

Title: Internally engineered Majorana modes in twisted bilayer graphene

Speakers: Jason Alicea

Series: Quantum Matter

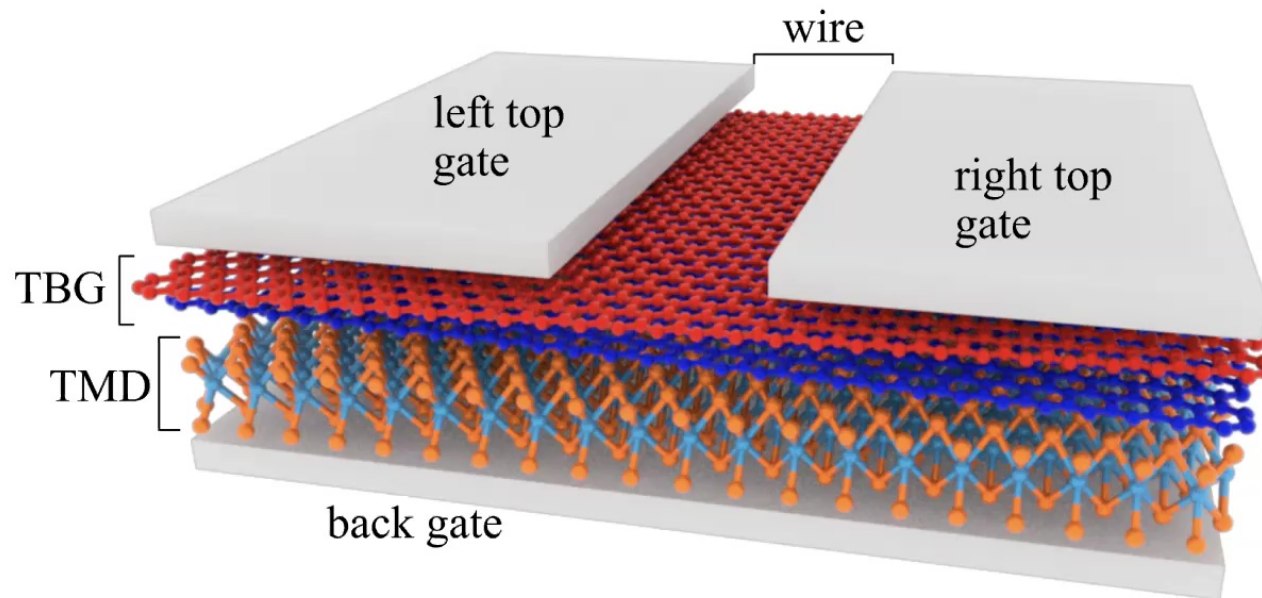
Date: September 27, 2021 - 12:00 PM

URL: <https://pirsa.org/21090017>

Abstract: Twisted bilayer graphene (TBG) realizes an exquisitely tunable, strongly interacting system featuring superconductivity and various correlated insulating states. In this talk I will introduce gate-defined wires in TBG as an enticing platform for Majorana-based fault-tolerant qubits. Our proposal notably relies on "internally" generated superconductivity in TBG - as opposed to "external" superconducting proximity effects commonly employed in Majorana devices - and may operate even at zero magnetic field. I will also describe how electrical measurements of gate-defined wires can reveal the nature of correlated insulators and shed light on the Cooper-pairing mechanism in TBG.

Zoom Link: https://pitp.zoom.us/meeting/register/tJcqc-ihqzMvHdW-YBm7mYd_XP9Amhypv5vO

Internally engineered Majorana modes in twisted bilayer graphene



Jason Alicea

Caltech, IQIM, & Walter Burke Institute



Acknowledgments



Alex Thomson



Ina Sorensen



Stevan Nadj-Perge



Gate-defined wires in twisted bilayer graphene: from electrical detection of inter-valley coherence to internally engineered Majorana modes

Alex Thomson,^{1,2,3,*} Ina Sorensen,^{1,2,*} Stevan Nadj-Perge,^{2,4} and Jason Alicea^{1,2,3}

arXiv:2105.02891



Topological quantum computation overview



Non-Abelian anyons



Anyons carry exotic
zero-energy modes

Locally
indistinguishable
ground states



**Inherently fault-
tolerant qubits!**



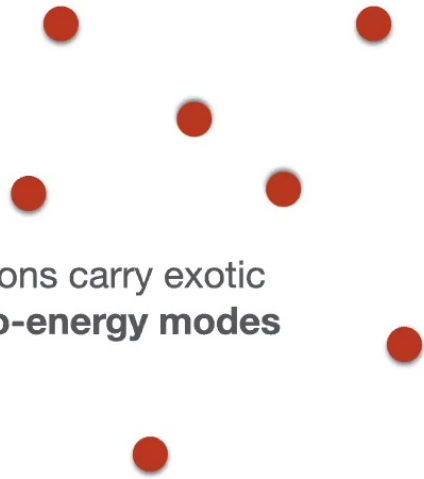
$|000\rangle, |001\rangle, \dots$



Alexei Kitaev



Non-Abelian anyons



Anyons carry exotic
zero-energy modes



Alexei Kitaev

Locally
indistinguishable
ground states



**Inherently fault-
tolerant qubits!**



$|000\rangle, |001\rangle, \dots$

Non-Abelian
statistics

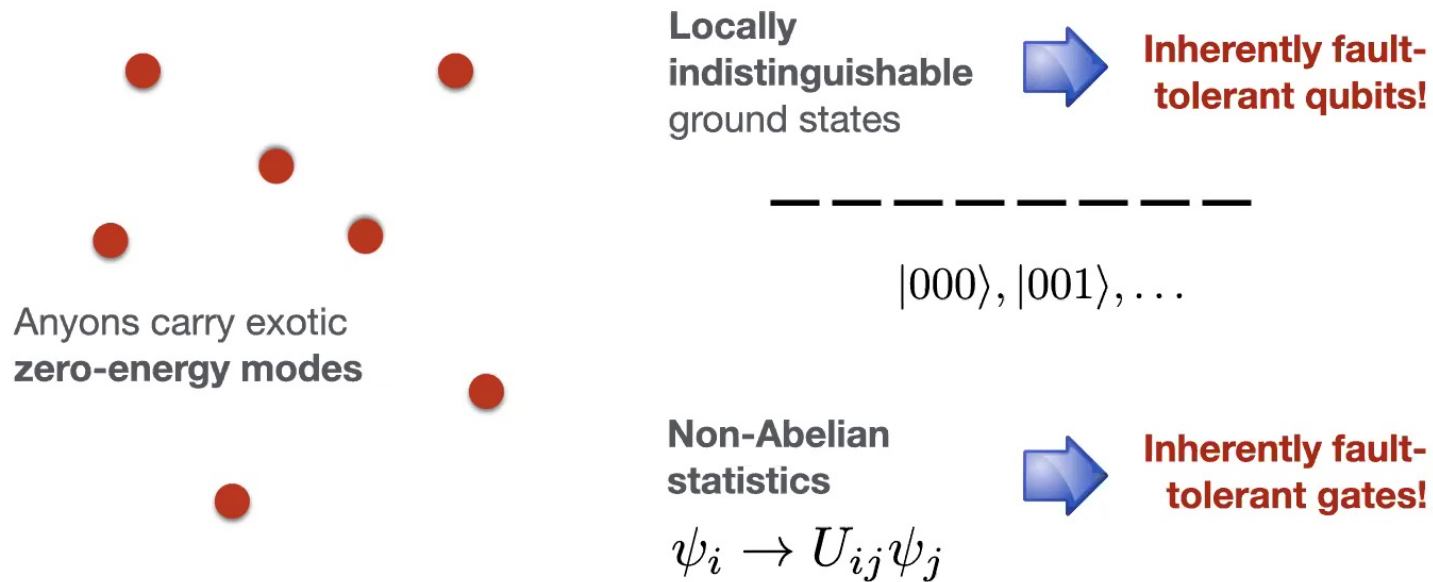
$$\psi_i \rightarrow U_{ij} \psi_j$$



**Inherently fault-
tolerant gates!**



Non-Abelian anyons



Alexei Kitaev

How to build the hardware?



Spinless 1D superconductors



$$\gamma = \gamma^\dagger \quad \gamma^2 = 1 \quad \{\gamma_1, \gamma_2\} = 0 \quad [\gamma, H] = 0$$

$$f = (\gamma_1 + i\gamma_2)/2$$

— —
|even⟩ |odd⟩

**Locally
indistinguishable
ground states**



Spinless 1D superconductors



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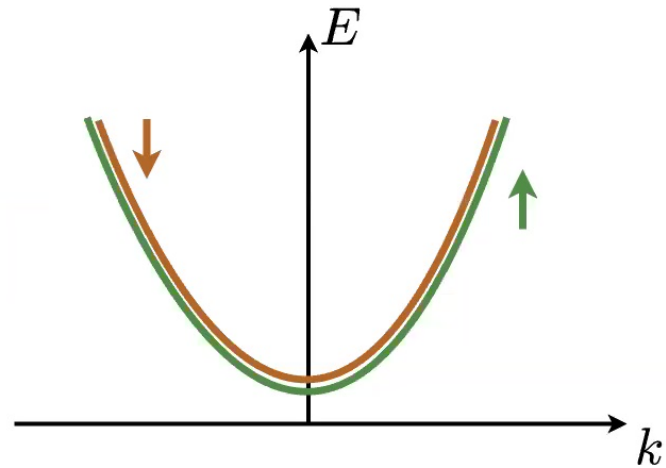
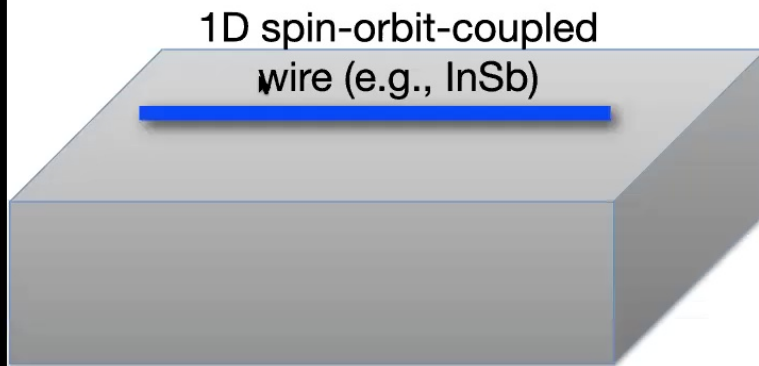
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**Locally
indistinguishable
ground states**

But...electrons carry spin, and nearly superconductors
display **spin-singlet** Cooper pairing

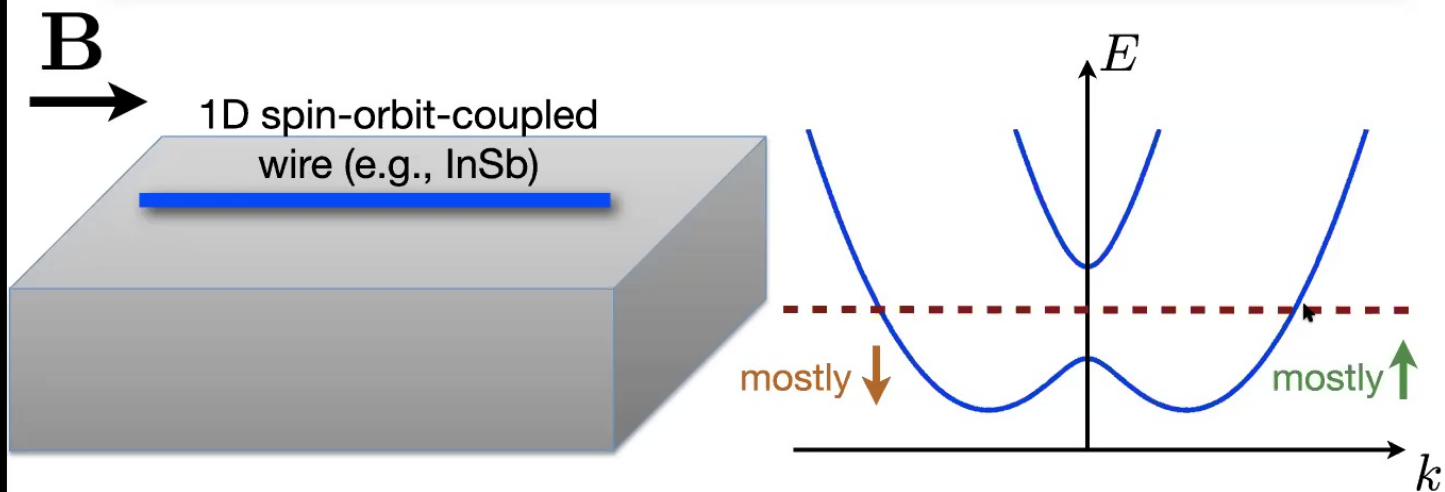


Engineered Majorana platforms



Lutchyn, Sau, Das Sarma PRL 2010; Oreg, Refael, von Oppen PRL 2010

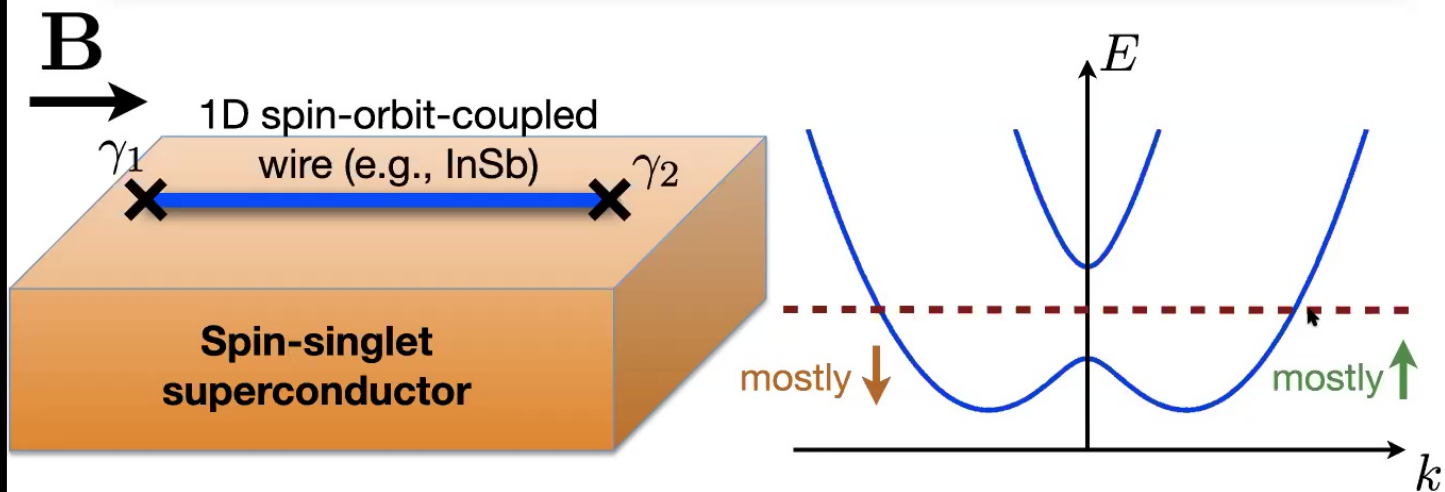
Engineered Majorana platforms



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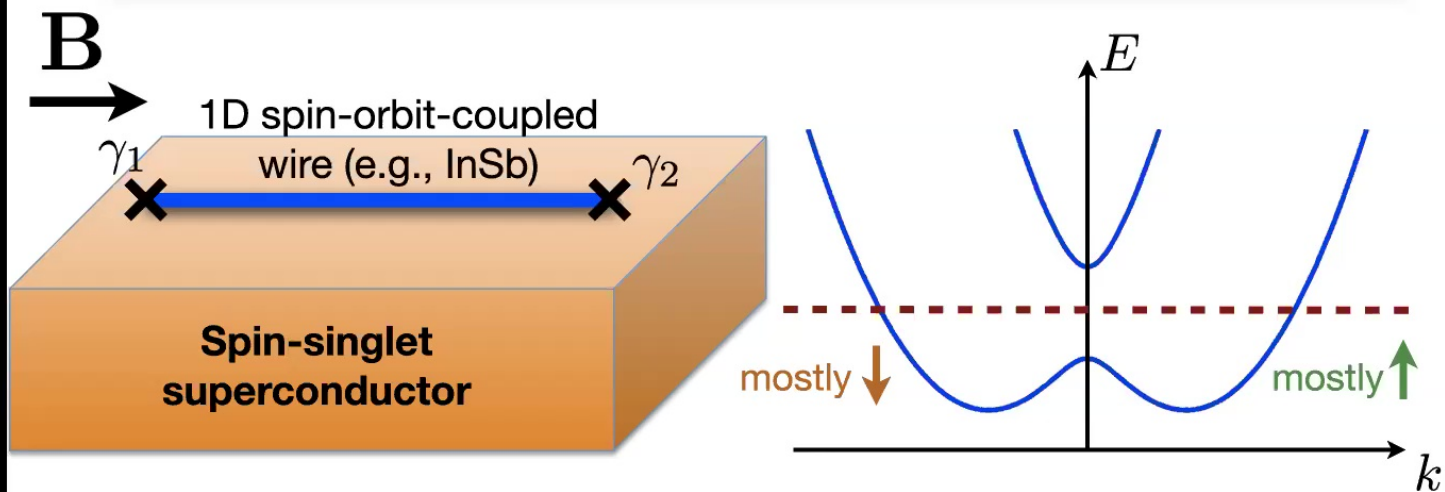
Engineered Majorana platforms



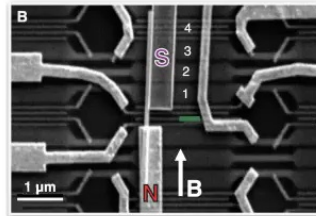
Lutchyn, Sau, Das Sarma PRL 2010; Oreg, Refael, von Oppen PRL 2010



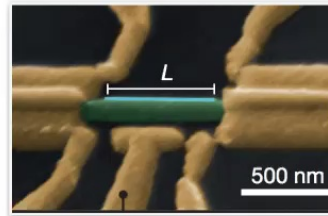
Engineered Majorana platforms



Many experiments followed...



