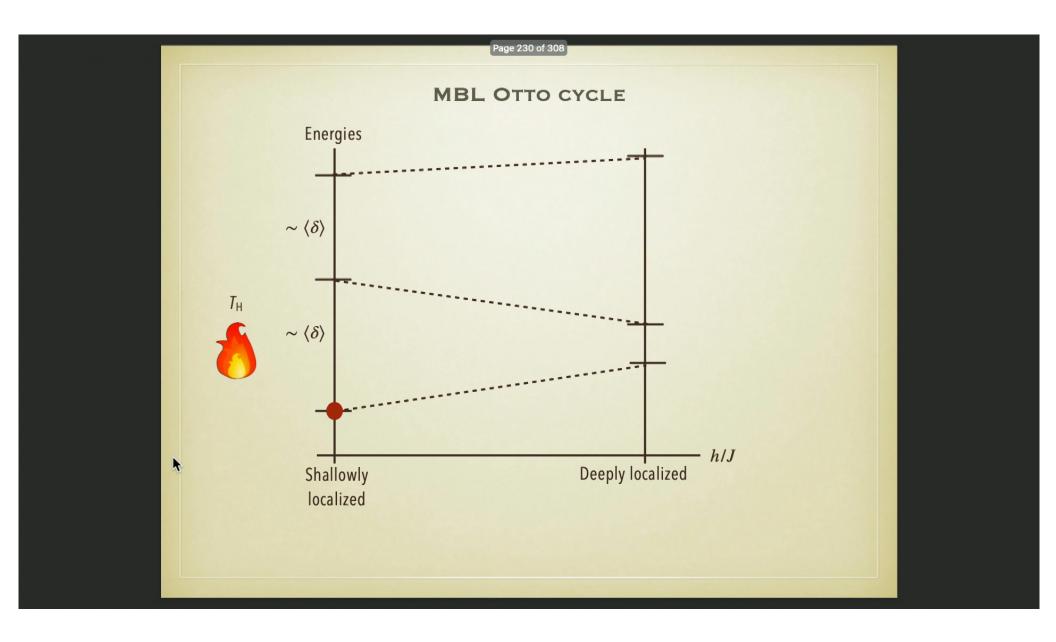
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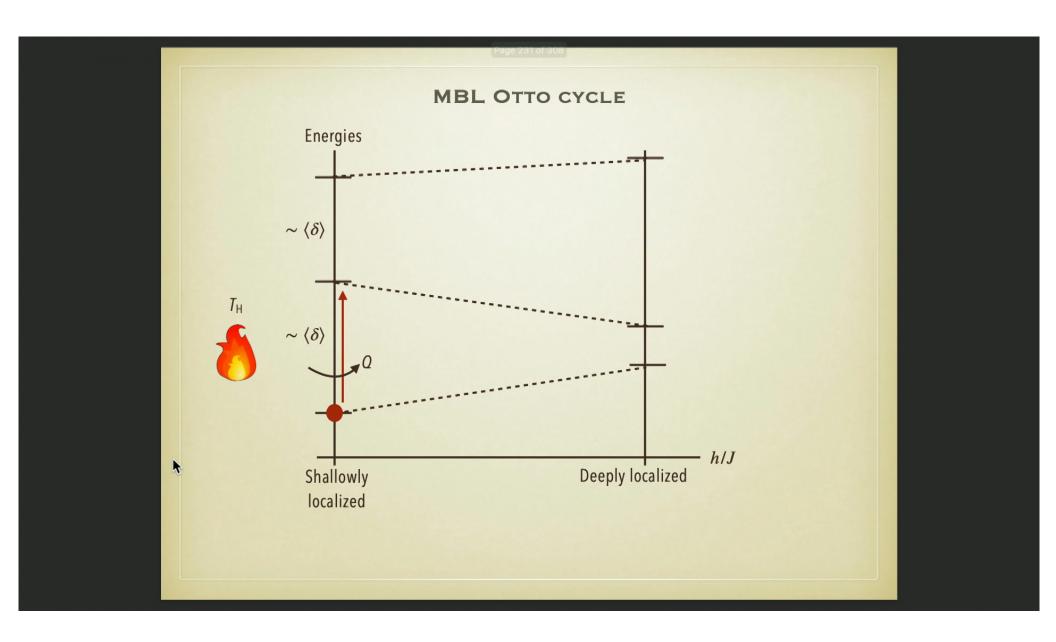
