Title: Discriminating between theories of the very early universe

Speakers: Jerome Quintin

Series: Cosmology & Gravitation

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Abstract: There exist various scenarios for the very early universe that could potentially be the explanation for the observed properties of the cosmic microwave background. The current paradigm -- inflationary cosmology -- has rightfully received much attention, but it is not the only theoretically viable explanation. Indeed, several alternative scenarios exist, for example a contracting universe prior to a bounce or a slowly expanding emerging universe. It thus bares the question: how can we discriminate between the various theories, both from a theoretical and an observational point of view? A few pathways to answering this question are discussed in this talk.

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# Discriminating Between Theories of the Very Early Universe

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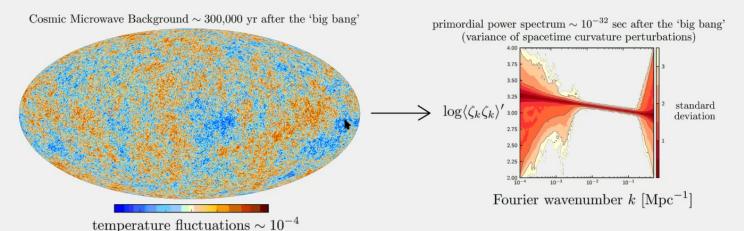


Perimeter Institute for Theoretical Physics Cosmology and Gravitation Seminar November 30th, 2021

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# What we know of the very early universe with certainty

Figures adapted from Planck [arXiv:1502.01582,1807.06211]



$$\langle \zeta_k \zeta_k \rangle' = \underbrace{(2.10 \pm 0.03) \times 10^{-9}}_{A_s = \text{amplitude}} \left( \frac{k}{0.05 \,\text{Mpc}^{-1}} \right)^{-0.0351 \pm 0.0042}$$

- ⇒ Nearly scale-invariant, Gaussian, scalar fluctuations
- ⇒ Currently no (statistically significant) sign of anything else! (e.g., primordial gravitational waves, non-Gaussianities, running of the spectrum, features, etc.)
- ⇒ Incredibly rich and complex, yet very simple!

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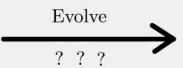
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# How can this be explained?

ASSUME initial conditions: quantum vacuum on small scales



MEASURE 'final conditions':  $\langle \zeta_k \zeta_k \rangle' \sim k^0$  on large scales

linearized Einstein equations  $\Rightarrow$ 

$$\partial_{\tau}^{2}(z\zeta_{k}) + \left(c_{s}^{2}k^{2} - \frac{\partial_{\tau}^{2}z}{z}\right)z\zeta_{k} = 0, \quad z \equiv \frac{a\sqrt{2\epsilon}}{c_{s}}$$

 $\tau = \text{conformal time}$ 

 $a(\tau) = \text{scale factor of the universe}$ 

 $\epsilon(\tau)$  = characterizes the equation of state of the matter content

 $c_{\rm s}(\tau) = \text{sound speed}$ 

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#### How can this be explained?