Mourik et al. Science **336**, 1003 (2012)



Albrecht et al. Nature **531**, 206 (2016)

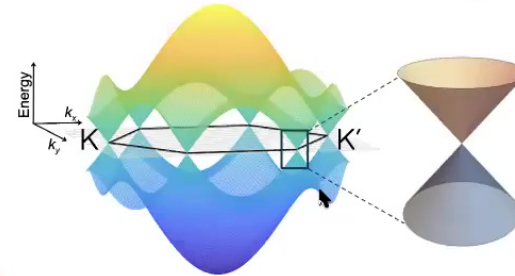
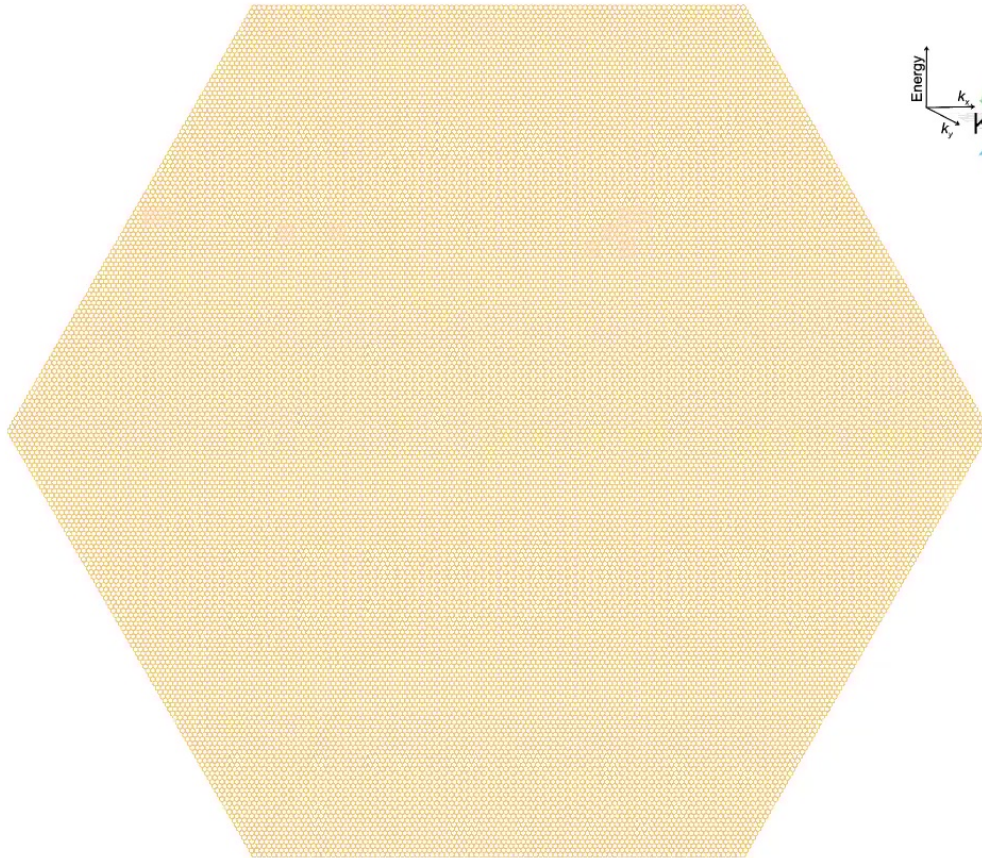
...but Majorana debate continues

Lutchyn, Sau, Das Sarma PRL 2010; Oreg, Refael, von Oppen PRL 2010

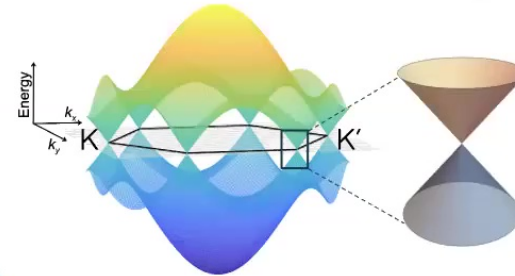
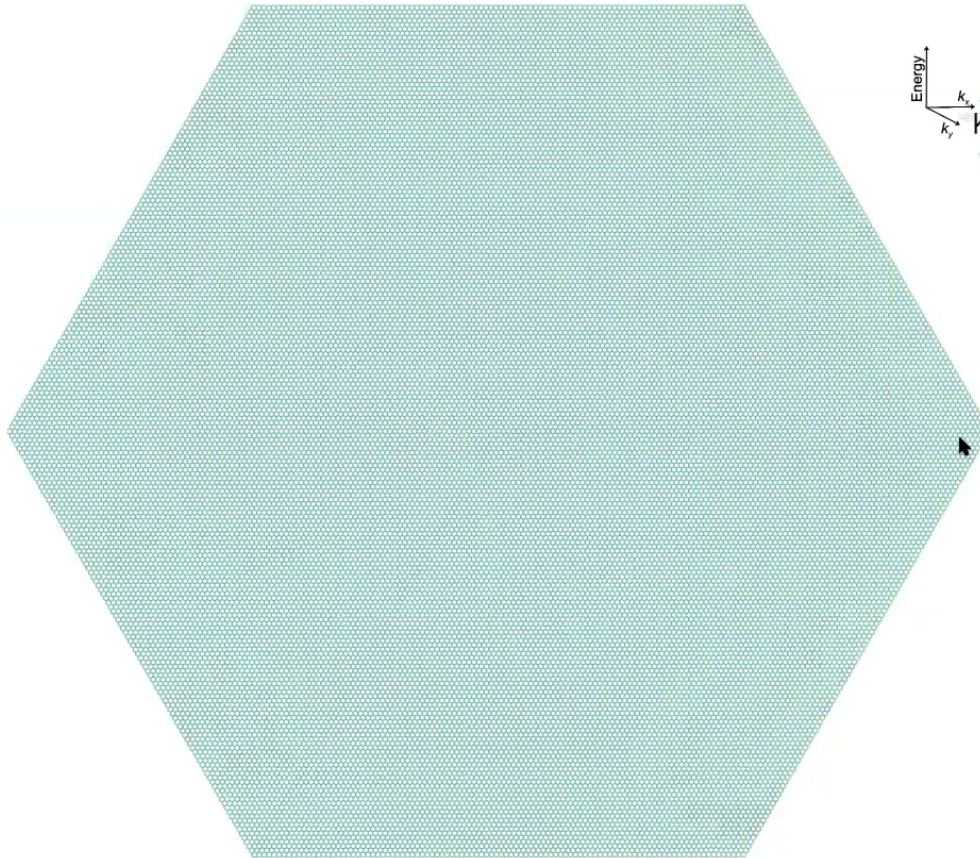
Twisted bilayer graphene



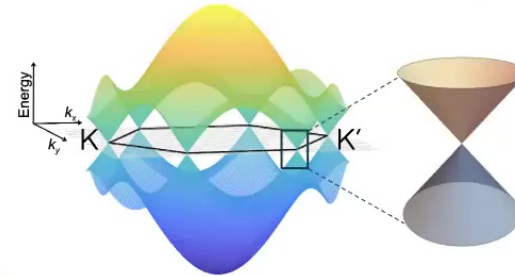
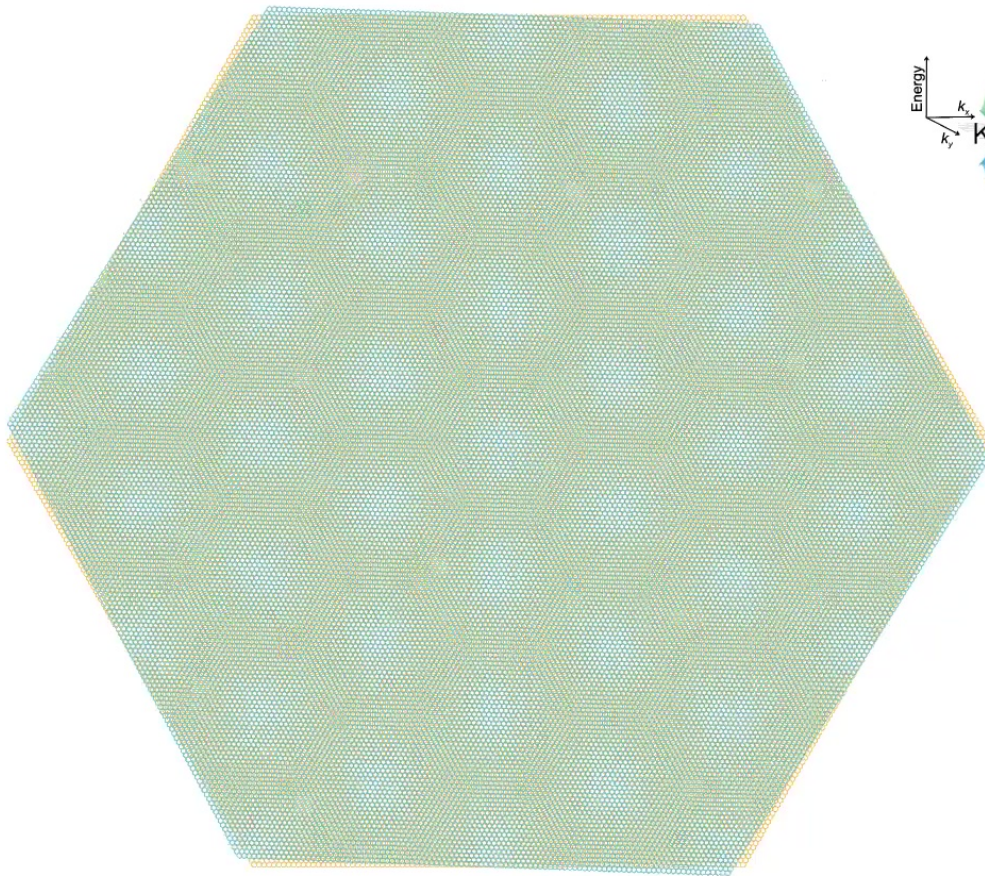
Twisted bilayer graphene



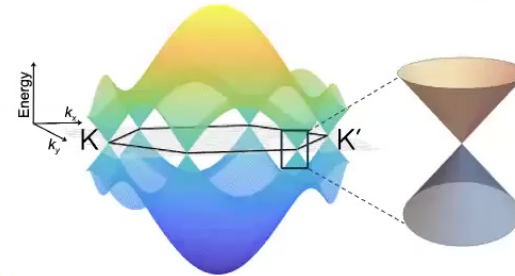
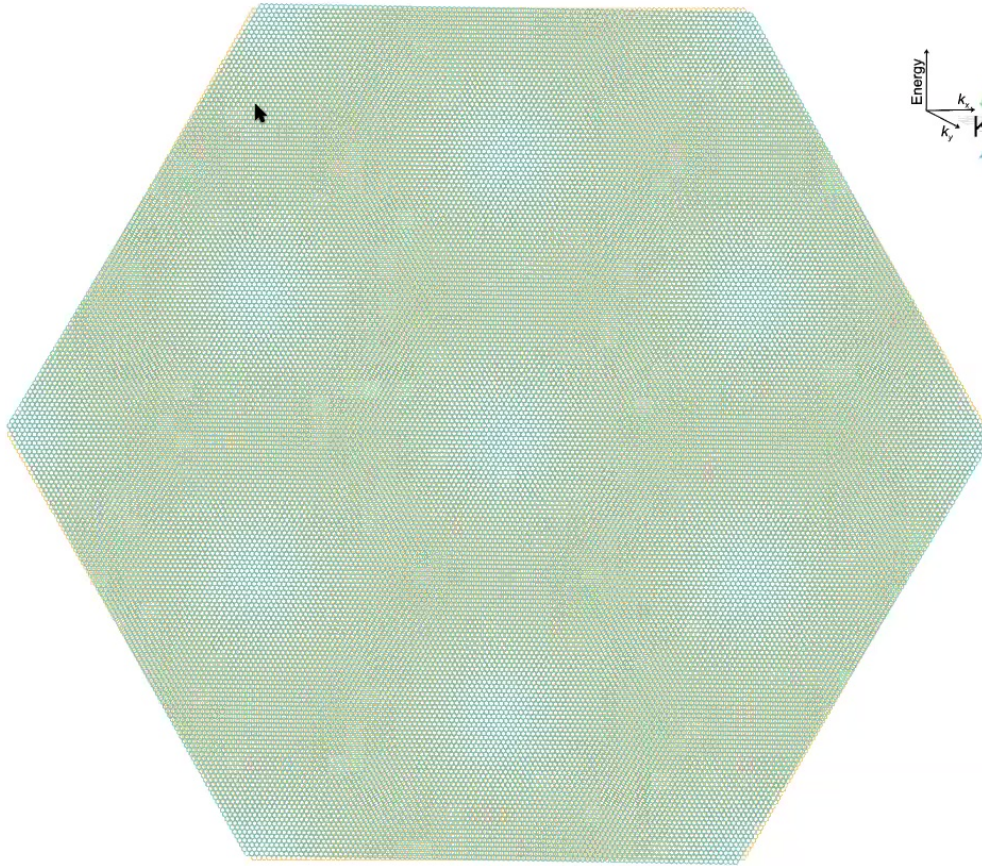
Twisted bilayer graphene



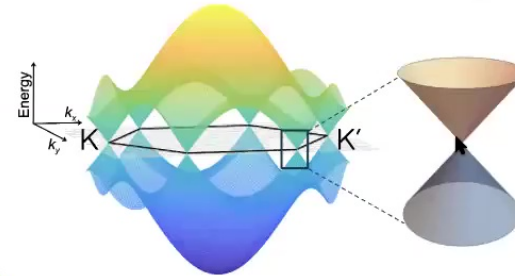
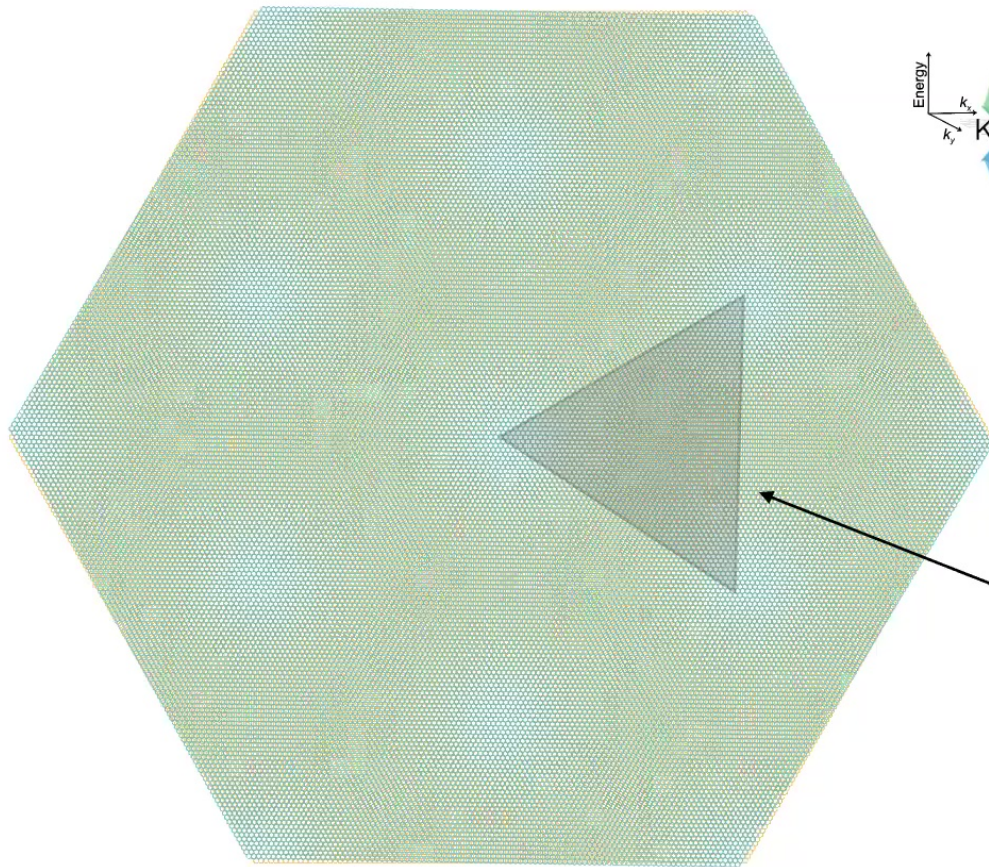
Twisted bilayer graphene