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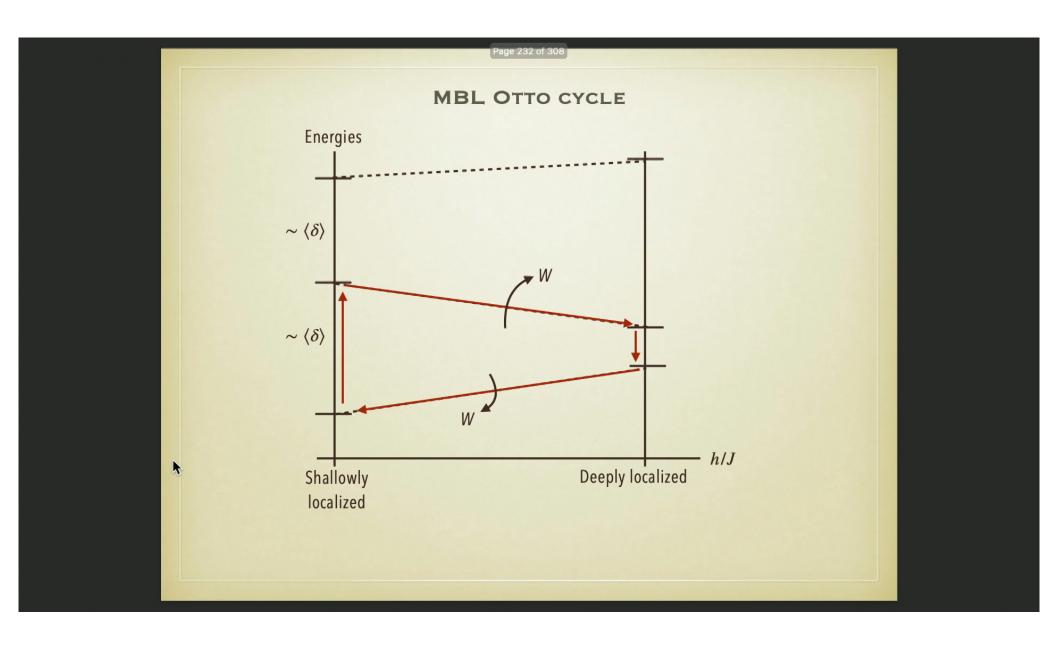
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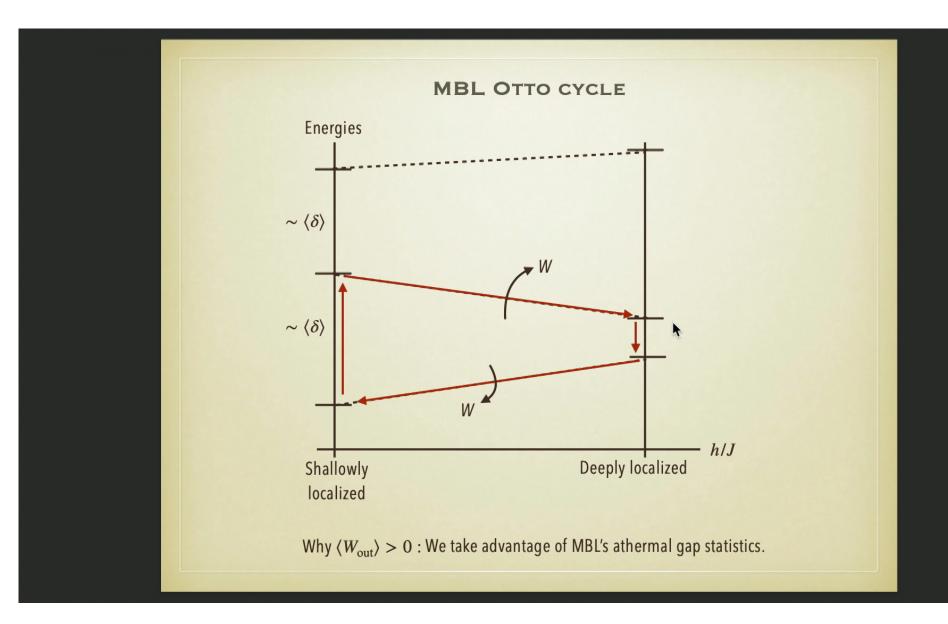