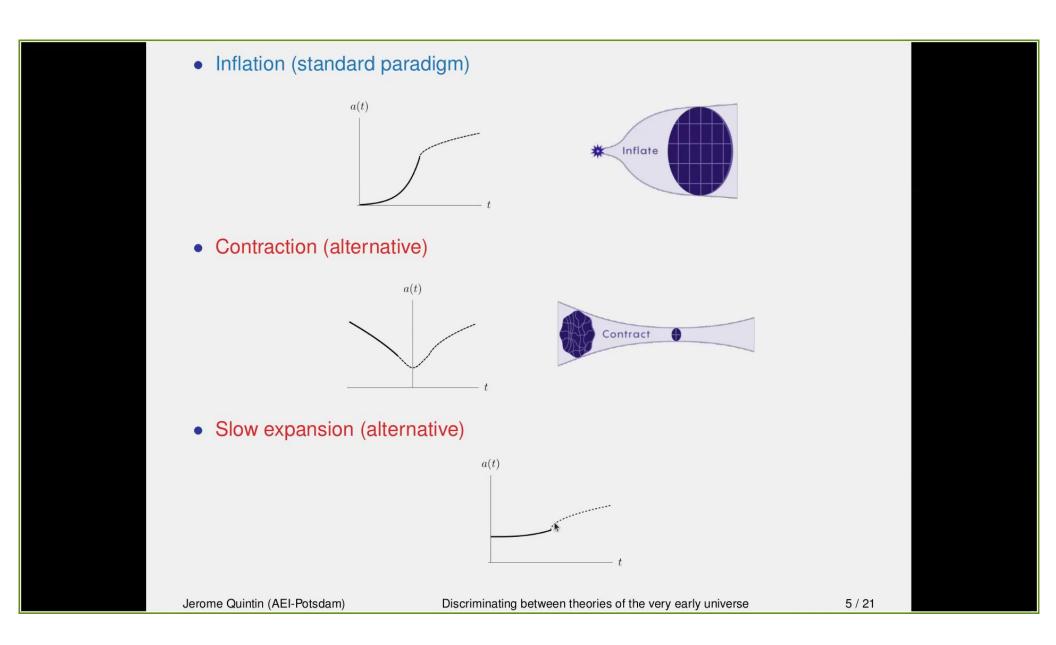
- E.g.,  $c_{\rm s}=1$ ,  $\epsilon\approx {\rm const.}$ ,  $a(\tau)\sim |\tau|^{1/(\epsilon-1)} \Rightarrow \partial_{\tau}^2 z/z=\frac{2-\epsilon}{(\epsilon-1)^2\tau^2}$ Approximate scale invariance is found for  $\partial_{\tau}^2 z/z\approx 2/\tau^2$ 
  - $\Rightarrow$  Inflation:  $\epsilon \ll 1$  (negative pressure, approx. vacuum EoS)
  - $\Rightarrow$  Fast contraction:  $\epsilon \approx 3/2$  (pressureless matter) wands [gr-qc/9809062]
- Time-dependent  $\epsilon$  or  $c_{\rm s}$  or additional fields open up many more possibilities e.g., Hinterbichler & Khoury [1106.1428], Geshnizjani *et al.* [1107.1241] E.g.:
  - Slow contraction (a.k.a. ekpyrosis):  $\epsilon > 3$  (ultra-stiff EoS) e.g., Lehners *et al.* [hep-th/0702153]
  - Slow expansion (a.k.a. genesis):  $\epsilon < 0$  (ghost-like EoS) e.g., Creminelli *et al.* [1007.0027]
- Can all be made consistent with the measured  $\langle \zeta_k \zeta_k \rangle'$
- More scenarios are also possible (e.g., 'beyond semi-classical GR'), but let's keep it simple for today

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## Can we realistically tell them apart?

With the running of the spectral index  $\alpha_s$ , non-Gaussianities ( $f_{NL}$ ,  $g_{NL}$ , ...), tensor-to-scalar ratio r, tensor tilt  $n_t$ , etc.?

Surely. But one can often find models that lead to closely degenerate predictions.

#### Example:

#### single-field slow-roll inflation

$$n_{\rm s} \approx 0.97 \,, \ \alpha_{\rm s} \approx -5 \times 10^{-4}$$
 
$$f_{\rm NL}^{\rm local} \approx 0.01$$
 
$$r \approx 0.01 \,, \ n_{\rm t} \approx -0.001$$

#### two-field ekpyrosis (slow contraction)

$$n_{\rm s} \approx 0.97$$
,  $\log_{10}(-\alpha_{\rm s}) \lesssim -2$ 

$$f_{\rm NL}^{\rm local} \approx \frac{3}{2} \kappa_3 \sqrt{\epsilon} + 5 \qquad (\in [-5, 5])$$
  
 $r \lesssim 0.06, \ n_{\rm t} \gtrsim 0.12$ 

Ijjas et al. [1404.1265], Lehners & Wilson-Ewing [1507.08112],

Fertig et al. [1607.05663],

Ben-Dayan+ [1604.07899,1812.06970]  $\rightarrow$  sourced perturbations

from gauge field production

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So are there ways of **discriminating** between those theories, in a **model-independent** way, both **theoretically and observationally**?

We need to invent new approaches!