Twisted bilayer graphene



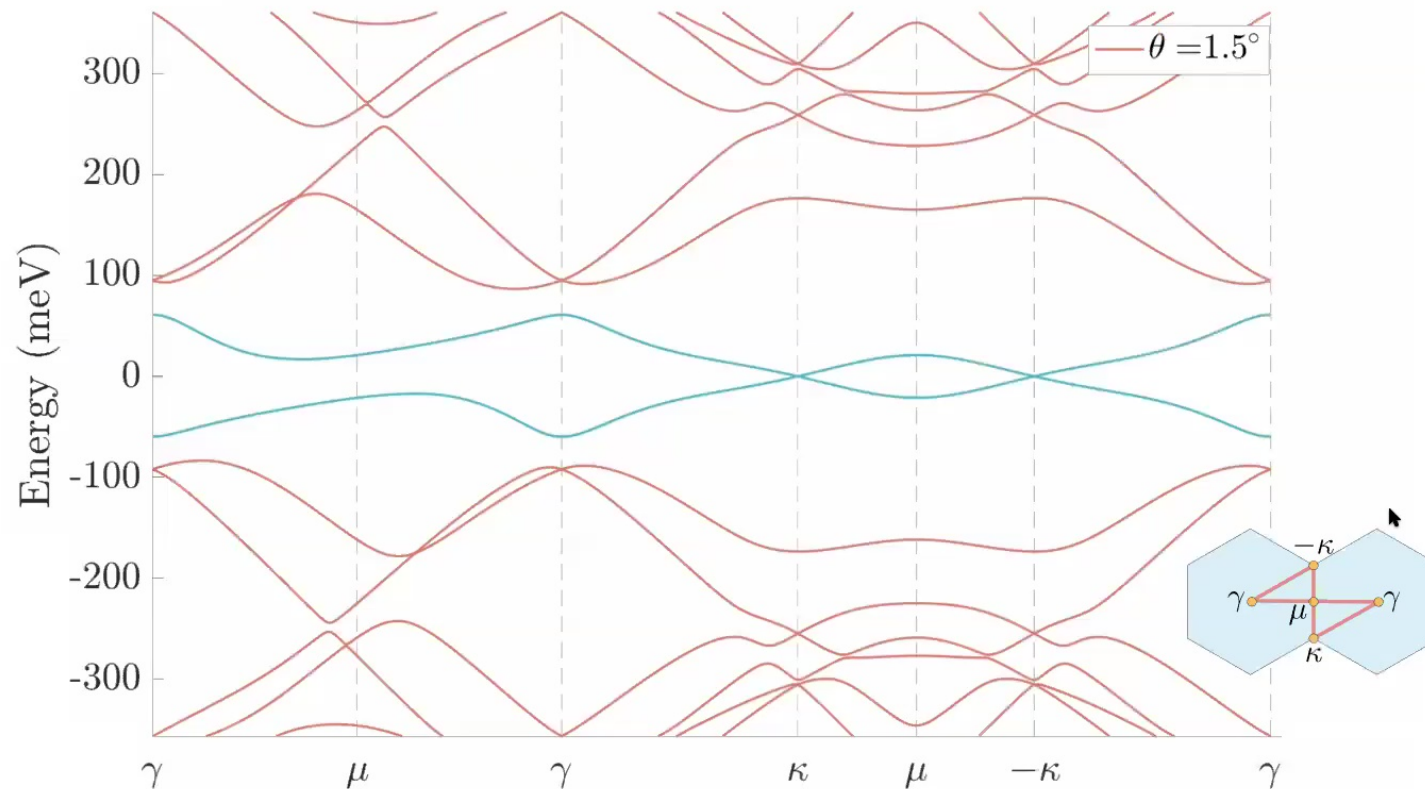
Twisted bilayer graphene



Moire unit cell for
1 degree twist angle.
~10nm in size with
1000's of atoms!



“Magic angle” band structure

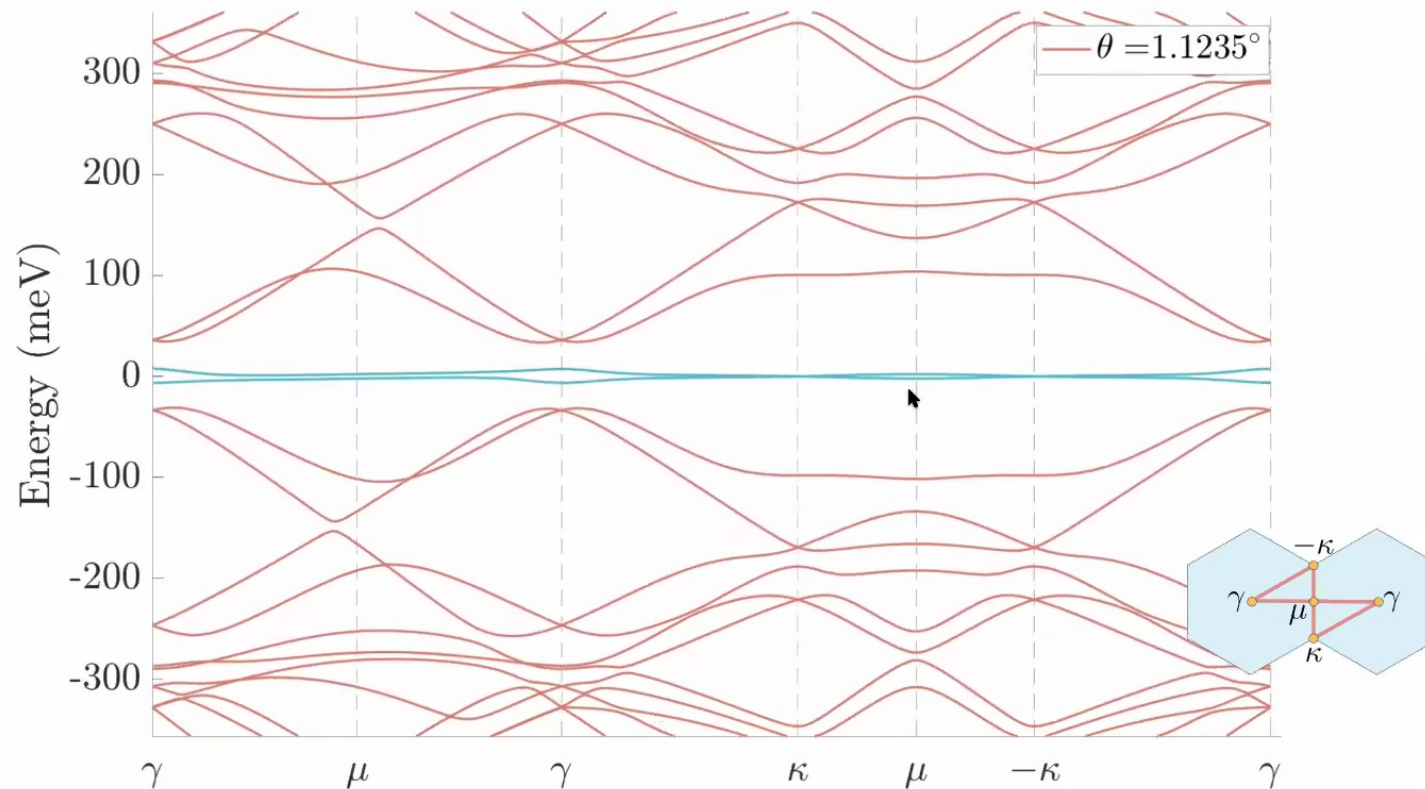


Bistritzer & MacDonald PNAS (2011)

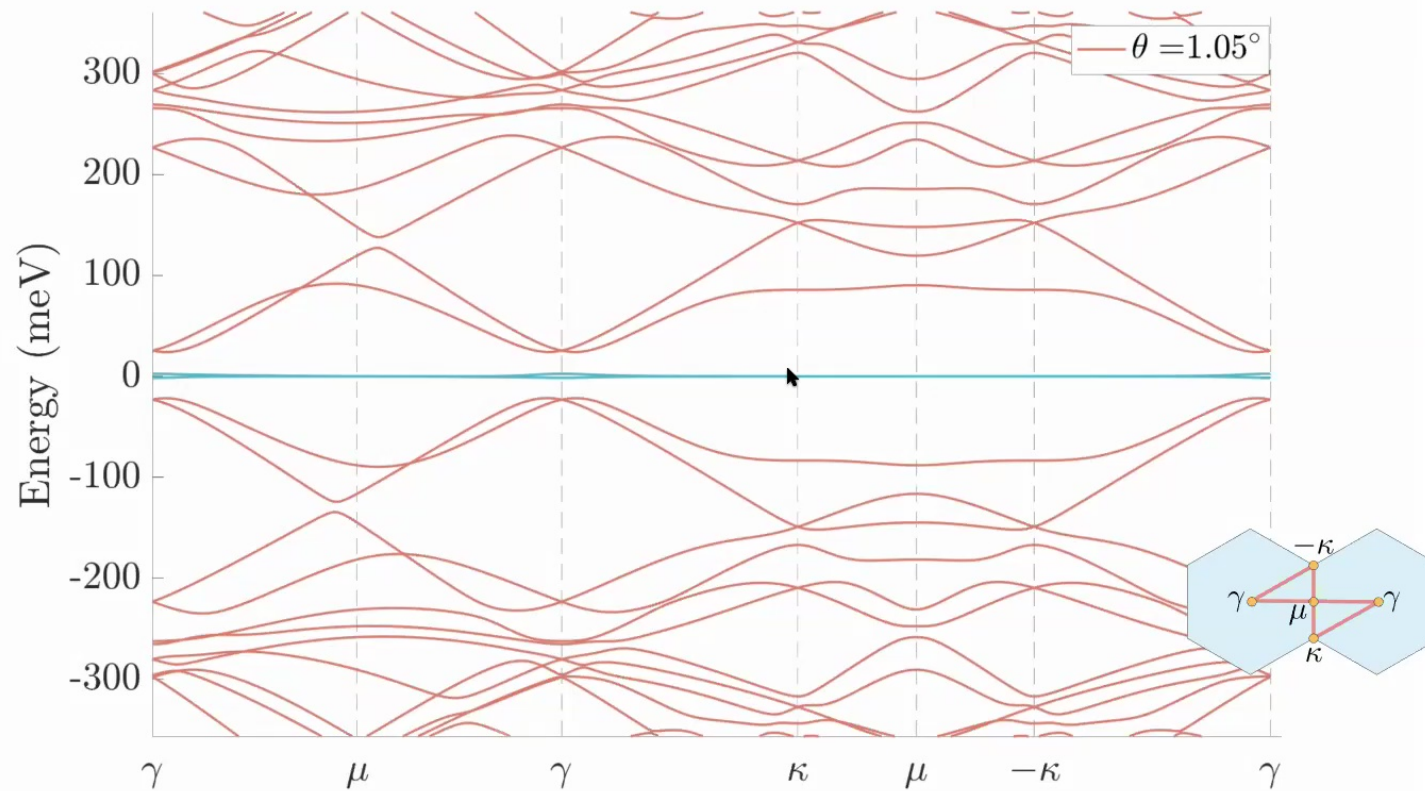
Band structures/movie courtesy of Alex Thomson.



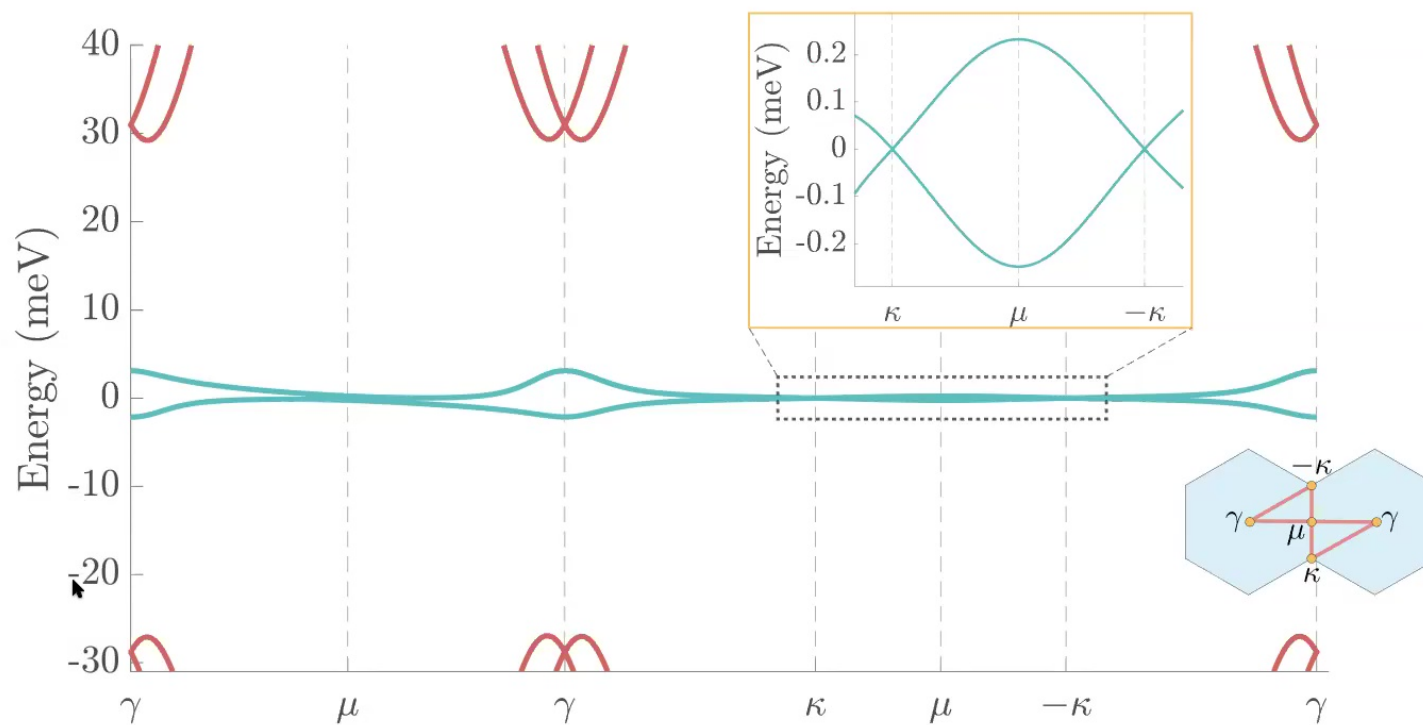
“Magic angle” band structure



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“Magic angle” band structure

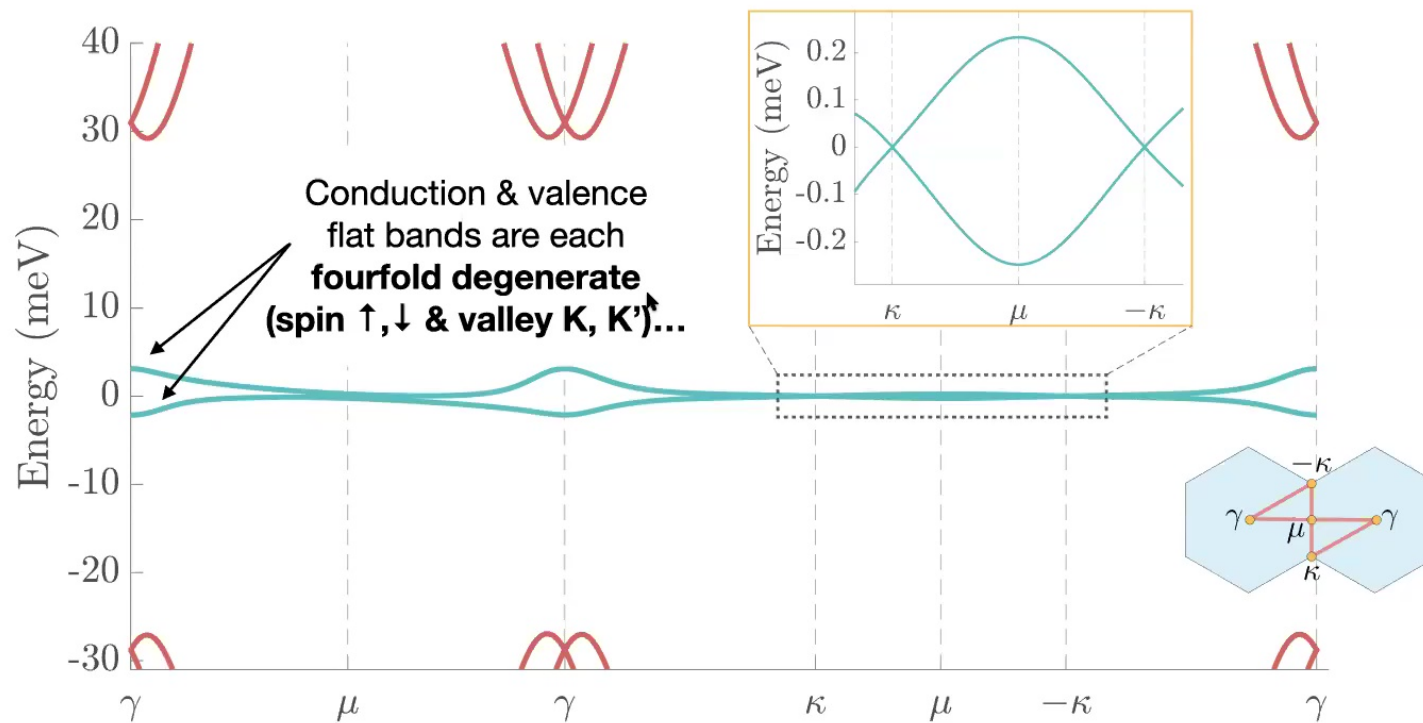


Bistritzer & MacDonald PNAS (2011)

Band structures/movie courtesy of Alex Thomson.



