

Title: Recent results on Kitaev interactions in Co based magnets

Speakers: Peter Armitage

Series: Quantum Matter

Date: October 25, 2021 - 12:00 PM

URL: <https://pirsa.org/21100049>

Abstract: Kitaev quantum spin liquids (QSLs) are exotic states of matter that are predicted to host Majorana fermions and gauge flux excitations. However, so far all known Kitaev QSL candidates are known to have appreciable non-Kitaev interactions that pushes these systems far from the QSL regime. Co based magnets have been proposed to be perhaps a more ideal platform for realizing Kitaev QSLs. In this talk I will show evidence for a Kitaev interactions in both the quasi-one-dimensional ferromagnet CoNb₂O₆ as well as the hexagonal magnet BaCo₂(AsO₄). Although it is usually believed to be the best material realization of a 1D Ising chain, by combining terahertz spectroscopy and calculations we have shown that CoNb₂O₆ is well described by a model with bond-dependent interactions. We call this model the 'twisted Kitaev chain', as these interactions are similar to those of the honeycomb Kitaev spin liquid. The ferromagnetic ground state of CoNb₂O₆ arises from the compromise between two axes. Owing to this frustration, even at zero field domain walls have quantum motion, which is described by the celebrated Su-Schrieffer-Heeger model of polyacetylene and shows rich behavior as a function of field. Most recently, we have shown also that the honeycomb cobalt-based Kitaev QSL candidate, BaCo₂(AsO₄)₂, has dominant Kitaev interactions. Due to only small non-Kitaev terms a magnetic continuum consistent with Majorana fermions and the existence of a Kitaev QSL can be induced by a small out-of-plane-magnetic field. Our results demonstrate BaCo₂(AsO₄)₂ as a far more ideal version of Kitaev QSL compared with other candidates.

C. M Morris et al. "Hierarchy of bound states in the one-dimensional ferromagnetic Ising chain CoNb₂O₆ investigated by high-resolution time-domain terahertz spectroscopy." Phys. Rev. Lett. 112.13 137403 (2014).

C.M. Morris et al. "Duality and domain wall dynamics in a twisted Kitaev chain", Nature Physics

volume 17, pages 832-836 (2021).

X. Zhang, et al., "In- and out-of-plane field induced quantum spin-liquid states in a more ideal Kitaev material: BaCo₂(AsO₄)", <https://arxiv.org/abs/2106.13418>

Zoom Link: https://pitp.zoom.us/meeting/register/tJcqc-ihqzMvHdW-YBm7mYd_XP9Amhypv5vO

Recent results on Kitaev interactions in Co based magnets: chains and honeycomb



N. Peter Armitage

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The Institute of Quantum Matter
Dept. of Physics and Astronomy
The Johns Hopkins University



U.S. DEPARTMENT OF
ENERGY



GORDON AND BETTY
MOORE
FOUNDATION



Chris Morris



Xinshu Zhang



**Tyrel
McQueen**



**Bob Cava
(Princeton)**



**Seyed
Koohpayeh**

N. Peter Armitage



**Ribhu Kaul
(Kentucky)**



Natalia Drichko



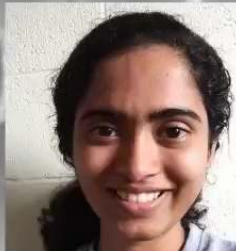
Yuanyuan Xu



**Ruin Zhong
(Princeton)**



**Oleg
Tchernyshyov**



**Nisheeta Desai
(Kentucky)**



**Toomas Room
(NICPB Estonia)**



Tom Halloran



Collin Broholm



**Subir Sachdev
(Harvard)**

Recent results on Kitaev interactions in Co based magnets



CoNb_2O_6 , best material realization of “Ising’s model”

- THz experiments on CoNb_2O_6 in zero field; 9 “meson” bound states at low temperature.

- Ising chain in transverse magnetic field; simplest example of a quantum phase transition; **Kramers-Wannier duality**; **twisted Kitaev** chain

Quantum spin-liquid states in a more ideal **Kitaev** material:

$\text{BaCo}_2(\text{AsO}_4)_2$

- small J and Γ terms.

- out-of-plane field of a few T can induce a **QSL**.

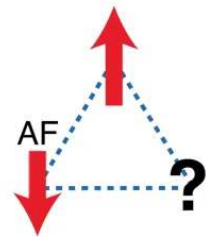
Morris et al. PRL 2014

Steinberg, NPA, et al. PRB 2019

Morris et al. Nature Physics 2021

Zhang et al. arXiv 2106.13418.

Frustrated magnets



$$H = - \frac{1}{2} \sum_{ij} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

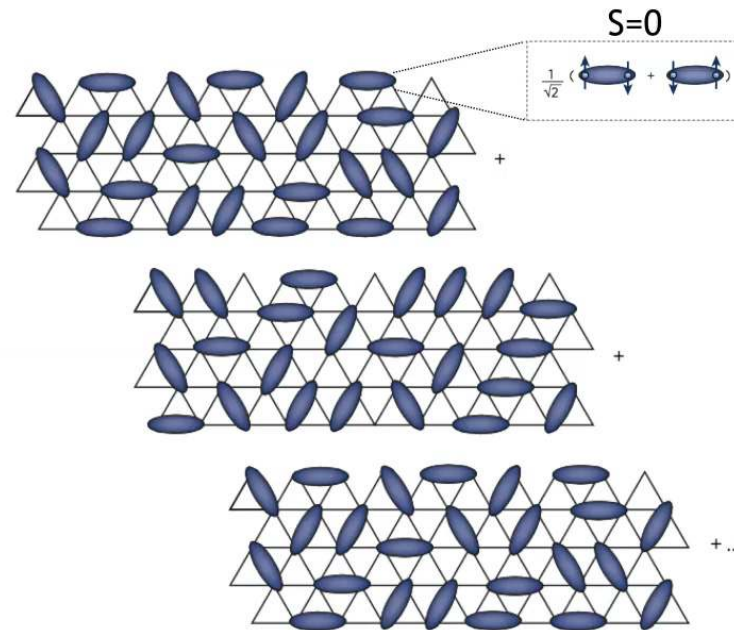
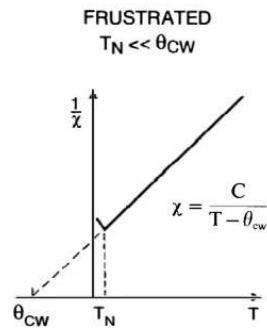
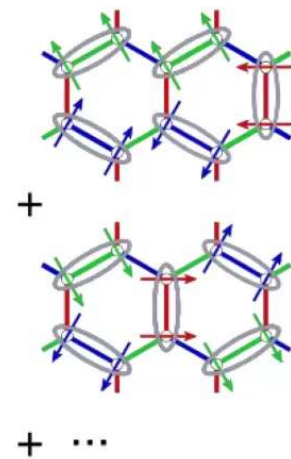
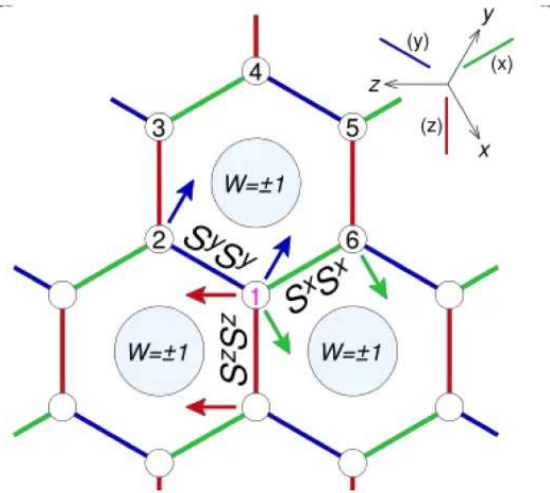


Image courtesy of L. Balents

Kitaev interaction in honeycomb lattice



Takagi et al.

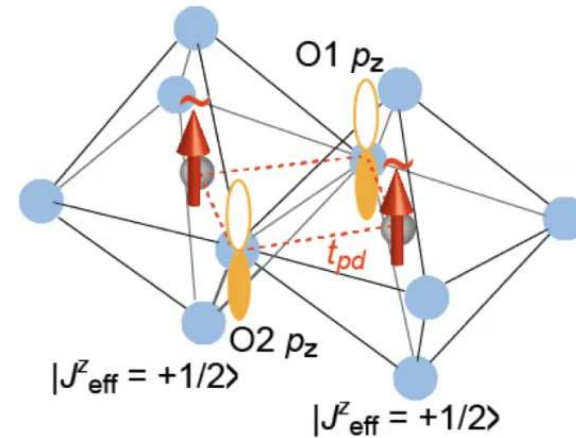
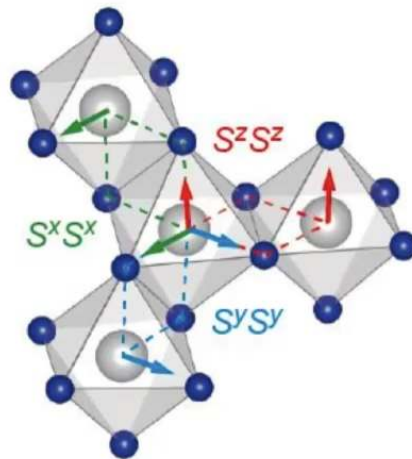
Kitaev demonstrated exactly solvable model of a spin liquid with each bond with Ising interaction in different direction.

$$H_K = \sum_{i,j} K^\gamma S_i^\gamma S_j^\gamma$$

5



Kitaev interaction in honeycomb lattice

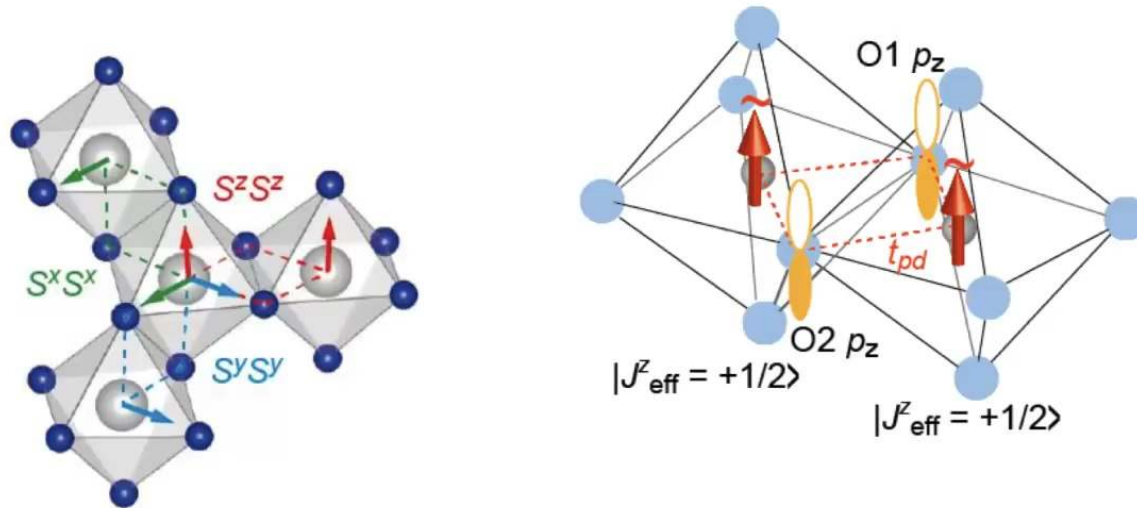


Jackeli and Khaliullin showed possible in edge sharing octahedra with strong SOC. But other interactions exist (Heisenberg etc.)