Let me propose a few avenues in that direction for the rest of this talk:

- (1) Primordial quantum circuit complexity
- (2) Primordial quantum transition amplitudes
- (3) Primordial standard clocks

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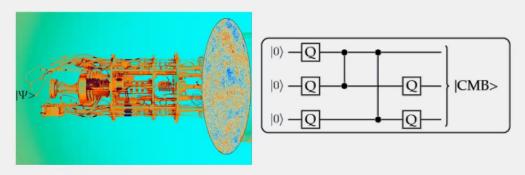
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## (1) Primordial quantum complexity

• How **complex** are the various scenarios? If we did a quantum simulation of the early universe, **how many quantum gates** would it require?



$$|\Psi_{\mathrm{Ref}}\rangle \xrightarrow{|\Psi_{\mathrm{Target}}\rangle = \hat{U}|\Psi_{\mathrm{Ref}}\rangle} |\Psi_{\mathrm{Target}}\rangle$$

- How many elementary quantum gates to construct  $\hat{U}$ ?  $\Longrightarrow$  complexity
- The general idea is that a circuit can have a continuous differential-geometry description
  - $\Rightarrow$  optimal quantum simulation  $\equiv$  smallest number of gates  $\equiv$  geodesic in the geometry of quantum gates

Nielsen [quant-ph/0502070], Jefferson & Myers [1707.08570], Camargo et al. [1807.07075], Chapman et al. [1810.05151], Bhattacharyya+ [1810.02734,2001.08664,2005.10854], Lehners & JQ [2012.04911]

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• Start with a Reference and a Target state, both Gaussian and with respective frequencies  $\omega$  and  $\Omega$  (1-d harmonic oscillators with 'position'  $\zeta$ ):

$$|\Psi_{\rm R}\rangle = \left(\frac{\omega}{\pi}\right)^{1/4} e^{-\frac{1}{2}\omega\zeta^2}, \quad |\Psi_{\rm T}\rangle = \left(\frac{\Omega}{\pi}\right)^{1/4} e^{-\frac{1}{2}\Omega\zeta^2}$$

• Example of gate that could constitute the unitary evolution ( $\hat{\Pi}=-i\hat{\partial}_{\zeta}$ ):

$$\hat{Q} \equiv e^{\frac{\epsilon}{2}} e^{i\epsilon \hat{\zeta}\hat{\Pi}}, \qquad \hat{Q}|\Psi(\zeta)\rangle = e^{\frac{\epsilon}{2}}|\Psi(e^{\epsilon}\zeta)\rangle$$

- Then  $\hat{U}=\hat{Q}^{lpha}$  yields  $|\Psi_{\rm T}\rangle=\hat{U}|\Psi_{\rm R}\rangle$  as long as  $2\epsilonlpha=\ln(\Omega/\omega)$
- Therefore, the # of gates (the complexity) goes as

$$C = \epsilon \alpha = \frac{1}{2} \ln \left( \frac{\Omega}{\omega} \right) \xrightarrow{\omega, \Omega \in \mathbb{C}} \frac{1}{2} \left| \ln \left( \frac{\Omega}{\omega} \right) \right|$$

• In cosmology,  $|\Psi_{\rm R}\rangle$  is the Bunch-Davies vacuum, and the late-time correlator is Lehners & JQ [2012.04911]

$$\Omega = z^2 \left( -i \frac{\partial_{\tau} (z\zeta)^*}{(z\zeta)^*} + i \frac{\partial_{\tau} z}{z} \right)$$

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## Quantum circuit complexity

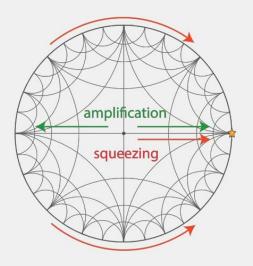
A convenient geometry is the hyperbolic one [it naturally arises when representing the Gaussian wavefunctions as covariance matrices, where elementary gates are elements of  $\mathrm{Sp}(2,\mathbb{R})$ ] Camargo *et al.* [1807.07075]

Poincaré half-plane:

$$(x_0, y_0) = (0, 1) \longrightarrow (x, y) = \left(-\frac{\operatorname{Im}\Omega}{\sqrt{2}\operatorname{Re}\Omega}, \frac{\omega}{\operatorname{Re}\Omega}\right)$$

Poincaré disk:

$$z = x + iy \longrightarrow \frac{z - i}{z + i}$$



Lehners & JQ [2012.04911]

