

Title: Toward realization of novel superconductivity based on twisted van der Waals Josephson junction in Cuprates

Speakers: Philip Kim

Series: Quantum Matter

Date: February 28, 2022 - 12:00 PM

URL: <https://pirsa.org/22020071>

Abstract: Twisted interfaces between stacked van der Waals Cuprate crystals enable tunable Josephson coupling, utilizing anisotropic superconducting order parameters. Employing a novel cryogenic assembly technique, we fabricate high-temperature Josephson junctions with an atomically sharp twisted interface between  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{\{8+x\}}$  crystals. The critical current density  $J_c$  sensitively depends on the twist angle. While near 0 degree twist,  $J_c$  nearly matches that of intrinsic junctions, it is suppressed almost 2-orders of magnitude but remained finite near 45 degree.  $J_c$  also exhibits non-monotonic behavior versus temperature due to competition between two supercurrent contributions from nodal and anti-nodal regions of the Fermi surface. Near 45 degree twist angle, we observe two-period Fraunhofer interference patterns and fractional Shapiro steps at half integer values, a signature of co-tunneling Cooper pairs necessary for high temperature topological superconductivity.

Zoom Link: [https://pitp.zoom.us/meeting/register/tJcqc-ihqzMvHdW-YBm7mYd\\_XP9Amhypv5vO](https://pitp.zoom.us/meeting/register/tJcqc-ihqzMvHdW-YBm7mYd_XP9Amhypv5vO)



# Toward realization of novel superconductivity based on twisted van der Waals Josephson junction in cuprates

Philip Kim

Department of Physics, Harvard University

# Acknowledgment



## Experiment

Frank Zhao, Nicolar Poccia, Xiaomeng Cui, Hyobin Yoo, Joon Young Park, Yuval Ronen, Rebecca Engelke



## TEM

Joules Gardener, Austin Akey (CNS); Sangmin Lee, Miyoung Kim (SNU)

## Samples

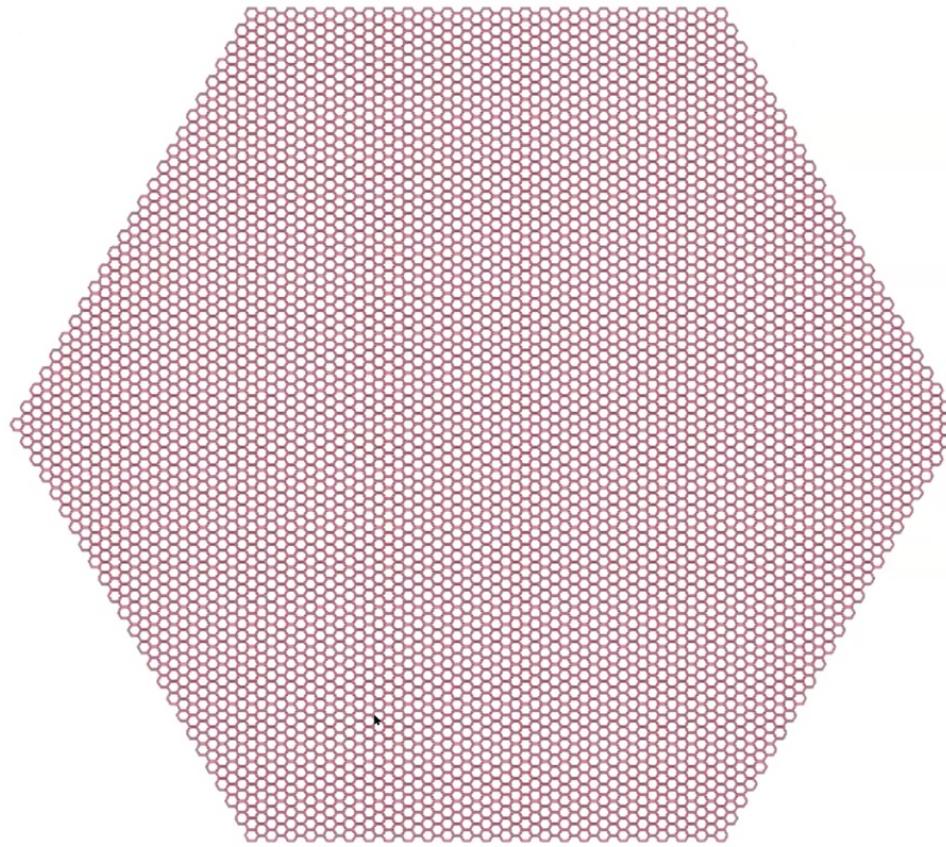
Rudan Zhong, Genda Gu (BNL); Kenji Watanabe, Takashi Taniguchi (NIMS)

## Theory

Pavel Volkov, Jed Pixley (Rutgers); Tarun Tummuru, Stephan Plugge, Marcel Franz (UBC)



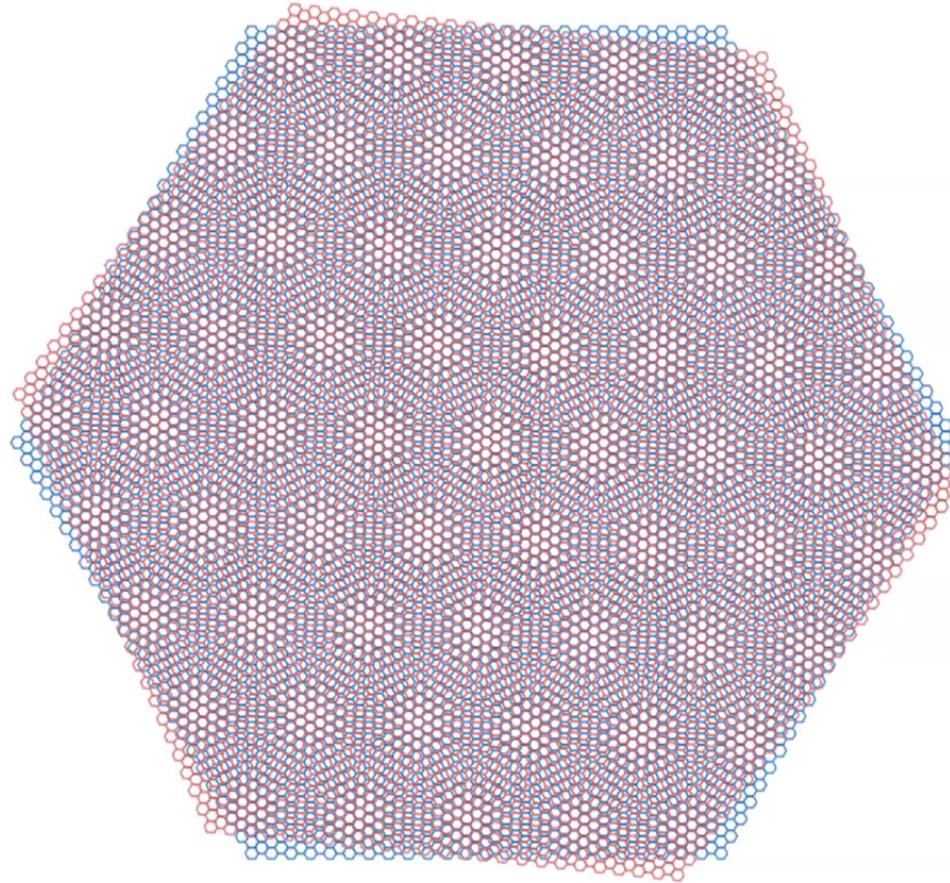
# Moire Superlattice Engineering in van der Waals Interface



Twisted van der Waals interface of homo & hetero structure

Animation from Jarillo-Herrero group

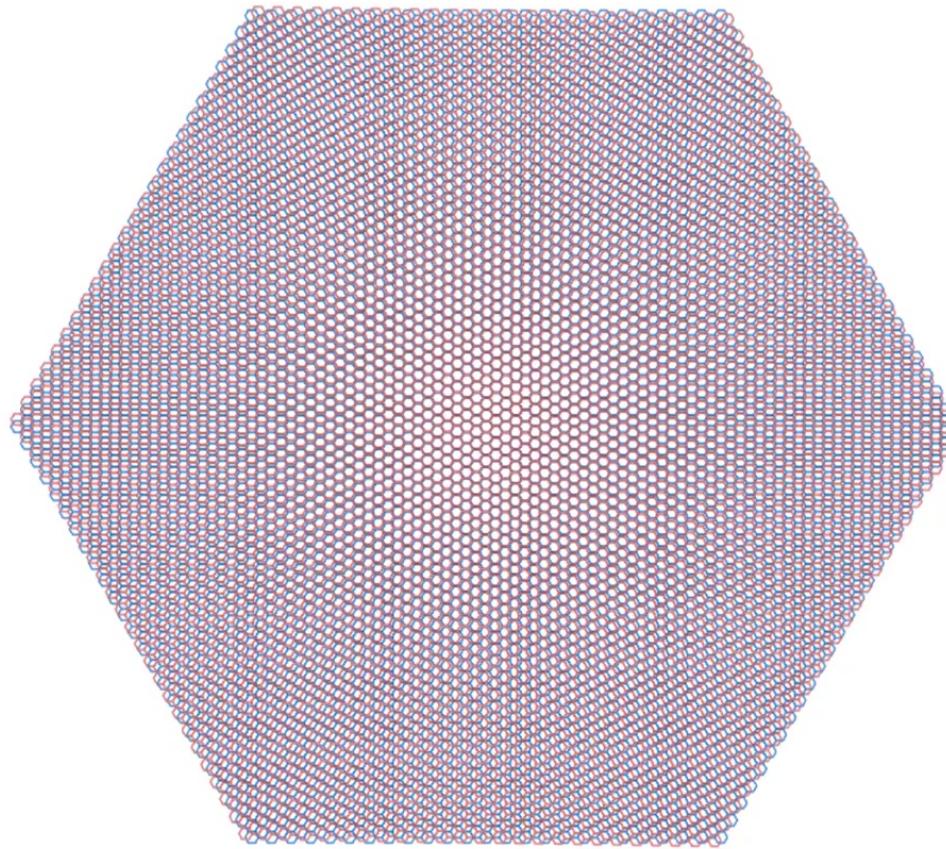
# Moire Superlattice Engineering in van der Waals Interface



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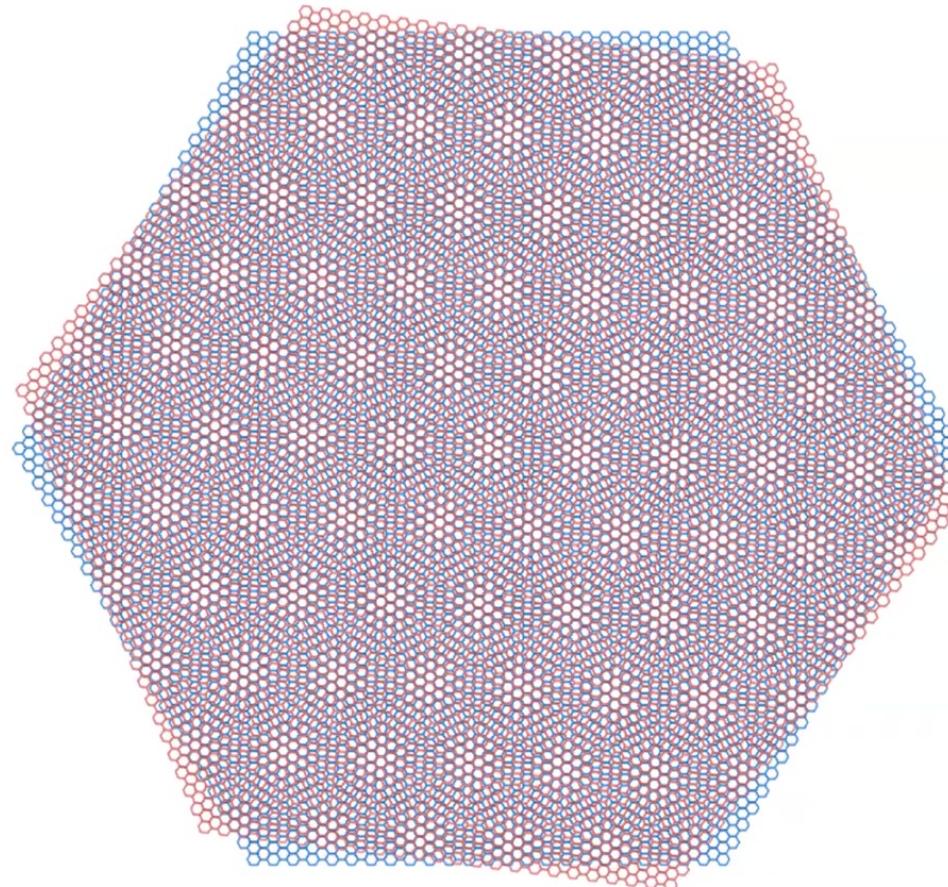
# Moire Superlattice Engineering in van der Waals Interface



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# Correlated Quantum State in Twisted Graphene Bilayer



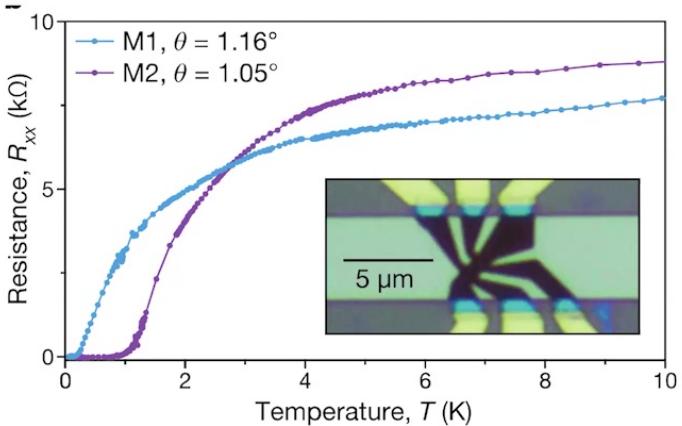
## ARTICLE

5 APRIL 2018 | VOL 556 | NATURE | 43

doi:10.1038/nature26160

## Unconventional superconductivity in magic-angle graphene superlattices

Yuan Cao<sup>1</sup>, Valla Fatemi<sup>1</sup>, Shiang Fang<sup>2</sup>, Kenji Watanabe<sup>2</sup>, Takashi Taniguchi<sup>2</sup>, Elithimios Kaxiras<sup>2,4</sup> & Pablo Jarillo-Herrero<sup>1</sup>



### Correlated insulator

Cao et al., Nature 556, 80–84 (2018).

Burg et al., PRL 123, 197702 (2019).

### Unconventional superconductivity

Cao et al., Nature 556, 43–50 (2018).

Yankowitz et al., Science 363, 1059–1064 (2019).

Lu et al., Nature 574, 653–657 (2019).

### Magnetism and Quantum Anomalous Hall Effect

Sharpe et al., Science 365, 605–608 (2019).

Serlin et al., arXiv:1907.00261 (2019).

### Trilayers double bilayers

Chen et al., Nature Physics 15, 237–241 (2019).

Chen et al., Nature 572, 215219 (2019). She et al., ArXiv 2019

### Double bilayers

Shen et al., arXiv:1903.06952 (2019).

Liu et al., arXiv:1903.08130 (2019).

Cao et al., arXiv:1903.08596 (2019).

Adak et al., arXiv:2001.09916 (2020)

### TMDC/TMDC; TMDC/TBG

Tang et al., arXiv:1910.08673 (2019).

Regan et al., arXiv:1910.09047 (2019).

Wang et al., arXiv:1910.12147 (2019).