Possible in Na_2IrO_3 , RuCl_3 and $\text{H}_3\text{LiIr}_2\text{O}_6$ and also proposed for Co^{+2} systems

$$\mathcal{H}_1 = \sum_{\langle ij \rangle_\gamma} K S_i^\gamma S_j^\gamma$$

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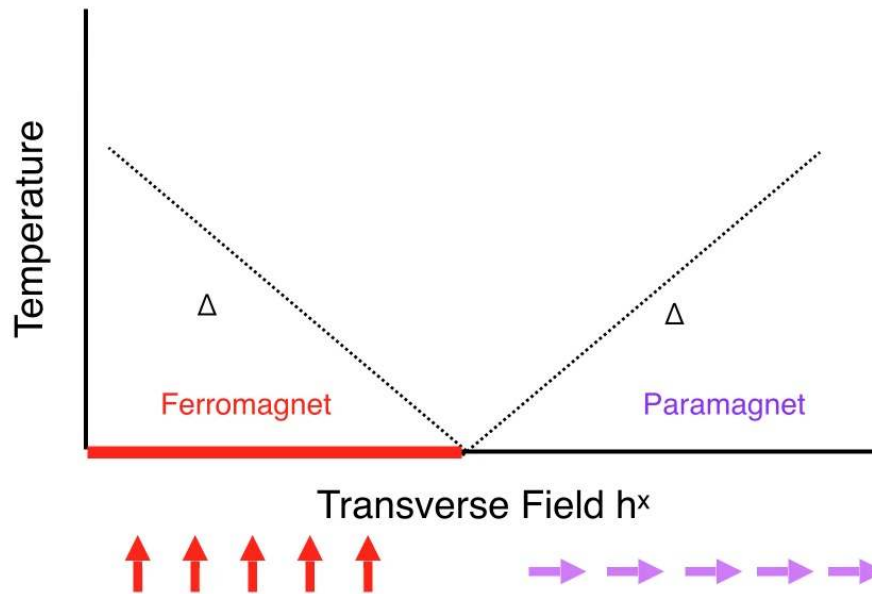
Possible in Na_2IrO_3 , ∞ - RuCl_3 and $\text{H}_3\text{LiIr}_2\text{O}_6$ and also proposed for Co^{+2} systems

$$\mathcal{H}_1 = \sum_{\langle ij \rangle_\gamma} \left[K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j + \Gamma \left(S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha \right) + \Gamma' \left(S_i^\gamma S_j^\alpha + S_i^\alpha S_j^\gamma + S_i^\beta S_j^\alpha + S_i^\alpha S_j^\beta \right) \right] \\ + J_3 \sum_{\langle ij \rangle_3} \mathbf{S}_i \cdot \mathbf{S}_j + \mu_B \sum_{\langle i \rangle} \mathbf{B} \cdot \mathbf{g} \cdot \mathbf{S}_i,$$



The Ising chain in transverse field

Energy scales collapse near a quantum phase transition



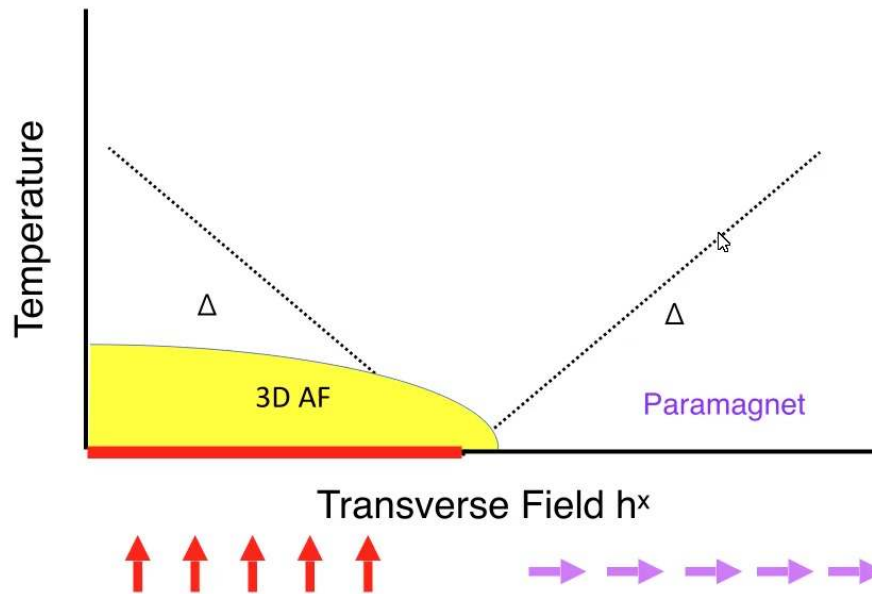
Limits of high field and low field are well defined.

There must be a QPT as ground state changes degeneracy

General phenomena → changing of ground state as function of non-thermal parameter; phase transition

$$H = -J' \sum_n S_n^z S_{n+1}^z - h^x \sum_n S_n^x$$

Energy scales collapse near a quantum phase transition



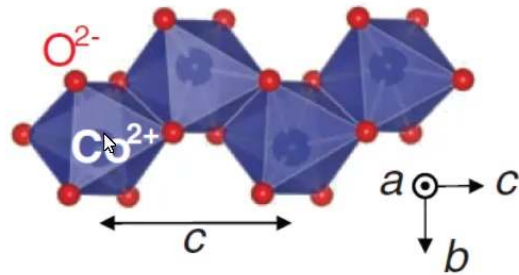
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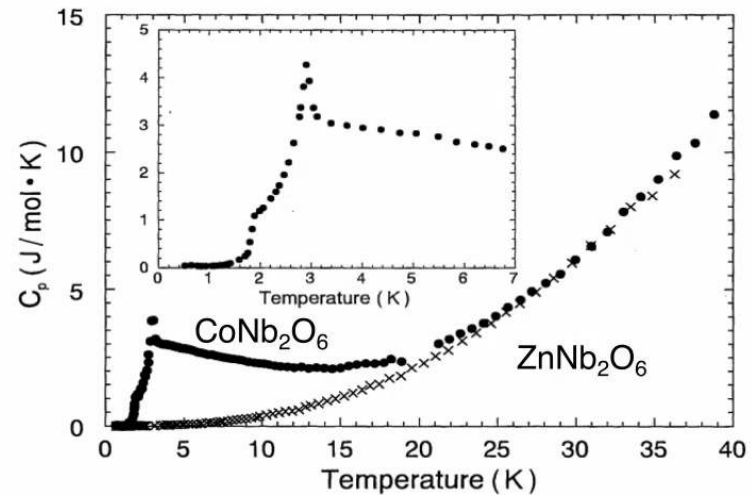
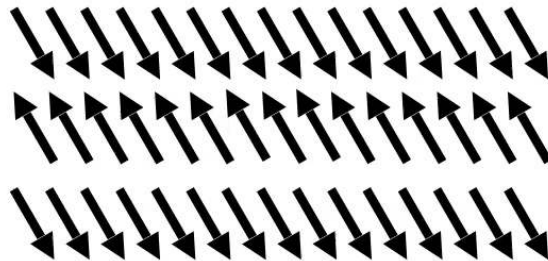
CoNb₂O₆ – Columbite - Ising chain material



R. Coldea et. al., Science **327**, 177 (2010)

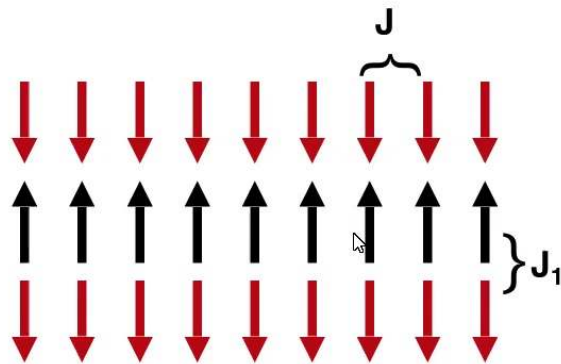
Spins point in a-c plane

- $T_{N1} = 2.95$ K, incommensurate AF ordering of FM chains
- $T_{N2} = 1.97$ K, commensurate AF ordering of FM chains
- Interesting QCP @ $H_b = 5.5$ Tesla



T. Hanawa et. al., J. Phys. Soc. Jap. **63**, 2706 (1994)

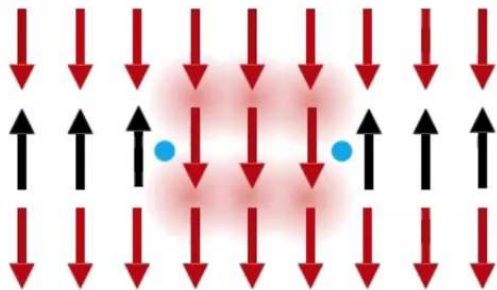
CoNb₂O₆ – Ising chain material - Excitations



Below T_{N2} , interchain mean field gives effective confining potential linear in separation of domain walls. Strong $S_z S_{z+1}$ interaction.

$$E_n = 2(J/2) + n J_1$$

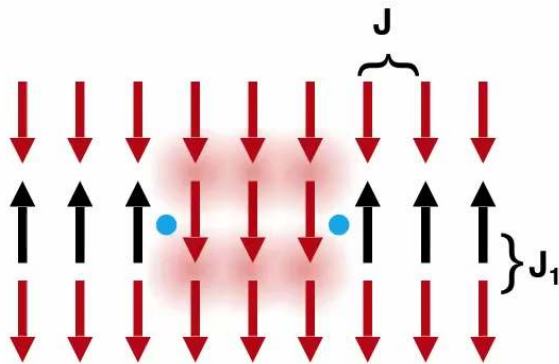
n is # of flipped spins



But real materials are not pure Ising! → S_x, S_y and inter-chain couplings give “kink” motion.

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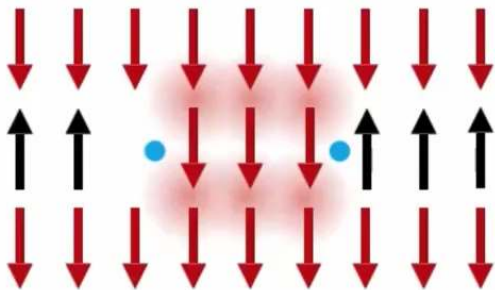
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00:01

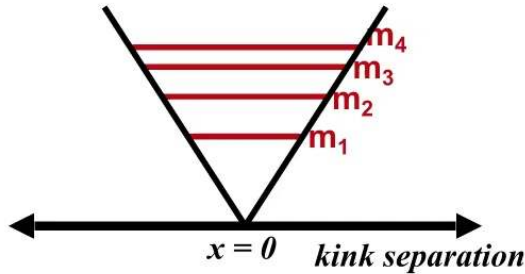


-00:05



CoNb₂O₆ – Ising chain material - Excitations

Rewrite equations of motion with kink as fundamental particle



$$V(x) = \lambda|x|$$

$$-\frac{\hbar^2}{\mu} \frac{d^2\varphi}{dx^2} + \lambda|x|\varphi = (m - 2m_0)\varphi \quad (2)$$

$$m_j = 2m_0 + z_j \lambda^{2/3} \left(\frac{\hbar^2}{\mu}\right)^{1/3} \quad j = 1, 2, 3, \dots$$

Mapping to continuum 1D
Schrodinger equation with linearly
confining potential

Solutions are Airy functions, z_j are the
negative roots to Airy functions ($z_j =$
2.34, 4.09, 5.52, 6.79, 7.94, 9.02, ...)

PHYSICAL REVIEW D

VOLUME 18, NUMBER 4

15 AUGUST 1978

Two-dimensional Ising field theory in a magnetic field: Breakup of the cut in the two-point function

Barry M. McCoy

Institute for Theoretical Physics, State University of New York, Stony Brook, New York 11794

Tai Tsun Wu*

Institute for Theoretical Physics, Utrecht, The Netherlands

(Received 12 April 1978)

We demonstrate that the cut which is present as the leading singularity in the two-point function of the Ising field theory for $T < T_c$ and $H = 0$ breaks up into a sequence of poles for $H \neq 0$. Both the positions and the residues of the low-lying poles are calculated.