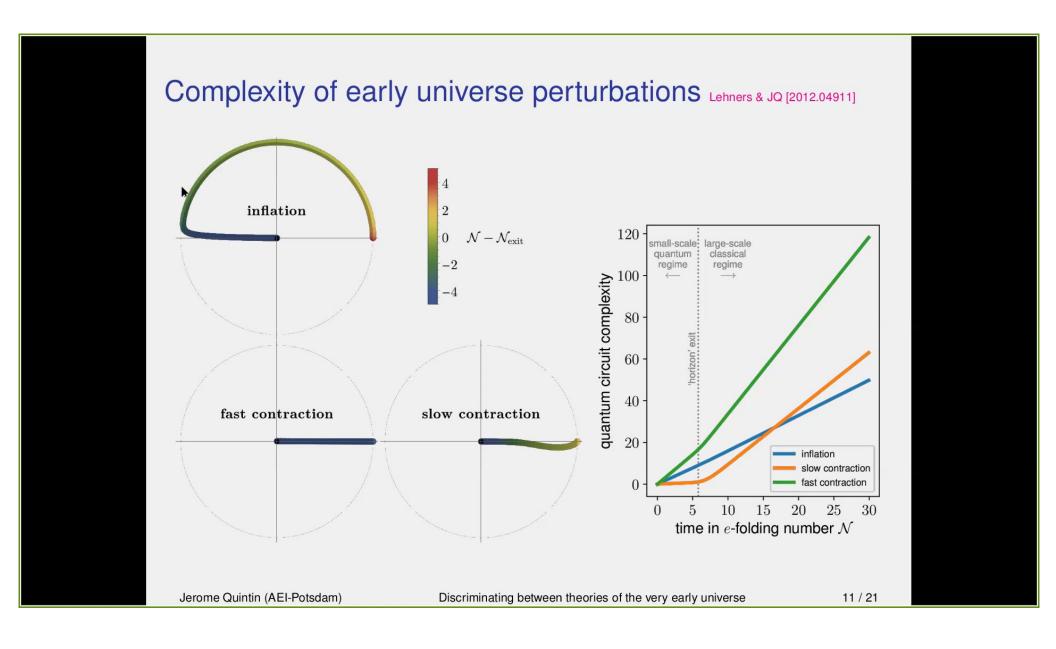
- ▶ amplification  $\leftrightarrow 1/\text{Re}\,\Omega \to \infty \iff$  growth of  $\langle \zeta_k \zeta_k \rangle'$
- **squeezing**  $\leftrightarrow |\operatorname{Im} \Omega/\operatorname{Re} \Omega| \to \infty \leftrightarrow \operatorname{classicalization}$  in the WKB sense
- ▶ complexity ↔ hyperbolic distance from the origin

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#### Complexity of early universe perturbations Lehners & JQ [2012.04911]

#### Super-horizon:

inflation 
$$(\epsilon < 1)$$
:  $\Delta C \simeq \sqrt{2} \underbrace{(1 + 2\epsilon)}_{\approx 1} \Delta \mathcal{N}_{\epsilon}$   
slow contraction  $(\epsilon > 3)$ :  $\Delta C \simeq 2\sqrt{2} \underbrace{\left(\frac{\epsilon - 3/2}{\epsilon - 1}\right)}_{\approx 1} \Delta \mathcal{N}$   
fast contraction  $(\epsilon \approx 3/2)$ :  $\Delta C \simeq 3\sqrt{2} \Delta \mathcal{N}$ 

- ⇒ inflation acts as a 'simple' quantum computer compared to its alternatives
- ⇒ very modest dependence on specific model realizations
- √ Good way to differentiate theories, theoretically speaking
- How can it be used to discriminate? Interpretation of chaos? Sensitivity to initial conditions?

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#### (2) Primordial quantum amplitudes Jonas, Lehners & JQ [2012.04911]

$$\mathcal{A}(\Phi_{i} \to \Phi_{f}) = \int_{\Phi_{i}}^{\Phi_{f}} \mathcal{D}\Phi \, e^{\frac{i}{\hbar}S[\Phi]} \stackrel{\hbar \leq 1}{\approx} \sum_{\text{saddles}} \mathcal{N}e^{\frac{i}{\hbar}S_{\text{on-shell}}[\Phi_{i} \to \Phi_{f}]}$$
$$\Phi = \{g_{\alpha\beta}, \phi, A_{\mu}, \ldots\}$$