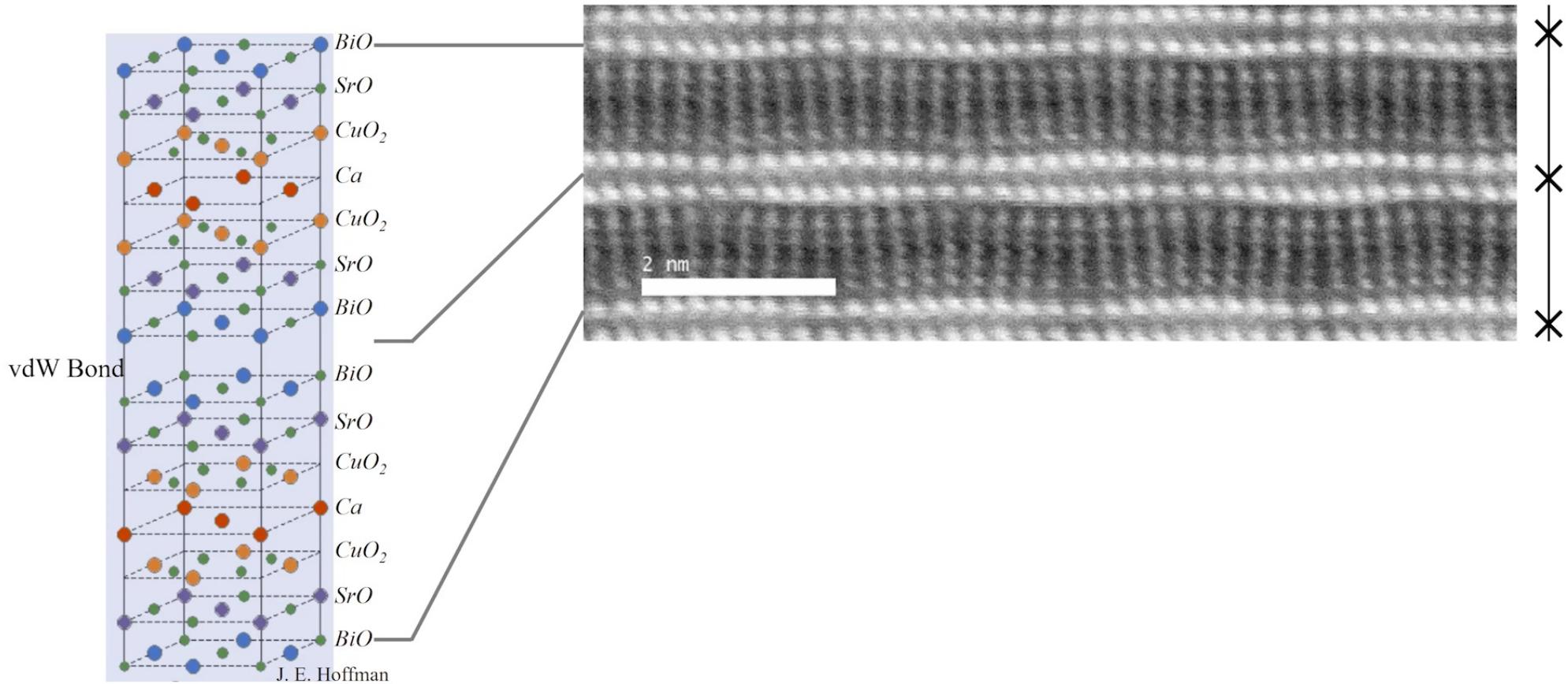
Arora et al., Nature 583, 379 (2020)

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# $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$ : A Cuprate van der Waals Material



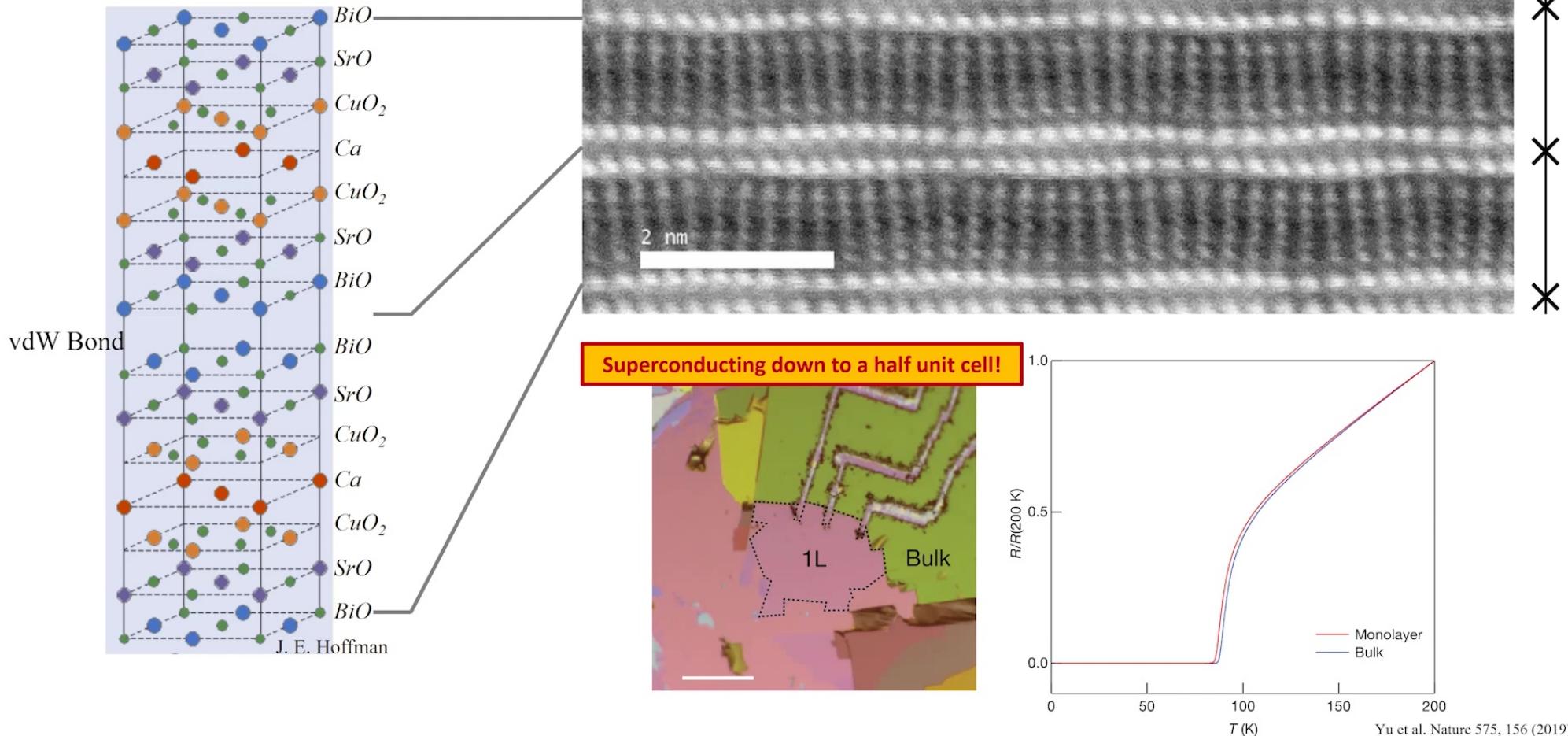
N. Poccia et al. Phys. Rev. Mater. 4, 114007 (2020)



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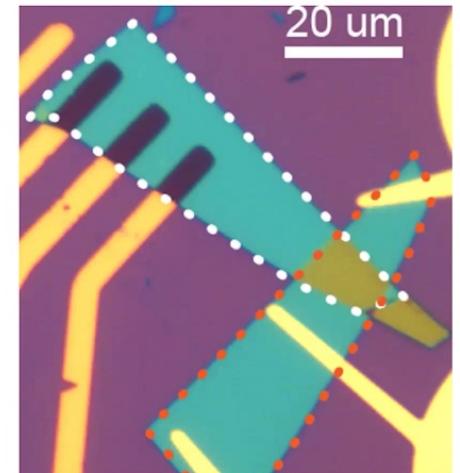


# Twisted Cuprate Junctions



## High-temperature topological superconductivity in twisted double-layer copper oxides

Oguzhan Can<sup>1,2</sup>, Tarun Tummuru<sup>1,2</sup>, Ryan P. Day<sup>1,2</sup>, Ilya Elfimov<sup>1,2</sup>, Andrea Damascelli<sup>1,2</sup> and  
Marcel Franz<sup>1,2</sup>✉



S. Y. F Zhao et al., arXiv 2108.13455

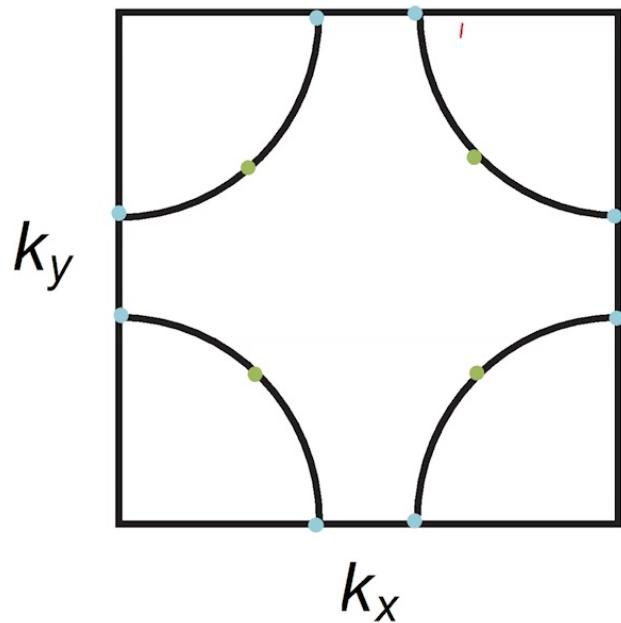
## Magic angles and current-induced topology in twisted nodal superconductors

Pavel A. Volkov,\* Justin H. Wilson, and J. H. Pixley  
*Department of Physics and Astronomy, Center for Materials Theory,  
Rutgers University, Piscataway, NJ 08854, USA*  
(Dated: December 16, 2020)

# Nodal d-wave Superconductor



Cuprate Brillouin Zone



Gap vanishes at the nodal points

D-wave order parameter

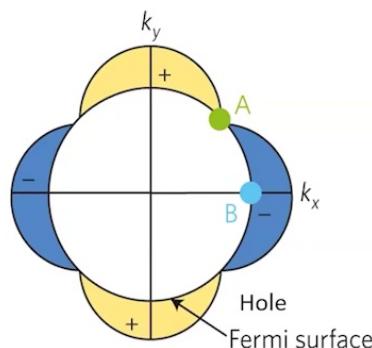
$$\Delta_{\mathbf{k}} = \Delta_0 (\cos k_x - \cos k_y)$$

BdG Hamiltonian:

$$\hat{H} = \sum_{\mathbf{k}} \begin{pmatrix} c_{\uparrow}(\mathbf{k}) \\ c_{\downarrow}^{\dagger}(\mathbf{k}) \end{pmatrix}^{\dagger} \begin{pmatrix} \varepsilon(\mathbf{k}) & \Delta(\mathbf{k}) \\ \Delta^*(\mathbf{k}) & -\varepsilon(\mathbf{k}) \end{pmatrix} \begin{pmatrix} c_{\uparrow}(\mathbf{k}) \\ c_{\downarrow}^{\dagger}(\mathbf{k}) \end{pmatrix}$$

$$\approx \sum_{\mathbf{k}} \begin{pmatrix} c_{\uparrow}(\mathbf{k}) \\ c_{\downarrow}^{\dagger}(\mathbf{k}) \end{pmatrix}^{\dagger} \begin{pmatrix} \mathbf{v}_F \cdot \mathbf{p} & \mathbf{v}_{\Delta} \cdot \mathbf{p} \\ \mathbf{v}_{\Delta} \cdot \mathbf{p} & -\mathbf{v}_F \cdot \mathbf{p} \end{pmatrix} \begin{pmatrix} c_{\uparrow}(\mathbf{k}) \\ c_{\downarrow}^{\dagger}(\mathbf{k}) \end{pmatrix}$$

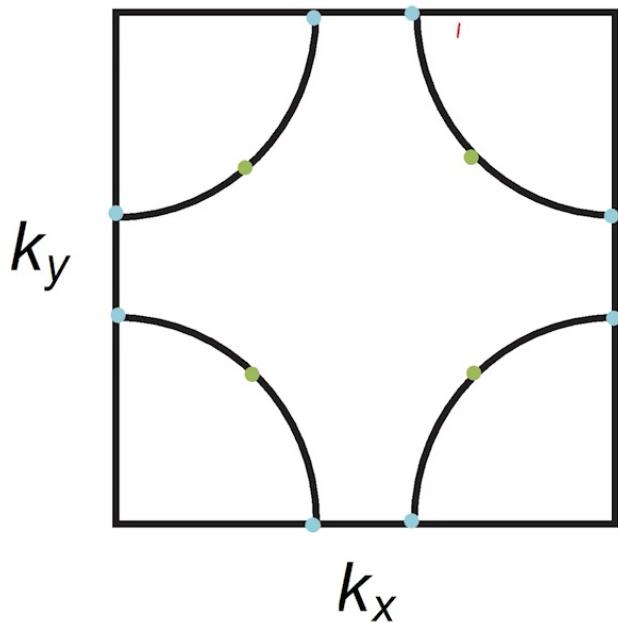
near the nodal points



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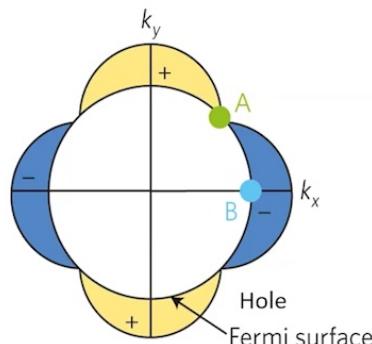
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near the nodal points

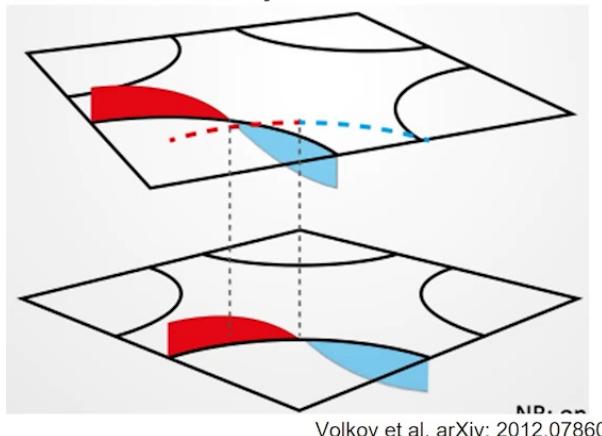
$$E_{0,\pm}(\mathbf{k}) = \pm \sqrt{v_F^2 k_{\parallel}^2 + v_{\Delta}^2 k_{\perp}^2}$$



# Twisted Cuprate Junction



Stacked twist layer



Double layer Nambu basis

$$\Psi_{\mathbf{k}} = (c_{\mathbf{k}\uparrow 1}, c_{-\mathbf{k}\downarrow 1}^\dagger, c_{\mathbf{k}\uparrow 2}, c_{-\mathbf{k}\downarrow 2}^\dagger)^T$$

BdG Hamiltonian

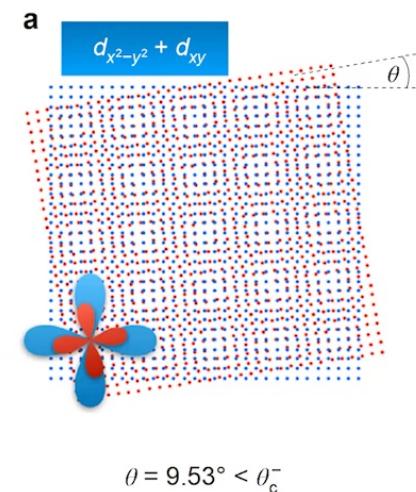
$$\mathcal{H} = \sum_{\mathbf{k}} \Psi_{\mathbf{k}}^\dagger h_{\mathbf{k}} \Psi_{\mathbf{k}} + E_0.$$

layer1      Interlayer coupling      layer2

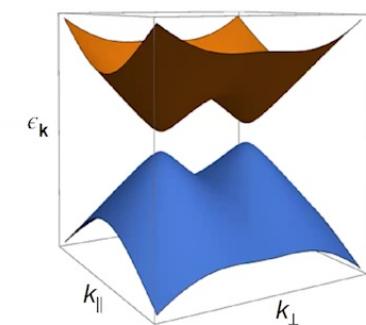
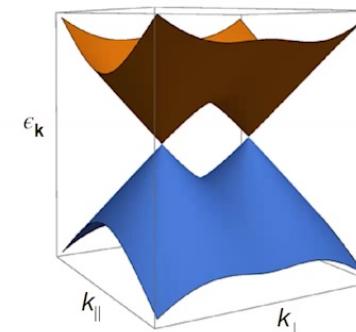
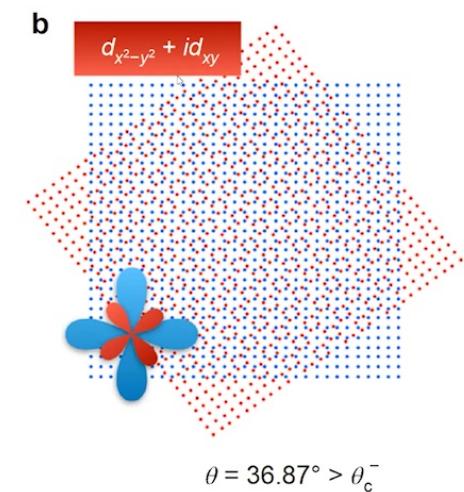
$$h_{\mathbf{k}} = \begin{pmatrix} \xi_{\mathbf{k}} & \Delta_{\mathbf{k}1} & g & 0 \\ \Delta_{\mathbf{k}1}^* & -\xi_{\mathbf{k}} & 0 & -g \\ g & 0 & \xi_{\mathbf{k}} & \Delta_{\mathbf{k}2} \\ 0 & -g & \Delta_{\mathbf{k}2}^* & -\xi_{\mathbf{k}} \end{pmatrix}$$



