

Title: An experiment to test the discreteness of time

Speakers: Pierre Martin-Dussaud

Series: Quantum Gravity

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URL: <https://pirsa.org/21110009>

Abstract: Time at the Planck scale is an unexplored physical regime. It is widely believed that probing Planck time will remain for long an impossible task. Yet, we propose an experiment to test the discreteness of time at the Planck scale and show that it is not far removed from current technological capabilities.



An experiment to test the discreteness of time

QG seminar
Perimeter Institute

Pierre Martin-Dussaud
from Langolen (France)
WWI Armistice Day 2021

[arXiv: 2007.08431](https://arxiv.org/abs/2007.08431)

in collaboration with Marios Christodoulou and Andrea Di Biagio

QISS

THE QUANTUM INFORMATION
STRUCTURE OF SPACETIME

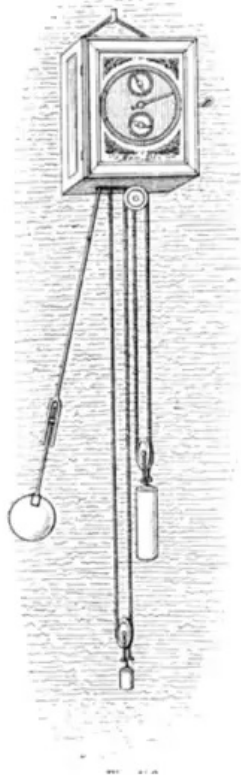


PennState

BRCP

Measuring Time

Good clock: stable periodic motion



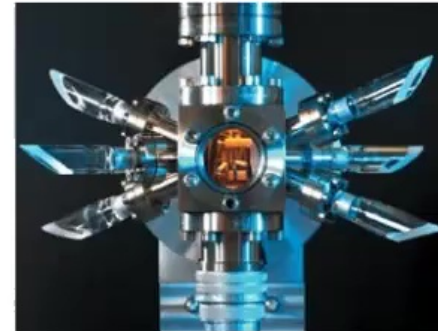
1656: Pendulum clock
(by Huygens)

1 s



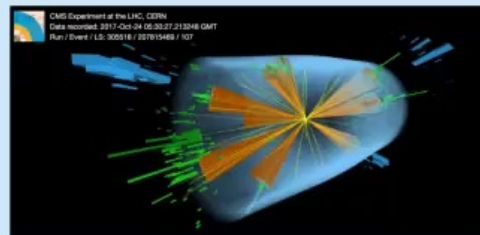
1927: Quartz clock

10^{-4} s



2018: Optical clock
(with Strontium)

10^{-15} s



Top quark lifetime

10^{-25} s

Planck Time

Can we probe it?

$$t_P \stackrel{\text{def}}{=} \sqrt{\frac{\hbar G}{c^5}} \approx 10^{-44} \text{ s.}$$

Probing quantum gravity regime?

High-energy physics: astronomical size accelerator?

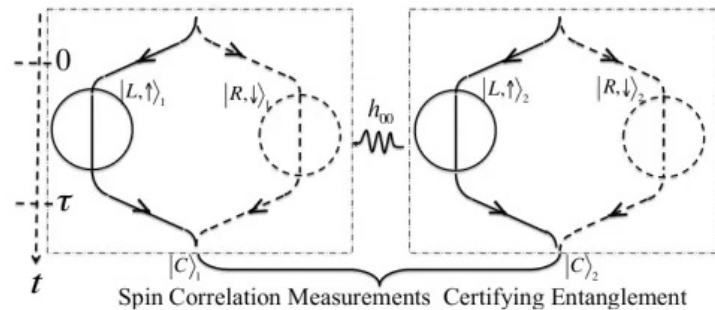
Low-energy experiment: gravity-mediated entanglement

Bose et al. 1707.06050

Marletto & Vedral 1707.06036

$$m_P \stackrel{\text{def}}{=} \sqrt{\frac{\hbar c}{G}} \approx 2 \times 10^{-8} \text{ kg.}$$

1. Two particles, each sent through a Stern-Gerlach
2. They interact only through the gravitational field.
3. Entanglement is created only if gravity is non-classical.