“Magic angle” band structure

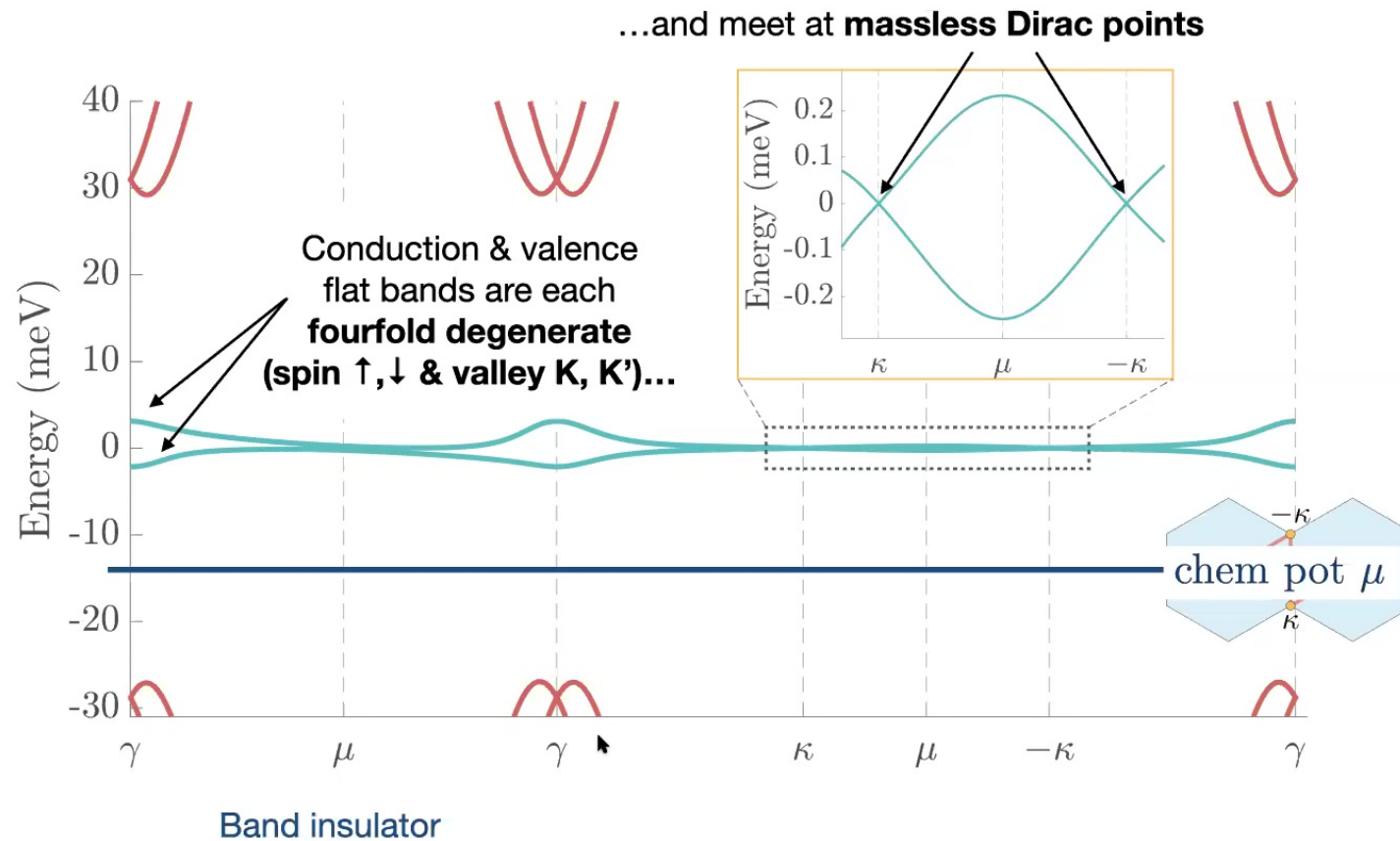


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“Magic angle” band structure

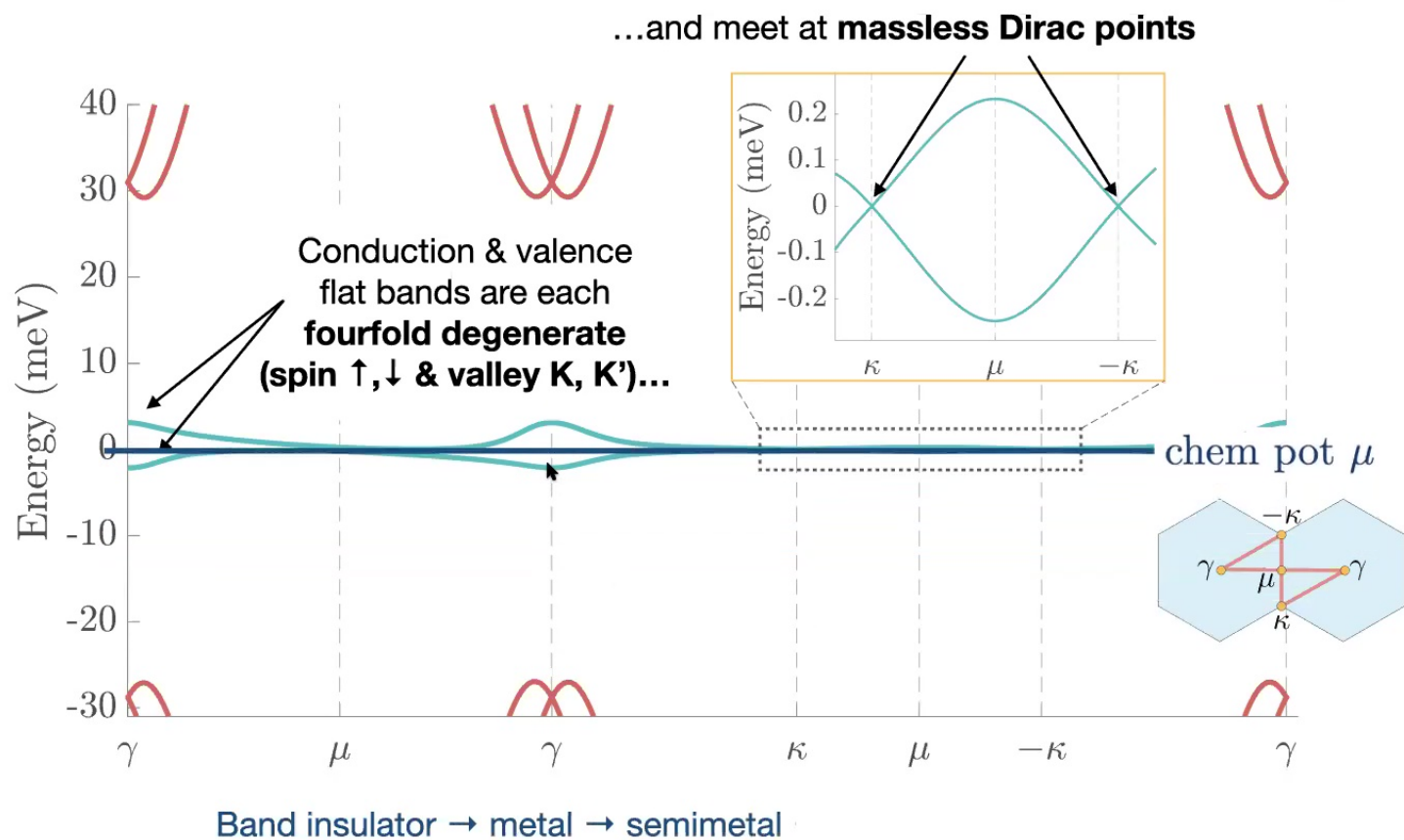


Bistritzer & MacDonald PNAS (2011)

Band structures/movie courtesy of Alex Thomson.

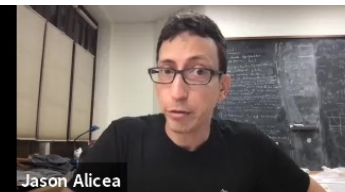


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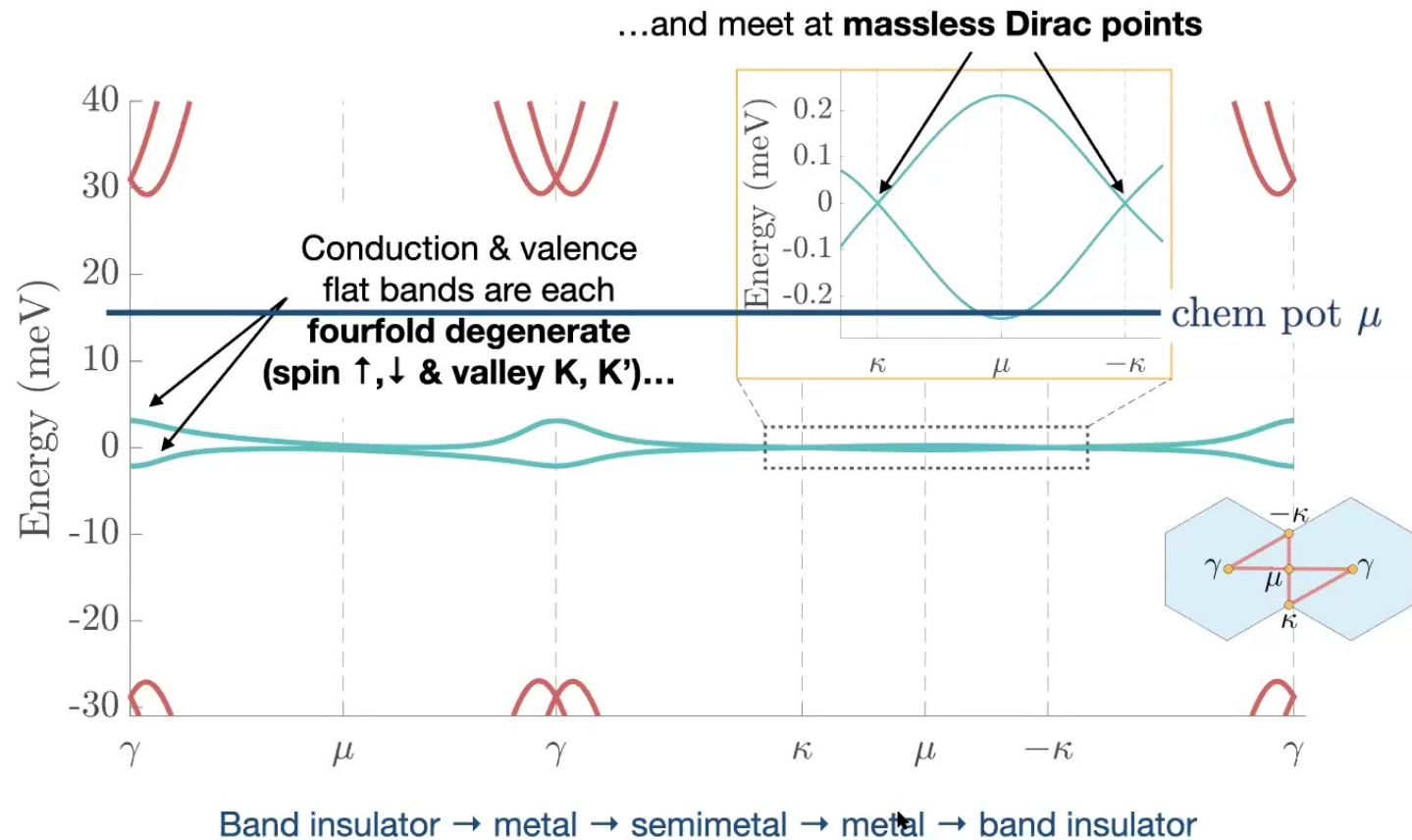


Bistritzer & MacDonald PNAS (2011)

Band structures/movie courtesy of Alex Thomson.



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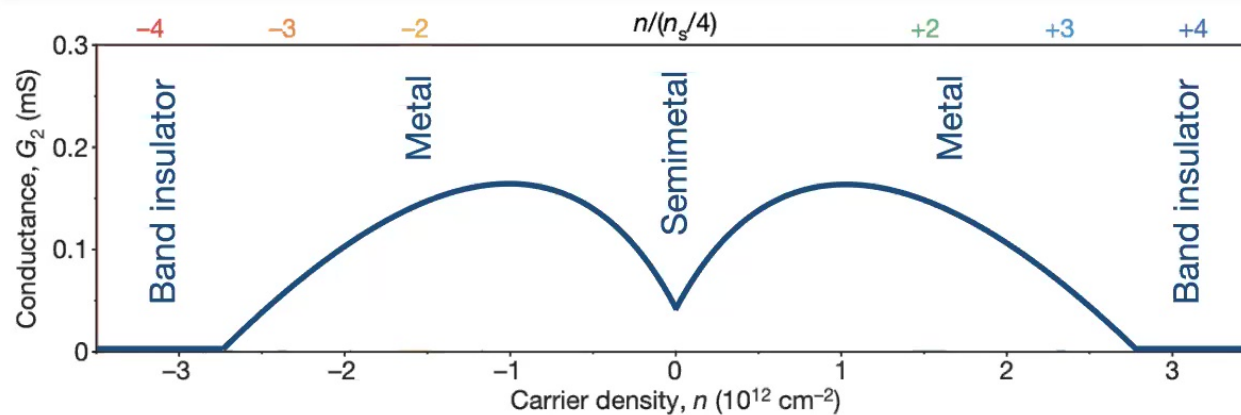


Bistritzer & MacDonald PNAS (2011)

Band structures/movie courtesy of Alex Thomson.

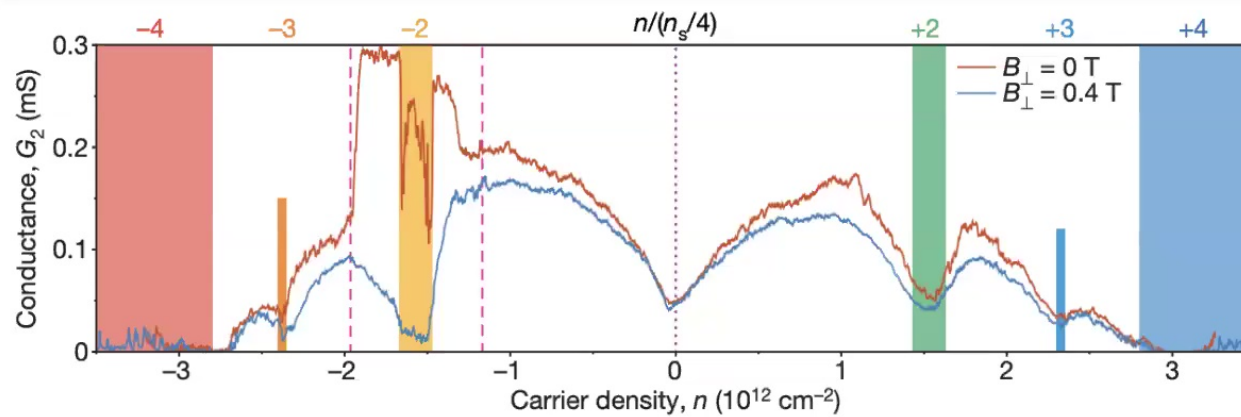


Magic-angle TBG experiments



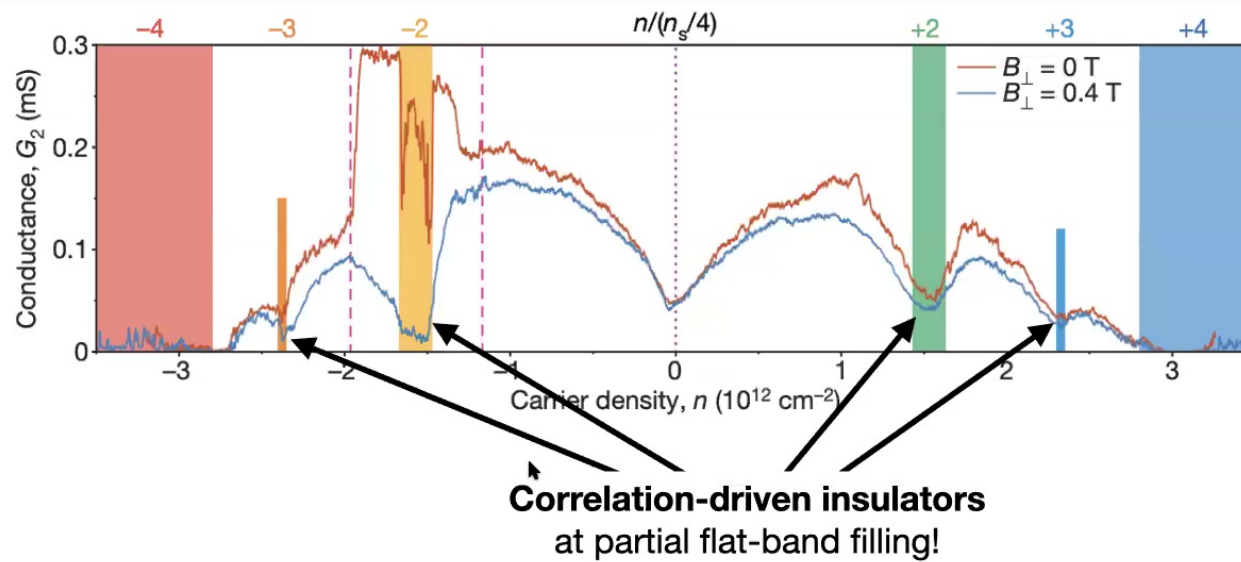
Cao et al., Nature (2018)