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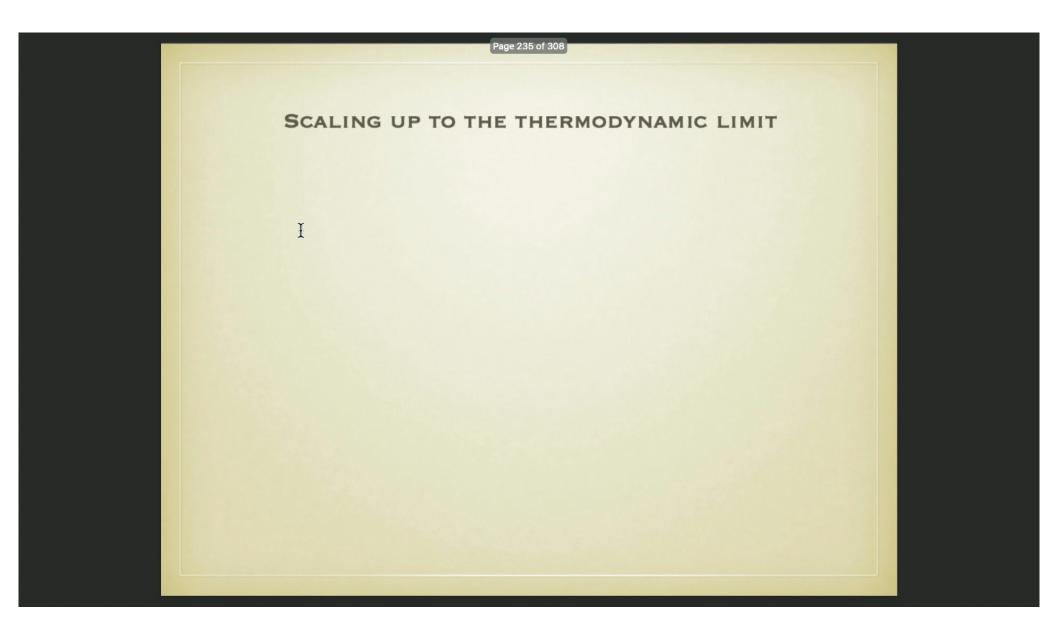
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