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Experimental setup

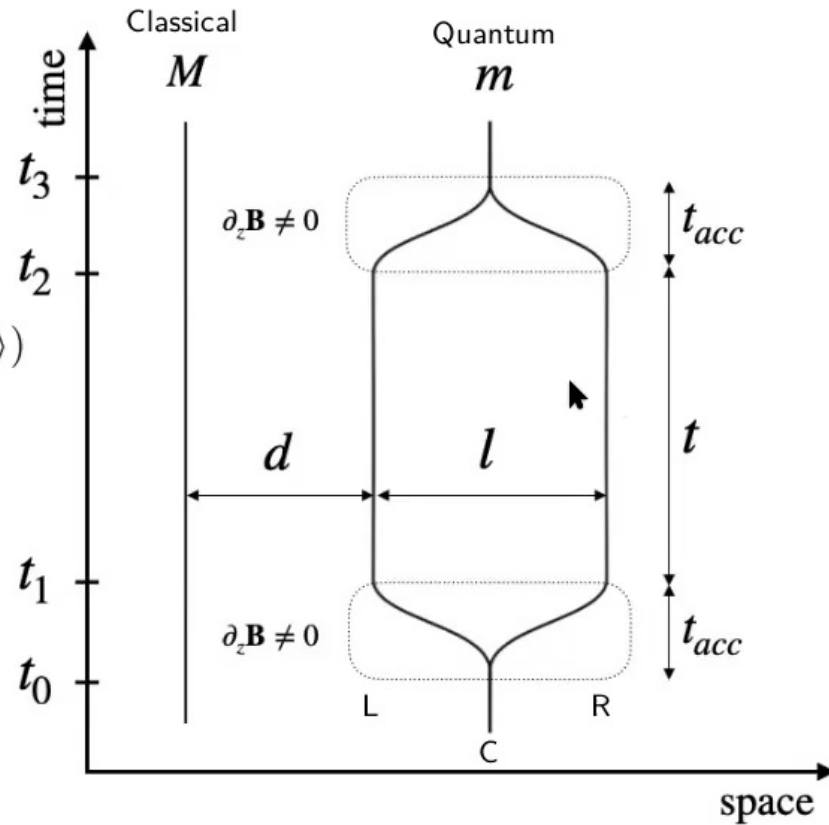
$$\delta\phi = \frac{GMmt}{\hbar} \frac{l}{d(d+l)}$$

$$|\psi_3\rangle = \frac{1}{\sqrt{2}} |C\rangle (|\uparrow\rangle + e^{i\delta\phi} |\downarrow\rangle)$$

$$|\psi_2\rangle = \frac{1}{\sqrt{2}} (e^{i\phi_L} |L \uparrow\rangle + e^{i\phi_R} |R \downarrow\rangle)$$

$$|\psi_1\rangle = \frac{1}{\sqrt{2}} (|L \uparrow\rangle + |R \downarrow\rangle)$$

$$|\psi_0\rangle = \frac{1}{\sqrt{2}} |C\rangle (|\uparrow\rangle + |\downarrow\rangle)$$



Hypothesis & Strategy

$$|\psi_3\rangle = \frac{1}{\sqrt{2}} |C\rangle (|\uparrow\rangle + e^{i\delta\phi} |\downarrow\rangle)$$