Small twist angle



Large twist angle

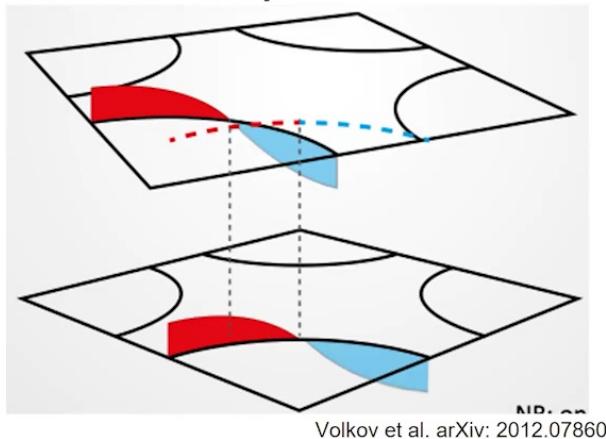


Can et al. Nature Phys (2021)

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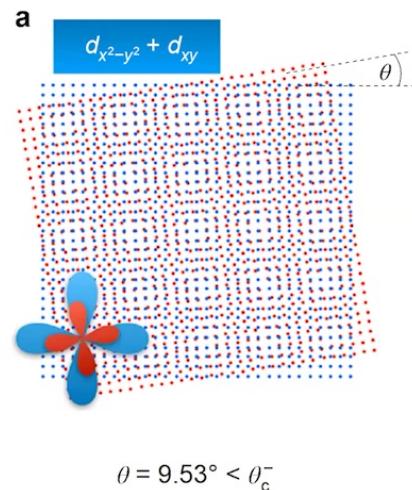
BdG Hamiltonian

$$\mathcal{H} = \sum_{\mathbf{k}} \Psi_{\mathbf{k}}^\dagger h_{\mathbf{k}} \Psi_{\mathbf{k}} + E_0.$$

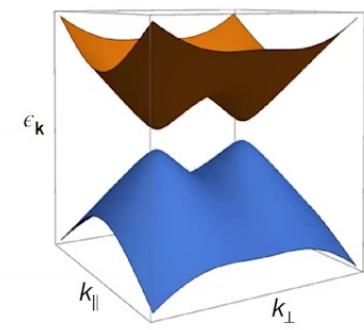
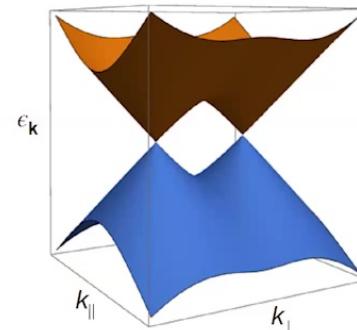
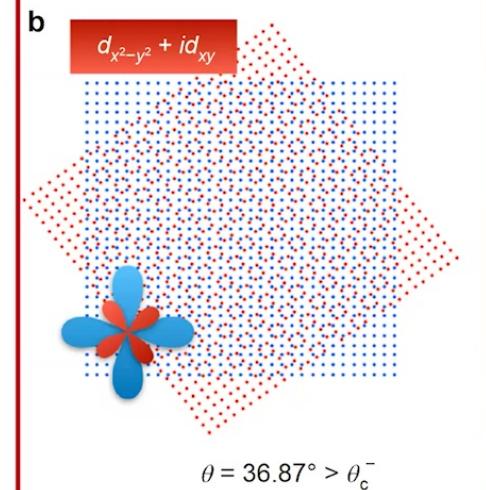
layer1      Interlayer coupling      layer2

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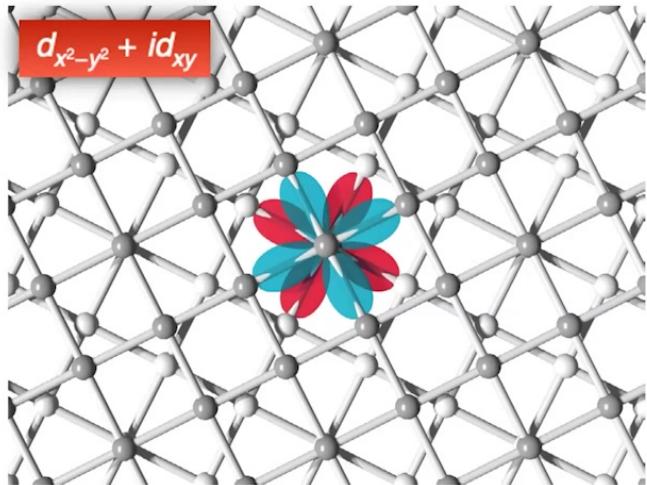


Large twist angle

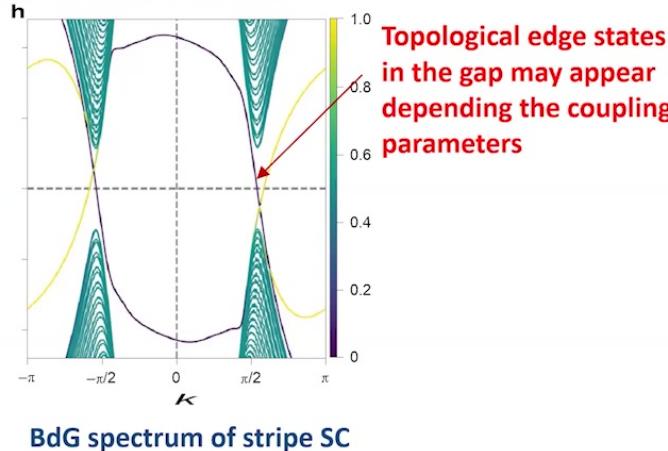
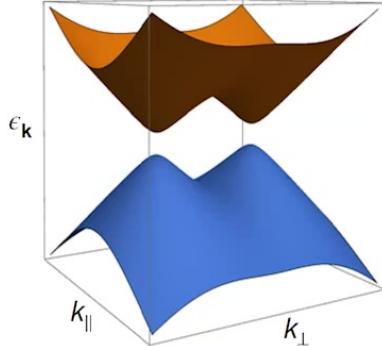


Can et al. Nature Phys (2021)

# 45° Twisted Junction: Superconductivity with Broken TRS



No nodal points: bulk has SC gap always!



BdG Free Energy

$$\mathcal{F}(\varphi) = E_0 - 2k_B T \sum_{k,a=\pm} \ln[2\cosh[E_{ka}(\varphi)/2k_B T]]$$

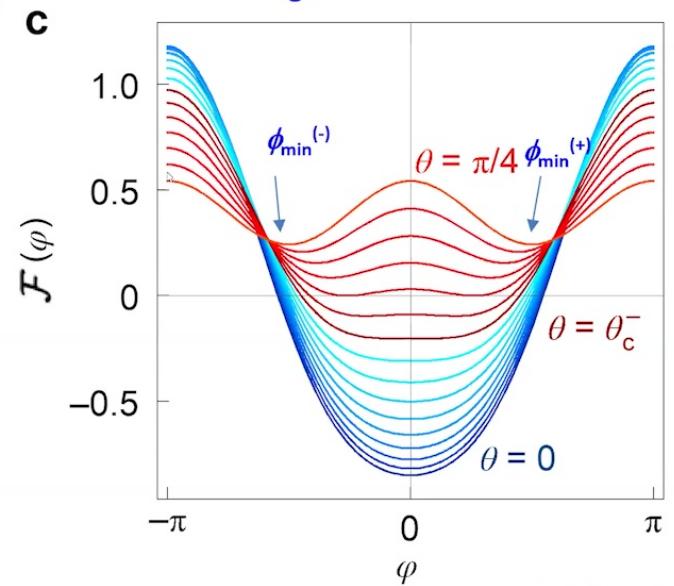
Ginzburg Landau Free Energy

$$\mathcal{F}(\varphi) = \mathcal{F}_0 + 2B_0\psi^2[-\cos(2\theta)\cos\varphi + \mathcal{K}\cos(2\varphi)]$$

Phase diff. between SCs

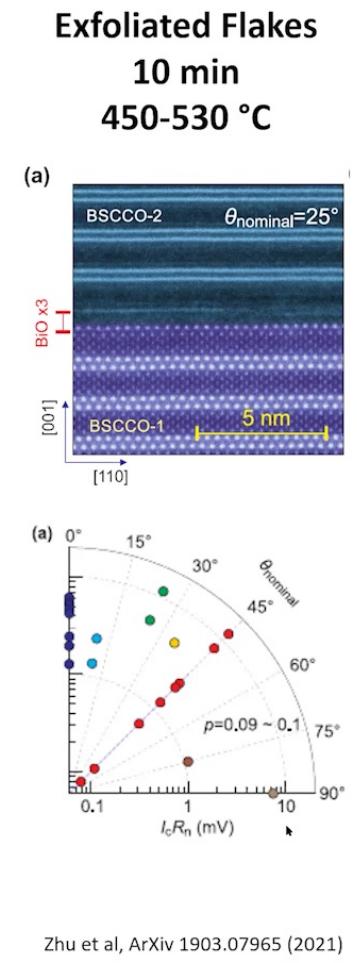
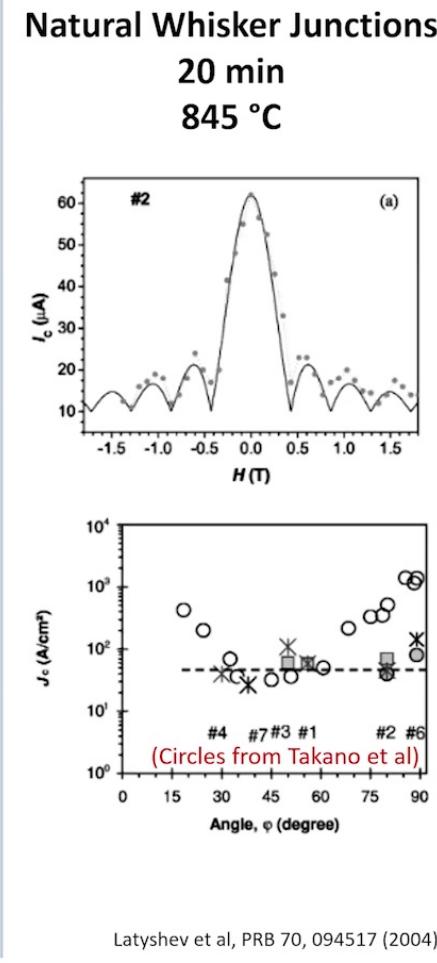
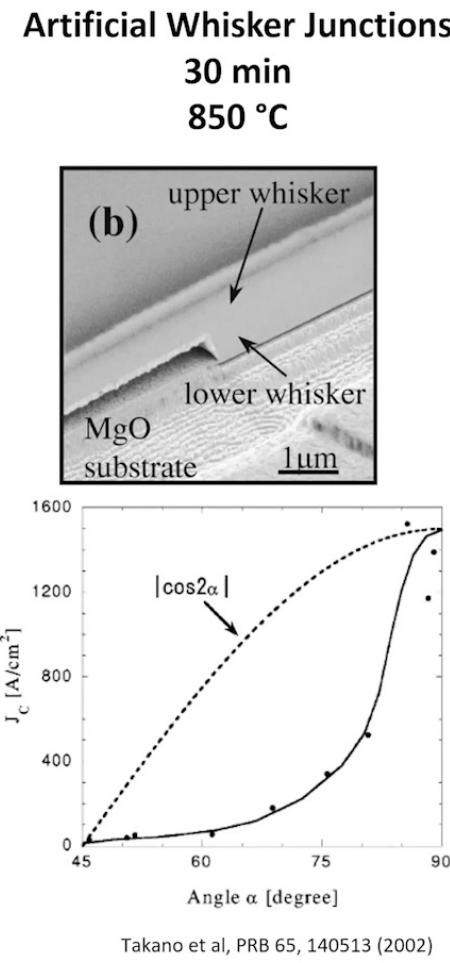
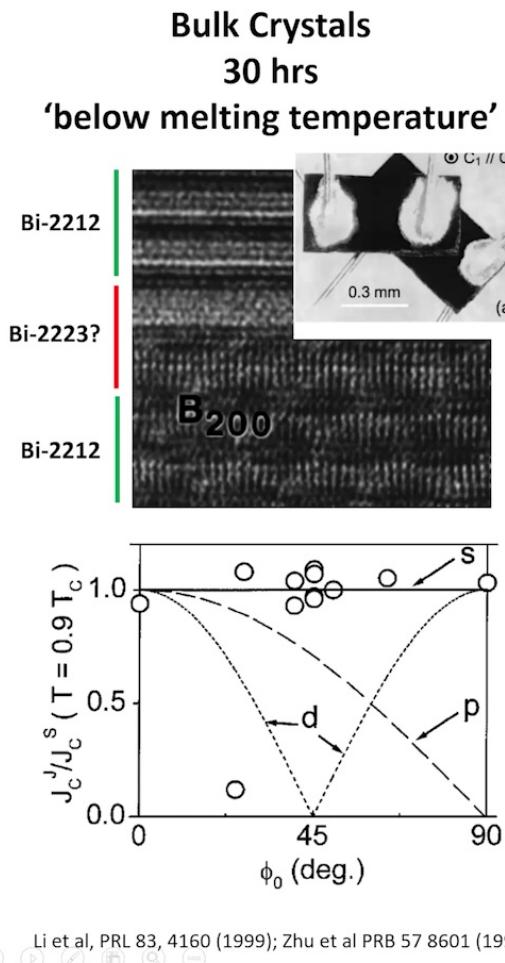
c

Twisted angle



Can et al. Nature Phys (2021)

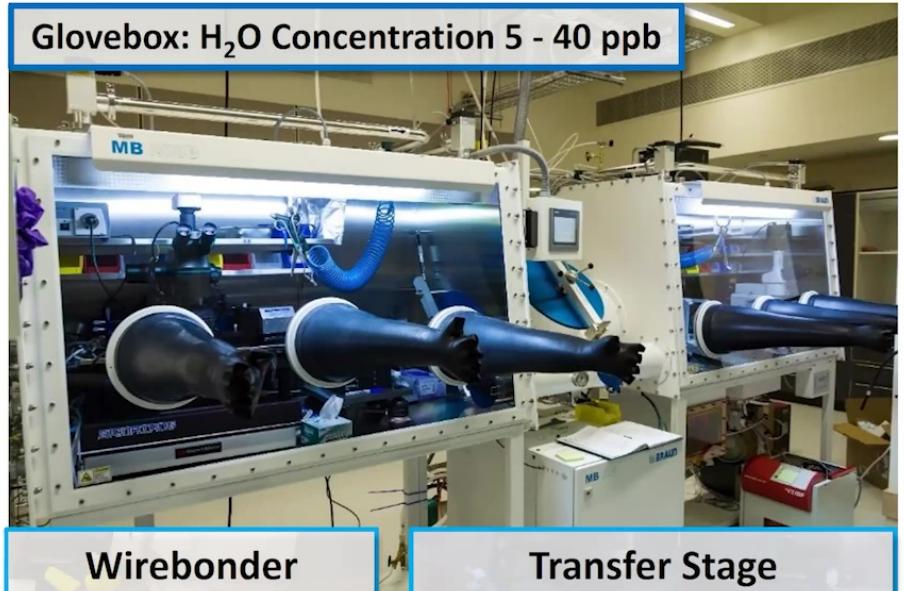
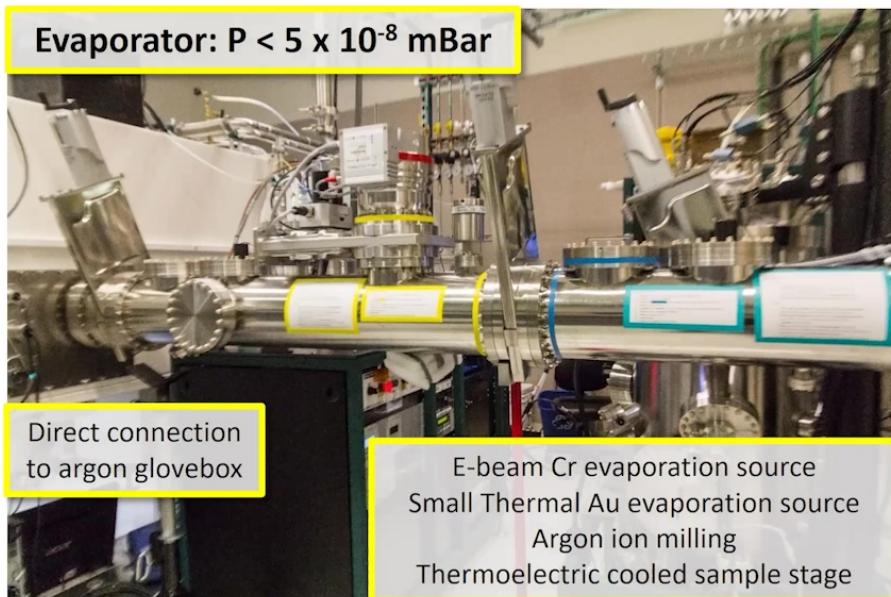
# Experiments on Twist Cuprate Josephson Junctions