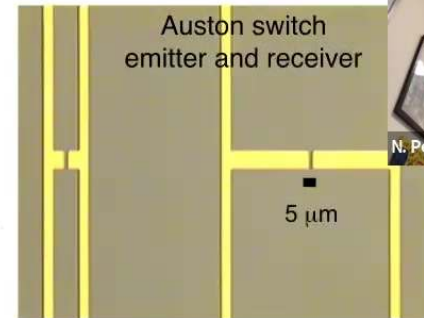
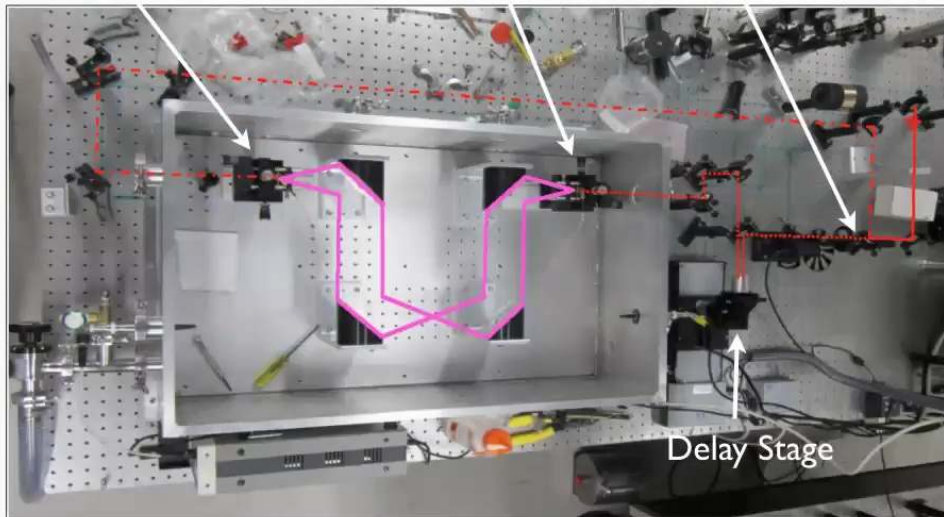
Analogy to quark confinement in QCD
kinks are quarks, bound state is a meson

Time Domain THz Spectroscopy

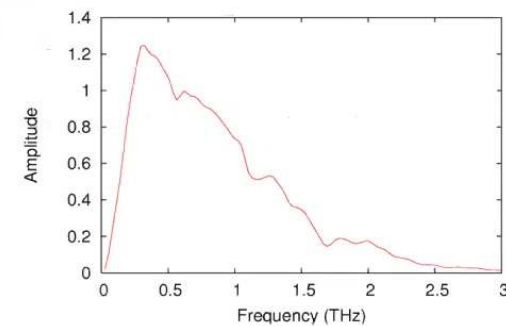
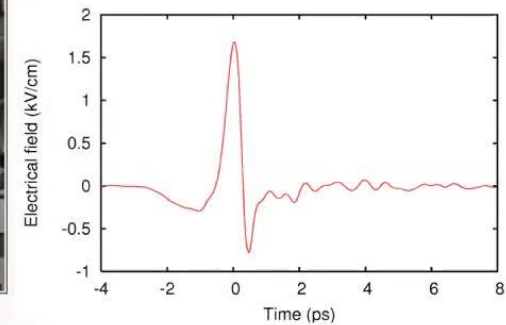
Receiver

Emitter

Beam Splitter



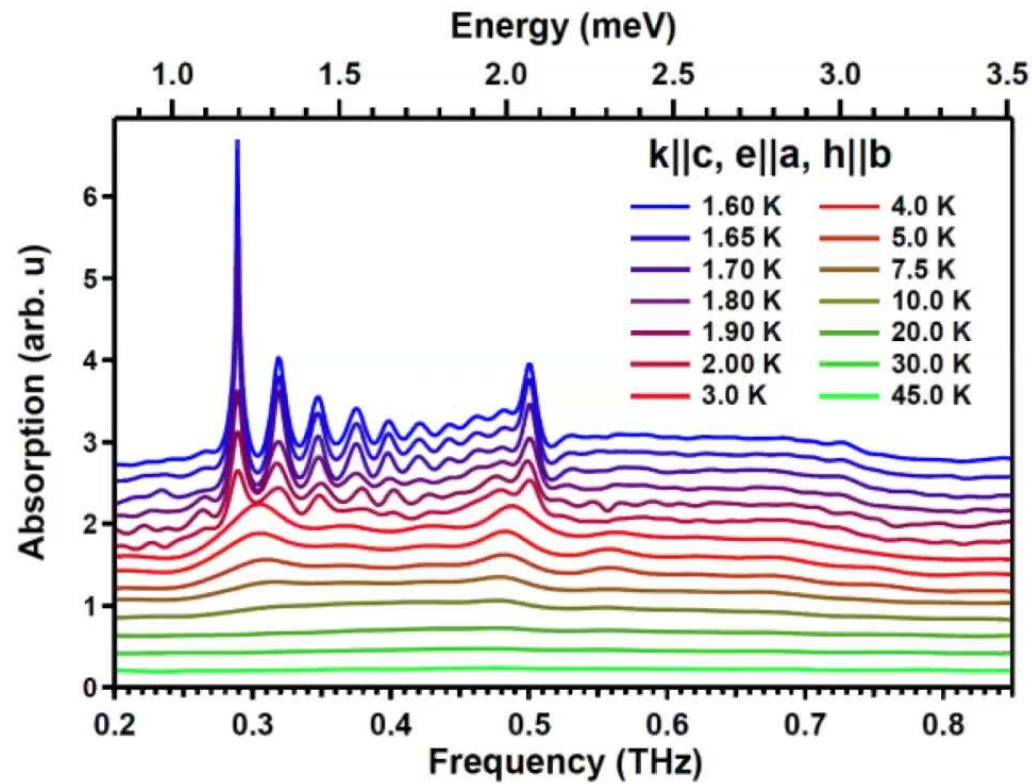
N. Peter Armitage



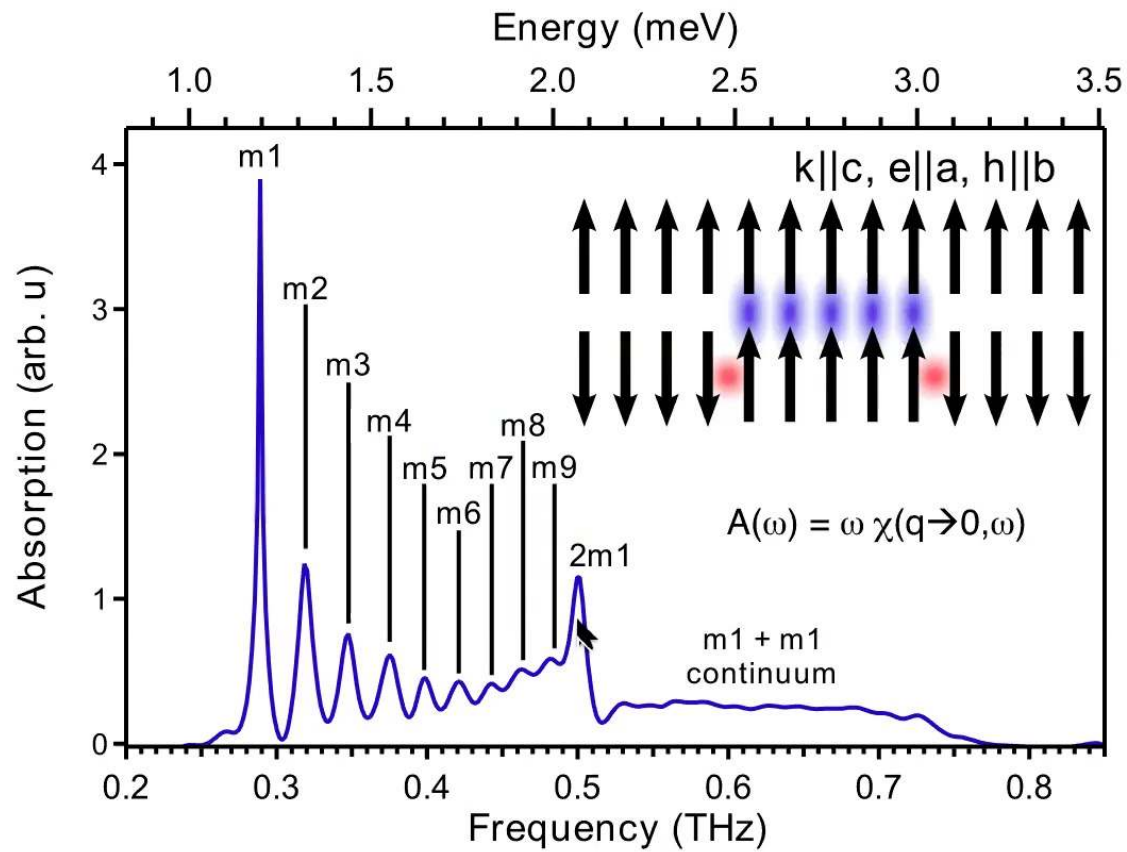
- fs laser excites photoconductive emitter and receiver. Coherent detection of field allows **complex** optical response functions to be measured: 100 GHz - 3 THz (0.8 meV - 12 meV), @ 1.4K - 300K.
- Usually light couples to charge, but can excite **magnetic** dipoles with THz B field
- Broad band THz electron spin resonance (ESR)
- Transmission $\rightarrow \ln(T(\omega)) \sim -\omega\chi(q\sim 0, \omega)$