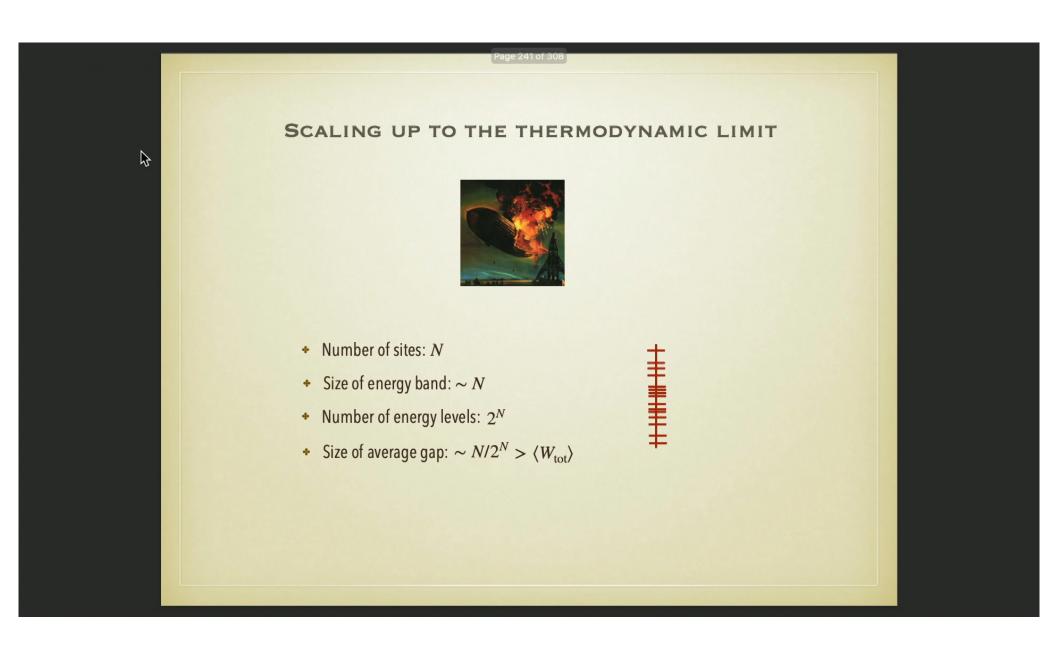
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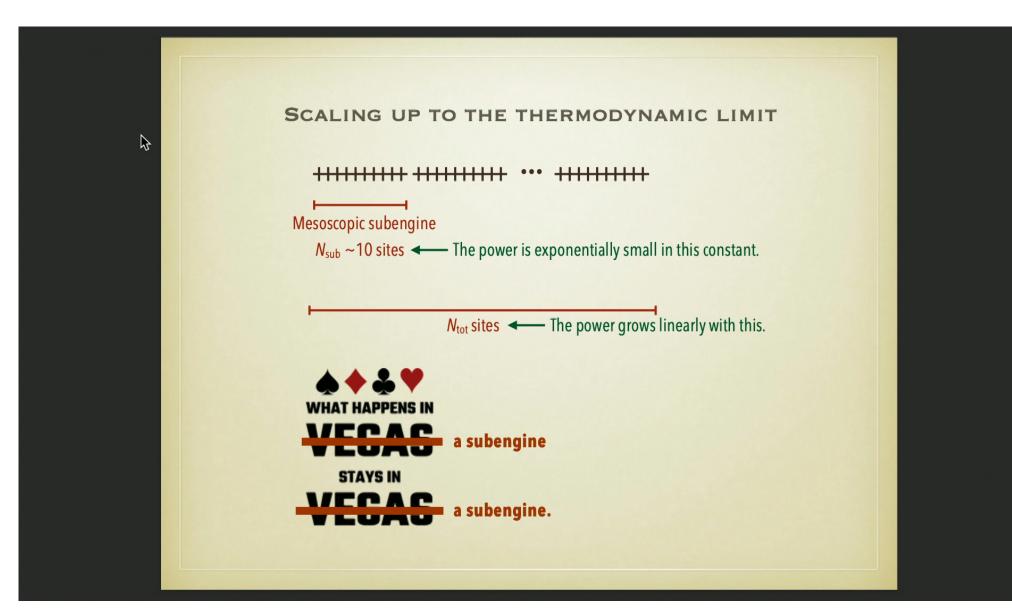