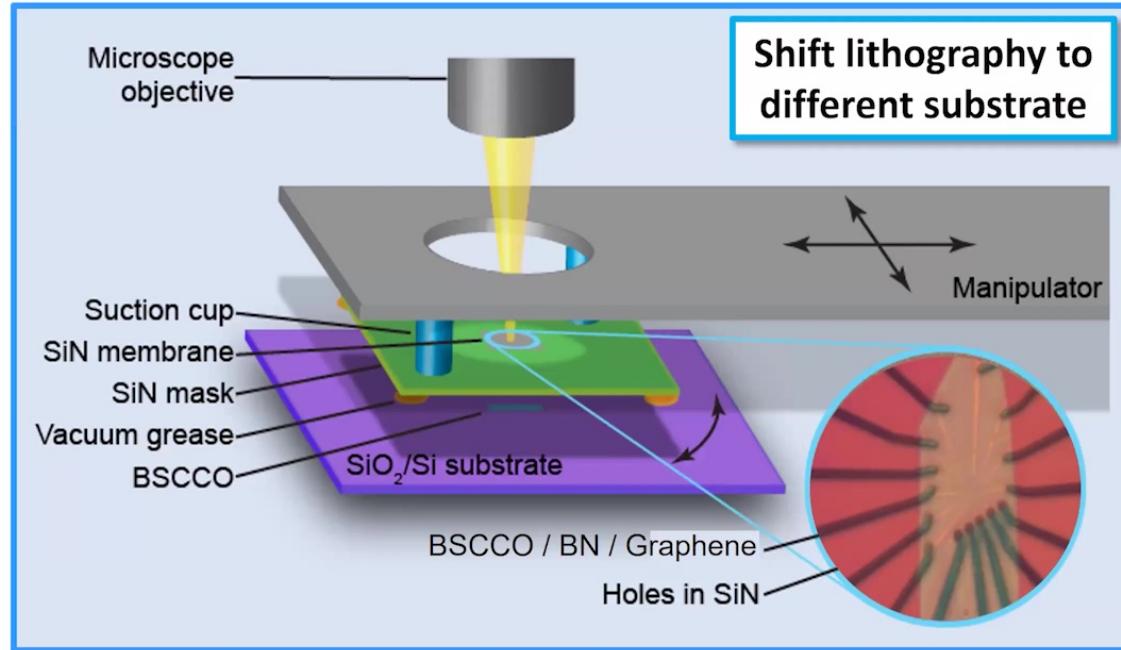
# Fab in a Glovebox UHV



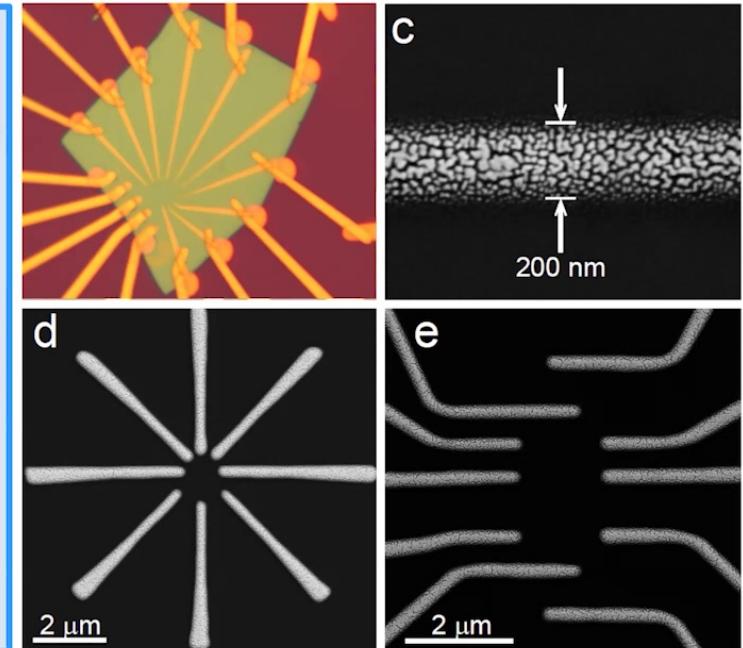
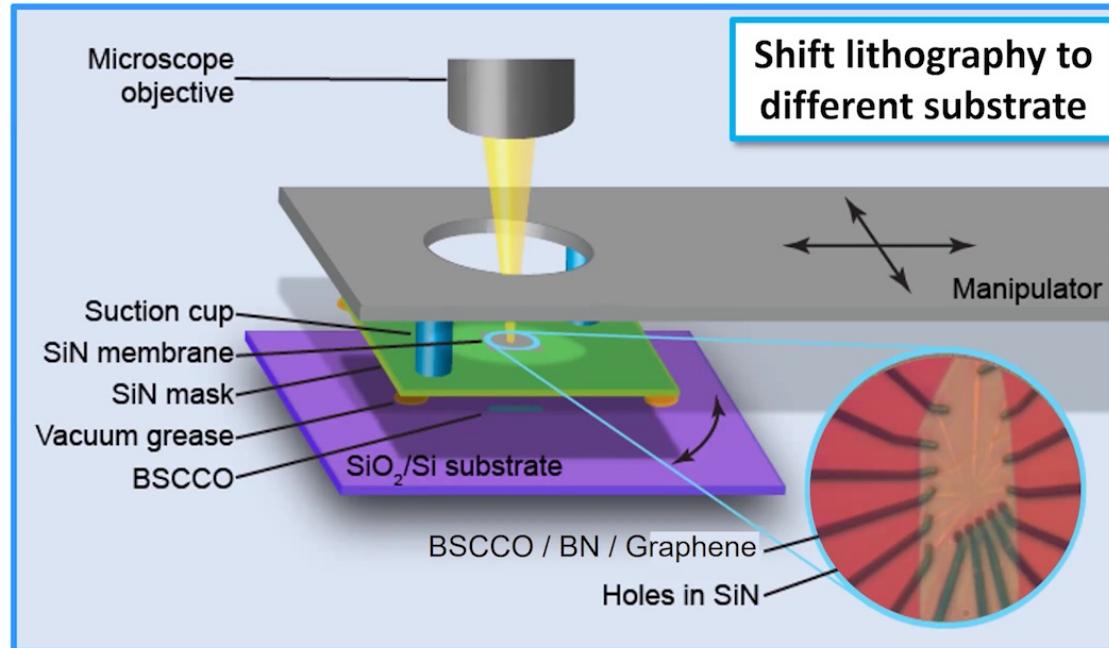
- *Stacking*
- *Selection*
- ✓ *Deposition*
- ✓ *Etch*
- ✓ *Packaging*



# Stencil Mask Lithography



# Stencil Mask Lithography



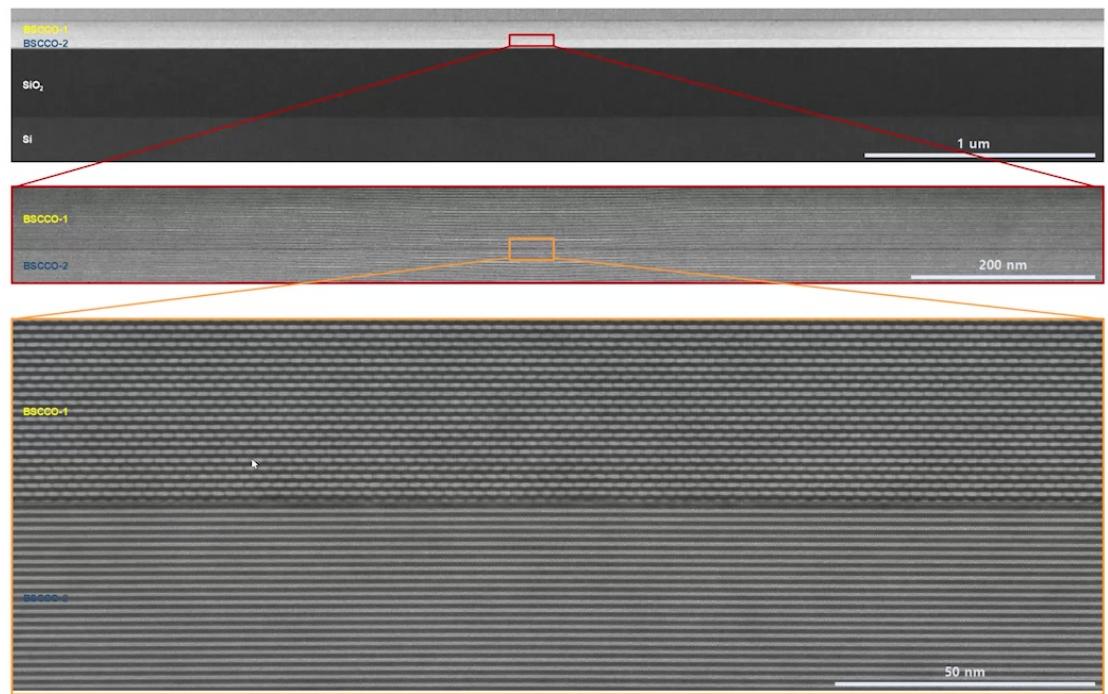
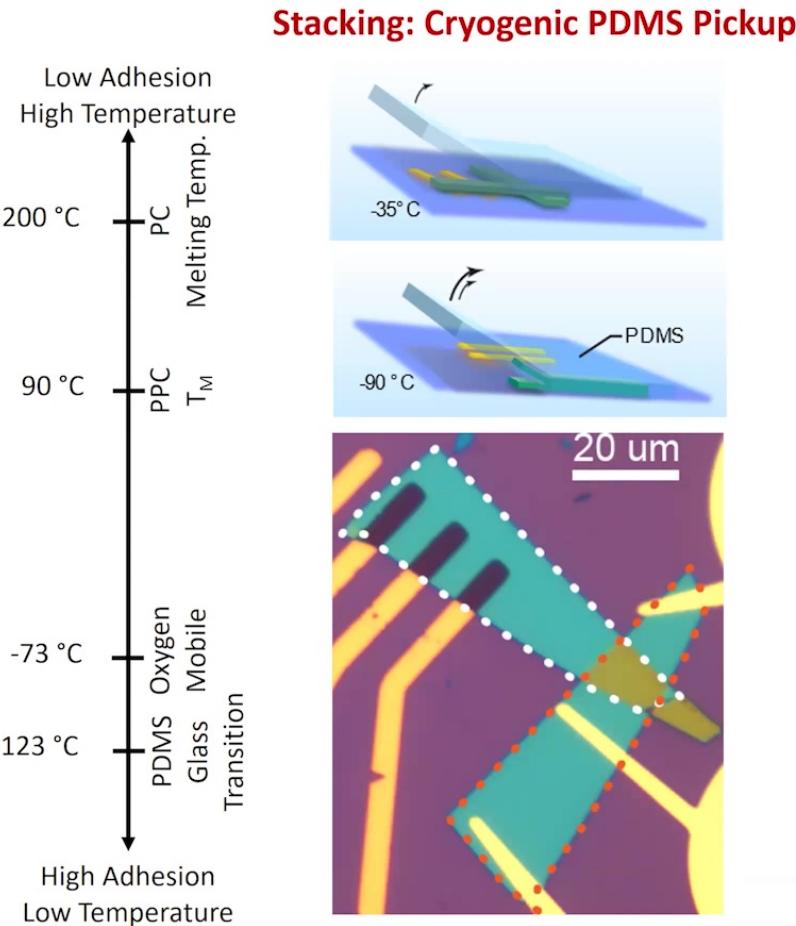
## Technique advantages:

- No air exposure
- No heating
- No solvent, no residue.

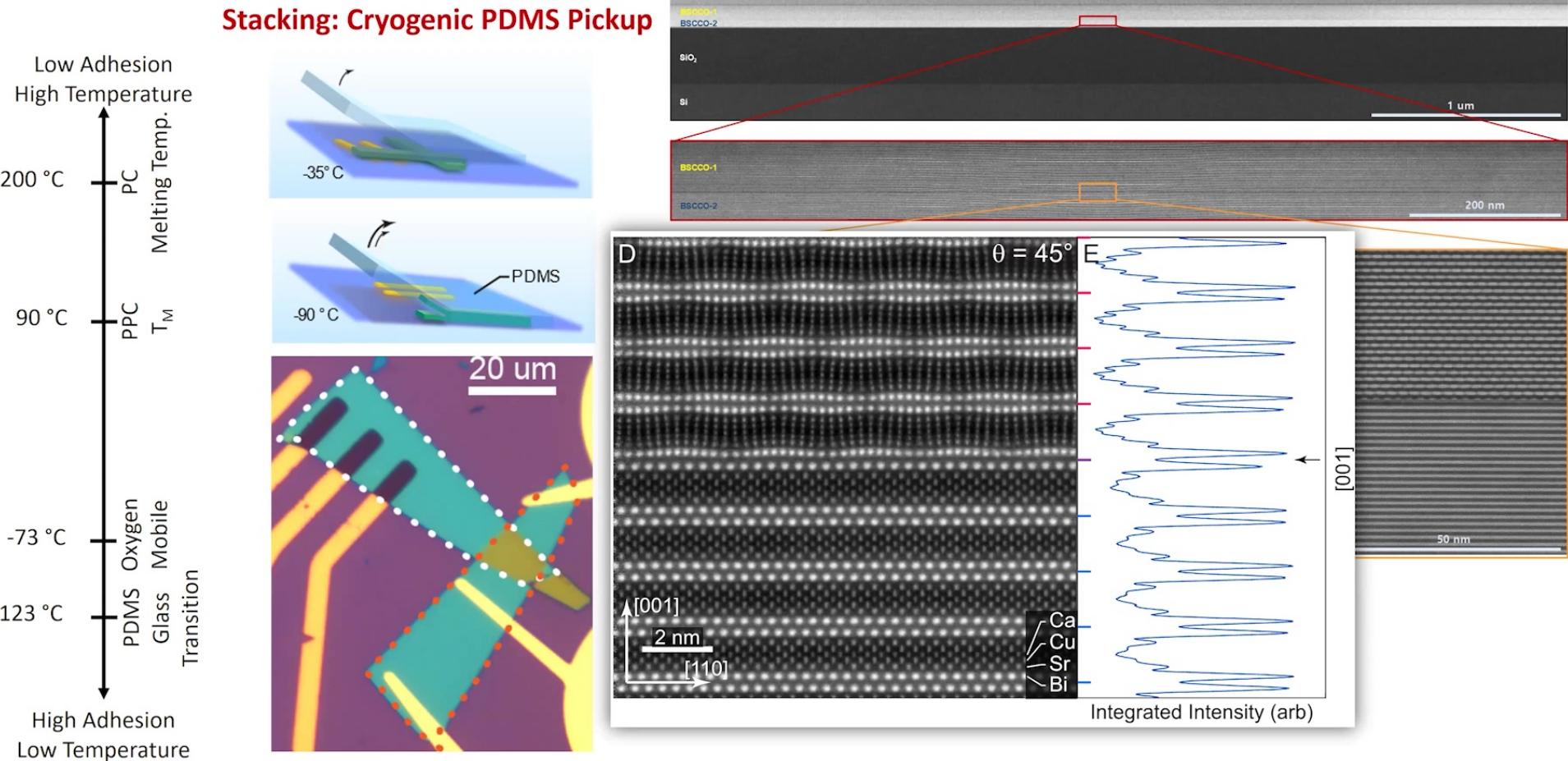
## Technique capabilities

- |             |          |
|-------------|----------|
| Resolution: | < 200 nm |
| Alignment:  | < 1 μm   |