→ this only yields a well-defined (and non-zero) amplitude if the relevant saddle points have finite classical on-shell action

$$S_{\text{on-shell}}[\Phi_{\rm i} \to \Phi_{\rm f}] < \infty$$

(Off-shell contributions are expected to blow up, but this is completely fine quantum mechanically)

 $\rightarrow$  E.g., in cosmology,

$$S_{\text{on-shell}} \sim \int_{t(\Phi_{\rm i})}^{t(\Phi_{\rm f})} dt \, a\dot{a}^{2} \stackrel{a \sim |t|^{1/\epsilon}}{\sim} \begin{cases} t^{\frac{3-\epsilon}{\epsilon}} \Big|_{0}^{t(\Phi_{\rm f})} & \text{inflation with } \epsilon \ll 1\\ (-t)^{\frac{3-\epsilon}{\epsilon}} \Big|_{-\infty}^{t(\Phi_{\rm f})} & \text{contraction with } \epsilon > 1 \end{cases}$$

 $\rightarrow$  Inflation appears to be fine, but contraction converges only if  $\epsilon > 3$  (only slow contraction!)

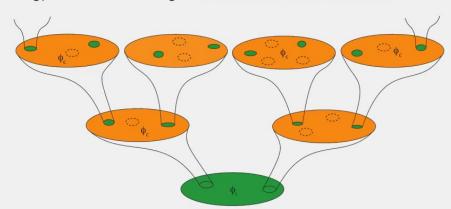
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# But the story is not that simple for inflation

- If inflation really goes all the way back to the big bang singularity (a=0), instabilities in the perturbations arise (interference among different saddle points)  $\Rightarrow$  unviable Di Tucci, Feldbrugge, Lehners & Turok [1906.09007]
- If inflation is eternal (potential is so flat that field stochastically jumps up the potential and keeps inflating), action is divergent Jonas, Lehners & JQ [2102.05550]



$$S \sim \int_0^\infty \mathrm{d}t \, a^3 \, V(\phi) \, \underbrace{\text{Prob}[\phi \text{ is inflating at time } t]}_{\text{sol, to Fokker-Planck equation}} \to \infty \quad \text{if } \frac{|V_{,\phi}|}{V^{3/2}} < \frac{1}{\sqrt{2} \pi}$$

→ Reminiscent of swampland criteria

e.g., Rudelius [1905.05198], Hamada, Montero, Vafa & Valenzuela [2111.00015]

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# Quadratic gravity (and beyond)

• Quadratic gravity is renormalizable Stelle [PRD 1977]

$$S_{\text{quad}} = \int d^4 x \sqrt{-g} \left( \frac{M_{\text{Pl}}^2}{2} R + \frac{\omega}{3\sigma} R^2 - \frac{1}{2\sigma} C_{\mu\nu\rho\sigma}^2 \right)$$

ightarrow FLRW solutions  $a(t)\sim t^s$  as  $t\to 0^+$  lead to finite amplitudes only if s>1  $\Rightarrow$  accelerating out of the big bang

Lehners & Stelle [1909.01169], Jonas, Lehners & JQ [2102.05550]

- → In Bianchi I, only 'bounded anisotropy' solutions satisfy the principle e.g., constant-Hubble and constant-shear solution Barrow & Hervik [gr-qc/0610013]
- For some generic higher-curvature theory (up to  $Riem^n$ ):

$$S_{\mathrm{Riem}^n} = \int \mathrm{d}^4 x \sqrt{-g} f(R^{\mu}{}_{\nu\rho\sigma})$$

- $\rightarrow a(t) \sim t^s$  solutions need to have s > (2n-3)/3
- $\Rightarrow$  If there are infinitely many  $(n = \infty)$ , as potentially required, no such solutions respect the principle
- A finite cosmological amplitude principle is a good theoretical discriminator (but more model dependent)

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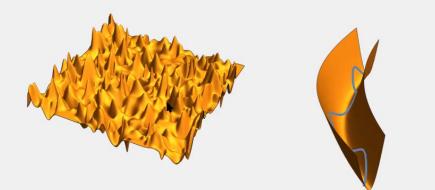
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# (3) Primordial standard clocks

 One generally expects a wealth of heavy spectator fields in the early universe



- These oscillating heavy fields are expected to leave oscillatory signals in the observations
- And the frequency dependence is expected to mainly depend on the background evolution Chen+ [1104.1323,1106.1635,1404.1536,1411.2349,1601.06228,1608.01299]