SCALING UP TO THE THERMODYNAMIC LIMIT



- Number of sites: N
- ◆ Size of energy band: ~ N
- Number of energy levels: 2^N
- Size of average gap: $\sim N/2^N > \langle W_{\rm tot} \rangle$
 - $\rightarrow 0\,$ in the thermodynamic limit





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Average work out per cycle $\sim N_{\rm tot}W_{\rm b}$ – (finite-temperature corrections) – (diabatic corrections)

• Estimate with phosphorus-doped silicon:

* Power $\sim 10^{-16} \,\mathrm{W} \sim 10 \left(\mathrm{power\ of}\right)$

Power density

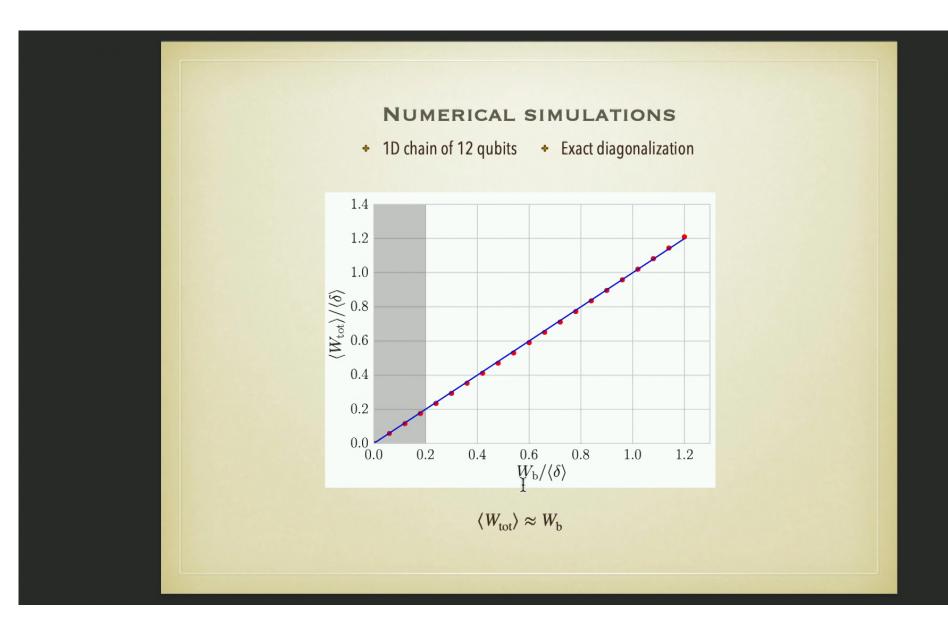
Average work out per cycle $\sim N_{\rm tot}W_{\rm b}$ – (finite-temperature corrections) – (diabatic corrections)

Estimate with phosphorus-doped silicon:

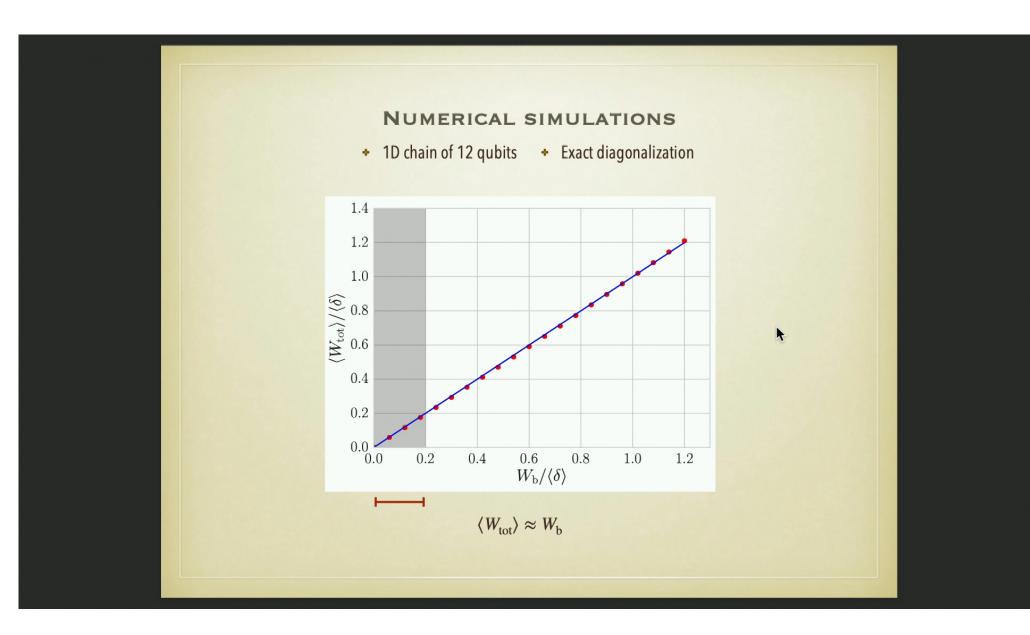
* Power $\sim 10^{-16} \,\mathrm{W} \sim 10 \left(\mathrm{power of}\right)$

* Power density ~ $100 \text{ kW/m}^3 \sim 10^{-1} \left(\text{power density of }\right)$