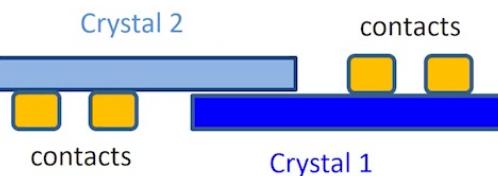
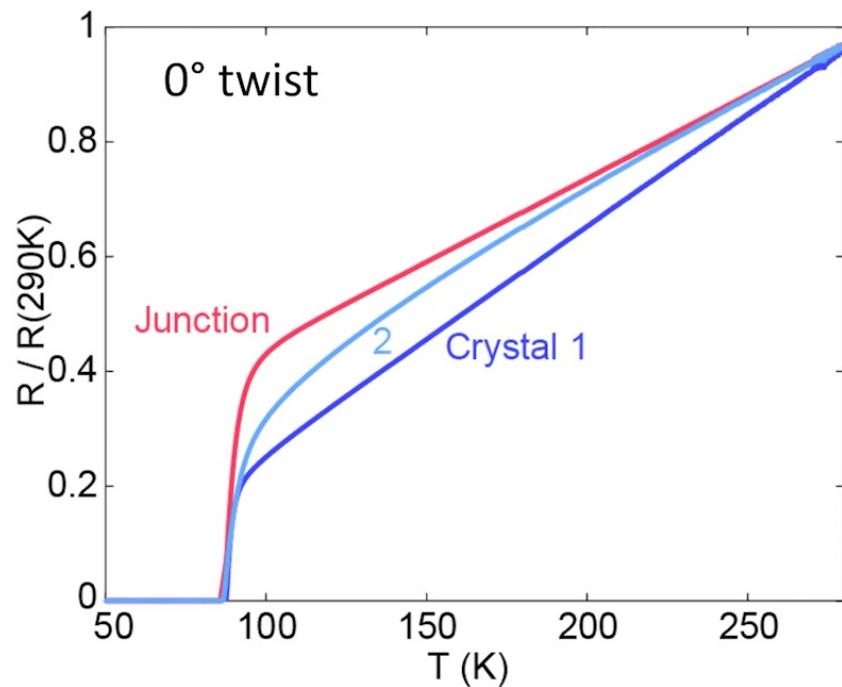
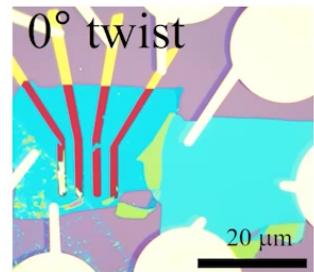
# Ultra-Clean twisted BSCCO Interface



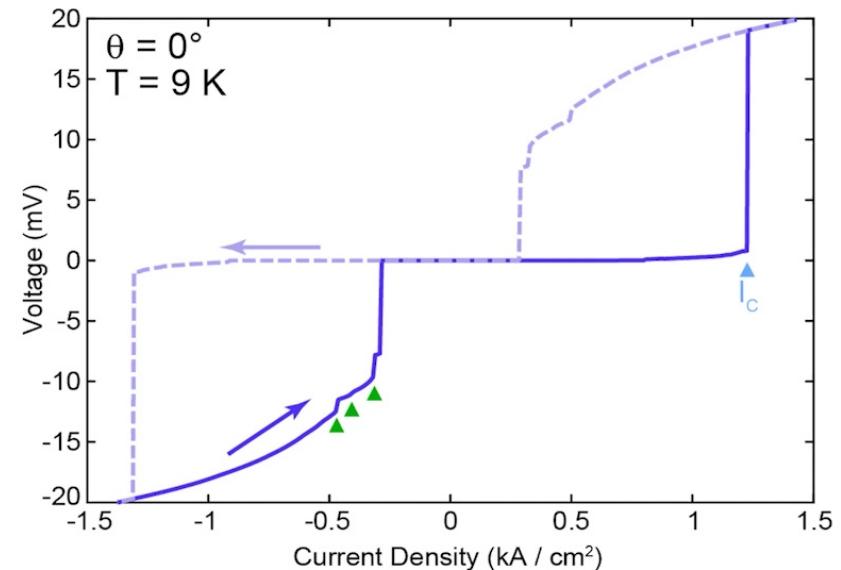
# Ultra-Clean twisted BSCCO Interface



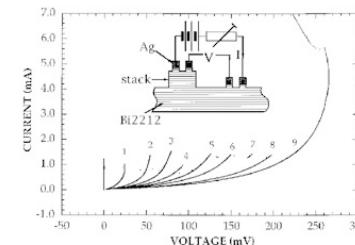
# Artificial Vertical Josephson Junction Characteristics



**Josephson Junction Characteristics: 0° twist**



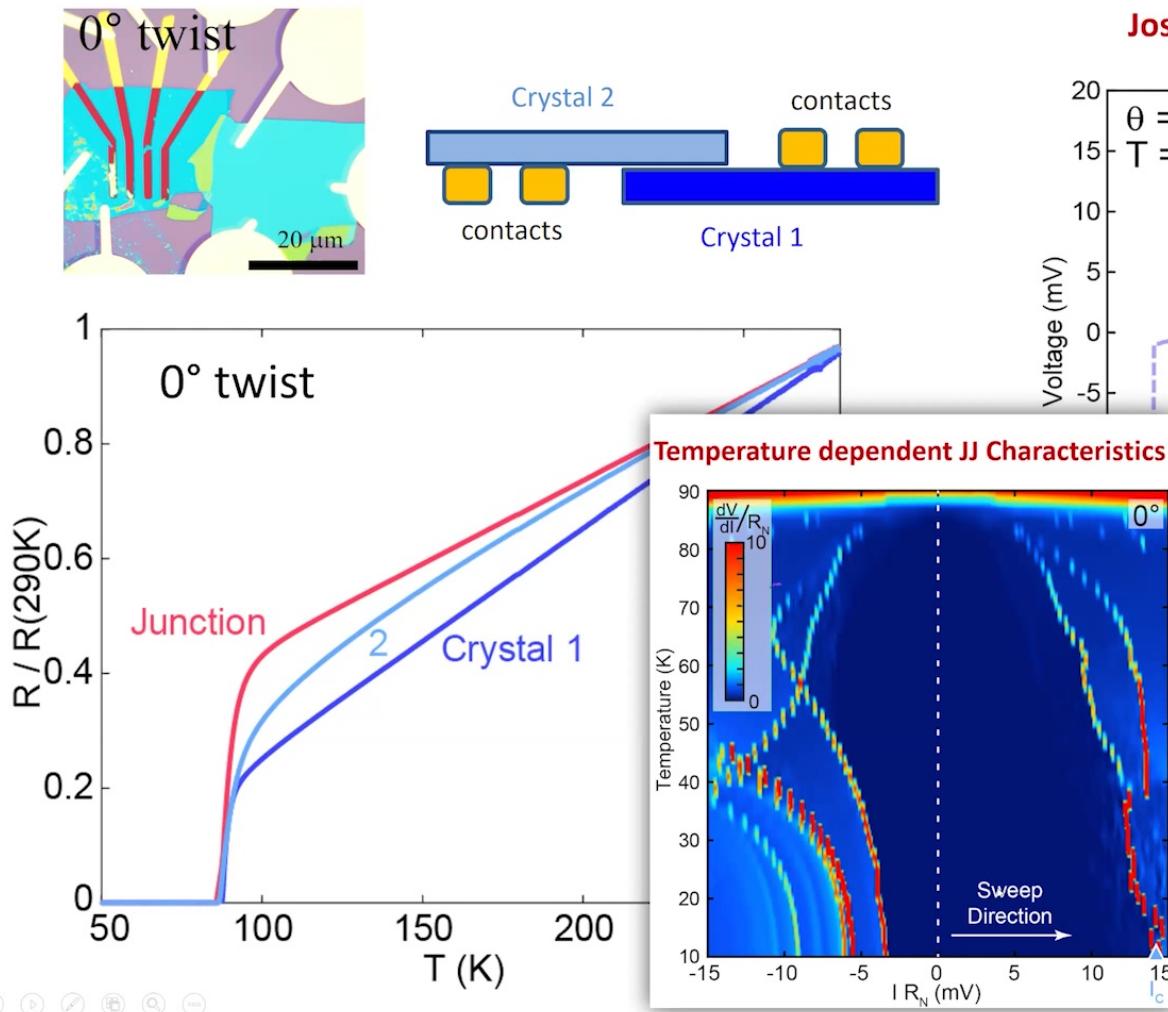
Critical switching current density is smaller than but comparable to intrinsic BSCCO JJ.



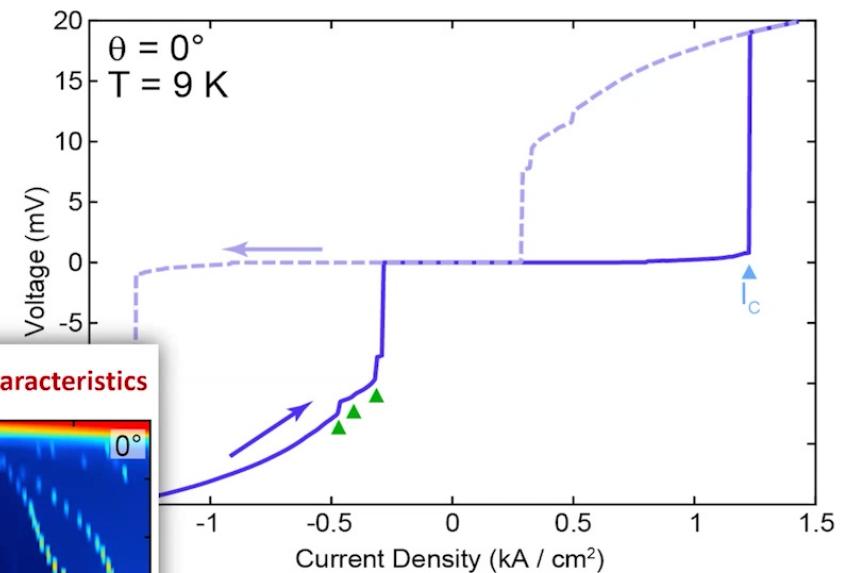
BSCCO intrinsic Junction  
Junction Area  $\sim 1000\text{ }\mu\text{m}^2$

Yurgens et. al., PRB 53 R8887 (1996)

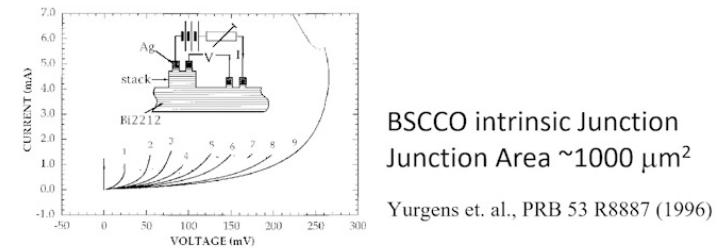
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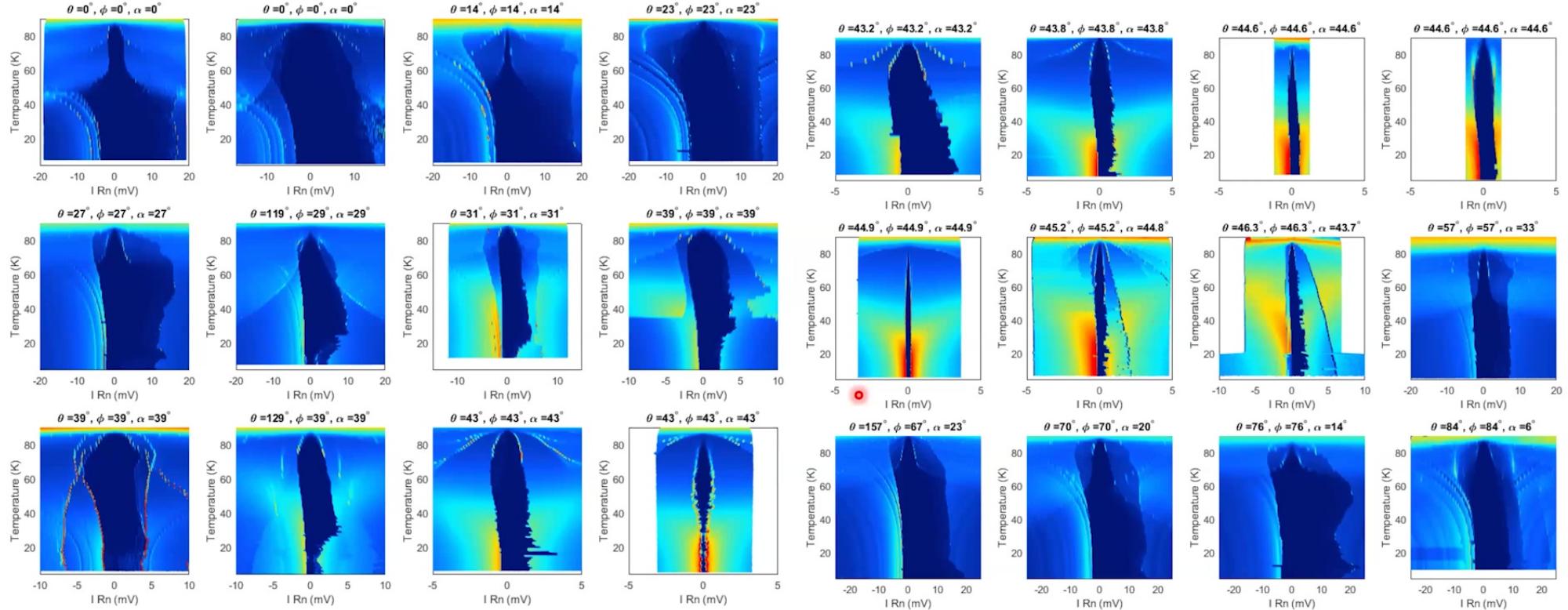
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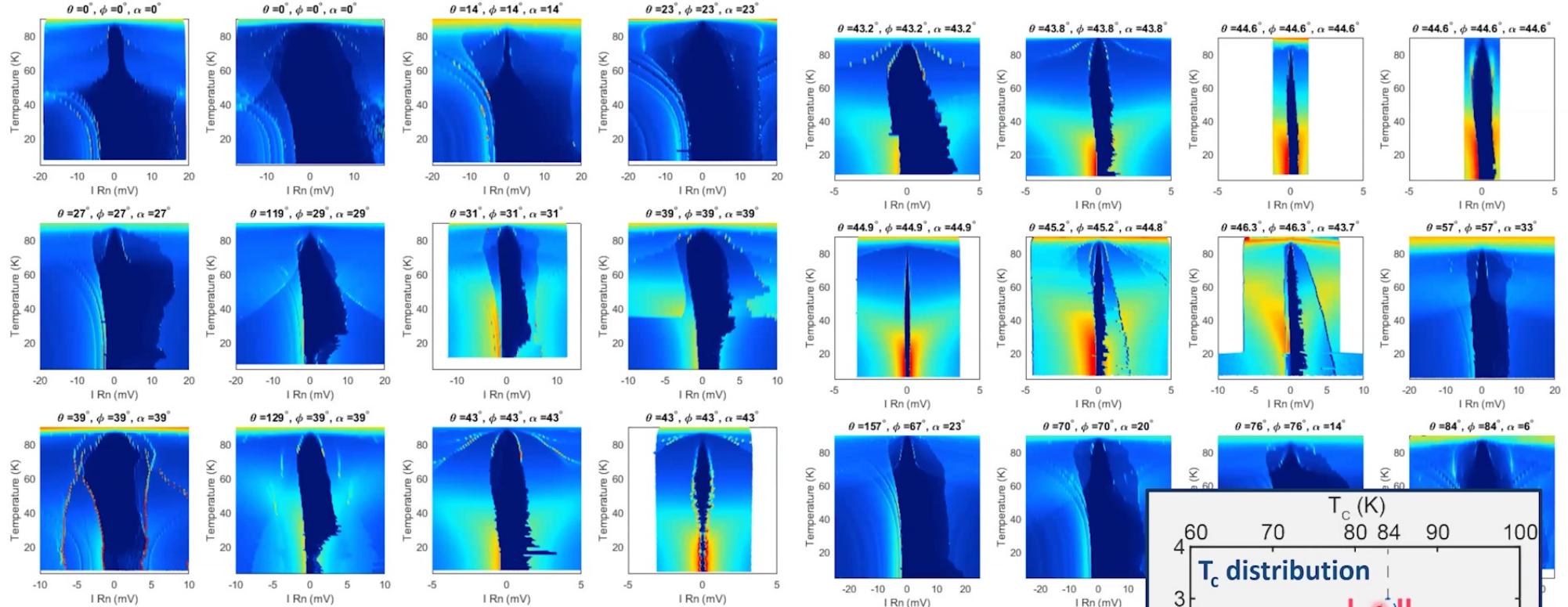