Measure in the diagonal basis $|\pm i\rangle \stackrel{\text{def}}{=} \frac{1}{\sqrt{2}} (|\uparrow\rangle \pm i |\downarrow\rangle)$

$$P_+ = \frac{1}{2} + \frac{1}{2} \sin(\delta\phi) = \frac{1}{2} + \frac{1}{2} \sin\left(\frac{m}{m_P} \frac{t}{\beta}\right)$$

$$\delta\phi = m \delta\tau$$

$$\delta\tau = \frac{t}{\beta} t_P$$

$$\beta \stackrel{\text{def}}{=} \frac{d(d+l)c^2}{GMl} t_P$$

Difference of proper time between the two branches

Christodoulou & Rovelli 1808.05842

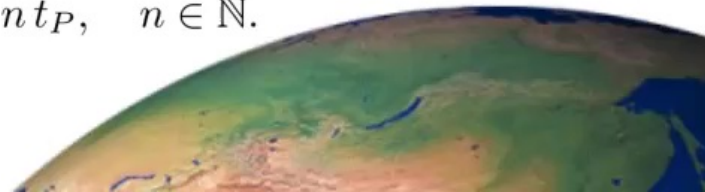
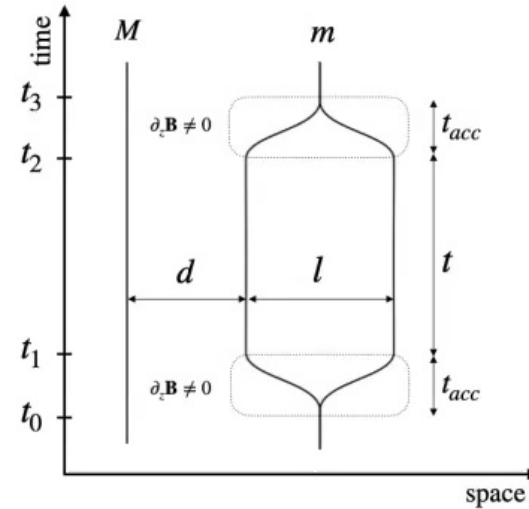
Colella et al. 1975

Hypothesis:

Time is flowing step by step.

Planck time is the fundamental period.

$$\delta\tau = n t_P, \quad n \in \mathbb{N}.$$



Hypothesis & Strategy

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Difference of proper time between the two branches

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$$\delta\tau = \left\lceil \frac{t}{\beta} \right\rceil t_P$$