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• Efficiency:
$$\eta := \frac{\langle W_{\rm tot} \rangle}{\langle Q_{\rm in} \rangle}$$

$$= 1 - \frac{W_{\rm b}}{2 \langle \delta \rangle}$$

$$= \eta_{\text{ideal-gas}} = 1 - \frac{1}{(V_{+}/V_{-})^{(C_{P}/C_{V})-1}}$$

• Efficiency:
$$\eta := \frac{\langle W_{\rm tot} \rangle}{\langle Q_{\rm in} \rangle}$$

$$= 1 - \frac{W_{\rm b}}{2 \langle \delta \rangle}$$

$$= \eta_{\text{ideal-gas}} = 1 - \frac{1}{\left(V_{+}/V_{-}\right)^{\left(\frac{C_{P}/C_{V}}{-}\right)-1}}$$
Heat capacities

• Efficiency:
$$\eta := \frac{\langle W_{\rm tot} \rangle}{\langle Q_{\rm in} \rangle}$$

$$= \boxed{1 - \frac{W_{\rm b}}{2 \langle \delta \rangle}}$$

$$= \eta_{\text{ideal-gas}} = 1 - \frac{1}{\left(V_{+}/V_{-}\right)^{\left(C_{\text{P}}/C_{\text{V}}\right)-1}}$$
Heat capacities

$$\leq \eta_{\rm Carnot} = 1 - \frac{T_{\rm C}}{T_{\rm H}}$$



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ADVANTAGES OF THE MBL-MOBILE Robust scaling • High power density (P/V) Reliability (small fluctuations in work outputted during successful trials)

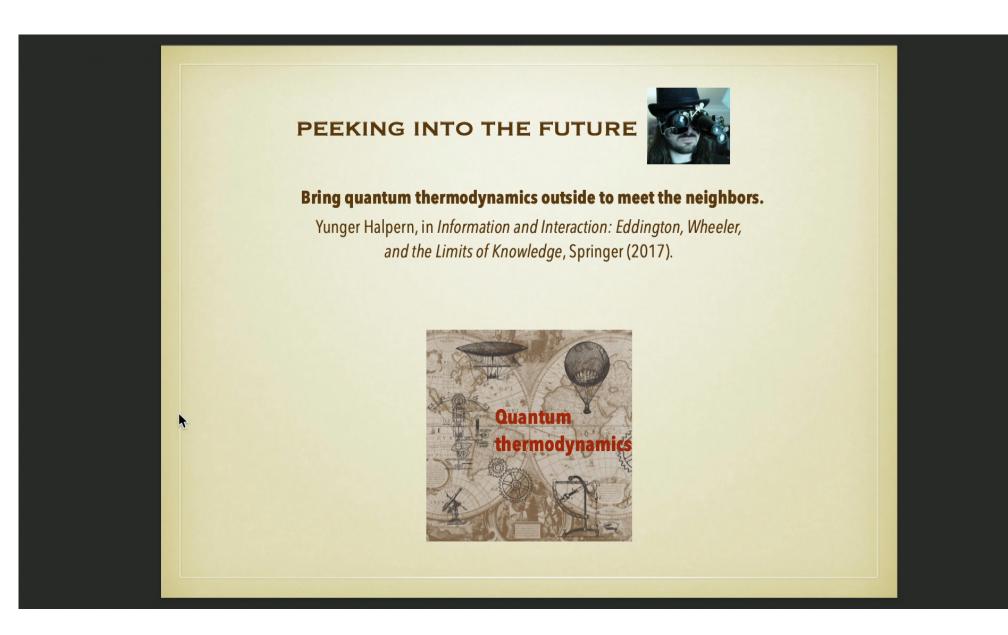
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ADVANTAGES OF THE MBL-MOBILE



- Robust scaling
- High power density (P/V)
- Reliability (small fluctuations in work outputted during successful trials)
 - Few worst-case trials ($W_{\text{out}} < 0$)

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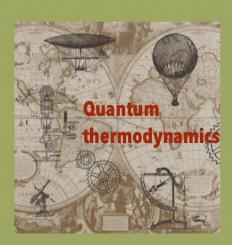
Bring quantum thermodynamics outside to meet the neighbors.