Magic-angle TBG experiments



Cao et al., Nature (2018)

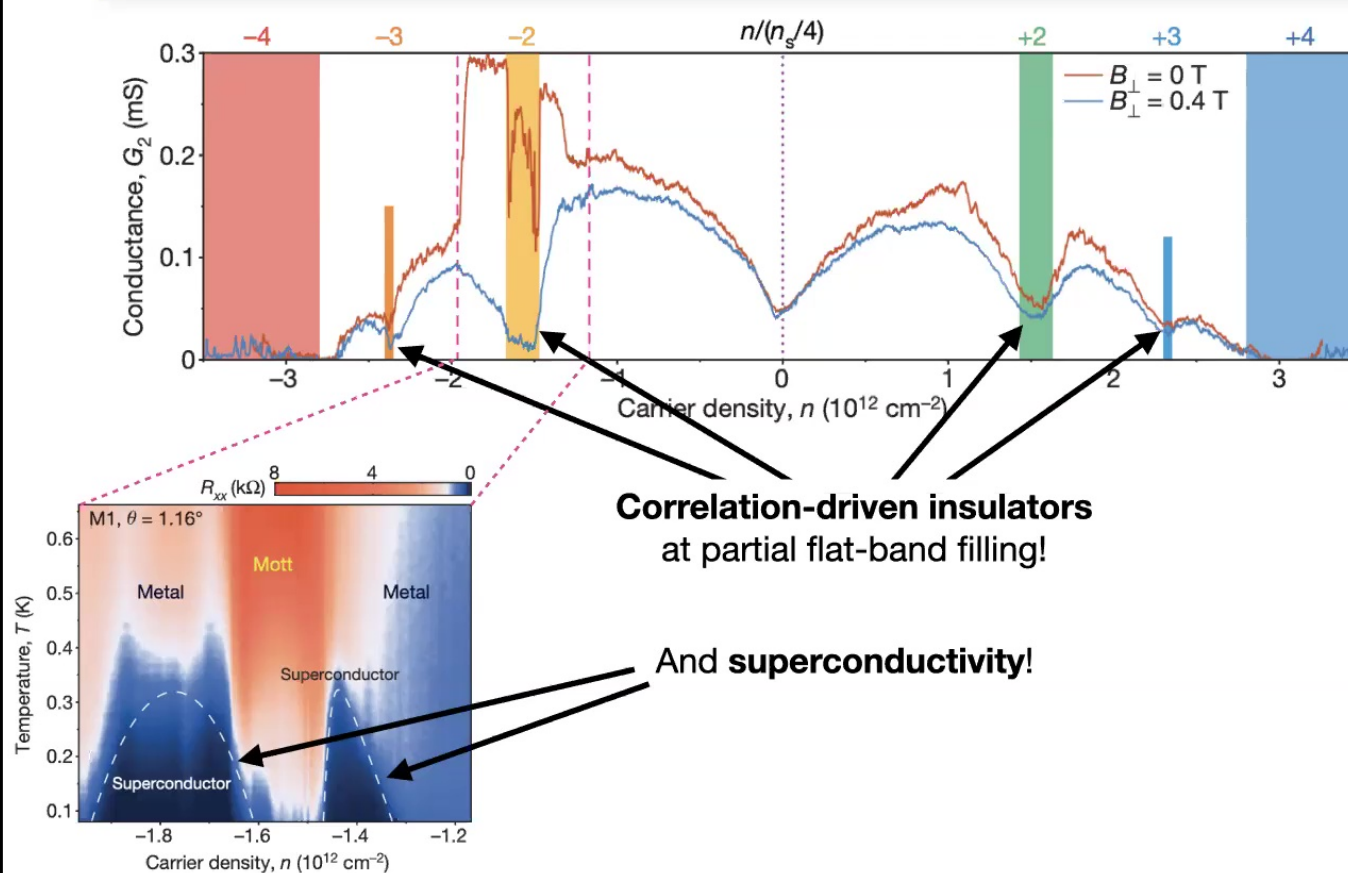
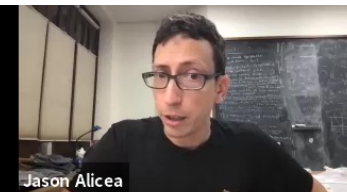
Magic-angle TBG experiments



Cao et al., Nature (2018)

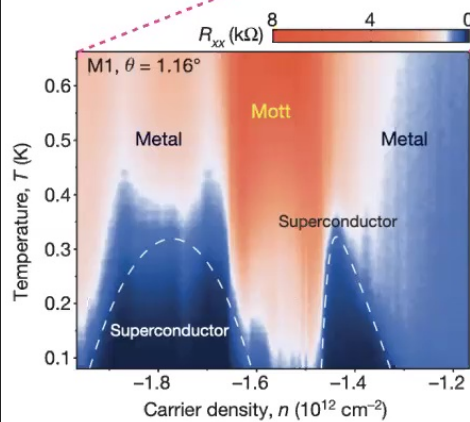
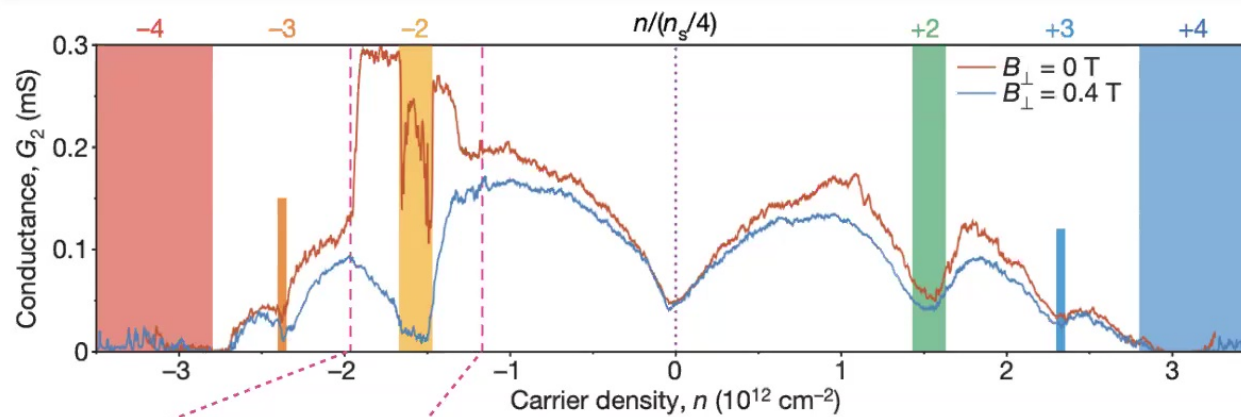


Magic-angle TBG experiments

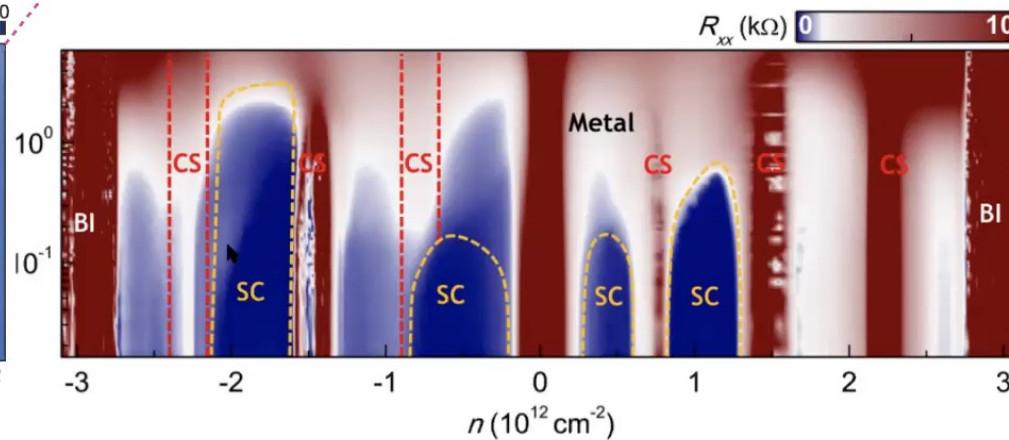


Cao et al., Nature (2018)

Magic-angle TBG experiments

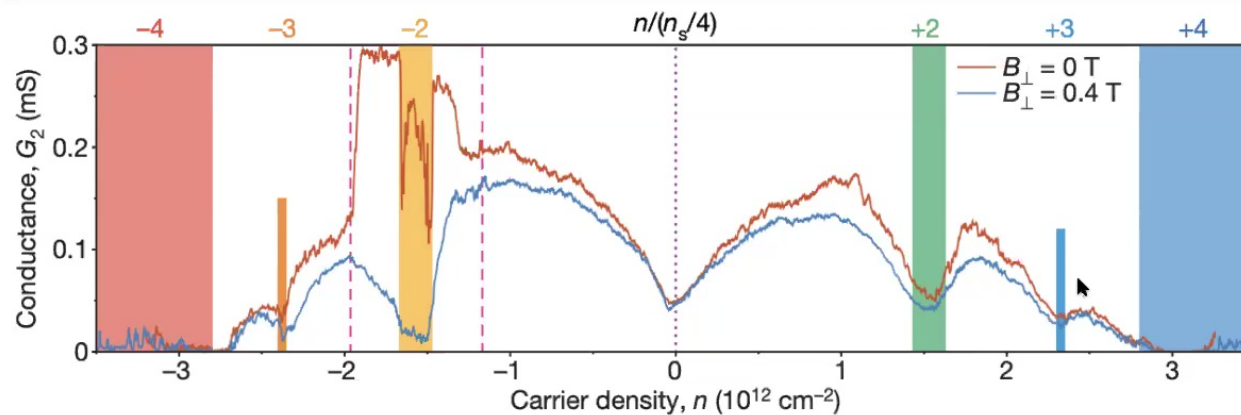


Cao et al., Nature (2018)



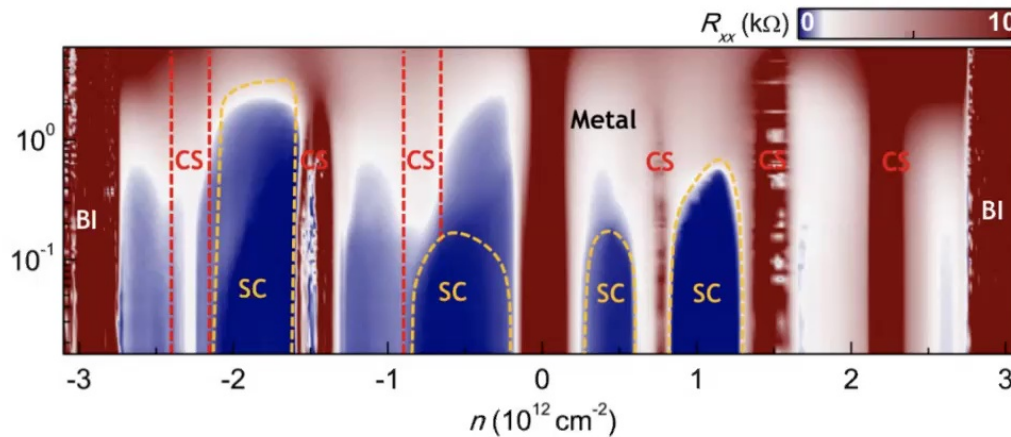
Lu et al., Nature (2019)

Magic-angle TBG experiments



Can readily gate tune
between band insulators,
metals, various correlated
insulators & superconductors!

Can we exploit this richness
& tunability for novel quantum
devices, e.g., Majorana zero
mode platforms?

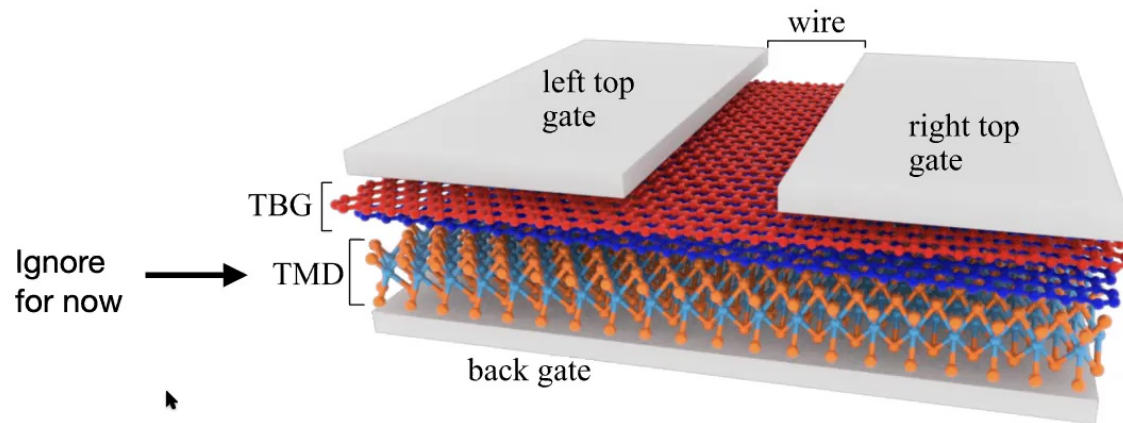


Cao et al., Nature (2018)

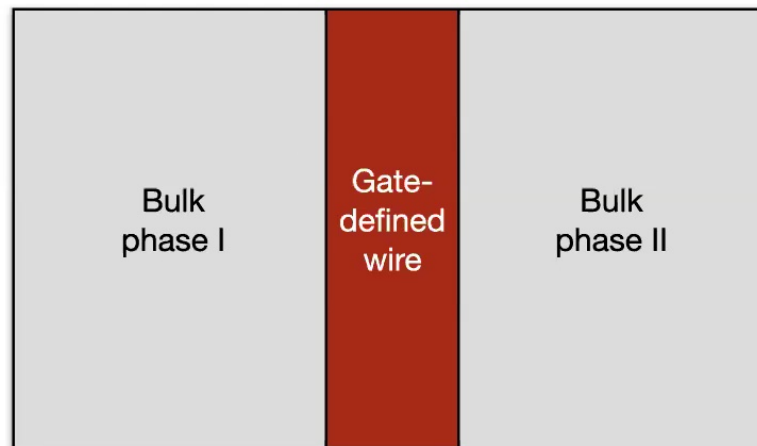
Lu et al., Nature (2019)



The big picture

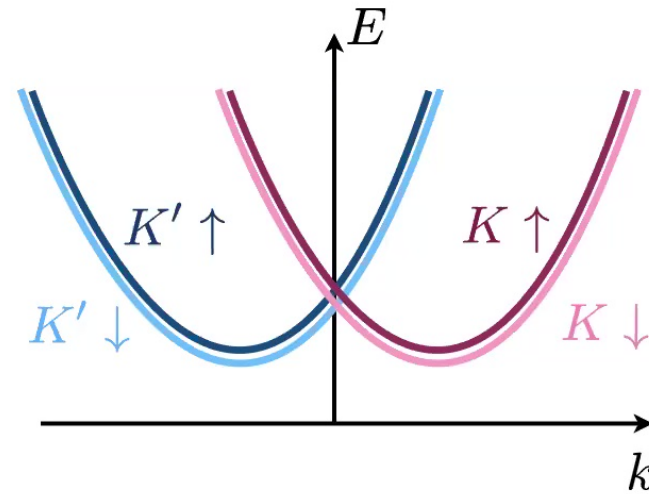
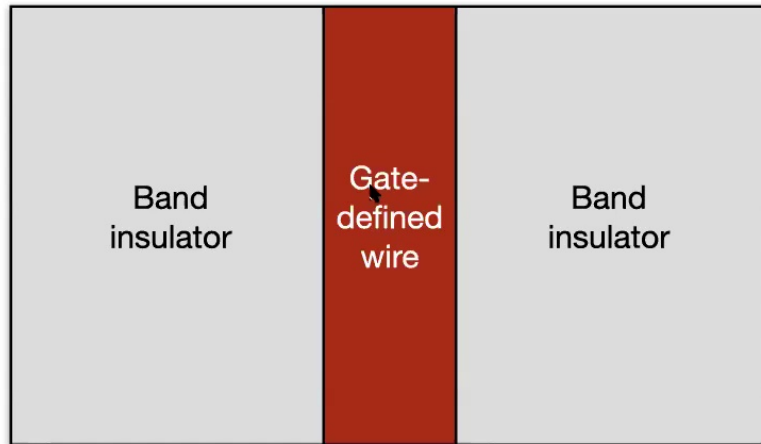