Laser
800nm
60fs

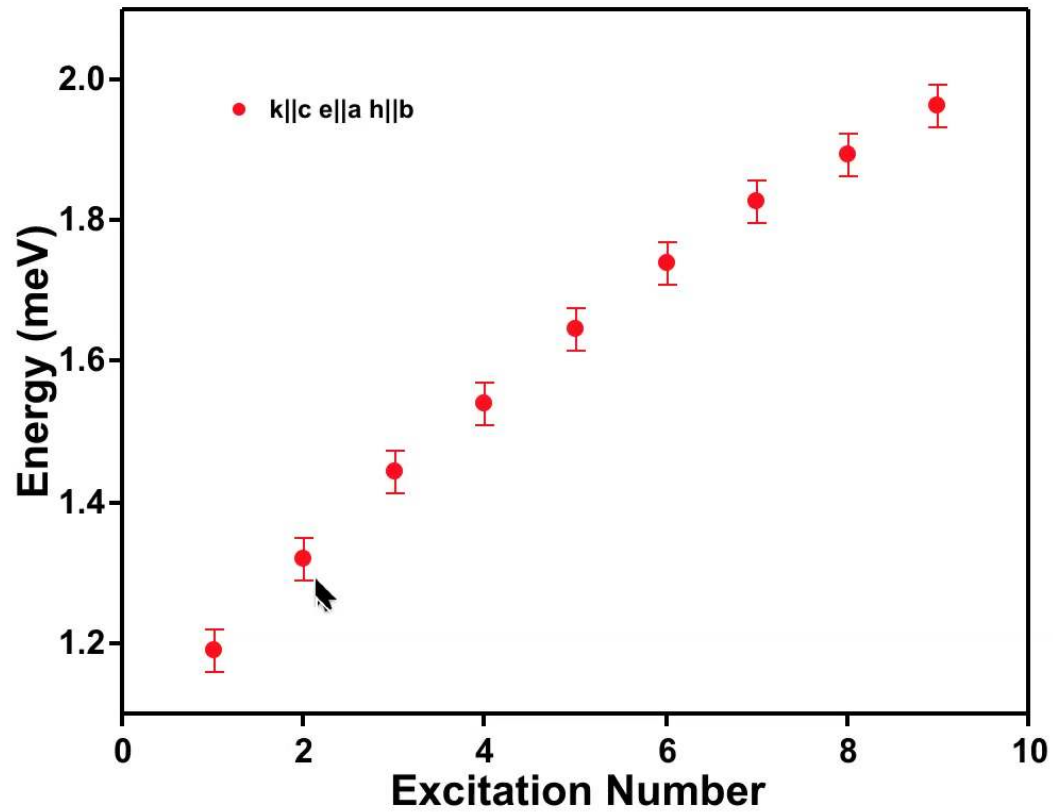
Temperature Dependence



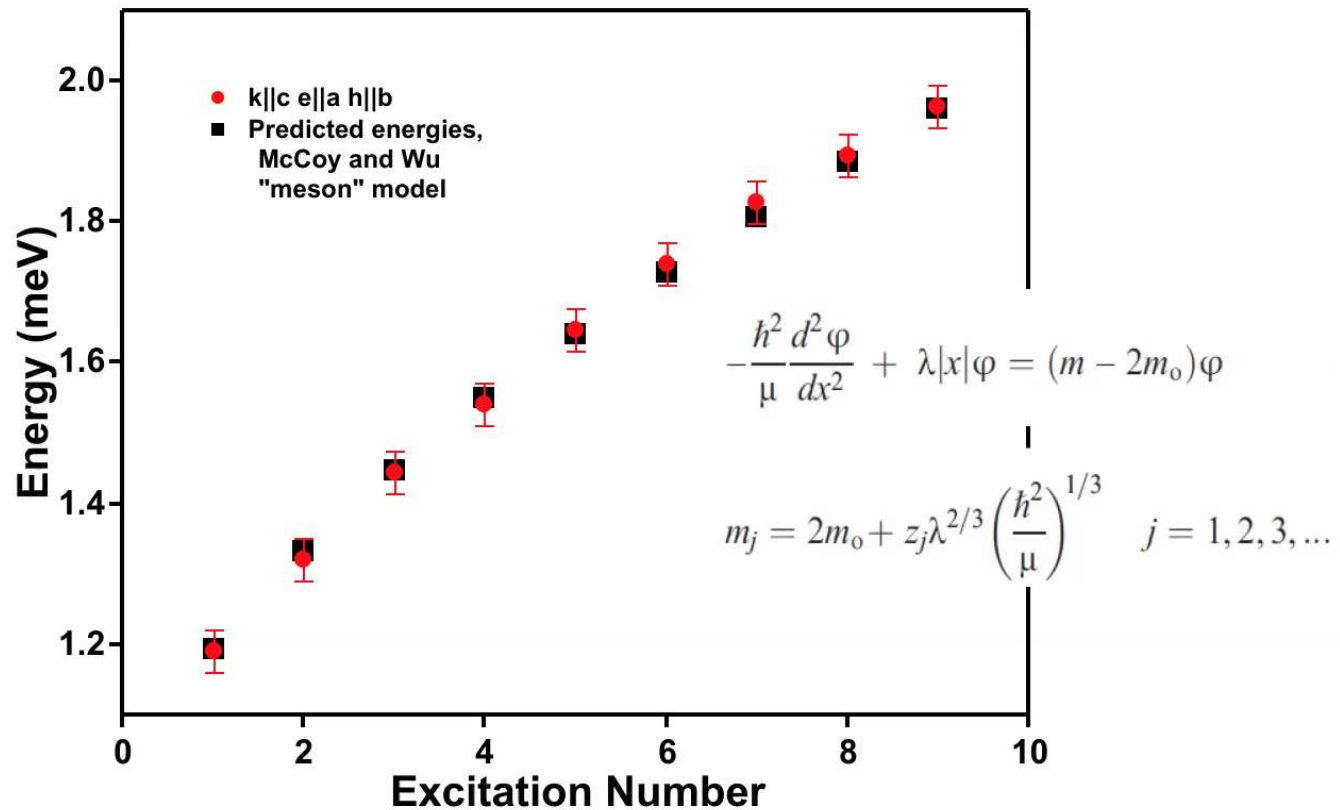
Nine “meson” bound states



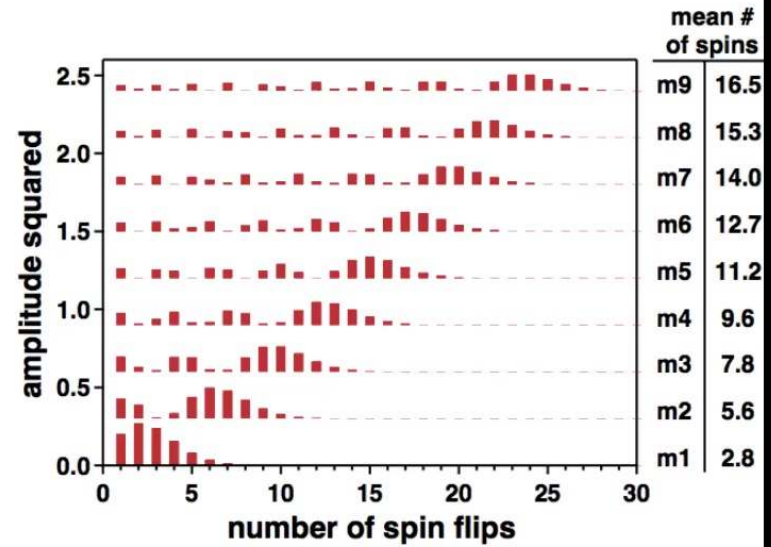
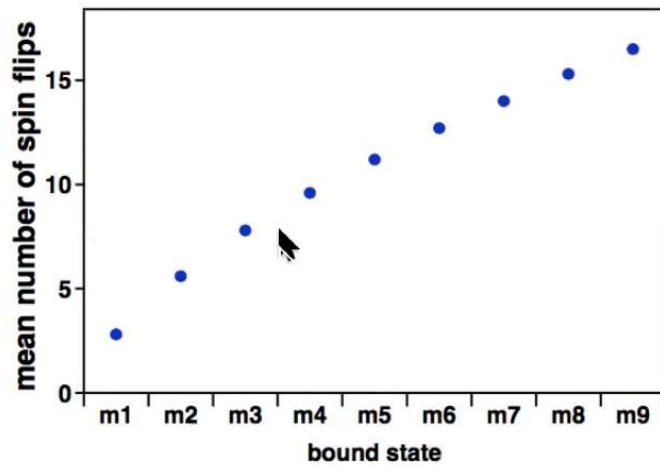
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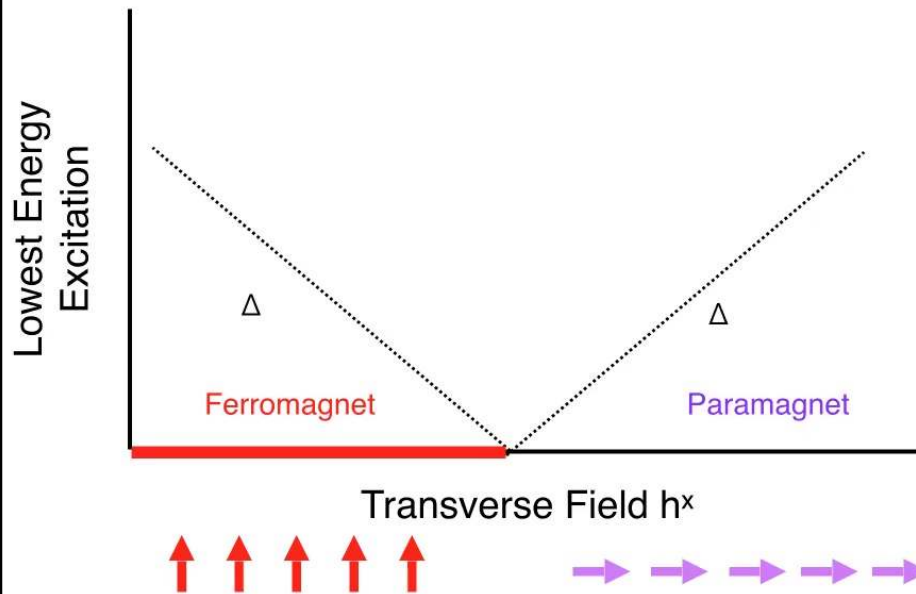
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Numerics of the 1D Ising Chain



Energy scales collapse near a quantum phase transition



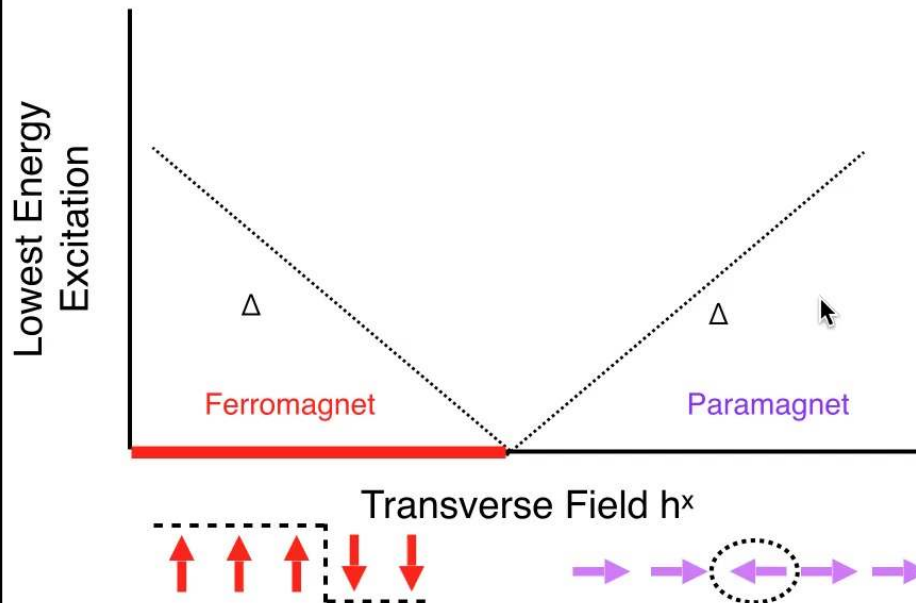
Limits of high field and low field are well defined.

There must be a QPT as ground state changes degeneracy

General phenomena \rightarrow changing of ground state as function of non-thermal parameter; phase transition