Yunger Halpern, in *Information and Interaction: Eddington, Wheeler, and the Limits of Knowledge*, Springer (2017).

Atomic, molecular, and optical physics

Chemistry

Biophysics



Condensed matter

High-energy physics

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PEEKING INTO THE FUTURE OF QUANTUM STEAMPUNK BROADLY



Yunger Halpern, in Information and Interaction: Eddington, Wheeler, and the Limits of Knowledge, Springer (2017).

- + Answer pre-existing questions in other fields.
 - Photosynthesis, photovoltaics, exciton hopping in quantum dots, ...
- Integrate with other fields' toolkits.
 - Eigenstate thermalization, quantum chaos, out-of-time-ordered correlators, Doob transforms, black-hole information paradox, ...

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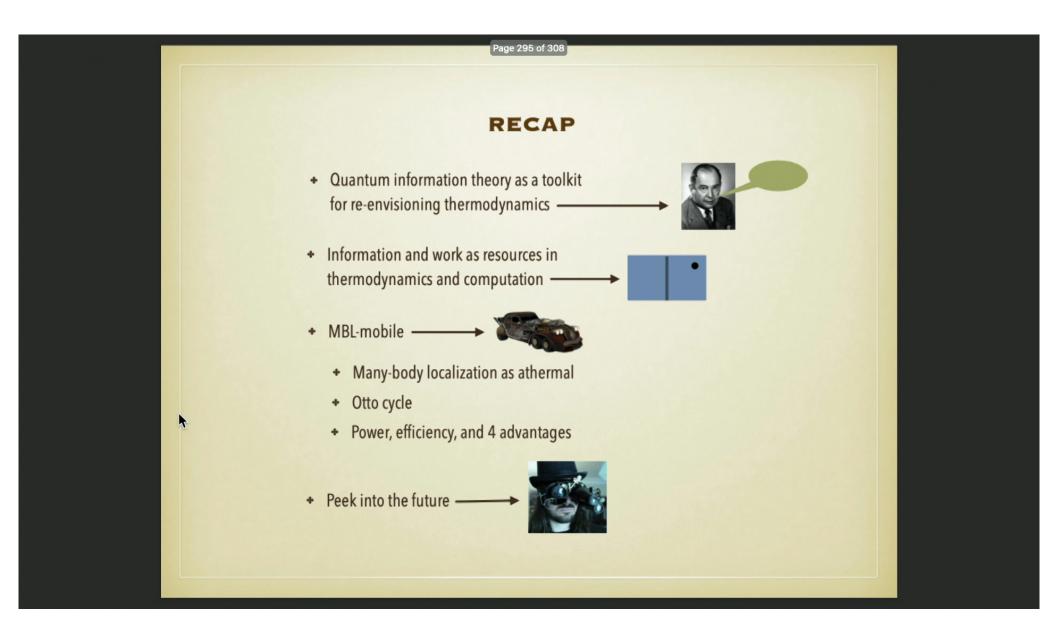
PEEKING INTO THE FUTURE OF QUANTUM STEAMPUNK BROADLY