Wire inherits properties of adjacent bulk phases via **“internal” proximity effects**

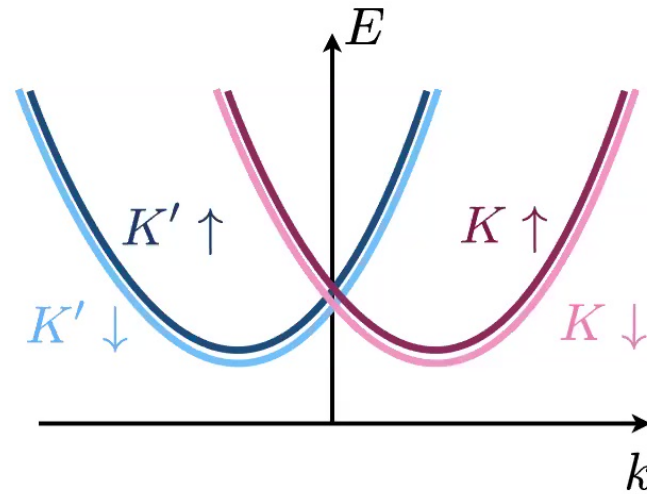
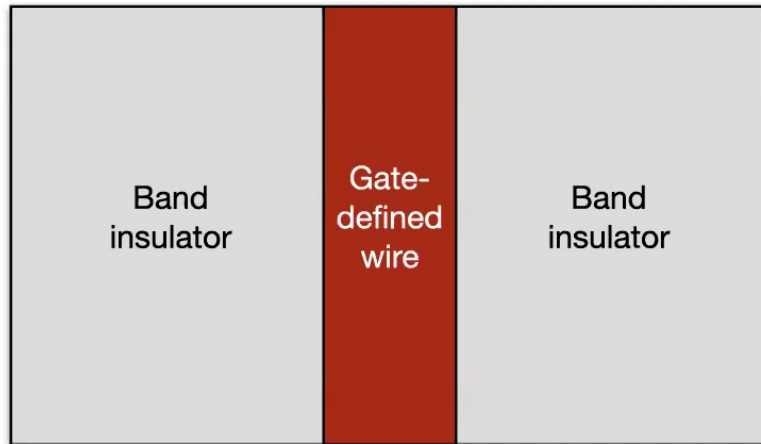


Will exploit for **electrical probes of symmetry-breaking order** and **Majorana engineering**

Trivial wire



Trivial wire



Challenge for Majorana engineering:
“Spinless” regime requires removing spin **and** valley degeneracy



Superconductivity in metallic twisted bilayer graphene stabilized by WSe₂

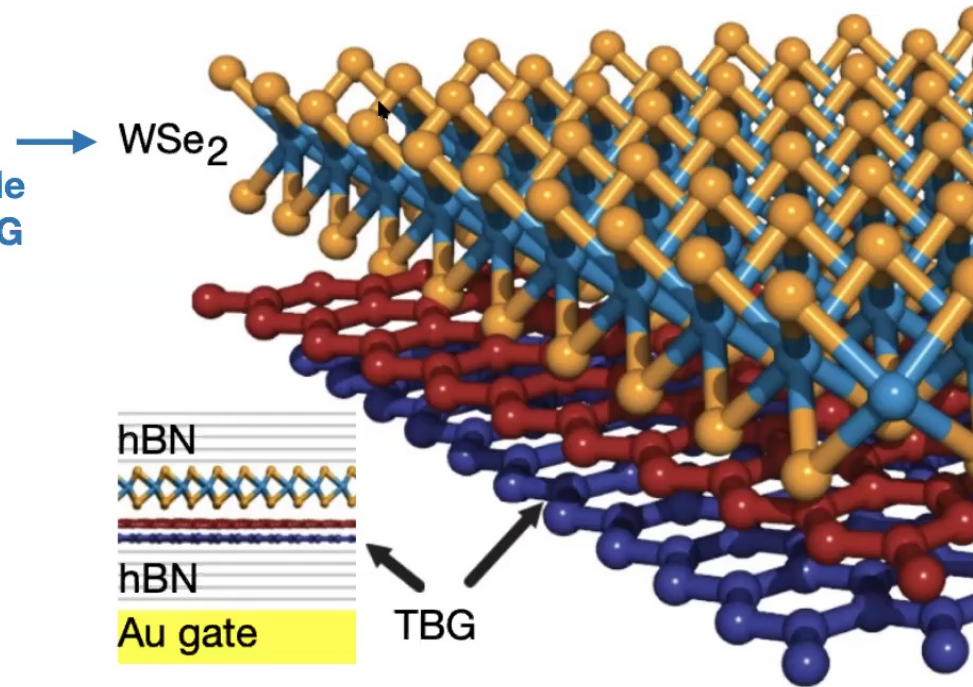
<https://doi.org/10.1038/s41586-020-2473-8>

Received: 31 January 2020

Accepted: 21 May 2020

Harpreet Singh Arora^{1,2,8}, Robert Polski^{1,2,8}, Yiran Zhang^{1,2,3,8}, Alex Thomson^{2,3,4},
Youngjoon Choi^{1,2,3}, Hyunjin Kim^{1,2,3}, Zhong Lin⁵, Ilham Zaky Wilson⁵, Xiaodong Xu^{5,6},
Jiun-Haw Chu⁵, Kenji Watanabe⁷, Takashi Taniguchi⁷, Jason Alicea^{2,3,4} & Stevan Nadj-Perge^{1,2}✉

Consistent with previous studies, **imparts meV-scale spin-orbit coupling to TBG** (Landau level spectrum, weak anti-localization)



Superconductivity in metallic twisted bilayer graphene stabilized by WSe₂

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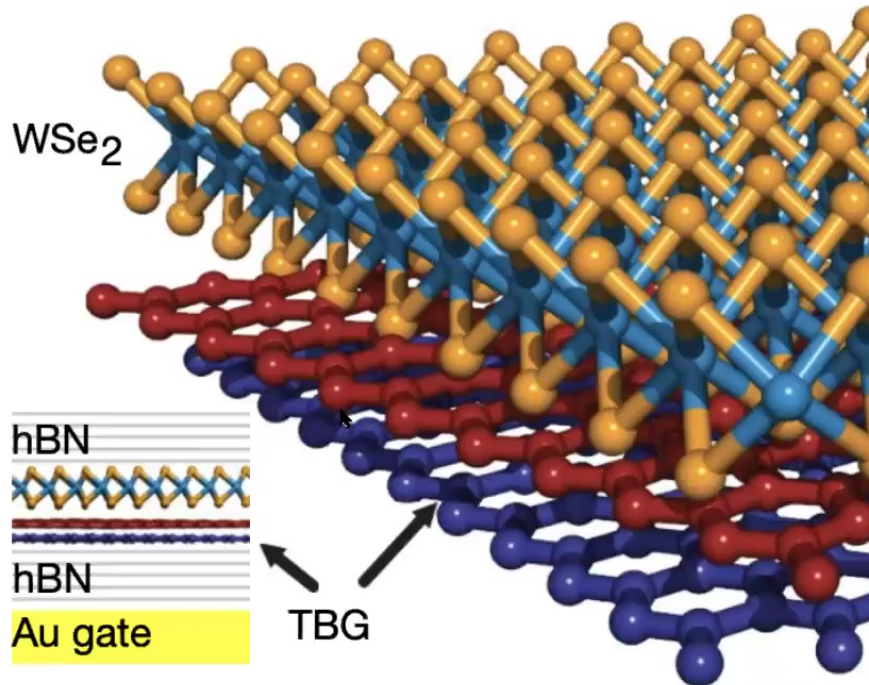
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Consistent with previous studies, **imparts meV-scale spin-orbit coupling to TBG** (Landau level spectrum, weak anti-localization)

But does the rich phase diagram of “pure” TBG persist?

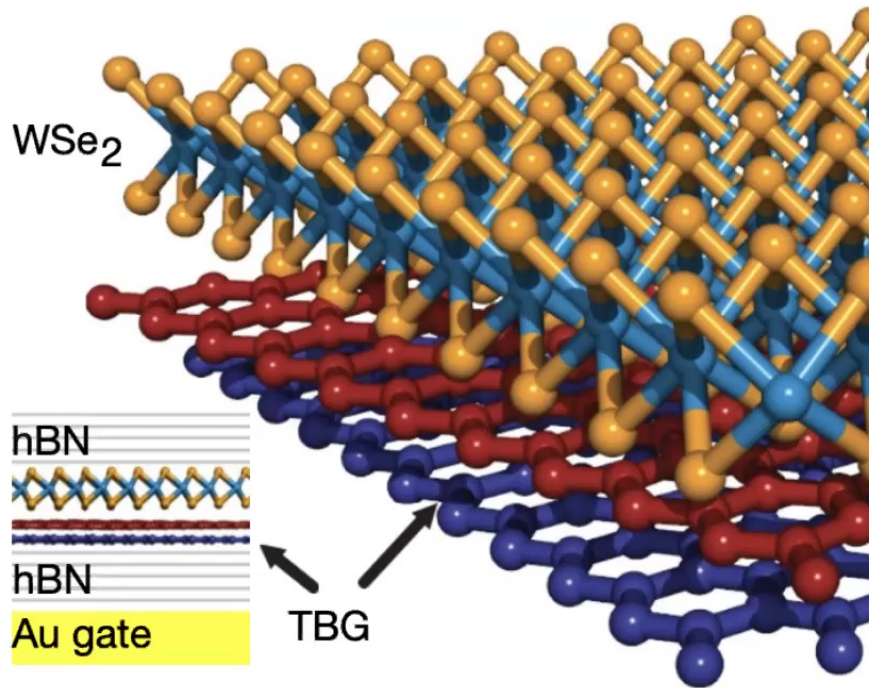
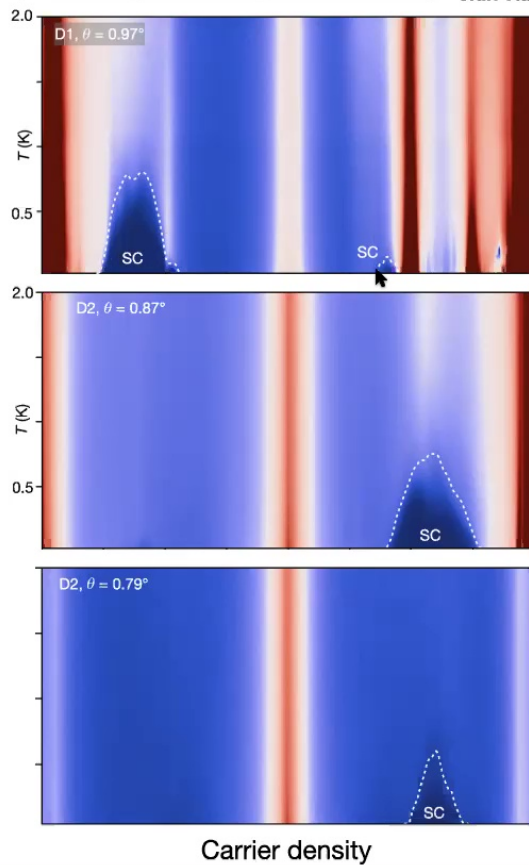


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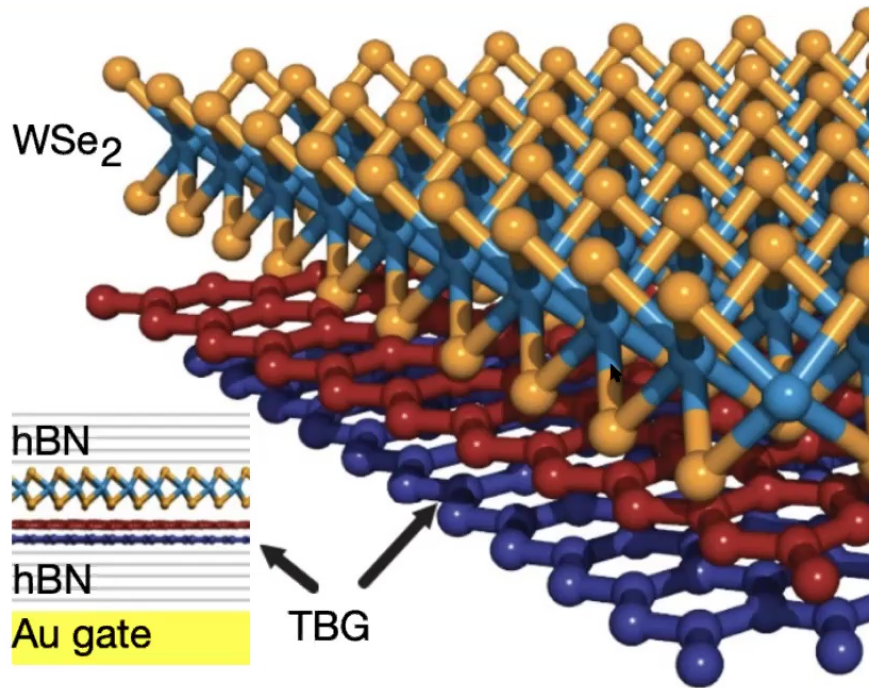
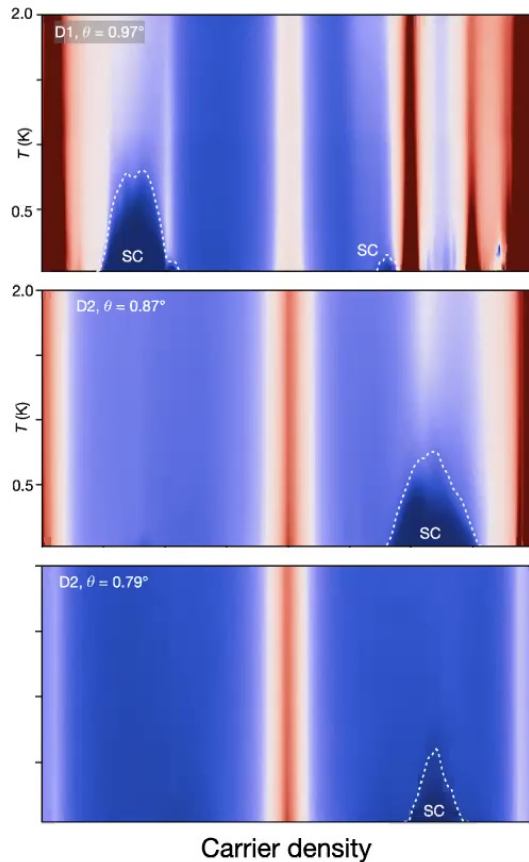


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TBG superconductivity not only survives but **thrives** with spin-orbit coupling!