$$H = -J' \sum_n S_n^z S_{n+1}^z$$

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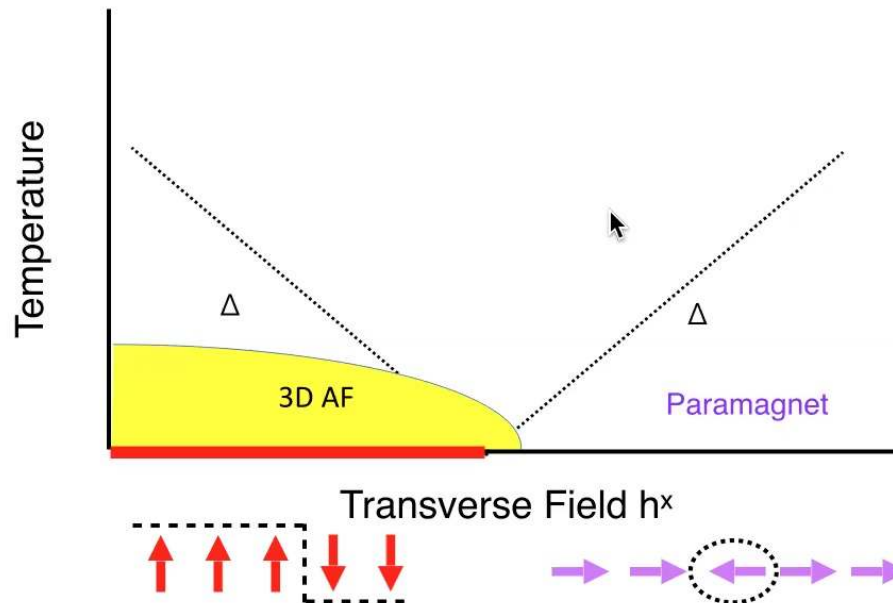
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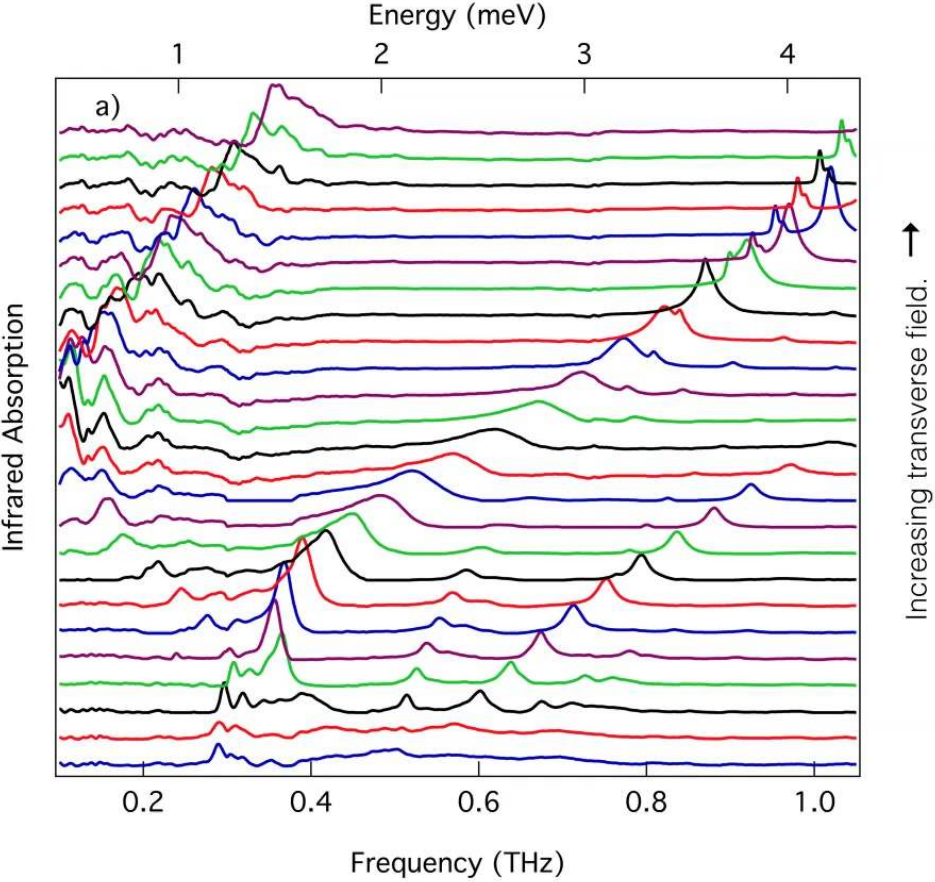
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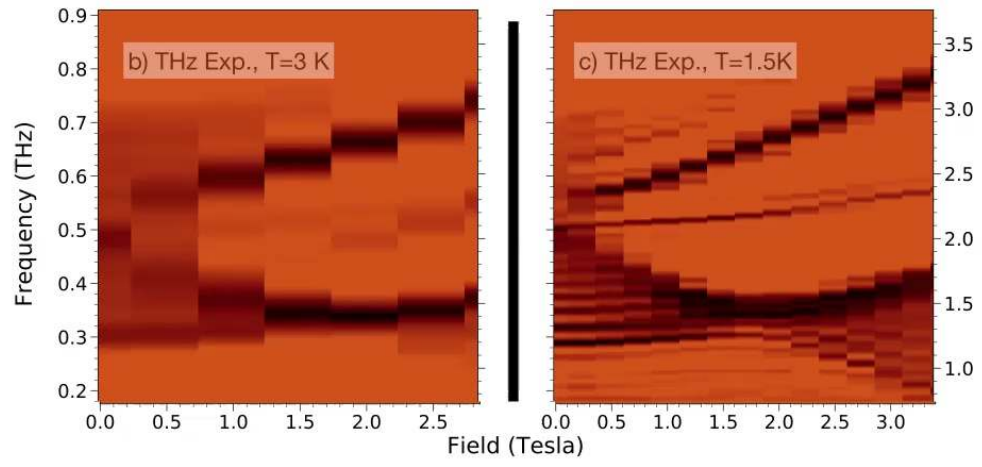
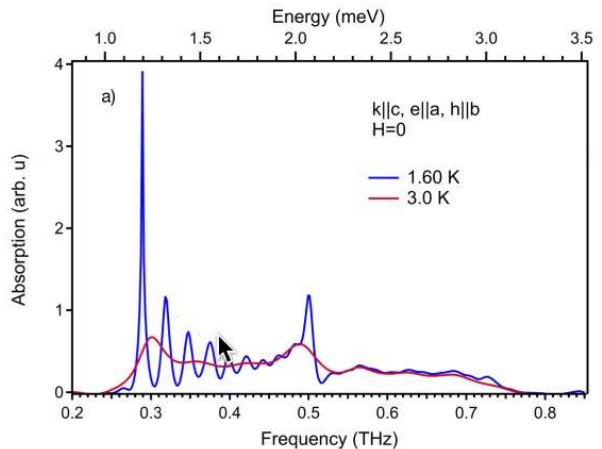
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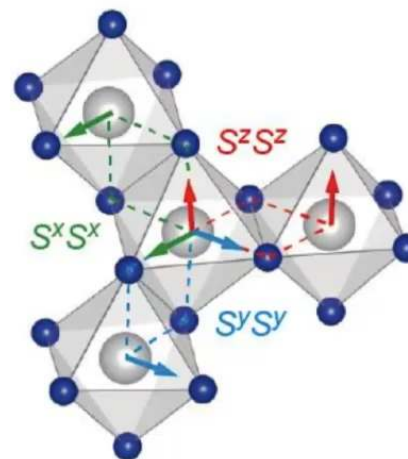
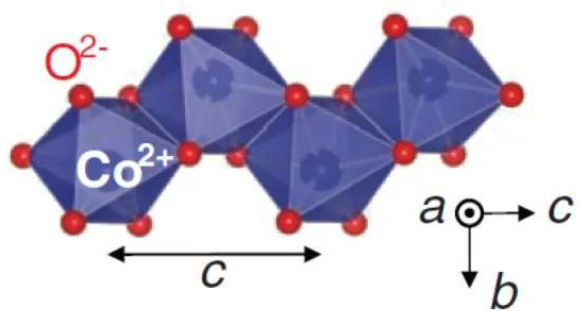
Quantum phase transition of Ising chain in transverse field



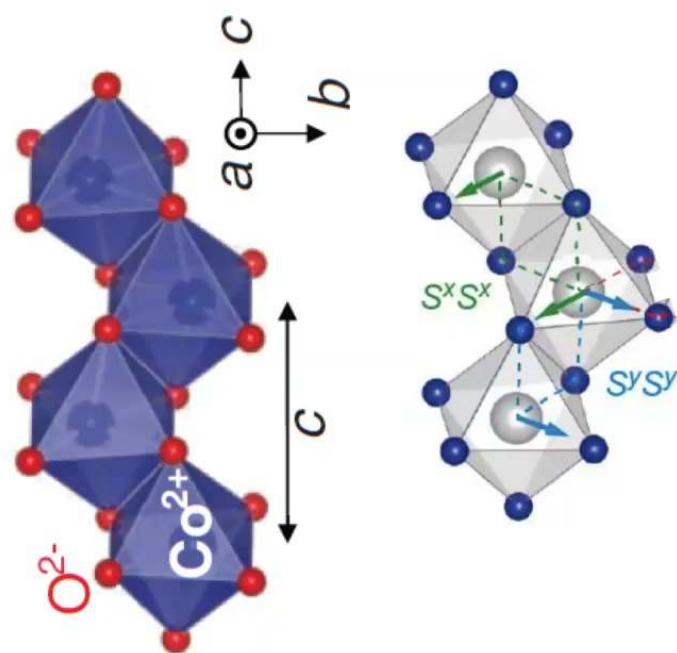
CoNb₂O₆ in transverse magnetic field



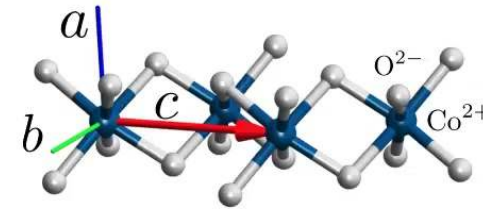
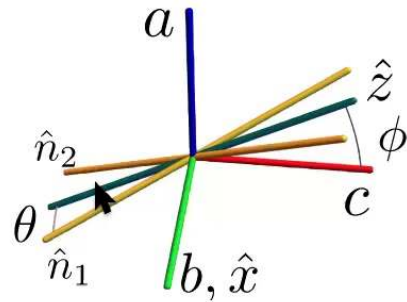
The twisted Kitaev chain



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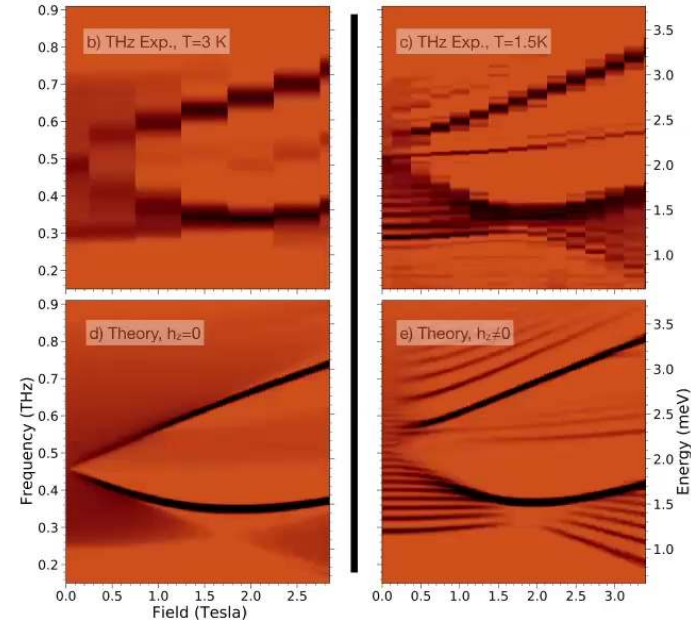


$$\mathcal{H}_K = -K \sum_{i \in \rho} \left(\tau_i^{\hat{n}_1} \tau_{i+1}^{\hat{n}_1} + \tau_{i+1}^{\hat{n}_2} \tau_{i+2}^{\hat{n}_2} \right)$$

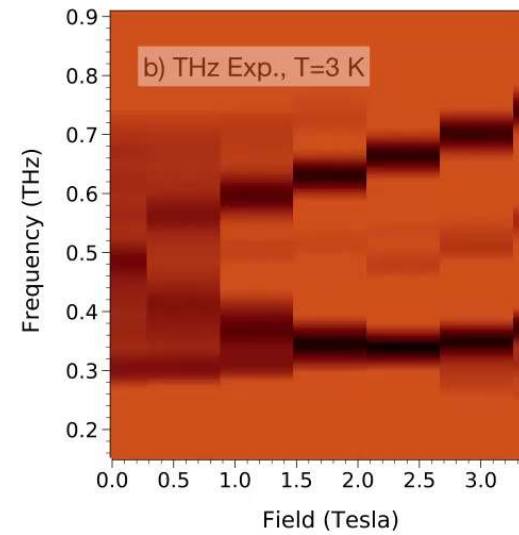
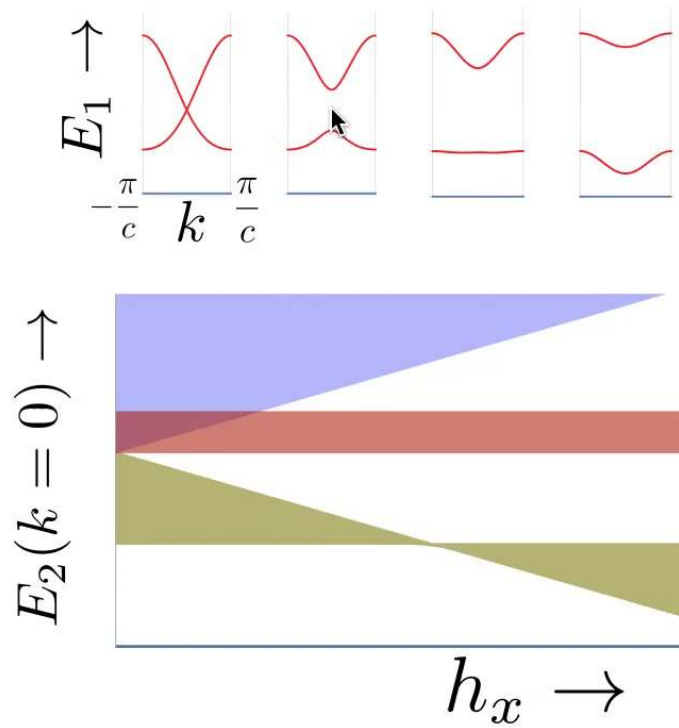
Local axes alternates sign of \hat{n} θ between octahedra

For $\theta, h_x/K, h_z/K \ll 1$.

$$\mathcal{H}_d = - \sum_n \left[(h_x + (-1)^n K \sin(2\theta)) (d_n^\dagger d_{n+1} + d_{n+1}^\dagger d_n) + K \sin^2(\theta) (d_n^\dagger d_{n+2} + d_{n+2}^\dagger d_n) \right],$$