# Twisted BSCCO vdW Josephson Junctions

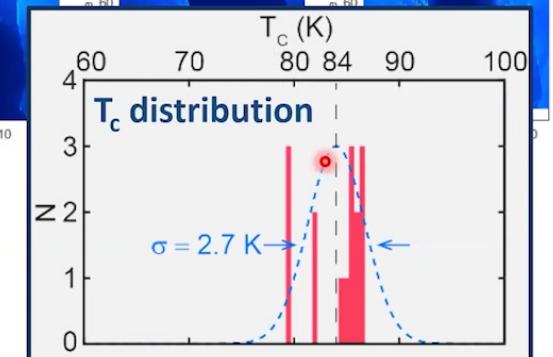


More than 24 junctions (so far):  $\theta$  ranges  $0^\circ$  to  $180^\circ$

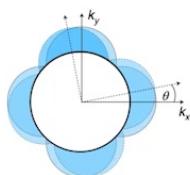
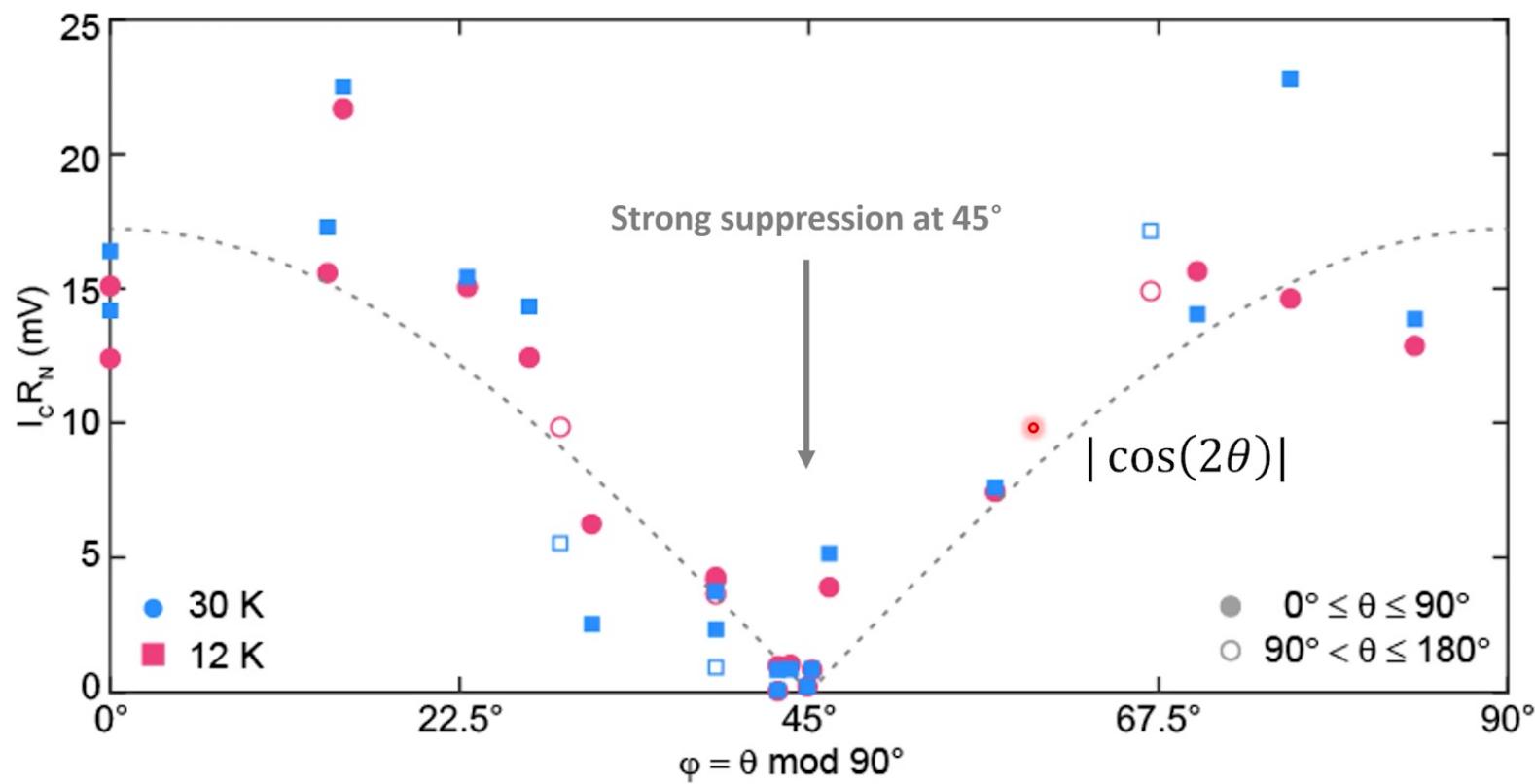
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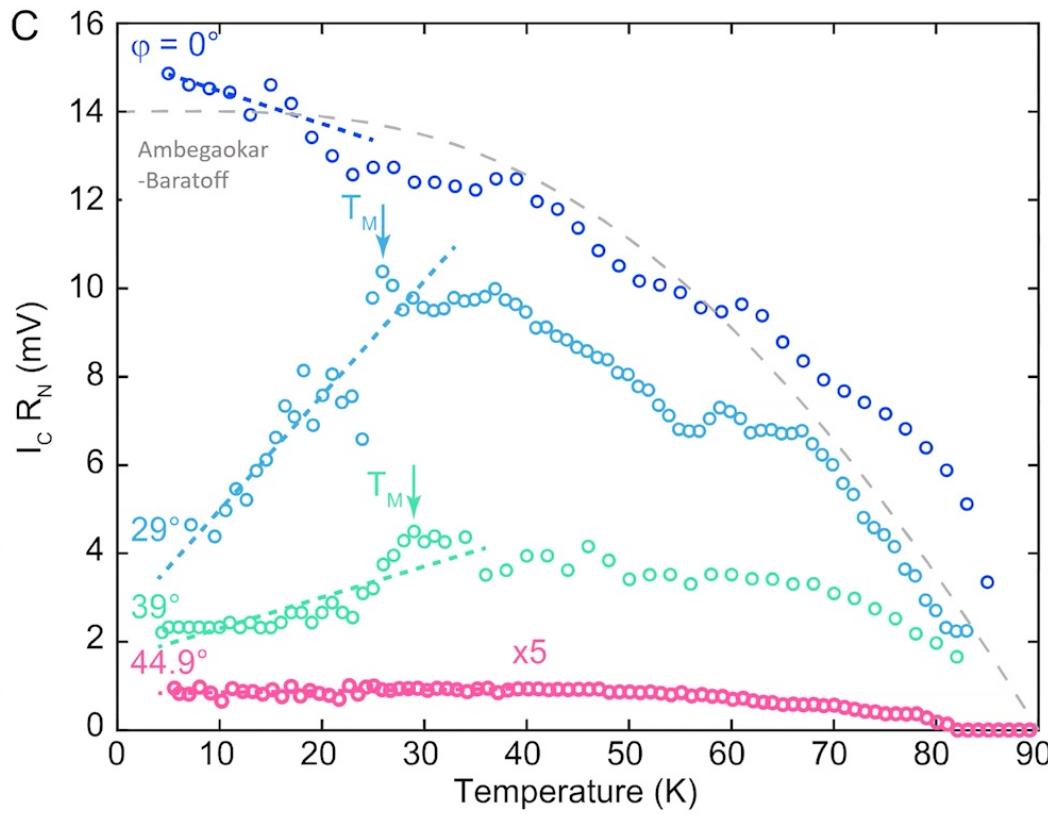
# Twisting Angle Dependence $I_c R_N$



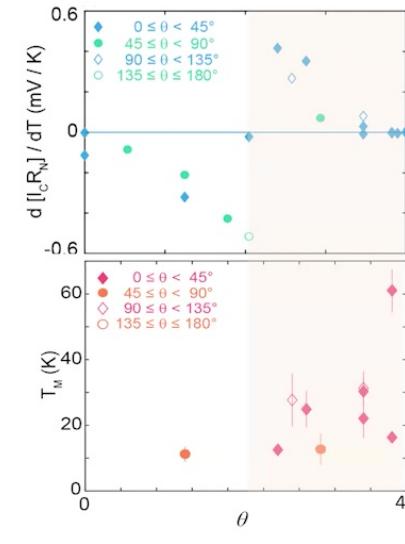
$$\Delta_{k1} = \Delta \cos(2\alpha_k + \theta), \quad \Delta_{k2} = \Delta \cos(2\alpha_k - \theta)$$

Twisted d-wave order parameters

# Temperature Dependent Critical Current



Non-monotonic temperature dependent  $I_c$



$0 \leq \theta \lesssim \pi/8$

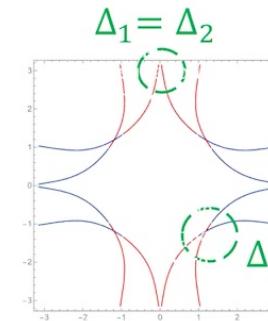
Decreasing  $I_c$  with increasing  $T$

$\pi/8 \lesssim \theta \lesssim \pi/4$

Increasing  $I_c$  with increasing  $T$  at low temperature (non-monotonic)

$\theta \approx \pi/4$

Suppressed (but finite)  $I_c$



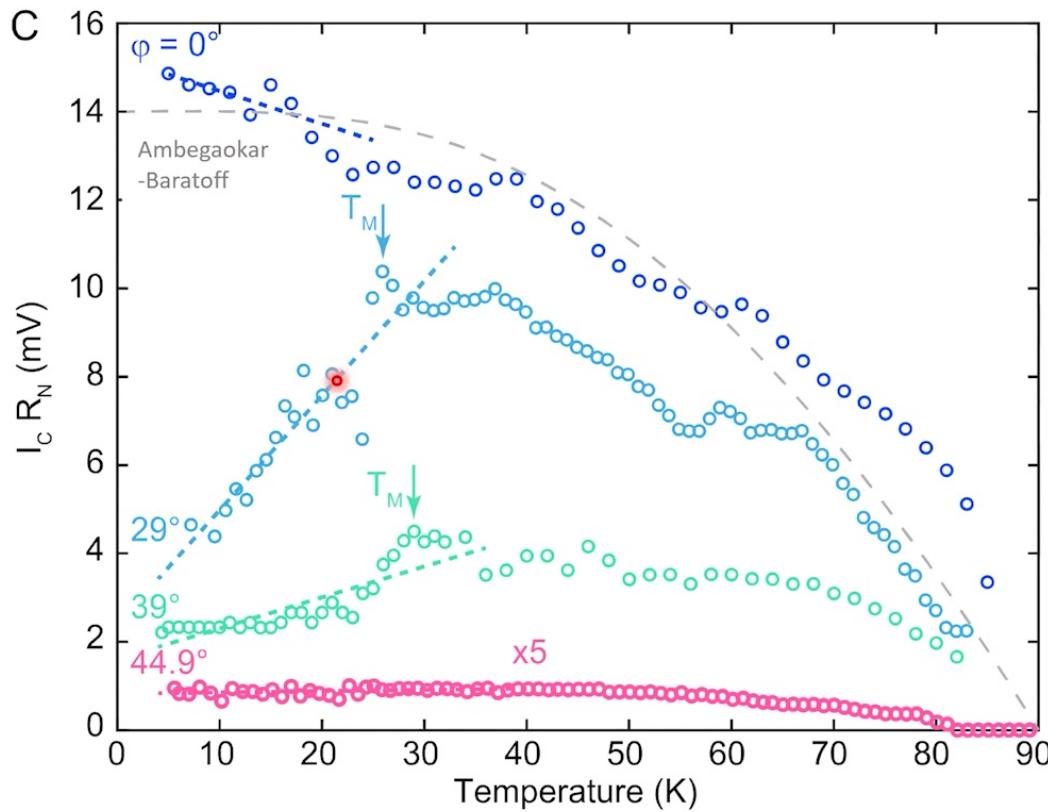
Supercurrent

$$J(\varphi) = \frac{2e}{\hbar} \frac{\partial \mathcal{F}(\varphi)}{\partial \varphi}$$

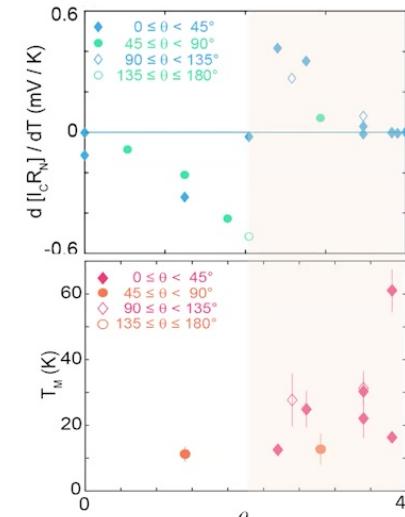
$$= \sin \varphi \frac{eg^2}{\hbar} \sum_k \Delta_{k1} \Delta_{k2} \sum_{a=\pm} \frac{\operatorname{atanh}(E_{ka}/2k_B T)}{E_{ka}(E_{k-}^2 - E_{k+}^2)}$$

$$> 0$$

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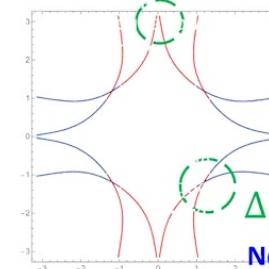
Increasing  $I_c$  with increasing  $T$  at low temperature (non-monotonic)

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Suppressed (but finite)  $I_c$

Anti-nodal contribution

$$\Delta_1 = \Delta_2$$



Nodal contribution

Supercurrent

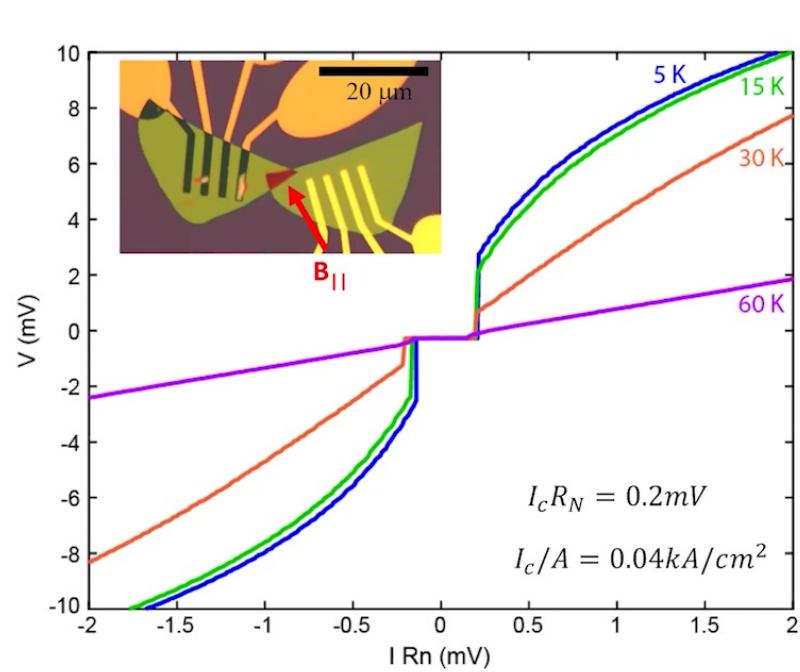
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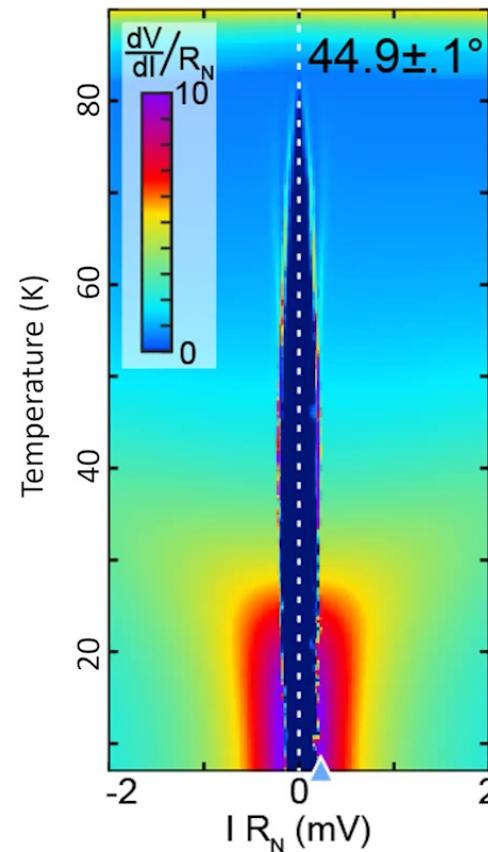
Competing nodal and anti-nodal supercurrent contributions!

# Near 45° Twisted Josephson Junctions

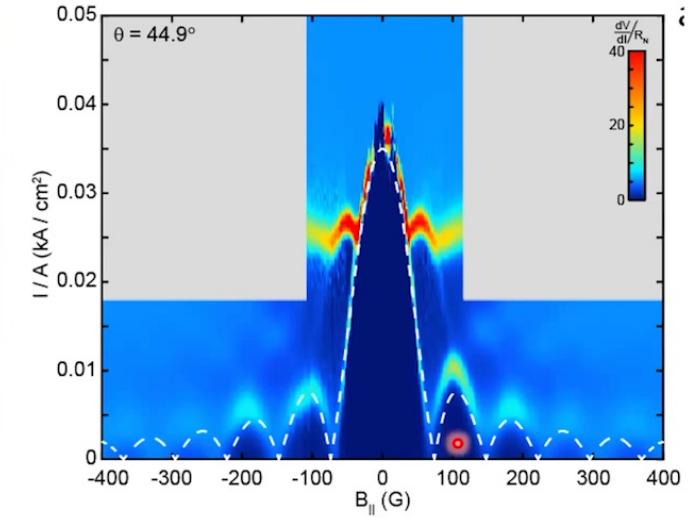


Reduced (~0.1 times of 0-twist), but finite  $I_c R_N$

Temperature Dependent Critical Current



Fraunhofer Pattern with in-plane magnetic field



Well developed FP patterns suggest high quality Josephson Junction.