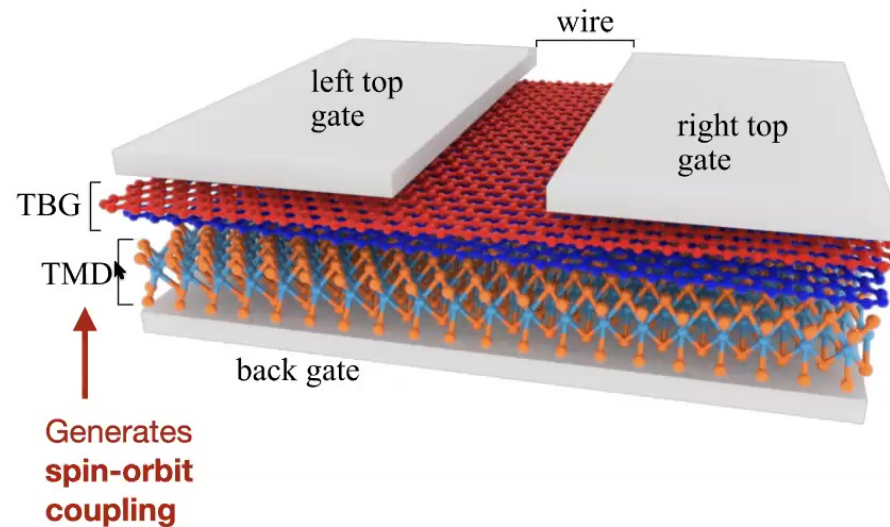
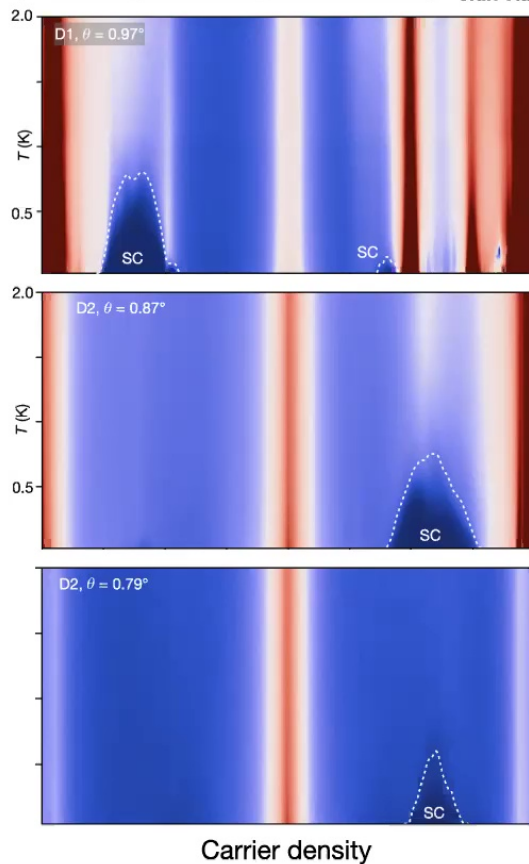


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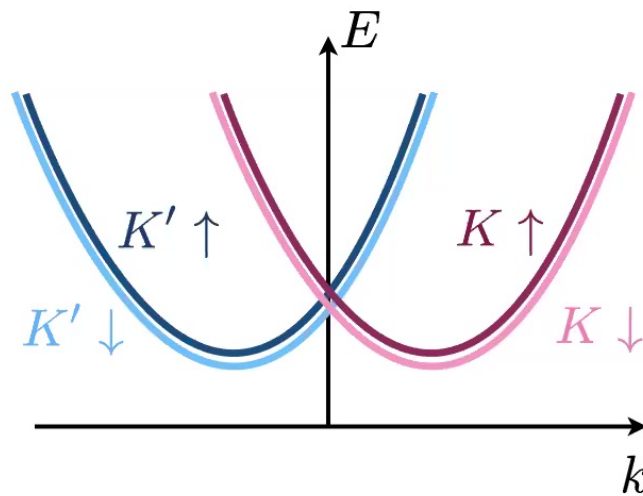
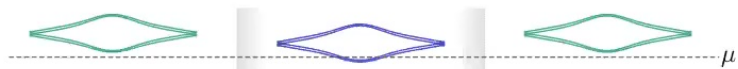
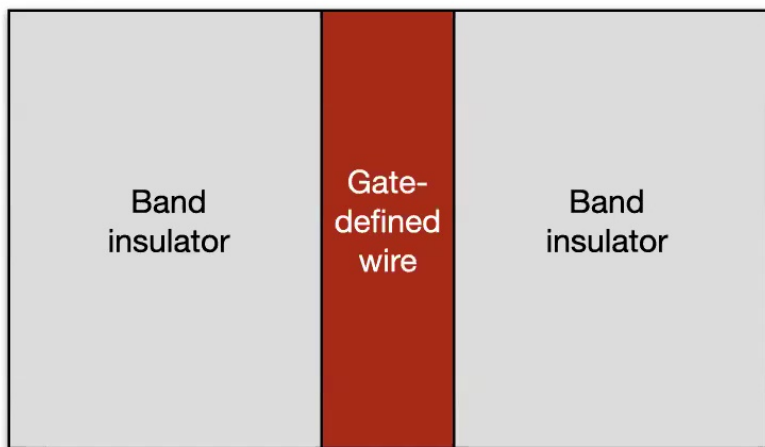
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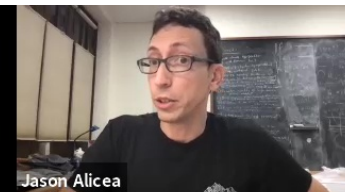
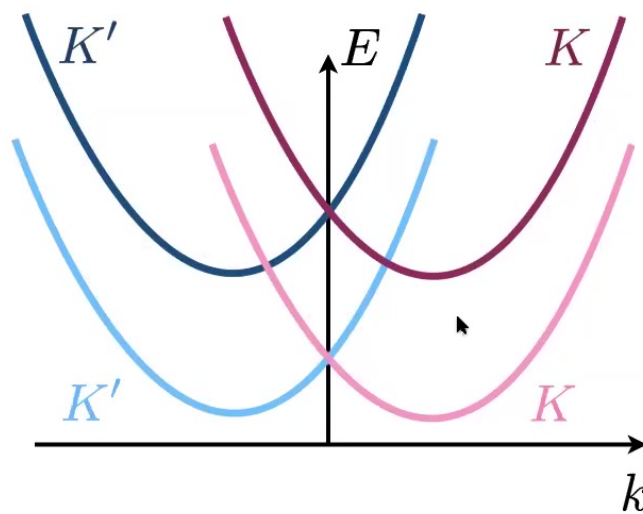
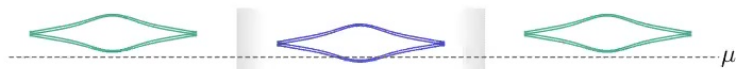
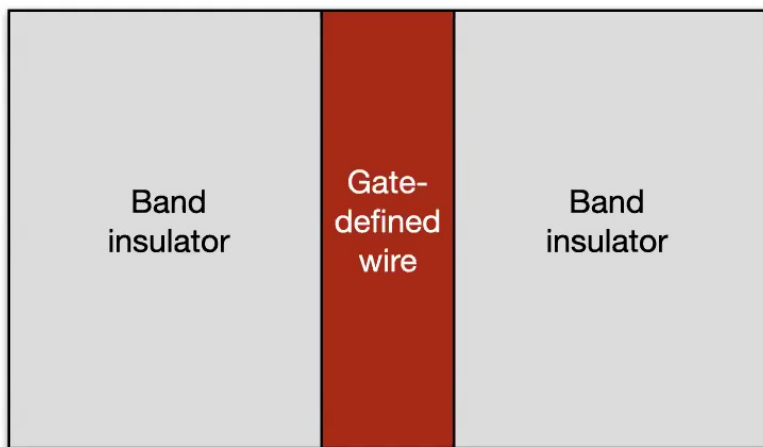
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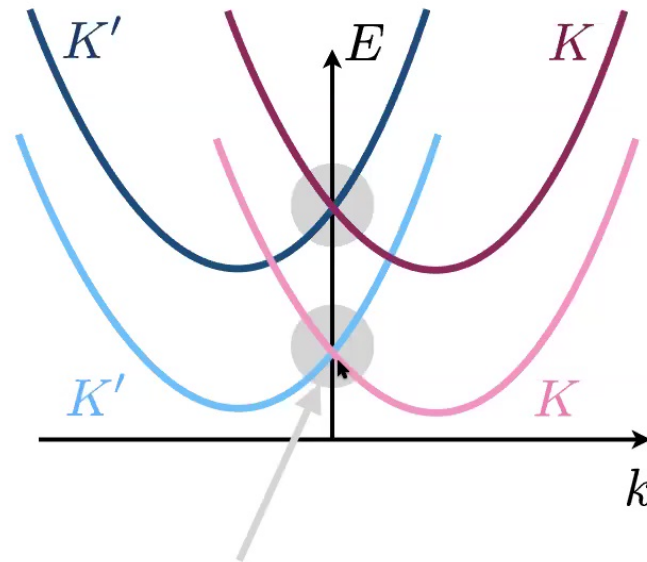
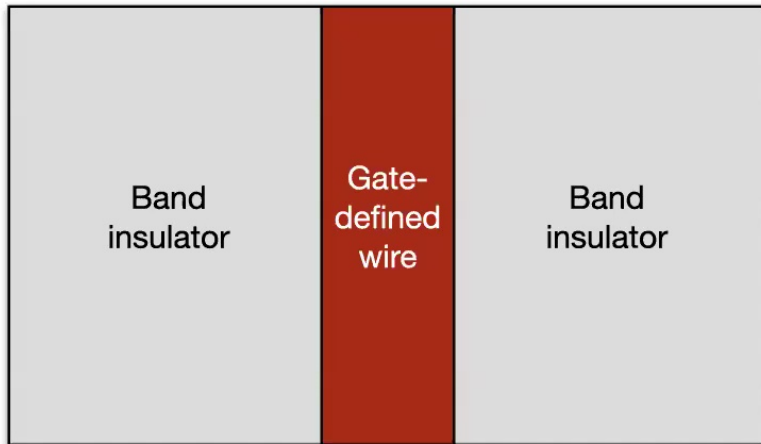
Trivial wire with spin-orbit coupling



Trivial wire with spin-orbit coupling



Trivial wire with spin-orbit coupling



Want to lift these crossings!
Requires **large momentum transfer/ultra-short-scale modulations**. Not trivial...



“Inter-valley coherent” correlated insulators

PHYSICAL REVIEW X **10**, 031034 (2020)

Ground State and Hidden Symmetry of Magic-Angle Graphene at Even Integer Filling

Nick Bultinck^{1,†}, Eslam Khalaf^{2,†}, Shang Liu², Shubhayu Chatterjee¹, Ashvin Vishwanath², and Michael P. Zaletel^{1,*}

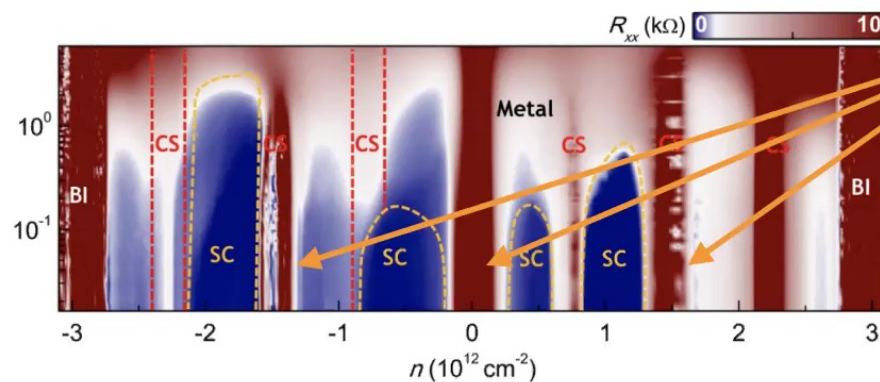
PHYSICAL REVIEW B **102**, 035136 (2020)

Correlated insulating phases of twisted bilayer graphene at commensurate filling fractions: A Hartree-Fock study

Yi Zhang¹, Kun Jiang^{2,3}, Ziqiang Wang³, and Fuchun Zhang^{1,4}

TBG IV: Exact Insulator Ground States and Phase Diagram of Twisted Bilayer Graphene

Biao Lian¹, Zhi-Da Song¹, Nicolas Regnault^{1,2}, Dmitri K. Efetov³, Ali Yazdani^{1,4}, and B. Andrei Bernevig¹



Predicted to exhibit
interaction-driven
spontaneous inter-
valley coherence!

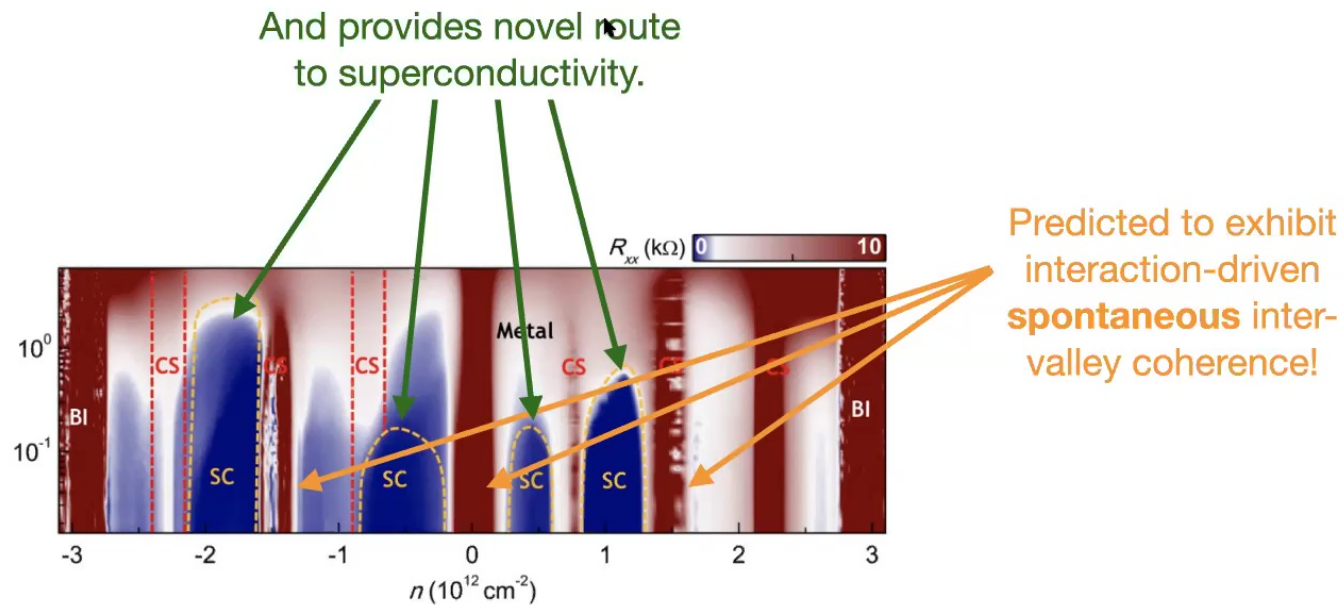
See also Kwan, Wagner, Soejima, Zaletel, Simon, Parameswaran, & Bultinck, arXiv:2105.05857; Wagner, Kwan, Bultinck, Simon, & Parameswaran, arXiv:2109.09749



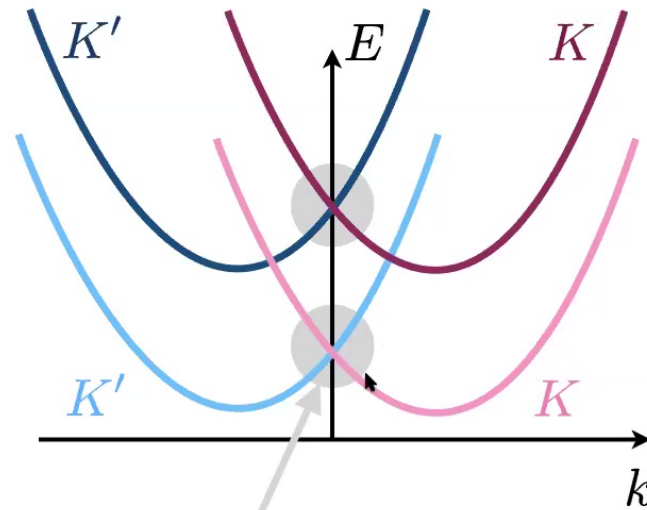
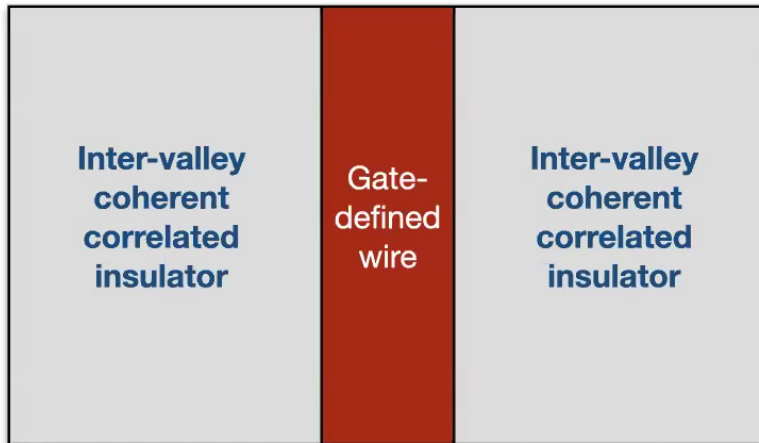
“Inter-valley coherent” correlated insulators

Charged Skyrmions and Topological Origin of Superconductivity in Magic Angle Graphene

Eslam Khalaf,¹ Shubhayu Chatterjee,² Nick Bultinck,^{2,3} Michael P. Zaletel,² and Ashvin Vishwanath^{1,*}



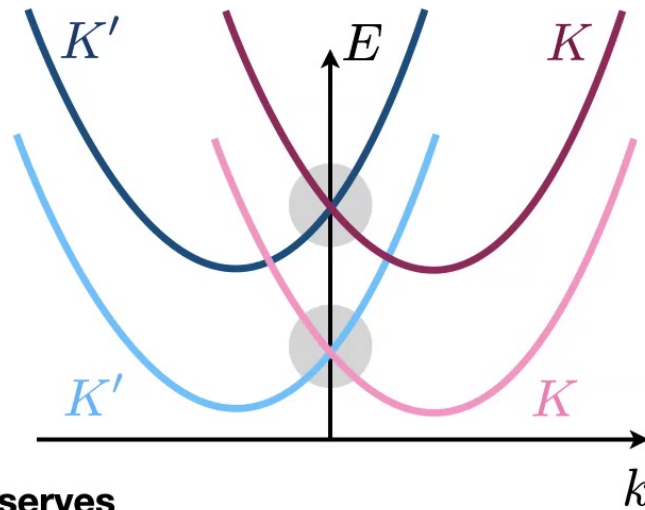
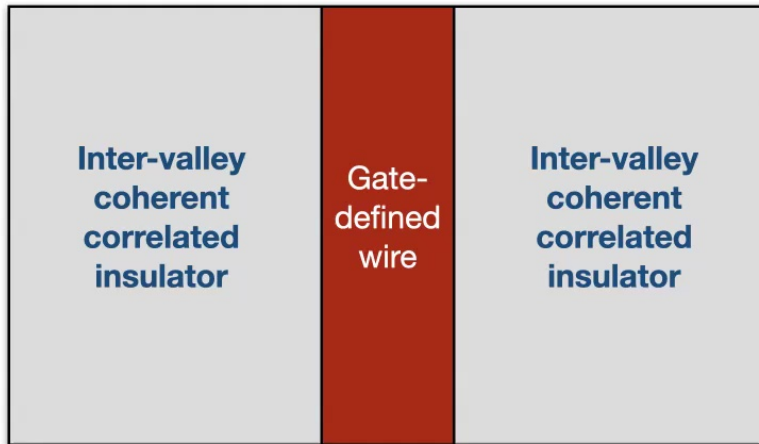
Wire with spin-orbit coupling + IVC order



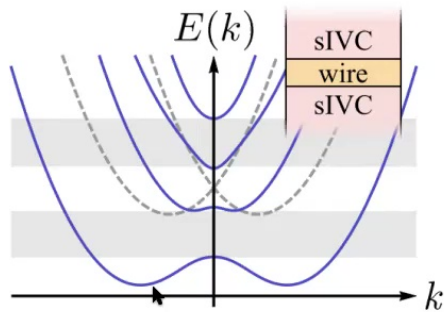
Crossings can now be lifted!