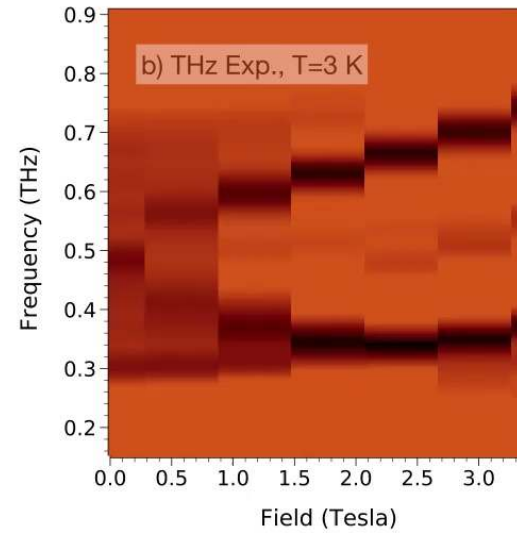
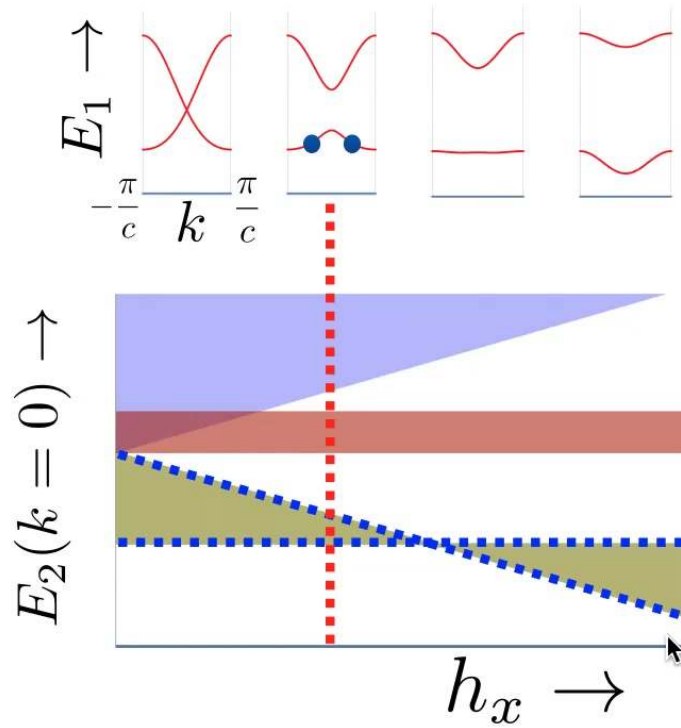


The twisted Kitaev chain



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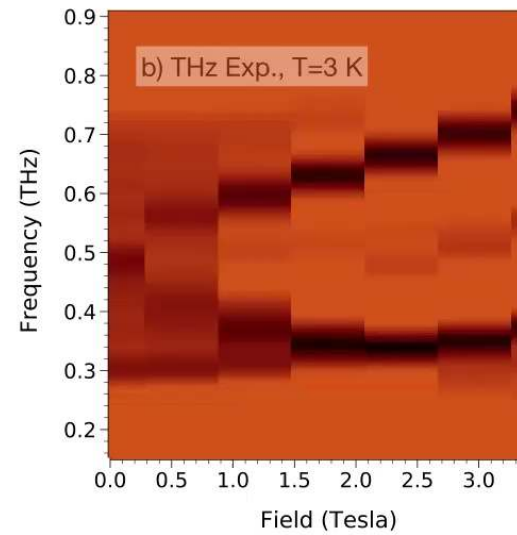
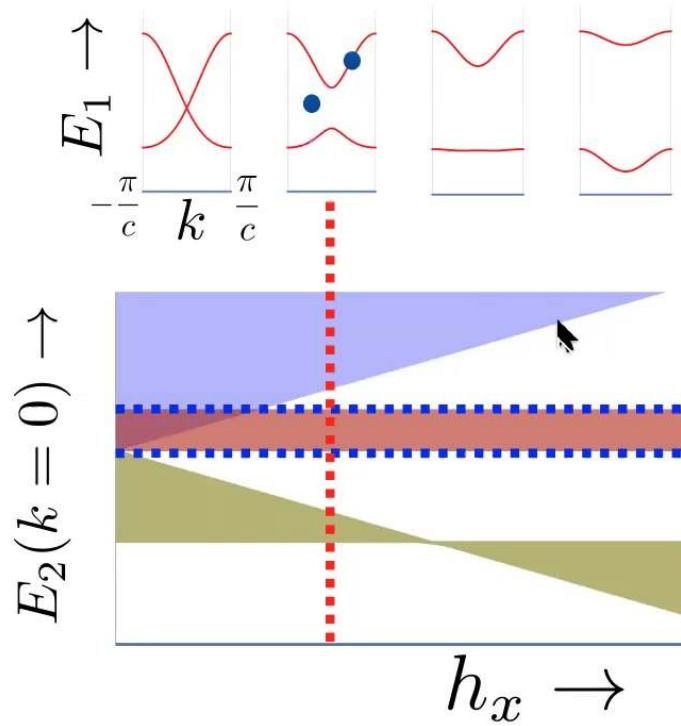
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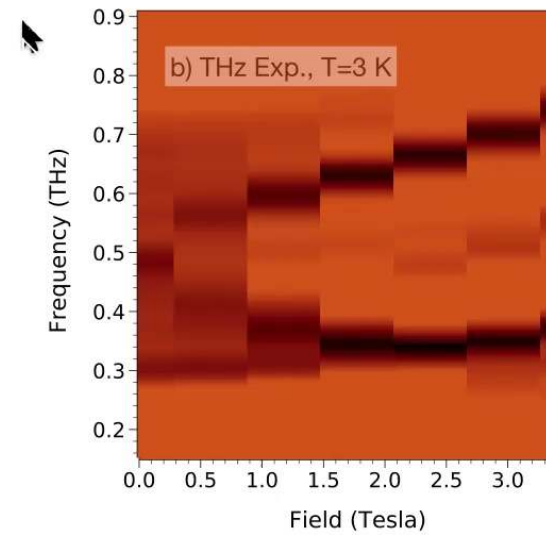
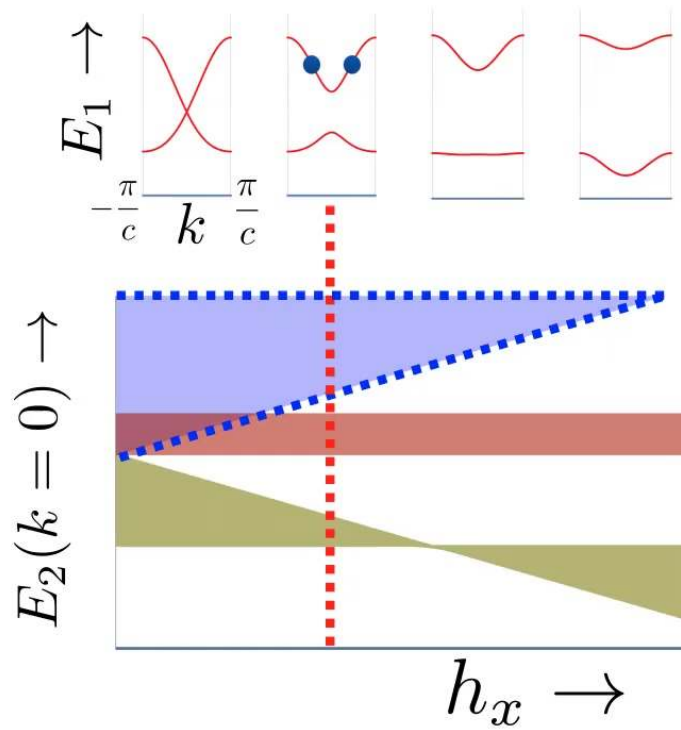
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The twisted Kitaev chain



$$\mathcal{H}_d = - \sum_n \left[(h_x + (-1)^n K \sin(2\theta)) (d_n^\dagger d_{n+1} + d_{n+1}^\dagger d_n) + K \sin^2(\theta) (d_n^\dagger d_{n+2} + d_{n+2}^\dagger d_n) \right],$$



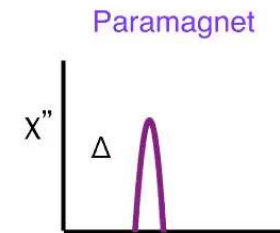
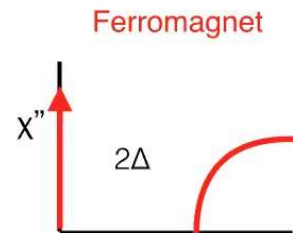
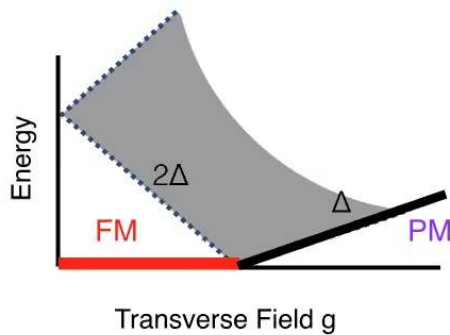
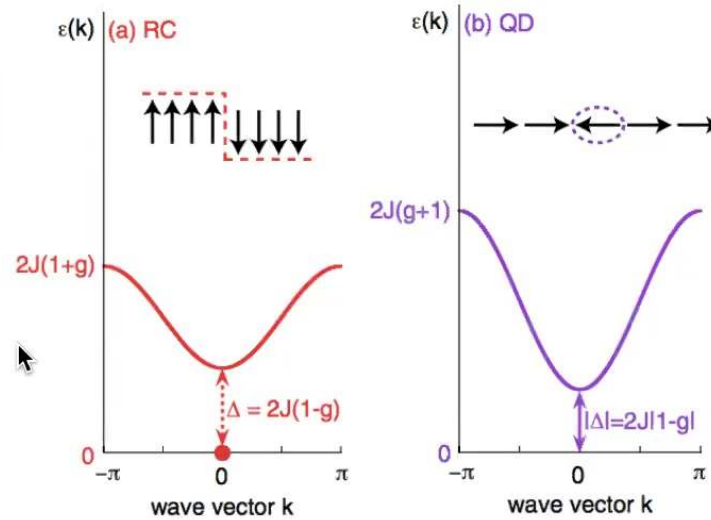
Quantum phase transition in transverse magnetic field



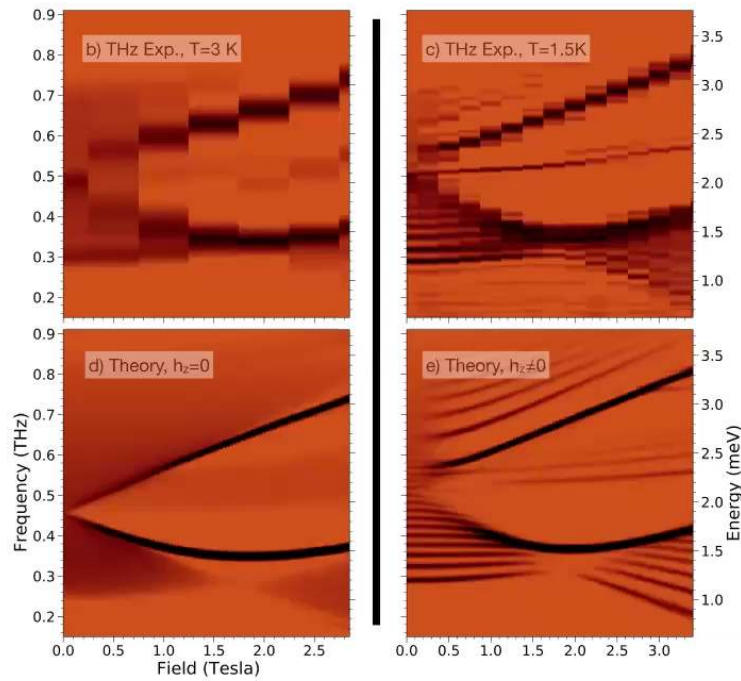
$$H = -J \sum_n \left(S_n^z S_{n+1}^z + g S_n^x \right)$$

In FM kinks are elementary excitations, but only pairs of kinks can be excited.