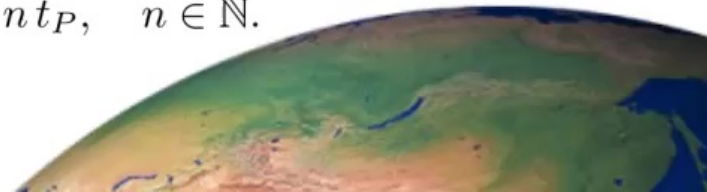
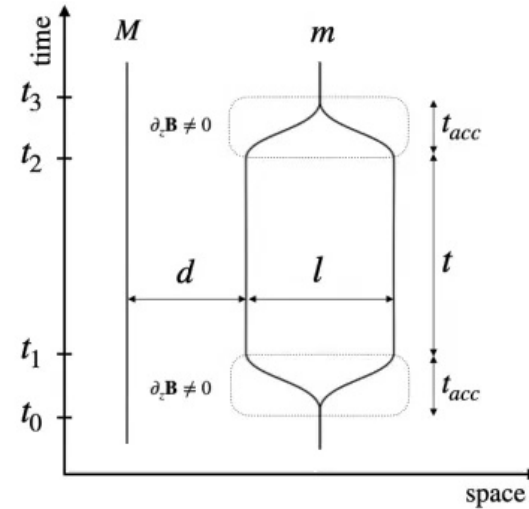
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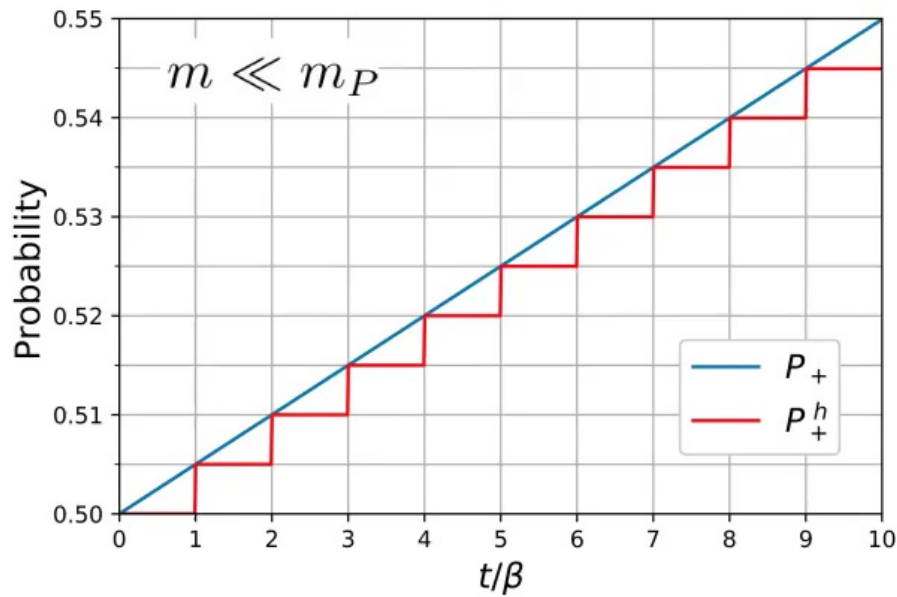
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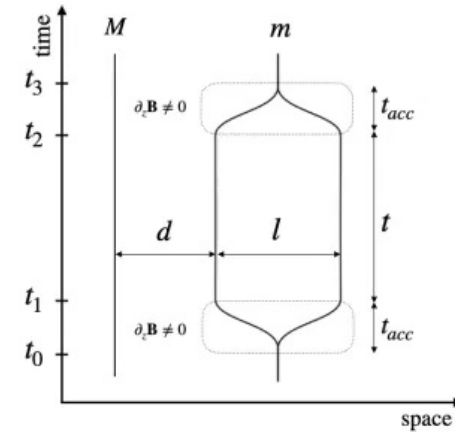
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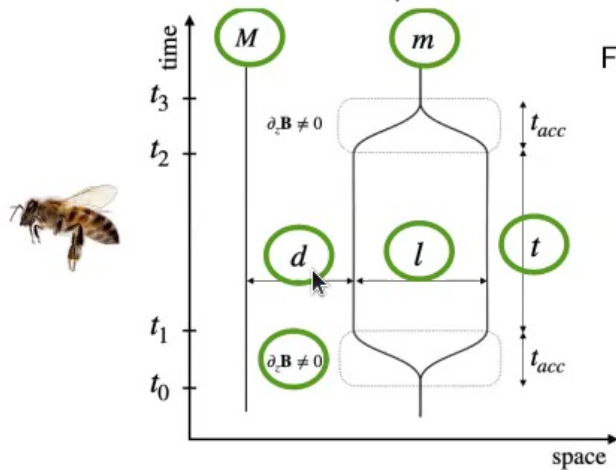
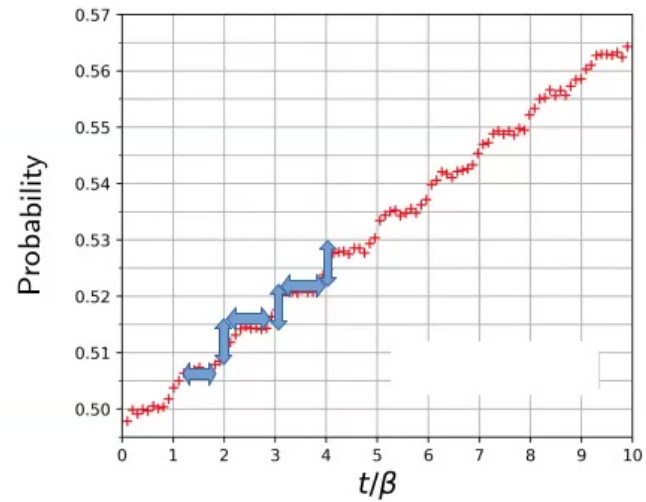
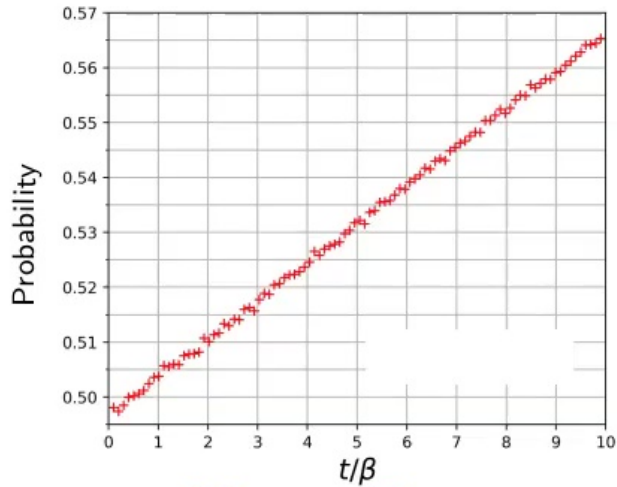
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$$\beta \stackrel{\text{def}}{=} \frac{d(d+l)c^2}{GMl} t_P$$