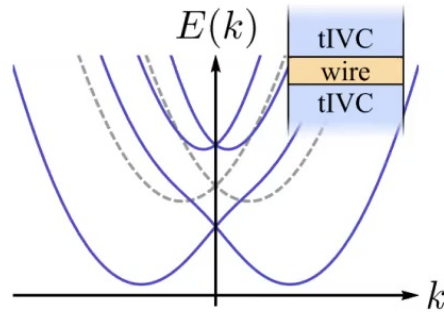
Wire with spin-orbit coupling + IVC order



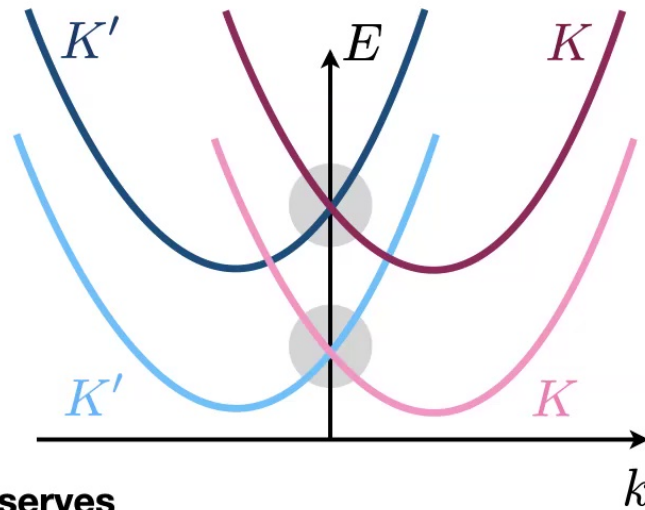
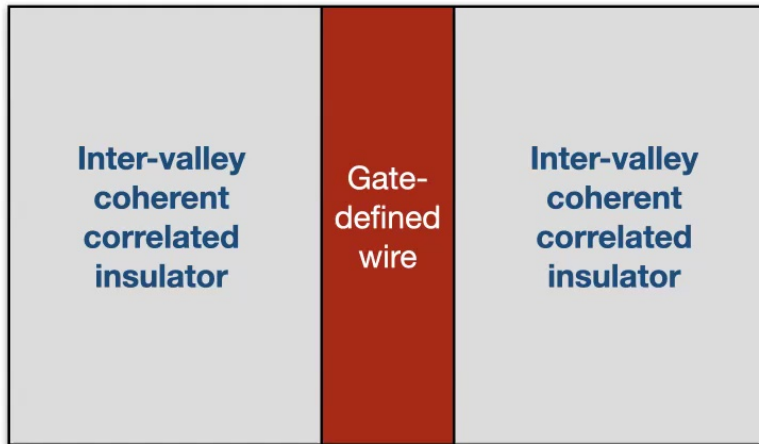
IVC order **breaks** time-reversal symmetry



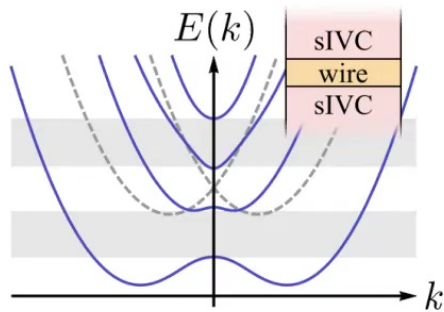
IVC order **preserves** time-reversal symmetry



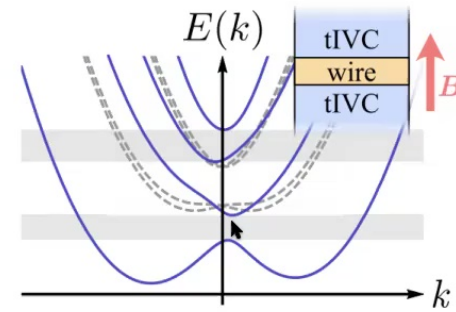
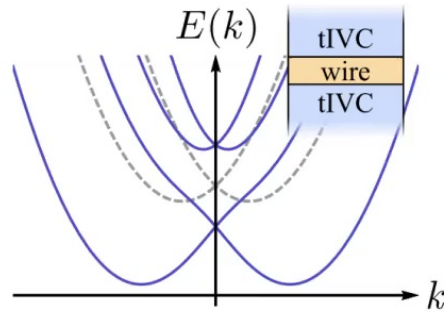
Wire with spin-orbit coupling + IVC order



IVC order **breaks** time-reversal symmetry

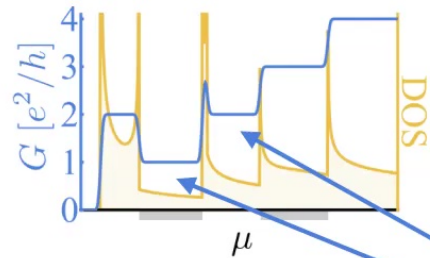
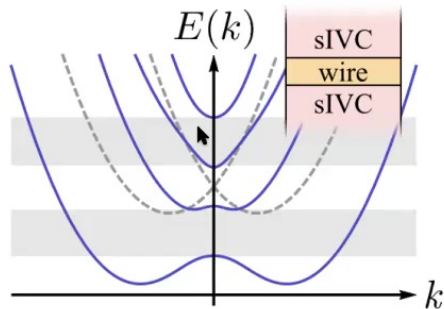


IVC order **preserves** time-reversal symmetry

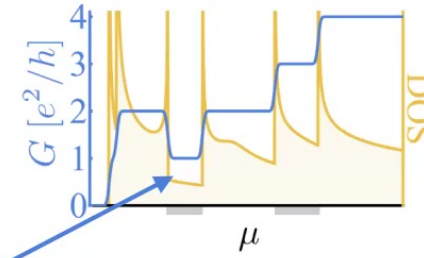
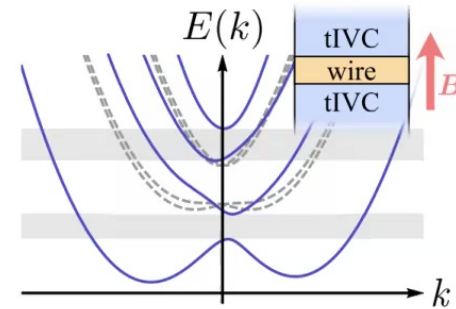
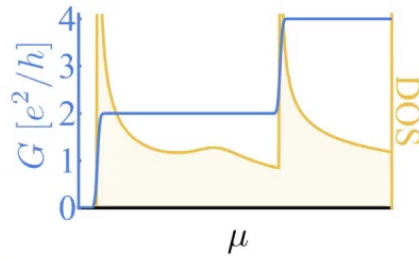
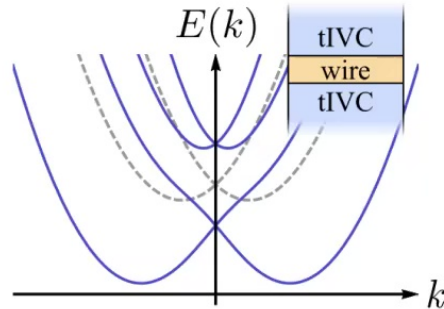


Electrical detection of IVC order

IVC order **breaks**
time-reversal symmetry



IVC order **preserves**
time-reversal symmetry



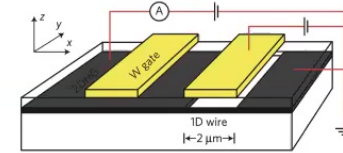
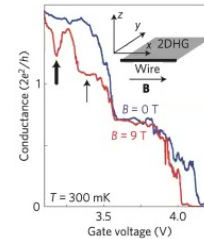
IVC-mediated conductance dips provide large-scale, electrical signature of ultra-short-scale symmetry breaking order!



Electrical detection of IVC order

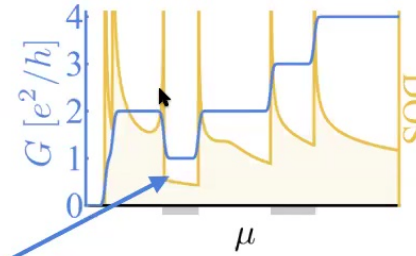
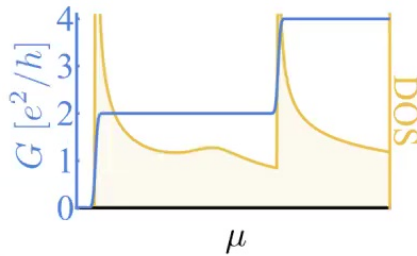
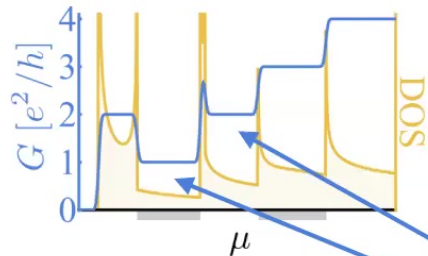
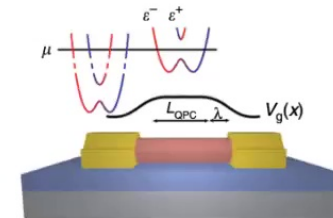
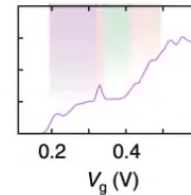
Observation of a one-dimensional spin-orbit gap in a quantum wire

C. H. L. Quay^{1,2*}, T. L. Hughes^{1†}, J. A. Sulpizio¹, L. N. Pfeiffer^{2†}, K. W. Baldwin^{2†}, K. W. West^{2†}, D. Goldhaber-Gordon¹ and R. de Picciotto^{2†}



Conductance through a helical state in an Indium antimonide nanowire

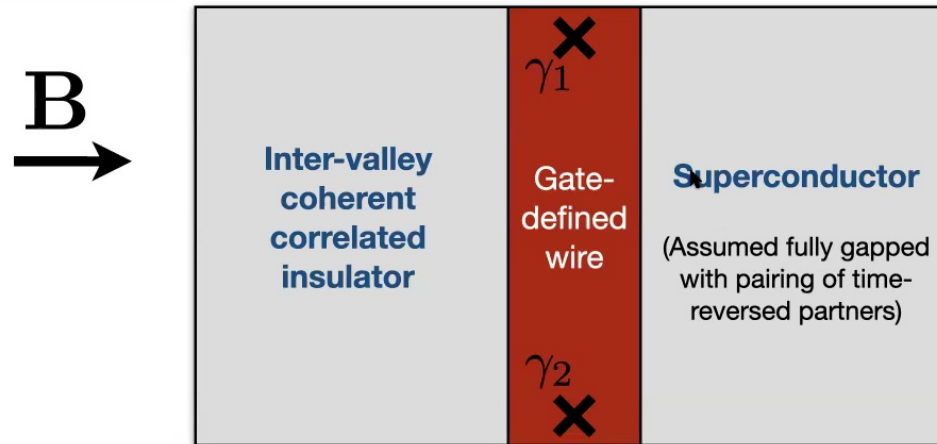
J. Kammhuber¹, M.C. Cassidy¹, F. Pei¹, M.P. Nowak^{1,2}, A. Vuik¹, Ö. Gül¹, D. Car^{1,3}, S.R. Plissard^{1,4}, E.P.A.M. Bakkers^{1,3}, M. Wimmer¹ & L.P. Kouwenhoven¹



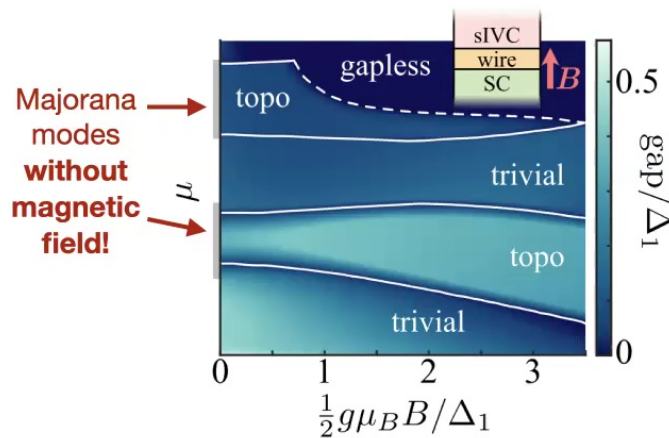
IVC-mediated conductance dips provide large-scale, electrical signature of ultra-short-scale symmetry breaking order!



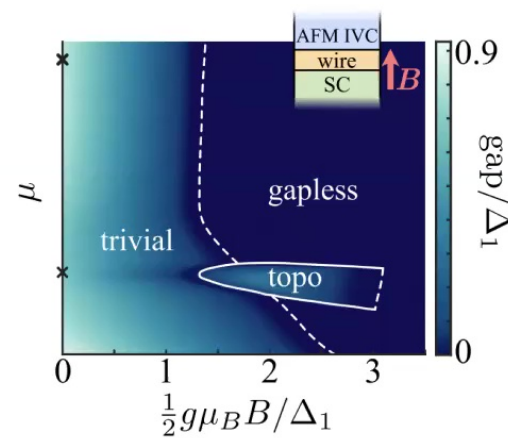
Internally engineered Majorana zero modes



IVC order **breaks** time-reversal symmetry



IVC order **preserves** time-reversal symmetry



Outlook

Electrical diagnostic of subtle symmetry-breaking order

May shed light on the Cooper-pairing mechanism

Promising platform for Majorana-based topological qubits

Virtues for Majorana engineering

Exquisite gate-tunability

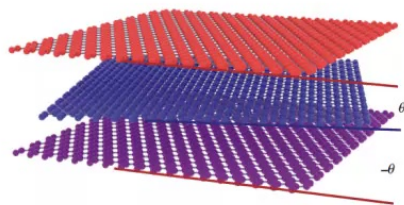
Eschews external superconducting proximity effect

Possible operation at zero magnetic field

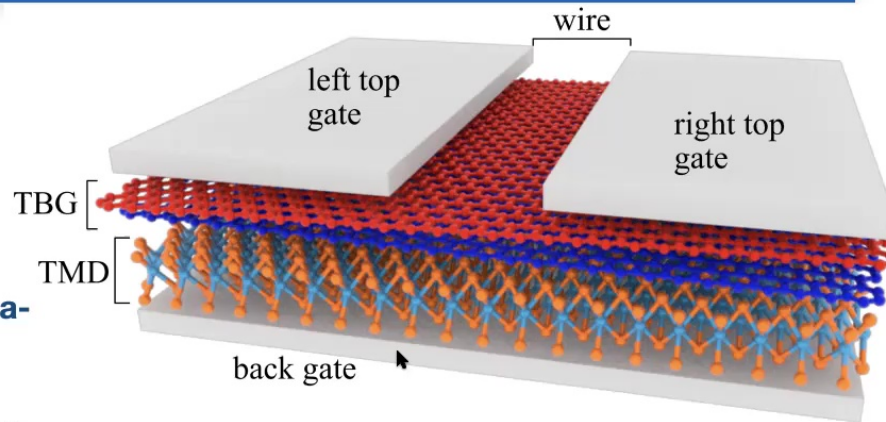
Real-time control over patterning of phases

Amenable to various transport/local probes

Adaptable to mesoscopic geometries for qubit operation



Park et al., Nature (2021); Hao et al., Science (2021)



Challenges

Low critical temperatures

Disorder

Sample-to-sample variation

Relies on IVC order (not yet confirmed)

**Extensions to twisted trilayer graphene,
other moire materials?**