On paramagnetic side, spin flips are elementary excitations



The twisted Kitaev chain



$$\mathcal{H} = -K \sum_i \left[\cos^2(\theta) \tau_i^z \tau_{i+1}^z + \sin^2(\theta) \tau_i^x \tau_{i+1}^x \right. \\ \left. + \frac{\sin(2\theta)}{2} (-1)^i (\tau_i^x \tau_{i+1}^z + \tau_i^z \tau_{i+1}^x) \right] \\ - h_x \sum_i \tau_i^x - h_z \sum_i \tau_i^z.$$

$K = 0.57 \text{ meV}$, $g = 3.5$ and $\theta = 17^\circ$

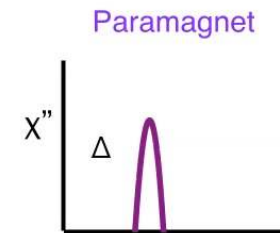
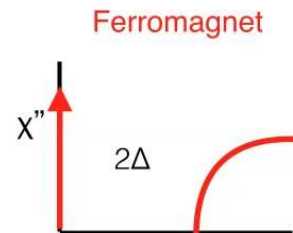
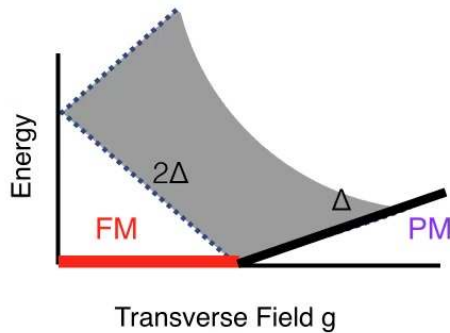
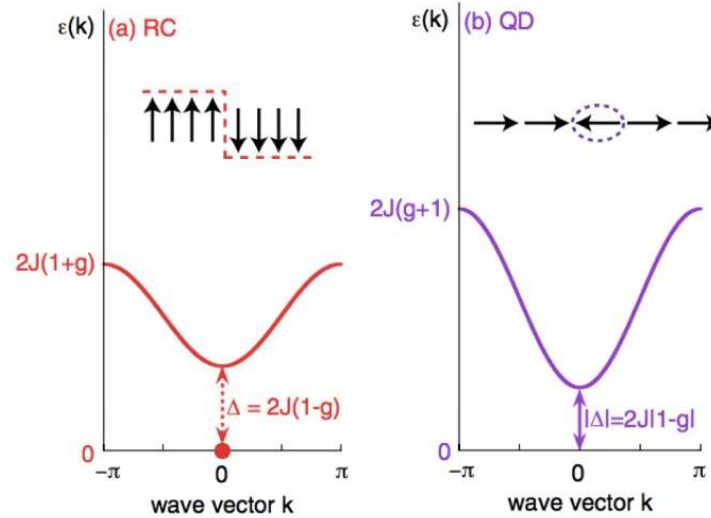
Quantum phase transition in transverse magnetic field



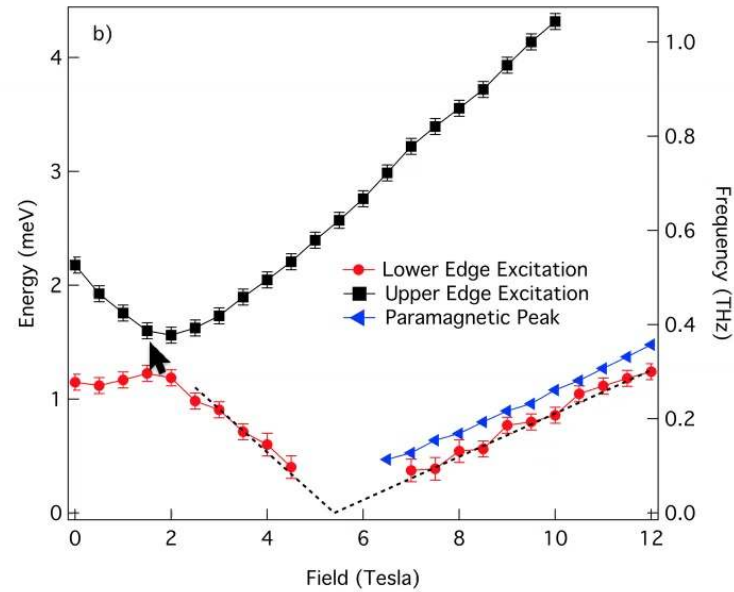
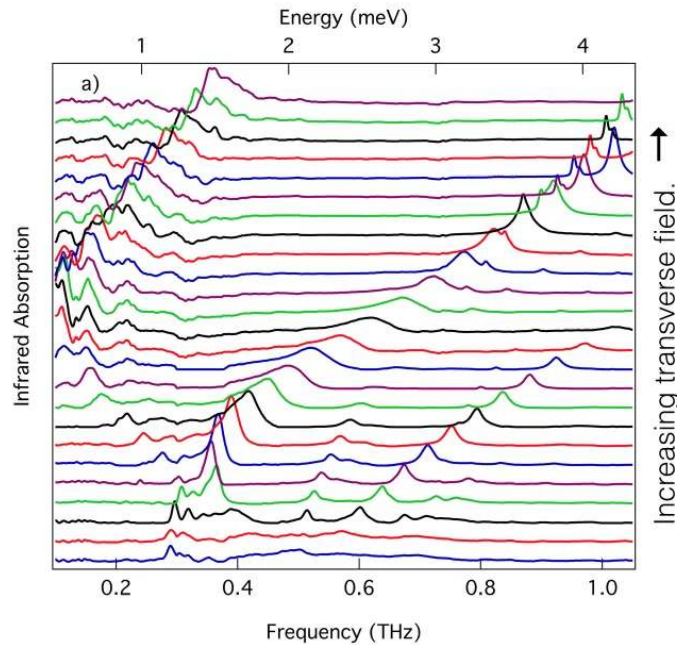
$$H = -J \sum_n \left(S_n^z S_{n+1}^z + g S_n^x \right)$$

In FM kinks are elementary excitations, but only pairs of kinks can be excited.

On paramagnetic side, spin flips are elementary excitations



Quantum phase transition of Ising chain in transverse field



Gap is suppressed twice as fast on FM side

Evidence for free fermion description of Ising chain

In FM kinks are elementary excitations, but only pairs of kinks can be excited.

On paramagnetic side, spin flips are elementary excitations

Evolution of Quantum Fluctuations Near the Quantum Critical Point of the Transverse Field Ising Chain System CoNb_2O_6

A. W. Kinross,¹ M. Fu,¹ T. J. Munsie,¹ H. A. Dabkowska,² G. M. Luke,^{1,3} Subir Sachdev,⁴ and T. Imai^{1,3*}

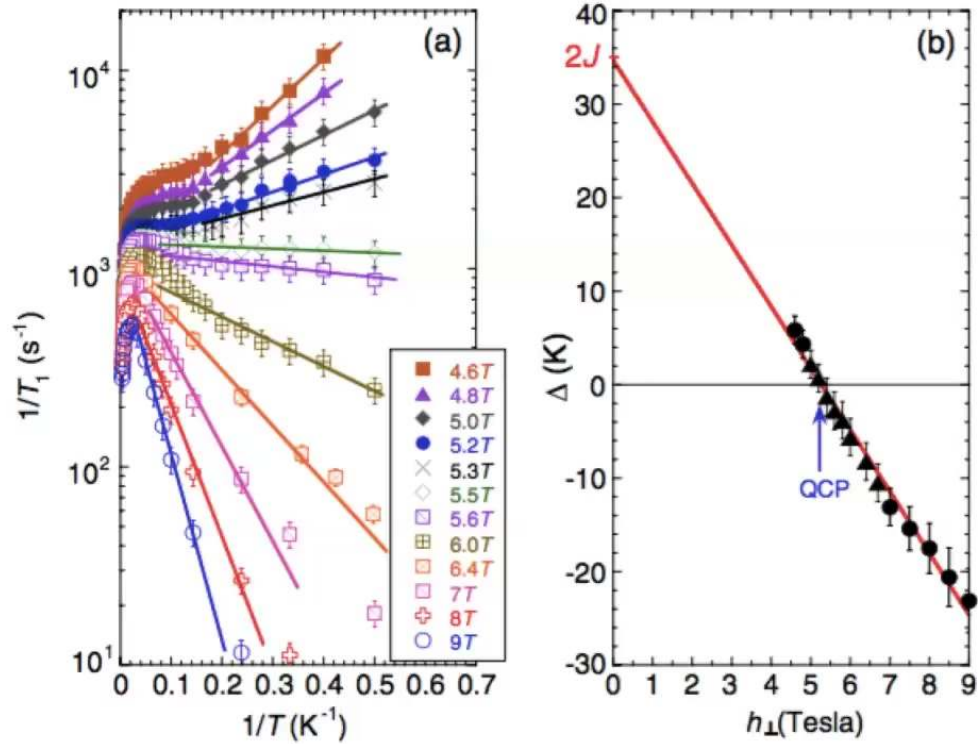
¹Department of Physics and Astronomy, McMaster University, Hamilton L8S4M1, Canada

²Brockhouse Institute for Materials Research, McMaster University, Hamilton L8S4M1, Canada

³Canadian Institute for Advanced Research, Toronto, Ontario M5G1Z8, Canada

⁴Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

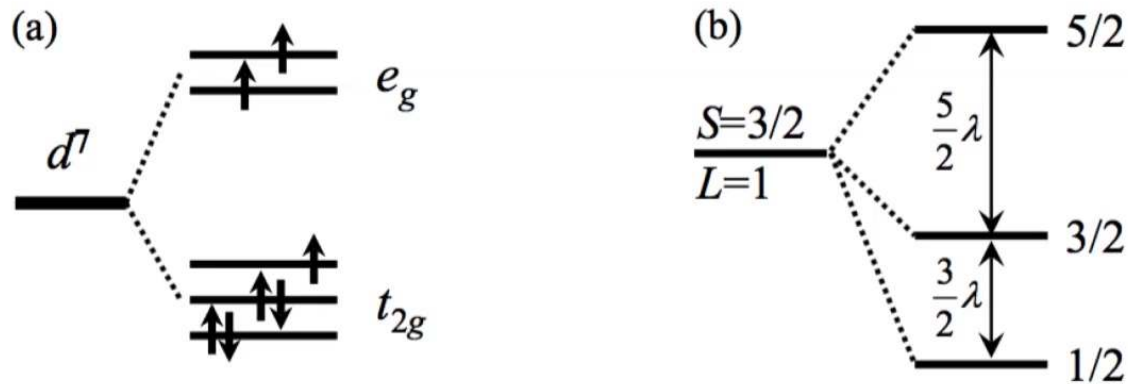
(Received 21 March 2014; published 14 July 2014)





A more ideal Kitaev material?: $\text{BaCo}_2(\text{AsO}_4)_2$

Pseudospin interactions in d7 cobalt compounds

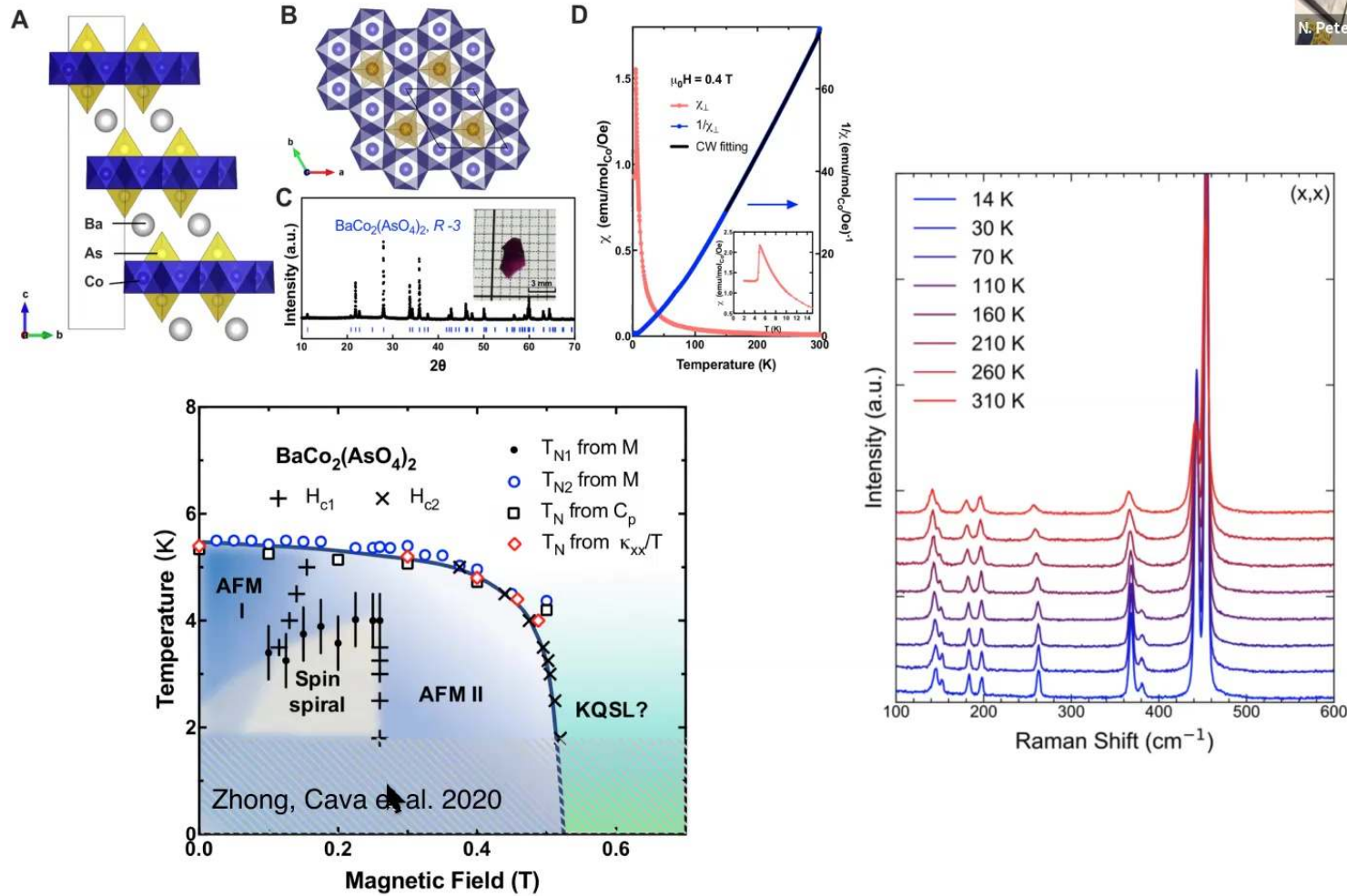


$L = 1$ and $S=3/2$ with negative spin orbit coupling parameter makes lowest **Kramers doublet** with $J=1/2$