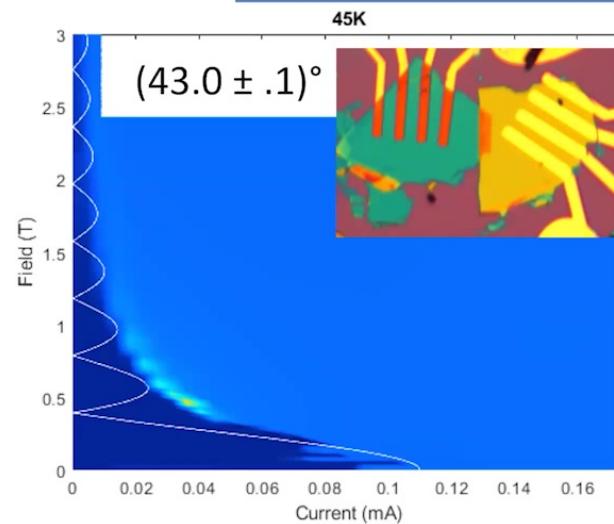
$$\text{Fitting function: } I_C = I_{C0} \left| \frac{\sin\left(\frac{\pi\phi}{\phi_0}\right)}{\frac{\pi\phi}{\phi_0}} \right|$$

$$\phi = B_{\text{wt}}; \quad \phi_0 = 2.0678 \times 10^{-15} \text{ T m}^2$$

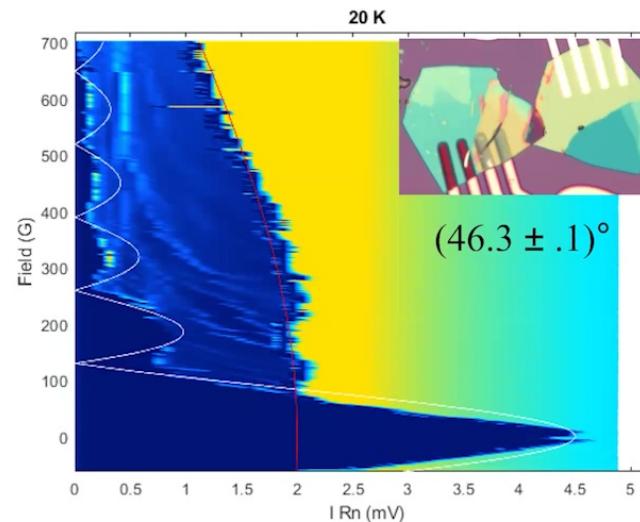
Width: 11 μm (measured)

Fitting Parameters: Thickness: 27 nm

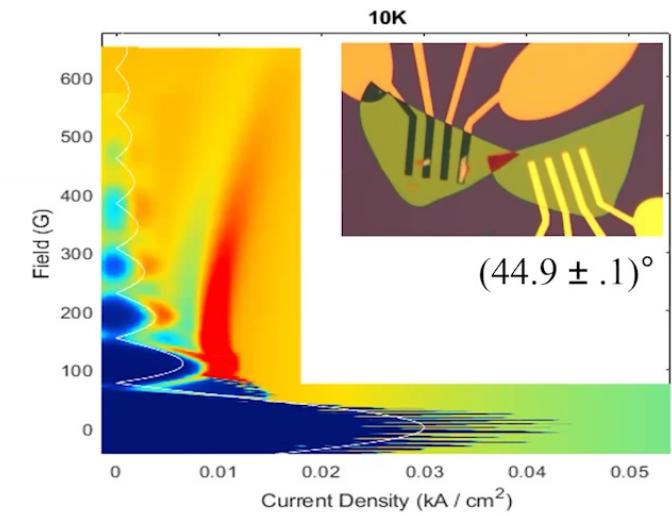
# Fraunhofer Patterns in Twisted BSCCO Josephson Junction



Fitting Parameters: Width:  $3.5 \mu\text{m}$   
Thickness:  $1.5 \text{ nm}$

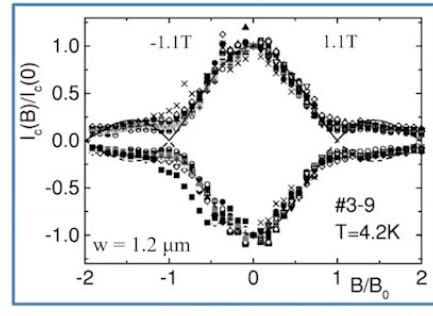


Fitting Parameters: Width:  $11 \mu\text{m}$   
Thickness:  $14.5 / 1.5 \text{ nm}$

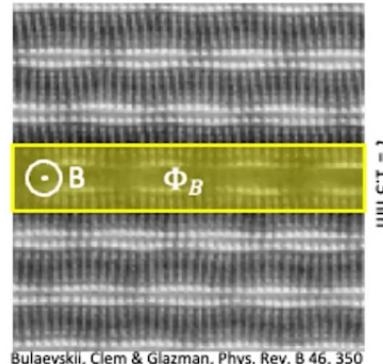


Fitting Parameters: Width:  $10 \mu\text{m}$   
Thickness:  $27 \text{ nm}$

## Intrinsic BSCCO Josephson Junction



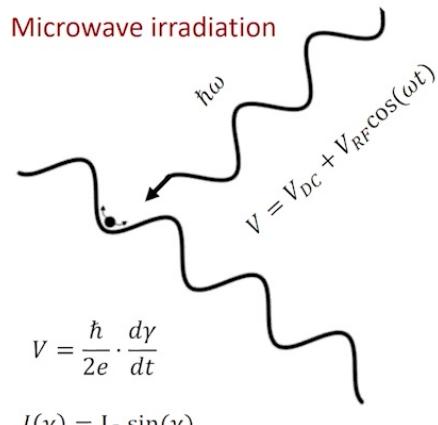
Irie et al, Phys. Rev. B 62 6681



Two different Josephson current contributions

$$\mathcal{F}(\varphi) = \mathcal{F}_0 + 2B_0\psi^2[-\cos(2\theta)\cos\varphi + \mathcal{K}\cos(2\varphi)]$$

# Shapiro Steps Measurement for JJ Current-Phase Relations



$$I(\gamma) = I_C \sin(\gamma)$$

$$I(\gamma) = I_C \sum_n (-1)^n J_n \left( \frac{2eV_{RF}}{\hbar\omega} \right) \sin(\gamma_0 + \frac{2eV_{DC}}{\hbar} t - n\omega_{RF}t)$$

Integer Shapiro steps

$$n = 1, 2, 3, \dots$$

$$V_{DC} = \frac{n \hbar}{2e} \cdot W_{RF}$$

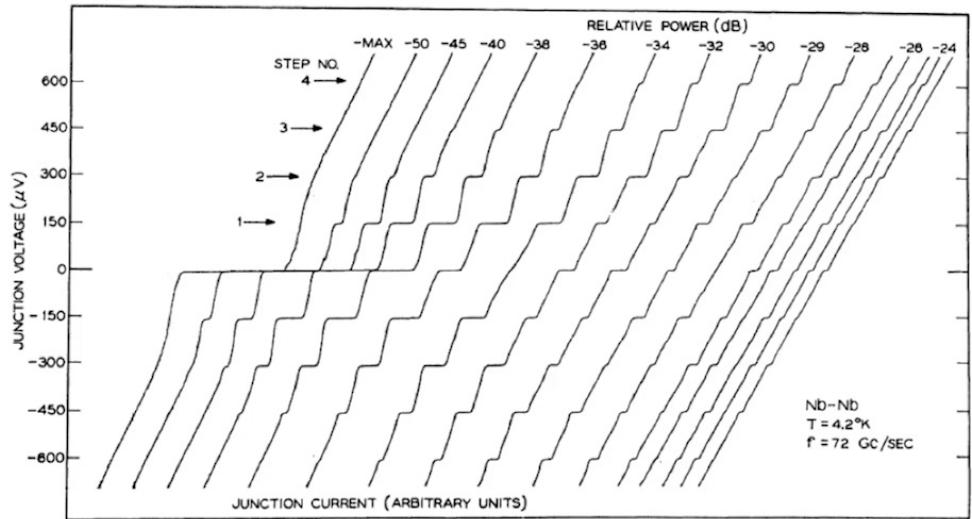
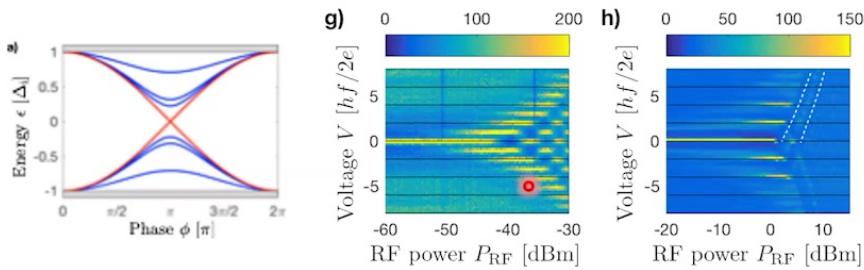


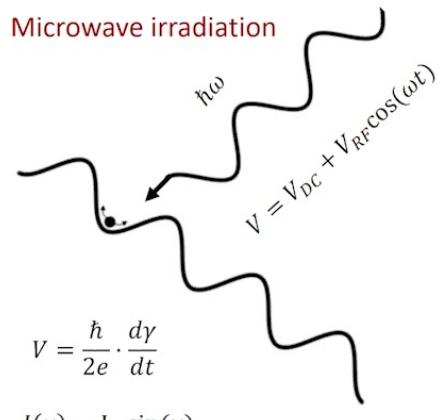
FIG. 1. Voltage-current curves for a Nb-Nb point-contact Josephson junction exposed to a 72-Gc/sec signal at various power levels.  
Grimes and Shapiro Phys. Rev. (1967)

## Fractional Josephson Effect: TI + Superconductors



Bocquillon et al., arXiv:1810.03862

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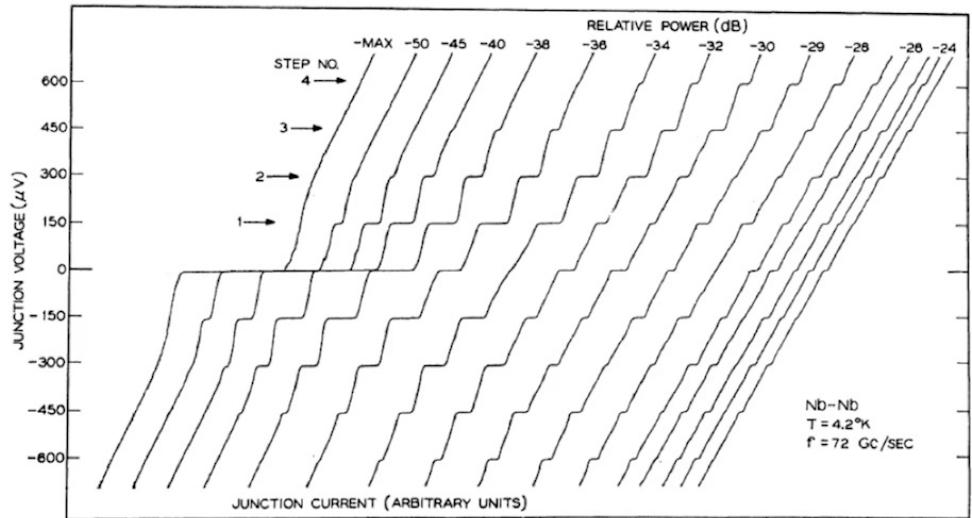
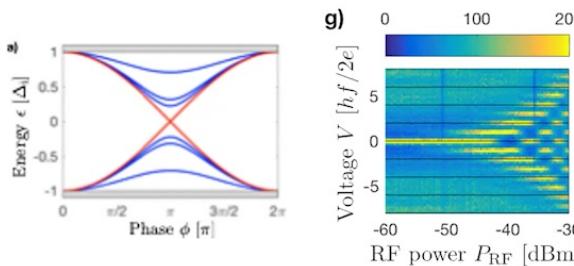


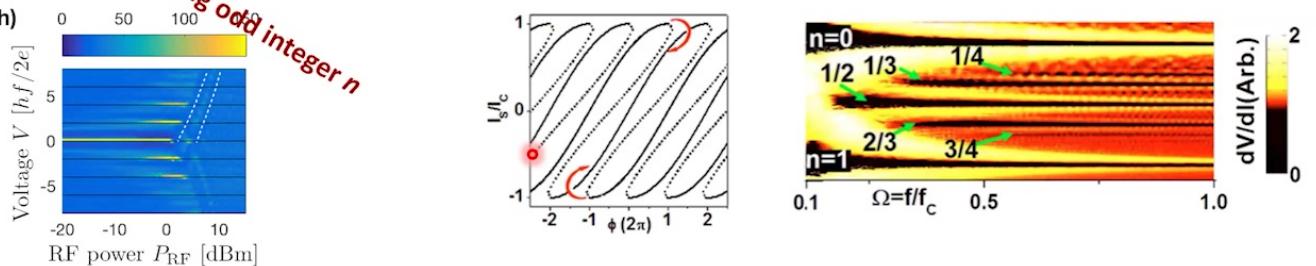
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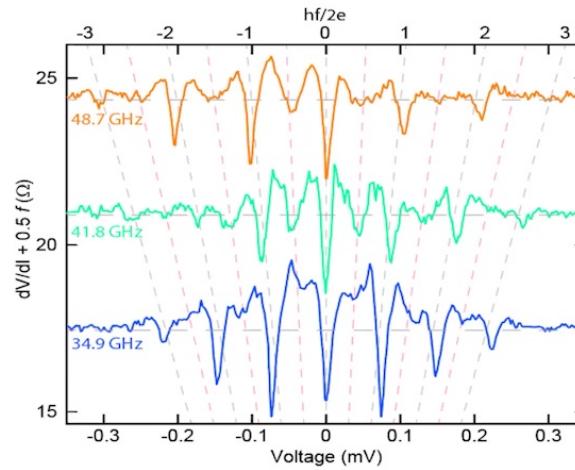
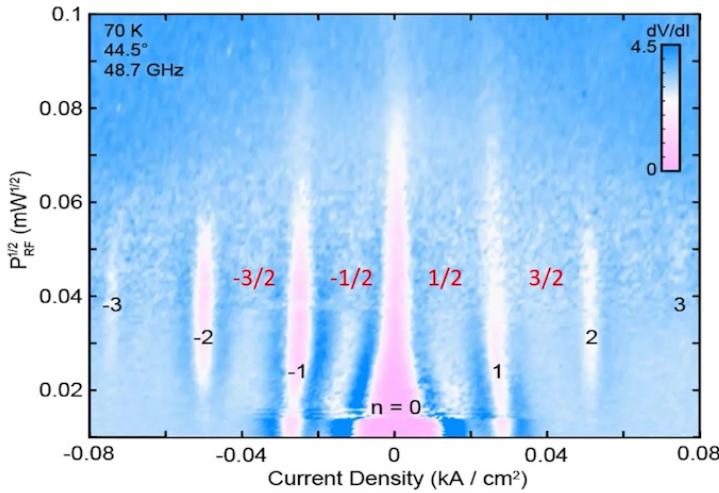
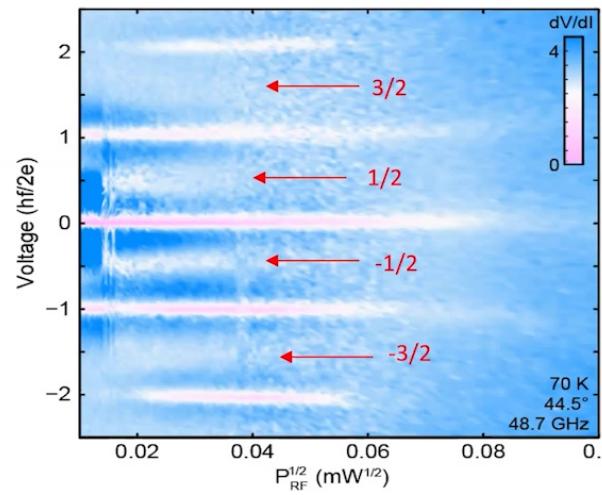
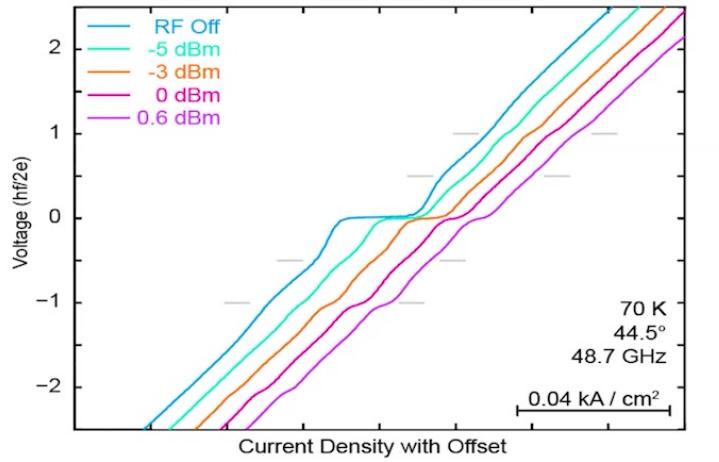
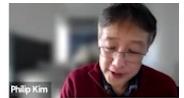
Bocquillon et al., arXiv:1810.03862