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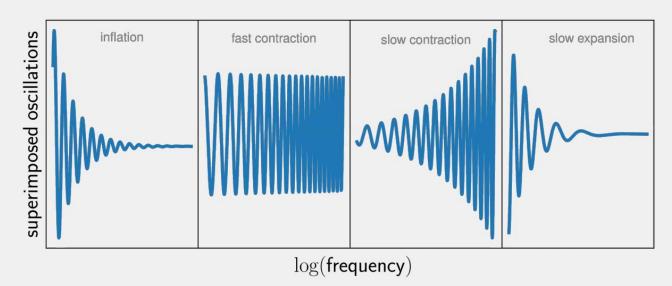
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#### Standard clocks

$$a(t) \sim |t|^{1/\epsilon} \longrightarrow \frac{\Delta \langle \zeta_k \zeta_k \rangle'}{\langle \zeta_k \zeta_k \rangle'_{\text{no oscil.}}} \sim k^{(\epsilon - 3)/2} \sin \left( \frac{m/H_{\star}}{\epsilon (1 - \epsilon)} k^{\epsilon} + \text{phase} \right)$$



ightarrow Oscillations superimposed on top of the nearly scale-invariant power spectrum could tell us about  $\epsilon$  and hence a(t) in the very early universe!

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→ Expected signals in other windows as well (3-pt function, GWs, etc.)
→ Potentially observable with next generation of telescopes!
Chen+ [1605.09364,1605.09365,1610.06559,2106.07546]

→ Explicit particle physics models have been constructed for inflation and the corresponding signals are currently extensively studied

Chen, Namjoo & Wang [1411.2349], Braglia *et al.* [2106.07546,2108.10110] and not to mention the cosmological collider program (Arkani-Hamed & Maldacena [1503.08043], Lee, Baumann & Pimentel [1607.03735], Chen, Wang & Xianyu [1610.06597], etc.)

→ Barely any exploration of the alternatives

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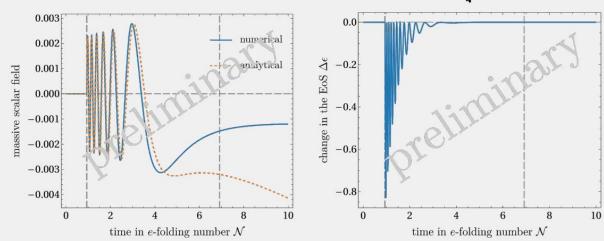
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#### First classical standard clock model in slow contraction

With Xingang Chen and Reza Ebadi

$$\mathcal{L} = \frac{R}{2} - \frac{1}{2} \mathcal{G}^{IJ}(\Phi_K) \partial_{\mu} \Phi_I \partial^{\mu} \Phi_J - V(\Phi_K) , \quad \Phi_K = (\phi, \chi, \sigma)$$

$$\ddot{\sigma} + 3H\dot{\sigma} + m^2\sigma = 0 \Rightarrow \sigma(t) \sim (-t)^{-3/(2\epsilon)}\sin(mt + \text{phase})$$



$$\mathcal{L} \supset \sigma(\partial \chi)^2 \longrightarrow \mathcal{H}_{\mathrm{int}}^{(2)} \sim -a^3 \sigma \left(\dot{\zeta}^2 - \frac{(\partial_i \zeta)^2}{a^2}\right) \implies \frac{\Delta \langle \zeta_k \zeta_k \rangle'}{\langle \zeta_k \zeta_k \rangle'_{\mathrm{no oscil.}}}$$

ightarrow Exact signals currently under investigation, so stay tuned!

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#### Conclusions and future directions

- Very different realizations of the very early universe can degenerately predict the same simple nearly scale-invariant primordial spectrum
- We need new ways of discriminating between theories, in the most model-independent way:
  - → quantum circuit complexity:
    - √ nice description of the quantum-to-classical transition
    - √ very modest model dependence
    - applicability?
  - → finite quantum cosmological amplitudes:
    - √ strong theoretical constraint on allowed models
    - more model dependent
  - → standard clocks (heavy spectator fields):
    - √ strong potential observational constraints on allowed models
    - √ quite model independent
    - a lot more work to be done on the alternatives

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#### Thank you for your attention!

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