The blur of experiments



Find a range of parameters compatible with the constraints:

- visibility on the vertical axis
- total time of the experiment
- visibility on the horizontal axis
- gravitational noise
- decoherence

$$\left\{ \begin{array}{l} 10^2 \frac{N_{dp} t}{T_{tot}} < \left(\frac{m}{m_P} \right)^2 \\ U \frac{t}{\beta} < 10^{-1} \\ Alt < 5 \times 10^{-2} \frac{t_P m_P}{l_P} \end{array} \right. \quad 31$$

Intuitive understanding

for why it is possible

A set of viable parameters?

Parameter	Value
m	3×10^{-10} kg
M	3×10^{-9} kg
t	10^{-1} s
l	10^{-7} m
d	[17, 54] cm

$\sim 10^{-2} m_p$. In GME experiment: $\sim 10^{-6} m_p$

N_{dp} 100

N 10^6

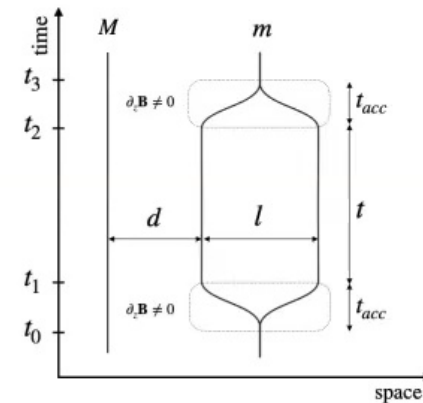
T_{tot} 1 year

n [0, 10]

Pressure 10^{-17} Pa

Temperature 4 K

A bee 200m away



Most serious difficulty? Interstellar medium: 10^{-14} Pa

Bold conclusion: we can probe Planck time regime!

Cautious conclusion: probing Planck time may not be so impossible as we used to think

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Intuitive understanding

for why it is possible

1. Gravity is weak!



Between the 2 bees, difference of proper time of 10^{-30} s !

2. Magnifying power of interferences



3. Leverage effect of fundamental constants

$$\delta\phi = \frac{GMmt}{\hbar} \frac{l}{d(d+l)}$$



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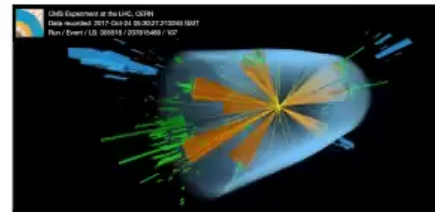
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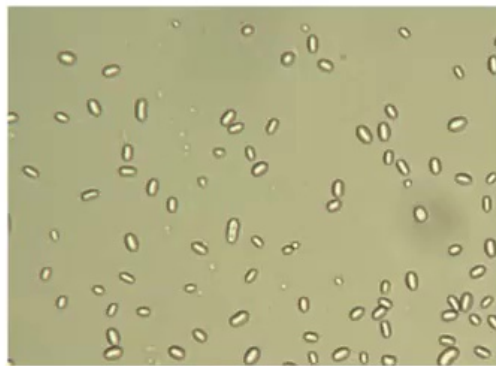
4. Leverage effect of statistics