## Fractional Shapiro Steps: phase slip CPR in superconducting nanowire

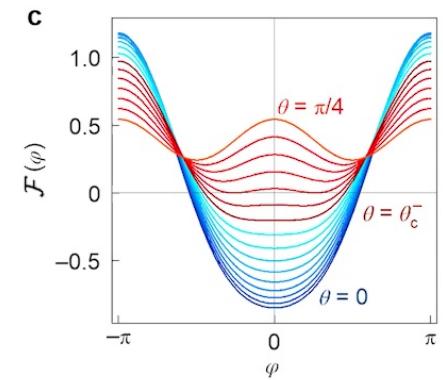


Dinsmore et al., APL 93, 192505 (2008)

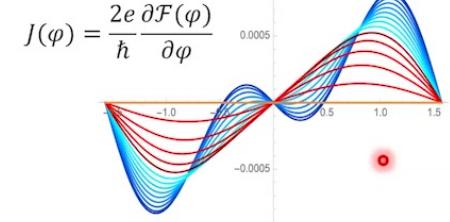
# Fractional Shapiro Steps: Presence of Second Harmonic Mode



Can et al. Nature Phys (2021)  
 $\mathcal{F}(\varphi) = \mathcal{F}_0 + 2B_0\varphi^2[-\cos(2\theta)\cos\varphi + \mathcal{K}\cos(2\varphi)]$



## JJ current phase relation

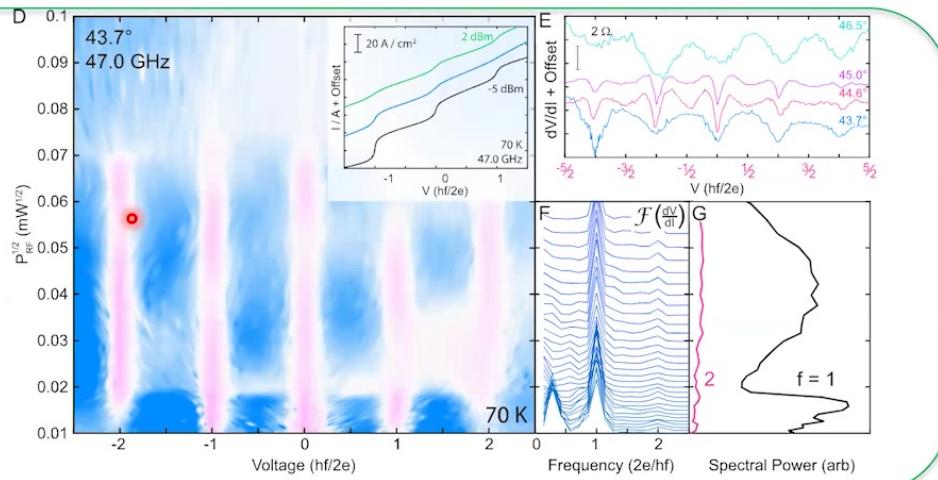


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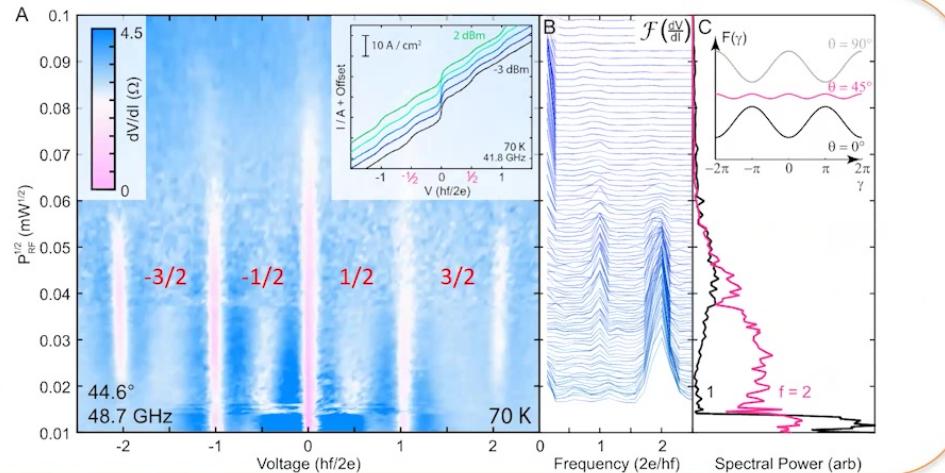
$(43.7 \pm .1)^\circ$

Integer Shapiro steps

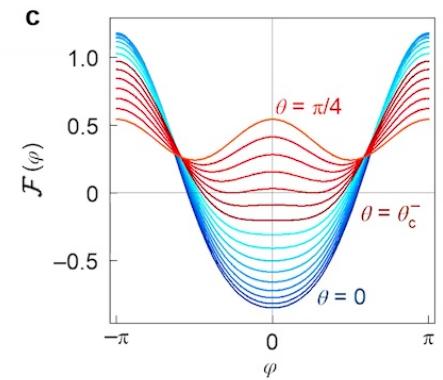


$(44.6 \pm .1)^\circ$

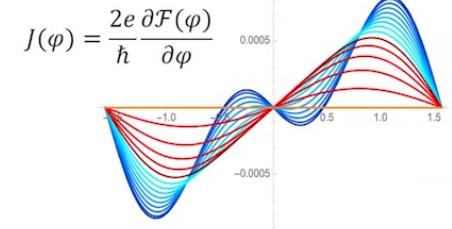
Dominant half Integer Shapiro steps



Can et al. Nature Phys (2021)  
 $\mathcal{F}(\varphi) = \mathcal{F}_0 + 2B_0\varphi^2[-\cos(2\theta)\cos\varphi + \mathcal{K}\cos(2\varphi)]$



JJ current phase relation

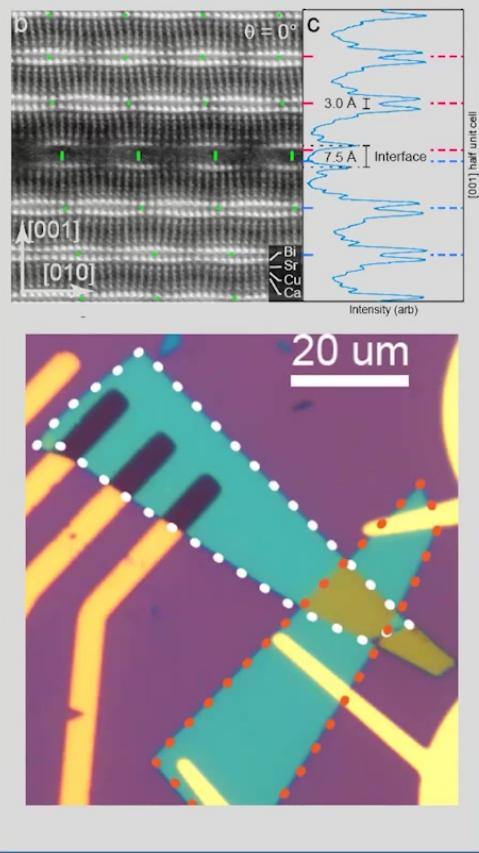


Observed fractional Shapiro steps suggest the presence of the second harmonic term!

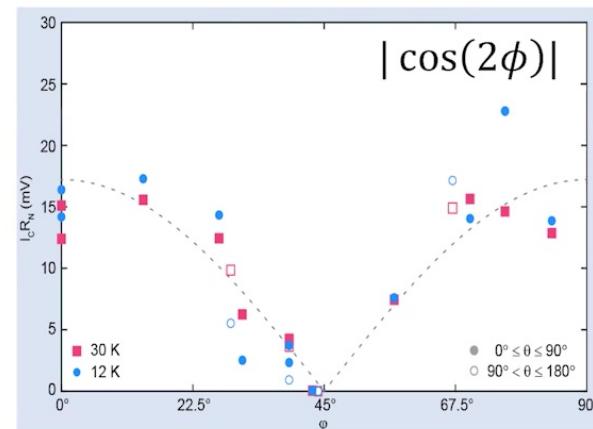
# Summary



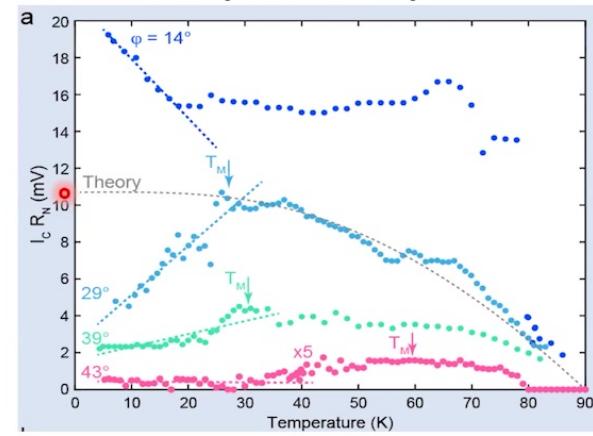
## Twist Josephson Junctions Fabrication



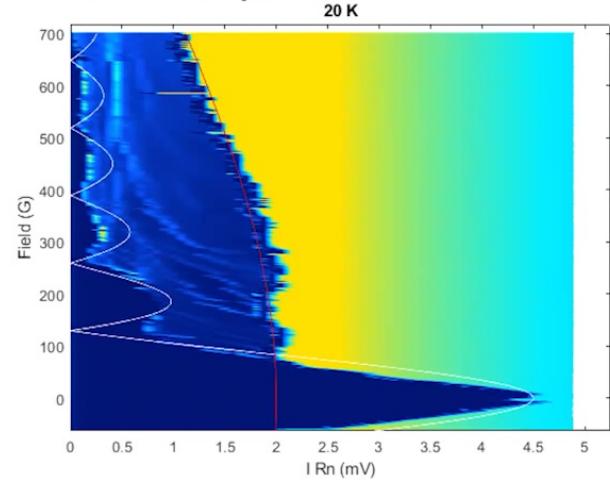
## Twist Angle Dependent Critical Current



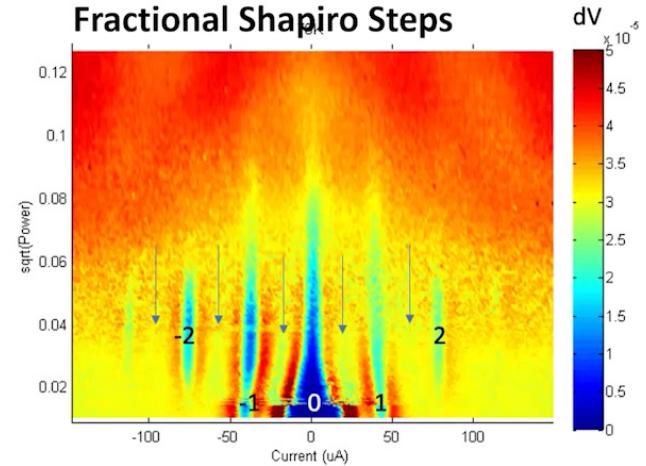
## Unusual temperature dependent $I_c$



## Fraunhofer pattern



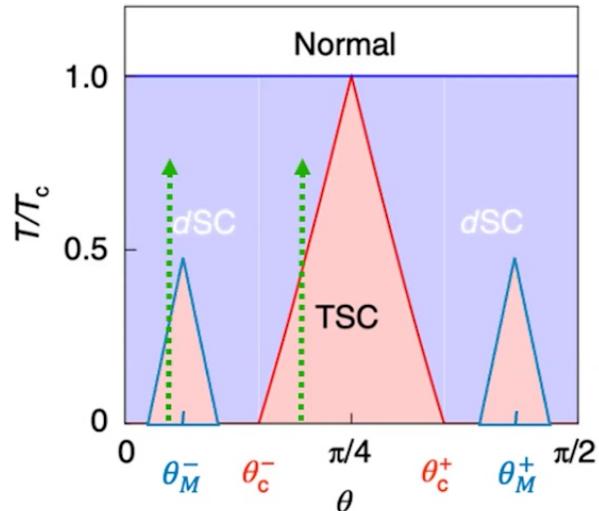
## Fractional Shapiro Steps





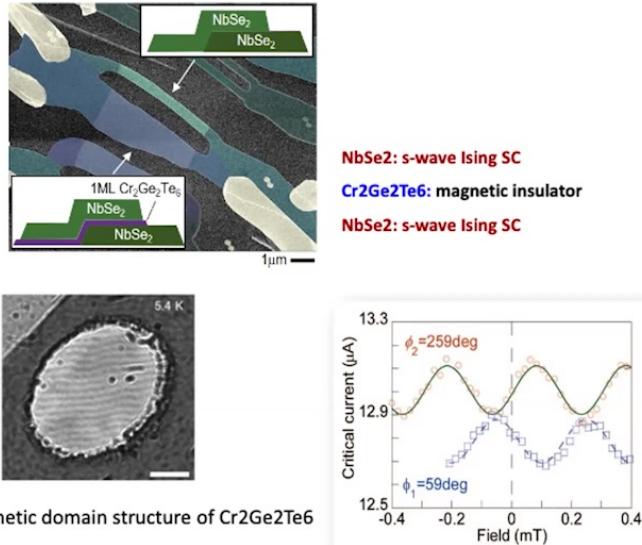
## Outlook

Can we directly probe TSC with broken TRS?



Can et al. Nature Phys (2021); Volkov et al. arXiv: 2012.07860

- Phase sensitive measurement: SQUID

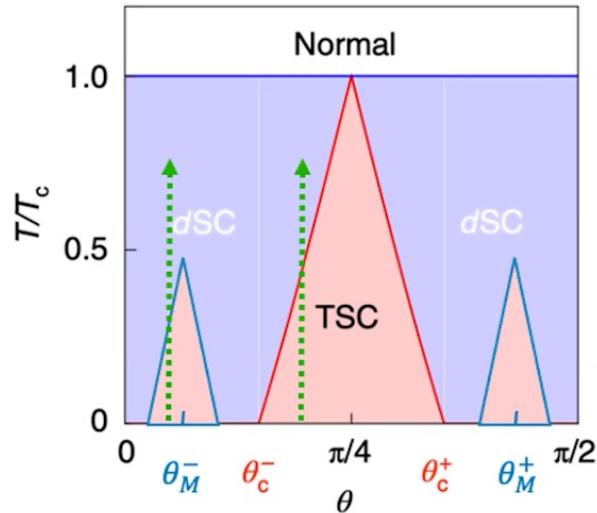


Idzuchi et al., Nature Comm. (2021)



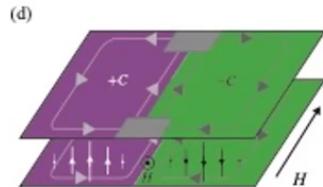
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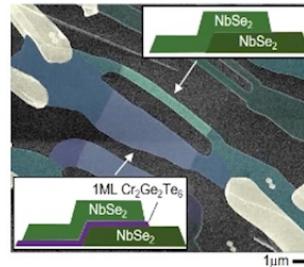


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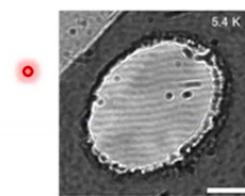
- Edge state measurement: thermal transport



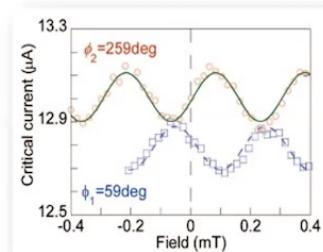
- Phase sensitive measurement: SQUID



**NbSe<sub>2</sub>:** s-wave Ising SC  
**Cr<sub>2</sub>Ge<sub>2</sub>Te<sub>6</sub>:** magnetic insulator  
**NbSe<sub>2</sub>:** s-wave Ising SC



Magnetic domain structure of  $Cr_2Ge_2Te_6$



Idzuchi et al., Nature Comm. (2021)

- Other means of broken TRS measurement: Kerr effect and etc

# Acknowledgment



## Experiment

Frank Zhao, Nicolar Poccia, Xiaomeng Cui, Hyobin Yoo, Joon Young Park, Yuval Ronen, Rebecca Engelke



## Samples

Rudan Zhong, Genda Gu (BNL); Kenji Watanabe, Takashi Taniguchi (NIMS)



## Theory

Pavel Volkov, Jed Pixley (Rutgers); Tarun Tummuru, Stephan Plugge, Marcel Franz (UBC)