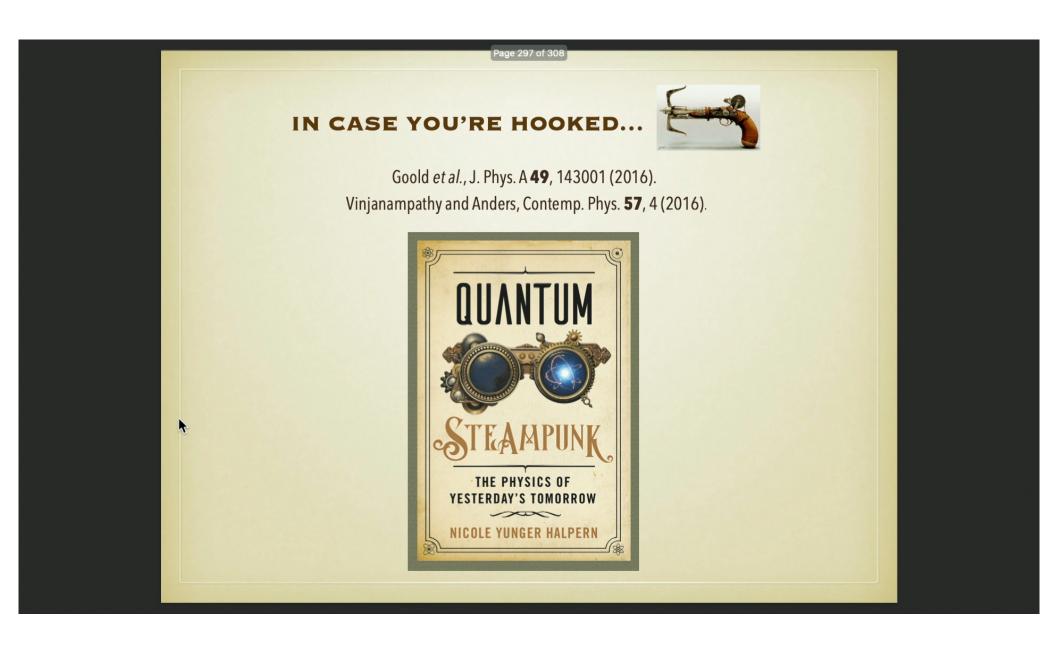
Yunger Halpern, in Information and Interaction: Eddington, Wheeler, and the Limits of Knowledge, Springer (2017).

- + Answer pre-existing questions in other fields.
 - Photosynthesis, photovoltaics, exciton hopping in quantum dots, ...
- Integrate with other fields' toolkits.
 - * Eigenstate thermalization, quantum chaos, out-of-time-ordered correlators, Doob transforms, black-hole information paradox, ...
- Extend from abstract theory to experiments and technologies.

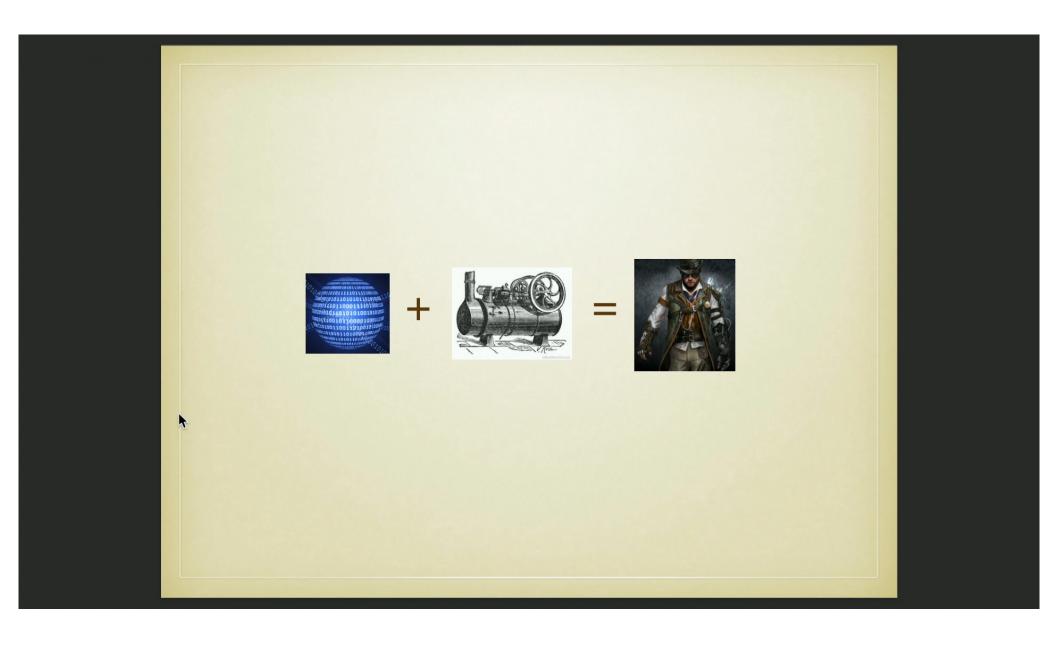
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QUANTUM-INFORMATION THERMODYNAMICISTS LIVE IT.

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