Historical examples

*Probing a microscopic scale with many
low-energy mesoscopic particles.*

1905: brownian motion of
pollen grains to measure
the size of atoms (Einstein)



1909: oil drop experiment
to measure the elementary
electric charge (Millikan)



Conclusion

- We propose an experiment to test an hypothesis about a possible granularity of time.
- We show that it is not too far removed from current technological capabilities.

Christodoulou, Di Biagio, Martin-Dussaud 2007.08431



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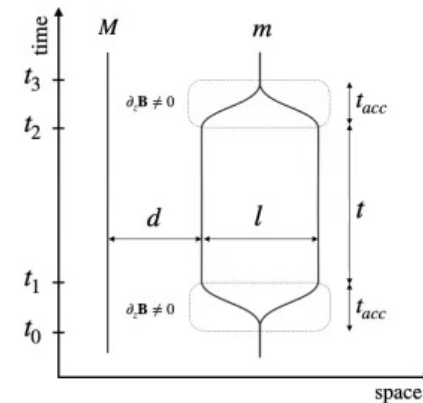
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Motivations and alternative hypotheses

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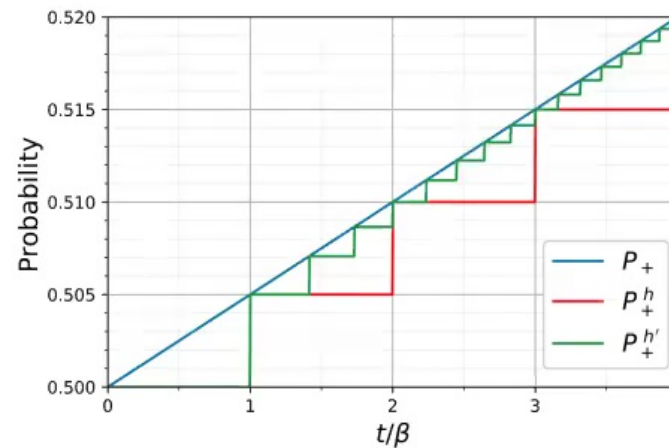
$$\delta\tau = n t_P, \quad n \in \mathbb{N}.$$



None of the main current theories predict such a behaviour.

Loop Quantum Gravity: discrete area $A_j = 8\pi\gamma l_P^2 \sqrt{j(j+1)}, \quad j \in \mathbb{N}/2$

Dimensional comparison: $\delta\tau = \sqrt{n} t_P$? 😊



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Motivations and alternative hypotheses

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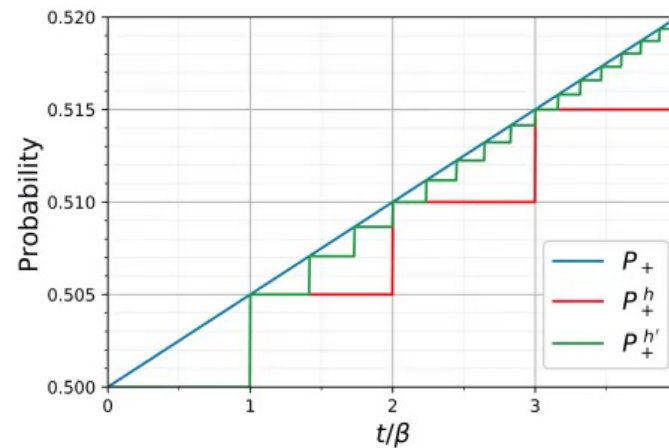
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$$\tau = \sqrt{n} t_P \quad ?$$

$$\delta\tau = \frac{n t_P}{N}$$



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