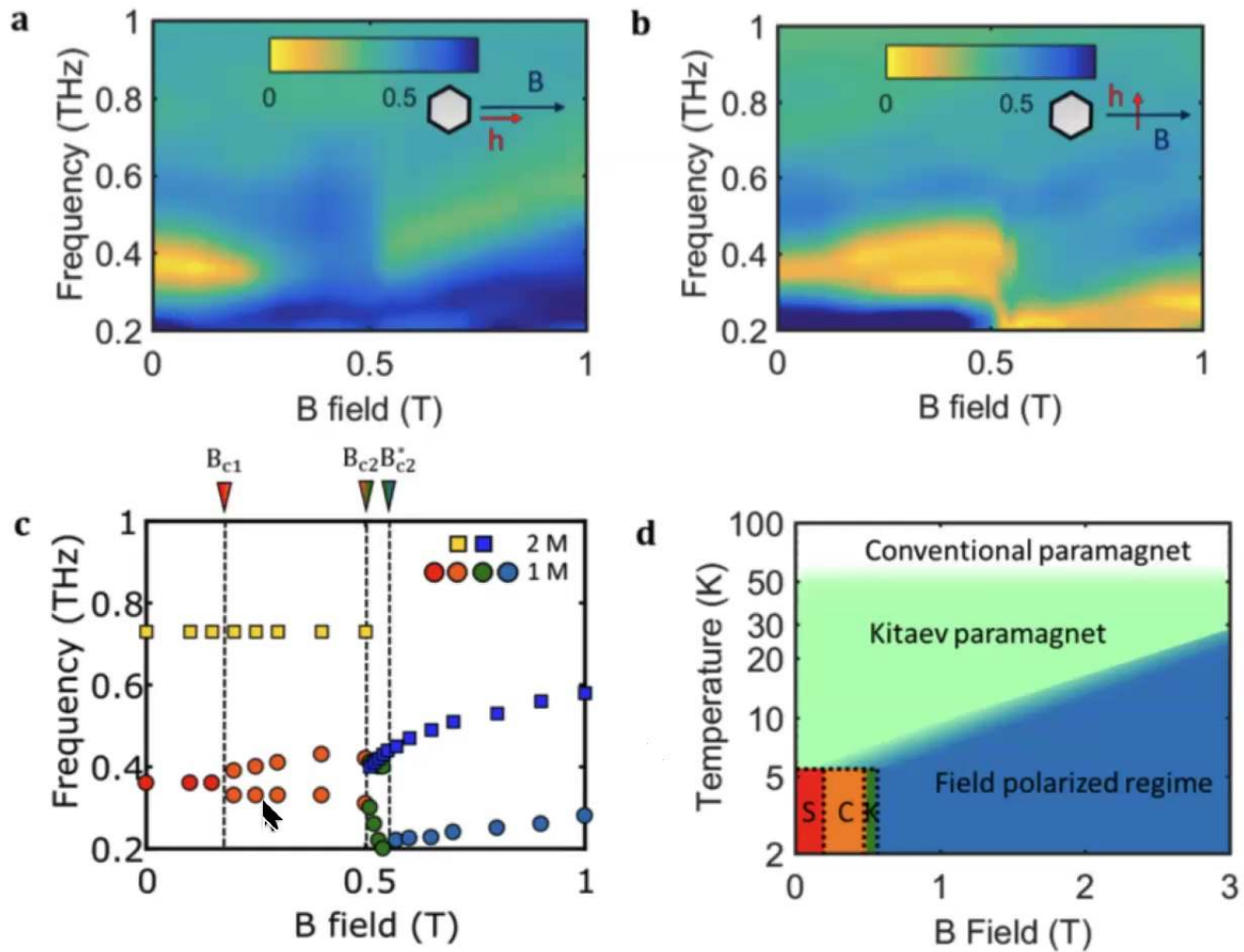
$$\begin{aligned} \left| +\frac{\tilde{1}}{2} \right\rangle &= \frac{1}{\sqrt{2}} \left| \frac{3}{2}, -1 \right\rangle - \frac{1}{\sqrt{3}} \left| \frac{1}{2}, 0 \right\rangle + \frac{1}{\sqrt{6}} \left| -\frac{1}{2}, 1 \right\rangle, \\ \left| -\frac{\tilde{1}}{2} \right\rangle &= \frac{1}{\sqrt{2}} \left| -\frac{3}{2}, 1 \right\rangle - \frac{1}{\sqrt{3}} \left| -\frac{1}{2}, 0 \right\rangle + \frac{1}{\sqrt{6}} \left| \frac{1}{2}, -1 \right\rangle. \end{aligned} \quad (1)$$

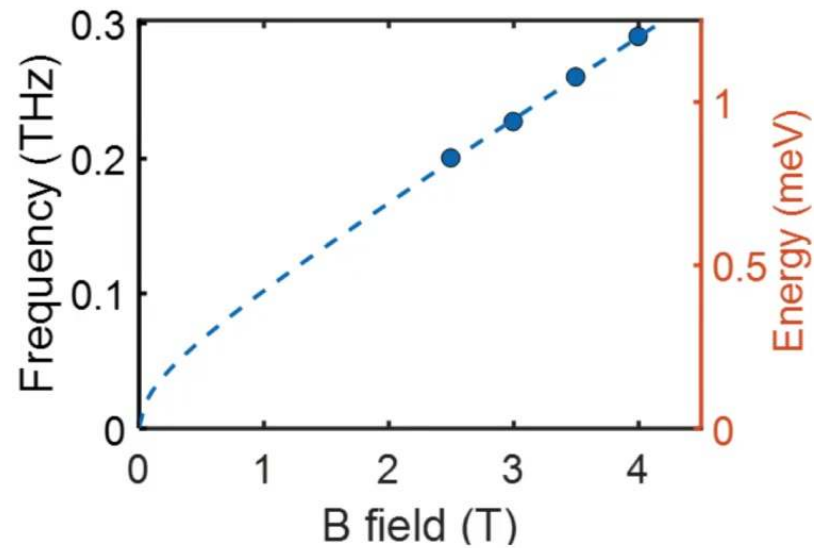
Sano, Kato, Motome (2018) and Liu, Khalullin (2018)

A more ideal Kitaev material?: $\text{BaCo}_2(\text{AsO}_4)_2$



THz spectra of $\text{BaCo}_2(\text{AsO}_4)_2$ with in-plane field



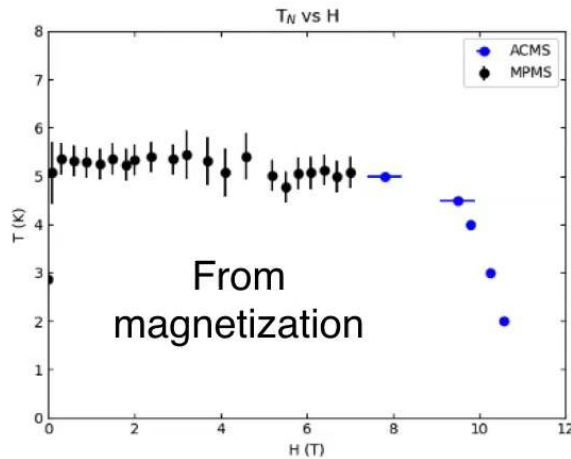
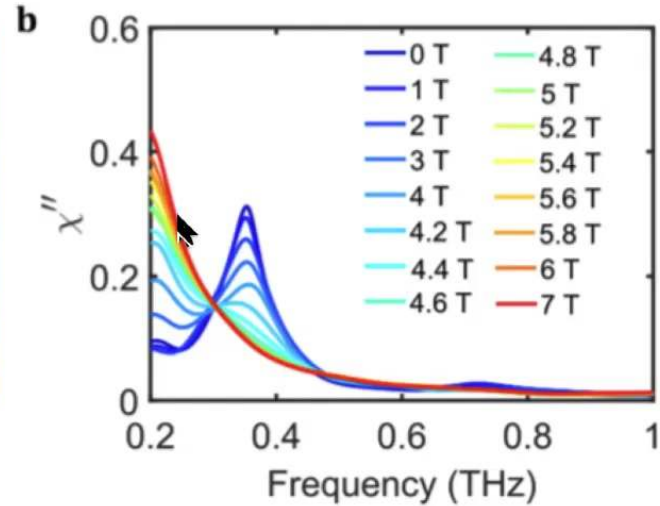
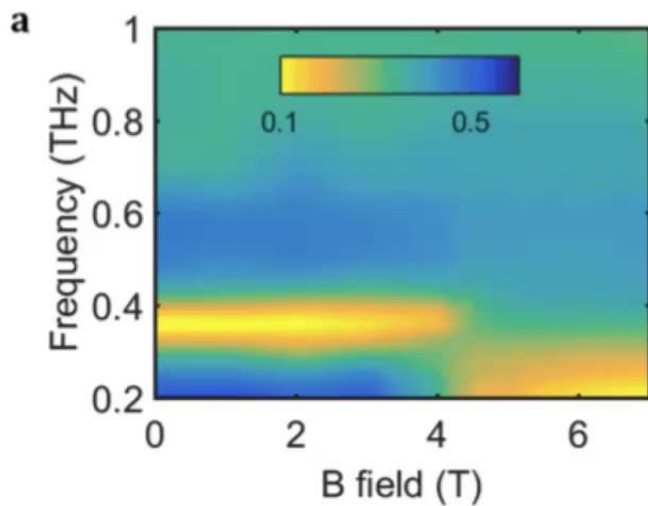


$$\mathcal{H}_1 = \sum_{\langle ij \rangle_\gamma} \left[K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j + \Gamma (S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha) + \Gamma' (S_i^\gamma S_j^\alpha + S_i^\alpha S_j^\gamma + S_i^\beta S_j^\gamma + S_i^\gamma S_j^\beta) \right]$$

$$\varepsilon_0^{(0)} = \sqrt{g\mu_B B (g\mu_B B + 3S(\Gamma + 2\Gamma'))}.$$

$$\Gamma_{\text{total}} = \Gamma + 2\Gamma = 0.32 \text{ meV}$$

THz spectra of BaCo₂(AsO₄)₂ with out-of-plane field



In-plane easy axis. Likely mixed field character to our THz data.

Recent results on Kitaev interactions in Co based magnets



CoNb_2O_6 , best material realization of “Ising’s model”

- THz experiments on CoNb_2O_6 in zero field; 9 “meson” bound states at low temperature.

- Ising chain in transverse magnetic field; simplest example of a quantum phase transition; **Kramers-Wannier duality**; **twisted Kitaev** chain

Quantum spin-liquid states in a more ideal **Kitaev** material:

$\text{BaCo}_2(\text{AsO}_4)_2$

- small J and Γ terms.

- out-of-plane field of a few T can induce a **QSL**.

Morris et al. PRL 2014

Steinberg, NPA, et al. PRB 2019

Morris et al. Nature Physics 2021

Zhang et al. arXiv 2106.13418.